# Mathematica 11.3 Integration Test Results

Test results for the 641 problems in "3.4 u (a+b log(c (d+e  $x^m)^n$ ))p.m"

Problem 80: Result more than twice size of optimal antiderivative.

$$\int \frac{Log \left[ \, c \, \left( \, a \, + \, b \, \, x^2 \, \right)^{\, p} \, \right]^{\, 2}}{x} \, \, \mathrm{d}x$$

Optimal (type 4, 72 leaves, 5 steps):

$$\frac{1}{2} \, \text{Log} \left[ -\frac{b \, x^2}{a} \right] \, \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right]^2 + p \, \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right] \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] - p^2 \, \text{PolyLog} \left[ 3, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2}{a} \right] + p \, \text{PolyLog} \left[ 2, \, 1 + \frac{b \, x^2$$

Result (type 4, 163 leaves):

$$\begin{split} & \text{Log}\left[x\right] \; \left(-p \, \text{Log}\left[\,a + b \, \, x^2\,\right] \, + \, \text{Log}\left[\,c \, \left(\,a + b \, \, x^2\,\right)^{\,p}\,\right]\,\right)^{\,2} \, + \, 2 \, p \, \left(-p \, \text{Log}\left[\,a + b \, \, x^2\,\right] \, + \, \text{Log}\left[\,c \, \left(\,a + b \, \, x^2\,\right)^{\,p}\,\right]\,\right) \\ & \left(\text{Log}\left[\,x\,\right] \; \left(\text{Log}\left[\,a + b \, \, x^2\,\right] \, - \, \text{Log}\left[\,1 + \frac{b \, x^2}{a}\,\right]\,\right) \, - \, \frac{1}{2} \, \text{PolyLog}\left[\,2 \, , \, - \frac{b \, x^2}{a}\,\right]\,\right) \, + \\ & \frac{1}{2} \, p^2 \, \left(\text{Log}\left[\,- \, \frac{b \, x^2}{a}\,\right] \, \text{Log}\left[\,a + b \, x^2\,\right]^2 \, + \, 2 \, \text{Log}\left[\,a + b \, x^2\,\right] \, \text{PolyLog}\left[\,2 \, , \, 1 + \frac{b \, x^2}{a}\,\right] \, - \, 2 \, \text{PolyLog}\left[\,3 \, , \, 1 + \frac{b \, x^2}{a}\,\right]\,\right) \end{split}$$

Problem 81: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\text{Log} \left[ \, c \, \left( \, a \, + \, b \, \, x^2 \, \right)^{\, p} \, \right]^{\, 2}}{x^3} \, \, \mathrm{d} x$$

Optimal (type 4, 80 leaves, 4 steps):

$$\frac{b \; p \; Log\left[\left.-\frac{b \; x^2}{a}\right.\right] \; Log\left[\left.c \; \left(a + b \; x^2\right)^{\, p}\right.\right]}{a} \; - \; \frac{\left(a + b \; x^2\right) \; Log\left[\left.c \; \left(a + b \; x^2\right)^{\, p}\right.\right]^2}{2 \; a \; x^2} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}{a} \; + \; \frac{b \; p^2 \; PolyLog\left[\left.2 \; , \; 1 + \frac{b \; x^2}{a}\right.\right]}$$

Result (type 4, 446 leaves):

$$\begin{split} &-\frac{1}{2\,a\,x^2}\left(2\,p\,\left(2\,b\,x^2\,\text{Log}[\,x\,]\,-\,\left(a+b\,x^2\right)\,\text{Log}\big[\,a+b\,x^2\,\big]\,\right)\,\left(p\,\text{Log}\big[\,a+b\,x^2\,\big]\,-\,\text{Log}\big[\,c\,\left(a+b\,x^2\right)^{\,p}\,\big]\right)\,+\\ &-a\,\left(-p\,\text{Log}\big[\,a+b\,x^2\,\big]\,+\,\text{Log}\big[\,c\,\left(a+b\,x^2\right)^{\,p}\,\big]\,\right)^2\,+\\ &-p^2\left(a\,\text{Log}\big[\,a+b\,x^2\,\big]^2\,+\,b\,x^2\,\left(\text{Log}\big[\,-\,\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\big]^2\,+\,\text{Log}\big[\,\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\big]^2\,+\,2\,\text{Log}\big[\,-\,\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\big]\\ &-\,\text{Log}\big[\,\frac{1}{2}\,-\,\frac{i\,\sqrt{b}\,\,x}{2\,\sqrt{a}}\,\big]\,+\,2\,\text{Log}\big[\,\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\big]\,\,\text{Log}\big[\,\frac{1}{2}\,+\,\frac{i\,\sqrt{b}\,\,x}{2\,\sqrt{a}}\,\big]\,+\,4\,\text{Log}[\,x\,]\,\,\text{Log}\big[\,1\,-\,\frac{i\,\sqrt{b}\,\,x}{\sqrt{a}}\,\big]\,+\\ &-\,4\,\text{Log}[\,x\,]\,\,\text{Log}\big[\,1\,+\,\frac{i\,\sqrt{b}\,\,x}{\sqrt{a}}\,\big]\,-\,4\,\text{Log}[\,x\,]\,\,\text{Log}\big[\,a+b\,x^2\,\big]\,-\,2\,\text{Log}\big[\,-\,\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\big]\,\,\text{Log}\big[\,a+b\,x^2\,\big]\,-\\ &-\,2\,\text{Log}\big[\,\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\big]\,\,\text{Log}\big[\,a+b\,x^2\,\big]\,+\,2\,\text{Log}\big[\,a+b\,x^2\,\big]^2\,+\,4\,\text{PolyLog}\big[\,2\,,\,\,-\,\frac{i\,\sqrt{b}\,\,x}{\sqrt{a}}\,\big]\,+\\ &-\,4\,\text{PolyLog}\big[\,2\,,\,\,\frac{i\,\sqrt{b}\,\,x}{\sqrt{a}}\,\big]\,+\,2\,\text{PolyLog}\big[\,2\,,\,\,\frac{1}{2}\,-\,\frac{i\,\sqrt{b}\,\,x}{2\,\sqrt{a}}\,\big]\,+\,2\,\text{PolyLog}\big[\,2\,,\,\,\frac{1}{2}\,+\,\frac{i\,\sqrt{b}\,\,x}{2\,\sqrt{a}}\,\big]\,\,\big)\,\big)\,\big)\,\end{split}$$

Problem 82: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log\left[c\,\left(a+b\,x^2\right)^p\right]^2}{x^5}\,\mathrm{d}x$$

Optimal (type 4, 129 leaves, 8 steps):

$$\frac{b^{2} \ p^{2} \ Log\left[x\right]}{a^{2}} - \frac{b \ p \ \left(a + b \ x^{2}\right) \ Log\left[c \ \left(a + b \ x^{2}\right)^{p}\right]}{2 \ a^{2} \ x^{2}} - \frac{Log\left[c \ \left(a + b \ x^{2}\right)^{p}\right]^{2}}{4 \ x^{4}} - \frac{b^{2} \ p \ Log\left[c \ \left(a + b \ x^{2}\right)^{p}\right] \ Log\left[1 - \frac{a}{a + b \ x^{2}}\right]}{2 \ a^{2}} + \frac{b^{2} \ p^{2} \ PolyLog\left[2, \ \frac{a}{a + b \ x^{2}}\right]}{2 \ a^{2}}$$

Result (type 4, 550 leaves):

$$\begin{split} &\frac{1}{4\,a^2\,x^4}\,\left[4\,b^2\,p^2\,x^4\,\text{Log}\,[\,x\,]\,+b^2\,p^2\,x^4\,\text{Log}\,\big[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\big]^2\,+\,b^2\,p^2\,x^4\,\text{Log}\,\big[\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\big]^2\,+\\ &2\,b^2\,p^2\,x^4\,\text{Log}\,\big[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\big]\,\,\text{Log}\,\Big[\frac{1}{2}\,-\frac{\mathrm{i}\,\sqrt{b}\,x}{2\,\sqrt{a}}\,\Big]\,+\,2\,b^2\,p^2\,x^4\,\text{Log}\,\Big[\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\Big]\,\,\text{Log}\,\Big[\frac{1}{2}\,+\,\frac{\mathrm{i}\,\sqrt{b}\,x}{2\,\sqrt{a}}\,\Big]\,+\\ &4\,b^2\,p^2\,x^4\,\text{Log}\,[\,x\,]\,\,\text{Log}\,\Big[1\,-\,\frac{\mathrm{i}\,\sqrt{b}\,x}{\sqrt{a}}\,\Big]\,+\,4\,b^2\,p^2\,x^4\,\text{Log}\,[\,x\,]\,\,\text{Log}\,\Big[1\,+\,\frac{\mathrm{i}\,\sqrt{b}\,x}{\sqrt{a}}\,\Big]\,-\\ &2\,b^2\,p^2\,x^4\,\text{Log}\,[\,a\,+\,b\,x^2\,]\,-\,2\,b^2\,p^2\,x^4\,\text{Log}\,\Big[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\Big]\,\,\text{Log}\,[\,a\,+\,b\,x^2\,]\,-\\ &2\,b^2\,p^2\,x^4\,\text{Log}\,\Big[\,\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,\Big]\,\,\text{Log}\,[\,a\,+\,b\,x^2\,]\,-\,2\,a\,b\,p\,x^2\,\text{Log}\,[\,c\,\,(\,a\,+\,b\,x^2\,)^{\,p}\,]\,-\\ &4\,b^2\,p\,x^4\,\text{Log}\,[\,x\,]\,\,\text{Log}\,[\,c\,\,(\,a\,+\,b\,x^2\,)^{\,p}\,]\,+\,2\,b^2\,p\,x^4\,\text{Log}\,[\,a\,+\,b\,x^2\,]\,\,\text{Log}\,[\,c\,\,(\,a\,+\,b\,x^2\,)^{\,p}\,]\,-\\ &a^2\,\text{Log}\,[\,c\,\,(\,a\,+\,b\,x^2\,)^{\,p}\,]^2\,+\,4\,b^2\,p^2\,x^4\,\text{PolyLog}\,[\,2\,,\,-\frac{\mathrm{i}\,\sqrt{b}\,x}{\sqrt{a}}\,]\,+\,4\,b^2\,p^2\,x^4\,\text{PolyLog}\,[\,2\,,\,\frac{\mathrm{i}\,\sqrt{b}\,x}{\sqrt{a}}\,]\,+\\ &2\,b^2\,p^2\,x^4\,\text{PolyLog}\,[\,2\,,\,\frac{1}{2}\,-\,\frac{\mathrm{i}\,\sqrt{b}\,x}{2\,\sqrt{a}}\,]\,+\,2\,b^2\,p^2\,x^4\,\text{PolyLog}\,[\,2\,,\,\frac{1}{2}\,+\,\frac{\mathrm{i}\,\sqrt{b}\,x}{2\,\sqrt{a}}\,]\,\Big) \end{split}$$

Problem 83: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log\left[c\left(a+bx^2\right)^p\right]^2}{x^7} \, dx$$

Optimal (type 4, 193 leaves, 12 steps):

$$-\frac{b^{2} p^{2}}{6 a^{2} x^{2}} - \frac{b^{3} p^{2} Log[x]}{a^{3}} + \frac{b^{3} p^{2} Log[a + b x^{2}]}{6 a^{3}} - \frac{b p Log[c (a + b x^{2})^{p}]}{6 a x^{4}} + \frac{b^{2} p (a + b x^{2}) Log[c (a + b x^{2})^{p}]}{3 a^{3} x^{2}} - \frac{Log[c (a + b x^{2})^{p}]^{2}}{6 x^{6}} + \frac{b^{3} p Log[c (a + b x^{2})^{p}] Log[1 - \frac{a}{a + b x^{2}}]}{3 a^{3}} - \frac{b^{3} p^{2} PolyLog[2, \frac{a}{a + b x^{2}}]}{3 a^{3}}$$

Result (type 4, 583 leaves):

$$-\frac{1}{6\,a^3\,x^6}\left(a\,b^2\,p^2\,x^4+6\,b^3\,p^2\,x^6\,\text{Log}\,[\,x\,]\,+b^3\,p^2\,x^6\,\text{Log}\,[\,-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,]^2\,+\,b^3\,p^2\,x^6\,\text{Log}\,[\,\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,]^2\,+\,\\ 2\,b^3\,p^2\,x^6\,\text{Log}\,[\,-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,]\,\,\text{Log}\,[\,\frac{1}{2}\,-\frac{\mathrm{i}\,\sqrt{b}\,x}{2\,\sqrt{a}}\,]\,+\,2\,b^3\,p^2\,x^6\,\text{Log}\,[\,\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,]\,\,\text{Log}\,[\,\frac{1}{2}\,+\frac{\mathrm{i}\,\sqrt{b}\,x}{2\,\sqrt{a}}\,]\,+\,\\ 4\,b^3\,p^2\,x^6\,\text{Log}\,[\,x\,]\,\,\text{Log}\,[\,1\,-\frac{\mathrm{i}\,\sqrt{b}\,x}{\sqrt{a}}\,]\,+\,4\,b^3\,p^2\,x^6\,\text{Log}\,[\,x\,]\,\,\text{Log}\,[\,1\,+\frac{\mathrm{i}\,\sqrt{b}\,x}{\sqrt{a}}\,]\,-\,3\,b^3\,p^2\,x^6\,\text{Log}\,[\,a+b\,x^2\,]\,-\,\\ 2\,b^3\,p^2\,x^6\,\text{Log}\,[\,-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,]\,\,\text{Log}\,[\,a+b\,x^2\,]\,-\,2\,b^3\,p^2\,x^6\,\,\text{Log}\,[\,\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}\,+\,x\,]\,\,\text{Log}\,[\,a+b\,x^2\,]\,+\,\\ a^2\,b\,p\,x^2\,\text{Log}\,[\,c\,\,(\,a+b\,x^2)^{\,p}\,]\,-\,2\,a\,b^2\,p\,x^4\,\text{Log}\,[\,c\,\,(\,a+b\,x^2)^{\,p}\,]\,-\,\\ 4\,b^3\,p\,x^6\,\,\text{Log}\,[\,x\,]\,\,\text{Log}\,[\,c\,\,(\,a+b\,x^2)^{\,p}\,]\,+\,2\,b^3\,p\,x^6\,\,\text{Log}\,[\,a+b\,x^2\,]\,\,\text{Log}\,[\,c\,\,(\,a+b\,x^2)^{\,p}\,]\,+\,\\ a^3\,\,\text{Log}\,[\,c\,\,(\,a+b\,x^2)^{\,p}\,]^2\,+\,4\,b^3\,p^2\,x^6\,\,\text{PolyLog}\,[\,2\,,\,-\frac{\mathrm{i}\,\sqrt{b}\,x}{\sqrt{a}}\,]\,+\,4\,b^3\,p^2\,x^6\,\,\text{PolyLog}\,[\,2\,,\,\frac{\mathrm{i}\,\sqrt{b}\,x}{\sqrt{a}}\,]\,+\,\\ 2\,b^3\,p^2\,x^6\,\,\text{PolyLog}\,[\,2\,,\,\frac{1}{2}\,-\frac{\mathrm{i}\,\sqrt{b}\,x}{2\,\sqrt{a}}\,]\,+\,2\,b^3\,p^2\,x^6\,\,\text{PolyLog}\,[\,2\,,\,\frac{1}{2}\,+\,\frac{\mathrm{i}\,\sqrt{b}\,x}{2\,\sqrt{a}}\,]\,\right)$$

#### Problem 87: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\left[c \left(a + b x^{2}\right)^{p}\right]^{2}}{x^{2}} dx$$

Optimal (type 4, 190 leaves, 7 steps):

$$\frac{4 \text{ i } \sqrt{b} \text{ } p^2 \text{ ArcTan} \left[\frac{\sqrt{b} \text{ } x}{\sqrt{a}}\right]^2}{\sqrt{a}} + \frac{8 \sqrt{b} \text{ } p^2 \text{ ArcTan} \left[\frac{\sqrt{b} \text{ } x}{\sqrt{a}}\right] \text{ Log} \left[\frac{2\sqrt{a}}{\sqrt{a} + i \sqrt{b} \text{ } x}\right]}{\sqrt{a}} + \frac{4 \sqrt{b} \text{ } p \text{ ArcTan} \left[\frac{\sqrt{b} \text{ } x}{\sqrt{a}}\right] \text{ Log} \left[c \left(a + b \text{ } x^2\right)^p\right]}{\sqrt{a}} - \frac{2\sqrt{a}}{\sqrt{a}} + \frac{4 \text{ } i \sqrt{b} \text{ } p^2 \text{ PolyLog} \left[2, 1 - \frac{2\sqrt{a}}{\sqrt{a} + i \sqrt{b} \text{ } x}\right]}{\sqrt{a}}$$

Result (type 4, 387 leaves):

$$\begin{split} & - \frac{1}{\sqrt{a} \ x} \left( 4 \ \sqrt{b} \ p^2 \ x \ \text{ArcTan} \big[ \frac{\sqrt{b} \ x}{\sqrt{a}} \big] \ \text{Log} \big[ - \frac{\text{i} \ \sqrt{a}}{\sqrt{b}} + x \big] + \text{i} \ \sqrt{b} \ p^2 \ x \ \text{Log} \big[ - \frac{\text{i} \ \sqrt{a}}{\sqrt{b}} + x \big]^2 + \\ & 4 \ \sqrt{b} \ p^2 \ x \ \text{ArcTan} \big[ \frac{\sqrt{b} \ x}{\sqrt{a}} \big] \ \text{Log} \big[ \frac{\text{i} \ \sqrt{a}}{\sqrt{b}} + x \big] - \text{i} \ \sqrt{b} \ p^2 \ x \ \text{Log} \big[ \frac{\text{i} \ \sqrt{a}}{\sqrt{b}} + x \big]^2 - \\ & 2 \ \text{i} \ \sqrt{b} \ p^2 \ x \ \text{Log} \big[ - \frac{\text{i} \ \sqrt{a}}{\sqrt{b}} + x \big] \ \text{Log} \big[ \frac{1}{2} - \frac{\text{i} \ \sqrt{b} \ x}{2 \sqrt{a}} \big] + 2 \ \text{i} \ \sqrt{b} \ p^2 \ x \ \text{Log} \big[ \frac{\text{i} \ \sqrt{a}}{\sqrt{b}} + x \big] \ \text{Log} \big[ \frac{1}{2} + \frac{\text{i} \ \sqrt{b} \ x}{2 \sqrt{a}} \big] - \\ & 4 \ \sqrt{b} \ p \ x \ \text{ArcTan} \big[ \frac{\sqrt{b} \ x}{\sqrt{a}} \big] \ \text{Log} \big[ c \ \left( a + b \ x^2 \right)^p \big] + \sqrt{a} \ \text{Log} \big[ c \ \left( a + b \ x^2 \right)^p \big]^2 + \\ & 2 \ \text{i} \ \sqrt{b} \ p^2 \ x \ \text{PolyLog} \big[ 2 , \ \frac{1}{2} - \frac{\text{i} \ \sqrt{b} \ x}{2 \sqrt{a}} \big] - 2 \ \text{i} \ \sqrt{b} \ p^2 \ x \ \text{PolyLog} \big[ 2 , \ \frac{1}{2} + \frac{\text{i} \ \sqrt{b} \ x}{2 \sqrt{a}} \big] \bigg] \end{split}$$

#### Problem 94: Result more than twice size of optimal antiderivative.

$$\int \frac{Log \left[ \, c \, \left( \, a \, + \, b \, \, x^2 \, \right)^{\, p} \, \right]^{\, 3}}{x} \, \, \mathrm{d} x$$

Optimal (type 4, 106 leaves, 6 steps):

$$\begin{split} &\frac{1}{2} \, \text{Log} \left[ -\frac{b \, x^2}{a} \right] \, \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right]^3 + \frac{3}{2} \, p \, \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right]^2 \, \text{PolyLog} \left[ 2 \, , \, 1 + \frac{b \, x^2}{a} \right] - \\ & 3 \, p^2 \, \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right] \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{b \, x^2}{a} \right] + 3 \, p^3 \, \text{PolyLog} \left[ 4 \, , \, 1 + \frac{b \, x^2}{a} \right] \end{split}$$

Result (type 4, 279 leaves):

$$\begin{split} & \text{Log}[x] \, \left( -p \, \text{Log} \Big[ \, a + b \, x^2 \, \Big] \, + \, \text{Log} \Big[ \, c \, \left( \, a + b \, x^2 \, \right)^p \, \Big] \, \right)^3 \, + \, 3 \, p \, \left( -p \, \text{Log} \Big[ \, a + b \, x^2 \, \Big] \, + \, \text{Log} \Big[ \, c \, \left( \, a + b \, x^2 \, \right)^p \, \Big] \, \right)^2 \\ & \left( \text{Log}[x] \, \left( \text{Log}[a + b \, x^2] \, - \, \text{Log} \Big[ 1 + \frac{b \, x^2}{a} \, \Big] \, \right) - \frac{1}{2} \, \text{PolyLog} \Big[ 2 \, , \, - \frac{b \, x^2}{a} \, \Big] \, \right) - \\ & \frac{3}{2} \, p^2 \, \left( p \, \text{Log} \Big[ \, a + b \, x^2 \, \Big] \, - \, \text{Log} \Big[ \, c \, \left( \, a + b \, x^2 \, \right)^p \, \Big] \, \right) \\ & \left( \text{Log} \Big[ - \frac{b \, x^2}{a} \, \Big] \, \text{Log} \Big[ \, a + b \, x^2 \, \Big]^2 \, + \, 2 \, \text{Log} \Big[ \, a + b \, x^2 \, \Big] \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{b \, x^2}{a} \, \Big] \, - \, 2 \, \text{PolyLog} \Big[ 3 \, , \, 1 + \frac{b \, x^2}{a} \, \Big] \, \right) \, + \\ & \frac{1}{2} \, p^3 \, \left( \text{Log} \Big[ - \frac{b \, x^2}{a} \, \Big] \, \text{Log} \Big[ \, a + b \, x^2 \, \Big]^3 \, + \, 3 \, \text{Log} \Big[ \, a + b \, x^2 \, \Big]^2 \, \text{PolyLog} \Big[ \, 2 \, , \, 1 + \frac{b \, x^2}{a} \, \Big] \, - \\ & 6 \, \text{Log} \Big[ \, a + b \, x^2 \, \Big] \, \, \text{PolyLog} \Big[ \, 3 \, , \, 1 + \frac{b \, x^2}{a} \, \Big] \, + \, 6 \, \text{PolyLog} \Big[ \, 4 \, , \, 1 + \frac{b \, x^2}{a} \, \Big] \, \right) \end{split}$$

Problem 95: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log \left[ \, c \, \left( \, a \, + \, b \, \, x^2 \, \right)^{\, p} \, \right]^{\, 3}}{x^3} \, \mathrm{d} x$$

Optimal (type 4, 119 leaves, 6 steps):

$$\frac{3 \, b \, p \, Log \left[\, - \, \frac{b \, x^2}{a} \, \right] \, Log \left[\, c \, \left(\, a + b \, x^2 \, \right)^{\, p} \, \right]^{\, 2}}{2 \, a} \, - \, \frac{\left(\, a + b \, x^2 \, \right) \, Log \left[\, c \, \left(\, a + b \, x^2 \, \right)^{\, p} \, \right]^{\, 3}}{2 \, a \, x^2} \, + \\ \frac{3 \, b \, p^2 \, Log \left[\, c \, \left(\, a + b \, x^2 \, \right)^{\, p} \, \right] \, PolyLog \left[\, 2 \, , \, 1 + \frac{b \, x^2}{a} \, \right]}{a} \, - \, \frac{3 \, b \, p^3 \, PolyLog \left[\, 3 \, , \, 1 + \frac{b \, x^2}{a} \, \right]}{a}$$

