

# ECON 4101 Econometrics

## CM27 Homework

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```
df <- fread('../Data/cm27.csv')
str(df)
```

```
## Classes 'data.table' and 'data.frame': 120 obs. of 2 variables:
## $ Date: chr "1965-01" "1965-02" "1965-03" "1965-04" ...
## $ x : int 52149 47205 82150 100931 98408 97351 96489 88830 80876 85750 ...
## - attr(*, ".internal.selfref")=<externalptr>
```

```
x <- ts(df$x, start=c(1965, 1), frequency = 12); str(x)
```

```
## Time-Series [1:120] from 1965 to 1975: 52149 47205 82150 100931 98408 97351 96489 88830 80876 85750
```

```
dcx <- decompose(x, type='mult')
```

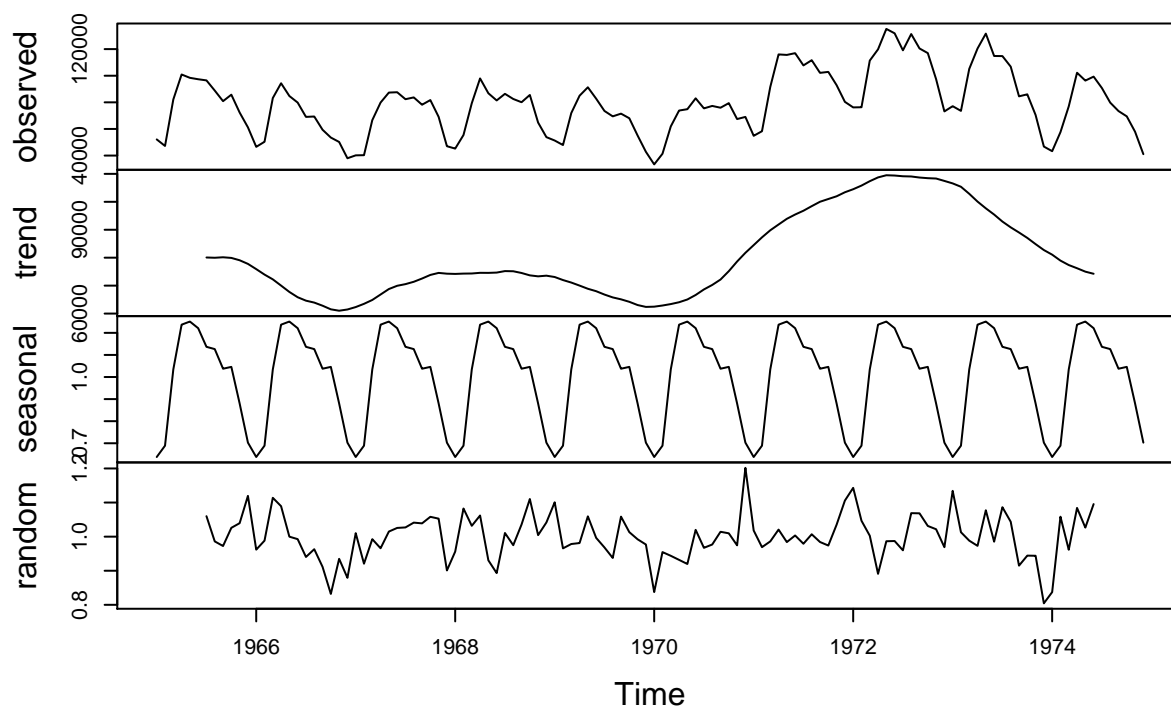
```
si <- dcx$figure; si
```

