

Practical - 01.

025

* Basics of R software :-

R is a software for data analysis of statistical computing.

This software is used for effective data handling and output storage is possible.

It is capable of graphical display.

It is a free software.

$$1) 2^2 + \sqrt{25} + 35$$

$$2^2 + \text{sqrt}(25) + 35 \\ = 44$$

$$2 \times 5 \times 3 + 62 \div 5 + \sqrt{49}$$

$$2 * 5 * 3 + 62 / 5 + \sqrt{49} \\ = 49.4$$

$$3) \sqrt{76 + 4 \times 2 + 9 \div 5}$$

$$\sqrt{76 + 4 * 2 + 9 / 5} \\ = 9.262329$$

$$4) 42 + |-10| + 7^2 + 8 \times 9$$

$$42 + \text{abs}(-10) + 7^2 + 8 * 9$$

$$= 128$$

$$x = 20 ; y = 30$$

$$\text{find } x + y ; x^2 + y^2 ; \sqrt{y^3 - x^3} ; \text{abs}(x-y)$$

$$\text{i) } \begin{aligned} x + y \\ = 50 \end{aligned}$$

$$\text{ii) } x^2 + y^2$$

$$\text{iii) } \sqrt{y^3 - x^3}$$

$$\text{iv) } \text{abs}(x-y)$$

$$= 137.8405$$

calculate the following

$$1) C\left(\begin{matrix} 2, 3, 4, 5 \\ 4, 9, 16, 25 \end{matrix}\right)^2$$

$$2) C\left(\begin{matrix} 4, 5, 6, 8 \\ 12, 15, 18, 24 \end{matrix}\right)^3$$

$$3) C\left(\begin{matrix} 2, 3, 5, 7 \\ -4, -9 \end{matrix}\right) * C\left(\begin{matrix} -2, -3, -5, -4 \\ -25, -23 \end{matrix}\right)$$

$$4) C\left(\begin{matrix} 2, 3, 5, 7 \\ 16, 27, 40, 63 \end{matrix}\right) * C(8, 9)$$

$$5) C\left(\begin{matrix} 1, 2, 3, 4, 5, 6 \\ 1, 8, 81, 46 \end{matrix}\right) \wedge C(2, 3, 4)$$

$$6) C(2, 3, 5, 7) * C(1, 2, 3)$$

warning message.

$$7) C(1, 2, 3, 4, 5) \wedge C(2, 3, 4)$$

warning message.

Find the sum, product, maximum, minimum of 026
the given value.

5, 8, 6, 7, 9, 10, 15, 5

$x = c(5, 8, 6, 7, 9, 10, 15, 5)$

1) $\text{length}(x)$
 $= 8$

2) $\text{Sum}(x)$
 $= 65$

3) $\text{max}(x)$
 $= 15$

4) $\text{prod}(x)$
 $= 11340000$

5) $\text{min}(x)$
 $= 5$

matrix calculation

$x \rightarrow \text{matrix}(\text{nrow} = 4, \text{ncol} = 2, \text{data} = c(1, 2, 3, 4, 5, 6, 7, 8))$

$$\begin{bmatrix} 1 & 5 \\ 2 & 6 \\ 3 & 7 \\ 4 & 8 \end{bmatrix}$$

$$x = \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$$

$$y = \begin{bmatrix} 2 & 4 & 10 \\ -2 & 8 & -11 \\ 10 & 6 & 12 \end{bmatrix}$$

find $x+y$, $x*y$, $2x+3y$

i) $x+y$

$$\begin{bmatrix} 3 & 8 & 17 \\ 0 & 13 & -3 \\ 13 & 12 & 21 \end{bmatrix}$$

ii) $x * y$

$$\begin{bmatrix} 2 & 16 & 70 \\ -4 & 40 & -88 \\ 30 & 36 & 108 \end{bmatrix}$$

iii) $2 * x + 3 * y$

$$\begin{bmatrix} 8 & 20 & 44 \\ -2 & 34 & -17 \\ 36 & 30 & 54 \end{bmatrix}$$

2)

Perform the following.

3) $x = [2, 4, 6, 1, 3, 5, 7, 18, 16, 14, 17, 19, 3, 3, 1, 2, 15, 9, 14, 18, 12]$

length (x)

23

a = table (x)

transform (a)

6)

x	freq	Frequency as multiple of width
0	1	$\{x_0 - x_1\} = 1$
1	1	$\{x_1 - x_2\} = 1$
2	2	$\{x_2 - x_3\} = 2$
3	3	$\{x_3 - x_4\} = 3$
4	1	$\{x_4 - x_5\} = 1$
5	2	$\{x_5 - x_6\} = 2$
6	1	$\{x_6 - x_7\} = 1$
7	1	$\{x_7 - x_8\} = 1$
9	1	$\{x_8 - x_9\} = 1$
10	1	$\{x_9 - x_{10}\} = 1$
12	1	$\{x_{10} - x_{12}\} = 1$
14	2	$\{x_{12} - x_{14}\} = 2$
15	1	$\{x_{14} - x_{15}\} = 1$
16	1	$\{x_{15} - x_{16}\} = 1$
17	1	$\{x_{16} - x_{17}\} = 1$
18	2	$\{x_{17} - x_{18}\} = 2$
19	1	$\{x_{18} - x_{19}\} = 1$