Result (type 4, 627 leaves):

$$\begin{split} \frac{1}{2 \, a \, x^2} \\ & \left( a \, \left( p \, \text{Log} \left[ a + b \, x^2 \right] - \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right] \right)^3 + 6 \, b \, p \, x^2 \, \text{Log} \left[ x \right] \, \left( - p \, \text{Log} \left[ a + b \, x^2 \right] + \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right] \right)^2 - \\ & 3 \, a \, p \, \text{Log} \left[ a + b \, x^2 \right] \, \left( - p \, \text{Log} \left[ a + b \, x^2 \right] + \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right] \right)^2 - \\ & 3 \, b \, p \, x^2 \, \text{Log} \left[ a + b \, x^2 \right] \, \left( - p \, \text{Log} \left[ a + b \, x^2 \right] + \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right] \right)^2 + \\ & 3 \, p^2 \, \left( p \, \text{Log} \left[ a + b \, x^2 \right] - \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right] \right) \, \left( a \, \text{Log} \left[ a + b \, x^2 \right]^2 + \\ & b \, x^2 \, \left( \text{Log} \left[ - \frac{i \, \sqrt{a}}{\sqrt{b}} + x \right]^2 + \text{Log} \left[ \frac{i \, \sqrt{a}}{\sqrt{b}} + x \right]^2 + 2 \, \text{Log} \left[ - \frac{i \, \sqrt{a}}{\sqrt{b}} + x \right] \, \text{Log} \left[ \frac{1}{2} - \frac{i \, \sqrt{b} \, x}{2 \, \sqrt{a}} \right] + \\ & 2 \, \text{Log} \left[ \frac{i \, \sqrt{a}}{\sqrt{b}} + x \right] \, \text{Log} \left[ \frac{1}{2} + \frac{i \, \sqrt{b} \, x}{2 \, \sqrt{a}} \right] + 4 \, \text{Log} \left[ x \right] \, \text{Log} \left[ 1 - \frac{i \, \sqrt{b} \, x}{\sqrt{a}} \right] + \\ & 4 \, \text{Log} \left[ x \right] \, \text{Log} \left[ 1 + \frac{i \, \sqrt{b} \, x}{\sqrt{a}} \right] - 4 \, \text{Log} \left[ x \right] \, \text{Log} \left[ a + b \, x^2 \right] - 2 \, \text{Log} \left[ - \frac{i \, \sqrt{b} \, x}{\sqrt{b}} + x \right] \, \text{Log} \left[ a + b \, x^2 \right] - \\ & 2 \, \text{Log} \left[ \frac{i \, \sqrt{a}}{\sqrt{b}} + x \right] \, \text{Log} \left[ a + b \, x^2 \right] + 2 \, \text{Log} \left[ a + b \, x^2 \right]^2 + 4 \, \text{PolyLog} \left[ 2 \, , \, - \frac{i \, \sqrt{b} \, x}{\sqrt{a}} \right] + \\ & 4 \, \text{PolyLog} \left[ 2 \, , \, \frac{i \, \sqrt{b} \, x}{\sqrt{a}} \right] + 2 \, \text{PolyLog} \left[ 2 \, , \, \frac{1}{2} - \frac{i \, \sqrt{b} \, x}{2 \, \sqrt{a}} \right] + 2 \, \text{PolyLog} \left[ 2 \, , \, \frac{1}{2} + \frac{i \, \sqrt{b} \, x}{2 \, \sqrt{a}} \right] \right) \right) - \\ & p^3 \, \left( \text{Log} \left[ a + b \, x^2 \right] \, \text{PolyLog} \left[ 2 \, , \, 1 + \frac{b \, x^2}{a} \right] + \left( a + b \, x^2 \right) \, \text{Log} \left[ a + b \, x^2 \right] \right) - \\ & 6 \, b \, x^2 \, \text{Log} \left[ a + b \, x^2 \right] \, \text{PolyLog} \left[ 2 \, , \, 1 + \frac{b \, x^2}{a} \right] + 6 \, b \, x^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{b \, x^2}{a} \right] \right) \right) \right)$$

Problem 96: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log\left[c\,\left(a+b\,x^2\right)^p\right]^3}{x^5}\,\mathrm{d}x$$

Optimal (type 4, 219 leaves, 10 steps):

$$\frac{3 \, b^{2} \, p^{2} \, Log\left[c\, \left(a + b\, x^{2}\right)^{p}\right]}{2 \, a^{2}} - \frac{3 \, b \, p \, \left(a + b\, x^{2}\right) \, Log\left[c\, \left(a + b\, x^{2}\right)^{p}\right]^{2}}{4 \, a^{2} \, x^{2}} - \frac{Log\left[c\, \left(a + b\, x^{2}\right)^{p}\right]^{3}}{4 \, x^{4}} - \frac{3 \, b^{2} \, p \, Log\left[c\, \left(a + b\, x^{2}\right)^{p}\right]^{2} \, Log\left[c\, \left(a + b\, x^{2}\right)^{p}\right]^{3}}{4 \, a^{2}} + \frac{3 \, b^{2} \, p^{2} \, Log\left[c\, \left(a + b\, x^{2}\right)^{p}\right] \, PolyLog\left[2, \, \frac{a}{a + b\, x^{2}}\right]}{2 \, a^{2}} + \frac{3 \, b^{2} \, p^{3} \, PolyLog\left[3, \, \frac{a}{a + b\, x^{2}}\right]}{2 \, a^{2}} + \frac{3 \, b^{2} \, p^{3} \, PolyLog\left[3, \, \frac{a}{a + b\, x^{2}}\right]}{2 \, a^{2}}$$

Result (type 4, 803 leaves):

$$\begin{split} &\frac{1}{4\,a^2\,x^4}\left(a^2\,\left(p\,\text{Log}\big[a+b\,x^2\big]-\text{Log}\big[c\,\left(a+b\,x^2\right)^p\big]\right)^3-3\,a\,b\,p\,x^2\,\left(-p\,\text{Log}\big[a+b\,x^2\big]+\text{Log}\big[c\,\left(a+b\,x^2\right)^p\big]\right)^2-6\,b^2\,p\,x^4\,\text{Log}\big[x\,\left(-p\,\text{Log}\big[a+b\,x^2\big]+\text{Log}\big[c\,\left(a+b\,x^2\right)^p\big]\right)^2-3\,a^2\,p\,\text{Log}\big[a+b\,x^2\big]\,\left(-p\,\text{Log}\big[a+b\,x^2\big]+\text{Log}\big[c\,\left(a+b\,x^2\right)^p\big]\right)^2+3\,b^2\,p\,x^4\,\text{Log}\big[a+b\,x^2\big]\,\left(-p\,\text{Log}\big[a+b\,x^2\big]+\text{Log}\big[c\,\left(a+b\,x^2\right)^p\big]\right)^2+3\,p^2\,\left(p\,\text{Log}\big[a+b\,x^2\big]-\text{Log}\big[c\,\left(a+b\,x^2\right)^p\big]\right)\left(a^2\,\text{Log}\big[a+b\,x^2\big]^2-b\,x^2\,\left(4\,b\,x^2\,\text{Log}\big[x\big]+b\,x^2\,\text{Log}\big[x^2+b\,x^2\,\text{L$$

Problem 97: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log \left[ \left. c \, \left( a + b \, x^2 \right)^p \right]^3}{x^7} \, \mathrm{d}x$$

Optimal (type 4, 352 leaves, 17 steps):

$$\frac{b^{3}\,p^{3}\,Log\left[x\right]}{a^{3}} - \frac{b^{2}\,p^{2}\,\left(a+b\,x^{2}\right)\,Log\left[c\,\left(a+b\,x^{2}\right)^{p}\right]}{2\,a^{3}\,x^{2}} - \frac{b^{3}\,p^{2}\,Log\left[-\frac{b\,x^{2}}{a}\right]\,Log\left[c\,\left(a+b\,x^{2}\right)^{p}\right]}{a^{3}} - \frac{b\,p\,Log\left[c\,\left(a+b\,x^{2}\right)^{p}\right]^{2}}{4\,a\,x^{4}} + \frac{b^{2}\,p\,\left(a+b\,x^{2}\right)\,Log\left[c\,\left(a+b\,x^{2}\right)^{p}\right]^{2}}{2\,a^{3}\,x^{2}} - \frac{Log\left[c\,\left(a+b\,x^{2}\right)^{p}\right]^{3}}{6\,x^{6}} - \frac{b^{3}\,p^{2}\,Log\left[c\,\left(a+b\,x^{2}\right)^{p}\right]\,Log\left[1-\frac{a}{a+b\,x^{2}}\right]}{2\,a^{3}} + \frac{b^{3}\,p\,Log\left[c\,\left(a+b\,x^{2}\right)^{p}\right]^{2}\,Log\left[1-\frac{a}{a+b\,x^{2}}\right]}{2\,a^{3}} + \frac{b^{3}\,p\,Log\left[c\,\left(a+b\,x^{2}\right)^{p}\right]^{p}\,PolyLog\left[2,\,\frac{a}{a+b\,x^{2}}\right]}{a^{3}} - \frac{b^{3}\,p^{2}\,Log\left[c\,\left(a+b\,x^{2}\right)^{p}\right]\,PolyLog\left[2,\,\frac{a}{a+b\,x^{2}}\right]}{a^{3}} - \frac{b^{3}\,p^{3}\,PolyLog\left[3,\,\frac{a}{a+b\,x^{2}}\right]}{a^{3}} - \frac{b^{3}\,p^{3}\,PolyLog\left[3,\,\frac{$$

Result (type 4, 1013 leaves):

$$\begin{split} \frac{1}{12\,a^3\,x^6} \\ \left(2\,a^3\,\left(p\,\text{Log}\left[a+b\,x^2\right] - \text{Log}\left[c\,\left(a+b\,x^2\right)^p\right]\right)^3 - 3\,a^2\,b\,p\,x^2\,\left(-p\,\text{Log}\left[a+b\,x^2\right] + \text{Log}\left[c\,\left(a+b\,x^2\right)^p\right]\right)^2 + \\ 6\,a\,b^2\,p\,x^4\,\left(-p\,\text{Log}\left[a+b\,x^2\right] + \text{Log}\left[c\,\left(a+b\,x^2\right)^p\right]\right)^2 + \\ 12\,b^3\,p\,x^6\,\text{Log}\left[x\right]\,\left(-p\,\text{Log}\left[a+b\,x^2\right] + \text{Log}\left[c\,\left(a+b\,x^2\right)^p\right]\right)^2 - \\ 6\,a^3\,p\,\text{Log}\left[a+b\,x^2\right]\,\left(-p\,\text{Log}\left[a+b\,x^2\right] + \text{Log}\left[c\,\left(a+b\,x^2\right)^p\right]\right)^2 - 6\,b^3\,p\,x^6\,\text{Log}\left[a+b\,x^2\right] \\ \left(-p\,\text{Log}\left[a+b\,x^2\right] + \text{Log}\left[c\,\left(a+b\,x^2\right)^p\right]\right)^2 + 6\,p^2\,\left(p\,\text{Log}\left[a+b\,x^2\right] - \text{Log}\left[c\,\left(a+b\,x^2\right)^p\right]\right) \\ \left(a^3\,\text{Log}\left[a+b\,x^2\right] + b\,x^2\,\left(a\,b\,x^2 + 6\,b^2\,x^4\,\text{Log}\left[x\right] + b^2\,x^4\,\text{Log}\left[-\frac{i\,\sqrt{a}}{\sqrt{b}} + x\right]^2 + b^2\,x^4\,\text{Log}\left[\frac{i\,\sqrt{a}}{\sqrt{b}} + x\right]^2 + \\ 2\,b^2\,x^4\,\text{Log}\left[-\frac{i\,\sqrt{a}}{\sqrt{b}} + x\right]\,\text{Log}\left[\frac{1}{2} - \frac{i\,\sqrt{b}\,x}{2\,\sqrt{a}}\right] + 2\,b^2\,x^4\,\text{Log}\left[\frac{i\,\sqrt{a}}{\sqrt{b}} + x\right]\,\text{Log}\left[\frac{1}{2} + \frac{i\,\sqrt{b}\,x}{2\,\sqrt{a}}\right] + \\ 4\,b^2\,x^4\,\text{Log}\left[x\right]\,\text{Log}\left[1 - \frac{i\,\sqrt{b}\,x}{\sqrt{a}}\right] + 4\,b^2\,x^4\,\text{Log}\left[x\right]\,\text{Log}\left[1 + \frac{i\,\sqrt{b}\,x}{\sqrt{a}}\right] + a^2\,\text{Log}\left[a+b\,x^2\right] - \\ 2\,a\,b\,x^2\,\text{Log}\left[a+b\,x^2\right] - 3\,b^2\,x^4\,\text{Log}\left[a+b\,x^2\right] - 4\,b^2\,x^4\,\text{Log}\left[x\right]\,\text{Log}\left[a+b\,x^2\right] - \\ 2\,b^2\,x^4\,\text{Log}\left[-\frac{i\,\sqrt{a}}{\sqrt{b}} + x\right]\,\text{Log}\left[a+b\,x^2\right] - 2\,b^2\,x^4\,\text{Log}\left[\frac{i\,\sqrt{a}}{\sqrt{b}} + x\right]\,\text{Log}\left[a+b\,x^2\right] + \\ 2\,b^2\,x^4\,\text{Log}\left[a+b\,x^2\right]^2 + 4\,b^2\,x^4\,\text{PolyLog}\left[2, -\frac{i\,\sqrt{b}\,x}{\sqrt{a}}\right] + 4\,b^2\,x^4\,\text{PolyLog}\left[2, \frac{i\,\sqrt{b}\,x}{\sqrt{a}}\right] + \\ 2\,b^2\,x^4\,\text{PolyLog}\left[2, \frac{1}{2} - \frac{i\,\sqrt{b}\,x}{2\,\sqrt{a}}\right] + 2\,b^2\,x^4\,\text{PolyLog}\left[2, \frac{1}{2} + \frac{i\,\sqrt{b}\,x}{2\,\sqrt{a}}\right] \right) \right) - \\ p^3\left(-6\,b^3\,x^6\,\text{Log}\left[-\frac{b\,x^2}{a}\right] + 6\,a\,b^2\,x^4\,\text{Log}\left[a+b\,x^2\right]^2 - 6\,a\,b^2\,x^4\,\text{Log}\left[a+b\,x^2\right]^3 - 9\,b^3\,x^6\,\text{Log}\left[a+b\,x^2\right]^2 - \\ 6\,b^3\,x^6\,\text{Log}\left[-\frac{b\,x^2}{a}\right] + \text{Log}\left[a+b\,x^2\right]^2 + 2\,a^3\,\text{Log}\left[a+b\,x^2\right]^3 + 2\,b^3\,x^6\,\text{Log}\left[a+b\,x^2\right]^3 + \\ 6\,b^3\,x^6\,\left(3 - 2\,\text{Log}\left[a+b\,x^2\right]\right)\,\text{PolyLog}\left[2, 1 + \frac{b\,x^2}{a}\right] + 12\,b^3\,x^6\,\text{PolyLog}\left[3, 1 + \frac{b\,x^2}{a}\right]\right) \right) \right) \right)$$

Problem 131: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log\left[c\left(d+e\,x^3\right)^p\right]^2}{x}\,\mathrm{d}x$$

Optimal (type 4, 77 leaves, 5 steps):

$$\begin{split} &\frac{1}{3} \, \text{Log} \Big[ -\frac{e \, x^3}{d} \Big] \, \, \text{Log} \Big[ c \, \left( d + e \, x^3 \right)^p \Big]^2 \, + \\ &\frac{2}{3} \, p \, \, \text{Log} \Big[ c \, \left( d + e \, x^3 \right)^p \Big] \, \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x^3}{d} \Big] \, - \frac{2}{3} \, p^2 \, \, \text{PolyLog} \Big[ 3 \, , \, 1 + \frac{e \, x^3}{d} \Big] \end{split}$$

#### Result (type 4, 2965 leaves):

$$\begin{split} & \log[x] \left( -p \log[d + e x^3] + \log[c \left(d + e x^3]^p] \right)^2 + 2p \left( -p \log[d + e x^3] + \log[c \left(d + e x^3)^p] \right) \\ & \left( \log[x] \left( \log[d + e x^3] - \log[1 + \frac{e x^3}{d}] \right) - \frac{1}{3} p Olylog[2], - \frac{e x^3}{d}] \right) + \\ & p^2 \left( \log\left[ - \frac{e^{1/3} x}{d^{1/3}} \right] \log\left[ \frac{d^{1/3}}{e^{1/3}} + x \right]^2 + 2 \log\left[ - \frac{e^{1/3} x}{d^{1/3}} \right] \log\left[ \frac{d^{1/3}}{e^{1/3}} + x \right] \log\left[ - \frac{(-1)^{1/3} d^{1/3}}{d^{1/3}} + x \right] + \\ & \log\left[ - \frac{(-1)^{2/3} e^{1/3} x}{d^{1/3}} \right] \log\left[ - \frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + 2 \log\left[ - \frac{e^{1/3} x}{d^{1/3}} \right] \log\left[ \frac{d^{1/3}}{e^{1/3}} + x \right] + \\ & \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} + x \right] + 2 \log\left[ \left( - \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) \log\left[ \frac{(-1)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \\ & \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) \log\left[ \left( \frac{(-1)^{1/3} d^{1/3} x}{e^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{e^{1/3}} \right) \right] \log\left[ \frac{(-1)^{1/3} e^{1/3} x}{e^{1/3}} \right] + \\ & \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{e^{1/3}} \right) - \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{e^{1/3}} \right) \right] \right) + \\ & \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{e^{1/3}} \right) - \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{e^{1/3}} \right) \right] \right) + \\ & \log\left[ \left( \frac{e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) - \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{e^{1/3}} \right) \right] \right) + \\ & \log\left[ \left( \frac{e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{e^{1/3}} \right) \right] + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) \right] \right) + \\ & \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) \right] + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) \right] + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) \right] + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) \right] + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) \right] + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) + \log\left[ \left( \frac{(-1)^{1/3} e^{1/3} x}{d^{1/3}} \right) \right] + \log\left[ \left( \frac$$

$$\begin{split} & 2 \left( -\log \left[ -\frac{e^{1/3} x}{d^{1/3}} \right] + \log \left[ -\frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] \right) \log \left[ \frac{d^{1/3} + \left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] \log \left[ 1 + \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] + \\ & \left[ \log \left[ -\frac{e^{1/3} x}{d^{2/3}} \right] - \log \left[ -\frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{2/3}} \right] \right) \log \left[ 1 + \frac{\left( -1 \right)^{2/3} e^{2/3} x}{d^{1/3}} \right] \right] + \\ & \left[ \log \left[ x \right] \left( \log \left[ \frac{d^{1/3}}{e^{1/3}} + x \right] + \log \left[ 1 + \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] \right) + \\ & \left[ \log \left[ x \right] \left( \log \left[ \frac{d^{1/3}}{e^{1/3}} + x \right] + \log \left[ -\frac{\left( -1 \right)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \log \left[ \frac{\left( -1 \right)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - \log \left[ d + e x^3 \right] \right)^2 - \\ & 2 \left( \log \left[ \frac{d^{1/3}}{e^{1/3}} + x \right] + \log \left[ -\frac{\left( -1 \right)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \log \left[ -\frac{\left( -1 \right)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - \log \left[ d + e x^3 \right] \right) \\ & \left( \log \left[ x \right] \log \left[ \frac{d^{1/3}}{e^{1/3}} + x \right] + \log \left[ x \right] \log \left[ -\frac{\left( -1 \right)^{1/3} d^{1/3}}{e^{1/3}} + x \right] + \log \left[ x \right] \log \left[ -\frac{\left( -1 \right)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - \log \left[ x \right] \log \left[ x \right] + \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] - \log \left[ x \right] \log \left[ x \right] + \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] - \log \left[ x \right] \log \left[ x \right] + \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] - \log \left[ x \right] \log \left[ x \right] + \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] - \log \left[ x \right] \log \left[ x \right] + \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] - \log \left[ x \right] \log \left[ x \right] + \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] - \log \left[ x \right] \log \left[ x \right] + \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} \left( \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3}} \right)}{e^{1/3}} + x \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{1/3} x} \right] + 2 \log \left[ \frac{\left( -1 \right)^{2/3} e^{1/3} x}{d^{1/3} + e^{$$

$$\begin{split} &2\left[\text{Log}\left[-\frac{\left(-1\right)^{1/3}\,\text{d}^{1/3}}{\text{e}^{1/3}} + x\right] + \text{Log}\left[\frac{\left(-1\right)^{2/3}\left(\frac{\left(-1\right)^{2/3}\,\text{d}^{1/3}}{\text{e}^{1/3}} + x\right)}{-\frac{\left(-1\right)^{1/3}\,\text{d}^{1/3}}{\text{e}^{1/3}}}\right] + \text{PolyLog}\left[2,\,1 - \frac{\left(-1\right)^{1/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3}}\right] + \\ &2\left[\text{Log}\left[\frac{\text{d}^{1/3}}{\text{e}^{1/3}} + x\right] + \text{Log}\left[\frac{\text{d}^{1/3} - \left(-1\right)^{1/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3} + \text{e}^{1/3}\,x}\right]\right] + \text{PolyLog}\left[2,\,1 - \frac{\left(-1\right)^{1/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3}}\right] + \\ &2\left[\text{Log}\left[-\frac{\left(-1\right)^{1/3}\,\text{d}^{1/3}}{\text{e}^{1/3}} + x\right] + \text{PolyLog}\left[2,\,1 + \frac{\left(-1\right)^{2/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3}}\right] + \\ &2\left[\text{Log}\left[\frac{\left(-1\right)^{2/3}\,\text{d}^{1/3}}{\text{e}^{1/3}} + x\right] - \text{Log}\left[\frac{\left(-1\right)^{2/3}\left(\frac{\left(-1\right)^{2/3}\,\text{d}^{1/3}\,\text{d}^{1/3}}{\text{e}^{1/3}\,x}\right)}{-\frac{\left(-1\right)^{1/3}\,\text{d}^{1/3}}{\text{e}^{1/3}\,x}}\right] \right] + \text{PolyLog}\left[2,\,1 + \frac{\left(-1\right)^{2/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3}}\right] + \\ &2\left[\text{Log}\left[\frac{\text{d}^{1/3}}{\text{e}^{1/3}} + x\right] + \text{Log}\left[\frac{\text{d}^{1/3} + \left(-1\right)^{2/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3} + \text{e}^{1/3}\,x}\right]\right] + \text{PolyLog}\left[3,\,\frac{\left(-1\right)^{2/3}\left(\frac{\left(-1\right)^{2/3}\,\text{d}^{1/3}}{\text{e}^{1/3}} + x\right)}{\text{d}^{1/3} + \text{e}^{1/3}\,x}\right] - 2\left[\text{PolyLog}\left[3,\,\frac{-\left(-1\right)^{1/3}\,\text{d}^{1/3} + \text{e}^{1/3}\,x}{\text{d}^{1/3} + \text{e}^{1/3}\,x}\right] - \\ &2\left[\text{PolyLog}\left[3,\,\frac{\left(-1\right)^{2/3}\,\text{d}^{1/3} + \text{e}^{1/3}\,x}{\text{d}^{1/3} + \text{e}^{1/3}\,x}\right] - 2\left[\text{PolyLog}\left[3,\,\frac{-\left(-1\right)^{1/3}\,\text{d}^{1/3} + \text{e}^{1/3}\,x}{\text{d}^{1/3} + \text{e}^{1/3}\,x}\right] - \\ &2\left[\text{PolyLog}\left[3,\,\frac{\text{d}^{1/3} - \left(-1\right)^{1/3}\,\text{d}^{1/3} + \text{e}^{1/3}\,x}{\text{d}^{1/3} + \text{e}^{1/3}\,x}\right] - 2\left[\text{PolyLog}\left[3,\,\frac{\text{d}^{1/3} + \left(-1\right)^{2/3}\,\text{d}^{1/3} + \text{e}^{1/3}\,x}{\text{d}^{1/3} + \text{e}^{1/3}\,x}\right] - \\ &2\left[\text{PolyLog}\left[3,\,\frac{\text{d}^{1/3} - \left(-1\right)^{1/3}\,\text{d}^{1/3}\,x}{\text{d}^{1/3}\,x}\right] - 2\left[\text{PolyLog}\left[3,\,\frac{\text{d}^{1/3} + \left(-1\right)^{2/3}\,\text{d}^{1/3}\,x}{\text{d}^{1/3} + \text{e}^{1/3}\,x}\right] - \\ &2\left[\text{PolyLog}\left[3,\,1 + \frac{\text{e}^{1/3}\,x}{\text{d}^{1/3}\,x}\right] - 6\left[\text{PolyLog}\left[3,\,1 - \frac{\left(-1\right)^{1/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3}}\right] - 6\left[\text{PolyLog}\left[3,\,1 - \frac{\left(-1\right)^{1/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3}}\right] - 6\left[\text{PolyLog}\left[3,\,1 - \frac{\left(-1\right)^{1/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3}}\right] - 6\left[\text{PolyLog}\left[3,\,1 - \frac{\left(-1\right)^{1/3}\,\text{e}^{1/3}\,x}{\text{d}^{1/3}}\right] - 6$$

