

Data Science II Homewrk 5

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```
knitr::opts_chunk$set(warning = FALSE, message = FALSE,
  fig.align = "center", cache = TRUE,
  fig.width = 6, fig.asp = 0.6, out.width = "90%")
theme_set(theme_minimal() + theme(legend.position = "bottom"))
```

Data import and partition

```
auto = read_csv("auto.csv") %>%
  janitor::clean_names() %>%
  na.omit() %>%
  distinct() %>%
  mutate(
    cylinders = as.factor(cylinders),
    origin = case_when(origin == "1" ~ "American",
                      origin == "2" ~ "European",
                      origin == "3" ~ "Japanese"),
    origin = as.factor(origin),
    mpg_cat = as.factor(mpg_cat),
    mpg_cat = fct_relevel(mpg_cat, "low", "high")
  ) %>%
  as.data.frame()

skimr::skim_without_charts(auto)
```

Table 1: Data summary

Name	auto
Number of rows	392
Number of columns	8
Column type frequency:	
factor	3
numeric	5
Group variables	None

Variable type: factor

skim_variable	n_missing	complete_rate	ordered	n_unique	top_counts
cylinders	0	1	FALSE	5	4: 199, 8: 103, 6: 83, 3: 4
origin	0	1	FALSE	3	Ame: 245, Jap: 79, Eur: 68
mpg_cat	0	1	FALSE	2	low: 196, hig: 196

Variable type: numeric

skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100
displacement	0	1	194.41	104.64	68	105.00	151.0	275.75	455.0

skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100
horsepower	0	1	104.47	38.49	46	75.00	93.5	126.00	230.0
weight	0	1	2977.58	849.40	1613	2225.25	2803.5	3614.75	5140.0
acceleration	0	1	15.54	2.76	8	13.78	15.5	17.02	24.8
year	0	1	75.98	3.68	70	73.00	76.0	79.00	82.0

```
# split the dataset into two parts: training data (70%) and test data (30%)
```

```
set.seed(0504)
```

```
indexTrain = createDataPartition(y = auto$mpg_cat,
                                  p = 0.7,
                                  list = FALSE)
```

Support Vector Machines

Linear Kernel

Fit a support vector classifier (linear kernel) to the training data. The linear kernel provides a linear decision boundary.

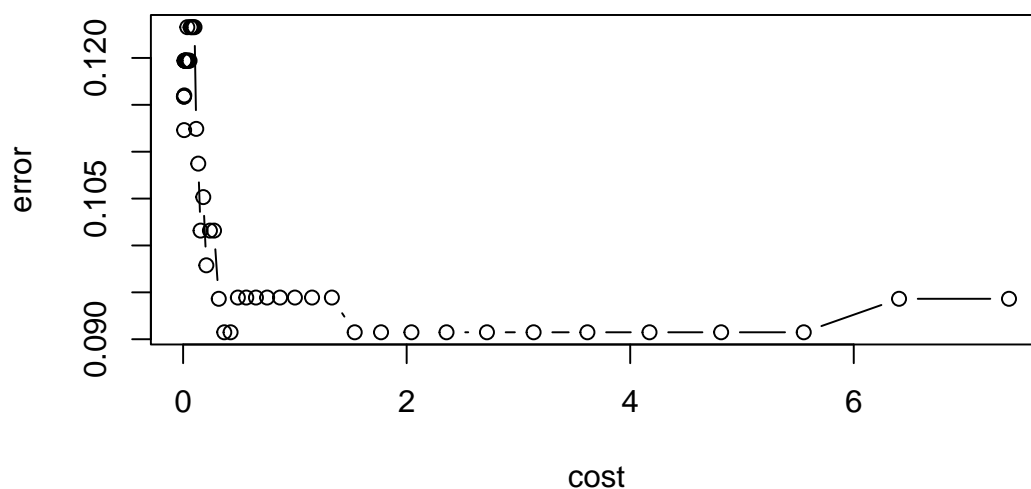
```
set.seed(0504)
```

```
# using package e1071
```

```
linear_svm = tune.svm(mpg_cat ~ .,
                      data = auto[indexTrain, ],
                      kernel = "linear",
                      cost = exp(seq(-5, 2, len = 50)),
                      scale = TRUE)
```

