



High Impact Skills Development Program

in Artificial Intelligence, Data Science, and Blockchain

Module: [Computer Vision]

Lecture 1: [Introduction to Computer Vision]

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[Assistant Professor], SEECS, NUST**



Module Objectives



- To understand the basics of Computer Vision and Image Processing
- To discuss practical applications of Computer Vision
- To learn about Convolutional Neural Networks (CNNs)
- To understand Transfer Learning and Model Optimization Concepts
- To gain hands-on experience with relevant Python libraries



Agenda



- What is Computer Vision?
- Applications of Computer Vision
- Computer Vision Tasks and Trends
- Fundamentals of Digital Image Processing
- What is a Digital Image?
- Image Manipulations and Geometric Transformations



Introduction to Computer Vision

Lecture 1 - A





What is Computer Vision?



- Computer Vision provides the ability to computers to see and understand images



Image credit: Manfred-Suzanne DANEGGER/Gamma-Rapho via Getty Images



What is Computer Vision?



Making a computer understand:

- What animal is this?
- How many lions are there?
- What are they doing?



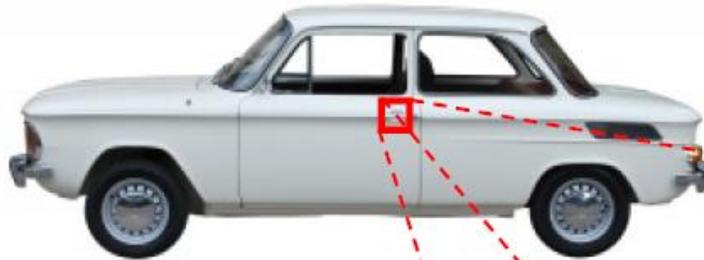
Image credit: Manfred-Suzanne DANEGGER/Gamma-Rapho via Getty Images



What is Computer Vision?



You see this:



But the camera sees this:

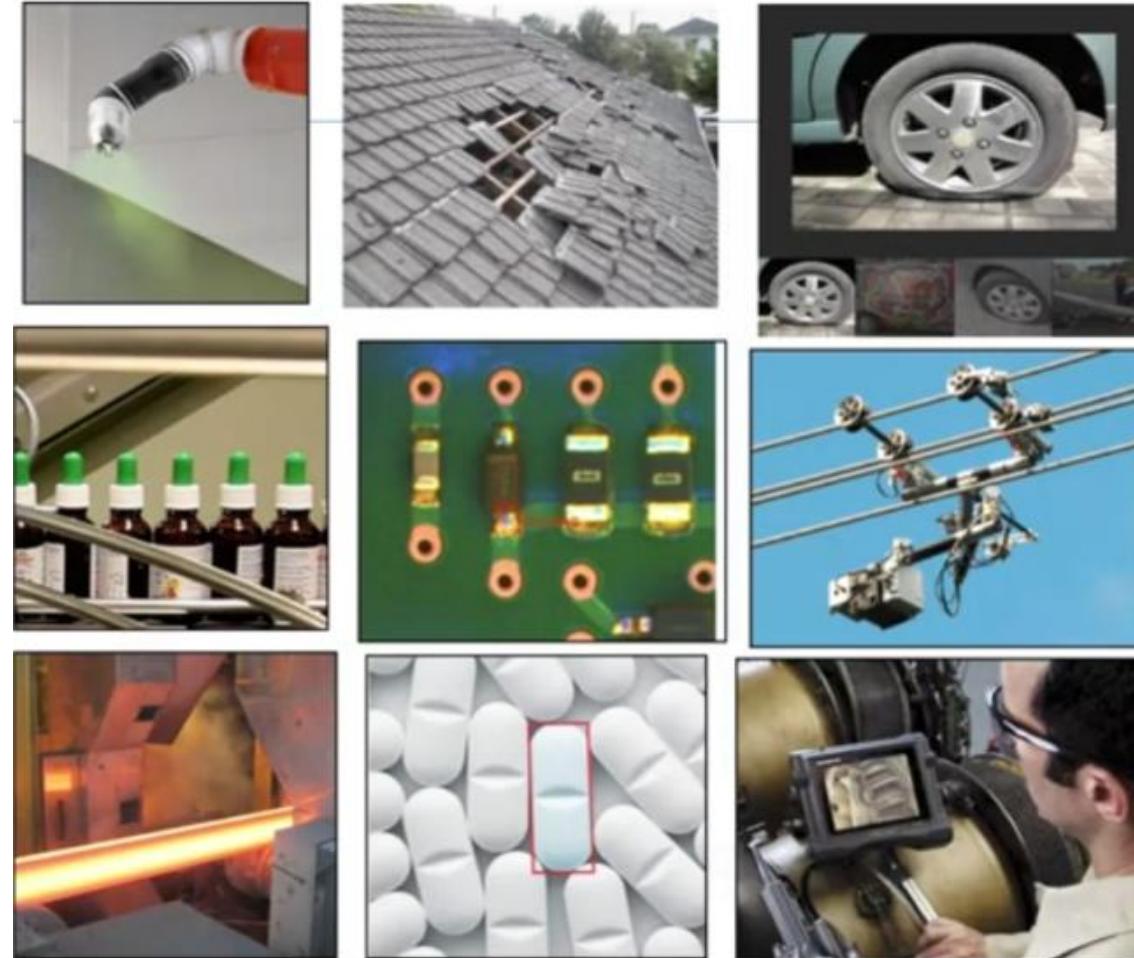
194	210	201	212	199	213	215	195	178	158	182	209
180	189	190	221	209	205	191	167	147	115	129	163
114	126	140	188	176	165	152	140	170	106	78	88
87	103	115	154	143	142	149	153	173	101	57	57
102	112	106	131	122	138	152	147	128	84	58	66
94	95	79	104	105	124	129	113	107	87	69	67
68	71	69	98	89	92	98	95	89	88	76	67
41	56	68	99	63	45	60	82	58	76	75	65
20	43	69	75	56	41	51	73	55	70	63	44
50	50	57	69	75	75	73	74	53	68	59	37
72	59	53	66	84	92	84	74	57	72	63	42
67	61	58	65	75	78	76	73	59	75	69	50



Applications of Computer Vision



- Automotive
- Waste Management
- Manufacturing
- Pharmaceutical
- Healthcare
- Customer Service
- Energy & Utilities
- Insurance
- Security & Surveillance
- Entertainment





Applications of Computer Vision

- ADNOC (Abu Dhabi National Oil Company)
- Uses Computer Vision with IBM Watson to classify 25,000 rock images per day

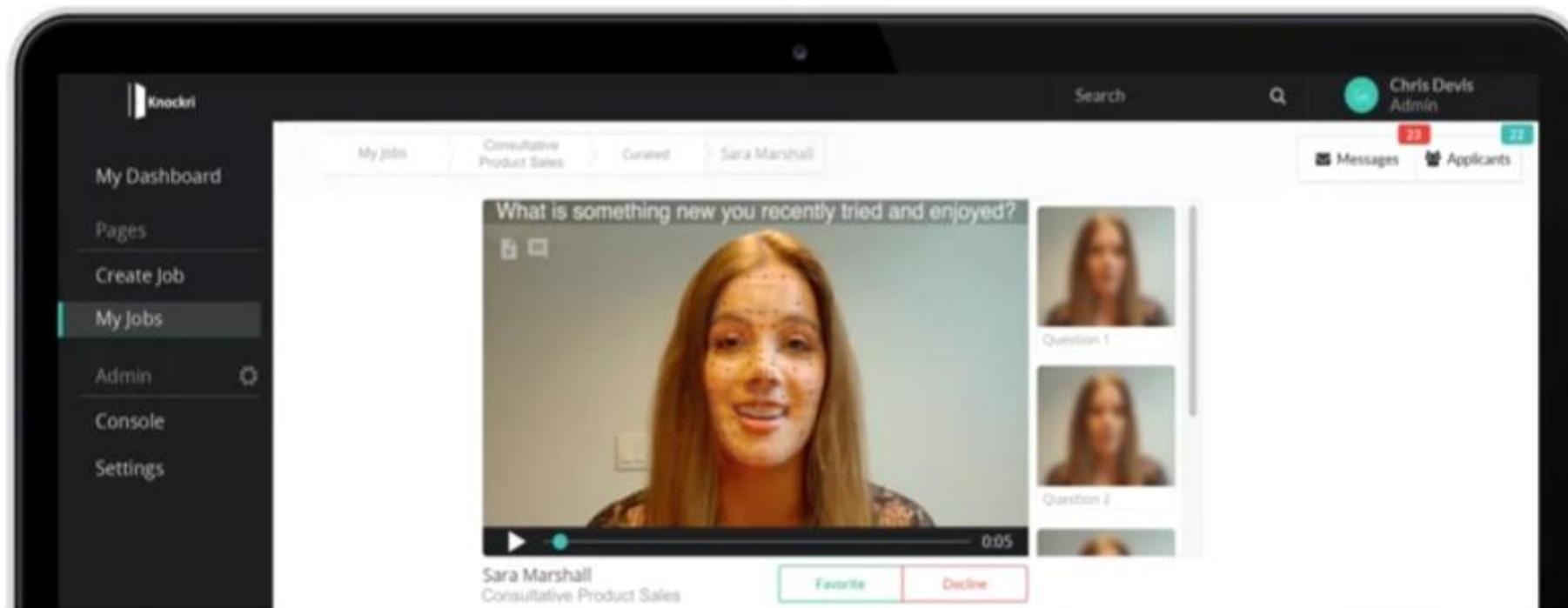


<https://www.ibm.com/case-studies/abu-dhabi-national-oil-company-adnoc>



Why use Computer Vision?

- Knockri – A Canadian-based startup
- Soft skills assessment tool to help large companies shortlist the candidates





Applications of Computer Vision

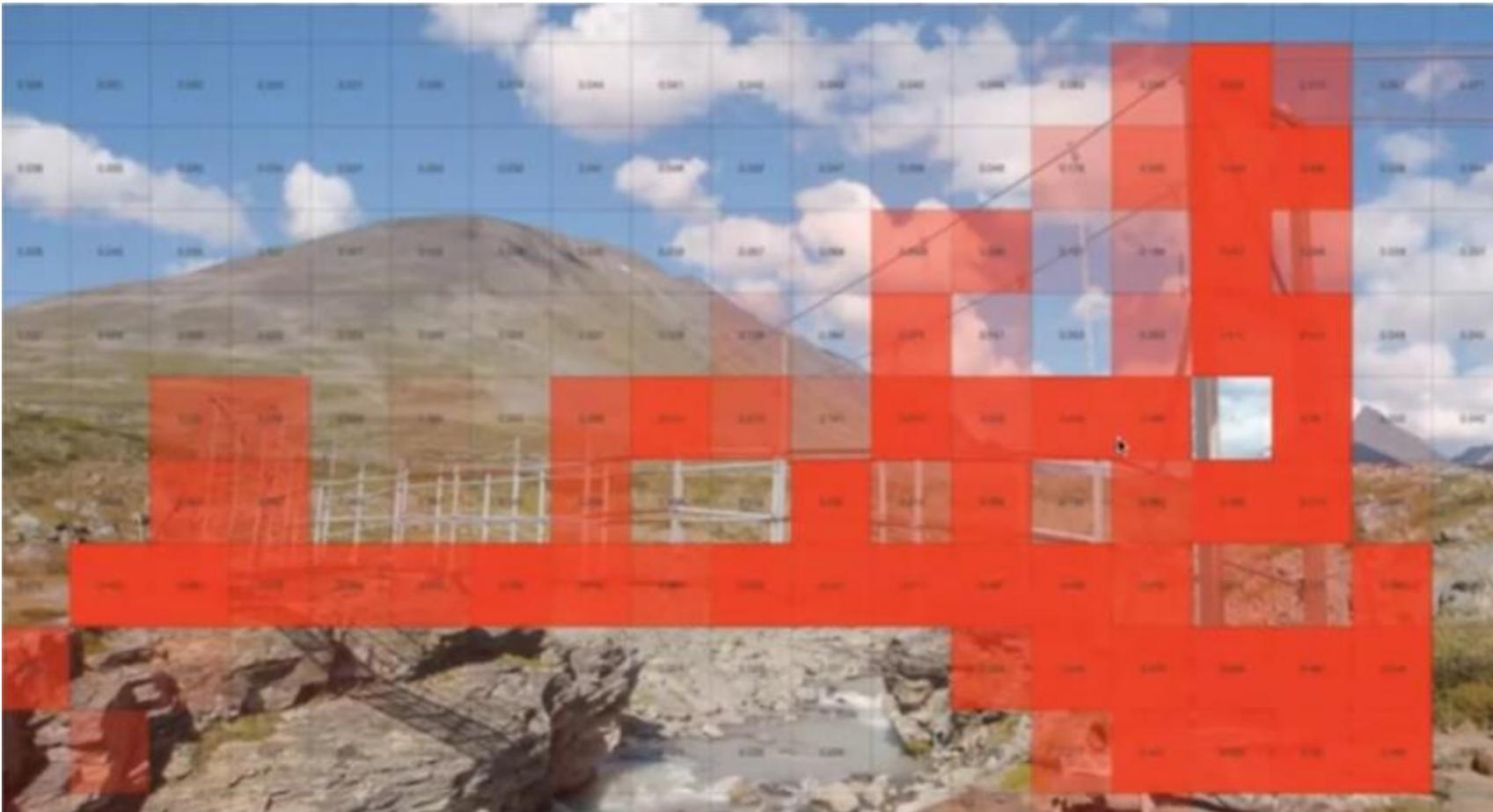
- Rust and Damage Detection





Applications of Computer Vision

- Rust and Damage Detection





Applications of Computer Vision



- Security & Surveillance



Image credit: coursera



Applications of Computer Vision

- Computer Vision in Healthcare

Bender_Gestalt_Test_Form1

Bender-Gestalt Test

Client :

Date :

Images

A.

1.

2.

3.

4.

5.

6.

7.

8.

Properties

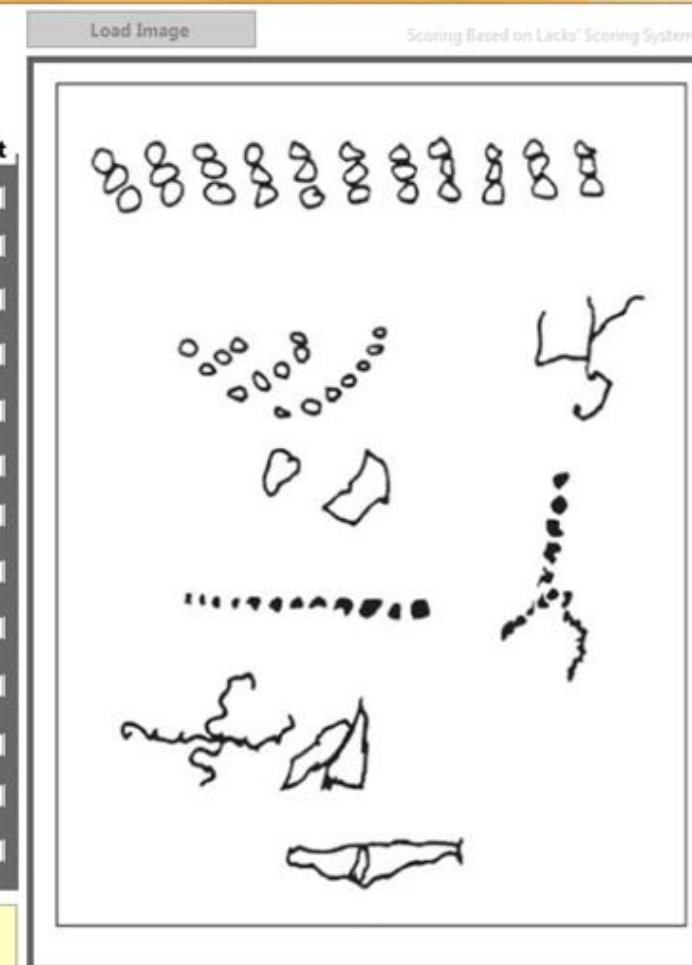
Rotation
Overlapping Difficulty
Simplification
Fragmentation
Retrogression
Preservation
Collusion Tendency
Impotence
Closuer Difficulty
Motor Incoordination
Angulation
Cohesion
Time

	A	1	2	3	4	5	6	7	8	Present
Rotation	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	1				
Overlapping Difficulty	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	1				
Simplification	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	1				
Fragmentation	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	1				
Retrogression	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	1				
Preservation	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	0				
Collusion Tendency	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	0				
Impotence	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	0				
Closuer Difficulty	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	1				
Motor Incoordination	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	1				
Angulation	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	1				
Cohesion	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	1				
Time	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>	0				