breaks = seq(0, 20, 5)

b = cut(x, breaks, right = false)

c = table(b)

b
0, 5
5, 10
10, 15
15, 20

freq

8

5

4

6

$\{x_0 - x_5\}$

$\{x_5 - x_{10}\}$

$\{x_{10} - x_{15}\}$

$\{x_{15} - x_{20}\}$

Problems on pdf and cdf
Can the following be pdf

ii) ① $f(x) = \begin{cases} 2-x & , 1 \leq x \leq 2 \\ 0 & \text{o.w.} \end{cases}$

$$\begin{aligned} \int f(x) dx &= 1 \\ &= \int^2 (2-x) dx \\ &= \int^2 2dx - \int^2 x dx \\ &= 2x \Big|_1^2 - \frac{x^2}{2} \Big|_1^2 \\ &= (4-2) - (2-0.5) \\ &\neq 1 \end{aligned}$$

② $F(x) = \begin{cases} 3x^2 & , 0 < x < 1 \\ 0 & \text{o.w.} \end{cases}$

$$\begin{aligned} \int F(x) dx &= 1 \quad (\text{from } 0 \text{ to } 1) \\ &= \int_0^1 3x^2 dx \\ &= \int_0^1 \left[\frac{3x^3}{3} \right]_0^1 \\ &= \left(\frac{3(1)^3}{3} \right)^3 - \left(\frac{3(0)^3}{3} \right)^3 \\ &= 1. \end{aligned}$$

$$\textcircled{3} \quad f(x) = \begin{cases} \frac{3x}{2} (1-x/2) ; & 0 \leq x \leq 2 \\ 0 & \text{otherwise} \end{cases}$$

$$\rightarrow \int f(x) dx = 1$$

$$\int_0^2 \frac{3x}{2} \left(1 - \frac{x}{2}\right) dx$$

$$= \int_0^2 \frac{3x}{2} - \frac{3x^2}{4} dx$$

$$= \left[\frac{3x}{2} \right]_0^2 - \left[\frac{3x^2}{4} \right]_0^2$$

$$= \left[\frac{3x^2}{4} \right]_0^2 - \left[\frac{3x^3}{12} \right]_0^2$$

$$= 3 - 2$$

$$= 1$$

Hence it is p.d.f.

Q.S.Q

Q.2 Can the following p.m.f

i)	x	1	2	3	4	5
	$f(x)$	0.2	0.8	-0.1	0.5	0.1

$$f(x) = -0.1$$

Since One probability is negative

Hence it is not p.m.f.

ii)	x	0	1	2	3	4	5
	$f(x)$	0.1	0.8	0.2	0.2	0.1	0.1

Since $P(x) \geq 0 \forall x$

$$\text{and } \sum P(x) = 1$$

Hence it is a p.m.f.

iii)	x	10	20	30	40	50
	$f(x)$	0.2	0.3	0.3	0.2	0.2

$$\begin{aligned}\sum f(x) &= 0.2 + 0.3 + 0.3 + 0.2 + 0.2 \\ &= 1.2\end{aligned}$$

Since $\sum P(x) \neq 1$

It is not a p.m.f.

• 3 Find

x	0	1	2	3	4	5	6
$P(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$\begin{aligned}i) P(X \leq 2) &= P(0) + P(1) + P(2) \\ &= 0.1 + 0.1 + 0.2 \\ &= 0.4.\end{aligned}$$

ii) $P(\text{at least } 4)$

~~80 - Inital~~

$$= P(4) + P(5) + P(6)$$

$$= 0.1 + 0.2 + 0.1$$

$$= 0.4$$

iii) $P(3 < x \leq 6)$

$$= P(4) + P(5)$$

$$= 0.1 + 0.2$$

$$= 0.3$$

Q.4. Find c.d.f

X	0	1	2	3	4	5	6
$P(X)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$\rightarrow F(x) = 0$$

$$= 0.1$$

$$= 0.2$$

$$= 0.4$$

$$= 0.6$$

$$= 0.7$$

$$= 0.9$$

$$= 1.0$$

$$\rightarrow X \text{ takes } 1.0, 1.2, 1.4, 1.6, 1.8$$

$$P(X) = 0.2, 0.35, 0.15, 0.25, 0.1$$

$$F(x) = 0.2$$

$$, x < 10$$

$$= 0.55$$

$$, 10 \leq x < 12$$

$$= 0.70$$

$$, 12 \leq x < 14$$

$$= 0.90$$

$$, 14 \leq x < 16$$

$$= 1.0$$

$$, x \geq 18$$

Probability distribution & Biometrical distribution

i) Find the following PDF of the following and draw the graph

X	10	20	30	40	50
F(x)	0.15	0.25	0.3	0.2	0.1

$$\begin{aligned}
 P(x) &= 0 && \text{if } x < 10 \\
 &= 0.15 && 10 \leq x < 20 \\
 &= 0.40 && 20 \leq x < 30 \\
 &= 0.70 && 30 \leq x < 40 \\
 &= 0.90 && 40 \leq x < 50 \\
 &= 1.0 && x \geq 50
 \end{aligned}$$