```
## [1] 0.6377157 0.6890862 1.0342534 1.2371012 1.2511790 1.2210904 1.1366869
```

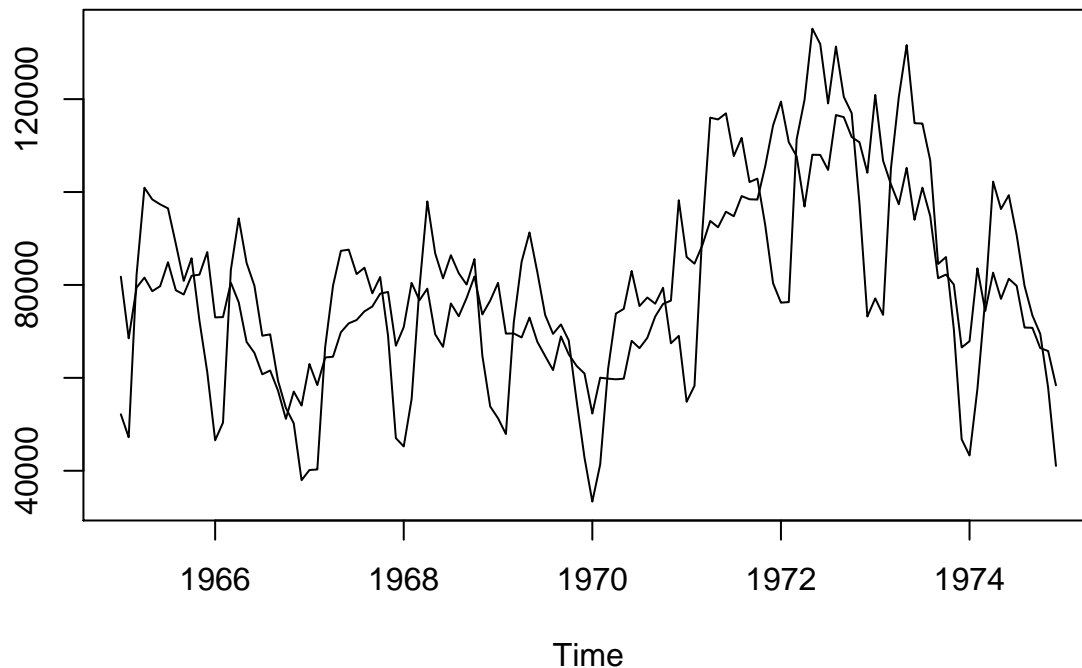
```
## [8] 1.1264665 1.0375980 1.0458780 0.8801633 0.7027814
```

```
plot(dcx)
```

### Decomposition of multiplicative time series



```
xsa <- seasadj(dcx)
ts.plot(x, xsa)
```



```
# Holt-Winter's Method
mod.hw <- HoltWinters(x, seasonal='multiplicative'); mod.hw

## Holt-Winters exponential smoothing with trend and multiplicative seasonal component.
##
## Call:
## HoltWinters(x = x, seasonal = "multiplicative")
##
## Smoothing parameters:
##   alpha: 0.6782381
##   beta : 0.05518518
##   gamma: 0.6475077
##
## Coefficients:
##           [,1]
## a    61687.3720937
## b   -1278.6636210
## s1     0.6493214
## s2     0.6967478
## s3     1.0025407
## s4     1.2517417
## s5     1.2853804
## s6     1.2471827
## s7     1.1553687
## s8     1.1122949
## s9     1.0152550
## s10    1.0186603
## s11    0.8662534
## s12    0.6731729

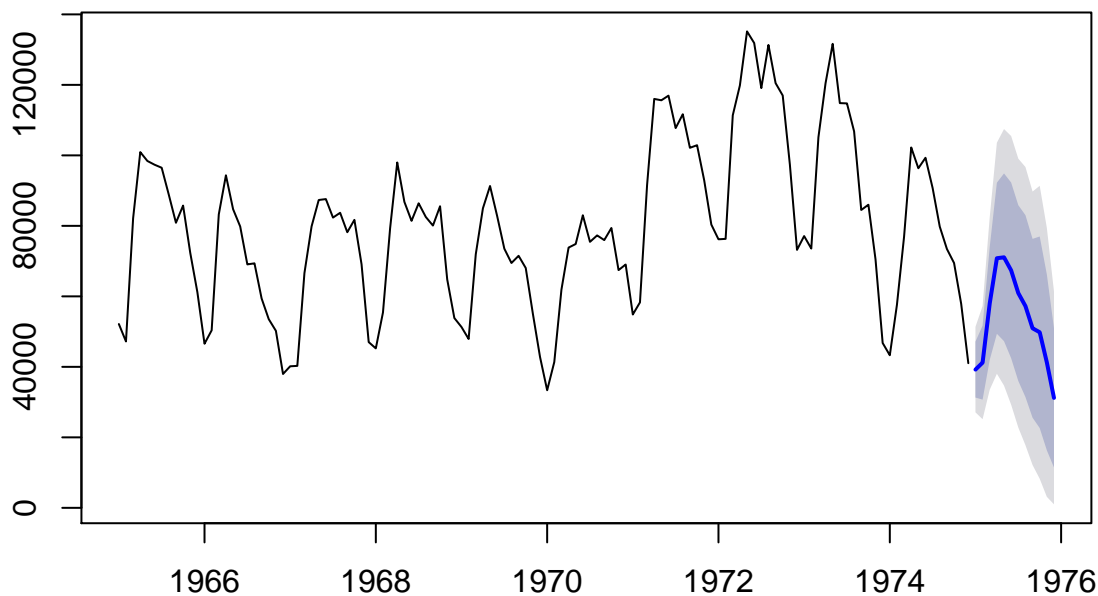
fcast.hw <- forecast(mod.hw, 12); fcast.hw