Problem 132: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log\left[c\left(d+e\,x^3\right)^p\right]^2}{x^4}\,\mathrm{d}x$$

Optimal (type 4, 86 leaves, 4 steps):

$$\frac{2 \, e \, p \, Log\left[\, c \, \left(\, d \, + \, e \, \, x^{3}\,\right)^{\, p}\,\right]}{3 \, d} \, - \, \frac{\left(\, d \, + \, e \, \, x^{3}\,\right)^{\, p}\,\right]}{3 \, d \, x^{3}} \, + \, \frac{2 \, e \, p^{2} \, PolyLog\left[\, 2 \, , \, \, 1 \, + \, \frac{e \, x^{3}}{d}\,\right]}{3 \, d}$$

Result (type 4, 1374 leaves):

$$-\frac{1}{9\,d\,x^3}\left[6\,p\,\left(3\,e\,x^3\,Log\,[\,x\,]\,-\,\left(d+e\,x^3\right)\,Log\,[\,d+e\,x^3\,]\,\right)\,\left(p\,Log\,[\,d+e\,x^3\,]\,-\,Log\,[\,c\,\left(d+e\,x^3\right)^{\,p}\,]\,\right)\,+\\\\ 3\,d\,\left(-\,p\,Log\,[\,d+e\,x^3\,]\,+\,Log\,[\,c\,\left(d+e\,x^3\right)^{\,p}\,]\,\right)^{\,2}\,+\\$$

$$\begin{split} p^2 \left[ 3 \, d \, \text{Log} \left[ d + e \, x^3 \right]^2 + e \, x^3 \left[ 6 \, \text{Log} \left[ 2 \right]^2 + \text{Log} \left[ 6 \right] \, \text{Log} \left[ 64 \right] - 4 \, \text{Log} \left[ 8 \right] \, \text{Log} \left[ x \right] - 2 \, \text{Log} \left[ 4096 \right] \, \text{Log} \left[ x \right] + 3 \, \text{Log} \left[ \frac{d^{1/3}}{e^{1/3}} + x \right]^2 - 2 \, \text{Log} \left[ 8 \right] \, \text{Log} \left[ \frac{-1 - i \, \sqrt{3}}{e^{1/3}} \right] d^{1/3} + 2 \, x \right] - \\ \text{Log} \left[ 46656 \right] \, \text{Log} \left[ \frac{\left( -1 - i \, \sqrt{3} \right)}{e^{1/3}} \right] d^{1/3} + 2 \, x \right] + 3 \, \text{Log} \left[ \frac{\left( -1 - i \, \sqrt{3} \right)}{e^{1/3}} \right] d^{1/3} + 2 \, x \right]^2 - \\ \text{Log} \left[ 64 \right] \, \text{Log} \left[ \frac{i \left( i + \sqrt{3} \right)}{e^{1/3}} \right] d^{1/3} + 2 \, x \right] + 3 \, \text{Log} \left[ \frac{i \left( i + \sqrt{3} \right)}{e^{1/3}} \right] d^{1/3} + 2 \, x \right] - \\ \text{Log} \left[ \frac{-2 \, i \, d^{1/3} + \left( i + \sqrt{3} \right)}{\left( -3 \, i + \sqrt{3} \right)} \right] d^{1/3} \, x}{\left( -3 \, i + \sqrt{3} \right)} d^{1/3} \, x} \right] + 6 \, \text{Log} \left[ \frac{i \left( i + \sqrt{3} \right)}{e^{1/3}} \right] d^{1/3} + 2 \, x \right] - \\ \text{Log} \left[ \frac{-2 \, i \, d^{1/3} + \left( i + \sqrt{3} \right)}{\left( -3 \, i + \sqrt{3} \right)} \right] d^{1/3} \, x}{\left( -3 \, i + \sqrt{3} \right)} d^{1/3} \, x} \right] + 18 \, \text{Log} \left[ \frac{i \left( i + \sqrt{3} \right)}{3 \, i + \sqrt{3}} \right] + 2 \, x \right] - \\ \text{Log} \left[ \frac{2 \, i \, \left( 1 + \frac{e^{3/3} \, x}{e^{1/3}} \right)}{3 \, i - \sqrt{3}} \right] + 6 \, \text{Log} \left[ \frac{d^{1/3}}{e^{1/3}} + x \right] \, \text{Log} \left[ \frac{1 + \frac{e^{3/3} \, x}{e^{1/3}}}{3 \, i + \sqrt{3}} \right] - \\ \text{Log} \left[ 64 \right] \, \text{Log} \left[ \frac{2 \, i \, \left( 1 + \frac{e^{3/3} \, x}{e^{3/3}} \right)}{3 \, i + \sqrt{3}} \right] + 6 \, \text{Log} \left[ \frac{e^{1/3}}{e^{1/3}} + 2 \, x \right] \, \text{Log} \left[ \frac{2 \, i \, \left( 1 + \frac{e^{3/3} \, x}{e^{3/3}} \right)}{3 \, i + \sqrt{3}} \right] - \\ \text{Log} \left[ 64 \right] \, \text{Log} \left[ \frac{2 \, i \, \left( 1 + \frac{e^{3/3} \, x}{e^{3/3}} \right)}{3 \, i + \sqrt{3}} \right] + 6 \, \text{Log} \left[ \frac{i \, \left( i + \sqrt{3} \right)}{3 \, i + \sqrt{3}} \right] + 2 \, x \right] \, \text{Log} \left[ \frac{2 \, i \, \left( 1 + \frac{e^{3/3} \, x}{e^{3/3}} \right)}{3 \, i + \sqrt{3}} \right] - \\ \text{Log} \left[ 64 \right] \, \text{Log} \left[ 3 + i \, \sqrt{3} - \frac{2 \, i \, \sqrt{3}}{3} \, e^{3/3} \right] + 2 \, x \right] \, \text{Log} \left[ \frac{2 \, i \, \left( 1 + \frac{e^{3/3} \, x}{e^{3/3}} \right)}{3 \, i + \sqrt{3}} \right] - \\ \text{Log} \left[ 10 \, \text{Log} \left[ 2 + \frac{\left( 1 - i \, \sqrt{3} \right)}{3} \, e^{3/3} \right] + 2 \, x \right] \, \text{Log} \left[ 2 + \frac{\left( 1 - i \, \sqrt{3} \right)}{3} \, e^{3/3}} \right] + \\ \text{Log} \left[ 10 \, \text{Log} \left[ 2 + \frac{\left( 1 - i \, \sqrt{3} \right)}{3} \, e^{3/3} \, x \right] \right] + 18 \, \text{Log} \left[ 2 \, \frac{i \,$$

$$6 \, \mathsf{PolyLog} \Big[ 2 , \, \frac{-2 \, \dot{\mathbb{I}} \, d^{1/3} + \left( \dot{\mathbb{I}} + \sqrt{3} \right) \, e^{1/3} \, x}{\left( -3 \, \dot{\mathbb{I}} + \sqrt{3} \right) \, d^{1/3}} \Big] + 6 \, \mathsf{PolyLog} \Big[ 2 , \, \frac{\dot{\mathbb{I}} + \sqrt{3} - \frac{2 \, \dot{\mathbb{I}} \, e^{1/3} \, x}{d^{1/3}}}{3 \, \dot{\mathbb{I}} + \sqrt{3}} \Big] + 6 \, \mathsf{PolyLog} \Big[ 2 , \, \frac{2 \, \dot{\mathbb{I}} \, \left( 1 + \frac{e^{1/3} \, x}{d^{1/3}} \right)}{3 \, \dot{\mathbb{I}} - \sqrt{3}} \Big] + 6 \, \mathsf{PolyLog} \Big[ 2 , \, \frac{2 \, \dot{\mathbb{I}} \, \left( 1 + \frac{e^{1/3} \, x}{d^{1/3}} \right)}{3 \, \dot{\mathbb{I}} - \sqrt{3}} \Big] + 6 \, \mathsf{PolyLog} \Big[ 2 , \, \frac{2 \, \dot{\mathbb{I}} \, \left( 1 + \frac{e^{1/3} \, x}{d^{1/3}} \right)}{3 \, \dot{\mathbb{I}} + \sqrt{3}} \Big] + 6 \, \mathsf{PolyLog} \Big[ 2 , \, \frac{1}{6} \, \left( 3 + \dot{\mathbb{I}} \, \sqrt{3} - \frac{2 \, \dot{\mathbb{I}} \, \sqrt{3} \, e^{1/3} \, x}{d^{1/3}} \right) \Big] \Bigg] \Bigg]$$

#### Problem 133: Result unnecessarily involves higher level functions.

$$\int x \, Log \left[ \, c \, \left( \, d + e \, x^3 \, \right)^{\, p} \, \right]^{\, 2} \, \mathrm{d}x$$

Optimizal (type 4, 1294 leaves, 49 steps). 
$$\frac{9 \, p^2 \, x^2}{4} + \frac{3 \, \sqrt{3} \, d^{2/3} \, p^2 \, \text{ArcTan} \left[ \frac{d^{1/2} - 2 \, e^{1/3} \, x}{\sqrt{3} \, d^{1/3}} \right] + \frac{3 \, d^{2/3} \, p^2 \, \text{Log} \left[ d^{1/3} + e^{1/3} \, x \right]}{2 \, e^{2/3}} + \frac{d^{2/3} \, p^2 \, \text{Log} \left[ d^{1/3} + e^{1/3} \, x \right]}{2 \, e^{2/3}} + \frac{d^{2/3} \, p^2 \, \text{Log} \left[ d^{1/3} + e^{1/3} \, x \right] \, \text{Log} \left[ - \frac{(-1)^{3/3} \, d^{1/3} + e^{3/3} \, x}{\left[ 1 - (-1)^{2/3} \right] \, d^{1/3}} \right]} - \frac{d^{2/3} \, p^2 \, \text{Log} \left[ \frac{(-1)^{3/3} \, \left[ d^{3/3} + e^{3/3} \, x \right]}{\left( 1 - (-1)^{3/3} \, d^{3/3} \, p^2 \, \text{Log} \left[ \frac{(-1)^{3/3} \, \left[ d^{3/3} + e^{3/3} \, x \right]}{\left( 1 - (-1)^{3/3} \, d^{3/3} \, x \right)^2} \right]} - \frac{e^{2/3}}{2 \, e^{2/3}} - \frac{\left( -1 \right)^{3/3} \, d^{2/3} \, p^2 \, \text{Log} \left[ \frac{d^{1/3} - \left( -1 \right)^{3/3} \, e^{1/3} \, x \right]}{\left( 1 - (-1)^{3/3} \, d^{3/3} \, e^{3/3} \, x \right)^2} + \frac{e^{2/3}}{2 \, e^{2/3}} + \frac{\left( -1 \right)^{2/3} \, d^{2/3} \, p^2 \, \text{Log} \left[ \frac{(-1)^{3/3} \, \left[ d^{3/3} + e^{3/3} \, x \right]}{\left( 1 - (-1)^{3/3} \, d^{3/3} \, x \right)^2} \right] \, \text{Log} \left[ d^{1/3} + \left( -1 \right)^{2/3} \, e^{1/3} \, x \right]}{e^{2/3}} + \frac{\left( -1 \right)^{2/3} \, d^{2/3} \, p^2 \, \text{Log} \left[ \frac{(-1)^{3/3} \, \left[ d^{3/3} + e^{3/3} \, x \right]}{\left( 1 - (-1)^{3/3} \, d^{3/3} \, x \right)^2} \right] \, + \frac{d^{2/3} \, p^2 \, \text{Log} \left[ d^{1/3} + \left( -1 \right)^{2/3} \, e^{3/3} \, x \right]}{e^{2/3}} - \frac{\left( -1 \right)^{2/3} \, d^{2/3} \, p^2 \, \text{Log} \left[ d^{3/3} + \left( -1 \right)^{2/3} \, e^{3/3} \, x \right]}{\left( 1 - (-1)^{2/3} \, \left[ d^{3/3} + \left( -1 \right)^{2/3} \, e^{3/3} \, x \right]} \right] \, - \frac{e^{2/3}}{e^{2/3}} - \frac{\left( -1 \right)^{2/3} \, d^{2/3} \, p^2 \, \text{Log} \left[ d^{3/3} + \left( -1 \right)^{2/3} \, e^{3/3} \, x \right]}{e^{2/3}} \, - \frac{\left( -1 \right)^{2/3} \, d^{2/3} \, p^2 \, \text{Log} \left[ d^{3/3} + \left( -1 \right)^{2/3} \, e^{3/3} \, x \right]}{\left( 1 - \left( -1 \right)^{2/3} \, \left( d^{3/3} + \left( -1 \right)^{2/3} \, e^{3/3} \, x \right)} \right] \, - \frac{e^{2/3}}{e^{2/3}}} - \frac{\left( -1 \right)^{3/3} \, d^{2/3} \, p^2 \, \text{Log} \left[ d^{3/3} - \left( -1 \right)^{3/3} \, e^{3/3} \, x \right]}{\left( 1 - \left( -1 \right)^{2/3} \, \left( d^{3/3} + \left( -1 \right)^{2/3} \, e^{3/3} \, x \right)} \right] \, - \frac{e^{2/3}}{e^{3/3}}} - \frac{e^{2/3} \, d^{3/3} \, p^2 \, \text{Log} \left[ d^{3/3} - \left( -1 \right)^{3/3} \, d^{3/3} \, x \right]} \, - \frac{e^{2/3} \, d^{3/3} \, p^2 \, \text{Log} \left[ d^{3/3}$$

$$\frac{3 \, d^{2/3} \, p^2 \, \text{Log} \left[ d^{2/3} - d^{1/3} \, e^{1/3} \, x + e^{2/3} \, x^2 \right]}{4 \, e^{2/3}} - \frac{3}{2} \, p \, x^2 \, \text{Log} \left[ c \, \left( d + e \, x^3 \right)^p \right] - \frac{d^{2/3} \, p \, \text{Log} \left[ d^{1/3} + e^{1/3} \, x \right] \, \text{Log} \left[ c \, \left( d + e \, x^3 \right)^p \right]}{e^{2/3}} + \frac{\left( -1 \right)^{1/3} \, d^{2/3} \, p \, \text{Log} \left[ d^{1/3} - \left( -1 \right)^{1/3} \, e^{1/3} \, x \right] \, \text{Log} \left[ c \, \left( d + e \, x^3 \right)^p \right]}{e^{2/3}} - \frac{\left( -1 \right)^{2/3} \, d^{2/3} \, p \, \text{Log} \left[ d^{1/3} + \left( -1 \right)^{2/3} \, e^{1/3} \, x \right] \, \text{Log} \left[ c \, \left( d + e \, x^3 \right)^p \right]}{e^{2/3}} + \frac{1}{2} \, x^2 \, \text{Log} \left[ c \, \left( d + e \, x^3 \right)^p \right]^2 + \frac{d^{2/3} \, p^2 \, \text{PolyLog} \left[ 2 \, , \, \frac{d^{1/3} + e^{1/3} \, x}{\left( 1 + \left( -1 \right)^{1/3} \, d^{1/3} \right)} \right]} - \frac{\left( -1 \right)^{2/3} \, d^{2/3} \, p^2 \, \text{PolyLog} \left[ 2 \, , \, - \frac{\left( -1 \right)^{2/3} \, \left( d^{1/3} + e^{1/3} \, x \right)}{\left( 1 - \left( -1 \right)^{2/3} \, d^{1/3} \right)} \right]} + \frac{d^{2/3} \, p^2 \, \text{PolyLog} \left[ 2 \, , \, - \frac{\left( -1 \right)^{1/3} \, \left( \left( -1 \right)^{2/3} \, d^{1/3} + e^{1/3} \, x \right)}{\left( 1 - \left( -1 \right)^{2/3} \, d^{1/3} \right)} \right]} - \frac{d^{2/3} \, p^2 \, \text{PolyLog} \left[ 2 \, , \, - \frac{\left( -1 \right)^{1/3} \, \left( \left( -1 \right)^{2/3} \, d^{1/3} + e^{1/3} \, x \right)}{\left( 1 - \left( -1 \right)^{2/3} \, d^{1/3} + e^{1/3} \, x} \right)} \right]} - \frac{e^{2/3}}{e^{2/3}} + \frac{\left( -1 \right)^{2/3} \, d^{2/3} \, p^2 \, \text{PolyLog} \left[ 2 \, , \, \frac{d^{1/3} + \left( -1 \right)^{2/3} \, e^{1/3} \, x}{\left( 1 + \left( -1 \right)^{1/3} \, d^{2/3} \, p} \right)} \right]} - \frac{e^{2/3}}{e^{2/3}}$$

#### Result (type 5, 2364 leaves)

$$\begin{split} p\left(-\frac{3 \text{ e } x^5 \text{ Hypergeometric} 2\text{F1}\left[1,\frac{5}{3},\frac{8}{3},-\frac{\text{ e } x^3}{\text{d}}\right]}{5 \text{ d}} + x^2 \text{ Log}\left[d+\text{ e } x^3\right]\right) \\ & \left(-p \text{ Log}\left[d+\text{ e } x^3\right] + \text{ Log}\left[c\left(d+\text{ e } x^3\right)^p\right]\right) + \frac{1}{2} \, x^2 \left(-p \text{ Log}\left[d+\text{ e } x^3\right] + \text{ Log}\left[c\left(d+\text{ e } x^3\right)^p\right]\right)^2 + \\ p^2\left(\frac{1}{2} \, x^2 \text{ Log}\left[d+\text{ e } x^3\right]^2 - 3 \text{ e} \left(\frac{1}{\text{e}}\left(-\frac{d^{1/3}}{\text{e}^{1/3}} + \frac{\left(-1\right)^{1/3} d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) \left(\frac{d^{1/3}}{\text{e}^{1/3}} + x\right) \right] \\ & \left(-1 + \text{ Log}\left[\frac{d^{1/3}}{\text{e}^{1/3}} + x\right]\right) - \frac{d^{4/3} \text{ Log}\left[\frac{d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right] \left(\frac{d^{4/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) + \frac{1}{\text{e}} \\ & \left(-\frac{d^{1/3}}{\text{e}^{1/3}} + \frac{\left(-1\right)^{1/3} d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) \left(-\frac{\left(-1\right)^{1/3} d^{1/3}}{\text{e}^{1/3}} + x\right) \left(-1 + \text{ Log}\left[-\frac{\left(-1\right)^{1/3} d^{1/3}}{\text{e}^{1/3}} + x\right]\right) + \\ & \frac{\left(-1\right)^{1/3} d^{4/3} \text{ Log}\left[-\frac{\left(-1\right)^{1/3} d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) + \frac{1}{\text{e}} \\ & \left(-\frac{d^{1/3}}{\text{e}^{1/3}} + \frac{\left(-1\right)^{1/3} d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) \left(\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} + x\right) \left(-1 + \text{ Log}\left[\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} + x\right]\right) + \\ & \frac{\left(-1\right)^{2/3} d^{4/3} \text{ Log}\left[\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) \left(\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} + x\right) \left(-1 + \text{ Log}\left[\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} + x\right]\right) + \\ & \frac{\left(-1\right)^{2/3} d^{4/3} \text{ Log}\left[\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) \left(-\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} + x\right) + \frac{1}{\text{e}} \\ & \frac{\left(-1\right)^{2/3} d^{4/3} \text{ Log}\left[\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) \left(-\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) + \frac{1}{\text{e}} \\ & \frac{\left(-1\right)^{2/3} d^{4/3} \text{ Log}\left[-\frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} - \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}}\right) + \frac{1}{\text{e}} \\ & \frac{\left(-1\right)^{2/3} d^{1/3}}{\text{e}^{1/3}} + \frac{1}{\text{e}} \\ & \frac{\left(-1\right)^{$$

$$\begin{split} &\left[-\frac{1}{2}\frac{e^{1/3}}{e^{1/3}}\left(-\frac{d^{1/3}}{e^{2/3}} + \frac{x^2}{2e^{1/3}} + \frac{d^{2/3}\log\left[d^{1/3} + e^{1/3}x\right]}{e}\right) + \frac{1}{2}x^2\log\left[\frac{d^{1/3} + e^{1/3}}{e^{1/3}}\right]\right) + \frac{1}{e} \\ &\left[-\frac{1}{4}\frac{e^{2/3}}{e^{1/3}}\left(e^{1/3}x\left(2\left(-1\right)^{1/3}\frac{d^{1/3} + e^{1/3}x}{e^{1/3}}\right)\right] + \frac{1}{e} \\ &\left[-\frac{1}{2}x^2\log\left[\frac{-\left(-1\right)^{1/3}\frac{d^{1/3}}{e^{1/3}} + e^{1/3}x}{e^{1/3}}\right]\right] + \frac{1}{e} \\ &\left[-\frac{1}{2}e^{1/3}\left(-\frac{\left(-1\right)^{2/3}\frac{d^{1/3}}{e^{1/3}} + \frac{e^{1/3}x}{2e^{1/3}}\right)\right] + \frac{1}{e} \\ &\left[-\frac{1}{2}e^{1/3}\left(-\frac{\left(-1\right)^{2/3}\frac{d^{1/3}}{e^{1/3}} + \frac{e^{1/3}x}{2e^{1/3}}\right)\right] + \frac{1}{e} \\ &\frac{1}{2}x^2\log\left[\frac{\left(-1\right)^{2/3}\frac{d^{1/3}}{e^{1/3}} + \frac{e^{1/3}x}{2e^{1/3}}\right] + \frac{1}{6}\frac{e^{5/3}}{8}\left(3e^{2/3}x^2 + 2\sqrt{3}\right)\frac{d^{2/3}}{d^{2/3}} + e^{1/3}x\right) + \frac{1}{2}x^2\log\left[\frac{1}{2}\frac{e^{1/3}}{e^{1/3}} + \frac{e^{1/3}x}{2e^{1/3}}\right] + \frac{1}{6}\frac{e^{5/3}}{8}\left(3e^{2/3}x^2 + 2\sqrt{3}\right)\frac{d^{2/3}}{d^{2/3}} + e^{1/3}x\right) + \frac{1}{2}x^2\log\left[\frac{1}{2}\frac{e^{1/3}}{e^{1/3}} + \frac{e^{1/3}x}{2e^{1/3}}\right] + \frac{1}{2}x^2\log\left[\frac{1}{2}\frac{e^{1/3}}{e^{1/3}} + \frac{1}{2}x^2\log\left[\frac{1}{2}\frac{e^{1/3}}{e^{1/3}} + \frac{e^{1/3}x}{2e^{1/3}}\right]\right] + \frac{1}{2}x^2\log\left[\frac{1}{2}\frac{e^{1/3}}{e^{1/3}} + \frac{e^{1/3}x}{2e^{1/3}}\right] + \frac{1}{2}x^2\log\left[\frac{1}{2}\frac{e^{1/3}}{e^{1/3}} + \frac{e^{1/3}x}{2$$

$$\begin{split} & \text{PolyLog}\Big[2, \frac{e^{1/3} \left(-\frac{(-1)^{1/3} \, d^{1/3}}{e^{1/3}} + x\right)}{-\left(-1\right)^{1/3} \, d^{1/3} - \left(-1\right)^{2/3} \, d^{1/3}}\Big] \right) \bigg| \\ & \left( \left( \frac{d^{1/3}}{e^{1/3}} - \frac{\left(-1\right)^{2/3} \, d^{1/3}}{e^{1/3}} \right) \left( -\frac{\left(-1\right)^{1/3} \, d^{1/3}}{e^{1/3}} - \frac{\left(-1\right)^{2/3} \, d^{1/3}}{e^{1/3}} \right) e^{7/3} \right) - \\ & \left( d^{4/3} \left( \text{Log}\left[ \frac{\left(-1\right)^{2/3} \, d^{1/3}}{e^{1/3}} + x \right] \, \text{Log}\left[ 1 - \frac{e^{1/3} \left( \frac{(-1)^{2/3} \, d^{1/3}}{e^{1/3}} + x \right)}{-d^{1/3} + \left(-1\right)^{2/3} \, d^{1/3}} \right] + \text{PolyLog}\Big[2, \\ & \left( -\frac{e^{1/3} \left( \frac{(-1)^{2/3} \, d^{1/3}}{e^{1/3}} + x \right)}{-d^{1/3} + \left(-1\right)^{2/3} \, d^{1/3}} \right] \right) \bigg| / \left( \left( -\frac{d^{1/3}}{e^{1/3}} - \frac{\left(-1\right)^{1/3} \, d^{1/3}}{e^{1/3}} \right) \left( \frac{d^{1/3}}{e^{1/3}} - \frac{\left(-1\right)^{2/3} \, d^{1/3}}{e^{1/3}} \right) e^{7/3} \right) + \\ & \left( -1 \right)^{1/3} \, d^{4/3} \left( \text{Log}\left[ \frac{\left(-1\right)^{2/3} \, d^{1/3}}{e^{1/3}} + x \right] \, \text{Log}\Big[ 1 - \frac{e^{1/3} \left( \frac{\left(-1\right)^{2/3} \, d^{1/3}}{e^{1/3}} + x \right)}{\left(-1\right)^{1/3} \, d^{1/3} + \left(-1\right)^{2/3} \, d^{1/3}} \right) + \\ & \text{PolyLog}\Big[ 2, \frac{e^{1/3} \left( \frac{\left(-1\right)^{2/3} \, d^{1/3}}{e^{1/3}} + x \right)}{\left(-1\right)^{1/3} \, d^{1/3} + \left(-1\right)^{2/3} \, d^{1/3}} \right) \bigg| \right) \bigg| / \\ & \left( \left( \frac{d^{1/3}}{e^{1/3}} + \frac{\left(-1\right)^{1/3} \, d^{1/3}}{e^{1/3}} \right) \left( -\frac{\left(-1\right)^{1/3} \, d^{1/3}}{e^{1/3}} - \frac{\left(-1\right)^{2/3} \, d^{1/3}}{e^{1/3}} \right) e^{7/3} \right) \bigg| \right) \bigg| \right) \end{aligned}$$