Status : Visual Perceptual Disorder Detected

PRT SCR Calculate Total 9

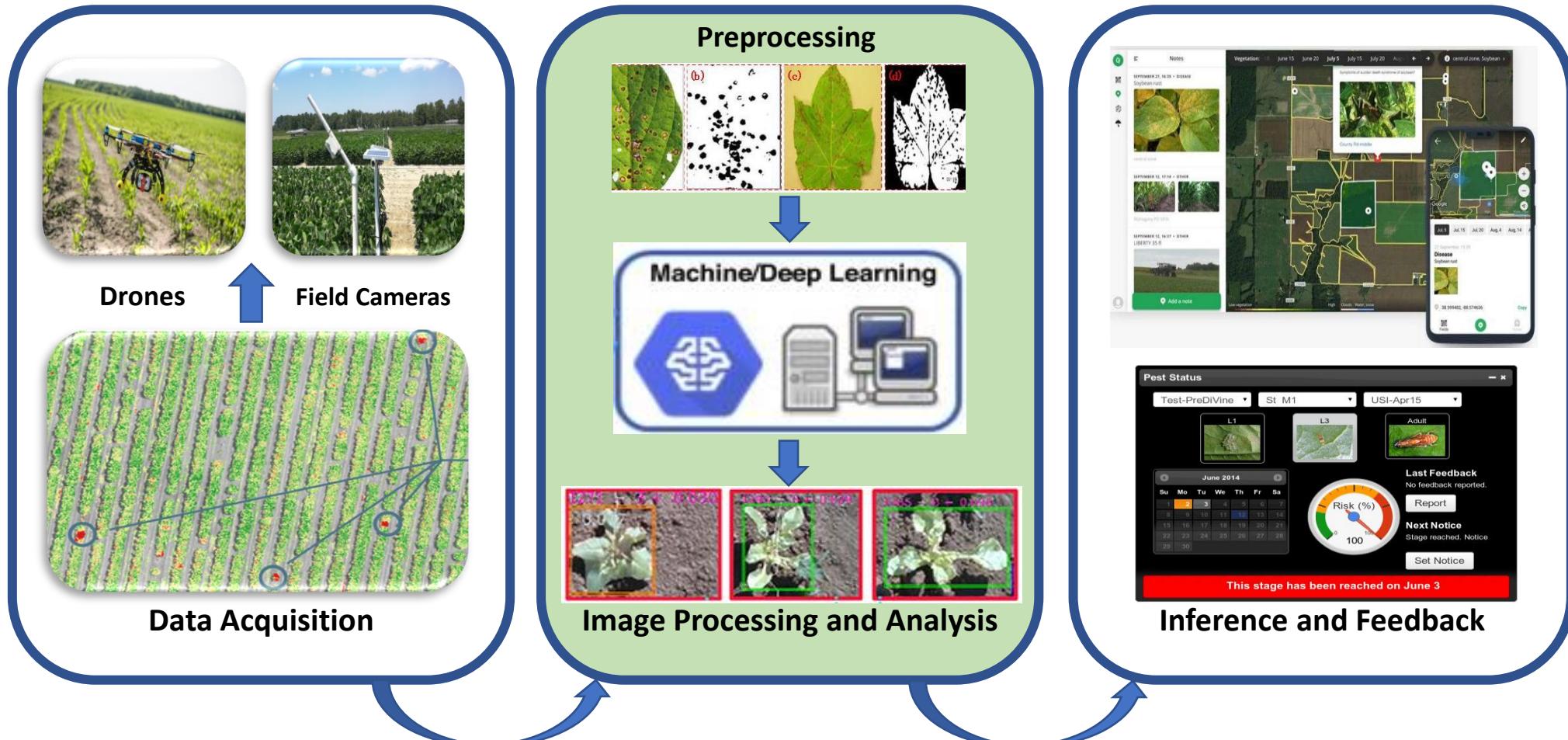
Load Image Scoring Based on Lacks' Scoring System





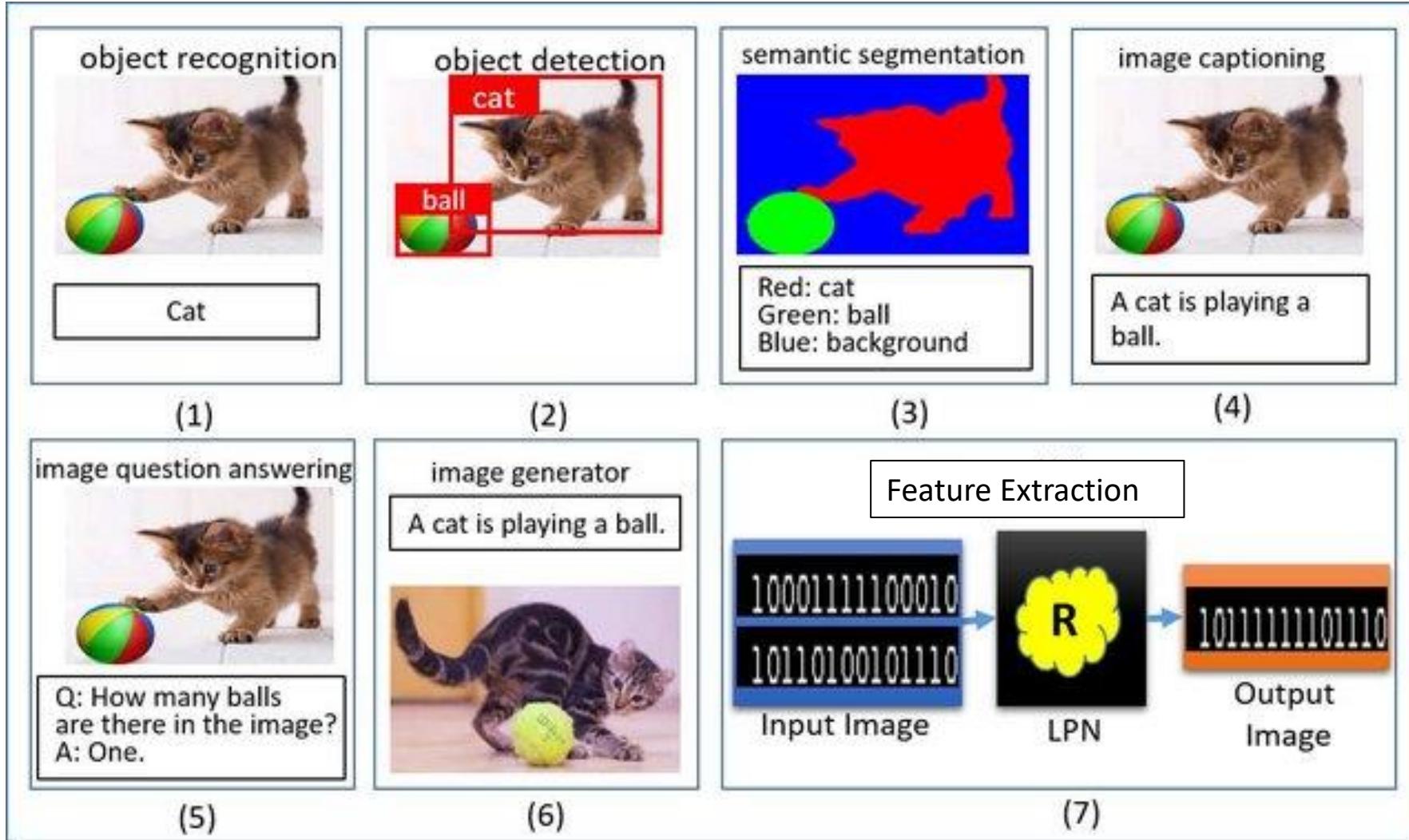
Applications of Computer Vision

- Computer Vision in Agriculture





Traditional Computer Vision Tasks





Advances in Computer Vision

- Image-to-Image Translation



zebra → horse



summer → winter



horse → zebra



winter → summer

Zhu et al. (2017). Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks. ICCV. <https://arxiv.org/pdf/1703.10593v6.pdf>



Advances in Computer Vision



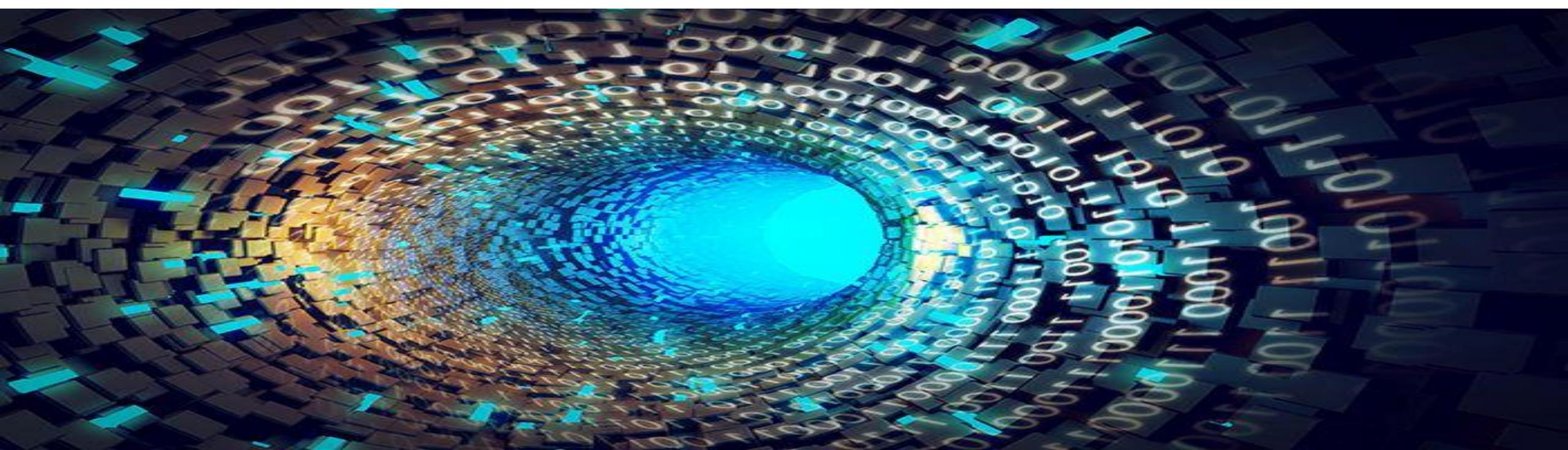
- Deep Fakes





Fundamentals of Digital Image Processing

Lecture 1 - B

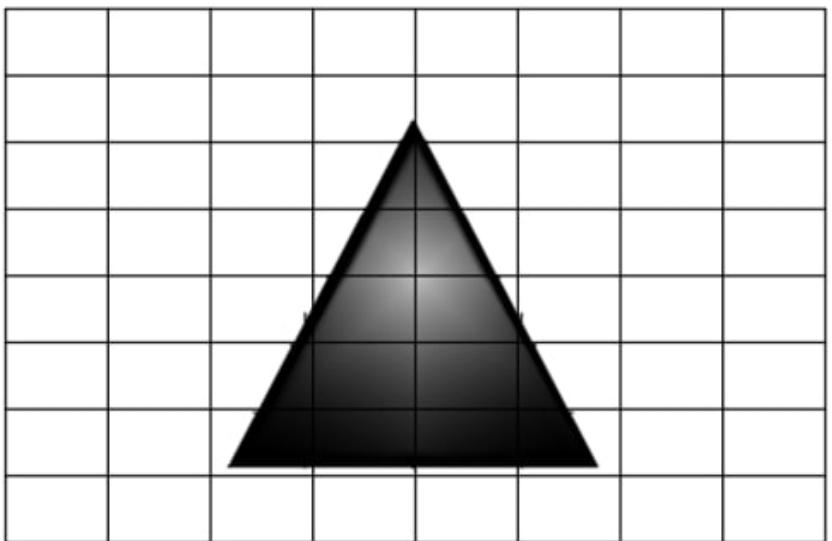




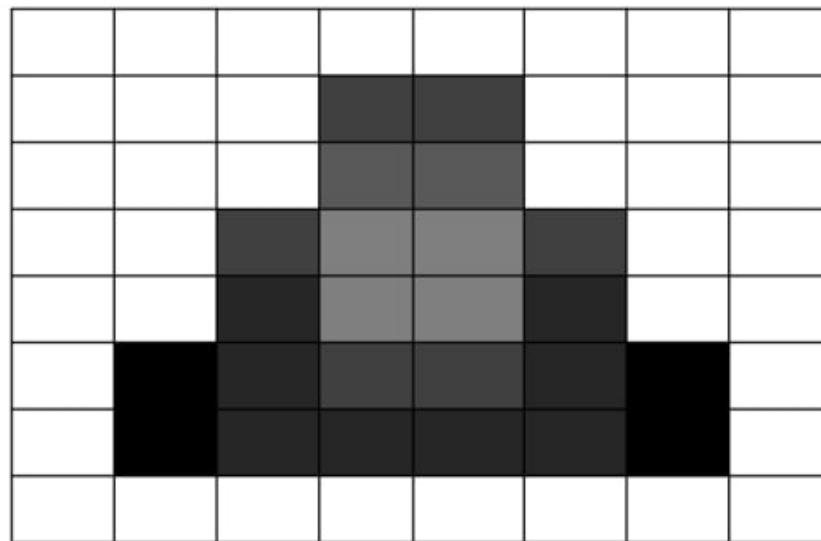
What is a Digital Image?



Digital Image is an approximation of a real world scene



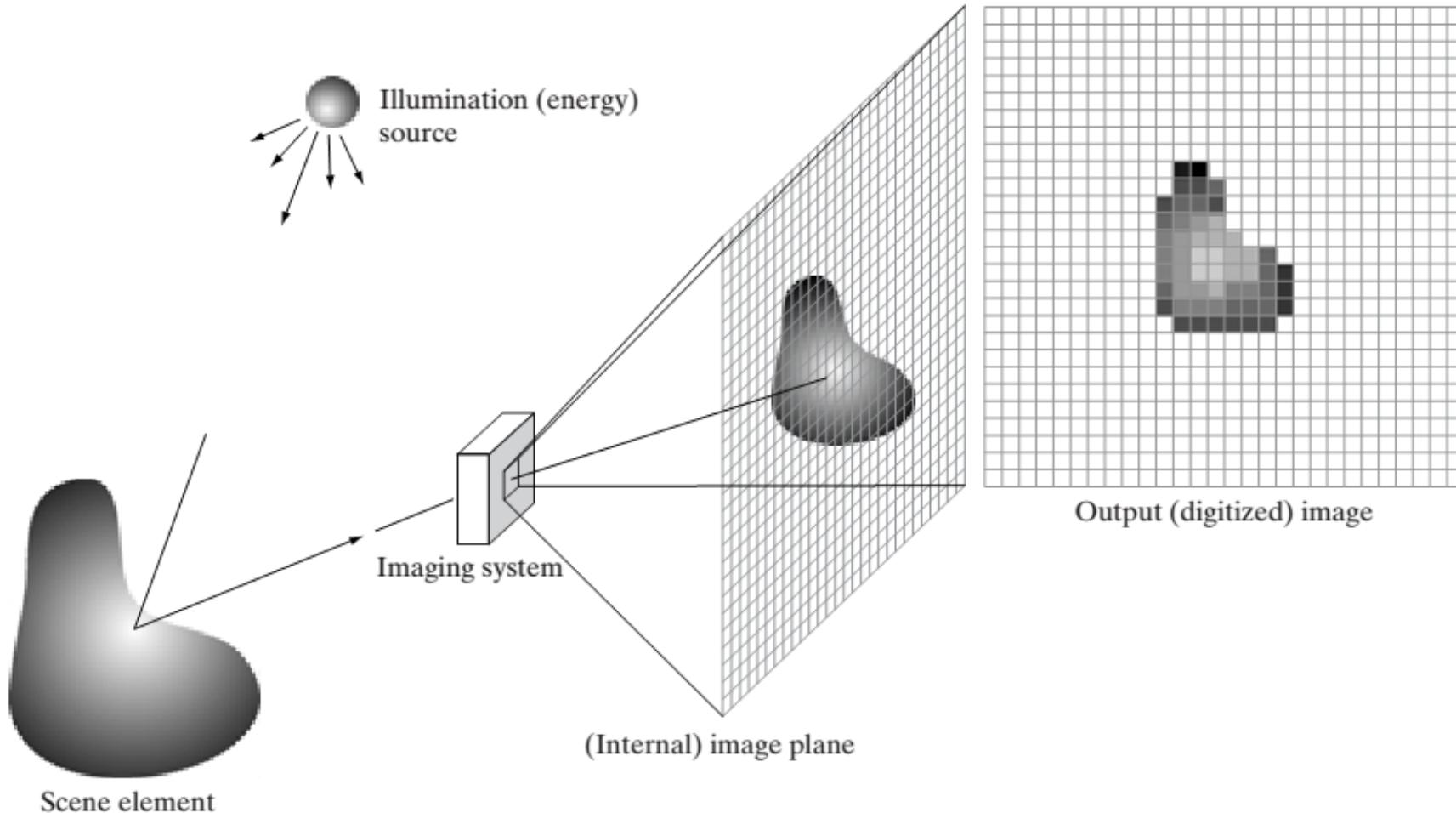
Continuous image projected onto a sensor array.