Command: x

```

> x = c(10, 20, 30, 40, 50)
> prob = c(0.15, 0.25, 0.3, 0.2, 0.1)
> cumsum prob
[1] 0.15 0.40 0.70 0.90
    
```

> Plot (x, cumsum(prob), xlab = "values", ylab = "probability", main = "graph of CDF", type = "s")

MINIMUM ENTROPY

030

After the 1974 oil price shock, energy prices increased rapidly. This was followed by a period of inflation in the early 1980s. The price of oil peaked in 1980 at \$39 per barrel. The price of oil fell sharply in 1986, reaching a low of \$18 per barrel. In 1990, the price of oil rose again, reaching a peak of \$39 per barrel in 1991. The price of oil then fell sharply again in 1998, reaching a low of \$18 per barrel. The price of oil has since risen again, reaching a peak of \$39 per barrel in 2008. The price of oil has since fallen again, reaching a low of \$18 per barrel in 2015.

The price of oil has been rising steadily since the late 1970s. This is due to the increasing demand for oil, which is driven by economic growth and population increases. The price of oil has also been affected by political events, such as the Iran-Iraq War and the Gulf War. The price of oil has also been affected by environmental concerns, such as climate change and the depletion of oil reserves.

The price of oil is currently around \$39 per barrel. This is a significant increase from the low of \$18 per barrel in 2015. The price of oil is expected to continue to rise in the future, as demand continues to grow and supply remains relatively constant.

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Binomial distribution

1) Suppose there are 12 MCQ in a test. Each has 5 options and only one of them is correct. Find the probability of having i) 5 correct answers ii) Atmost 4 correct answers.

It is given that $n=12$, $p=1/5$, $q=4/5$
 $x = \text{total correct no. of correct answer}$
 $x \sim B(n, p)$

① Correct Answer

$$> n=12, p=1/5, q=4/5, x=5 \\ \text{pbinom}(5, 12, 1/5) \\ 0.05315022$$

② Almost 4 correct answer

$$> n=12, p=1/5, q=4/5, x=5 \\ \text{pbinom}(5, 12, 1/5) \\ 0.927444$$

2) There are 10 members in a committee, the probability of any member attending a meeting is 0.9, find the probability i) 7 members attended

(ii) Atleast 5 members

(iii) Almost 6 members

Q1 It is given that

$$n=10, p=0.9, q=0.1$$

~~x~~ Total number of member attended

$$x \sim B(n, p)$$

i) 7 members attended :-

$$n=10, p=0.9, q=0.1, x=7 \\ \text{dbinom}(7, 10, 0.9) \\ =[1] 0.0573$$

ii)

iii)

ii) At least 5 members attended

$$n = 10, p = 0.9, q = 0.1, x = 5$$

[1] $\text{pbinom}(5, 10, 0.9)$
0.9933

iii) At most 6 members attended

$$n = 10, p = 0.9, q = 0.1, x = 5$$

[1] $\text{pbinom}(6, 10, 0.9)$
0.01279

Find the cdf and draw the graph

	x	1	2	3	4	5	6
	$F(x)$	0.1	0.1	0.2	0.2	0.1	0.1

Command

> $x = c(0, 1, 2, 3, 4, 5, 6)$
> ~~prob~~ prob = c(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)
> cumsum(prob)

[1] 0.1 0.2 0.4 0.6 0.7 0.9 1.0

$$P(x) = 0 \quad \text{if } x \leq 0$$

$$0.1 \quad 0 \leq x \leq 1$$

$$0.2 \quad 1 \leq x \leq 2$$

$$0.4 \quad 2 \leq x \leq 3$$

$$0.6 \quad 3 \leq x \leq 4$$

$$0.7 \quad 4 \leq x \leq 5$$

$$0.9 \quad 5 \leq x \leq 6$$

$$1.0 \quad 6 \leq x \leq 7$$

$$1.0$$

Practical -04.

Binomial distribution

- i) find $n = 5$ & $P = 0.1$ complete Binomial distribution of exactly 10 success
- ii) find the probability with $P = 0.1$
- iii) x follows binomial distribution with $n=12$ & $P(x > 7)$
- And i) $P(x=5)$ ii) $P(x \leq 5)$ iii) $P(5 < x < 7)$
- iv) $P(x \geq 7)$
- 4) Probability of sales man makes sale is 0.15
Find the probability i) No sale from 10 customers
ii) More than 3 sale in 20 customers.
- 5) A student wrote 5 mcq. Each question has 4 option, out of which 1 is correct.
Calculate the probability for atleast 3 correct answers.
- 6) \bar{x} follows Binomial Distribution $n=10, p=0.4$
Plot the graph pmf and cdf.