Problem 135: Result unnecessarily involves higher level functions.

$$\int \frac{Log\left[c\,\left(d+e\,x^3\right)^p\right]^2}{x^2}\,\mathrm{d}x$$

Optimal (type 4, 1137 leaves, 39 steps):

$$\frac{e^{2/3} \, p^2 \, \text{Log} \left[ \frac{d^{1/3}}{d^{1/3}} + e^{1/3} \, x \right]^2}{d^{1/3}} + \frac{2 \, e^{1/3} \, p^2 \, \text{Log} \left[ \frac{d^{1/3}}{d^{1/3}} + e^{1/3} \, x \right] \, \text{Log} \left[ \frac{-13^{1/3} \, e^{1/3} \, p^2 \, \text{Log} \left[ \frac{d^{1/3}}{d^{1/3}} + e^{1/3} \, x \right]}{d^{1/3}} \right]}{d^{1/3}} + \frac{2 \, \left[ (-1)^{1/3} \, e^{1/3} \, p^2 \, \text{Log} \left[ \frac{d^{1/3} \, e^{1/3} \, p^2 \, \text{Log} \left[ \frac{d^{1/3} \, e^{1/3} \, x}{d^{1/3}} \right]}{d^{1/3}} \right] \, \text{Log} \left[ d^{1/3} \, - \left( -1 \right)^{1/3} \, e^{1/3} \, x \right]}{d^{1/3}} + \frac{2 \, \left[ (-1)^{1/3} \, e^{1/3} \, p^2 \, \text{Log} \left[ -\frac{(-1)^{1/3} \, e^{1/3} \, x}{(1 - (-1)^{1/3})^3 \, e^{1/3}} \right]} \, \text{Log} \left[ d^{1/3} \, + \left( -1 \right)^{2/3} \, e^{1/3} \, x \right]}{d^{1/3}} + \frac{1}{d^{1/3}} + \frac{1}{d^$$

Result (type 5, 994 leaves):

$$\begin{split} &2p\left(\frac{3\text{ ex}^2\text{ Hypergeometric}2F1\left[\frac{2}{3},1,\frac{5}{3},\frac{ex^2}{e^3}\right]}{2d} - \frac{\log[d+ex^3]}{x}\right) \\ & \left(\text{ p Log}\left[d+ex^3\right] + \text{Log}\left[c\left(d+ex^3\right)^p\right]\right)^2 + p^2\left(-\frac{\log\left[d+ex^3\right]^2}{x} - \frac{1}{\sqrt{3}}\frac{d^{1/3}}{d^{1/3}} + i^2\left[c\left(d+ex^3\right)^p\right]\right)^2 + p^2\left(-\frac{\log\left[d+ex^3\right]^2}{x} - \frac{1}{\sqrt{3}}\frac{d^{1/3}}{d^{1/3}} + i^2\left[c\left(d+ex^3\right)^p\right]\right)^2 + p^2\left(-1\right)^{1/3}\left(-1+\left(-1\right)^{2/3}\right)\log\left[-\frac{\left(-1\right)^{1/3}d^{1/3}}{e^{1/3}} + x\right]^2 + \frac{1}{\sqrt{3}}\frac{d^{1/3}}{d^{1/3}} + i^2\left[c\left(d+ex^3\right)^p\right] + i^2\left(-1\right)^{1/3}\frac{d^{1/3}}{e^{1/3}} + i^2\left[c\left(d+ex^3\right)^p\right] + i^2\left(-1\right)^{1/3}\frac{d^{1/3}}{e^{1/3}} + i$$

Problem 136: Result unnecessarily involves higher level functions.

$$\int\!\frac{Log\!\left[\left.c\,\left(d+e\;x^{3}\right)^{p}\right]^{2}}{x^{3}}\,\mathrm{d}x$$

Optimal (type 4, 1170 leaves, 39 steps):

$$\frac{e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} - e^{1/3} \, x \Big]^2}{2 \, d^{2/3}} = \frac{e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} - e^{1/3} \, x \Big] \, \text{Log} \Big[ -\frac{(-1)^{2/3} \, e^{2/3} \, x}{[1-(-1)^{2/3}] \, e^{1/3} \, x} \Big]}{d^{2/3}} = \frac{e^{2/3} \, p^2 \, \text{Log} \Big[ \frac{(-1)^{3/3} \left[ d^{3/3} + v^2 \right]}{(1-(-1)^{3/3}] \, e^{3/3} \, x} \Big]}{d^{2/3}} = \frac{e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} + \left( -1 \right)^{1/3} \, e^{1/3} \, x \Big]}{2 \, d^{2/3}} = \frac{e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} + \left( -1 \right)^{1/3} \, e^{1/3} \, x \Big]}{2 \, d^{2/3}} + \frac{1}{d^{2/3}}$$
 
$$\left( -1 \right)^{1/3} \, e^{2/3} \, p^2 \, \text{Log} \Big[ -\frac{(-1)^{3/3} \left[ d^{1/3} - \left( -1 \right)^{1/3} \, e^{1/3} \, x \right]}{(1 + (-1)^{1/3}) \, d^{1/3}} \Big] \, \text{Log} \Big[ -d^{1/3} - \left( -1 \right)^{2/3} \, e^{1/3} \, x \Big]}{1 + \left( -1 \right)^{1/3} \, e^{2/3} \, p^2 \, \text{Log} \Big[ -\frac{(-1)^{2/3} \left[ d^{1/3} - \left( -1 \right)^{1/3} \, e^{1/3} \, x \right]}{(1 + (-1)^{1/3}) \, d^{1/3}} \Big] \, \text{Log} \Big[ -d^{1/3} - \left( -1 \right)^{2/3} \, e^{1/3} \, x \Big] + \frac{1}{d^{2/3}}$$
 
$$\left( -1 \right)^{1/3} \, e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} - \left( -1 \right)^{2/3} \, e^{1/3} \, x \right]^2 - \frac{e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} - \left( -1 \right)^{2/3} \, e^{1/3} \, x \Big] \, + \frac{1}{d^{2/3}} \, d^{2/3}} \right] \, d^{2/3}$$
 
$$\left( -1 \right)^{1/3} \, e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} - \left( -1 \right)^{2/3} \, e^{1/3} \, x \right]^2 - \frac{e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} - \left( -1 \right)^{2/3} \, e^{1/3} \, x \Big] \, d^{2/3}}{d^{2/3}} \right] \, d^{2/3}$$
 
$$\left( -1 \right)^{1/3} \, e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} + \left( -1 \right)^{1/3} \, e^{1/3} \, x \Big] \, \text{Log} \Big[ \frac{e^{1/3} + \left( -1 \right)^{2/3} \, e^{1/3} \, x \Big]}{d^{2/3}} \right] + \frac{e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} - \left( -1 \right)^{1/3} \, e^{1/3} \, x \Big] \, \text{Log} \Big[ e^{1/3} + \left( -1 \right)^{1/3} \, e^{1/3} \, x \Big] + \frac{e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} + \left( -1 \right)^{1/3} \, e^{1/3} \, x \Big]}{d^{2/3}} \Big] + \frac{e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} + \left( -1 \right)^{1/3} \, e^{1/3} \, x \Big] \, \text{Log} \Big[ e^{1/3} + \left( -1 \right)^{1/3} \, e^{1/3} \, x \Big] + \frac{e^{2/3} \, e^{1/3} \, x^2}{\left[ -1 \right)^{2/3} \, e^{2/3} \, p^2 \, \text{Log} \Big[ -d^{1/3} + \left( -1 \right)^{1/3} \, e^{1/3} \, x \Big] + \frac{e^{2/3} \, e^{1/3} \, e^{1/3} \, x \Big] + \frac{e^{2/3} \, e^{1/3} \, e^{1/3} \, x \Big] + \frac{e^{2/3} \, e^{1/3} \, e^{1/3} \, x \Big] + \frac{e^$$

Result (type 5, 964 leaves):

$$\begin{split} p\left[\frac{3 \text{ ex Hypergeometric} 2\text{F1}\left[\frac{1}{3}, 1, \frac{4}{3}, -\frac{6 \times 7}{6}\right]}{d} - \frac{\log[d + e \, x^3]}{x^2}\right] \left(-p \log[d + e \, x^3] + \log[c \, \left(d + e \, x^3\right)^p]\right) - \frac{\left(-p \log[d + e \, x^3] + \log[c \, \left(d + e \, x^3\right)^p]\right)^2}{2 \, x^2} + p^2 \left(-\frac{\log[d + e \, x^3]^2}{2 \, x^2} - \frac{1}{2 \, x^2}\right) - \frac{1}{2 \, \sqrt{3}} \frac{1}{6^{2/3}} \frac{1}{6^{2/3}} \frac{1}{6^{2/3}} + x^2\right)^2 - \left(-1 + \left(-1\right)^{2/3}\right) \log\left[-\frac{\left(-1\right)^{3/3} d^{1/3}}{e^{1/3}} + x\right]^2 - \frac{1}{2^{3/3}} \frac{1}{6^{3/3}} + x^2\right] - \frac{1}{2^{3/3}} \frac{1}{6^{3/3}} + x^2\right] - \frac{1}{2^{3/3}} \frac{1}{6^{3/3}} \frac{1}{6^{3/3}} + x^2\right] - \frac{1}{2^{3/3}} \frac{1}{6^{3/3}} \frac{1}{6^{3/3}} + x^2\right] - \frac{1}{2^{3/3}} \frac{1}{6^{3/3}} \frac{1}{2^{3/3}} - 2 \log\left[\frac{d^{1/3}}{6^{3/3}} + \frac{1}{2^{3/3}} + \log\left[\frac{d^{2/3}}{6^{3/3}} + x\right] - \log\left[d + e \, x^3\right]\right] + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x^2 + \log\left[\frac{-1}{2^{3/3}} \frac{1}{2^{3/3}} + x\right] + \log\left[\frac{d^{1/3}}{6^{3/3}} + x\right] - \log\left[d + e \, x^3\right] + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x^2 + \log\left[d + e \, x^3\right] + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x^2 - \log\left[d + e \, x^3\right] + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x^3 - \log\left[d + e \, x^3\right] + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x^3 - \log\left[d + e \, x^3\right] + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x^3 - \log\left[d + e \, x^3\right] + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x^3 - \log\left[\frac{d^{3/3}}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + \frac{e^{3/3}}{2^{3/3}} + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + \frac{1}{2^{3/3}} \frac{1}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + \frac{1}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + \frac{1}{2^{3/3}} + \frac{1}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + \frac{1}{2^{3/3}} + \frac{1}{2^{3/3}} + x\right] + \log\left[\frac{d^{3/3}}{2^{3/3}} + \frac{1}{2^{3/3}} + \frac{1}{2^{3/3}} + \frac{1}{2^{3/3}} + \frac{1}{2^{3/3}} + \frac{1}{2^{3/3}} + \frac{1}{2^{3/3}} + \frac{1}{2$$

### Problem 137: Result unnecessarily involves higher level functions.

$$\int \frac{Log\left[c\,\left(d+e\,x^3\right)^p\right]^2}{x^5}\,\mathrm{d}x$$

Optimal (type 4, 1328 leaves, 48 steps):

$$\frac{3\sqrt{3} \ e^{4/3} \ p^2 \ ArcTan \Big[ \frac{d^{1/2} \cdot 2 \ e^{4/3}}{\sqrt{3} \ d^{1/3}} \Big] }{2 \ d^{4/3}} = \frac{2 \ d^{4/3}}{2 \ d^{4/3}} = \frac{2 \ d^{4/3} \ p^2 \ Log \Big[ d^{1/3} + e^{1/3} \ x \Big] }{2 \ d^{4/3}} = \frac{e^{4/3} \ p^2 \ Log \Big[ d^{1/3} + e^{1/3} \ x \Big] \ Log \Big[ - \frac{(-1)^{1/3} e^{4/3} \ p^2 \ Log \Big[ \frac{(-1)^{1/3} \left[ d^{1/3} + e^{1/3} \ x \Big]}{\left[ 1 + (-1)^{3/3} \right] d^{1/3}} \Big] } + \frac{e^{4/3} \ p^2 \ Log \Big[ \frac{(-1)^{1/3} \left[ d^{1/3} + e^{1/3} \ x \Big]}{\left( 1 + (-1)^{3/3} \right] d^{1/3}} \Big] \ Log \Big[ d^{1/3} - (-1)^{1/3} e^{1/3} \ x \Big] }{2 \ d^{4/3}} + \frac{(-1)^{1/3} \ e^{4/3} \ p^2 \ Log \Big[ \frac{(-1)^{1/3} \left[ d^{1/3} + e^{1/3} \ x \Big]}{\left( 1 + (-1)^{3/3} \right] d^{1/3}} \Big] \ Log \Big[ d^{1/3} + \left( -1 \right)^{2/3} e^{1/3} \ x \Big] }{2 \ d^{4/3}} + \frac{(-1)^{2/3} e^{4/3} \ p^2 \ Log \Big[ \frac{(-1)^{1/3} \left[ d^{1/3} + e^{1/3} \ x \Big]}{\left( 1 + (-1)^{3/3} \right] d^{1/3}} \Big] \ Log \Big[ d^{1/3} + \left( -1 \right)^{2/3} e^{1/3} \ x \Big] }{2 \ d^{4/3}} - \frac{(-1)^{2/3} e^{4/3} \ p^2 \ Log \Big[ \frac{(-1)^{1/3} \left[ d^{1/3} + (-1)^{2/3} e^{1/3} \ x \Big]}{\left( 1 + (-1)^{3/3} \right] d^{1/3}} \Big] \ Log \Big[ \frac{d^{1/3} + (-1)^{2/3} e^{1/3} \ x \Big]}{2 \ d^{4/3}} + \frac{1}{2 \ d^{4/3}} + \frac{1}{2$$

$$\frac{e^{4/3} \ p^2 \ PolyLog \left[2, \ \frac{d^{1/3} + e^{1/3} \ x}{\left(1 + (-1)^{1/3}\right) \ d^{1/3}}\right]}{2 \ d^{4/3}} + \frac{\left(-1\right)^{2/3} \ e^{4/3} \ p^2 \ PolyLog \left[2, \ -\frac{(-1)^{2/3} \left(d^{1/3} + e^{1/3} \ x\right)}{\left(1 - (-1)^{2/3}\right) \ d^{1/3}}\right]}{2 \ d^{4/3}} - \frac{e^{4/3} \ p^2 \ PolyLog \left[2, \ -\frac{(-1)^{1/3} \left((-1)^{2/3} \ d^{1/3} + e^{1/3} \ x\right)}{\left(1 - (-1)^{2/3}\right) \ d^{1/3}}\right]}{2 \ d^{4/3}} + \frac{\left(-1\right)^{1/3} e^{4/3} \ p^2 \ PolyLog \left[2, \ -\frac{(-1)^{1/3} \left((-1)^{2/3} \ d^{1/3} + e^{1/3} \ x\right)}{\left(1 - (-1)^{2/3}\right) \ d^{1/3}}\right]}{2 \ d^{4/3}} + \frac{\left(-1\right)^{1/3} e^{4/3} \ p^2 \ PolyLog \left[2, \ -\frac{(-1)^{1/3} \left((-1)^{2/3} \ d^{1/3} + e^{1/3} \ x\right)}{\left(1 - (-1)^{2/3}\right) \ d^{1/3}}\right]}{2 \ d^{4/3}} + \frac{\left(-1\right)^{1/3} e^{4/3} \ p^2 \ PolyLog \left[2, \ -\frac{d^{1/3} + (-1)^{2/3} e^{1/3} \ x}{\left(1 + (-1)^{1/3}\right) \ d^{1/3}}\right]}{2 \ d^{4/3}}$$

#### Result (type 5, 1296 leaves):

$$\begin{split} \frac{1}{4\,x^4} \left( \frac{1}{d} 2\,p \left( 3\,e\,x^3\,\text{Hypergeometric} 2F1\left[ -\frac{1}{3}\,,\,1,\,\frac{2}{3}\,,\,-\frac{e\,x^3}{d} \right] + d\,\text{Log}\left[ d + e\,x^3 \right] \right) \\ & \left( p\,\text{Log}\left[ d + e\,x^3 \right] - \text{Log}\left[ c\,\left( d + e\,x^3 \right)^p \right] \right) - \\ & \left( -p\,\text{Log}\left[ d + e\,x^3 \right] + \text{Log}\left[ c\,\left( d + e\,x^3 \right)^p \right] \right)^2 + p^2 \left( -\text{Log}\left[ d + e\,x^3 \right]^2 + \frac{1}{2} + 2 \left( -1 \right)^{1/3} \left( -1 + \left( -1 \right)^{1/3} \right)^2 e^{1/3} \, x \right) \right) \\ & \frac{1}{\left( 1 + \left( -1 \right)^{1/3} \right)^2 e^{4/3}} \, e\,x^3 \left[ 3\,\left( -1 \right)^{1/3} e^{1/3} \, x \, \text{Log}\left[ \frac{d^{1/3}}{e^{1/3}} + x \right]^2 + 3\,\left( -1 \right)^{1/3} \left( -1 + \left( -1 \right)^{1/3} \left( -1 + \left( -1 \right)^{1/3} \right) \left( -1 + \left( -1 \right)^{1/3} \right)^2 e^{1/3} \, x \, \text{Log}\left[ \frac{\left( -1 \right)^{2/3} d^{1/3}}{e^{1/3}} + x \right]^2 + 3 \left( -1 \right)^{1/3} \left( -1 + \left( -1 \right)^{1/3} \right)^2 e^{1/3} \, x \, \text{Log}\left[ \left( \frac{\left( -1 \right)^{2/3} d^{1/3}}{e^{1/3}} + x \right] - e^{1/3} \, x \, \text{Log}\left[ \left( \frac{\left( -1 \right)^{1/3} d^{1/3}}{e^{1/3}} + x \right] - e^{1/3} \, x \, \text{Log}\left[ \left( \frac{\left( -1 \right)^{1/3} d^{1/3}}{e^{1/3}} + x \right] - e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} d^{1/3} + e^{1/3} \, x \right] \right) + e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} d^{1/3} + e^{1/3} \, x \right] \right) - e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} d^{1/3} + e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} d^{1/3} + e^{1/3} \, x \right] \right) + e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{2/3} d^{1/3} + e^{1/3} \, x \right] \right) + e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{2/3} d^{1/3} + e^{1/3} \, x \right] \right) + e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} e^{1/3} \, x \right] \right) + e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} e^{1/3} \, x \right] \right) \right) + e^{1/3} \, x \, \text{Log}\left[ \left( -1 \right)^{1/3} e$$

# Problem 169: Result more than twice size of optimal antiderivative.

$$\int \frac{Log \, [\, 1 + e \, x^n \, ]}{x} \, \mathrm{d} x$$

Optimal (type 4, 13 leaves, 1 step):

Result (type 4, 30 leaves):

$$\underline{\text{Log}\,[\, -\, e\; x^n\,] \;\, \text{Log}\,[\, 1+e\; x^n\,] \,\, + \text{PolyLog}\,[\, 2\, \text{, }\, 1+e\; x^n\,]}$$

Problem 174: Result more than twice size of optimal antiderivative.

$$\int \frac{Log \left[ \, c \, \left( \, d + e \, \, x^n \, \right)^{\, p} \, \right]^{\, 2}}{x} \, \, \mathrm{d} x$$

Optimal (type 4, 79 leaves, 5 steps):

$$\frac{\text{Log}\left[-\frac{e\,x^{n}}{d}\right]\,\text{Log}\left[\,c\,\left(\,d\,+\,e\,\,x^{n}\,\right)^{\,p}\,\right]^{\,2}}{n}\,+\,\frac{2\,p\,\text{Log}\left[\,c\,\left(\,d\,+\,e\,\,x^{n}\,\right)^{\,p}\,\right]\,\text{PolyLog}\left[\,2\,,\,\,1\,+\,\frac{e\,x^{n}}{d}\,\right]}{n}\,-\,\frac{2\,p^{2}\,\text{PolyLog}\left[\,3\,,\,\,1\,+\,\frac{e\,x^{n}}{d}\,\right]}{n}$$

Result (type 4, 164 leaves):

$$\begin{split} & \text{Log}\left[x\right] \, \left(-p \, \text{Log}\left[d + e \, x^n\right] + \text{Log}\left[c \, \left(d + e \, x^n\right)^p\right]\right)^2 + 2 \, p \, \left(-p \, \text{Log}\left[d + e \, x^n\right] + \text{Log}\left[c \, \left(d + e \, x^n\right)^p\right]\right) \\ & \left(\text{Log}\left[x\right] \, \left(\text{Log}\left[d + e \, x^n\right] - \text{Log}\left[1 + \frac{e \, x^n}{d}\right]\right) - \frac{\text{PolyLog}\left[2, \, -\frac{e \, x^n}{d}\right]}{n}\right) + \frac{1}{n} \\ & p^2 \, \left(\text{Log}\left[-\frac{e \, x^n}{d}\right] \, \text{Log}\left[d + e \, x^n\right]^2 + 2 \, \text{Log}\left[d + e \, x^n\right] \, \text{PolyLog}\left[2, \, 1 + \frac{e \, x^n}{d}\right] - 2 \, \text{PolyLog}\left[3, \, 1 + \frac{e \, x^n}{d}\right]\right) \end{split}$$

