

**CSC 225 FALL 2015**  
**ALGORITHMS AND DATA STRUCTURES I**  
**ASSIGNMENT 3**  
**UNIVERSITY OF VICTORIA**

1. Design a  $O(n \log n)$ -time algorithm to compute the number of inversions in a given array.
2. Suppose that your Quick-Sort algorithm uses the following pivot rule that picks the element in the “middle” - For an array  $A[0, 1, \dots, n-1]$  of size  $n$ , it uses the element in  $A[n/2]$  as pivot if  $n$  is even and the element in  $A[(n-1)/2]$  as pivot if  $n$  is odd. Give an input array of size 7, with values 1 to 7, on which your quick-sort algorithm that run the slowest.
3. Prove that it is impossible to develop a comparison-based implementation of the Priority Queue ADT such that both Insert and RemoveMin run in  $O(\log \log n)$  time.
4. Suppose that we are given a sequence  $S$  of  $n$  elements, each of which is an integer in the range  $[0, n^2 - 1]$ . Describe a simple method for sorting  $S$  in  $O(n)$  time. (Hint: Think of alternate ways of viewing the elements so that you can use Radix-Sort.)