```
# plot misclassification error based on cross validation against tuning parameter(cost)
plot(linear_svm)
```

Performance of 'svm'



```
# optimal tuning parameter with minimum cross-validation error
linear_svm$best.parameters
```

```
##          cost
## 29 0.3678794
```

```
# best model
best_linear_svm = linear_svm$best.model
summary(best_linear_svm)
```

```
##
## Call:
## best.svm(x = mpg_cat ~ ., data = auto[indexTrain, ], cost = exp(seq(-5,
##      2, len = 50)), kernel = "linear", scale = TRUE)
##
##
## Parameters:
##   SVM-Type:  C-classification
##   SVM-Kernel: linear
##      cost:  0.3678794
##
## Number of Support Vectors:  70
##
##  ( 34 36 )
##
##
## Number of Classes:  2
##
## Levels:
##  low high
```

From the results above, the optimum tuning parameter is achieved when cost is 0.368, which minimizes the cross-validation error.

```
# calculate training error rate from confusion matrix
confusionMatrix(data = linear_svm$best.model$fitted,
                 reference = auto$mpg_cat[indexTrain])
```

```
## Confusion Matrix and Statistics
##
##           Reference
## Prediction low high
##      low  121    8
##      high   17   130
##
##              Accuracy : 0.9094
##              95% CI : (0.8692, 0.9405)
##      No Information Rate : 0.5
##      P-Value [Acc > NIR] : <2e-16
##
##              Kappa : 0.8188
##
##  Mcnemar's Test P-Value : 0.1096
##
##              Sensitivity : 0.8768
##              Specificity : 0.9420
##      Pos Pred Value : 0.9380
##      Neg Pred Value : 0.8844
##      Prevalence : 0.5000
##      Detection Rate : 0.4384
##      Detection Prevalence : 0.4674
##      Balanced Accuracy : 0.9094
##
##      'Positive' Class : low
##
```

Accuracy is 90.94%, therefore training error rate is 9.06%. We can also do the calculation: the optimal linear support vector classifier with linear kernel incorrectly classifies 25 out of 276 training observations, giving a 9.06% error rate.

```
set.seed(0504)

linear_svm_pred = predict(best_linear_svm, newdata = auto[-indexTrain, ])

# calculate test error rate from confusion matrix
confusionMatrix(data = linear_svm_pred,
                 reference = auto$mpg_cat[-indexTrain])
```

```
## Confusion Matrix and Statistics
##
##           Reference
## Prediction low high
##      low    51    3
##      high    7   55
```

```
##
##           Accuracy : 0.9138
##           95% CI : (0.8472, 0.9579)
##      No Information Rate : 0.5
##      P-Value [Acc > NIR] : <2e-16
##
##           Kappa : 0.8276
##
##  McNemar's Test P-Value : 0.3428
##
##      Sensitivity : 0.8793
##      Specificity : 0.9483
##      Pos Pred Value : 0.9444
##      Neg Pred Value : 0.8871
##      Prevalence : 0.5000
##      Detection Rate : 0.4397
##      Detection Prevalence : 0.4655
##      Balanced Accuracy : 0.9138
##
##      'Positive' Class : low
##
```

Accuracy is 91.38%, therefore test error rate is 8.62%. Calculation by hand: the classifier incorrectly classifies 10 out of 116 observations, giving a 8.62% error rate.

Radial Kernel

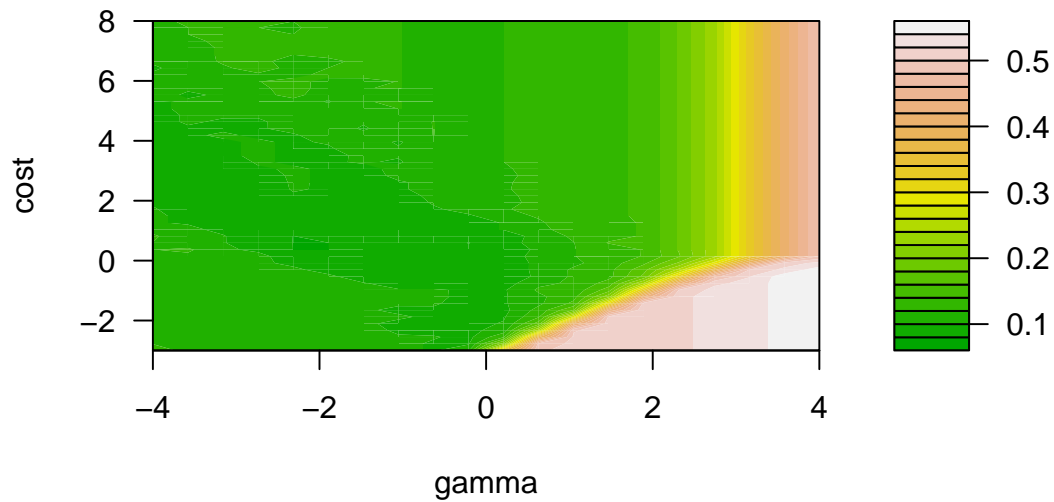
Fit a support vector machine with a radial kernel to the training data. This gives a nonlinear decision boundary.