Solution :-

1) $n = 5, p = 0.1, x = 0.5$
 Command $\text{dbinom}(0.5, 5, 0.1)$
 [1] 0.59409 0.32805 0.07290 0.00310 0.0045 0.00001

2) $n = 100, p = 0.1, x = 10$

Command $\text{dbinom}(10, 100, 0.1)$
 [1] 0.1318653

3) i) $n = 12, p = 0.25, x = 5$

Command $\text{dbinom}(5, 12, 0.25)$

[1] 0.1032414

ii) $n = 12, p = 0.25, x = 5$

Command $\text{dbinom}(5, 12, 0.25)$

[1] 0.9455978

iii) $n = 12, p = 0.25, x = 7$

[1] 0.00278151

4) i) $n = 10, p = 0.15, x = 0$

$\text{dbinom}(0, 10, 0.15)$

[1] 0.1968744

ii) $n = 30, p = 0.15$

$$P(X > 3) = 1 - P(X \leq 3) = 1 - \text{pbisom}(3, 20, 0.15)$$

[1] 0.3522748

5) $n = 6$, $p = 1/4$, all $x \leq 2$

command $1 - pbinom(2, 5; 1/4)$

[1] 0.1035156

6) $n = 10$; $p = 0.4$
 $x = 0:n$

prob = dbinom(x, n, p, log, log)

cumprob = pbinom(x, n, p)

d = data.frame("x" = values, "prob" = prob)

print(d)

X-values

0
1
2
3
4
5
6
7
8
9
10

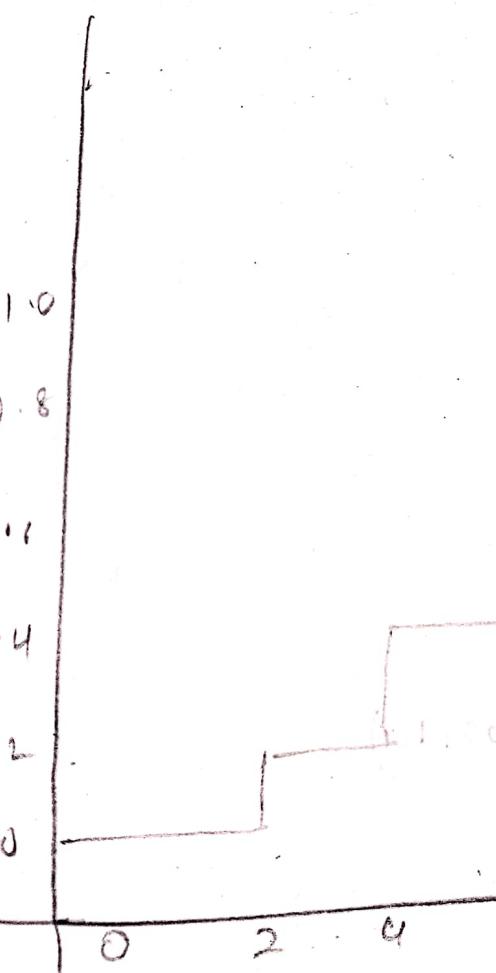
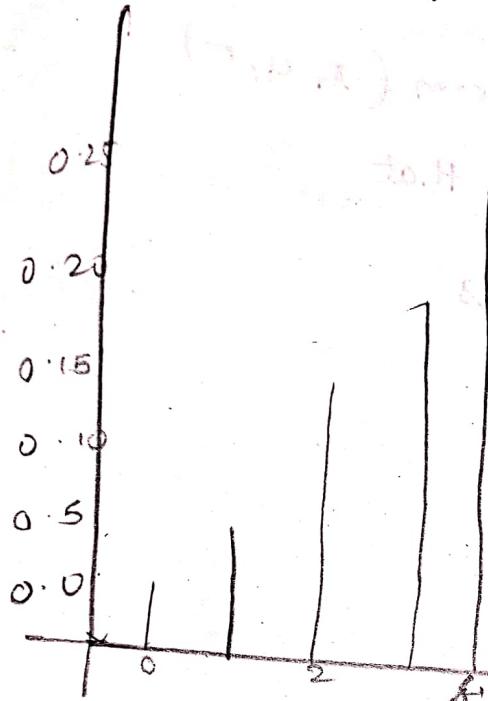
Probability

0	0.0060466176
1	0.0403107340
2	0.1209323520
3	0.2149903480
4	0.2503226560
5	0.2006581243
6	0.11147673280
7	0.0424673280
8	0.0106168320
9	0.0013728640
10	0.0001048574

Plot

(x, plob, "h")

Plot (x, cumplob, "s")



Practical - 05.

- i) $P[x = r] = \text{dnorm}(x, \mu, \sigma)$
ii) $P[x \leq x] = \text{pnorm}(x, \mu, \sigma)$
iii) $P[x > r] = 1 - \text{pnorm}(r, \mu, \sigma)$
iv) $P[x, cr, cr] = \text{pnorm}(x_2, \mu, \sigma) - \text{pnorm}(x_1, \mu, \sigma)$

⑤ To find the value of K so that

⑥ To generate n random numbers

i) $x \sim N(\mu = 50, \sigma^2 = 100)$
ii) $P(x \leq 40)$
iii) $P(x > 55)$
iv) $P(x \leq k) = 0.7 \Rightarrow k = ?$