Result of image sampling and quantization.

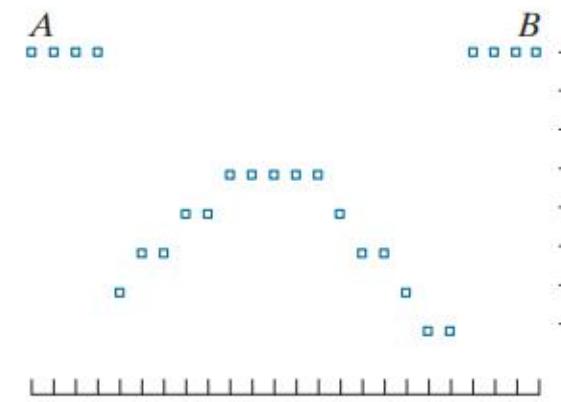
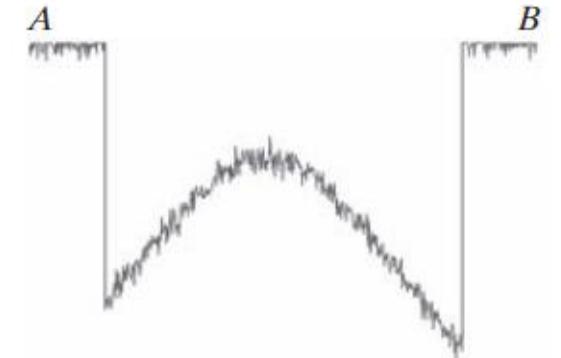
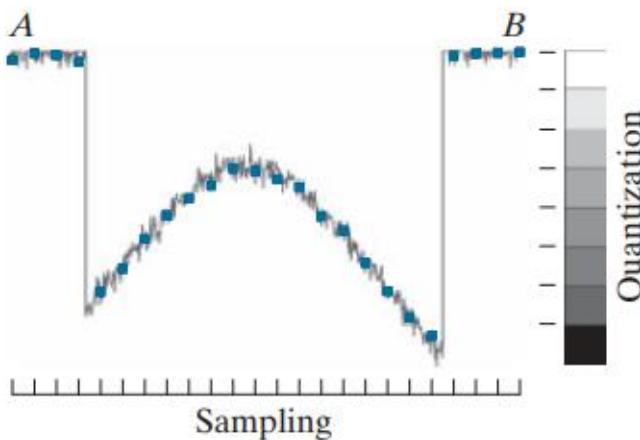
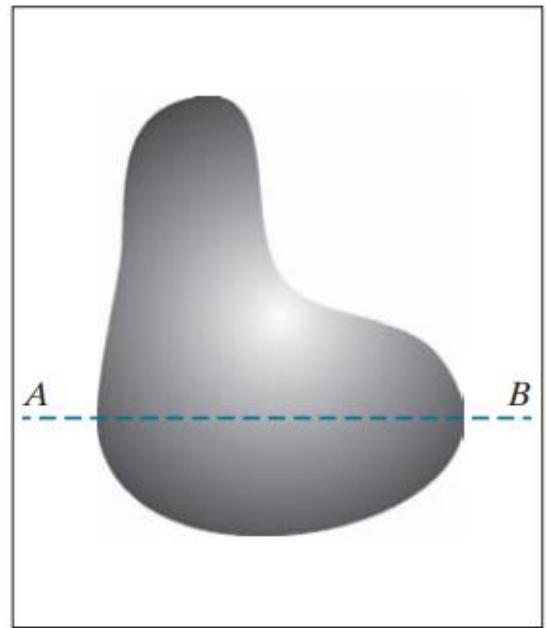


Digital Image Formation





Continuous to Digital

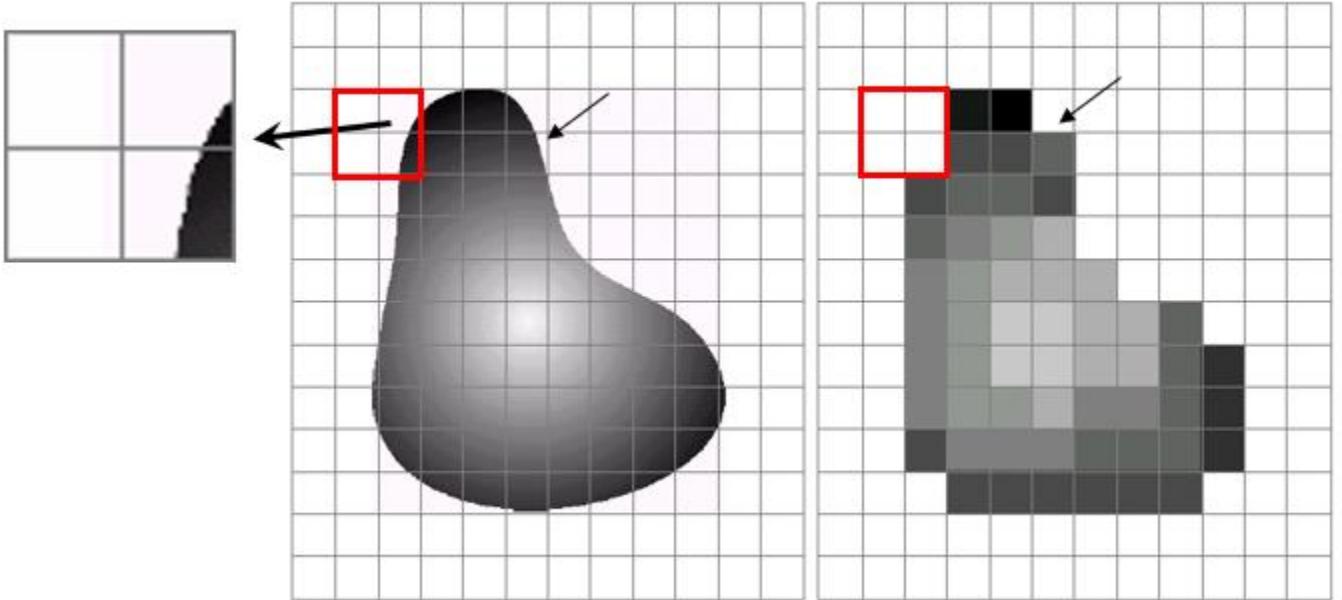




Sampling



- Sampling is a spatial resolution of the digital image.
- The rate of sampling determines the quality of the digitized image.

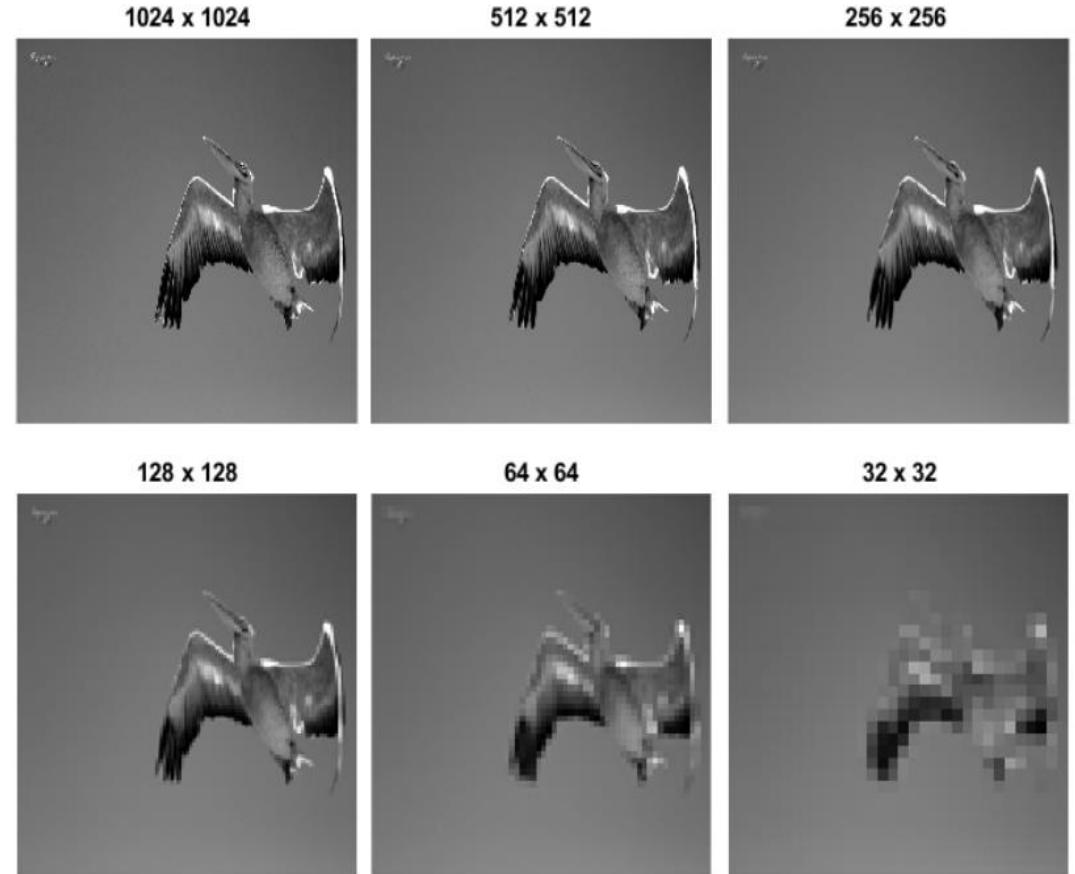




Spatial Resolution



- The spatial resolution of an image is determined by how sampling was carried out.
- There are 3 measures which we see often relating to Image Size/Resolution
 - a. **Pixel count** - e.g., 3000x2000 pixels
 - b. **Physical size** - e.g., 8" x 10"
 - c. **Resolution** - e.g., 240 pixels per inch (PPI)

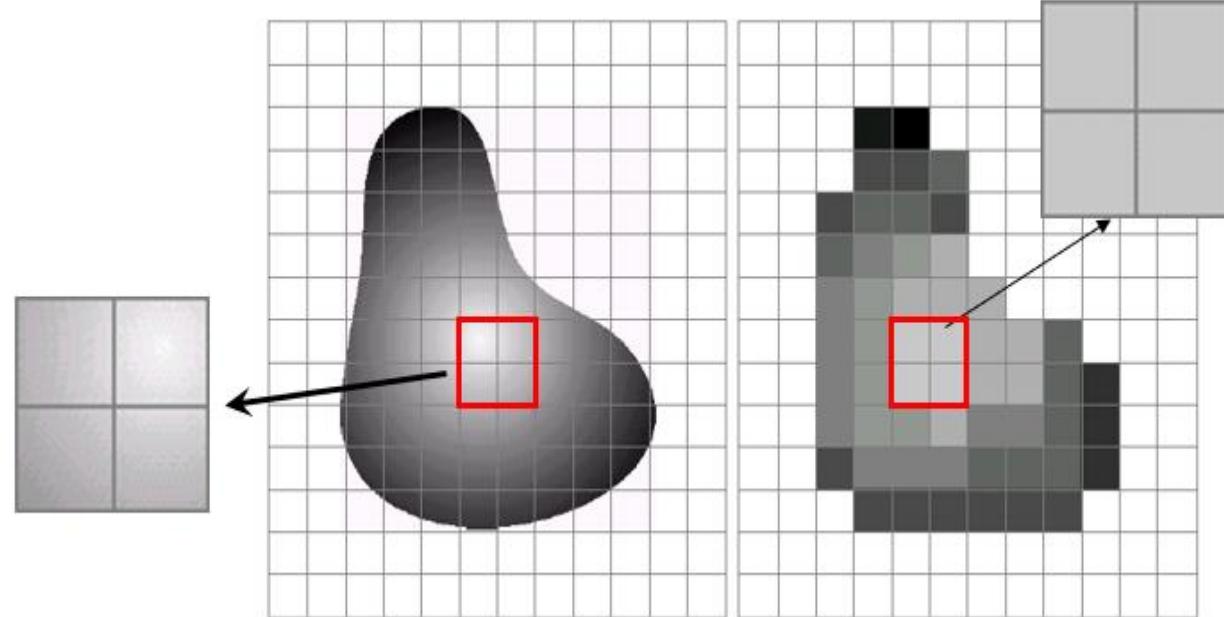




Quantization



- The transition of the continuous values from the image function to its digital equivalent is called quantization.
- Quantization is the number of grey levels in the digital image.
- It is related to the intensity values of the image.
- 8-bit quantization: $2^8 = 256$ gray levels
(0: black, 255: white)
- 1-bit quantization: 2 gray levels
(0: black, 1: white) – binary



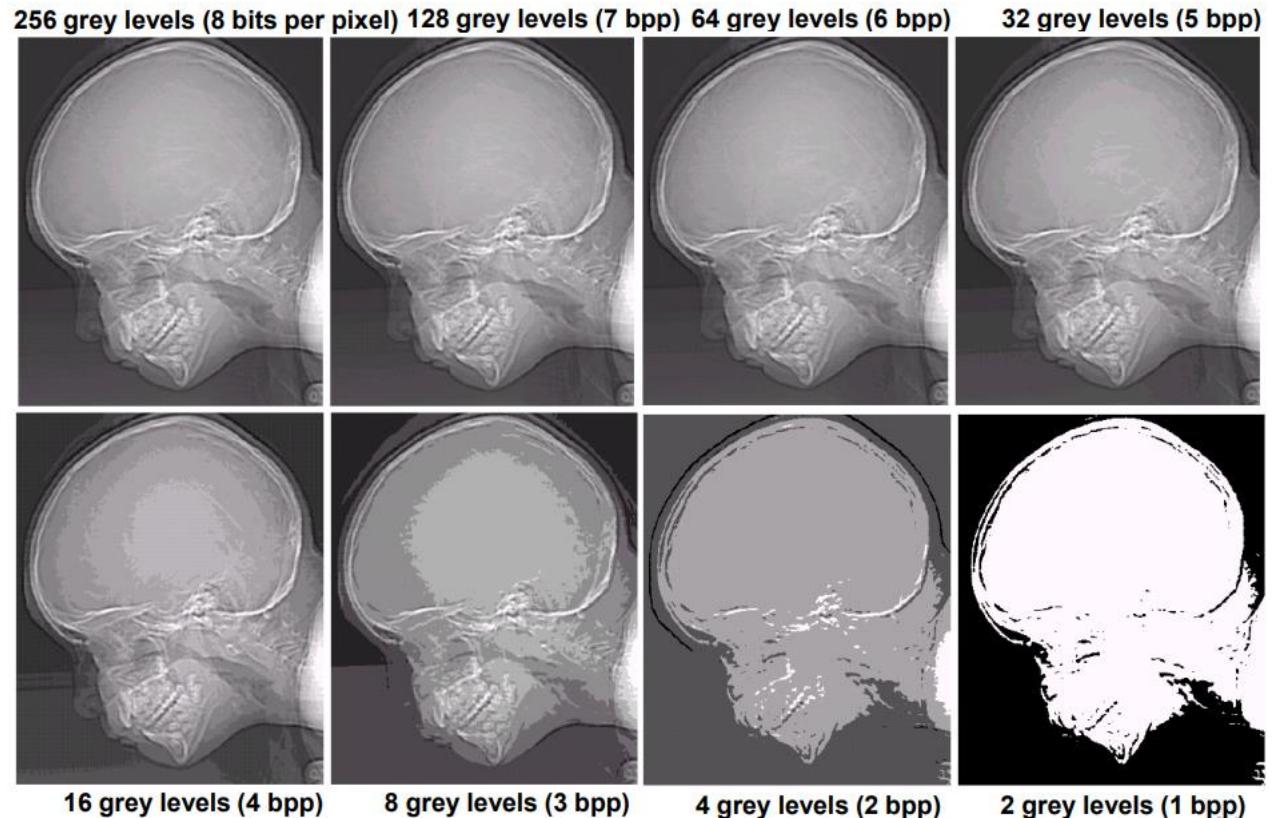
Number of Bits	Number of Intensity Levels	Examples
1	2	0, 1
2	4	00, 01, 10, 11
4	16	0000, 0101, 1111
8	256	00110011, 01010101
16	65,536	1010101010101010



Intensity Resolution



- Intensity level resolution refers to the number of intensity levels used to represent the image
- The more intensity levels used, the finer the level of detail in an image
- Intensity level resolution is usually given in terms of the number of bits used to store each intensity level





Resolution: How Much is Enough?