```
set.seed(0504)

# using package e1071
radial_svm = tune.svm(mpg_cat ~ .,
                      data = auto[indexTrain, ],
                      kernel = "radial",
                      cost = exp(seq(-3, 8, len = 50)),
                      gamma = exp(seq(-4, 4, len = 20)),
                      scale = TRUE)

plot(radial_svm, transform.y = log, transform.x = log, color.palette = terrain.colors)
```

Performance of 'svm'



```
radial_svm$best.parameters
```

```
##      gamma      cost
## 348 0.3490181 2.262175
```

```
best_radial_svm = radial_svm$best.model
summary(radial_svm$best.model)
```

```
##
## Call:
## best.svm(x = mpg_cat ~ ., data = auto[indexTrain, ], gamma = exp(seq(-4,
##      4, len = 20)), cost = exp(seq(-3, 8, len = 50)), kernel = "radial",
##      scale = TRUE)
##
##
## Parameters:
##   SVM-Type:  C-classification
##   SVM-Kernel: radial
##      cost:  2.262175
##
## Number of Support Vectors:  91
##
##  ( 46 45 )
##
##
## Number of Classes:  2
##
## Levels:
##  low high
```

From the results above, the optimum tuning parameter is achieved when gamma is 0.349 cost is 2.262, which minimizes the cross-validation error.

```
# calculate training error rate from confusion matrix
confusionMatrix(data = radial_svm$best.model$fitted,
                 reference = auto$mpg_cat[indexTrain])
```

```
## Confusion Matrix and Statistics
##
##           Reference
## Prediction low high
##      low  130    6
##      high   8  132
##
##              Accuracy : 0.9493
##              95% CI : (0.9164, 0.972)
##      No Information Rate : 0.5
##      P-Value [Acc > NIR] : <2e-16
##
##              Kappa : 0.8986
##
##  Mcnemar's Test P-Value : 0.7893
##
##              Sensitivity : 0.9420
##              Specificity : 0.9565
##      Pos Pred Value : 0.9559
##      Neg Pred Value : 0.9429
##      Prevalence : 0.5000
##      Detection Rate : 0.4710
##      Detection Prevalence : 0.4928
##      Balanced Accuracy : 0.9493
##
##      'Positive' Class : low
##
```

Accuracy is 94.93%, therefore training error rate is 5.07%. We can also do the calculation: the optimal linear support vector classifier with radial kernel incorrectly classifies 14 out of 276 training observations, giving a 5.07% error rate.

```
set.seed(0504)

radial_svm_pred = predict(best_radial_svm, newdata = auto[-indexTrain, ])

# calculate test error rate from confusion matrix
confusionMatrix(data = radial_svm_pred,
                 reference = auto$mpg_cat[-indexTrain])
```

```
## Confusion Matrix and Statistics
##
##           Reference
## Prediction low high
##      low   56    1
##      high   2   57
```