Problem 175: Result more than twice size of optimal antiderivative.

$$\int \frac{Log \left[ c \left( d + e \, x^n \right)^p \right]^3}{x} \, \mathrm{d}x$$

Optimal (type 4, 113 leaves, 6 steps):

$$\frac{Log\left[-\frac{e\,x^{n}}{d}\right]\,Log\left[c\,\left(d+e\,x^{n}\right)^{\,p}\right]^{\,3}}{n}\,+\,\frac{3\,p\,Log\left[c\,\left(d+e\,x^{n}\right)^{\,p}\right]^{\,2}\,PolyLog\left[2\,,\,1+\frac{e\,x^{n}}{d}\right]}{n}\,-\,\frac{6\,p^{2}\,Log\left[c\,\left(d+e\,x^{n}\right)^{\,p}\right]\,PolyLog\left[3\,,\,1+\frac{e\,x^{n}}{d}\right]}{n}\,+\,\frac{6\,p^{3}\,PolyLog\left[4\,,\,1+\frac{e\,x^{n}}{d}\right]}{n}$$

Result (type 4, 270 leaves):

$$\begin{split} &\frac{1}{n} \left( -n\,p^3\,Log\big[x\big]\,Log\big[d+e\,x^n\big]^3 + p^3\,Log\big[-\frac{e\,x^n}{d}\big]\,Log\big[d+e\,x^n\big]^3 + \\ &3\,n\,p^2\,Log\big[x\big]\,Log\big[d+e\,x^n\big]^2\,Log\big[c\,\left(d+e\,x^n\right)^p\big] - 3\,p^2\,Log\big[-\frac{e\,x^n}{d}\big]\,Log\big[d+e\,x^n\big]^2\,Log\big[c\,\left(d+e\,x^n\right)^p\big] - \\ &3\,n\,p\,Log\big[x\big]\,Log\big[d+e\,x^n\big]\,Log\big[c\,\left(d+e\,x^n\right)^p\big]^2 + 3\,p\,Log\big[-\frac{e\,x^n}{d}\big]\,Log\big[d+e\,x^n\big]\,Log\big[c\,\left(d+e\,x^n\right)^p\big]^2 + \\ &n\,Log\big[x\big]\,Log\big[c\,\left(d+e\,x^n\right)^p\big]^3 + 3\,p\,Log\big[c\,\left(d+e\,x^n\right)^p\big]^2\,PolyLog\big[2,\,1+\frac{e\,x^n}{d}\big] - \\ &6\,p^2\,Log\big[c\,\left(d+e\,x^n\right)^p\big]\,PolyLog\big[3,\,1+\frac{e\,x^n}{d}\big] + 6\,p^3\,PolyLog\big[4,\,1+\frac{e\,x^n}{d}\big] \right) \end{split}$$

Problem 188: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log\left[c\left(a+b\,x^2\right)^p\right]}{d+e\,x}\,\mathrm{d}x$$

Optimal (type 4, 201 leaves, 9 steps):

$$-\frac{p \, Log \left[\frac{e \, \left(\sqrt{-a} \, - \sqrt{b} \, x\right)}{\sqrt{b} \, d + \sqrt{-a} \, e}\right] \, Log \left[d + e \, x\right]}{e} - \frac{p \, Log \left[-\frac{e \, \left(\sqrt{-a} \, + \sqrt{b} \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right] \, Log \left[d + e \, x\right]}{e} + \\ \frac{Log \left[d + e \, x\right] \, Log \left[c \, \left(a + b \, x^2\right)^p\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d + \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, Poly Log \left[2, \, \frac{\sqrt{b} \, \left(d + e \, x\right)}{\sqrt{b}$$

#### Result (type 4, 262 leaves):

$$\begin{split} &\frac{1}{e}\left[-p\,Log\left[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\,[\,d+e\,x\,]\,\,-\right.\\ &p\,Log\left[\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\,[\,d+e\,x\,]\,+p\,Log\left[\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\left[\frac{\sqrt{b}\,\left(d+e\,x\right)}{\sqrt{b}\,d-\mathrm{i}\,\sqrt{a}\,e}\right]\,+\\ &p\,Log\left[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\left[\frac{\sqrt{b}\,\left(d+e\,x\right)}{\sqrt{b}\,d+\mathrm{i}\,\sqrt{a}\,e}\right]\,+Log\,[\,d+e\,x\,]\,\,Log\left[\,c\,\left(a+b\,x^2\right)^{\,p}\right]\,+\\ &p\,PolyLog\left[\,2\,,\,\frac{e\,\left(\sqrt{a}\,-\mathrm{i}\,\sqrt{b}\,x\right)}{\mathrm{i}\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+p\,PolyLog\left[\,2\,,\,\frac{e\,\left(\sqrt{a}\,+\mathrm{i}\,\sqrt{b}\,x\right)}{-\mathrm{i}\,\sqrt{b}\,d+\sqrt{a}\,e}\right] \end{split}$$

### Problem 206: Result is not expressed in closed-form.

$$\int (d + e x)^m Log[c (a + b x^3)^p] dx$$

Optimal (type 5, 301 leaves, 6 steps):

$$\begin{split} \frac{b^{1/3}\,p\,\left(\text{d}+\text{e}\,x\right)^{\,2+\text{m}}\,\text{Hypergeometric}2\text{F1}\!\left[\text{1, 2+m, 3+m, }\frac{b^{1/3}\,\left(\text{d}+\text{e}\,x\right)}{b^{1/3}\,d-\text{a}^{1/3}\,\text{e}}\right]}{\text{e}\,\left(b^{1/3}\,d-\text{a}^{1/3}\,\text{e}\right)\,\left(\text{1+m}\right)\,\left(\text{2+m}\right)} + \\ &\left(b^{1/3}\,p\,\left(\text{d}+\text{e}\,x\right)^{\,2+\text{m}}\,\text{Hypergeometric}2\text{F1}\!\left[\text{1, 2+m, 3+m, }\frac{b^{1/3}\,\left(\text{d}+\text{e}\,x\right)}{b^{1/3}\,d+\left(-1\right)^{\,1/3}\,\text{a}^{\,1/3}\,\text{e}}\right]\right] \middle/ \\ &\left(\text{e}\,\left(b^{1/3}\,d+\left(-1\right)^{\,1/3}\,\text{a}^{\,1/3}\,\text{e}\right)\,\left(\text{1+m}\right)\,\left(\text{2+m}\right)\right) + \\ &\left(b^{1/3}\,p\,\left(\text{d}+\text{e}\,x\right)^{\,2+\text{m}}\,\text{Hypergeometric}2\text{F1}\!\left[\text{1, 2+m, 3+m, }\frac{b^{1/3}\,\left(\text{d}+\text{e}\,x\right)}{b^{1/3}\,d-\left(-1\right)^{\,2/3}\,\text{a}^{\,1/3}\,\text{e}}\right]\right) \middle/ \\ &\left(\text{e}\,\left(b^{1/3}\,d-\left(-1\right)^{\,2/3}\,\text{a}^{\,1/3}\,\text{e}\right)\,\left(\text{1+m}\right)\,\left(\text{2+m}\right)\right) + \frac{\left(\text{d}+\text{e}\,x\right)^{\,1+\text{m}}\,\text{Log}\!\left[\text{c}\,\left(\text{a}+\text{b}\,x^3\right)^{\,p}\right]}{\text{e}\,\left(\text{1+m}\right)} \end{split}$$

Result (type 7, 399 leaves):

$$\frac{1}{b \text{ e m } \left(1+m\right)^2} \left(d+ex\right)^m \left(-\left(b \ d^3-a \ e^3\right) \ \left(1+m\right) \text{ p RootSum} \left[b \ d^3-a \ e^3-3 \ b \ d^2 \ \sharp 1+3 \ b \ d \ \sharp 1^2-b \ \sharp 1^3 \ \&, \right. \right. \\ \left. \frac{\text{Hypergeometric2F1} \left[-m,-m,1-m,-\frac{\sharp 1}{d+ex-\sharp 1}\right] \left(\frac{d+ex}{d+ex-\sharp 1}\right)^{-m}}{d^2-2 \ d \ \sharp 1+\sharp 1^2} \ \& \right] + \\ \left. b \left(m \ \left(d+ex\right) \ \left(-3 \ p+\left(1+m\right) \ \text{Log} \left[c \ \left(a+b \ x^3\right)^p\right]\right) + 2 \ d^2 \ \left(1+m\right) \text{ p RootSum} \left[b \ d^3-a \ e^3-3 \ b \ d^2 \ \sharp 1+3 \ b \ d \ \sharp 1^2 - b \ \sharp 1^3 \ \&, \right. \right. \\ \left. \left. d \ \left(1+m\right) \text{ p RootSum} \left[b \ d^3-a \ e^3-3 \ b \ d^2 \ \sharp 1+3 \ b \ d \ \sharp 1^2-b \ \sharp 1^3 \ \&, \right. \\ \left. d^2-2 \ d \ \sharp 1+\sharp 1^2 \ d^2-2 \ d \ \sharp 1+\sharp 1^2 \right. \\ \left. d^2-2 \ d \ \sharp 1+\sharp 1^2 \ \& \right] \right| \\ \left. d^2-2 \ d \ \sharp 1+\sharp 1^2 \ \& \right] \right|$$

### Problem 207: Result unnecessarily involves imaginary or complex numbers.

$$\int (d + e x)^m Log[c (a + b x^2)^p] dx$$

Optimal (type 5, 205 leaves, 5 steps):

$$\frac{\sqrt{b} \ p \ \left( \text{d} + \text{e} \ x \right)^{2+m} \ \text{Hypergeometric2F1} \left[ \text{1, 2+m, 3+m, } \frac{\sqrt{b} \ \left( \text{d} + \text{e} \ x \right)}{\sqrt{b} \ d - \sqrt{-a} \ e} \right]}{e \left( \sqrt{b} \ d - \sqrt{-a} \ e \right) \ \left( \text{1+m} \right) \ \left( \text{2+m} \right)} + \frac{e \left( \sqrt{b} \ d + e \ x \right)^{2+m} \ \text{Hypergeometric2F1} \left[ \text{1, 2+m, 3+m, } \frac{\sqrt{b} \ \left( \text{d} + \text{e} \ x \right)}{\sqrt{b} \ d + \sqrt{-a} \ e} \right]}{e \left( \sqrt{b} \ d + \sqrt{-a} \ e \right) \ \left( \text{1+m} \right) \ \left( \text{2+m} \right)} + \frac{\left( \text{d} + e \ x \right)^{1+m} \ \text{Log} \left[ c \ \left( \text{a} + b \ x^2 \right)^p \right]}{e \ \left( \text{1+m} \right)}$$

Result (type 5, 285 leaves):

$$\begin{split} &\frac{1}{\sqrt{b}~e~m~\left(1+m\right)^{2}}\left(d+e~x\right)^{m}\left(-\left(\sqrt{b}~d+i~\sqrt{a}~e\right)~\left(1+m\right)~p\left(\frac{\sqrt{b}~\left(d+e~x\right)}{e~\left(-i~\sqrt{a}~+\sqrt{b}~x\right)}\right)^{-m} \\ &\text{Hypergeometric} 2F1\big[-m,~-m,~1-m,~\frac{\sqrt{b}~d+i~\sqrt{a}~e}{i~\sqrt{a}~e-\sqrt{b}~e~x}\big]-\left(\sqrt{b}~d-i~\sqrt{a}~e\right)~\left(1+m\right) \\ &p\left(\frac{\sqrt{b}~\left(d+e~x\right)}{e~\left(i~\sqrt{a}~+\sqrt{b}~x\right)}\right)^{-m} \\ &\text{Hypergeometric} 2F1\big[-m,~-m,~1-m,~-\frac{\sqrt{b}~d-i~\sqrt{a}~e}{i~\sqrt{a}~e+\sqrt{b}~e~x}\big]+\\ &\sqrt{b}~m~\left(d+e~x\right)~\left(-2~p+\left(1+m\right)~Log\big[c~\left(a+b~x^{2}\right)^{p}\big]\right) \end{split}$$

## Problem 210: Result unnecessarily involves imaginary or complex numbers.

$$\int \left(d+e\;x\right)^m\;Log\left[\;c\;\left(a+\frac{b}{x^2}\right)^p\right]\;\text{d}\;x$$

Optimal (type 5, 257 leaves, 9 steps):

$$\frac{\sqrt{-a} \ p \ \left(d + e \ x\right)^{2 + m} \ Hypergeometric 2F1 \left[1, \ 2 + m, \ 3 + m, \ \frac{\sqrt{-a} \ \left(d + e \ x\right)}{\sqrt{-a} \ d - \sqrt{b} \ e}\right]}{e \ \left(\sqrt{-a} \ d - \sqrt{b} \ e\right) \ \left(1 + m\right) \ \left(2 + m\right)} + \\ \frac{\sqrt{-a} \ p \ \left(d + e \ x\right)^{2 + m} \ Hypergeometric 2F1 \left[1, \ 2 + m, \ 3 + m, \ \frac{\sqrt{-a} \ \left(d + e \ x\right)}{\sqrt{-a} \ d + \sqrt{b} \ e}\right]}{e \ \left(\sqrt{-a} \ d + \sqrt{b} \ e\right) \ \left(1 + m\right) \ \left(2 + m\right)} - \\ \frac{2 \ p \ \left(d + e \ x\right)^{2 + m} \ Hypergeometric 2F1 \left[1, \ 2 + m, \ 3 + m, \ 1 + \frac{e \ x}{d}\right]}{d \ e \ \left(2 + 3 \ m + m^2\right)} + \frac{\left(d + e \ x\right)^{1 + m} \ Log \left[c \ \left(a + \frac{b}{x^2}\right)^p\right]}{e \ \left(1 + m\right)}$$

Result (type 5, 310 leaves):

$$\begin{split} &\frac{1}{e\,\mathsf{m}\,\left(1+\mathsf{m}\right)} \\ &\left(\mathsf{d}+\mathsf{e}\,\mathsf{x}\right)^\mathsf{m} \left(2\,\mathsf{d}\,\mathsf{p}\,\left(1+\frac{\mathsf{d}}{\mathsf{e}\,\mathsf{x}}\right)^{-\mathsf{m}}\,\mathsf{Hypergeometric}2\mathsf{F1}\big[-\mathsf{m},\,-\mathsf{m},\,1-\mathsf{m},\,-\frac{\mathsf{d}}{\mathsf{e}\,\mathsf{x}}\big] - \frac{1}{\sqrt{\mathsf{a}}}\left(\sqrt{\mathsf{a}}\,\,\mathsf{d}+\dot{\imath}\,\sqrt{\mathsf{b}}\,\,\mathsf{e}\right) \\ &\mathsf{p}\left(\frac{\sqrt{\mathsf{a}}\,\left(\mathsf{d}+\mathsf{e}\,\mathsf{x}\right)}{\mathsf{e}\,\left(-\dot{\imath}\,\sqrt{\mathsf{b}}\,+\sqrt{\mathsf{a}}\,\,\mathsf{x}\right)}\right)^{-\mathsf{m}}\,\mathsf{Hypergeometric}2\mathsf{F1}\big[-\mathsf{m},\,-\mathsf{m},\,1-\mathsf{m},\,\frac{\sqrt{\mathsf{a}}\,\,\mathsf{d}+\dot{\imath}\,\sqrt{\mathsf{b}}\,\,\mathsf{e}}{\dot{\imath}\,\sqrt{\mathsf{b}}\,\,\mathsf{e}-\sqrt{\mathsf{a}}\,\,\mathsf{e}\,\mathsf{x}}\big] - \\ &\frac{1}{\sqrt{\mathsf{a}}}\left(\sqrt{\mathsf{a}}\,\,\mathsf{d}-\dot{\imath}\,\sqrt{\mathsf{b}}\,\,\mathsf{e}\right)\,\mathsf{p}\left(\frac{\sqrt{\mathsf{a}}\,\left(\mathsf{d}+\mathsf{e}\,\mathsf{x}\right)}{\mathsf{e}\,\left(\dot{\imath}\,\sqrt{\mathsf{b}}\,+\sqrt{\mathsf{a}}\,\,\mathsf{x}\right)}\right)^{-\mathsf{m}} \\ &\mathsf{Hypergeometric}2\mathsf{F1}\big[-\mathsf{m},\,-\mathsf{m},\,1-\mathsf{m},\,-\frac{\sqrt{\mathsf{a}}\,\,\mathsf{d}-\dot{\imath}\,\sqrt{\mathsf{b}}\,\,\mathsf{e}}{\dot{\imath}\,\sqrt{\mathsf{b}}\,\,\mathsf{e}+\sqrt{\mathsf{a}}\,\,\mathsf{e}\,\mathsf{x}}\big] + \mathsf{m}\,\left(\mathsf{d}+\mathsf{e}\,\mathsf{x}\right)\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{a}+\frac{\mathsf{b}}{\mathsf{x}^2}\right)^\mathsf{p}\big] \\ \end{split}$$

# Problem 216: Attempted integration timed out after 120 seconds.

$$\int \frac{Log\left[\left.c\,\left(d+e\,x^{n}\right)^{\,p}\right.\right]}{f+g\,x}\,\mathrm{d}x$$

Optimal (type 8, 23 leaves, 0 steps):

Int 
$$\left[\frac{Log\left[c\left(d+ex^{n}\right)^{p}\right]}{f+gx}, x\right]$$

Result (type 1, 1 leaves):

???

### Problem 226: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^3 \, \mathsf{Log} \left[ c \, \left( \mathsf{a} + \mathsf{b} \, \mathsf{x}^2 \right)^{\mathsf{p}} \right]}{\mathsf{d} + \mathsf{e} \, \mathsf{x}} \, \mathrm{d} \mathsf{x}$$

Optimal (type 4, 394 leaves, 21 steps):

$$-\frac{2\,d^{2}\,p\,x}{e^{3}} + \frac{2\,a\,p\,x}{3\,b\,e} + \frac{d\,p\,x^{2}}{2\,e^{2}} - \frac{2\,p\,x^{3}}{9\,e} + \frac{2\,\sqrt{a}\,d^{2}\,p\,\text{ArcTan}\Big[\frac{\sqrt{b}\,x}{\sqrt{a}}\Big]}{\sqrt{b}\,e^{3}} - \frac{2\,a^{3/2}\,p\,\text{ArcTan}\Big[\frac{\sqrt{b}\,x}{\sqrt{a}}\Big]}{3\,b^{3/2}\,e} + \frac{d^{3}\,p\,\text{Log}\Big[\frac{e\,\left(\sqrt{-a}\,-\sqrt{b}\,x\right)}{\sqrt{b}\,d+\sqrt{-a}\,e}\Big]\,\text{Log}\,[d+e\,x]}{e^{4}} + \frac{d^{3}\,p\,\text{Log}\Big[-\frac{e\,\left(\sqrt{-a}\,+\sqrt{b}\,x\right)}{\sqrt{b}\,d-\sqrt{-a}\,e}\Big]\,\text{Log}\,[d+e\,x]}{e^{4}} + \frac{d^{2}\,x\,\text{Log}\Big[c\,\left(a+b\,x^{2}\right)^{p}\Big]}{3\,e} - \frac{d\,\left(a+b\,x^{2}\right)\,\text{Log}\Big[c\,\left(a+b\,x^{2}\right)^{p}\Big]}{2\,b\,e^{2}} - \frac{d^{3}\,p\,\text{PolyLog}\Big[2\,,\frac{\sqrt{b}\,(d+e\,x)}{\sqrt{b}\,d-\sqrt{-a}\,e}\Big]}{e^{4}} + \frac{d^{3}\,p\,\text{PolyLog}\Big[2\,,\frac{\sqrt{b}\,(d+e\,x)}{\sqrt{b}\,d-\sqrt{a}\,e}\Big]}{e^{4}} + \frac{d^{3}\,p\,\text{PolyLog}\Big[2\,,\frac{\sqrt{b}\,(d+e\,x)}{\sqrt{b}\,d-\sqrt{a}\,e}\Big]}{e^{4}} + \frac{d^{3}\,p\,\text{PolyLog}\Big[2\,,\frac{\sqrt{b}\,(d+e\,x)}{\sqrt{b}\,d-\sqrt{a}\,e}\Big]}{e^{4}} + \frac{d^{3}\,p\,\text{PolyLog}\Big[2\,,\frac{\sqrt{b}\,(d+e\,x)}{$$

Result (type 4, 509 leaves):

$$-\frac{1}{18\,e^4}\left[36\,d^2\,e\,p\,x\,-\,\frac{12\,a\,e^3\,p\,x}{b}\,-\,9\,d\,e^2\,p\,x^2\,+\,4\,e^3\,p\,x^3\,+\,\frac{12\,a^{3/2}\,e^3\,p\,ArcTan\left[\frac{\sqrt{b}\cdot x}{\sqrt{a}}\right]}{b^{3/2}}\,+\,\frac{18\,i\,\sqrt{a}\,d^2\,e\,p\,Log\left[\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\right]}{\sqrt{b}}\,-\,\frac{18\,i\,\sqrt{a}\,d^2\,e\,p\,Log\left[\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\right]}{\sqrt{b}}\,-\,\frac{18\,d^3\,p\,Log\left[-\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\right]\,Log\left[d+e\,x\right]\,-\,18\,d^3\,p\,Log\left[\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\right]\,Log\left[d+e\,x\right]\,+\,\frac{18\,d^3\,p\,Log\left[\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\right]\,Log\left[\frac{\sqrt{b}\,\left(d+e\,x\right)}{\sqrt{b}\,d-i\,\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,Log\left[-\frac{i\,\sqrt{a}}{\sqrt{b}}\,+\,x\right]\,Log\left[\frac{\sqrt{b}\,\left(d+e\,x\right)}{\sqrt{b}\,d+i\,\sqrt{a}\,e}\right]\,+\,\frac{9\,a\,d\,e^2\,p\,Log\left[a+b\,x^2\right]}{b}\,-\,18\,d^2\,e\,x\,Log\left[c\,\left(a+b\,x^2\right)^p\right]\,+\,9\,d\,e^2\,x^2\,Log\left[c\,\left(a+b\,x^2\right)^p\right]\,-\,6\,e^3\,x^3\,Log\left[c\,\left(a+b\,x^2\right)^p\right]\,+\,18\,d^3\,Log\left[d+e\,x\right]\,Log\left[c\,\left(a+b\,x^2\right)^p\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,-\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]}\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]}\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]}\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]}\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]}\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]}\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]}\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]}\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{a}\,+i\,\sqrt{b}\,x\right)}{i\,\sqrt{b}\,d+\sqrt{a}\,e}\right]}\,+\,18\,d^3\,p\,PolyLog\left[2\,\frac{e\,\left(\sqrt{$$

Problem 227: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2 \, \mathsf{Log} \left[ \, c \, \left( \, \mathsf{a} + \mathsf{b} \, \, \mathsf{x}^2 \, \right)^{\, \mathsf{p}} \, \right]}{\mathsf{d} + \mathsf{e} \, \, \mathsf{x}} \, \, \mathrm{d} \, \mathsf{x}$$

