# 1 Algebraic Functions

## 1.1 Linear

- Rule 1.1.1:  $Int[(a+b x)^m, x] \to Int111[a, b, m, x]$
- Rule 1.1.2: Int[(a+b x)^m (c+d x)^n, x]  $\rightarrow$  Int112[a, b, m, c, d, n, x]
- Rule 1.1.3:  $Int[(a+b x)^m (c+d x)^n (e+f x)^p, x] \rightarrow Int113[a, b, m, c, d, n, e, f, p, x]$
- Rule 1.1.4:  $Int[(a+b \ x)^m (c+d \ x)^n (e+f \ x)^p (g+h \ x)^q, x] \rightarrow Int 114[a, b, m, c, d, n, e, f, p, g, h, q, x]$
- Rule 1.1.5:  $Int[P[x] (a+b x)^m, x] \rightarrow Int115[P[x], a, b, m, x]$
- Rule 1.1.6: Int[P[x] (a+b x)^m (c+d x)^n, x]  $\rightarrow$  Int116[P[x], a, b, m, c, d, n, x]
- Rule 1.1.7: Int[P[x]  $(a+b x)^m (c+d x)^n (e+f x)^p, x] \rightarrow Int[17][P[x], a, b, m, c, d, n, e, f, p, x]$
- Rule 1.1.8: Int[P[x]  $(a+b x)^m (c+d x)^n (e+f x)^p (g+h x)^q, x] \rightarrow Int118[P[x], a, b, m, c, d, n, e, f, p, g, h, q, x]$

### 1.2 Quadratic

- Rule 1.2.1: Int[(a+b x+c  $x^2$ )^p, x]  $\rightarrow$  Int121[a, b, c, p, x]
- Rule 1.2.2:  $Int[(d+e x)^m (a+b x+c x^2)^p, x] \rightarrow Int[(d+e x)^m (a+b x+c x^2)^p, x]$
- Rule 1.2.3:  $Int[(d+e x)^m (f+g x)^n (a+b x+c x^2)^p, x] \rightarrow Int[23[d, e, m, f, g, n, a, b, c, p, x]$
- Rule 1.2.4:  $Int[(a+b x+c x^2)^p (d+e x+f x^2)^q, x] \rightarrow Int[24[a, b, c, p, d, e, f, q, x]]$
- Rule 1.2.5:  $Int[(g+h x)^m (a+b x+c x^2)^p (d+e x+f x^2)^q, x] \rightarrow Int[25[g, h, m, a, b, c, p, d, e, f, q, x]]$
- Rule 1.2.6: Int[P[x]  $(a+b x+c x^2)^p$ , x]  $\rightarrow$  Int126[P[x], a, b, c, p, x]
- Rule 1.2.7: Int[P[x]  $(d+e x)^m (a+b x+c x^2)^p, x] \rightarrow Int127[P[x], d, e, m, a, b, c, p, x]$
- Rule 1.2.8: Int[P[x]  $(d+e x)^m (f+g x)^n (a+b x+c x^2)^p, x] \rightarrow Int128[P[x], d, e, m, f, g, n, a, b, c, p, x]$
- Rule 1.2.9: Int[P[x] (a+b x+c  $x^2$ )^p (d+e x+f  $x^2$ )^q, x]  $\rightarrow$  Int129[P[x], a, b, c, p, d, e, f, q, x]
- Rule 1.2.10: Int[P[x]  $(g+h x)^m (a+b x+c x^2)^p (d+e x+f x^2)^q, x] \rightarrow Int1210[P[x], g, h, m, a, b, c, p, d, e, f, q, x]$

## 1.3 Cubic

- Rule 1.3.1: Int[(a+b x+c  $x^2+d x^3$ )^p, x]  $\rightarrow$  Int131[a, b, c, d, p, x]
- Rule 1.3.2:  $Int[(e+f x)^m (a+b x+c x^2+d x^3)^p, x] \rightarrow Int132[e, f, m, a, b, c, d, p, x]$
- Rule 1.3.3: Int[(e+f x)^m (g+h x)^n (a+b x+c x^2+d x^3)^p, x]  $\rightarrow$  Int133[e, f, m, g, h, n, a, b, c, d, p, x]