```
##
##           Accuracy : 0.9741
##           95% CI   : (0.9263, 0.9946)
##    No Information Rate : 0.5
##    P-Value [Acc > NIR] : <2e-16
##
##           Kappa : 0.9483
##
##    McNemar's Test P-Value : 1
##
##           Sensitivity : 0.9655
##           Specificity : 0.9828
##           Pos Pred Value : 0.9825
##           Neg Pred Value : 0.9661
##           Prevalence : 0.5000
##           Detection Rate : 0.4828
##    Detection Prevalence : 0.4914
##           Balanced Accuracy : 0.9741
##
##           'Positive' Class : low
##
```

Accuracy is 97.41%, therefore test error rate is 2.59%. Calculation by hand: the classifier incorrectly classifies 3 out of 116 observations, giving a 2.59% error rate.

For support vector machine with radial kernel, the training and test error rate are both lower than that of svm with linear kernel. So the model with radial kernel performs better.

Hierachical Clustering

Without scaling

```
data(USArrests)

arrests = USArrests %>% as.data.frame()

dim(arrests)
```

```
## [1] 50  4
```

```
skimr::skim_without_charts(arrests)
```

Table 4: Data summary

Name	arrests
Number of rows	50
Number of columns	4
Column type frequency:	
numeric	4

Table 4: Data summary

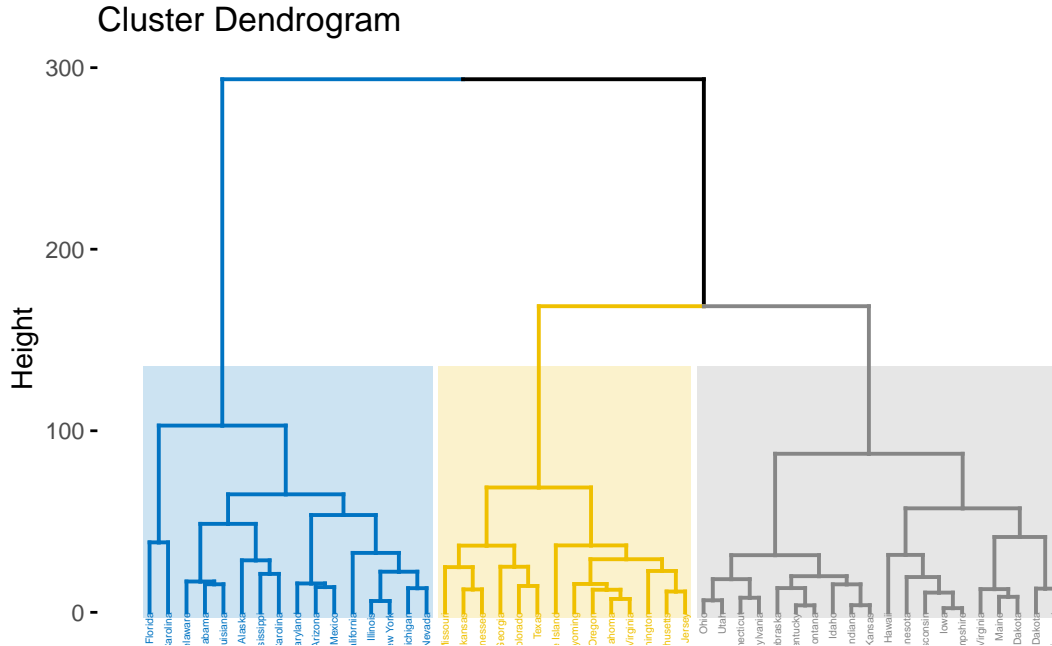
Group variables	None
-----------------	------

Variable type: numeric

skim_variable	n_missing	complete_rate	mean	sd	p0	p25	p50	p75	p100
Murder	0	1	7.79	4.36	0.8	4.08	7.25	11.25	17.4
Assault	0	1	170.76	83.34	45.0	109.00	159.00	249.00	337.0
UrbanPop	0	1	65.54	14.47	32.0	54.50	66.00	77.75	91.0
Rape	0	1	21.23	9.37	7.3	15.08	20.10	26.17	46.0

```
# hierarchical clustering with complete linkage and Euclidean distance (without scaling)
hc = hclust(dist(arrests), method = "complete")
```