##           Point Forecast    Lo 80    Hi 80    Lo 95    Hi 95
## Jan 1975          39224.67 31292.34 47156.99 27093.215 51356.12
```

```
## Feb 1975      41198.73 30704.44 51693.02 25149.102  57248.36
## Mar 1975      57998.36 41997.16 73999.57 33526.628  82470.10
## Apr 1975      70814.43 49383.51 92245.35 38038.672 103590.19
## May 1975      71073.89 47281.36 94866.43 34686.353 107461.44
## Jun 1975      67367.06 42447.09 92287.04 29255.248 105478.87
## Jul 1975      60930.36 35996.32 85864.41 22797.028  99063.70
## Aug 1975      57236.54 31438.04 83035.04 17781.144  96691.93
## Sep 1975      50944.89 25583.75 76306.02 12158.374  89731.40
## Oct 1975      49813.24 22642.35 76984.12  8258.950  91367.52
## Nov 1975      41252.78 16318.43 66187.13  3118.988  79386.58
## Dec 1975      31197.12 11454.64 50939.61  1003.593  61390.66
```

```
plot(fcast.hw)
```

## Forecasts from HoltWinters



```
# SSARIMA method
```

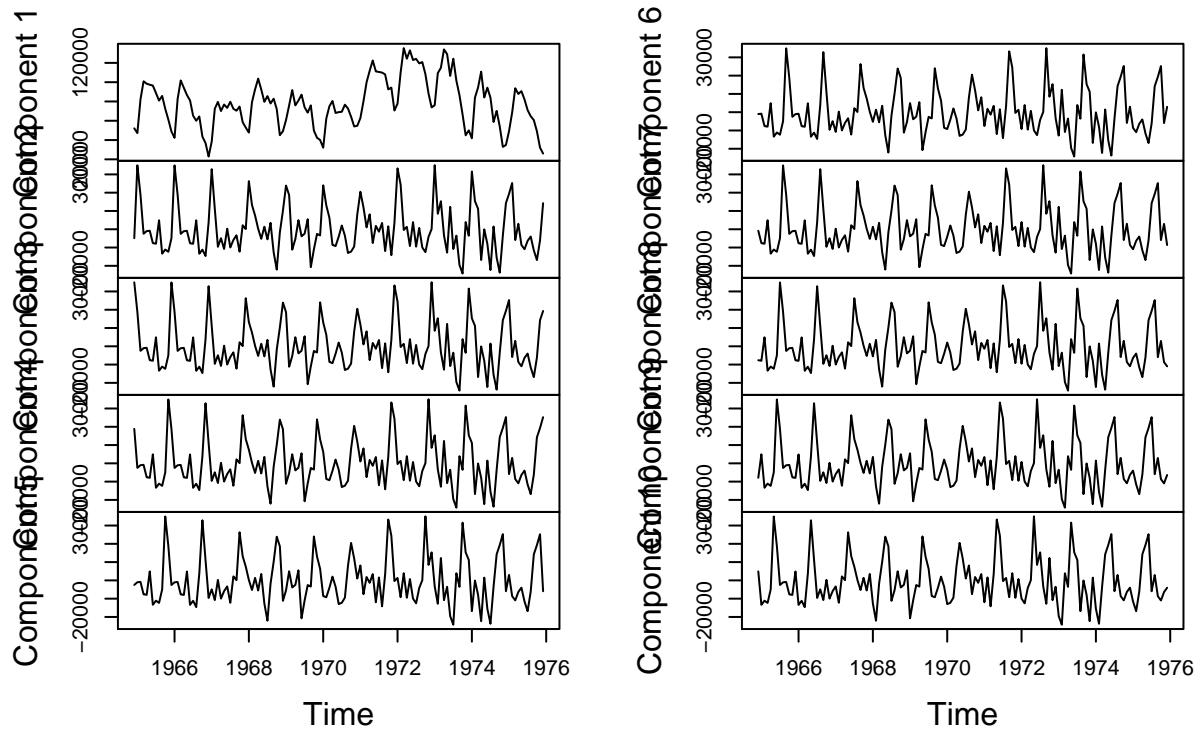
```
mod.ssarima <- auto.ssarima(x, h = 12, initial = 'optimal', stepwise = F, silent = 'all'); mod.ssarima
```