Image Contains Information



Image with low level of details



Image with medium level of details



Image with highest level of details



Image Representations



- Gray scale Images

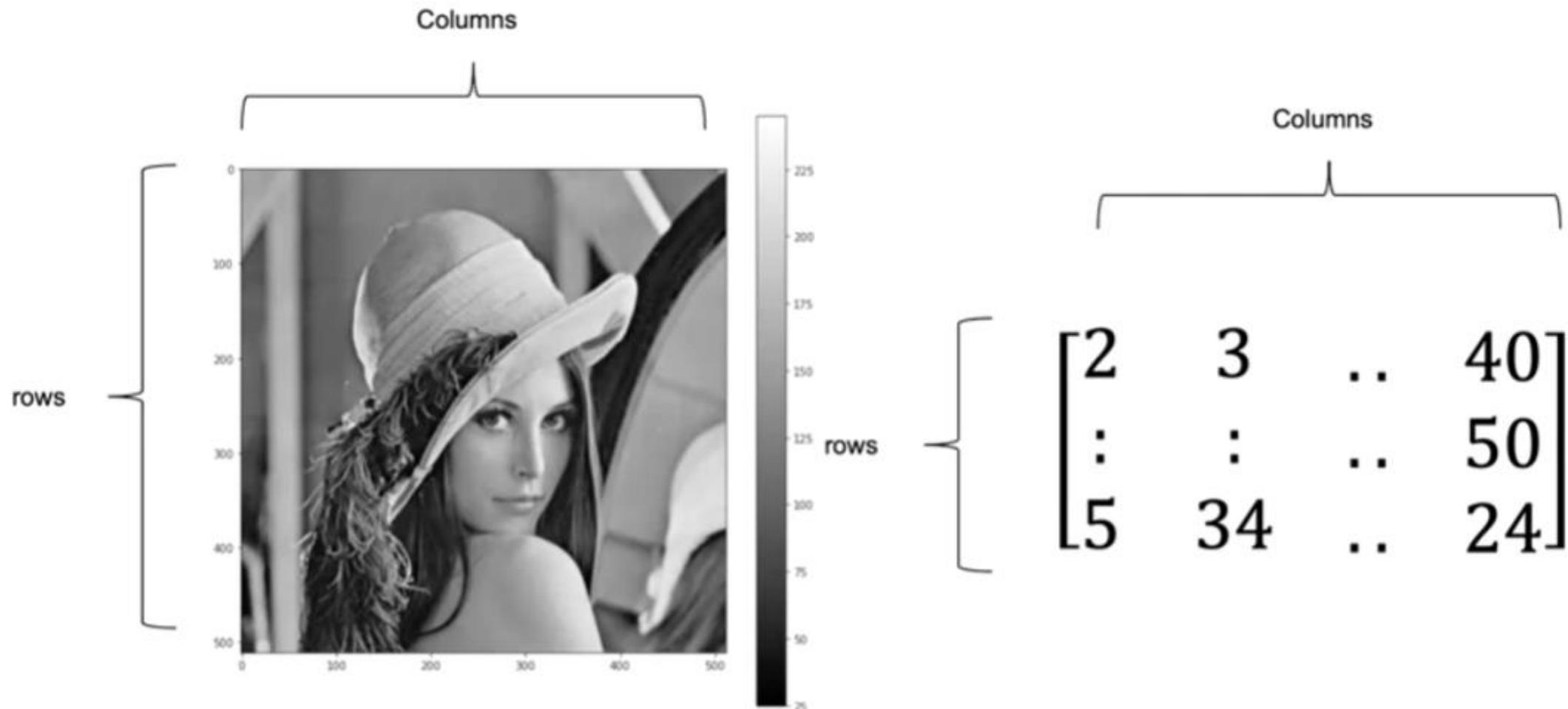




Image Representations



- Colored (RGB) Images



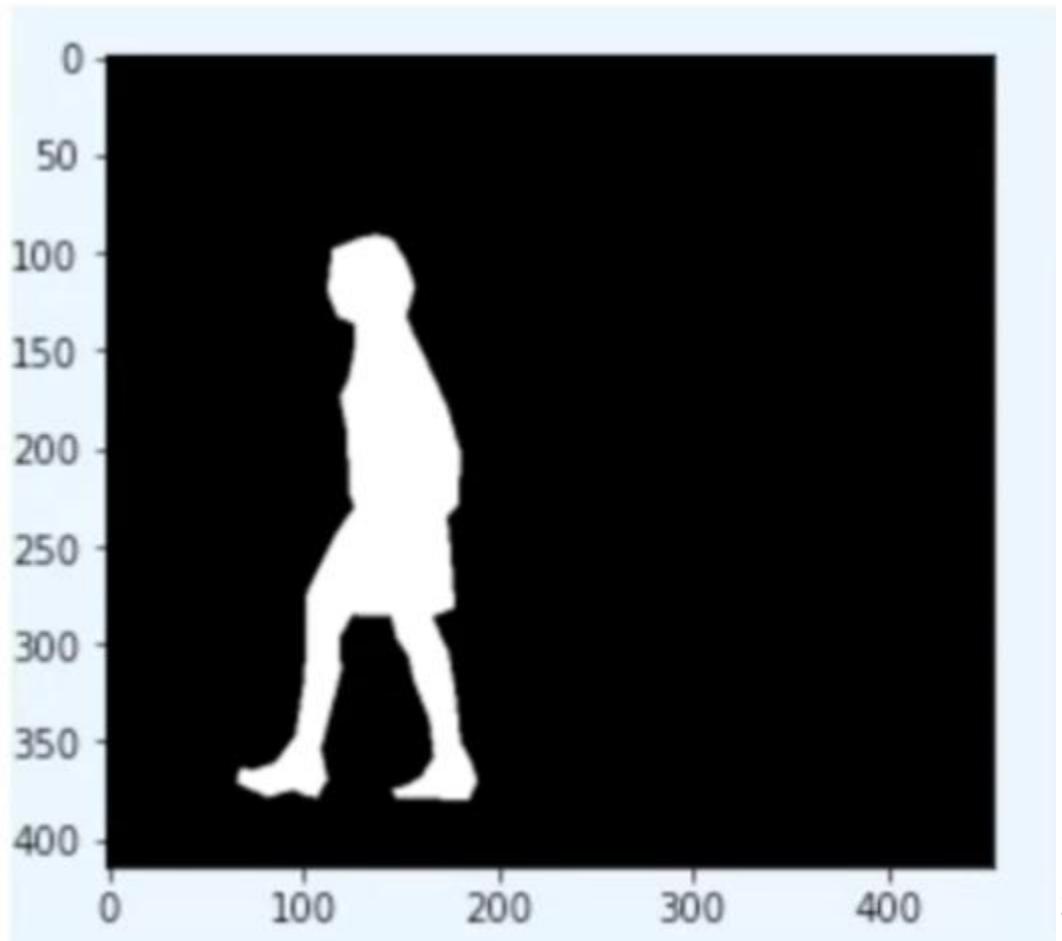
$$\begin{bmatrix} 9 & 3 & .. & 40 \\ \vdots & \vdots & \ddots & 50 \\ 2 & 3 & 34 & \dots 40 \\ 5 & 34 & .. & 24 \\ \vdots & \vdots & .. & 50 \\ 4 & 3 & 34 & .. 40 \\ 5 & 34 & .. & 24 \end{bmatrix}$$



Image Representations

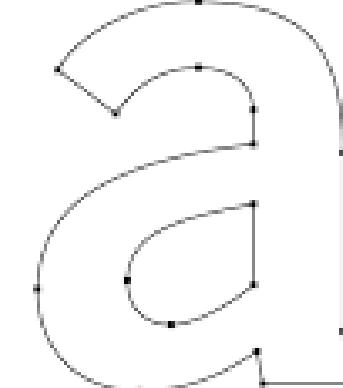
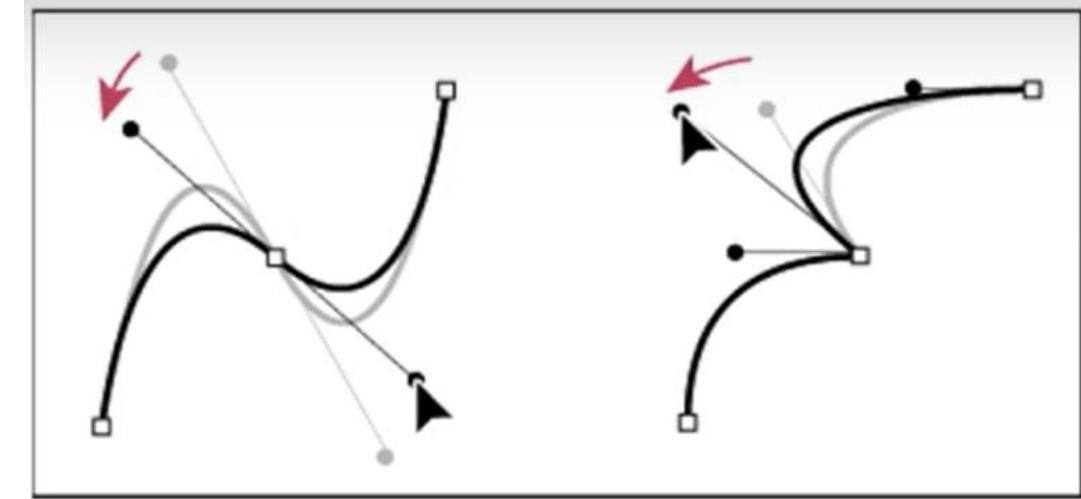


- Black and White (Binary) Image

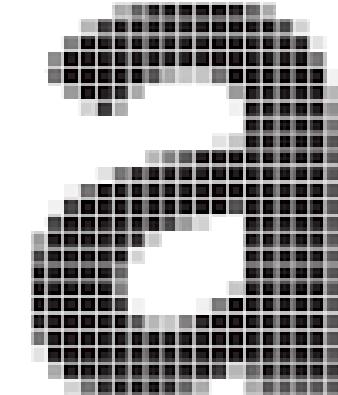




Classification – Raster vs. Vector (Space vs. Quality)



VECTOR



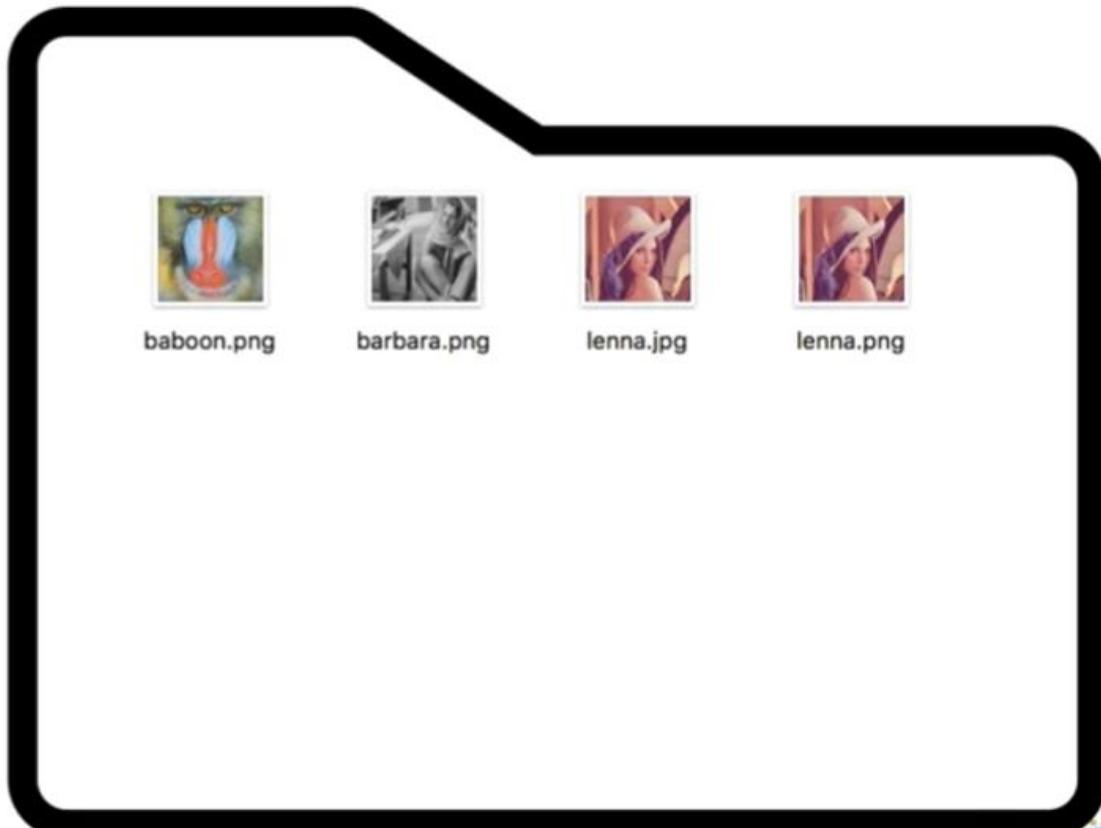
RASTER



Image Formats



- **Image Formats**
 - **JPEG (Raster)**
 - **PNG (Raster)**
 - **GIF (Raster)**
 - **BMP (Raster)**
 - **SVG (Vector)**





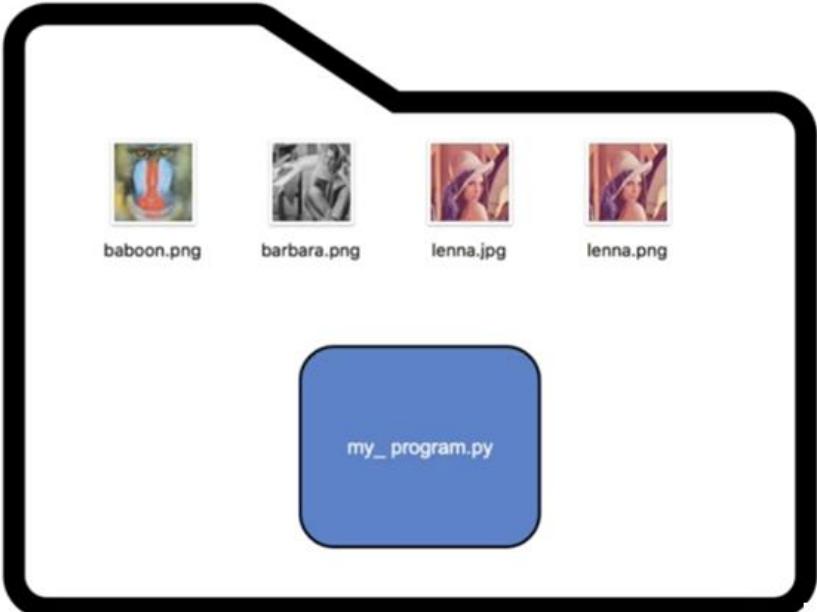
Storing Images



Lossy vs. Lossless (Compression)