```
# cut the dendrogram at a height that results in three distinct clusters
fviz_dend(hc, k = 3,
  cex = 0.3,
  palette = "jco",
  color_labels_by_k = TRUE,
  rect = TRUE, rect_fill = TRUE, rect_border = "jco",
  labels_track_height = 2.5)
```



The cluster on the left includes some populous states, such as New York, California, Florida, North Carolina, Illinois, etc.

The middle cluster includes some Southern states, such as Missouri, Arkansas, Tennessee, but also some others, like Washington, Massachusetts and New Jersey. The cluster on the right contains some less populous

states, like Ohio, Utah, Kentucky, and others.

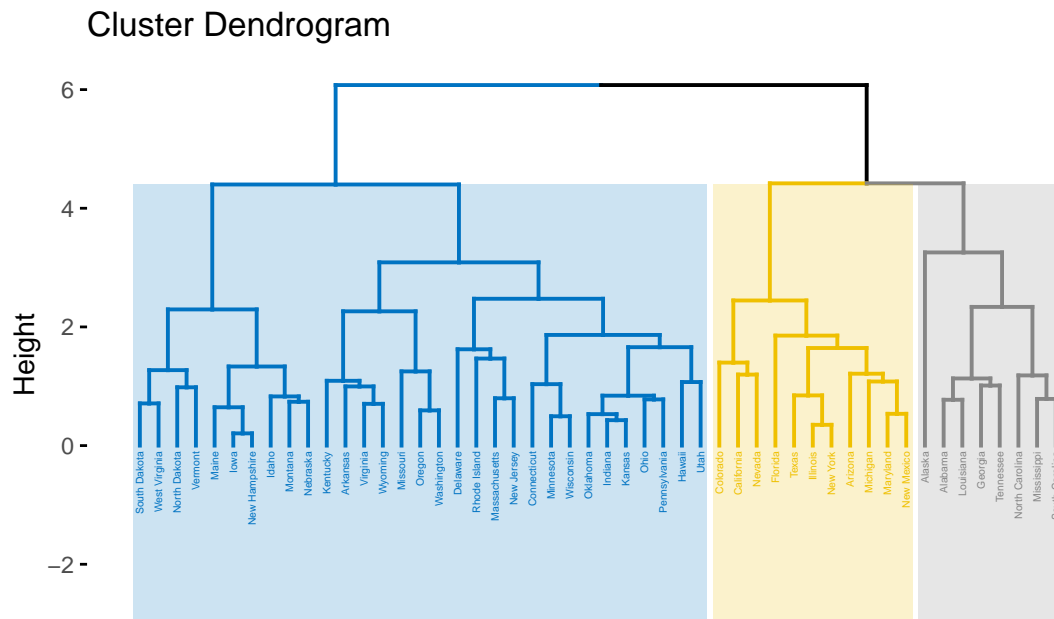
There seems not be any clear pattern pattern of the clustering based on geography, but there might be some grouping tendencies based on population of the states.

With scaling

```
# scale and center data
arrests_scaled = scale(arrests, center = TRUE, scale = TRUE)

# hierarchical clustering with complete linkage and Euclidean distance
hc_scaled = hclust(dist(arrests_scaled), method = "complete")

# cut the dendrogram at a height that results in three distinct clusters
fviz_dend(hc_scaled, k = 3,
  cex = 0.3,
  palette = "jco",
  color_labels_by_k = TRUE,
  rect = TRUE, rect_fill = TRUE, rect_border = "jco",
  labels_track_height = 2.5)
```



We can see that there are more states in the left cluster than other 2 clusters. And the distribution of the states is quite different from the dendrogram without clustering.

Discussion

Scaling the variables change the clustering results.

With scaling, one cluster contains South Dakota, West Virginia, any many other of the less populous states; another cluster contains California, Nevada, Texas, New York, and primarily more populous states in major

urban metro areas; and a third cluster with Alaska, Alabama, Louisiana, Georgia, and a number of other mostly Southern U.S. states. This is quite different from the dendrogram plotted without scaling.

This is because the clustering algorithms requires the method of calculating distance to be specified, as we are using Euclidean distance here. Without scaling numeric variables, the variables with greater magnitudes might be put more importance. In this case, if we do the classification without scaling, we're more likely to cluster based on **assault** than other variables, since it has greater values.

In my opinion, the variables should be scaled before the inter-observation dissimilarities are computed in order to ensure the variables are of comparable units.