```
## Time elapsed: 13.35 seconds
## Model estimated: SARIMA(0,1,1)[1](0,1,0)[12] with drift
## Matrix of MA terms:
##      Lag 1
## MA(1) -0.321
## Constant value is: -46.83
## Initial values were optimised.
## 16 parameters were estimated in the process
## Residuals standard deviation: 8637.039
## Cost function type: MSE; Cost function value: 64651983.907
##
## Information criteria:
##      AIC      AICc      BIC
## 2530.689 2535.970 2575.289
```

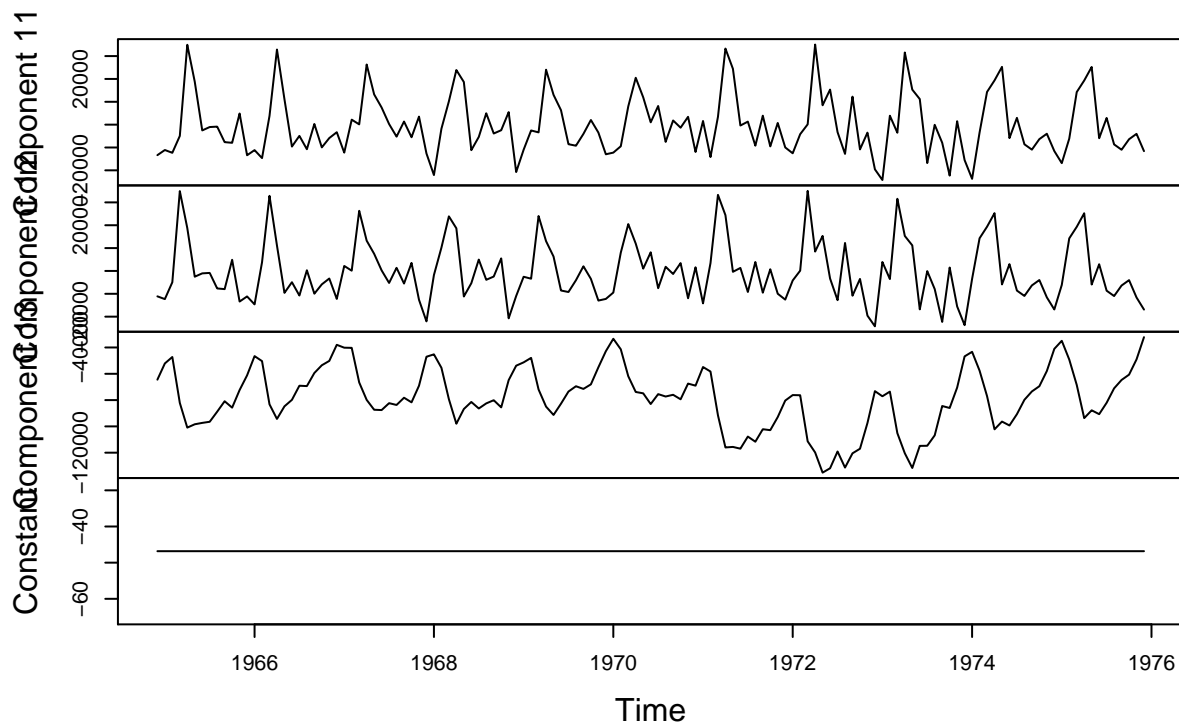
```
plot(mod.ssarima)
```