Color Range

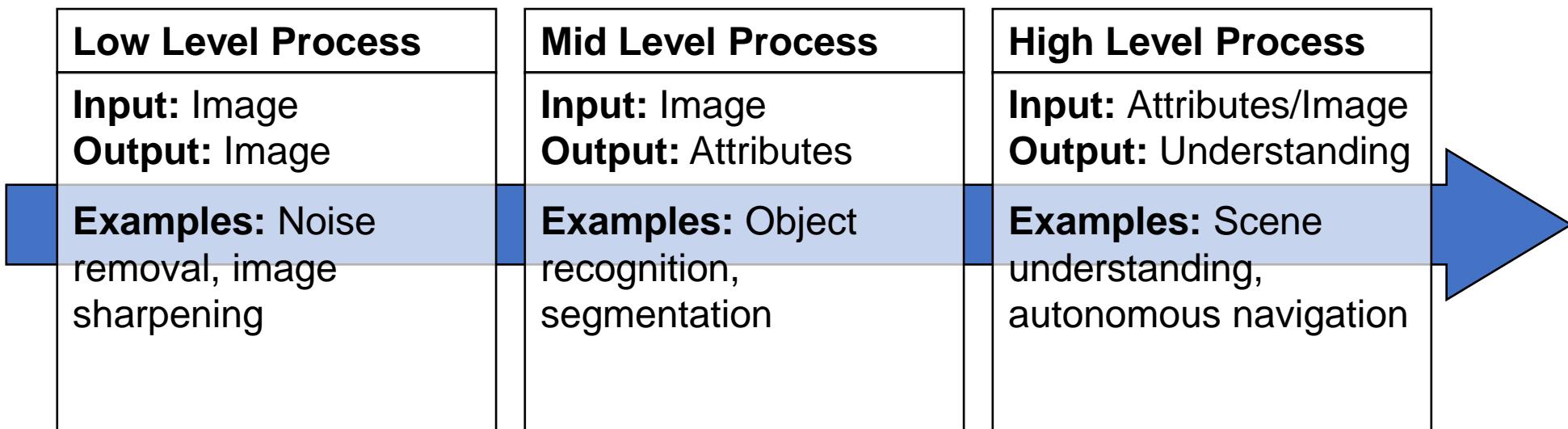
Pixels vs. Vector





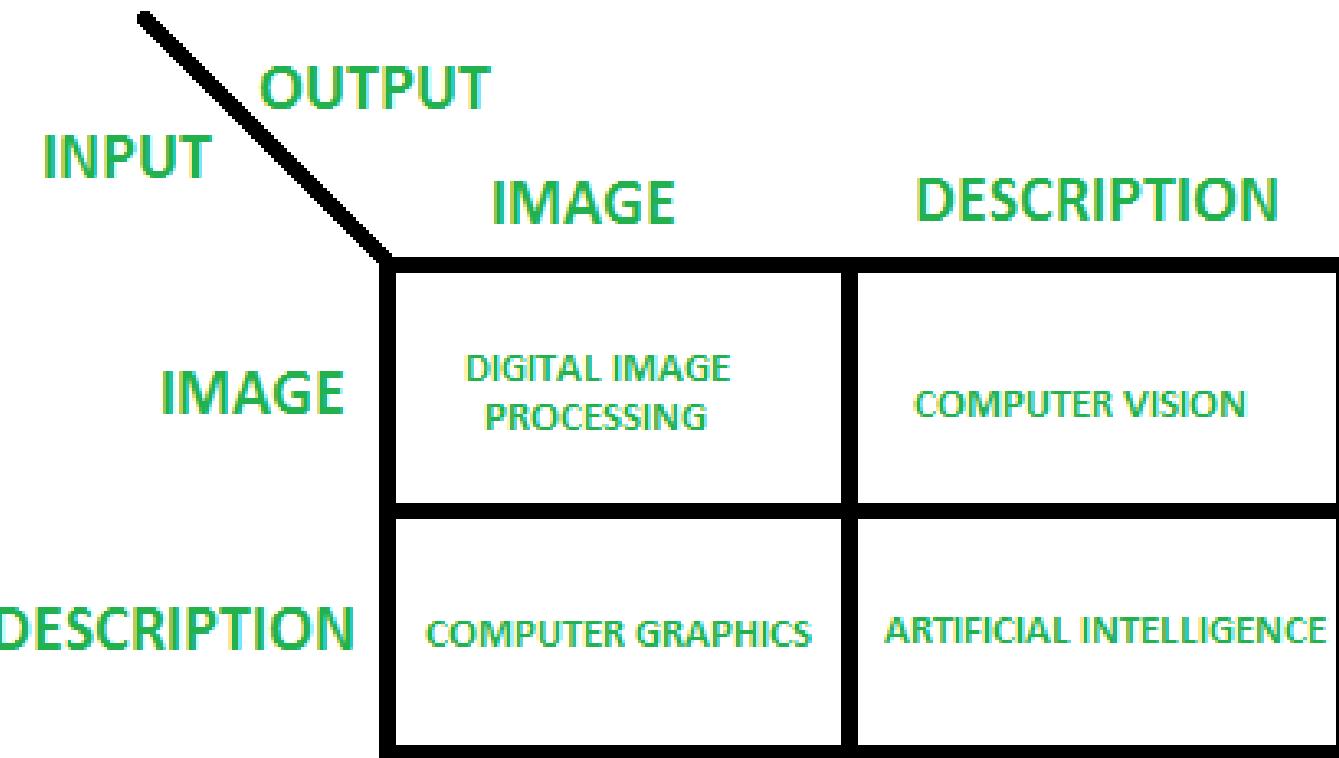
Relation of DIP and CV

- Digital Image Processing is a method to perform some operations on the image in order to get an **enhanced image** or to **extract some useful information from it**.





Relation of DIP and CV





Python Libraries for DIP and CV

- Pillow
- OpenCV



OpenCV

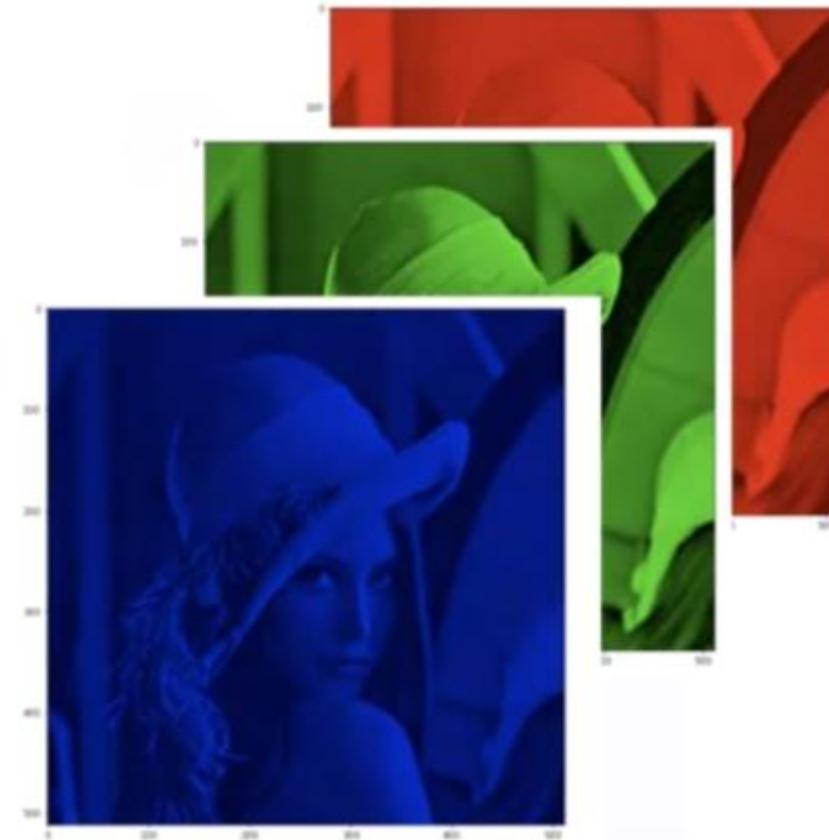
- Open Source Computer Vision
- Supports Python, C++, Java
- Processes images and videos for feature extraction
- Reads the images in BGR format by default

PIL (Python Imaging Library)

- Image processing package exclusively for Python
- A project named Pillow is forked to the original PIL library for its use in Python3.x and above
- Reads the images in RGB format by default



PIL vs OpenCV



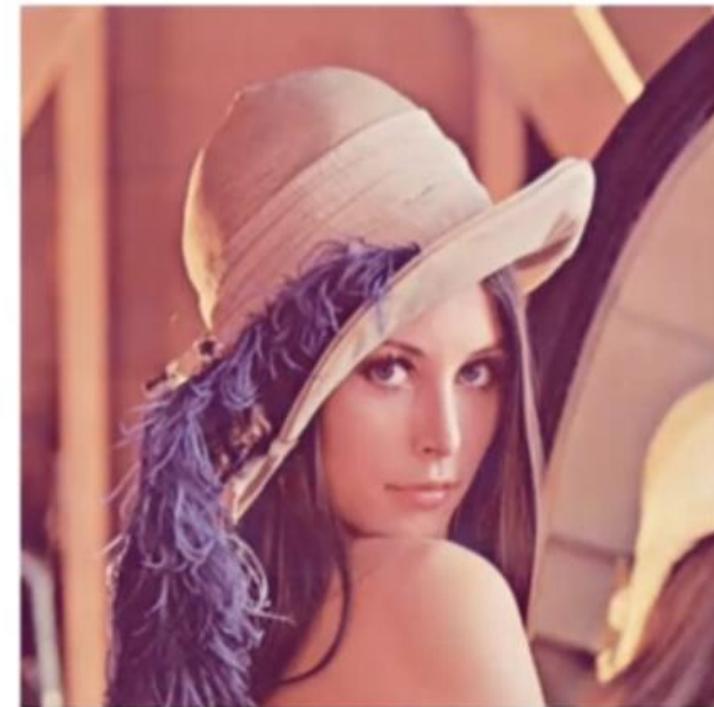


Working with PILLOW (PIL)



```
from PIL import Image  
  
image = Image.open(my_image)  
  
import matplotlib.pyplot as plt  
plt.imshow(image)  
  
image.format:PNG  
  
image.size:(512, 512)  
  
image.mode:RGB
```

PIL.PngImagePlugin.PngImageFile





Working with PILLOW (PIL)



```
from PIL import ImageOps  
  
image_gray = ImageOps.grayscale(image)  
  
image_gray.mode:L  
  
image_gray.save("lenna.jpg")
```



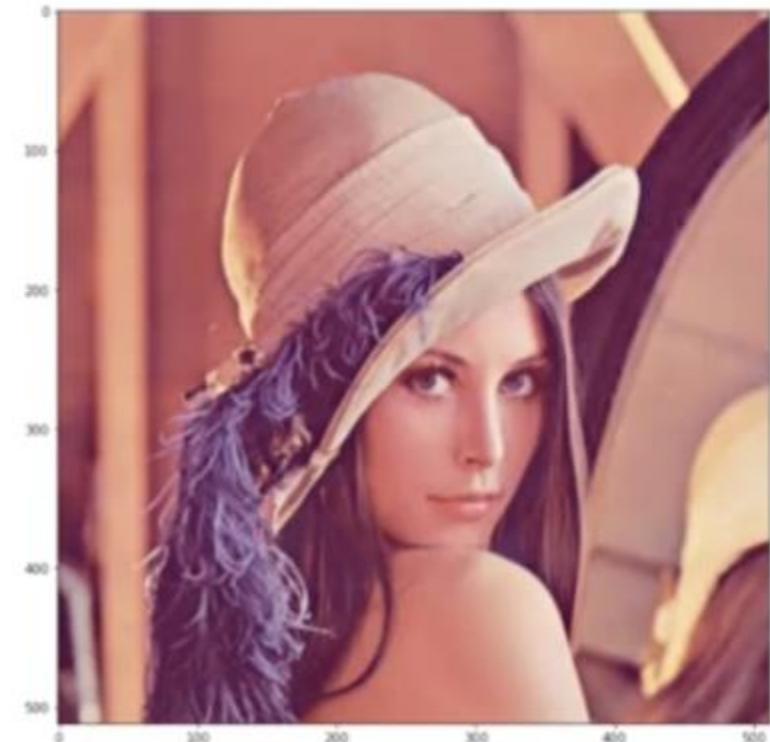


Working with OpenCV



```
new_image = cv2.cvtColor(image, cv2.COLOR_BGR2RGB)
```

```
plt.imshow(new_image )
```





Working with OpenCV



```
image_gray = cv2.cvtColor(image, cv2.COLOR_BGR2GRAY)
```

```
plt.imshow(image_gray )
```

```
cv2.imwrite('lena_gray_cv.jpg', image_gray)
```

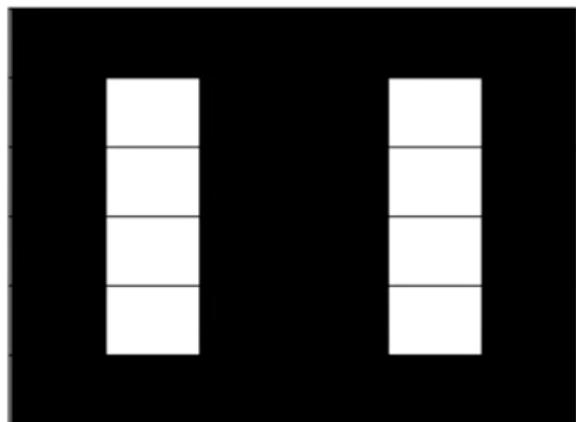




Image Manipulations



I[0,0]	I[0,1]	I[0,2]	I[0,3]	I[0,4]	I[0,5]
I[1,0]	I[1,2]	I[1,2]	I[1,3]	I[1,4]	I[1,5]
I[2,0]	I[2,2]	I[2,2]	I[2,3]	I[2,4]	I[2,5]
I[3,0]	I[3,1]	I[3,2]	I[3,3]	I[3,4]	I[3,5]
I[4,0]	I[4,1]	I[4,2]	I[4,3]	I[4,4]	I[4,5]
I[5,0]	I[5,1]	I[5,2]	I[5,3]	I[5,4]	I[5,5]



I[0,0]	I[1,0]	I[2,0]	I[3,0]	I[4,0]	I[5,0]
I[0,1]	I[1,1]	I[2,1]	I[3,1]	I[4,1]	I[5,1]
I[0,2]	I[1,2]	I[2,2]	I[3,2]	I[4,2]	I[5,2]
I[0,3]	I[1,3]	I[2,3]	I[3,3]	I[4,3]	I[5,3]
I[0,4]	I[1,4]	I[2,4]	I[3,4]	I[4,4]	I[5,4]
I[0,5]	I[1,5]	I[2,5]	I[3,5]	I[4,5]	I[5,5]

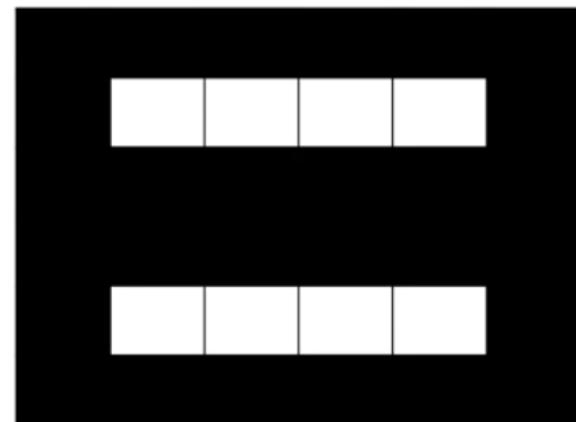




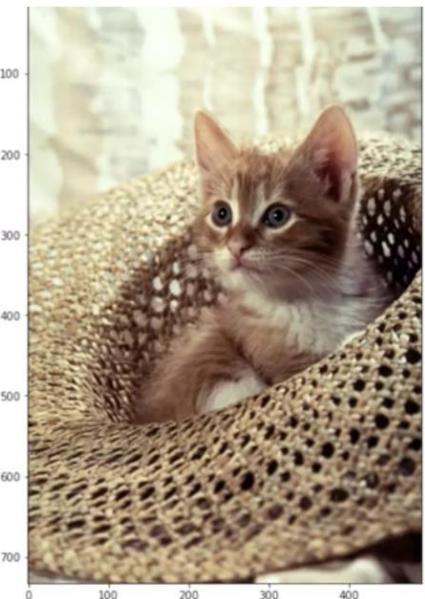
Image Manipulations



```
from PIL import ImageOps
```

```
im_flip = ImageOps.flip(image)
```

```
im_mirror = ImageOps.mirror(image)
```