Optimal (type 4, 313 leaves, 17 steps):

$$\frac{2\,d\,p\,x}{e^{2}} - \frac{p\,x^{2}}{2\,e} - \frac{2\,\sqrt{a}\,d\,p\,\text{ArcTan}\Big[\frac{\sqrt{b}\,\,x}{\sqrt{a}}\Big]}{\sqrt{b}\,e^{2}} - \frac{d^{2}\,p\,\text{Log}\Big[\frac{e\,\left(\sqrt{-a}\,-\sqrt{b}\,\,x\right)}{\sqrt{b}\,d+\sqrt{-a}\,e}\,\Big]\,\text{Log}\,[d+e\,x]}{e^{3}} - \frac{d^{2}\,p\,\text{Log}\Big[\frac{e\,\left(\sqrt{-a}\,-\sqrt{b}\,\,x\right)}{\sqrt{b}\,d+\sqrt{-a}\,e}\,\Big]\,\text{Log}\,[d+e\,x]}{e^{2}} + \frac{\left(a+b\,x^{2}\right)\,\text{Log}\,\Big[c\,\left(a+b\,x^{2}\right)^{p}\Big]}{2\,b\,e} + \frac{d^{2}\,\text{Log}\,\Big[c\,\left(a+b\,x^{2}\right)^{p}\Big]}{2\,b\,e} + \frac{d^{2}\,\text{Log}\,\Big[c\,\left(a+b\,x^{2}\right)^{p}\Big]}{2\,b\,e} + \frac{d^{2}\,\text{PolyLog}\,\Big[c\,\left(a+b\,x^{2}\right)^{p}\Big]}{2\,b\,e} + \frac{d^{2}\,\text{PolyLog}\,\Big[c\,\left(a+b\,x^$$

Result (type 4, 438 leaves):

$$\frac{1}{2 \, b \, e^3} \left( 4 \, b \, d \, e \, p \, x - b \, e^2 \, p \, x^2 + 2 \, i \, \sqrt{a} \, \sqrt{b} \, d \, e \, p \, \text{Log} \Big[ - \frac{i \, \sqrt{a}}{\sqrt{b}} + x \Big] - 2 \, b \, d^2 \, p \, \text{Log} \Big[ - \frac{i \, \sqrt{a}}{\sqrt{b}} + x \Big] \, \text{Log} [d + e \, x] - 2 \, b \, d^2 \, p \, \text{Log} \Big[ - \frac{i \, \sqrt{a}}{\sqrt{b}} + x \Big] \, \text{Log} [d + e \, x] - 2 \, b \, d^2 \, p \, \text{Log} \Big[ \frac{i \, \sqrt{a}}{\sqrt{b}} + x \Big] \, \text{Log} \Big[ \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - i \, \sqrt{a} \, e} \Big] + 2 \, b \, d^2 \, p \, \text{Log} \Big[ \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - i \, \sqrt{a} \, e} \Big] + 2 \, b \, d^2 \, p \, \text{Log} \Big[ a + b \, x^2 \Big] - 2 \, b \, d \, e \, x \, \text{Log} \Big[ c \, \left( a + b \, x^2 \right)^p \Big] + b \, e^2 \, x^2 \, \text{Log} \Big[ c \, \left( a + b \, x^2 \right)^p \Big] + 2 \, b \, d^2 \, \text{Log} \Big[ d + e \, x \Big] \, \text{Log} \Big[ c \, \left( a + b \, x^2 \right)^p \Big] + 2 \, b \, d^2 \, p \, \text{PolyLog} \Big[ 2 , \frac{e \, \left( \sqrt{a} + i \, \sqrt{b} \, x \right)}{i \, \sqrt{b} \, d + \sqrt{a} \, e} \Big] + 2 \, b \, d^2 \, p \, \text{PolyLog} \Big[ 2 , \frac{e \, \left( \sqrt{a} + i \, \sqrt{b} \, x \right)}{-i \, \sqrt{b} \, d + \sqrt{a} \, e} \Big]$$

## Problem 228: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x \log \left[c \left(a + b x^{2}\right)^{p}\right]}{d + e x} dx$$

Optimal (type 4, 256 leaves, 14 steps):

$$-\frac{2 p x}{e} + \frac{2 \sqrt{a} p ArcTan \left[\frac{\sqrt{b} x}{\sqrt{a}}\right]}{\sqrt{b} e} + \frac{d p Log \left[\frac{e \left(\sqrt{-a} - \sqrt{b} x\right)}{\sqrt{b} d + \sqrt{-a} e}\right] Log [d + e x]}{e^{2}} + \frac{d p Log \left[-\frac{e \left(\sqrt{-a} + \sqrt{b} x\right)}{\sqrt{b} d - \sqrt{-a} e}\right] Log [d + e x]}{e^{2}} + \frac{x Log \left[c \left(a + b x^{2}\right)^{p}\right]}{e} - \frac{d Log \left[d + e x\right] Log \left[c \left(a + b x^{2}\right)^{p}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d - \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d + \sqrt{-a} e}\right]}{e^{2}} + \frac{d p PolyLog \left[2, \frac{\sqrt{b} (d + e x)}{\sqrt{b} d$$

Result (type 4, 357 leaves):

$$\begin{split} &-\frac{1}{e^2}\left[2\,e\,p\,x+\frac{\mathrm{i}\,\sqrt{a}\,\,e\,p\,Log\left[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]}{\sqrt{b}}-\frac{\mathrm{i}\,\sqrt{a}\,\,e\,p\,Log\left[\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]}{\sqrt{b}}-\right.\\ &d\,p\,Log\left[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\,[d+e\,x]-d\,p\,Log\left[\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\,[d+e\,x]+\\ &d\,p\,Log\left[\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\left[\frac{\sqrt{b}\,\,(d+e\,x)}{\sqrt{b}\,\,d-\mathrm{i}\,\sqrt{a}\,\,e}\right]+d\,p\,Log\left[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\left[\frac{\sqrt{b}\,\,(d+e\,x)}{\sqrt{b}\,\,d+\mathrm{i}\,\sqrt{a}\,\,e}\right]-\\ &e\,x\,Log\left[c\,\,(a+b\,x^2)^p\right]+d\,Log\,[d+e\,x]\,Log\left[c\,\,(a+b\,x^2)^p\right]+\\ &d\,p\,PolyLog\left[2\,,\,\frac{e\,\left(\sqrt{a}\,-\mathrm{i}\,\sqrt{b}\,\,x\right)}{\mathrm{i}\,\sqrt{b}\,\,d+\sqrt{a}\,\,e}\right]+d\,p\,PolyLog\left[2\,,\,\frac{e\,\left(\sqrt{a}\,+\mathrm{i}\,\sqrt{b}\,\,x\right)}{-\mathrm{i}\,\sqrt{b}\,\,d+\sqrt{a}\,\,e}\right] \end{split}$$

## Problem 229: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log\left[\left.c\,\left(a+b\,x^2\right)^{\,p}\right.\right]}{d+e\,x} \, \mathrm{d}x$$

Optimal (type 4, 201 leaves, 9 steps):

$$-\frac{p \, Log \left[\frac{e \left(\sqrt{-a} - \sqrt{b} \, x\right)}{\sqrt{b} \, d + \sqrt{-a} \, e}\right] \, Log \left[d + e \, x\right]}{e} - \frac{p \, Log \left[-\frac{e \left(\sqrt{-a} + \sqrt{b} \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right] \, Log \left[d + e \, x\right]}{e} + \\ \frac{Log \left[d + e \, x\right] \, Log \left[c \, \left(a + b \, x^2\right)^p\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d + \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\right]}{e} - \frac{p \, PolyLog \left[2, \frac{\sqrt{b} \, (d$$

Result (type 4, 262 leaves):

$$\begin{split} &\frac{1}{e}\left[-p\,Log\left[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\,[\,d+e\,x\,]\,\,-\right.\\ &p\,Log\left[\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\,[\,d+e\,x\,]\,+p\,Log\left[\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\left[\frac{\sqrt{b}\,\left(d+e\,x\right)}{\sqrt{b}\,d-\mathrm{i}\,\sqrt{a}\,e}\right]\,+\\ &p\,Log\left[-\frac{\mathrm{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,Log\left[\frac{\sqrt{b}\,\left(d+e\,x\right)}{\sqrt{b}\,d+\mathrm{i}\,\sqrt{a}\,e}\right]\,+Log\,[\,d+e\,x\,]\,\,Log\left[\,c\,\left(a+b\,x^2\right)^p\right]\,+\\ &p\,PolyLog\left[\,2\,,\,\frac{e\,\left(\sqrt{a}\,-\mathrm{i}\,\sqrt{b}\,x\right)}{\mathrm{i}\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,+p\,PolyLog\left[\,2\,,\,\frac{e\,\left(\sqrt{a}\,+\mathrm{i}\,\sqrt{b}\,x\right)}{-\mathrm{i}\,\sqrt{b}\,d+\sqrt{a}\,e}\right]\,\end{split}$$

# Problem 230: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log\left[\left.c\right.\left(a+b\right.x^{2}\right)^{p}\right]}{x\left.\left(d+e\right.x\right)}\,\mathrm{d}x$$

Optimal (type 4, 247 leaves, 14 steps):

$$\frac{p \, Log \Big[\frac{e \, \left(\sqrt{-a} \, -\sqrt{b} \, x\right)}{\sqrt{b} \, d + \sqrt{-a} \, e}\Big] \, Log \, [d + e \, x]}{d} + \frac{p \, Log \Big[-\frac{e \, \left(\sqrt{-a} \, +\sqrt{b} \, x\right)}{\sqrt{b} \, d - \sqrt{-a} \, e}\Big] \, Log \, [d + e \, x]}{d} + \\ \frac{Log \Big[-\frac{b \, x^2}{a}\Big] \, Log \Big[c \, \left(a + b \, x^2\right)^p\Big]}{2 \, d} - \frac{Log \, [d + e \, x] \, Log \Big[c \, \left(a + b \, x^2\right)^p\Big]}{d} + \\ \frac{p \, Poly Log \Big[2, \, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d - \sqrt{-a} \, e}\Big]}{d} + \frac{p \, Poly Log \Big[2, \, \frac{\sqrt{b} \, (d + e \, x)}{\sqrt{b} \, d + \sqrt{-a} \, e}\Big]}{d} + \frac{p \, Poly Log \Big[2, \, 1 + \frac{b \, x^2}{a}\Big]}{2 \, d}$$

Result (type 4, 361 leaves):

$$-\frac{1}{d}\left(p \ \text{Log}\left[x\right] \ \text{Log}\left[1-\frac{i\sqrt{b} \ x}{\sqrt{a}}\right] + p \ \text{Log}\left[x\right] \ \text{Log}\left[1+\frac{i\sqrt{b} \ x}{\sqrt{a}}\right] - p \ \text{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \ \text{Log}\left[d+e \ x\right] - p \ \text{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \ \text{Log}\left[d+e \ x\right] + p \ \text{Log}\left[\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \ \text{Log}\left[\frac{\sqrt{b} \ (d+e \ x)}{\sqrt{b} \ d-i\sqrt{a} \ e}\right] + p \ \text{Log}\left[-\frac{i\sqrt{a}}{\sqrt{b}} + x\right] \ \text{Log}\left[\frac{\sqrt{b} \ (d+e \ x)}{\sqrt{b} \ d+i\sqrt{a} \ e}\right] - \text{Log}\left[x\right] \ \text{Log}\left[c \ (a+b \ x^2)^p\right] + p \ \text{Log}\left[d+e \ x\right] \ \text{Log}\left[c \ (a+b \ x^2)^p\right] + p \ \text{PolyLog}\left[2, -\frac{i\sqrt{b} \ x}{\sqrt{a}}\right] + p \ \text{PolyLog}\left[2, \frac{i\sqrt{b} \ x}{\sqrt{a$$

# Problem 231: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log\left[\left.c\right.\left(a+b\right.x^{2}\right)^{p}\right]}{x^{2}\,\left(d+e\left.x\right)}\,\mathrm{d}x$$

Optimal (type 4, 306 leaves, 16 steps):

$$\frac{2\,\sqrt{b}\,\,p\,\text{ArcTan}\!\left[\frac{\sqrt{b}\,\,x}{\sqrt{a}}\right]}{\sqrt{a}\,\,d} - \frac{e\,p\,\text{Log}\!\left[\frac{e\,\left(\sqrt{-a}\,-\sqrt{b}\,\,x\right)}{\sqrt{b}\,\,d+\sqrt{-a}\,\,e}\right]\,\text{Log}\!\left[d+e\,x\right]}{d^2} - \frac{e\,p\,\text{Log}\!\left[-\frac{e\,\left(\sqrt{-a}\,+\sqrt{b}\,\,x\right)}{\sqrt{b}\,\,d-\sqrt{-a}\,\,e}\right]\,\text{Log}\!\left[d+e\,x\right]}{d^2} - \frac{e\,\text{Log}\!\left[c\,\left(a+b\,x^2\right)^p\right]}{d^2} - \frac{e\,\text{Log}\!\left[c\,\left(a+b\,x^2\right)^p\right]}{2\,d^2} + \frac{e\,\text{Log}\!\left[d+e\,x\right]\,\text{Log}\!\left[c\,\left(a+b\,x^2\right)^p\right]}{d^2} - \frac{e\,p\,\text{PolyLog}\!\left[2\,,\frac{\sqrt{b}\,\,(d+e\,x)}{\sqrt{b}\,\,d-\sqrt{-a}\,\,e}\right]}{d^2} - \frac{e\,p\,\text{PolyLog}\!\left[2\,,\frac{\sqrt{b}\,\,(d+e\,x)}{\sqrt{b}\,\,d+\sqrt{-a}\,\,e}\right]}{d^2} - \frac{e\,p\,\text{PolyLog}\!\left[2\,,\,1+\frac{b\,x^2}{a}\right]}{2\,d^2}$$

Result (type 4, 417 leaves):

$$\begin{split} &\frac{1}{d^2} \left( \frac{2 \sqrt{b} \ d \, p \, \text{ArcTan} \left[ \frac{\sqrt{b} \ x}{\sqrt{a}} \right]}{\sqrt{a}} + e \, p \, \text{Log} \left[ x \right] \, \text{Log} \left[ 1 - \frac{i \, \sqrt{b} \, x}{\sqrt{a}} \right] + \\ &e \, p \, \text{Log} \left[ x \right] \, \text{Log} \left[ 1 + \frac{i \, \sqrt{b} \, x}{\sqrt{a}} \right] - e \, p \, \text{Log} \left[ - \frac{i \, \sqrt{a}}{\sqrt{b}} + x \right] \, \text{Log} \left[ d + e \, x \right] - \\ &e \, p \, \text{Log} \left[ \frac{i \, \sqrt{a}}{\sqrt{b}} + x \right] \, \text{Log} \left[ d + e \, x \right] + e \, p \, \text{Log} \left[ \frac{i \, \sqrt{a}}{\sqrt{b}} + x \right] \, \text{Log} \left[ \frac{\sqrt{b} \, \left( d + e \, x \right)}{\sqrt{b} \, d - i \, \sqrt{a} \, e} \right] + \\ &e \, p \, \text{Log} \left[ - \frac{i \, \sqrt{a}}{\sqrt{b}} + x \right] \, \text{Log} \left[ \frac{\sqrt{b} \, \left( d + e \, x \right)}{\sqrt{b} \, d + i \, \sqrt{a} \, e} \right] - \frac{d \, \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right]}{x} - e \, \text{Log} \left[ x \right] \, \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right] + \\ &e \, \text{Log} \left[ d + e \, x \right] \, \text{Log} \left[ c \, \left( a + b \, x^2 \right)^p \right] + e \, p \, \text{PolyLog} \left[ 2 \, , \, - \frac{i \, \sqrt{b} \, x}{\sqrt{a}} \right] + e \, p \, \text{PolyLog} \left[ 2 \, , \, \frac{i \, \sqrt{b} \, x}{\sqrt{a}} \right] + \\ &e \, p \, \text{PolyLog} \left[ 2 \, , \, \frac{e \, \left( \sqrt{a} - i \, \sqrt{b} \, x \right)}{i \, \sqrt{b} \, d + \sqrt{a} \, e} \right] + e \, p \, \text{PolyLog} \left[ 2 \, , \, \frac{e \, \left( \sqrt{a} + i \, \sqrt{b} \, x \right)}{-i \, \sqrt{b} \, d + \sqrt{a} \, e} \right] \end{split}$$

## Problem 232: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log\left[\left.c\right.\left(a+b\right.x^{2}\right)^{p}\right]}{x^{3}\,\left(d+e\left.x\right.\right)}\,\mathrm{d}x$$

Optimal (type 4, 371 leaves, 21 steps):

$$-\frac{2\sqrt{b} \ e \ p \ ArcTan \left[\frac{\sqrt{b} \ x}{\sqrt{a}}\right]}{\sqrt{a} \ d^{2}} + \frac{b \ p \ Log \left[x\right]}{a \ d} + \frac{e^{2} \ p \ Log \left[\frac{e \left(\sqrt{-a} - \sqrt{b} \ x\right)}{\sqrt{b} \ d + \sqrt{-a} \ e}\right] \ Log \left[d + e \ x\right]}{d^{3}} + \frac{e^{2} \ p \ Log \left[d + e \ x\right]}{d^{3}} - \frac{b \ p \ Log \left[a + b \ x^{2}\right]}{2 \ a \ d} - \frac{Log \left[c \ \left(a + b \ x^{2}\right)^{p}\right]}{2 \ d \ x^{2}} + \frac{e^{2} \ Log \left[c \ \left(a + b \ x^{2}\right)^{p}\right]}{d^{3}} + \frac{e^{2} \ Log \left[-\frac{b \ x^{2}}{a}\right] \ Log \left[c \ \left(a + b \ x^{2}\right)^{p}\right]}{2 \ d^{3}} - \frac{e^{2} \ Log \left[d + e \ x\right] \ Log \left[c \ \left(a + b \ x^{2}\right)^{p}\right]}{d^{3}} + \frac{e^{2} \ p \ PolyLog \left[2, \frac{\sqrt{b} \ \left(d + e \ x\right)}{\sqrt{b} \ d - \sqrt{-a} \ e}\right]}{d^{3}} + \frac{e^{2} \ p \ PolyLog \left[2, \frac{\sqrt{b} \ \left(d + e \ x\right)}{\sqrt{b} \ d + \sqrt{-a} \ e}\right]}{d^{3}} + \frac{e^{2} \ p \ PolyLog \left[2, 1 + \frac{b \ x^{2}}{a}\right]}{2 \ d^{3}}$$

Result (type 4, 503 leaves):

$$\begin{split} &-\frac{1}{2\,d^3}\left(\frac{4\,\sqrt{b}\,\,d\,e\,p\,\text{ArcTan}\Big[\frac{\sqrt{b}\,\,x}{\sqrt{a}}\Big]}{\sqrt{a}} - \frac{2\,b\,d^2\,p\,\text{Log}\,[\,x\,]}{a} + 2\,e^2\,p\,\text{Log}\,[\,x\,]\,\,\text{Log}\,[\,1 - \frac{\mathrm{i}\,\,\sqrt{b}\,\,x}{\sqrt{a}}\,] + \\ &-2\,e^2\,p\,\text{Log}\,[\,1 + \frac{\mathrm{i}\,\,\sqrt{b}\,\,x}{\sqrt{a}}\,] - 2\,e^2\,p\,\text{Log}\,[\,-\frac{\mathrm{i}\,\,\sqrt{a}}{\sqrt{b}} + x\,]\,\,\text{Log}\,[\,d + e\,x\,] - \\ &-2\,e^2\,p\,\text{Log}\,[\,\frac{\mathrm{i}\,\,\sqrt{a}}{\sqrt{b}} + x\,]\,\,\text{Log}\,[\,d + e\,x\,] + 2\,e^2\,p\,\text{Log}\,[\,\frac{\mathrm{i}\,\,\sqrt{a}}{\sqrt{b}} + x\,]\,\,\text{Log}\,[\,\frac{\sqrt{b}\,\,(d + e\,x)}{\sqrt{b}\,\,d - \mathrm{i}\,\,\sqrt{a}\,\,e}\,] + \\ &-2\,e^2\,p\,\text{Log}\,[\,-\frac{\mathrm{i}\,\,\sqrt{a}}{\sqrt{b}} + x\,]\,\,\text{Log}\,[\,\frac{\sqrt{b}\,\,(d + e\,x)}{\sqrt{b}\,\,d + \mathrm{i}\,\,\sqrt{a}\,\,e}\,] + \frac{b\,d^2\,p\,\text{Log}\,[\,a + b\,x^2\,]}{a} + \\ &-\frac{d^2\,\text{Log}\,[\,c\,\,(\,a + b\,x^2\,)^{\,p}\,]}{x^2} - \frac{2\,d\,e\,\text{Log}\,[\,c\,\,(\,a + b\,x^2\,)^{\,p}\,]}{x} - 2\,e^2\,\text{Log}\,[\,x\,]\,\,\text{Log}\,[\,c\,\,(\,a + b\,x^2\,)^{\,p}\,] + \\ &-2\,e^2\,\text{Log}\,[\,d + e\,x\,]\,\,\text{Log}\,[\,c\,\,(\,a + b\,x^2\,)^{\,p}\,] + 2\,e^2\,p\,\text{PolyLog}\,[\,2\,,\,\,\frac{\mathrm{i}\,\,\sqrt{b}\,\,x}{\sqrt{a}}\,] + 2\,e^2\,p\,\text{PolyLog}\,[\,2\,,\,\,\frac{\mathrm{i}\,\,\sqrt{b}\,\,x}{\sqrt{a}}\,] + \\ &-2\,e^2\,p\,\text{PolyLog}\,[\,2\,,\,\,\frac{\mathrm{e}\,\,(\,\sqrt{a}\,-\,\mathrm{i}\,\,\sqrt{b}\,\,x}{\sqrt{a}\,\,e}\,] + 2\,e^2\,p\,\text{PolyLog}\,[\,2\,,\,\,\frac{\mathrm{e}\,\,(\,\sqrt{a}\,+\,\mathrm{i}\,\,\sqrt{b}\,\,x}{\sqrt{a}\,\,e}\,] \\ &-\frac{\mathrm{i}\,\,\sqrt{b}\,\,x}{\sqrt{a}\,\,e}\,] \end{pmatrix}$$

#### Problem 247: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^3 Log \left[c \left(a + \frac{b}{x^2}\right)^p\right]}{d + e x} dx$$

$$\frac{2 \, b \, p \, x}{3 \, a \, e} + \frac{2 \, \sqrt{b} \, d^2 \, p \, \text{ArcTan} \left[\frac{\sqrt{a} \, x}{\sqrt{b}}\right]}{\sqrt{a} \, e^3} - \frac{2 \, b^{3/2} \, p \, \text{ArcTan} \left[\frac{\sqrt{a} \, x}{\sqrt{b}}\right]}{3 \, a^{3/2} \, e} + \frac{d^2 \, x \, \text{Log} \left[c \, \left(a + \frac{b}{x^2}\right)^p\right]}{e^3} - \frac{d \, x^2 \, \text{Log} \left[c \, \left(a + \frac{b}{x^2}\right)^p\right]}{2 \, e^2} + \frac{x^3 \, \text{Log} \left[c \, \left(a + \frac{b}{x^2}\right)^p\right]}{3 \, e} - \frac{d^3 \, \text{Log} \left[c \, \left(a + \frac{b}{x^2}\right)^p\right] \, \text{Log} \left[d + e \, x\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{Log} \left[-\frac{e \, x}{d}\right] \, \text{Log} \left[d + e \, x\right]}{e^4} + \frac{d^3 \, p \, \text{Log} \left[\frac{e \, \left(\sqrt{b} - \sqrt{-a} \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right] \, \text{Log} \left[d + e \, x\right]}{e^4} + \frac{d^3 \, p \, \text{Log} \left[b + a \, x^2\right]}{2 \, a \, e^2} + \frac{d^3 \, p \, \text{PolyLog} \left[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{PolyLog} \left[2, \, 1 + \frac{e \, x}{d}\right]}{e^4} + \frac{d^3 \, p \, \text{PolyLog} \left[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{PolyLog} \left[2, \, 1 + \frac{e \, x}{d}\right]}{e^4} + \frac{d^3 \, p \, \text{PolyLog} \left[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{PolyLog} \left[2, \, 1 + \frac{e \, x}{d}\right]}{e^4} + \frac{d^3 \, p \, \text{PolyLog} \left[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{PolyLog} \left[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{PolyLog} \left[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{PolyLog} \left[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{PolyLog} \left[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{PolyLog} \left[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\right]}{e^4} - \frac{2 \, d^3 \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p \, \text{PolyLog} \left[2, \, \frac{d^3 \, p \, p$$