```
## Too many states. Plotting them one by one on several graphs.
```

### States of SARIMA(0,1,1)[1](0,1,0)[12] with drift, part 1



### States of SARIMA(0,1,1)[1](0,1,0)[12] with drift, part 2



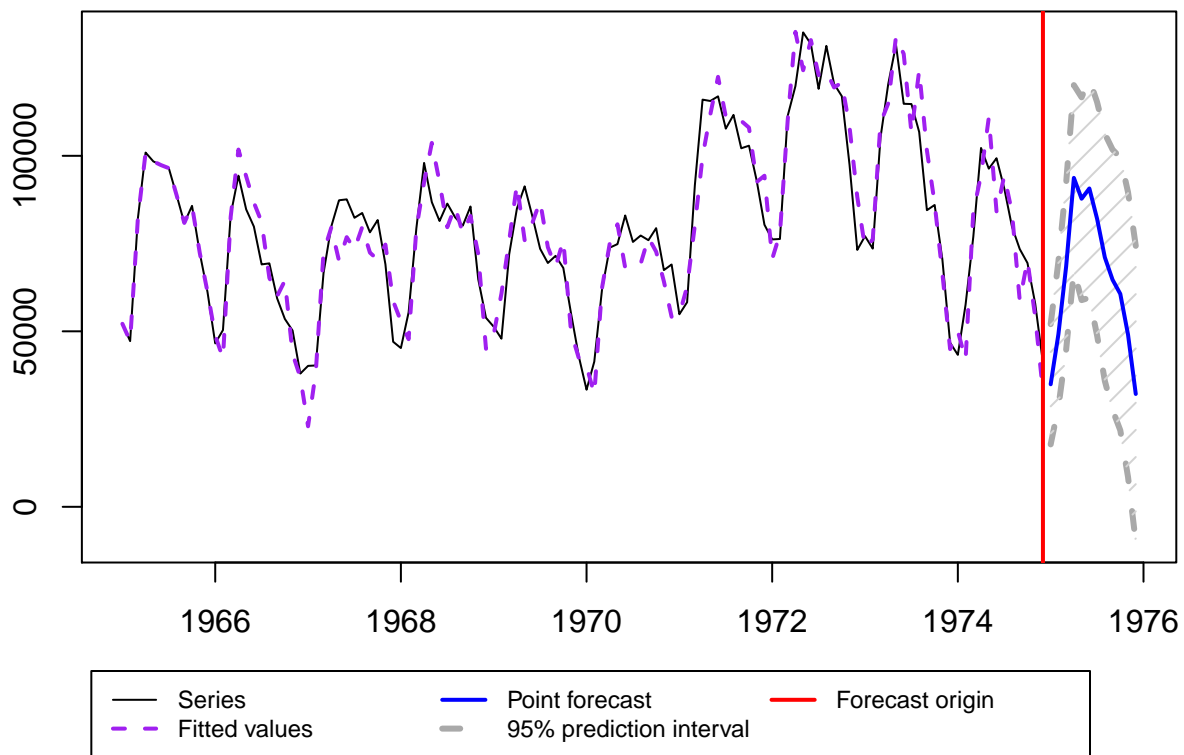
```
fcast.ssarima <- forecast(mod.ssarima, 12); fcast.ssarima
```

```
## Point forecast Lower bound (2.5%) Upper bound (97.5%)
```

```
## Jan 1975      34911.67      17784.097      52039.24
## Feb 1975      49165.84      28463.820      69867.86
## Mar 1975      68472.01      44727.674      92216.34
## Apr 1975      93716.18      67277.319      120155.04
## May 1975      87772.35      58889.254      116655.44
## Jun 1975      90703.52      59567.478      121839.56
## Jul 1975      82053.69      48817.069      115290.31
## Aug 1975      71073.86      35861.747      106285.97
## Sep 1975      64688.03      27605.517      101770.53
## Oct 1975      60658.20      21795.201      99521.19
## Nov 1975      49049.36       8483.959      89614.77
## Dec 1975      32145.53     -10053.660      74344.73
```

```
plot(fcast.ssarima)
```

### SARIMA(0,1,1)[1](0,1,0)[12] with drift



```
accuracies <- lapply(list('HoltWinters' = fcast.hw, 'SSARIMA' = fcast.ssarima), accuracy); accuracies
```

```
## $HoltWinters
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set -101.3616 6949.799 5362.592 -0.297502 7.191015 0.3601703
##           ACF1
## Training set 0.01727807
##
## $SSARIMA
##           ME      RMSE      MAE      MPE      MAPE      MASE
## Training set 0.0002327301 8040.646 6168.398 0.1626143 8.396789 0.414291
##           ACF1
## Training set -0.01169984
```