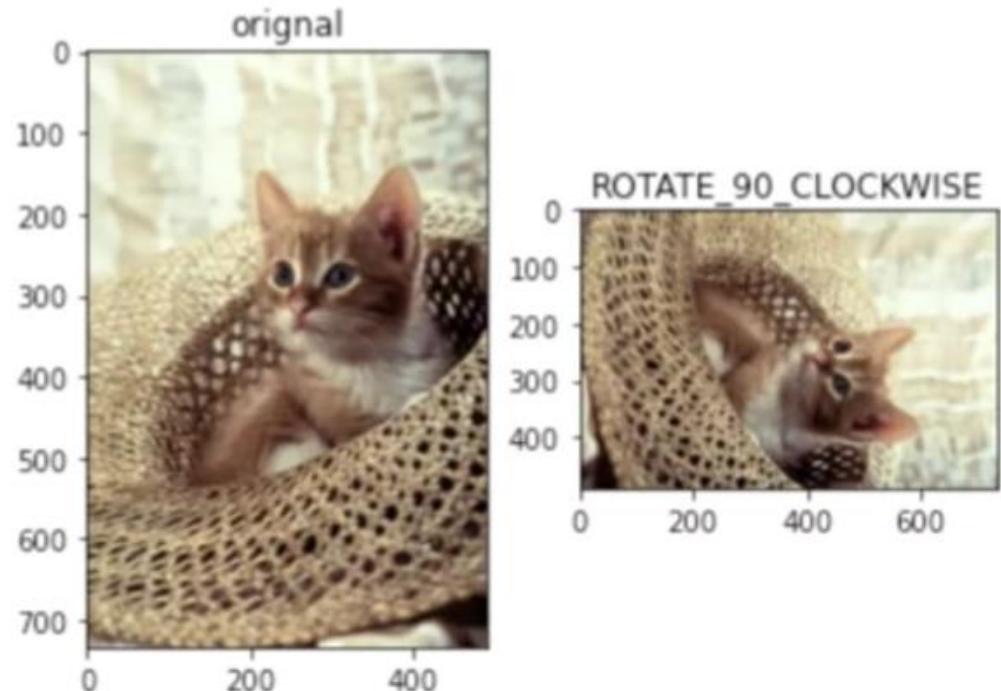
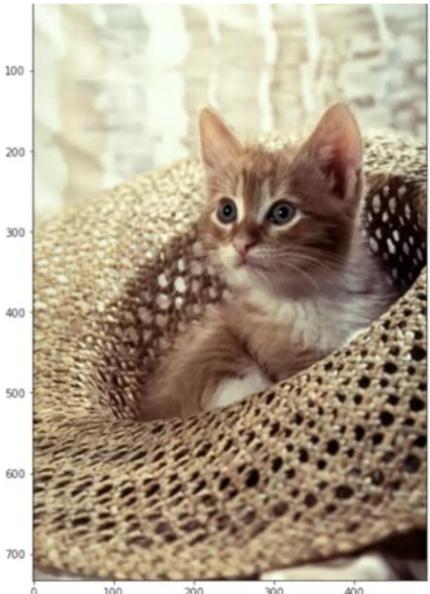
pillow (PIL)



Image Manipulations



```
import cv2  
  
im_flip = cv2.flip(image,0)  
  
im_flip=cv2.rotate(image, cv2.ROTATE_90_CLOCKWISE)
```





Manipulating Images



$I =$

0	I[0,0]	I[0,1]	I[0,2]	I[0,3]	I[0,4]	I[0,5]
1	I[1,0]	I[1, 1]	I[1,2]	I[1,3]	I[1,4]	I[1,5]
2	I[2,0]	I[2, 1]	I[2,2]	I[2,3]	I[2,4]	I[2,5]
3	I[3,0]	I[3,1]	I[3,2]	I[3,3]	I[3,4]	I[3,5]
4	I[4,0]	I[4,1]	I[4,2]	I[4,3]	I[4,4]	I[4,5]
5	I[5,0]	I[5,1]	I[5,2]	I[5,3]	I[5,4]	I[5,5]

0	1	2	3	4	5
---	---	---	---	---	---



Manipulating Images



`I[2:5,:]`

0	I[0,0]	I[0,1]	I[0,2]	I[0,3]	I[0,4]	I[0,5]
1	I[1,0]	I[1,2]	I[1,2]	I[1,3]	I[1,4]	I[1,5]
2	I[2,0]	I[2,2]	I[2,2]	I[2,3]	I[2,4]	I[2,5]
3	I[3,0]	I[3,1]	I[3,2]	I[3,3]	I[3,4]	I[3,5]
4	I[4,0]	I[4,1]	I[4,2]	I[4,3]	I[4,4]	I[4,5]
5	I[5,0]	I[5,1]	I[5,2]	I[5,3]	I[5,4]	I[5,5]

0	1	2	3	4	5
---	---	---	---	---	---



Manipulating Images - Cropping



$I[2:5, 1:3]$

$A = I[2:5, 1:3]$

0	$I[0,0]$	$I[0,1]$	$I[0,2]$	$I[0,3]$	$I[0,4]$	$I[0,5]$
1	$I[1,0]$	$I[1,2]$	$I[1,2]$	$I[1,3]$	$I[1,4]$	$I[1,5]$
2	$I[2,0]$	$I[2,2]$	$I[2,2]$	$I[2,3]$	$I[2,4]$	$I[2,5]$
3	$I[3,0]$	$I[3,1]$	$I[3,2]$	$I[3,3]$	$I[3,4]$	$I[3,5]$
4	$I[4,0]$	$I[4,1]$	$I[4,2]$	$I[4,3]$	$I[4,4]$	$I[4,5]$
5	$I[5,0]$	$I[5,1]$	$I[5,2]$	$I[5,3]$	$I[5,4]$	$I[5,5]$

0	1	2	3	4	5
---	---	---	---	---	---

0	$A[0,0]$	$A[0,1]$
1	$A[1,0]$	$A[1,1]$
2	$A[2,0]$	$A[2,1]$

0	1
---	---

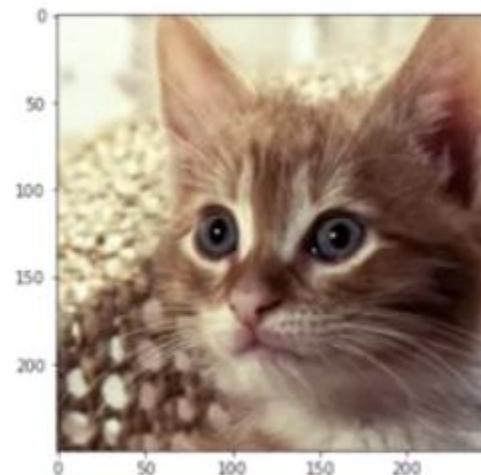


Manipulating Images



```
upper= 150  
lower=400  
crop_top=image[upper: lower,:,:]
```

```
left = 150  
right=400  
crop_horizontal=crop_top[:,left:right,:]
```



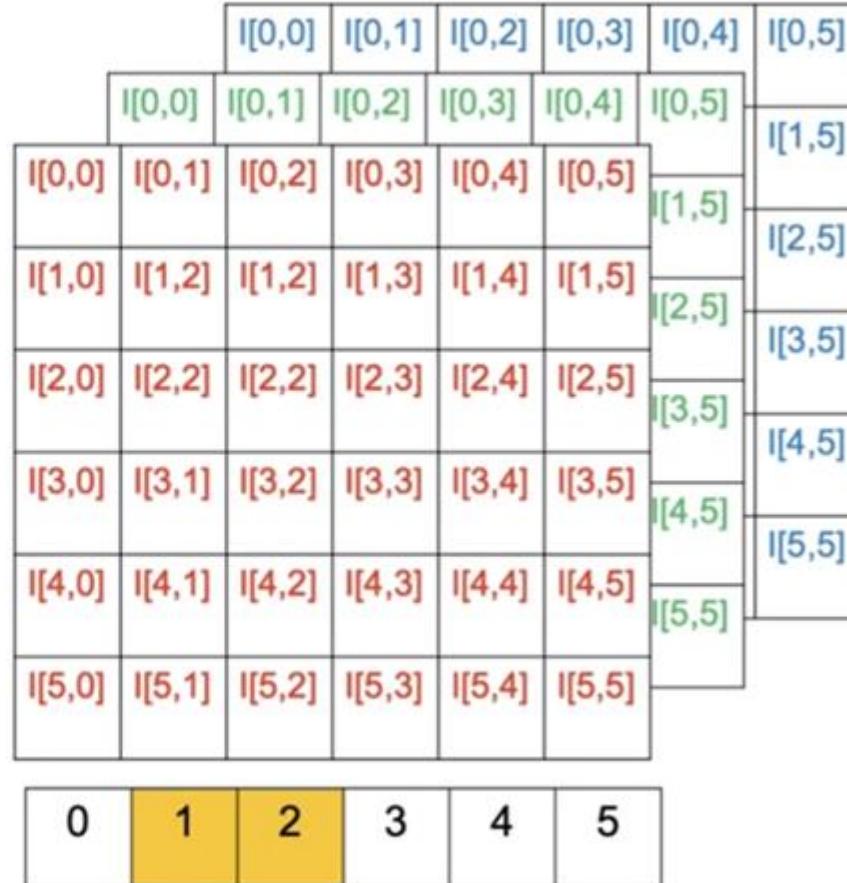


Manipulating Images



$A = I[2:5, 1:3, :]$

0
1
2
3
4
5





Manipulating Images



```
from PIL import Image  
import numpy as np  
  
image = Image.open("cat.png")  
image = np.array(image)  
  
import cv2  
image = cv2.imread("cat.png")
```





Manipulating Images



0	0	0	0	0	0
1	0	0	0	0	0
2	0	0	0	0	0
3	0	0	0	0	0
4	0	0	0	0	0
5	0	0	0	0	0

0	1	2	3	4	5
---	---	---	---	---	---

0	0	0	0	0	0
1	0	0	0	0	0
2	0	255	255	0	0
3	0	255	255	0	0
4	0	255	255	0	0
5	0	0	0	0	0

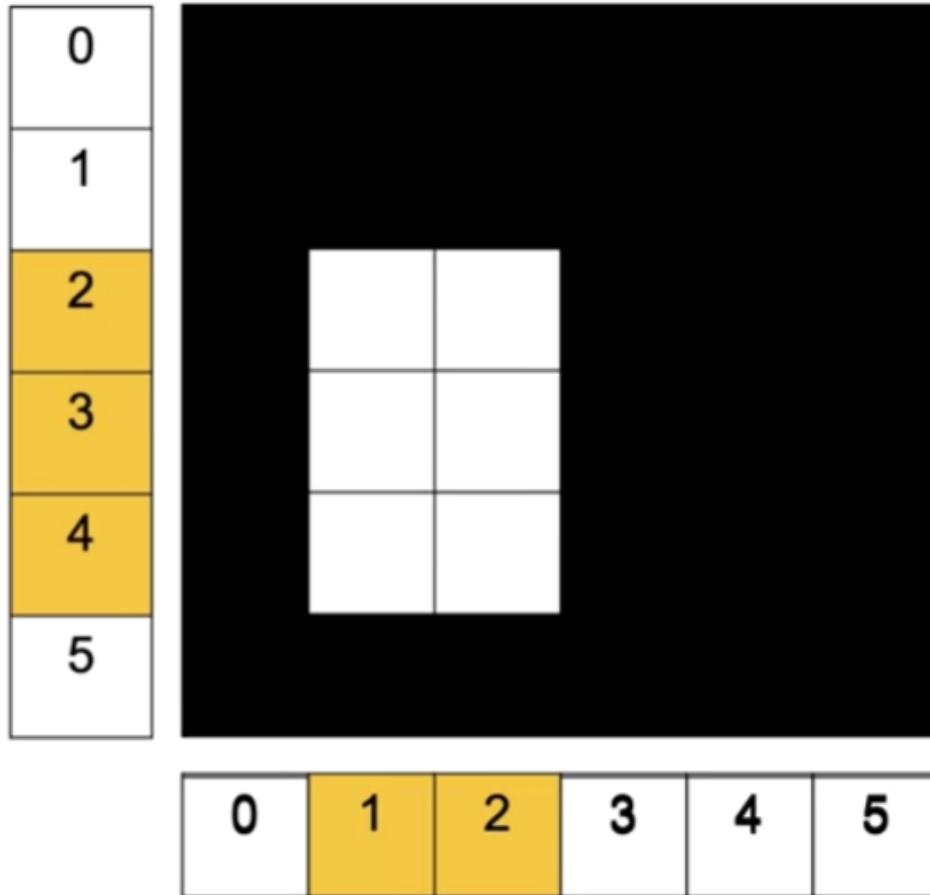
0	1	2	3	4	5
---	---	---	---	---	---



Manipulating Images



$$A = I[2:5, 1:3] = 255$$





Manipulating Images



$$I[4, 1:5] = 255$$

$$I[1, 1] = 255$$

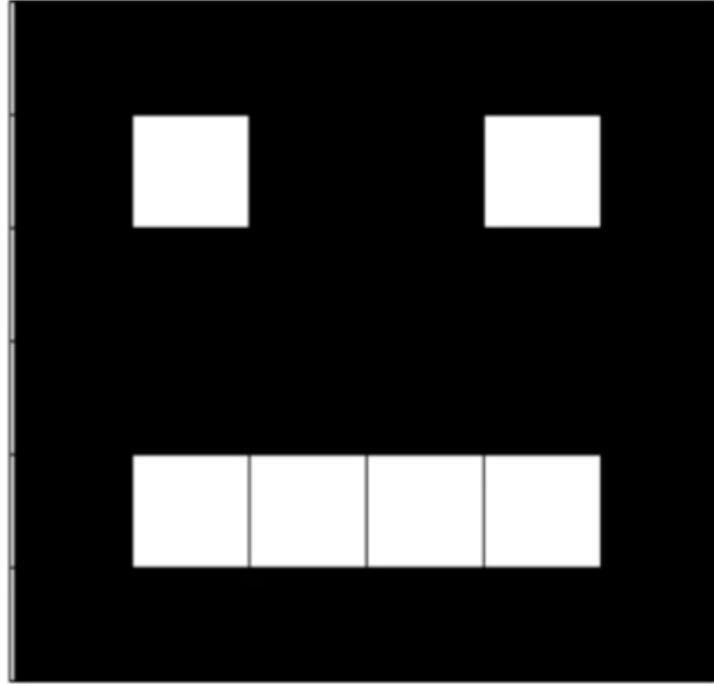
$$I[1, 4] = 255$$

I:

0	0	0	0	0	0	0
1	0	255	0	0	255	0
2	0	0	0	0	0	0
3	0	0	0	0	0	0
4	0	255	255	255	255	0
5	0	0	0	0	0	0
	0	1	2	3	4	5

I:

0
1
2
3
4
5



0	1	2	3	4	5
---	---	---	---	---	---



Manipulating Images

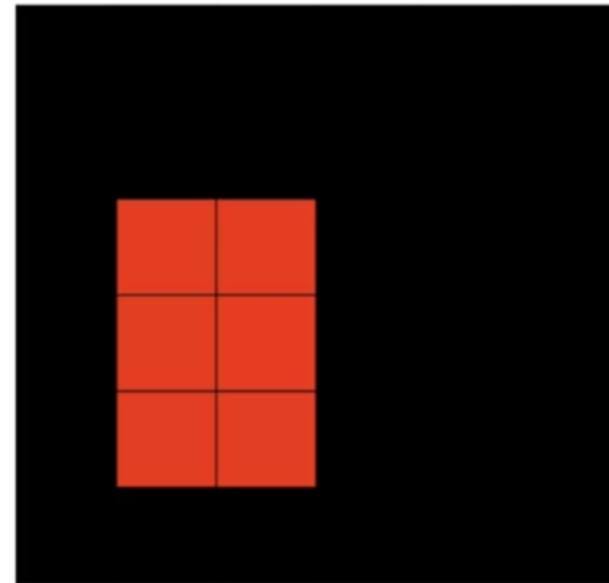


$$A = I[2:5, 1:3, 0] = 255$$

0
1
2
3
4
5

0	0	0	0	0	0	0
0	0	0	0	0	0	0
0	255	255	0	0	0	0
0	255	255	0	0	0	0
0	255	255	0	0	0	0
0	0	0	0	0	0	0

0 1 2 3 4 5

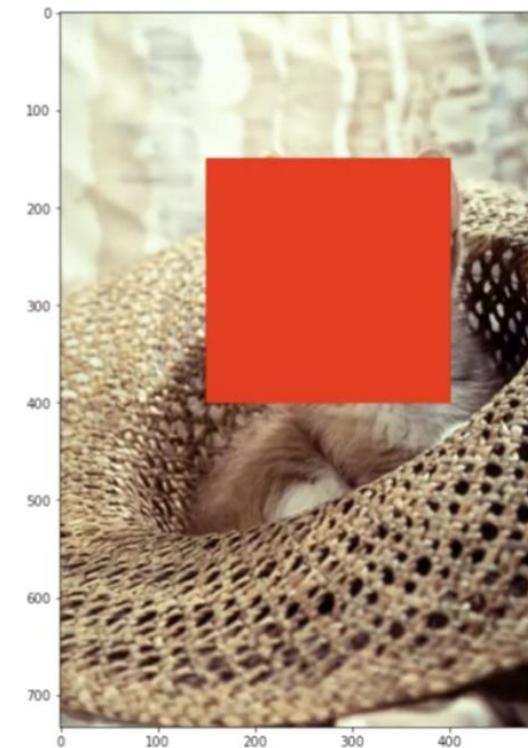
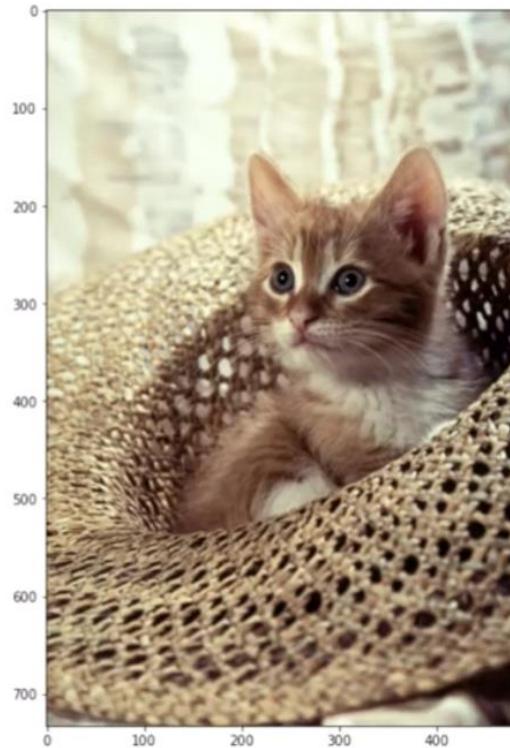