Result (type 4, 528 leaves):

$$\begin{split} &-\frac{1}{6\,e^4}\left[-\frac{4\,b\,e^3\,p\,x}{a} + \frac{4\,b^{3/2}\,e^3\,p\,\text{ArcTan}\Big[\frac{\sqrt{a}\,x}{\sqrt{b}}\Big]}{a^{3/2}} - 6\,d^2\,e\,x\,\text{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big] + \\ &-3\,d\,e^2\,x^2\,\text{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big] - 2\,e^3\,x^3\,\text{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big] + \frac{6\,i\,\sqrt{b}\,d^2\,e\,p\,\text{Log}\Big[-\frac{i\,\sqrt{b}}{\sqrt{a}} + x\Big]}{\sqrt{a}} - \\ &-\frac{6\,i\,\sqrt{b}\,d^2\,e\,p\,\text{Log}\Big[\frac{i\,\sqrt{b}}{\sqrt{a}} + x\Big]}{\sqrt{a}} + 6\,d^3\,\text{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big]\,\text{Log}[d + e\,x] + 12\,d^3\,p\,\text{Log}[x]\,\,\text{Log}[d + e\,x] - \\ &-6\,d^3\,p\,\text{Log}\Big[-\frac{i\,\sqrt{b}}{\sqrt{a}} + x\Big]\,\,\text{Log}\Big[d + e\,x\Big] - 6\,d^3\,p\,\text{Log}\Big[\frac{i\,\sqrt{b}}{\sqrt{a}} + x\Big]\,\,\text{Log}\Big[d + e\,x\Big] + \\ &-6\,d^3\,p\,\text{Log}\Big[\frac{i\,\sqrt{b}}{\sqrt{a}} + x\Big]\,\,\text{Log}\Big[\frac{\sqrt{a}\,\left(d + e\,x\right)}{\sqrt{a}\,d - i\,\sqrt{b}\,e}\Big] + 6\,d^3\,p\,\text{Log}\Big[-\frac{i\,\sqrt{b}}{\sqrt{a}} + x\Big]\,\,\text{Log}\Big[\frac{\sqrt{a}\,\left(d + e\,x\right)}{\sqrt{a}\,d + i\,\sqrt{b}\,e}\Big] - \\ &-12\,d^3\,p\,\text{Log}[x]\,\,\text{Log}\Big[1 + \frac{e\,x}{d}\Big] + \frac{3\,b\,d\,e^2\,p\,\text{Log}\Big[b + a\,x^2\Big]}{a} - 12\,d^3\,p\,\text{PolyLog}\Big[2, -\frac{e\,x}{d}\Big] + \\ &-6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big] + 6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,+ i\,\sqrt{a}\,x\right)}{- i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big] - \\ &-6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big] + 6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,+ i\,\sqrt{a}\,x\right)}{- i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big] - \\ &-6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big] + 6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{- i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big]} - \\ &-6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big] + 6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{- i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big]} - \\ &-6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big]} - \frac{e\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{- i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big]} - \\ &-6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big]} - \frac{e\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{- i\,\sqrt{a}\,d + \sqrt{b}\,e}\Big]} - \\ &-6\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{2} + \frac{e\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{2} + \frac{e\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{2} + \frac{e\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,- i\,\sqrt{a}\,x\right)}{2} + \frac{e\,d^3\,p\,\text{PolyLog}\Big[2, \frac{e\,\left(\sqrt{b}\,-$$

#### Problem 248: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x^2 Log \left[c \left(a + \frac{b}{x^2}\right)^p\right]}{d + e x} dx$$

Optimal (type 4, 353 leaves, 21 steps):

$$-\frac{2\,\sqrt{b}\,\,d\,p\,\text{ArcTan}\Big[\frac{\sqrt{a}\,\,x}{\sqrt{b}}\Big]}{\sqrt{a}\,\,e^{2}} - \frac{d\,x\,\text{Log}\Big[c\,\left(a + \frac{b}{x^{2}}\right)^{p}\Big]}{e^{2}} + \frac{x^{2}\,\text{Log}\Big[c\,\left(a + \frac{b}{x^{2}}\right)^{p}\Big]}{2\,e} + \frac{2\,e}{2\,e} + \frac{d^{2}\,\text{Log}\Big[c\,\left(a + \frac{b}{x^{2}}\right)^{p}\Big]}{2\,e} + \frac{e^{2}\,\,d^{2}\,p\,\text{Log}\Big[-\frac{e\,x}{d}\Big]\,\text{Log}\Big[d + e\,x\Big]}{e^{3}} - \frac{e^{3}\,\,d^{2}\,p\,\text{Log}\Big[\frac{e\,\left(\sqrt{b}\,-\sqrt{-a}\,x\right)}{\sqrt{-a}\,d + \sqrt{b}\,e}\Big]\,\text{Log}\Big[d + e\,x\Big]}{e^{3}} - \frac{d^{2}\,p\,\text{Log}\Big[-\frac{e\,\left(\sqrt{b}\,+\sqrt{-a}\,x\right)}{\sqrt{-a}\,d - \sqrt{b}\,e}\Big]\,\text{Log}\Big[d + e\,x\Big]}{e^{3}} + \frac{b\,p\,\text{Log}\Big[b + a\,x^{2}\Big]}{2\,a\,e} - \frac{d^{2}\,p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{-a}\,(d + e\,x)}{\sqrt{-a}\,d + \sqrt{b}\,e}\Big]}{e^{3}} + \frac{2\,d^{2}\,p\,\text{PolyLog}\Big[2,\,1 + \frac{e\,x}{d}\Big]}{e^{3}}$$

Result (type 4, 470 leaves):

$$\begin{split} &\frac{1}{2\,a\,e^3} \left[ -2\,a\,d\,e\,x\,\text{Log} \Big[ c\,\left( a + \frac{b}{x^2} \right)^p \Big] + a\,e^2\,x^2\,\text{Log} \Big[ c\,\left( a + \frac{b}{x^2} \right)^p \Big] + \right. \\ &2\,i\,\sqrt{a}\,\sqrt{b}\,d\,e\,p\,\text{Log} \Big[ - \frac{i\,\sqrt{b}}{\sqrt{a}} + x \Big] - 2\,i\,\sqrt{a}\,\sqrt{b}\,d\,e\,p\,\text{Log} \Big[ \frac{i\,\sqrt{b}}{\sqrt{a}} + x \Big] + \\ &2\,a\,d^2\,\text{Log} \Big[ c\,\left( a + \frac{b}{x^2} \right)^p \Big]\,\text{Log} \Big[ d + e\,x \Big] + 4\,a\,d^2\,p\,\text{Log} \Big[ x \Big]\,\text{Log} \Big[ d + e\,x \Big] - \\ &2\,a\,d^2\,p\,\text{Log} \Big[ - \frac{i\,\sqrt{b}}{\sqrt{a}} + x \Big]\,\text{Log} \Big[ d + e\,x \Big] - 2\,a\,d^2\,p\,\text{Log} \Big[ \frac{i\,\sqrt{b}}{\sqrt{a}} + x \Big]\,\text{Log} \Big[ d + e\,x \Big] + \\ &2\,a\,d^2\,p\,\text{Log} \Big[ \frac{i\,\sqrt{b}}{\sqrt{a}} + x \Big]\,\text{Log} \Big[ \frac{\sqrt{a}\,\left( d + e\,x \right)}{\sqrt{a}\,d - i\,\sqrt{b}\,e} \Big] + 2\,a\,d^2\,p\,\text{Log} \Big[ - \frac{i\,\sqrt{b}}{\sqrt{a}} + x \Big]\,\text{Log} \Big[ \frac{\sqrt{a}\,\left( d + e\,x \right)}{\sqrt{a}\,d + i\,\sqrt{b}\,e} \Big] - \\ &4\,a\,d^2\,p\,\text{Log} \Big[ x \Big]\,\text{Log} \Big[ 1 + \frac{e\,x}{d} \Big] + b\,e^2\,p\,\text{Log} \Big[ b + a\,x^2 \Big] - 4\,a\,d^2\,p\,\text{PolyLog} \Big[ 2 , - \frac{e\,x}{d} \Big] + \\ &2\,a\,d^2\,p\,\text{PolyLog} \Big[ 2 , \frac{e\,\left( \sqrt{b} - i\,\sqrt{a}\,x \right)}{i\,\sqrt{a}\,d + \sqrt{b}\,e} \Big] + 2\,a\,d^2\,p\,\text{PolyLog} \Big[ 2 , \frac{e\,\left( \sqrt{b} + i\,\sqrt{a}\,x \right)}{-i\,\sqrt{a}\,d + \sqrt{b}\,e} \Big] \\ &\Big] \end{split}$$

### Problem 249: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{x \, \mathsf{Log} \left[ c \, \left( \mathsf{a} + \frac{\mathsf{b}}{\mathsf{x}^2} \right)^{\mathsf{p}} \right]}{\mathsf{d} + \mathsf{e} \, \mathsf{x}} \, \mathrm{d} \mathsf{x}$$

Optimal (type 4, 291 leaves, 18 steps):

$$\frac{2\sqrt{b} \ p \, \text{ArcTan} \Big[\frac{\sqrt{a} \ x}{\sqrt{b}}\Big]}{\sqrt{a} \ e} + \frac{x \, \text{Log} \Big[c \, \left(a + \frac{b}{x^2}\right)^p\Big]}{e} - \frac{d \, \text{Log} \Big[c \, \left(a + \frac{b}{x^2}\right)^p\Big] \, \text{Log} \Big[d + e \, x\Big]}{e^2} - \frac{2 \, d \, p \, \text{Log} \Big[-\frac{e \, x}{d}\Big] \, \text{Log} \Big[d + e \, x\Big]}{e^2} + \frac{d \, p \, \text{Log} \Big[-\frac{e \, \left(\sqrt{b} + \sqrt{-a} \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\Big] \, \text{Log} \Big[d + e \, x\Big]}{e^2} + \frac{d \, p \, \text{Log} \Big[-\frac{e \, \left(\sqrt{b} + \sqrt{-a} \, x\right)}{\sqrt{-a} \, d - \sqrt{b} \, e}\Big] \, \text{Log} \Big[d + e \, x\Big]}{e^2} + \frac{d \, p \, \text{PolyLog} \Big[2, \, \frac{\sqrt{-a} \, \left(d + e \, x\right)}{\sqrt{-a} \, d + \sqrt{b} \, e}\Big]}{e^2} - \frac{2 \, d \, p \, \text{PolyLog} \Big[2, \, 1 + \frac{e \, x}{d}\Big]}{e^2}$$

Result (type 4, 392 leaves):

$$\begin{split} &-\frac{1}{e^2}\left[-e\,x\,\text{Log}\!\left[c\left(a+\frac{b}{x^2}\right)^p\right] + \frac{i\,\sqrt{b}\,\,e\,p\,\text{Log}\!\left[-\frac{i\,\sqrt{b}}{\sqrt{a}}+x\right]}{\sqrt{a}} - \frac{i\,\sqrt{b}\,\,e\,p\,\text{Log}\!\left[\frac{i\,\sqrt{b}}{\sqrt{a}}+x\right]}{\sqrt{a}} + \\ &d\,\text{Log}\!\left[c\left(a+\frac{b}{x^2}\right)^p\right]\,\text{Log}\!\left[d+e\,x\right] + 2\,d\,p\,\text{Log}\!\left[x\right]\,\text{Log}\!\left[d+e\,x\right] - d\,p\,\text{Log}\!\left[-\frac{i\,\sqrt{b}}{\sqrt{a}}+x\right]\,\text{Log}\!\left[d+e\,x\right] - \\ &d\,p\,\text{Log}\!\left[\frac{i\,\sqrt{b}}{\sqrt{a}}+x\right]\,\text{Log}\!\left[d+e\,x\right] + d\,p\,\text{Log}\!\left[\frac{i\,\sqrt{b}}{\sqrt{a}}+x\right]\,\text{Log}\!\left[\frac{\sqrt{a}\,\left(d+e\,x\right)}{\sqrt{a}\,d-i\,\sqrt{b}\,e}\right] + \\ &d\,p\,\text{Log}\!\left[-\frac{i\,\sqrt{b}}{\sqrt{a}}+x\right]\,\text{Log}\!\left[\frac{\sqrt{a}\,\left(d+e\,x\right)}{\sqrt{a}\,d+i\,\sqrt{b}\,e}\right] - 2\,d\,p\,\text{Log}\!\left[x\right]\,\text{Log}\!\left[1+\frac{e\,x}{d}\right] - 2\,d\,p\,\text{PolyLog}\!\left[2,-\frac{e\,x}{d}\right] + \\ &d\,p\,\text{PolyLog}\!\left[2,\frac{e\,\left(\sqrt{b}\,-i\,\sqrt{a}\,x\right)}{i\,\sqrt{a}\,d+\sqrt{b}\,e}\right] + d\,p\,\text{PolyLog}\!\left[2,\frac{e\,\left(\sqrt{b}\,+i\,\sqrt{a}\,x\right)}{-i\,\sqrt{a}\,d+\sqrt{b}\,e}\right] \end{split}$$

# Problem 250: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log\left[c\left(a + \frac{b}{x^2}\right)^p\right]}{d + ex} dx$$

#### Optimal (type 4, 241 leaves, 13 steps):

$$\frac{\text{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right] \text{Log}\left[d+e\,x\right]}{e} + \frac{2\,p\,\text{Log}\left[-\frac{e\,x}{d}\right] \text{Log}\left[d+e\,x\right]}{e} - \\ \frac{p\,\text{Log}\left[\frac{e\left(\sqrt{b}-\sqrt{-a}\,x\right)}{\sqrt{-a}\,d+\sqrt{b}\,e}\right] \text{Log}\left[d+e\,x\right]}{e} - \frac{p\,\text{Log}\left[-\frac{e\left(\sqrt{b}+\sqrt{-a}\,x\right)}{\sqrt{-a}\,d-\sqrt{b}\,e}\right] \text{Log}\left[d+e\,x\right]}{e} - \\ \frac{p\,\text{PolyLog}\left[2,\frac{\sqrt{-a}\,(d+e\,x)}{\sqrt{-a}\,d-\sqrt{b}\,e}\right]}{e} - \frac{p\,\text{PolyLog}\left[2,\frac{\sqrt{-a}\,(d+e\,x)}{\sqrt{-a}\,d+\sqrt{b}\,e}\right]}{e} + \frac{2\,p\,\text{PolyLog}\left[2,1+\frac{e\,x}{d}\right]}{e}$$

#### Result (type 4. 299 leaves):

$$\begin{split} &\frac{1}{e}\left(\text{Log}\big[c\left(a+\frac{b}{x^2}\right)^p\big]\,\text{Log}\,[d+e\,x]\,+2\,p\,\text{Log}\,[x]\,\,\text{Log}\,[d+e\,x]\,-p\,\text{Log}\big[-\frac{i\,\sqrt{b}}{\sqrt{a}}\,+x\big]\,\,\text{Log}\,[d+e\,x]\,-p\,\text{Log}\,[\frac{i\,\sqrt{b}}{\sqrt{a}}\,+x\big]\,\,\text{Log}\,[d+e\,x]\,-p\,\text{Log}\,[\frac{i\,\sqrt{b}}{\sqrt{a}}\,+x\big]\,\,\text{Log}\,[\frac{\sqrt{a}\,\,(d+e\,x)}{\sqrt{a}\,\,d-i\,\sqrt{b}\,\,e}\big]\,+p\,\text{Log}\,[\frac{i\,\sqrt{b}}{\sqrt{a}}\,+x\big]\,\,\text{Log}\,[\frac{\sqrt{a}\,\,(d+e\,x)}{\sqrt{a}\,\,d-i\,\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,-i\,\sqrt{a}\,\,x)}{i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,+p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,d+\sqrt{b}\,\,e}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,a+\sqrt{b}\,\,a}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,a+\sqrt{b}\,\,a}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,a+\sqrt{b}\,\,a}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,a+\sqrt{b}\,\,a}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,a+\sqrt{b}\,\,a}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,a+\sqrt{b}\,\,a}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,a+\sqrt{b}\,\,a}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+i\,\sqrt{a}\,\,x)}{-i\,\sqrt{a}\,\,a+\sqrt{b}\,\,a}\big]\,-p\,\text{PolyLog}\,[2,\frac{e\,(\sqrt{b}\,+$$

# Problem 251: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log\left[c\left(a+\frac{b}{x^2}\right)^p\right]}{x\left(d+ex\right)} dx$$

Optimal (type 4, 287 leaves, 18 steps):

$$-\frac{\text{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right]\text{Log}\left[-\frac{b}{a\,x^2}\right]}{2\,d}-\frac{\text{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right]\text{Log}\left[d+e\,x\right]}{d}-\frac{2\,p\,\text{Log}\left[-\frac{e\,x}{d}\right]\text{Log}\left[d+e\,x\right]}{d}+\frac{p\,\text{Log}\left[-\frac{e\,(\sqrt{b}\,+\sqrt{-a}\,x)}{\sqrt{-a}\,d-\sqrt{b}\,e}\right]\text{Log}\left[d+e\,x\right]}{d}-\frac{p\,\text{PolyLog}\left[2,\,1+\frac{b}{a\,x^2}\right]}{2\,d}+\frac{p\,\text{PolyLog}\left[2,\,\frac{\sqrt{-a}\,(d+e\,x)}{\sqrt{-a}\,d+\sqrt{b}\,e}\right]}{d}-\frac{2\,p\,\text{PolyLog}\left[2,\,1+\frac{e\,x}{d}\right]}{d}$$

Result (type 4, 405 leaves):

$$-\frac{1}{d}\left(-\text{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right]\text{Log}[x]-p\text{Log}[x]^2+p\text{Log}[x]\text{Log}\left[1-\frac{i\sqrt{a}}{\sqrt{b}}\right]+\right.\\ \left.p\text{Log}[x]\text{Log}\left[1+\frac{i\sqrt{a}}{\sqrt{b}}x\right]+\text{Log}\left[c\left(a+\frac{b}{x^2}\right)^p\right]\text{Log}[d+ex]+2p\text{Log}[x]\text{Log}[d+ex]-\\ \left.p\text{Log}\left[-\frac{i\sqrt{b}}{\sqrt{a}}+x\right]\text{Log}[d+ex]-p\text{Log}\left[\frac{i\sqrt{b}}{\sqrt{a}}+x\right]\text{Log}[d+ex]+\\ \left.p\text{Log}\left[\frac{i\sqrt{b}}{\sqrt{a}}+x\right]\text{Log}\left[\frac{\sqrt{a}\left(d+ex\right)}{\sqrt{a}\left(d-i\sqrt{b}\right)e}\right]+p\text{Log}\left[-\frac{i\sqrt{b}}{\sqrt{a}}+x\right]\text{Log}\left[\frac{\sqrt{a}\left(d+ex\right)}{\sqrt{a}\left(d+i\sqrt{b}\right)e}\right]-\\ \left.2p\text{Log}[x]\text{Log}\left[1+\frac{ex}{d}\right]+p\text{PolyLog}\left[2,-\frac{i\sqrt{a}x}{\sqrt{b}}\right]+p\text{PolyLog}\left[2,\frac{i\sqrt{a}x}{\sqrt{b}}\right]-\\ \left.2p\text{PolyLog}\left[2,-\frac{ex}{d}\right]+p\text{PolyLog}\left[2,\frac{e\left(\sqrt{b}-i\sqrt{a}x\right)}{\sqrt{b}}\right]+p\text{PolyLog}\left[2,\frac{e\left(\sqrt{b}+i\sqrt{a}x\right)}{\sqrt{b}}\right]\right]$$

# Problem 252: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log\left[\left.c\left(a+\frac{b}{x^2}\right)^p\right.\right]}{x^2\,\left(d+e\,x\right)}\,\mathrm{d}x$$

Optimal (type 4, 357 leaves, 22 steps):

$$\frac{2 p}{d \, x} + \frac{2 \sqrt{a} \ p \, \text{ArcTan} \Big[ \frac{\sqrt{a} \ x}{\sqrt{b}} \Big]}{\sqrt{b} \ d} - \frac{\text{Log} \Big[ c \ \Big( a + \frac{b}{x^2} \Big)^p \Big]}{d \, x} + \frac{e \, \text{Log} \Big[ c \ \Big( a + \frac{b}{x^2} \Big)^p \Big] \, \text{Log} \Big[ - \frac{b}{a \, x^2} \Big]}{2 \, d^2} + \frac{e \, \text{Log} \Big[ c \ \Big( a + \frac{b}{x^2} \Big)^p \Big] \, \text{Log} \Big[ d + e \, x \Big]}{d^2} + \frac{2 \, e \, p \, \text{Log} \Big[ - \frac{e \, x}{d} \Big] \, \text{Log} \Big[ d + e \, x \Big]}{d^2} - \frac{e \, p \, \text{Log} \Big[ \frac{e \, \Big( \sqrt{b} - \sqrt{-a} \, x \Big)}{\sqrt{-a} \, d + \sqrt{b} \, e} \Big] \, \text{Log} \Big[ d + e \, x \Big]}{d^2} - \frac{e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{b}{a \, x^2} \Big]}{2 \, d^2} - \frac{e \, p \, \text{PolyLog} \Big[ 2 \, , \, \frac{\sqrt{-a} \, (d + e \, x)}{\sqrt{-a} \, d + \sqrt{b} \, e} \Big]}{d^2} - \frac{e \, p \, \text{PolyLog} \Big[ 2 \, , \, \frac{\sqrt{-a} \, (d + e \, x)}{\sqrt{-a} \, d + \sqrt{b} \, e} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{2 \, e \, p \, \text{PolyLog} \Big[ 2 \, , \, 1 + \frac{e \, x}{d} \Big]}{d^2} + \frac{$$

#### Result (type 4, 472 leaves):

$$\frac{1}{d^2}\left[\frac{2\,d\,p}{x} + \frac{2\,\sqrt{a}\,d\,p\,\mathsf{ArcTan}\Big[\frac{\sqrt{a}\,x}{\sqrt{b}}\Big]}{\sqrt{b}} - \frac{d\,\mathsf{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big]}{x} - e\,\mathsf{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big]\,\mathsf{Log}\big[x\big] - e\,\mathsf{p\,Log}\big[x\big]^2 + e\,\mathsf{p\,Log}\big[x\big]\,\mathsf{Log}\Big[1 - \frac{i\,\sqrt{a}\,x}{\sqrt{b}}\Big] + e\,\mathsf{p\,Log}\big[x\big]\,\mathsf{Log}\Big[1 + \frac{i\,\sqrt{a}\,x}{\sqrt{b}}\Big] + e\,\mathsf{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big]\,\mathsf{Log}\big[d + e\,x\big] + 2\,\mathsf{e\,p\,Log}\big[x\big]\,\mathsf{Log}\big[d + e\,x\big] - e\,\mathsf{p\,Log}\big[\frac{i\,\sqrt{b}}{\sqrt{a}} + x\big]\,\mathsf{Log}\big[d + e\,x\big] + e\,\mathsf{p\,Log}\Big[\frac{i\,\sqrt{b}}{\sqrt{a}} + x\big]\,\mathsf{Log}\big[d + e\,x\big] + e\,\mathsf{p\,Log}\Big[\frac{i\,\sqrt{b}}{\sqrt{a}} + x\big]\,\mathsf{Log}\Big[\frac{\sqrt{a}\,\left(d + e\,x\right)}{\sqrt{a}\,d + i\,\sqrt{b}\,e}\Big] - 2\,\mathsf{e\,p\,Log}\big[x\big]\,\mathsf{Log}\Big[1 + \frac{e\,x}{d}\Big] + e\,\mathsf{p\,PolyLog}\Big[2, -\frac{i\,\sqrt{a}\,x}{\sqrt{b}}\Big] + e\,\mathsf{p\,PolyLog}\Big[2, -\frac{i\,\sqrt{a}\,x}{\sqrt{b}}\Big] - 2\,\mathsf{e\,p\,PolyLog}\Big[2, -\frac{e\,x}{d}\Big] + e\,\mathsf{p\,PolyLog}\Big[2, -\frac{e\,\sqrt{b}\,a + i\,\sqrt{a}\,x}{\sqrt{b}\,e}\Big] - 2\,\mathsf{p\,PolyLog}\Big[2, -\frac{e\,\sqrt{b}\,a + i\,\sqrt{a}\,x}{d}\Big] - 2\,\mathsf{p\,PolyLog}\Big[2, -\frac{e\,x}{d}\Big] + e\,\mathsf{p\,PolyLog}\Big[2, -\frac{e\,\sqrt{b}\,a + i\,\sqrt{a}\,x}{2}\Big] - 2\,\mathsf{p\,PolyLog}\Big[2, -\frac{e\,x}{d}\Big] + e\,\mathsf{p\,PolyLog}\Big[2, -\frac{e\,\sqrt{b}\,a + i\,\sqrt{a}\,x}{2}\Big] - 2\,\mathsf{p\,PolyLog}\Big[2, -\frac{e\,x}{d}\Big] - 2\,\mathsf{p\,PolyLog}\Big[2, -\frac$$