Soln :-

$$\begin{aligned} ① &> a = \text{pnorm}(40, 50, 10) \\ &> \text{cat}({}^4 P(x \leq 40) = {}^4, a) \\ &P(x \leq 40) = 0.1586553. \end{aligned}$$

$$\begin{aligned} ② &> b = 1 - \text{pnorm}(55, 50, 10) \\ &> \text{cat}({}^4 P(x > 55) = {}^4, b) \\ &P(x > 55) = 0.3085375. \end{aligned}$$

$$\begin{aligned} ③ &> c = \text{pnorm}(60, 50, 10) \\ &> \text{cat}({}^4 P(42 \leq x \leq 60) = {}^4, c) - \text{pnorm}(42, 50, 10) \\ &P(42 \leq x \leq 60) = 0.6294893. \end{aligned}$$

$$\text{Q. } \begin{aligned} &> d = \text{pnorm}(0.7, 50, 10) \\ &> \text{cat}\left(^4P(x \leq k) = 0.7, k = 11, d\right) \\ &\quad P(x \leq k) = 0.7, k = 55.24401 \end{aligned}$$

$$2] x \sim N(\mu = 100, \sigma^2 = 36)$$

Soln :-

$$\text{i) } \mu = 100, \sigma^2 = 36, \sigma = 6.$$

$$\begin{aligned} &> a = \text{pnorm}(110, 100, 6) \\ &> \text{cat}\left(^4P(x \leq 110) = 4, a\right) \\ &\quad P(x \leq 110) = 0.9522096. \end{aligned}$$

$$\text{ii) } > b = \text{pnorm}(95, 100, 6)$$

$$\begin{aligned} &> \text{cat}\left(^4P(x \leq 95) = 4, b\right) \\ &\quad = 0.2023284. \end{aligned}$$

$$\text{iii) } > c = 1 - \text{pnorm}(115, 100, 6)$$

$$\begin{aligned} &> \text{cat}\left(^4P(x \leq 115) = 4, c\right) \\ &\quad = 0.006209665. \end{aligned}$$

$$\text{iv) } > d = \text{pnorm}(105, 100, 6) - \text{pnorm}(95, 100, 6)$$

$$\begin{aligned} &> \text{cat}\left(^4P(95 \leq x \leq 105) = 4, d\right) \\ &\quad = 0.953432. \end{aligned}$$

780

- 3) Generate 10 random numbers from normal distribution with mean = 60 & s.d = 5. also [sample] mean, median & standard deviation.

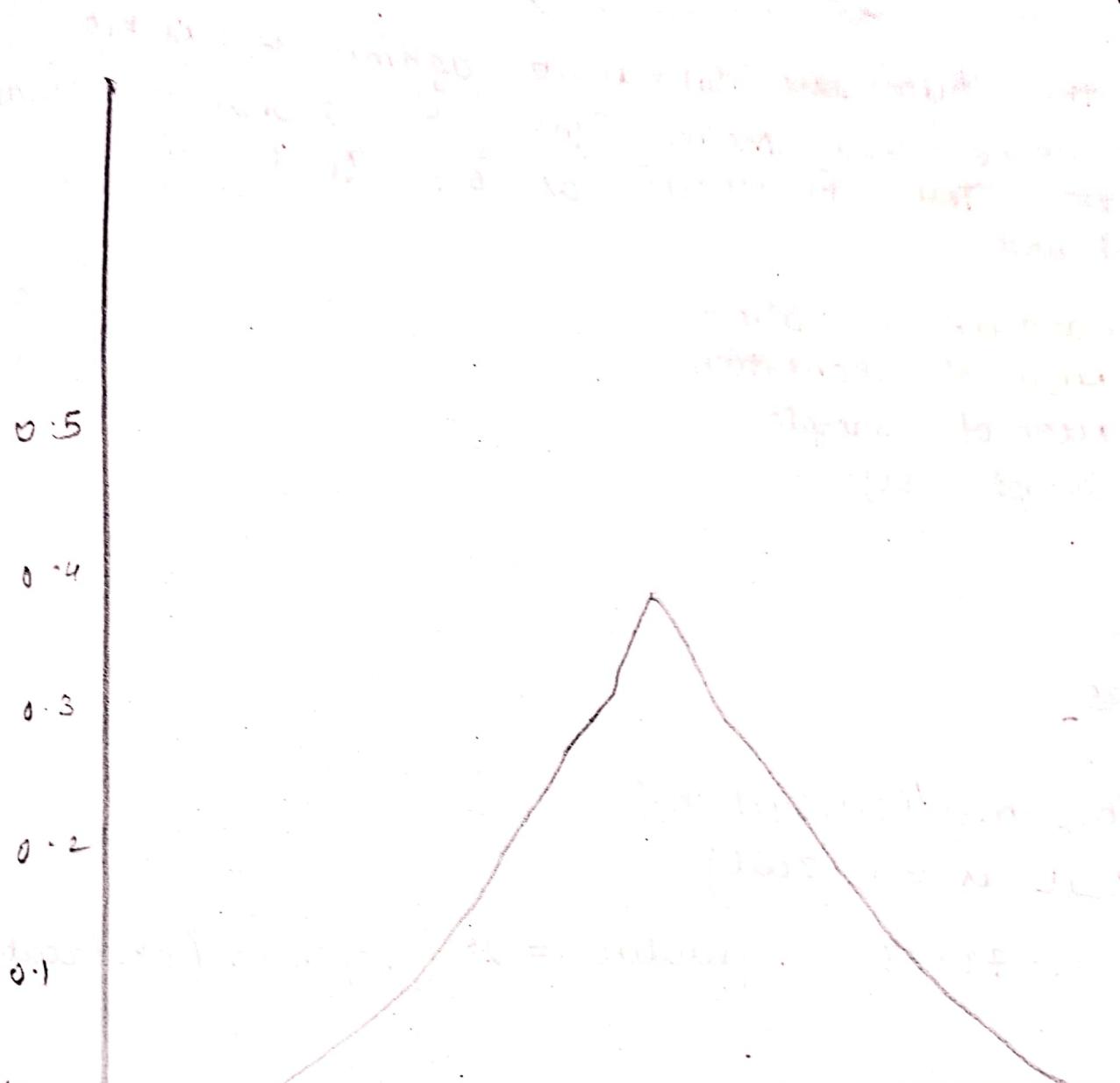
Solution :-

```
> x norm (10, 60, 5)
> a.m = mean(x)
> a.m
[1] 60.01123
> m.e = median(x)
> m.e
[1] 59.86623
> n = 10
> variance = (n-1) * var(x) / n
> variance
[1] 44.45974
> s.d = sqrt(variance)
> sd
[1] 6.667814.
```