Manipulating Images



```
from PIL import ImageDraw  
  
image_draw=image.copy()  
  
image_fn= ImageDraw.Draw(im=image_draw)  
  
shape = [left, upper, right, lower]  
image_fn.rectangle(xy=shape,fill="red")
```



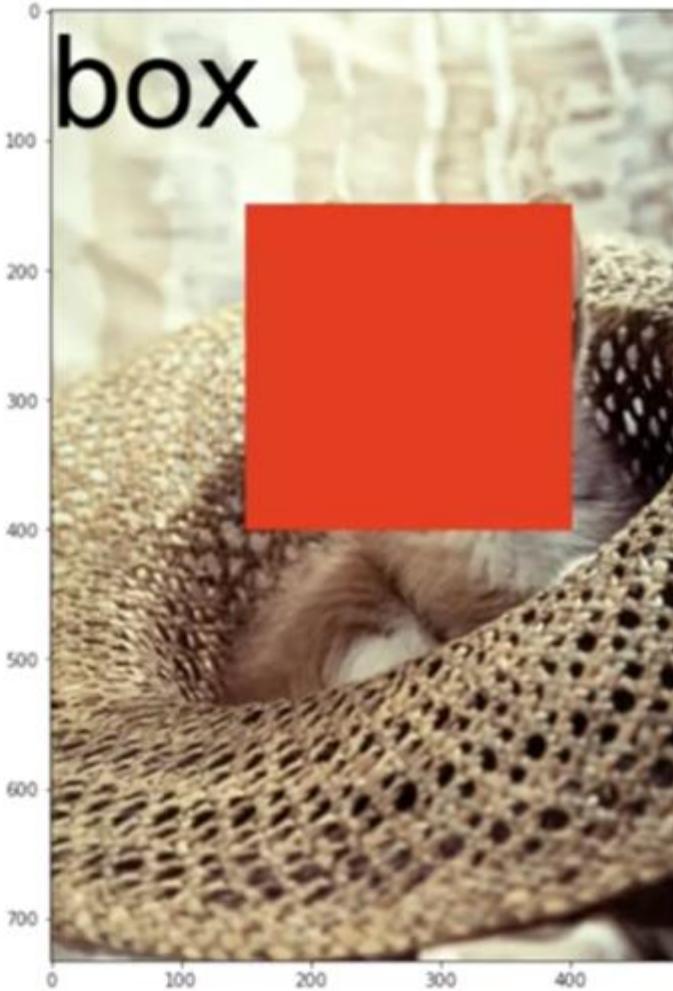


Manipulating Images



```
from PIL import ImageFont  
  
fnt = ImageFont.truetype( '/Library/Fonts/Arial.ttf' , 100)  
  
image_fn.text(xy=(0,0),text="box",font=fnt,fill=(0,0,0))
```

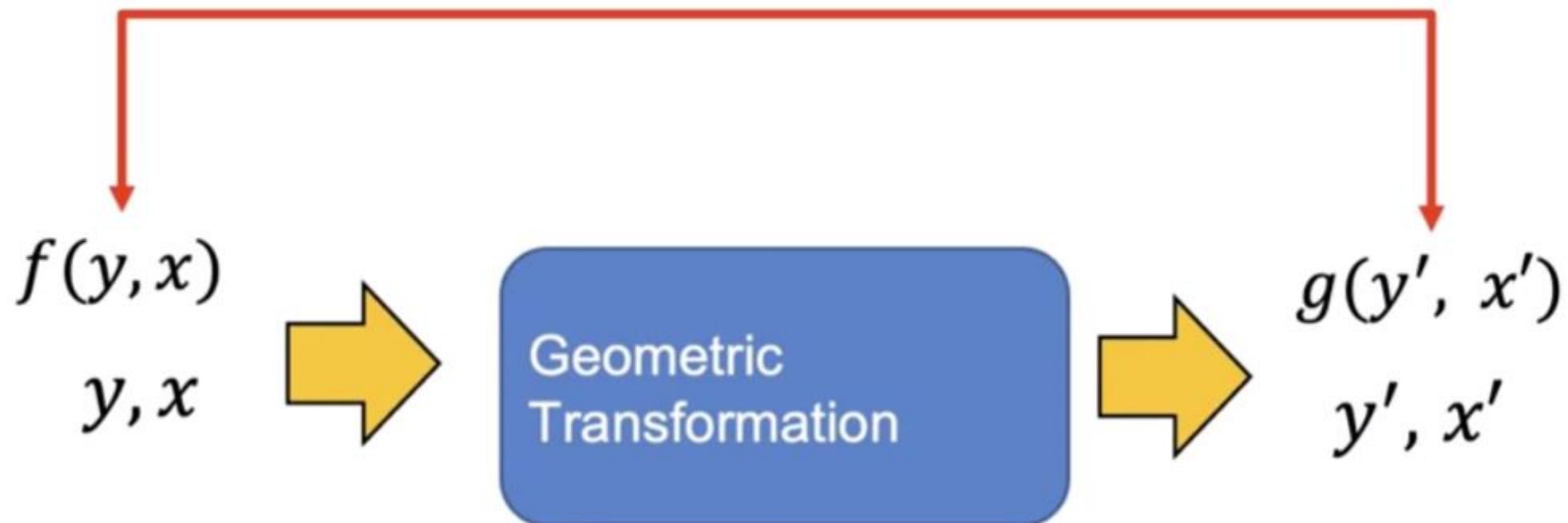
image_draw:





Geometric Transformation

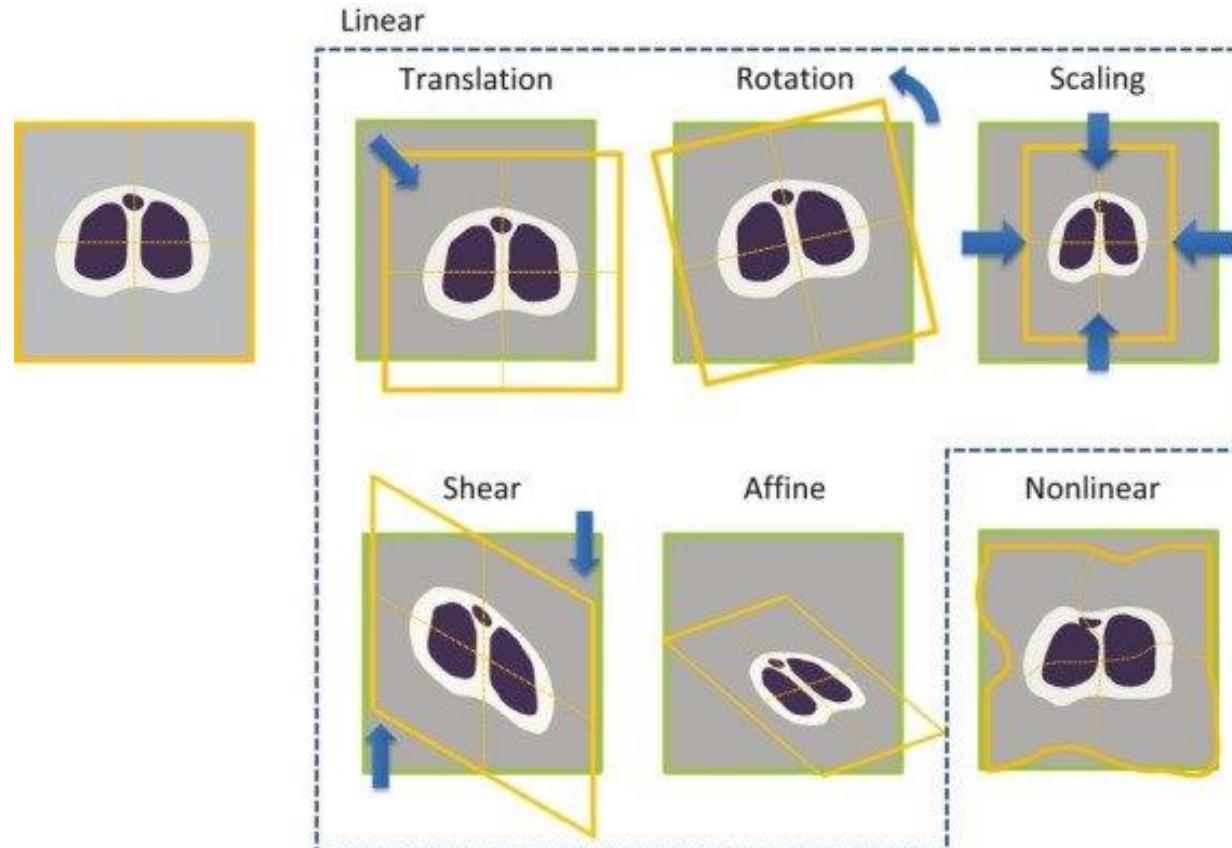
- In a geometric transformation, we change the coordinates of the image
- Also known as Spatial Transformation





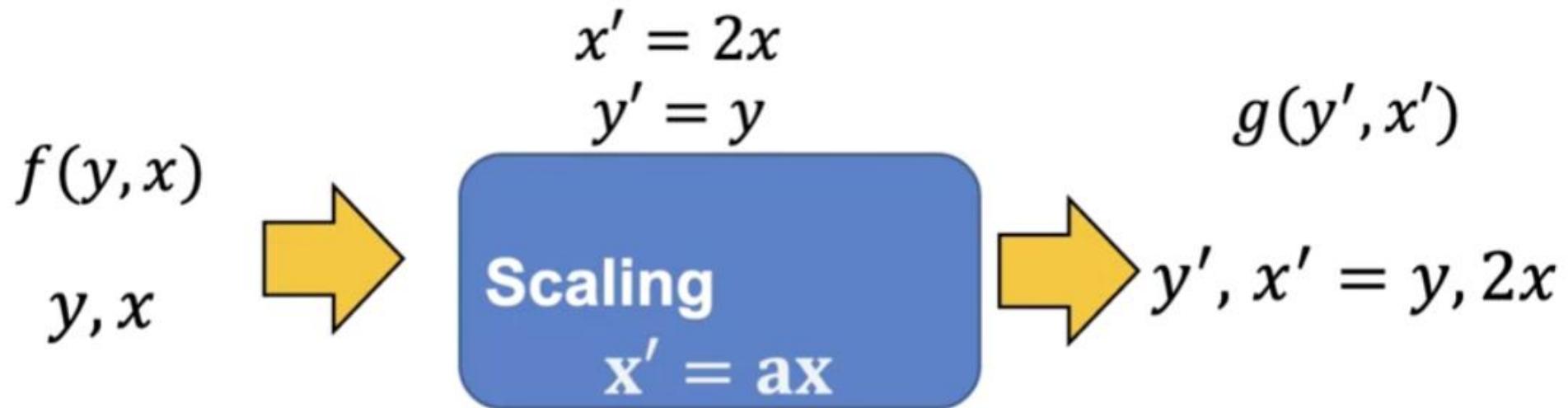
Geometric Operations

- Different types of operations can be performed to do geometric transformation of an image.





Geometric Operations - Scaling



$$g(y, 2x) = f(y, x)$$

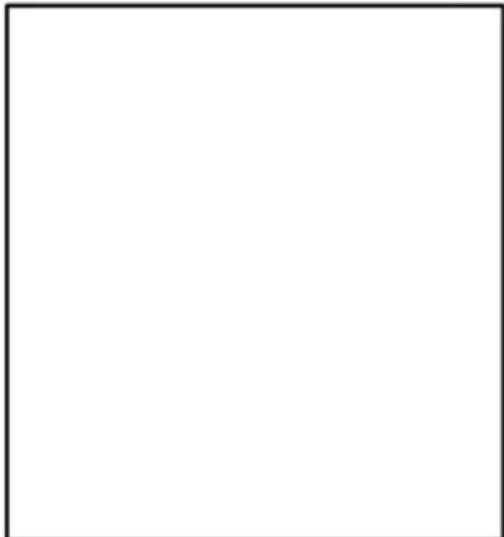


Geometric Operations - Scaling



$$x' = ax \quad x' = 2x$$

$f[0,0]$ $f[0,5]$



$f[5,0]$ $f[5,5]$

$g[0,0]$ $g[0,10]$



$g[5,0]$ $g[5,10]$

$$x' = 2x = 10$$



Geometric Operations - Scaling



f[0,0]	f[0,1]	f[0,2]	f[0,3]	f[0,4]	f[0,5]
f[1,0]	f[1,2]	f[1,2]	f[1,3]	f[1,4]	f[1,5]
f[2,0]	f[2,2]	f[2,2]	f[2,3]	f[2,4]	f[2,5]
f[3,0]	f[3,1]	f[3,2]	f[3,3]	f[3,4]	f[3,5]
f[4,0]	f[4,1]	f[4,2]	f[4,3]	f[4,4]	f[4,5]
f[5,0]	f[5,1]	f[5,2]	f[5,3]	f[5,4]	f[5,5]

g[0,0]	g[0,1]	g[0,2]	g[0,3]	g[0,4]	g[0,5]	g[0,6]	g[0,7]	g[0,8]	g[0,9]	g[0,10]
g[1,0]	g[1,1]	g[1,2]	g[1,3]	g[1,4]	f[1,5]	g[1,6]	g[1,7]	g[1,8]	g[1,9]	g[1,10]
g[2,0]	g[2,1]	g[2,2]	g[2,3]	g[2,4]	g[2,5]	g[2,6]	g[2,7]	g[2,8]	g[2,9]	g[2,10]
g[3,0]	g[3,1]	g[3,2]	g[3,3]	g[3,4]	g[3,5]	g[3,6]	g[3,7]	g[3,8]	g[3,9]	g[3,10]
g[4,0]	g[4,1]	g[4,2]	g[4,3]	g[4,4]	g[4,5]	g[4,6]	g[4,7]	g[4,8]	g[4,9]	g[4,10]
g[5,0]	g[5,1]	g[5,2]	g[5,3]	g[5,4]	g[5,5]	g[5,6]	g[5,7]	g[5,8]	g[5,9]	g[5,10]



Geometric Operations - Scaling

- Interpolation – to determine the value of the unknown pixels based on the neighboring pixel values

f[0,0]	f[0,1]	f[0,2]	f[0,3]	f[0,4]	f[0,5]
f[1,0]	f[1,2]	f[1,2]	f[1,3]	f[1,4]	f[1,5]
f[2,0]	f[2,2]	f[2,2]	f[2,3]	f[2,4]	f[2,5]
f[3,0]	f[3,1]	f[3,2]	f[3,3]	f[3,4]	f[3,5]
f[4,0]	f[4,1]	f[4,2]	f[4,3]	f[4,4]	f[4,5]
f[5,0]	f[5,1]	f[5,2]	f[5,3]	f[5,4]	f[5,5]

g[0,0]	g[0,0]	g[0,2]	g[0,2]	g[0,4]	g[0,4]	g[0,6]	g[0,6]	g[0,8]	g[0,8]	g[0,10]
g[1,0]	g[1,0]	g[1,2]	g[1,2]	g[1,4]	g[1,4]	g[1,6]	g[1,6]	g[1,8]	g[1,8]	g[1,10]
g[2,0]	g[2,0]	g[2,2]	g[2,2]	g[2,4]	g[2,4]	g[2,6]	g[2,6]	g[2,8]	g[2,8]	g[2,10]
g[3,0]	g[3,0]	g[3,2]	g[3,2]	g[3,4]	g[3,4]	g[3,6]	g[3,6]	g[3,8]	g[3,8]	g[3,10]
g[4,0]	g[4,0]	g[4,2]	g[4,2]	g[4,4]	g[4,4]	g[4,6]	g[4,6]	g[4,8]	g[4,8]	g[4,10]
g[5,0]	g[5,0]	g[5,2]	g[5,2]	g[5,4]	g[5,4]	g[5,6]	g[5,6]	g[5,8]	g[5,8]	g[5,10]



