

In[*]:= Steps@Int[(Sec[x]^2 + Sec[x]^2 * Tan[x]) / ((2 - Tan[x]) * Sqrt[1 + Tan[x]^3]), x]

$$\triangleright \int F(\tan(a + b x)) \, dx \rightarrow \frac{\text{Subst}\left(\int \frac{F(x)}{1+x^2} \, dx, x, \tan(a + b x)\right)}{b}$$

$$\text{Subst}\left[\text{Int}\left[\frac{1+x}{(2-x)\sqrt{1+x^3}}, x\right], x, \tan[x]\right]$$

$$\triangleright \int \frac{e + f x}{(c + d x) \sqrt{a + b x^3}} \, dx \rightarrow - \frac{(2 e) \text{Subst}\left(\int \frac{1}{9 - a x^2} \, dx, x, \frac{\left(1 + \frac{f x}{e}\right)^2}{\sqrt{a + b x^3}}\right)}{d}$$

$$\text{Dist}\left[2, \text{Subst}\left[\text{Int}\left[\frac{1}{9 - x^2}, x\right], x, \frac{(1 + \tan[x])^2}{\sqrt{1 + \tan[x]^3}}\right], x\right]$$

$$\triangleright \int \frac{1}{a + b x^2} \, dx \rightarrow \frac{\tanh^{-1}\left(\frac{\sqrt{-b} x}{\sqrt{a}}\right)}{\sqrt{a} \sqrt{-b}}$$

$$\frac{2}{3} \text{ArcTanh}\left[\frac{(1 + \tan[x])^2}{3 \sqrt{1 + \tan[x]^3}}\right]$$

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$$\text{Out[*]} = \frac{2}{3} \text{ArcTanh}\left[\frac{(1 + \tan[x])^2}{3 \sqrt{1 + \tan[x]^3}}\right]$$