- 4) Draw the graph of standard normal distribution

```
> z = seq(-3, 3, by = 0.1)
> y = dnorm(z)
> plot (x, y, xlab = "x values", ylab = "probability",
       main = "standard normal graph")
```

036



Practical - 06
 z-distribution
 n n n n n

280

- i) Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$
 Sample size = 400, mean = 10.2 & standard deviation = 2.25. Test hypothesis at 5% level of significance

→
 s.d = standard deviation
 m_0 = mean of population
 m_x = mean of sample
 n = sample size

$$> m_0 = 10$$

$$> m_x = 10.2$$

$$> s.d = 2.25$$

$$> n = 400$$

$$> z_{cal} = (m_x - m_0) / (s.d / \sqrt{n})$$

$$> cat("z_{cal} is ", z_{cal})$$

$$z_{cal} \text{ is } = 1.777778 \quad > pvalue = 2 * (1 - pnorm(abs(z_{cal})))$$

> pvalue

[1] 0.07544036

Since the 0.07544036 is greater than 0 then we will accept the value.

2) Test the hypothesis (H_0) : $\mu = 75$ against (H_1) : $\mu \neq 75$
 at 5%. Level of significance
 $> m_0 = 75$
 $> mx = 80$
 $> s.d = 3$
 $> n = 100$
 $> z_{cal} = \frac{(mx - m_0)}{(s.d / \sqrt{n})}$
 $> z_{cal} = \frac{80 - 75}{3 / \sqrt{100}} = 5$
 $> p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$
 $(\text{if } 0)$

value accepted

→
 20 24 27 30 46 35 26 46 27 10 20 21 30 37 20
 22 30 37 35 21 22 23 24 25 26 27 19 28 29 30 29 27
 19 28 29 30 29 27 15 22 20 18

$x = c(20, 24, 27, 30, 46, 35, 26, 46, 27, 10, 20, 21, 30, 37, 35, 21, 23, 24, 25, 26, 27, 19, 28, 29, 30, 29, 27, 15, 22, 20, 18)$

$> mx = \text{mean}(x)$

$> mx$

$(\text{if } 26.06667)$

$> n = \text{length}(x)$

$> n$

30

580

5)

$$> \text{variance} = (n-1) * \text{var}(x) / n$$

> variance

[1] 52.995666

$$> \text{sd} = \text{sqrt}(\text{variance})$$

> sd

[1] 7.279805

$$> m_0 = 25$$

$$> z_{\text{cal}} = (m_x - m_0) / (\text{sd} / \sqrt{n})$$

$$> \text{cat}(\text{z}_{\text{cal}} \text{ is } \text{z}_{\text{cal}})$$

$$\text{z}_{\text{cal}} \text{ is } = 0.80254547$$

> pvalue

[1] 0.4222375

value accepted

4)

$$> p = 0.2$$

$$> q = 1-p$$

$$> p = 50/100$$

$$> n = 400$$

$$> z_{\text{cal}} = (p - P) / (\sqrt{P * q / n})$$

$$> \text{cat}(\text{z}_{\text{cal}} \text{ is } \text{z}_{\text{cal}})$$

$$\text{z}_{\text{cal}} \text{ is } -3.75$$

$$> \text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(\text{z}_{\text{cal}})))$$

> pvalue

[1] 0.0001768346.

$$> p$$

[1] 0.129

value rejected

038

5)
 $n = 200$

$p = 0.5$

$p = 0.56$

$n = 200$

$z_{\text{cal}} = (p - p) / (\sqrt{p * q / n})$

cat (⁴ zcal is : ⁴ zcal)

zcal is 4.697056

$p_{\text{value}} = 2 \times \text{pnorm}(\text{abs}(z_{\text{cal}}))$

pvalue

[i] 0.08968602

P

[i] 0.5

H₀ accepted

Practical-07

889

Large sample
test
Two hospital is
noise level in two hospital are same.

y A study of noise level in two hospital is calculated below. Test the hypothesis that the noise level in two hospital are same.

Hos A
84
61
 \bar{x}

Hos B
34
5
8

H_0 the noise levels are same.

> $n_1 = 84$

> $n_2 = 34$

> $m_x = 61$

> $m_y = 59$

> $sdx = 7$

> $sdy = 8$

> $z = (m_x - m_y) / \sqrt{((sdx^2/n_1) + (sdy^2/n_2))}$

> z.

[1] 1.273682.