## 1.4 Quartic

Rule 1.4.1:  $Int[(a+b \ x+c \ x^2+d \ x^3+e \ x^4)^p, x] \rightarrow Int141[a, b, c, d, e, p, x]$ 

- Rule 1.4.2: Int[(f+g x)^m (a+b x+c x^2+d x^3+e x^4)^p, x]  $\rightarrow$  Int142[f, g, m, a, b, c, d, e, p, x]
- Rule 1.4.3: Int[(f+g x)^m (h+i x)^n (a+b x+c x^2+d x^3+e x^4)^p, x]  $\rightarrow$  Int143[f, g, m, h, i, n, a, b, c, d, e, p, x]

### 1.5 Binomial

- Rule 1.5.1:  $Int[(a+b x^n)^p, x], x] \rightarrow Int151[a, b, p, n, x]$
- Rule 1.5.2:  $Int[(c x)^m (a+b x^n)^p, x] \to Int[52[c, m, a, b, p, n, x]]$
- Rule 1.5.3: Int[ $(a+b x^n)^p (c+d x^n)^q, x$ ]  $\rightarrow$  Int153[a, b, p, c, d, q, n, x]
- Rule 1.5.4:  $Int[(e x)^m (a+b x^n)^p (c+d x^n)^q, x] \rightarrow Int[(e x)^m (a+b x^n)^q, x] \rightarrow Int[(e x)^$
- Rule 1.5.5:  $Int[(a+b x^n)^p (c+d x^n)^q (e+f x^n)^r, x] \to Int155[a, b, p, c, d, q, e, f, r, n, x]$
- Rule 1.5.6: Int[ $(g x)^m (a+b x^n)^p (c+d x^n)^q (e+f x^n)^r, x] \rightarrow Int[56[g, m, a, b, p, c, d, q, e, f, r, n, x]]$
- Rule 1.5.7: Int[P[x]  $(a+b x^n)^p$ , x]  $\to$  Int157[P[x], a, b, p, n, x]
- Rule 1.5.8:  $Int[(c x)^m P[x] (a+b x^n)^p, x] \to Int158[c, m, P[x], a, b, p, n, x]$
- Rule 1.5.9:  $Int[P[x] (a+b x^n)^p (c+d x^n)^q, x] \to Int159[P[x], a, b, p, c, d, q, n, x]$
- Rule 1.5.10:  $Int[(e x)^n P[x] (a+b x^n)^p (c+d x^n)^q, x] \rightarrow Int1510[e, m, P[x], a, b, p, c, d, q, n, x]$

#### 1.6 Trinomial

- Rule 1.6.1: Int[(a+b  $x^n+c x^n(2 n))^p, x] \to Int161[a, b, c, p, n, x]$
- Rule 1.6.2: Int[ $(d x)^m (a+b x^n+c x^n(2 n))^p, x$ ]  $\to$  Int162[d, m, a, b, c, p, n, x]
- Rule 1.6.3: Int[ $(d+e x^n)^n q (a+b x^n+c x^n(2 n))^n p, x$ ]  $\rightarrow$  Int163[d, e, q, a, b, c, p, n, x]
- Rule 1.6.4:  $Int[(f x)^n (d+e x^n)^q (a+b x^n+c x^n(2 n))^p, x] \rightarrow Int164[f, m, d, e, q, a, b, c, p, n, x]$
- Rule 1.6.5:  $Int[P[x] (a+b x^n+c x^n(2 n))^p, x] \rightarrow Int165[P[x], a, b, c, p, n, x]$
- Rule 1.6.6:  $Int[(d x)^n P[x] (a+b x^n+c x^n(2 n))^p, x] \rightarrow Int 166[d, m, P[x], a, b, c, p, n, x]$
- Rule 1.6.7: Int[P[x]  $(d+e x^n)^q (a+b x^n+c x^n(2n))^p, x] \rightarrow Int167[P[x], d, e, q, a, b, c, p, n, x]$
- Rule 1.6.8: Int[(f x)^m P[x] (d+e x^n)^q (a+b x^n+c x^(2 n))^p, x]  $\rightarrow$  Int168[f, m, P[x], d, e, q, a, b, c, p, n, x]