Geometric Operations - Scaling



```
from PIL import Image  
  
image = Image.open("lenna.png")  
  
width= 512  
height=512  
new_width=2*width  
new_height=height  
  
new_image=image.resize((new_width,new_height))
```





Geometric Operations - Translation

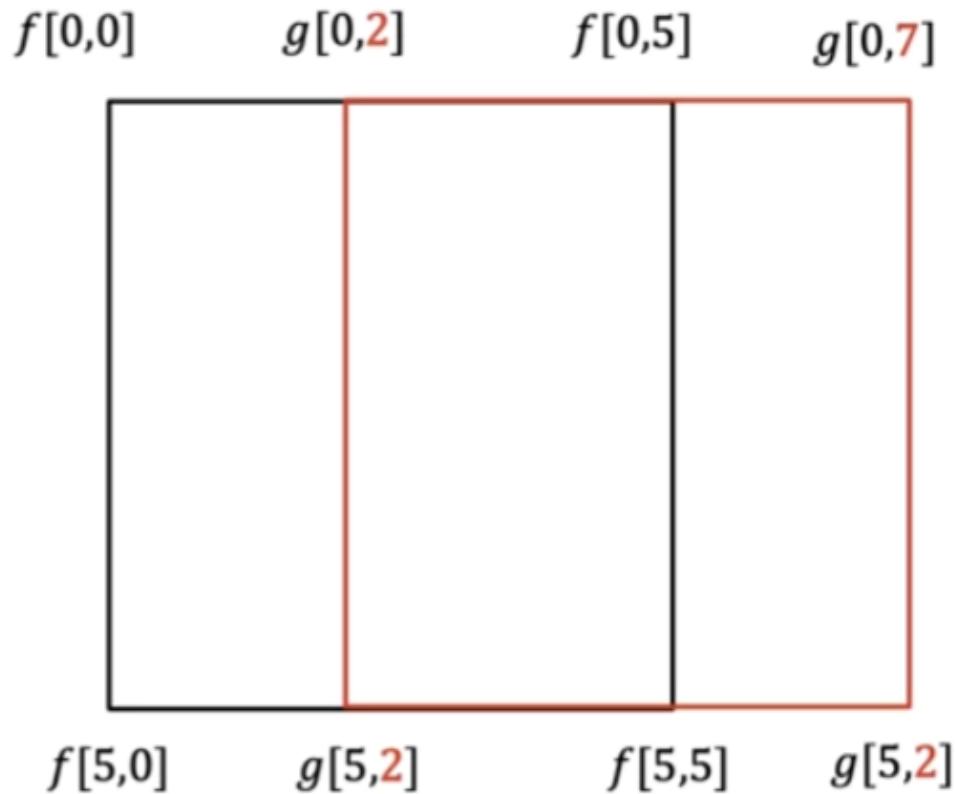


$$x' = x + t_x$$

$$x' = x + 2$$

$$x' = 0 + 2 = 2$$

$$x' = 5 + 2 = 7$$





Geometric Operations - Translation



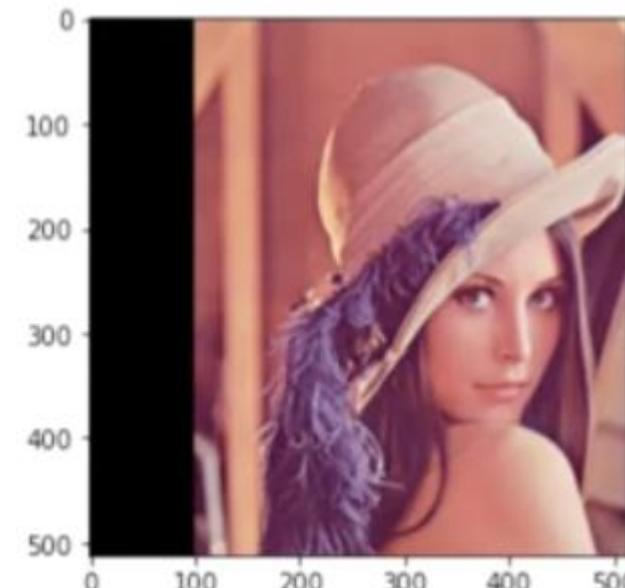
```
rows,cols,_=image.shape
```

```
tx=100
```

```
ty=0
```

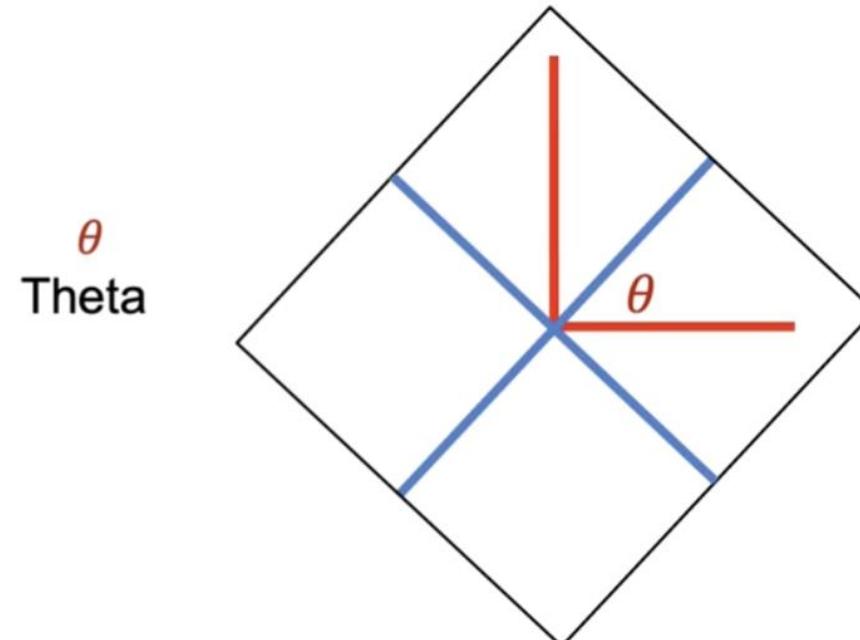
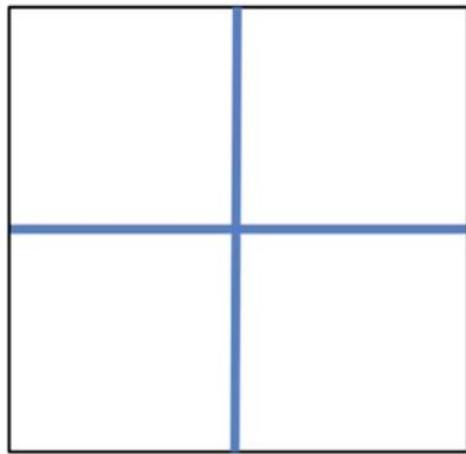
```
M = np.float32([[1,0,tx],[0,1,ty]])
```

```
new_image = cv2.warpAffine(image,M,(cols,rows))
```





Geometric Operations - Rotation



$$\begin{bmatrix} r\cos(\theta) & r\sin(\theta) & \text{stuff} \\ -r\sin(\theta) & r\cos(\theta) & \text{stuff} \end{bmatrix}$$



Geometric Operations - Rotation



```
image = Image.open("lenna.png")
```

```
theta=45
```

```
new_image=image.rotate(theta)
```





Some Other Geometric Operations



- Rigid Transformation – Translation + Rotation
- Similarity Transformation – Translation + Rotation + Scaling
- Affine - Translation + Rotation + Scaling + Shearing
- Achieved by changing the factors in the transformation matrix,
see this video for animation:
https://www.youtube.com/watch?v=AheaTd_I5Is



Geometric Transformation Matrix



$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & t_x \\ c & d & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

where:

- (x, y) : Original coordinates of a point in the image.
- (x', y') : New coordinates after transformation.
- a, b, c, d : Elements that control rotation, scaling, and shearing.
- t_x, t_y : Elements that control translation in the x and y directions, respectively.



Geometric Transformation Matrix



Translation

$$\begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & sh_x & 0 \\ sh_y & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Shearing

Scaling

$$\begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Rotation



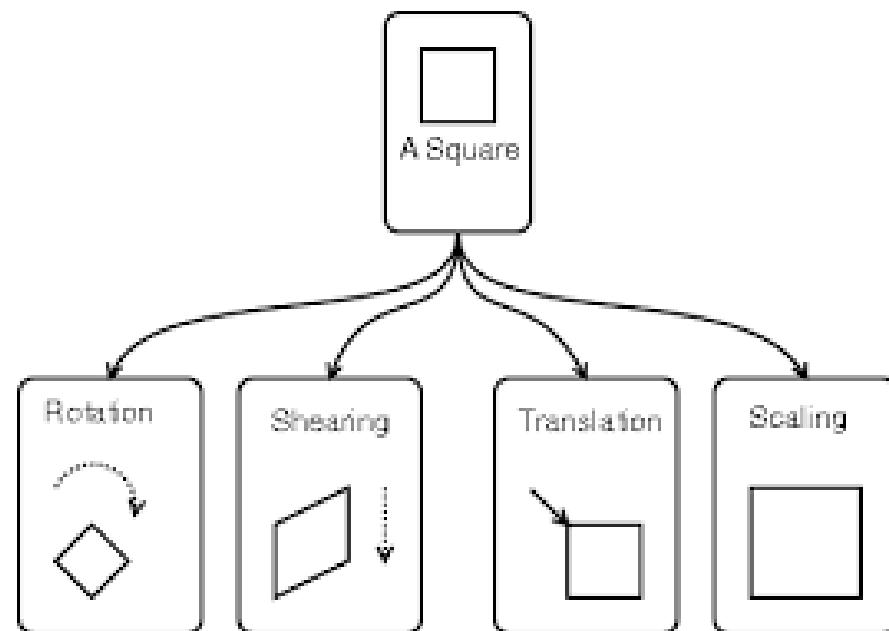
Geometric Operations - Affine

- Affine Transformations

$$\begin{aligned}x' &= ax + t_x \\y' &= dy + t_y\end{aligned}$$

$$\begin{bmatrix}x' \\ y'\end{bmatrix} = \begin{bmatrix}a & 0 \\ 0 & d\end{bmatrix} \begin{bmatrix}x \\ y\end{bmatrix} + \begin{bmatrix}t_x \\ t_y\end{bmatrix}$$

$$\begin{bmatrix}a & c & t_x \\ d & b & t_y\end{bmatrix}$$





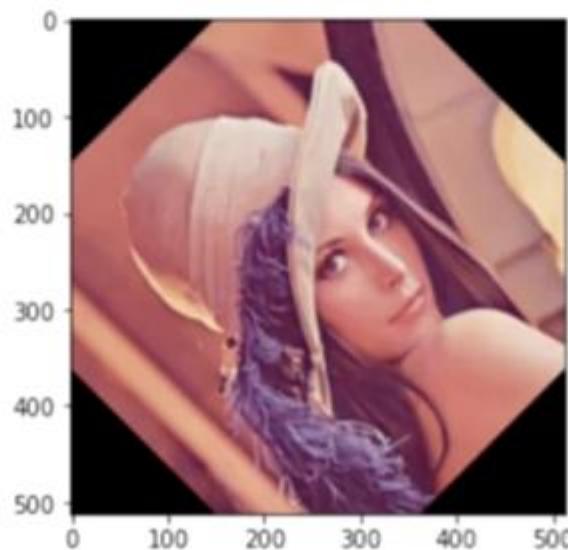
Geometric Operations - Affine



theta=45.0

```
M = cv2.getRotationMatrix2D(center=(cols//2-1,rows//2-1),angle=theta,scale=1)
```

```
new_image = cv2.warpAffine(image,M,(cols,rows))
```





Geometric Transformation Matrix - Affine



Combining rotation, scaling, shearing, and translation gives the general affine transformation:

$$\begin{bmatrix} a & b & t_x \\ c & d & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

where the elements a , b , c , and d are calculated based on the specific transformations desired:

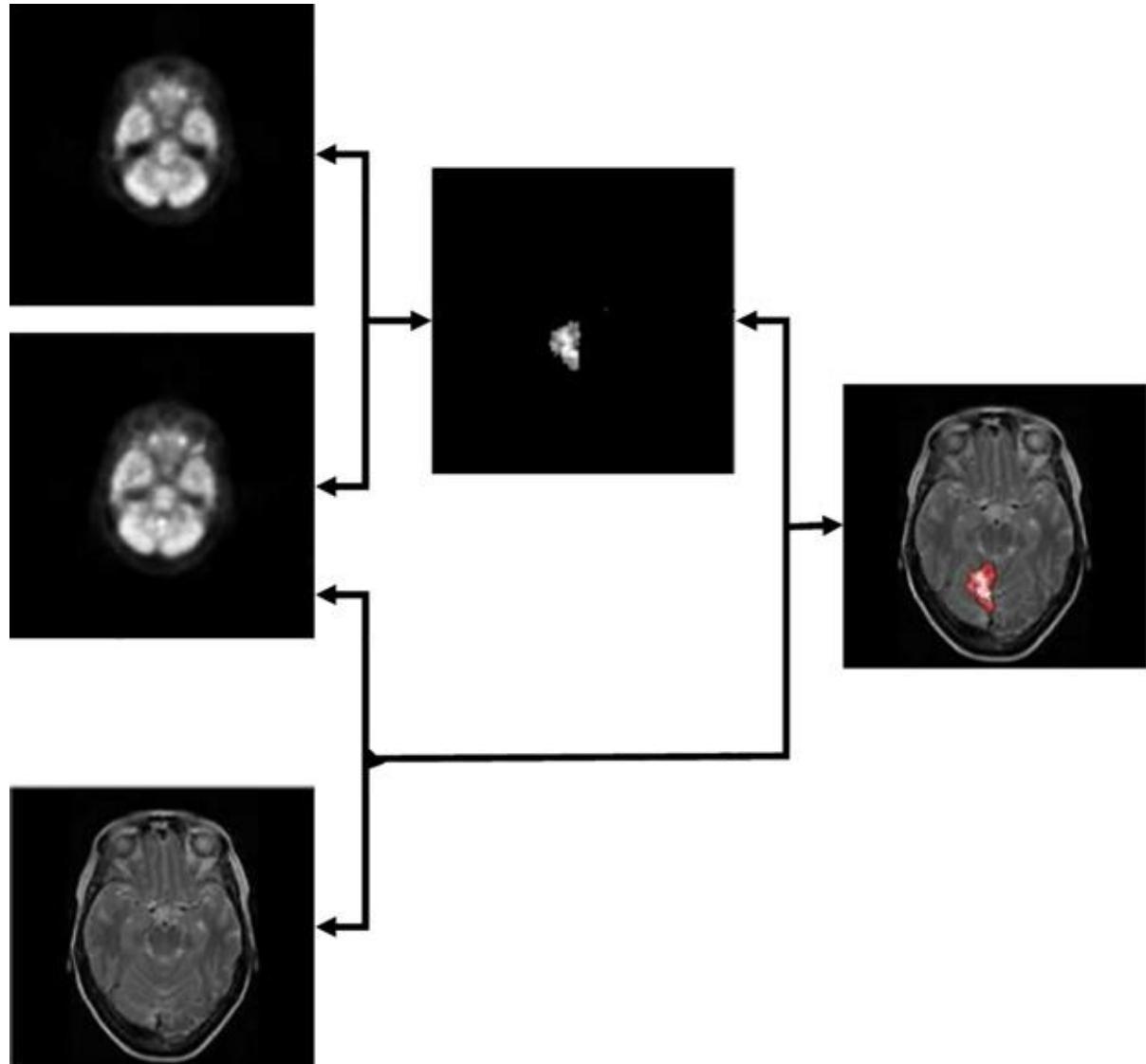
- $a = s_x \cdot \cos(\theta) - sh_y \cdot \sin(\theta)$
- $b = s_x \cdot \sin(\theta) + sh_y \cdot \cos(\theta)$
- $c = -sh_x \cdot \cos(\theta) + s_y \cdot \sin(\theta)$
- $d = sh_x \cdot \sin(\theta) + s_y \cdot \cos(\theta)$



Why Geometrics Transformation?



- Alignment of images taken at different time stamps, from different angles and from different devices for better understanding of the domain.
- Example: Brain Image Registration taken from different devices CT, XRAY, MRI etc





Acknowledgements



Some of the content of these slides is taken from:

- www.coursera.com
- Digital Image Processing by Gonzalez