> cat ("x calculated is = ", z)

x calculated is = 1.273682

> pvalue = 2 * (1 - pnorm (abs(z)))

> pvalue

[1] 0.202761

since pvalue > 0.05 we accept H_0 value at 5% level of significance

2)

```

> n1 = 1000
> n2 = 2000
> mx = 67.5
> my = 68
> sdx = 2.5
> stdy = 2.5
> z = (mx - my) / sqrt((sdx^2/n1) + (stdy^2/n2))
> z
[1] -5.163978
> cat("Calculated z = ", z)
[1] "Calculated z = -5.163978"
> pvalue = 2 * (1 - pnorm(abs(z)))
> pvalue
[1] 2.417564e-07

```

" Pvalue > 0.5 , we accept H_0 at 5% level of significance "

3)

H_0 = The proportion of the population are equal

```

> n1 = 400
> n2 = 500
> p1 = 0.2
> p2 = 0.155
> p = (n1 * p1 + n2 * p2) / (n1 + n2)
> p
[1] 0.175
> z = (p1 - p2) / sqrt(p * q * (1/n1 + 1/n2))
> z
[1] 1.76547

```

B60

- > cat ("z calculated is *y, z")
- = z calculated is 1.7654
- > pvalue = $2^* (1 - \text{pnorm}(\text{abs}(z)))$
- > pvalue

[1] 0.07748487

*: H₀ value > 0 we accept H₀ at 5% level of significance

4]. from each of the box of the apples a sample size of 200 is collected. It is found that there are 44 bad apples in first and 30 (in second). Test the hypothesis

→ H₀ The two box are equivalent.

> n₁ = 200

> n₂ = 200

> p₁ = 44/200

> p₂ = 30/200

> P = $(n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

> P

[1] 0.185

> q = 1 - p.

> q

[1] 0.815

> z

[1] 1.802741

> pvalue = $2^* (1 - \text{pnorm}(\text{abs}(z)))$

> pvalue

[1] 0.07142888

H₀ value is accepted.

5]

 H_0 : Heights

$$\begin{aligned} \rightarrow n_1 &= 60 \\ \rightarrow n_2 &= 50 \end{aligned}$$

$$\rightarrow \bar{x}_M = 63.5$$

$$\rightarrow \bar{x}_m = 69.5$$

$$\rightarrow s_{dX} = 2.5$$

$$\rightarrow s_{dY} = 2.5$$

$$\rightarrow z = (\bar{x}_M - \bar{x}_m) / \sqrt{s_{dX}^2/n_1 + s_{dY}^2/n_2}$$

[1] -12.53359.

$$\rightarrow p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

[1] pvalue

[1] 0

Since $p\text{value} < 0.05$, we reject H_0 at 0.05% level of significance.

Practical - 08

Q8

Small sample test

- 1) The ten are selected & height are found to be 63, 63, 68, 69, 71, 71, 72 cms Test the hypothesis that mean height is 66 cm or not at 1.
- H_0 mean = 66 cms

$$> \text{mean} = 66$$

$$> x = c(63, 63, 68, 69, 71, 71, 72)$$

> t-test(x)

one sample t-test

data : x

$$t = 47.94, df = 6, pvalue = 5.22e-09$$

alternative hypothesis ($: \text{true mean} \neq 66$) is not equal to
95 percent confidence interval :

$$64.66479 \quad 71.62092$$

Sample estimates :

mean of x

$$68.14286$$

\therefore pvalue < 0.01 is rejected in 1-t. level of significance

- 2) Two random sample was drawn from two different population -

$$\text{Sample 1} = 8, 10, 12, 11, 16, 15, 18, 7$$

$$\text{Sample 2} = 20, 15, 18, 9, 8, 10, 11, 12$$

Test the hypothesis that there is no difference between population

$> x = c(8, 10, 12, 11, 16, 15, 18, 7)$
 $> y = c(20, 15, 18, 9, 8, 10, 11, 17)$
 $> t\text{-test}(x, y)$

Two sample t-test
data : x & y

$t = -0.36247$, $df = 13.887$, $p\text{-value} = 0.7225$

alternative hypothesis: difference is not equal.

Sample estimates = 12.125

12.875

H_0 value is accepted.

3] following the weights of 10 people

Before (100, 125, 95, 96, 98, 102, 115, 104, 109, 110)

After (95, 80, 95, 98, 90, 100, 110, 85, 100, 101)

H_0 The diet program is not effective.

$> x = c(100, 125, 95, 96, 98, 102, 115, 104, 109, 110)$
 $> y = c(95, 80, 95, 98, 90, 100, 110, 85, 100, 101)$
 $> t\text{-test}(x, y, \text{paired} = \text{TRUE}, \text{alternative} = \text{"less"})$

data: x and y.

$t = 2.3215$, $df = 9$, $p\text{-value} = 0.9773$.

alternative hypothesis: true

95 percent confidence interval

mean of the differences : 10

→ 4) Marks before & after a training program

$$\text{Before} = (20, 26, 32, 28, 27, 36, 35, 25)$$

$$\text{After} = (30, 35, 32, 37, 37, 40, 40, 23)$$

H₀: The training program is not effective.

$$> r = c(20, 25, 32, 28, 27, 36, 35, 25)$$

$$> y = c(30, 35, 32, 37, 37, 40, 40, 23)$$

> t-test (x, y, paired = T, alternative = "greater")

Paired t-test

data: x and y

t = -3.3859, df = 7, p-value = 0.9942

alternative hypothesis: true

interval:

$$(-8.96733, 9.31911)$$

Sample estimates:

mean of difference

→ 5) H₀: variance of population is not equal

$$> x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$$

$$> y = c(64, 66, 74, 78, 82, 85, 87, 92, 93, 95, 96)$$

F test

data: x and y to compare two variances.

$$F = 0.70686$$

$$1 / \text{num} \quad df = 8 \quad \text{denom df} = 10, \text{Pval}$$

$$0.6359$$

9.5 percent confidence interval:
 0.1833632 3.0360393
 ratio of variances 0.7068507

042

6]. The A.P of s.d \bar{u} of population mean significance. sample 100 test 55 or not at 5% level of observation is 52 out of the hypothesis that the

$$H_0 \text{ population mean} = 55$$

$$> m = 100$$

$$> mx = 52$$

$$> mo = 55$$

$$> sd = 7$$

$$> zcal = (mx - mo) / (sd / \sqrt{n})$$

$$> pvalue = 2 * (1 - pnorm (abs(zcal)))$$

> pvalue

$$[1] 1.82153e-05$$

chi square distribution

SPPU

Q) Use the following data to test whether the cleanliness of home depends upon child's condition or not.

		Condition of Home		
Condition of Child	clean	70	50	45
	fairly clean	80	60	20
	dirty	35		

SOM :- H_0 : Condition of home & the child independent.

> $x = c(70, 80, 35, 50, 20, 45)$

> $m = 3$

> $n = 2$

> $y = \text{matrix}(x, \text{ncol} = m, \text{nrow} = n)$

$[1,]$

$[1,]$

70

$[2,]$

$[2,]$

80

$[3,]$

$[3,]$

35

$[1,2]$

50

80

45

> pvalue = chisq.test(y)

data : y.

χ^2 -squared = 25.646, df = 2, pvalue = 2.698e-06

H_0 value is rejected.

27. Table below shows the relation between the performance between mathematics and computer of CS students.

		Maths		
		MGr	MGr	LGr
Computer	HGr	56	71	12
	MGr	47	163	38
	LGr	14	42	85

→ H_0 performance between maths & computer is indep

$$\lambda = c(56, 47, 14, 71, 163, 38, 14, 42, 85)$$

$$m = 3$$

$$n = 3$$

$$Y = \text{matrix}(x, \text{newrow} = 3, \text{ncol} = 3)$$

$$y.$$

$$\begin{bmatrix} 17 \\ 127 \\ 13 \end{bmatrix}$$

EAD

j 8

x = read.csv("C:/users/admin/Desktop/m
x

	Stats	Calc
1	40	60
2	45	48
3	42	97
4	15	20
5	34	25
6	36	27
7	49	57
8	59	58
9	20	25
10	21	27

Practical -10

Topic :-

Q. following are the amounts of sulphur oxide emitted by a factory

17, 15, 20, 29, 19, 18, 22, 25, 27, 9,

24, 20, 17, 6, 24, 14, 15, 23, 24, 26

Apply sign test, to test the hypothesis that the population median is 21.5

H_0 : population median is 21.5

H_1 : It is less than 21.5

$$x = \{17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, \\ 20, 17, 6, 24, 14, 15, 23, 24, 26\}$$

$$m = 21.5$$

$$sp = \text{length} \{x | x > m\}$$

$$sn = \text{length} \{x | x < m\}$$

$$h = sp + sn$$

$$n$$

[1] 20

$$pv = \text{pbineom}(sp, n, 0.5)$$

p.v

[1] 0.4119015

since, p-value > 0.05, we accept the H_0

5% level of significance

[Note : If the alternative is greater than median $PV = \text{Pbinom}(sn, n, 0.5)$]

- of fair the observations 12, 19, 31, 28, 43, 49, 70, 63. Apply sign test to test median is 25 against the alternative than 25.

H_0 : median is 25.

H_1 : It is more than 25.

$$x = C(12, 19, 31, 28, 43, 40, 55, 49, 70, 63)$$

$$m = 25$$

$$sp = \text{length}(\{x | x > m\})$$

$$sn = \text{length}(\{x | x < m\})$$

$$n = sp + sn$$

$$n$$

[1] 10

$$PV = \text{Pbinom}(sn, n, 0.5)$$

$$PV$$

[1] 0.0546875

Since, P-value > 0.05 , we accept the H_0 level of significance.

- 8] for the following data 60, 65, 63, 84, 61, 71, 51, 48, 66. Test the hypothesis using Wilcoxon's signed rank test. For testing the hypothesis median is 60 against the alternative it is greater than 60.

H_0 : Median is 60.

H_1 : It is greater than 60.

$$x = (60, 65, 63, 89, 61, 71, 58, 51, 48, 66)$$

median

$$\mu = 60$$

wilcox. test (x , alter = "greater", $\mu = 60$)

wikoxon signed rank test with continuity correction.

data: x

$$V = 29, p\text{-value} = 0.2386$$

alternative hypothesis: true location is greater than 60.

Since, $p\text{-value} > 0.05$, we accept the H_0 at 5% level of significance.