# Problem 253: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log\left[c\left(a+\frac{b}{x^2}\right)^p\right]}{x^3\left(d+ex\right)} dx$$

Optimal (type 4, 414 leaves, 25 steps):

$$\frac{p}{2\,d\,x^2} - \frac{2\,e\,p}{d^2\,x} - \frac{2\,\sqrt{a}\,e\,p\,\text{ArcTan}\Big[\frac{\sqrt{a}\,x}{\sqrt{b}}\Big]}{\sqrt{b}\,d^2} - \frac{\left(a + \frac{b}{x^2}\right)\,\text{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big]}{2\,b\,d} + \\ \frac{e\,\text{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big]}{d^2\,x} - \frac{e^2\,\text{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big]\,\text{Log}\Big[-\frac{b}{a\,x^2}\Big]}{2\,d^3} - \frac{e^2\,\text{Log}\Big[c\,\left(a + \frac{b}{x^2}\right)^p\Big]\,\text{Log}\Big[d + e\,x\Big]}{d^3} - \\ \frac{2\,e^2\,p\,\text{Log}\Big[-\frac{e\,x}{d}\Big]\,\text{Log}\Big[d + e\,x\Big]}{d^3} + \frac{e^2\,p\,\text{Log}\Big[\frac{e\,\left(\sqrt{b}\,-\sqrt{-a}\,x\right)}{\sqrt{-a}\,d + \sqrt{b}\,e}\Big]\,\text{Log}\Big[d + e\,x\Big]}{d^3} + \\ \frac{e^2\,p\,\text{Log}\Big[-\frac{e\,\left(\sqrt{b}\,+\sqrt{-a}\,x\right)}{\sqrt{-a}\,d - \sqrt{b}\,e}\Big]\,\text{Log}\Big[d + e\,x\Big]}{d^3} - \frac{e^2\,p\,\text{PolyLog}\Big[2\,,\,1 + \frac{b}{a\,x^2}\Big]}{2\,d^3} + \\ \frac{e^2\,p\,\text{PolyLog}\Big[2\,,\,\frac{\sqrt{-a}\,\left(d + e\,x\right)}{\sqrt{-a}\,d - \sqrt{b}\,e}\Big]}{d^3} + \frac{e^2\,p\,\text{PolyLog}\Big[2\,,\,\frac{\sqrt{-a}\,\left(d + e\,x\right)}{\sqrt{-a}\,d + \sqrt{b}\,e}\Big]}{d^3} - \frac{2\,e^2\,p\,\text{PolyLog}\Big[2\,,\,1 + \frac{e\,x}{d}\Big]}{d^3}$$

### Result (type 4, 643 leaves):

$$-\frac{1}{2 \, b \, d^3 \, x^2} \left( -b \, d^2 \, p + 4 \, b \, d \, e \, p \, x + 4 \, \sqrt{a} \, \sqrt{b} \, d \, e \, p \, x^2 \, ArcTan \left[ \frac{\sqrt{a} \, x}{\sqrt{b}} \right] + b \, d^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] - 2 \, b \, d \, e \, x \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] - 2 \, a \, d^2 \, p \, x^2 \, Log \left[ x \right] - 2 \, b \, e^2 \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ x \right] - 2 \, b \, e^2 \, p \, x^2 \, Log \left[ x \right] \, Log \left[ 1 - \frac{i \, \sqrt{a} \, x}{\sqrt{b}} \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ x \right] \, Log \left[ 1 - \frac{i \, \sqrt{a} \, x}{\sqrt{b}} \right] + 2 \, b \, e^2 \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ d + e \, x \right] + 4 \, b \, e^2 \, p \, x^2 \, Log \left[ x \right] \, Log \left[ d + e \, x \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ d + e \, x \right] + 4 \, b \, e^2 \, p \, x^2 \, Log \left[ x \right] \, Log \left[ d + e \, x \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ d + e \, x \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ d + e \, x \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c + e \, x \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c + e \, x \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c + e \, x \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c + e \, x \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c + e \, x \right] + 2 \, b \, e^2 \, p \, x^2 \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right] \, Log \left[ c \, \left( a + \frac{b}{x^2} \right)^p \right]$$

### Problem 263: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{Log \left[ \, c \, \left( d + e \, x \right)^{\, p} \, \right]}{f + g \, x^2} \, \mathrm{d} x$$

Optimal (type 4, 229 leaves, 8 steps):

$$\frac{\text{Log}\!\left[c\,\left(d+e\,x\right)^p\right]\,\text{Log}\!\left[\frac{e\,\left(\sqrt{-f}\,-\sqrt{g}\,x\right)}{e\,\sqrt{-f}\,+d\,\sqrt{g}}\right]}{2\,\sqrt{-f}\,\sqrt{g}} - \frac{\text{Log}\!\left[c\,\left(d+e\,x\right)^p\right]\,\text{Log}\!\left[\frac{e\,\left(\sqrt{-f}\,+\sqrt{g}\,x\right)}{e\,\sqrt{-f}\,-d\,\sqrt{g}}\right]}{2\,\sqrt{-f}\,\sqrt{g}} - \frac{p\,\text{PolyLog}\!\left[2\,,\,-\frac{\sqrt{g}\,\left(d+e\,x\right)}{e\,\sqrt{-f}\,-d\,\sqrt{g}}\right]}{2\,\sqrt{-f}\,\sqrt{g}} + \frac{p\,\text{PolyLog}\!\left[2\,,\,\frac{\sqrt{g}\,\left(d+e\,x\right)}{e\,\sqrt{-f}\,+d\,\sqrt{g}}\right]}{2\,\sqrt{-f}\,\sqrt{g}}$$

Result (type 4, 232 leaves):

$$\begin{split} \frac{\text{ArcTan}\Big[\frac{\sqrt{g} \cdot x}{\sqrt{f}}\Big] \cdot \Big(-p \, \text{Log} \big[d + e \, x\big] + \text{Log} \Big[c \cdot \Big(d + e \, x\Big)^p\Big]\Big)}{\sqrt{f} \cdot \sqrt{g}} + \\ p \cdot \left[\frac{\text{i} \cdot \Big(\text{Log} \big[d + e \, x\big] \cdot \text{Log} \Big[1 - \frac{\sqrt{g} \cdot (d + e \, x)}{-\text{i} \cdot e \cdot \sqrt{f} + d \cdot \sqrt{g}}\Big] + \text{PolyLog} \Big[2, \frac{\sqrt{g} \cdot (d + e \, x)}{-\text{i} \cdot e \cdot \sqrt{f} + d \cdot \sqrt{g}}\Big]\Big)}}{2 \cdot \sqrt{f} \cdot \sqrt{g}} - \\ \frac{\text{i} \cdot \Big(\text{Log} \big[d + e \, x\big] \cdot \text{Log} \Big[1 - \frac{\sqrt{g} \cdot (d + e \, x)}{\text{i} \cdot e \cdot \sqrt{f} + d \cdot \sqrt{g}}\Big] + \text{PolyLog} \Big[2, \frac{\sqrt{g} \cdot (d + e \, x)}{\text{i} \cdot e \cdot \sqrt{f} + d \cdot \sqrt{g}}\Big]\Big)}{2 \cdot \sqrt{f} \cdot \sqrt{g}} \end{split}$$

# Problem 266: Result is not expressed in closed-form.

$$\int \frac{\text{Log}\left[c\left(d+e\sqrt{x}\right)^{p}\right]}{f+gx^{2}} dx$$

Optimal (type 4, 541 leaves, 19 steps):

$$\frac{\text{Log} \Big[ c \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)^{\mathsf{p}} \Big] \, \text{Log} \Big[ \frac{\mathsf{e} \left[ \sqrt{-\sqrt{-f}} \, - \mathsf{g}^{1/4} \, \sqrt{x} \, \right]}{\mathsf{e} \, \sqrt{-\sqrt{-f}} \, + \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \\ \frac{\text{Log} \Big[ c \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)^{\mathsf{p}} \Big] \, \text{Log} \Big[ \frac{\mathsf{e} \left( (-f)^{1/4} - \mathsf{g}^{1/4} \, \sqrt{x} \, \right)}{\mathsf{e} \, (-f)^{1/4} + \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{\mathsf{Log} \Big[ c \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)^{\mathsf{p}} \Big] \, \mathsf{Log} \Big[ \frac{\mathsf{e} \left( \sqrt{-\sqrt{-f}} \, + \mathsf{g}^{1/4} \, \sqrt{x} \, \right)}{\mathsf{e} \, (-f)^{1/4} + \mathsf{g}^{1/4} \, \sqrt{x}} \Big]}}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{\mathsf{p} \, \mathsf{PolyLog} \Big[ 2 \, , \, - \frac{\mathsf{g}^{1/4} \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)}{\mathsf{e} \, \sqrt{-\sqrt{-f}} \, - \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\mathsf{p} \, \mathsf{PolyLog} \Big[ 2 \, , \, \frac{\mathsf{g}^{1/4} \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)}{\mathsf{e} \, \sqrt{-\sqrt{-f}} \, - \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\mathsf{p} \, \mathsf{PolyLog} \Big[ 2 \, , \, \frac{\mathsf{g}^{1/4} \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)}{\mathsf{e} \, \left( -f \, \right)^{1/4} + \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\mathsf{p} \, \mathsf{PolyLog} \Big[ 2 \, , \, \frac{\mathsf{g}^{1/4} \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)}{\mathsf{e} \, \left( -f \, \right)^{1/4} + \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\mathsf{p} \, \mathsf{PolyLog} \Big[ 2 \, , \, \frac{\mathsf{g}^{1/4} \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)}{\mathsf{e} \, \left( -f \, \right)^{1/4} + \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\mathsf{p} \, \mathsf{PolyLog} \Big[ 2 \, , \, \frac{\mathsf{g}^{1/4} \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)}{\mathsf{e} \, \left( -f \, \right)^{1/4} + \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\mathsf{p} \, \mathsf{polyLog} \Big[ 2 \, , \, \frac{\mathsf{g}^{1/4} \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)}{\mathsf{e} \, \left( -f \, \right)^{1/4} + \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\mathsf{p} \, \mathsf{polyLog} \Big[ 2 \, , \, \frac{\mathsf{g}^{1/4} \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)}{\mathsf{e} \, \left( -f \, \right)^{1/4} + \mathsf{d} \, \mathsf{g}^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\mathsf{p} \, \mathsf{polyLog} \Big[ 2 \, , \, \frac{\mathsf{g}^{1/4} \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{x} \, \right)}{\mathsf{e} \, \sqrt{-f} \, \sqrt{g}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\mathsf{p} \, \mathsf{polyLog} \Big[ 2 \, , \, \frac{\mathsf{p}^{1/4} \, \mathsf{e} \, \sqrt{g} \, \right]}{\mathsf{polyLog} \Big[ 2 \, , \, \frac{\mathsf{p}^{1/4} \, \left( \mathsf{e} \, -f \, \sqrt{g} \, \right)}{\mathsf{polyLog} \Big[ 2 \, , \, \frac{\mathsf{p}^{1/4} \, \left( \mathsf{e} \, -f \, \sqrt{g} \, \right)}{\mathsf{polyLog} \Big[ 2 \, , \, \frac{\mathsf{p}^{1/4} \, \left( \mathsf{e} \, -f \, \sqrt{g} \, \right)}{\mathsf{polyLog}$$

#### Result (type 7, 227 leaves):

$$\begin{split} &\frac{1}{\sqrt{f} \, \sqrt{g}} \\ &\left( \text{ArcTan} \Big[ 1 - \frac{\sqrt{2} \, \, \mathsf{g}^{1/4} \, \sqrt{\mathsf{x}}}{\mathsf{f}^{1/4}} \Big] + \text{ArcTan} \Big[ 1 + \frac{\sqrt{2} \, \, \mathsf{g}^{1/4} \, \sqrt{\mathsf{x}}}{\mathsf{f}^{1/4}} \Big] \right) \, \left( \mathsf{p} \, \mathsf{Log} \Big[ \, \mathsf{d} + \mathsf{e} \, \sqrt{\mathsf{x}} \, \, \Big] - \mathsf{Log} \Big[ \, \mathsf{c} \, \, \left( \mathsf{d} + \mathsf{e} \, \sqrt{\mathsf{x}} \, \, \right)^\mathsf{p} \Big] \right) + \\ &\frac{1}{4 \, \mathsf{g}} \mathsf{e}^2 \, \mathsf{p} \, \mathsf{RootSum} \Big[ \, \mathsf{e}^4 \, \mathsf{f} + \mathsf{d}^4 \, \mathsf{g} - 4 \, \mathsf{d}^3 \, \mathsf{g} \, \sharp 1 + 6 \, \mathsf{d}^2 \, \mathsf{g} \, \sharp 1^2 - 4 \, \mathsf{d} \, \mathsf{g} \, \sharp 1^3 + \mathsf{g} \, \sharp 1^4 \, \&, \, \frac{1}{\mathsf{d}^2 - 2 \, \mathsf{d} \, \sharp 1 + \sharp 1^2} \\ &\left( - \, \mathsf{Log} \Big[ \, \mathsf{d} + \mathsf{e} \, \sqrt{\mathsf{x}} \, \, \Big]^2 + 2 \, \mathsf{Log} \Big[ \, \mathsf{d} + \mathsf{e} \, \sqrt{\mathsf{x}} \, \, \Big] \, \, \mathsf{Log} \Big[ 1 - \frac{\mathsf{d} + \mathsf{e} \, \sqrt{\mathsf{x}}}{\sharp 1} \Big] + 2 \, \mathsf{PolyLog} \Big[ 2 \, , \, \frac{\mathsf{d} + \mathsf{e} \, \sqrt{\mathsf{x}}}{\sharp 1} \Big] \right) \, \, \& \Big] \end{split}$$

# Problem 267: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Log}\left[c\left(d + \frac{e}{\sqrt{x}}\right)^{p}\right]}{f + g x^{2}} dx$$

Optimal (type 4, 561 leaves, 20 steps):

$$-\frac{\text{Log} \Big[ c \left( d + \frac{e}{\sqrt{x}} \right)^p \Big] \, \text{Log} \Big[ \frac{e}{d\sqrt{-\sqrt{-f}}} \frac{e}{\sqrt{x}} \Big]}{d\sqrt{-\sqrt{-f}} + e \, g^{1/4}} \Big] }{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{\text{Log} \Big[ c \left( d + \frac{e}{\sqrt{x}} \right)^p \Big] \, \text{Log} \Big[ -\frac{e}{d\sqrt{-\sqrt{-f}}} \frac{e^{1/4}}{\sqrt{x}} \Big]}{d\sqrt{-\sqrt{-f}} - e \, g^{1/4}} \Big] }{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\text{Log} \Big[ c \left( d + \frac{e}{\sqrt{x}} \right)^p \Big] \, \text{Log} \Big[ -\frac{e}{d\sqrt{x}} \frac{e^{1/4} + \frac{(-f)^{1/4}}{\sqrt{x}}}{\sqrt{x}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{\text{Log} \Big[ c \left( d + \frac{e}{\sqrt{x}} \right)^p \Big] \, \text{Log} \Big[ -\frac{e}{d\sqrt{x}} \frac{e^{1/4} + \frac{(-f)^{1/4}}{\sqrt{x}}}{\sqrt{x}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{2 \, \sqrt{-f} \, \sqrt{g}}{\sqrt{g}} + \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} + \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]} - \frac{p \, \text{PolyLog} \Big[ 2, \, \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{d \, (-f)^{1/4} - e \, g^{1/4}} \Big]}{2 \, \sqrt{-f} \, \sqrt{g}} - \frac{(-f)^{1/4} \left( d + \frac{e}{\sqrt{x}} \right)}{2$$

Result (type 4, 895 leaves):

$$\begin{split} &\frac{1}{4\sqrt{f}\sqrt{g}}\left[4\,\mathsf{p}\,\mathsf{ArcTan}\Big[1-\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}\sqrt{x}}{\mathsf{f}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\Big] + 4\,\mathsf{p}\,\mathsf{ArcTan}\Big[\frac{\sqrt{g}}{\sqrt{f}}\,\mathsf{x}\Big]\,\mathsf{Log}\Big[\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\Big] - 4\,\mathsf{ArcTan}\Big[1-\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}\sqrt{x}}{\mathsf{f}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}\sqrt{x}}{\mathsf{f}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}\sqrt{x}}{\mathsf{f}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}\sqrt{x}}{\mathsf{f}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}\sqrt{x}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}\sqrt{x}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}\sqrt{x}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}\sqrt{x}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\sqrt{2}}{f^{1/4}}\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{e}}{\sqrt{x}}\right)^p\Big] - 4\,\mathsf{ArcTan}\Big[1+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big)\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big)^p\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big)^p\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{d}+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big),\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{g}+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}\Big)^p\Big]\,\mathsf{Log}\Big[\mathsf{c}\left(\mathsf{g}+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big),\mathsf{Log}\Big[\mathsf{g}\left(\mathsf{g}+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big)^p\Big]\,\mathsf{Log}\Big[\mathsf{g}\left(\mathsf{g}\left(\mathsf{g}+\frac{\mathsf{g}^{1/4}}{\mathsf{g}^{1/4}}\Big),\mathsf{Log}\Big[\mathsf{g}\left(\mathsf{g}\left(\mathsf{g}\right)^p\Big],\mathsf{Log}\Big[\mathsf{g}\left(\mathsf{g}\right)^p\Big],\mathsf{Log}\Big[\mathsf{g}\left(\mathsf{g}\right)^p\Big],\mathsf{Log}\Big[\mathsf{g}\left(\mathsf{g}\right)^p\Big],\mathsf{Log}\Big[\mathsf$$

# Problem 274: Result more than twice size of optimal antiderivative.

$$\int (f + g x^2) Log[c (d + e x^2)^p]^2 dx$$

Optimal (type 4, 548 leaves, 30 steps):

$$\begin{split} &8 \, \mathsf{f} \, \mathsf{p}^2 \, \mathsf{x} - \frac{32 \, \mathsf{d} \, \mathsf{g} \, \mathsf{p}^2 \, \mathsf{x}}{9 \, \mathsf{e}} + \frac{8}{27} \, \mathsf{g} \, \mathsf{p}^2 \, \mathsf{x}^3 - \frac{8 \, \sqrt{\mathsf{d}} \, \mathsf{f} \, \mathsf{p}^2 \, \mathsf{ArcTan} \Big[ \frac{\sqrt{\mathsf{e}} \, \mathsf{x}}{\sqrt{\mathsf{d}}} \Big]}{\sqrt{\mathsf{e}}} + \frac{4 \, \mathsf{i} \, \sqrt{\mathsf{d}} \, \mathsf{f} \, \mathsf{p}^2 \, \mathsf{ArcTan} \Big[ \frac{\sqrt{\mathsf{e}} \, \mathsf{x}}{\sqrt{\mathsf{d}}} \Big]^2}{\sqrt{\mathsf{e}}} - \frac{4 \, \mathsf{i} \, \mathsf{d}^{3/2} \, \mathsf{g} \, \mathsf{p}^2 \, \mathsf{ArcTan} \Big[ \frac{\sqrt{\mathsf{e}} \, \mathsf{x}}{\sqrt{\mathsf{d}}} \Big]^2}{3 \, \mathsf{e}^{3/2}} + \frac{8 \, \sqrt{\mathsf{d}} \, \mathsf{f} \, \mathsf{p}^2 \, \mathsf{ArcTan} \Big[ \frac{\sqrt{\mathsf{e}} \, \mathsf{x}}{\sqrt{\mathsf{d}}} \Big] \, \mathsf{Log} \Big[ \frac{2 \, \sqrt{\mathsf{d}}}{\sqrt{\mathsf{d}} + \mathsf{i} \, \sqrt{\mathsf{e}} \, \mathsf{x}} \Big]}{\sqrt{\mathsf{e}}} - \frac{8 \, \mathsf{d}^{3/2} \, \mathsf{g} \, \mathsf{p}^2 \, \mathsf{ArcTan} \Big[ \frac{\sqrt{\mathsf{e}} \, \mathsf{x}}{\sqrt{\mathsf{d}}} \Big] \, \mathsf{Log} \Big[ \frac{2 \, \sqrt{\mathsf{d}}}{\sqrt{\mathsf{d}} + \mathsf{i} \, \sqrt{\mathsf{e}} \, \mathsf{x}} \Big]}{3 \, \mathsf{e}^{3/2}} - \frac{4 \, \mathsf{d} \, \mathsf{g} \, \mathsf{p} \, \mathsf{x} \, \mathsf{Log} \Big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \Big]}{3 \, \mathsf{e}^{3/2}} - \frac{4 \, \mathsf{d} \, \mathsf{g} \, \mathsf{p} \, \mathsf{x} \, \mathsf{Log} \Big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \Big]}{3 \, \mathsf{e}^{3/2}} - \frac{4 \, \mathsf{d} \, \mathsf{g} \, \mathsf{p} \, \mathsf{x} \, \mathsf{Log} \Big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \Big]}{3 \, \mathsf{e}^{3/2}} - \frac{4 \, \mathsf{d} \, \mathsf{d} \, \mathsf{g} \, \mathsf{p} \, \mathsf{Log} \Big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \Big]}{3 \, \mathsf{e}^{3/2}} - \frac{4 \, \mathsf{d} \, \mathsf{d} \, \mathsf{g} \, \mathsf{p} \, \mathsf{e} \, \mathsf{Log} \Big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \Big]}{3 \, \mathsf{e}^{3/2}} - \frac{4 \, \mathsf{d} \, \mathsf{d} \, \mathsf{g} \, \mathsf{g} \, \mathsf{e} \, \mathsf{e} \, \mathsf{d} \, \mathsf{e} \, \mathsf{g} \, \mathsf{e} \,$$

Result (type 4, 1125 leaves):

$$\begin{split} &2 \, \mathsf{f} \, \mathsf{p} \left[ -2 \, \mathsf{e} \left[ \frac{\mathsf{x}}{\mathsf{e}} - \frac{\sqrt{\mathsf{d}} \, \mathsf{ArcTan} \left[ \frac{\sqrt{\mathsf{e}} \, \mathsf{x}}{\sqrt{\mathsf{d}}} \right]}{\mathsf{e}^{3/2}} \right] + \mathsf{x} \, \mathsf{Log} \big[ \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \big] \right] + \mathsf{p} \, \mathsf{Log} \big[ \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \big] + \mathsf{Log} \big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \big] \right) + \\ &2 \, \mathsf{g} \, \mathsf{p} \left[ -\frac{2}{3} \, \mathsf{e} \left( -\frac{\mathsf{d} \, \mathsf{x}}{\mathsf{e}^2} + \frac{\mathsf{x}^3}{3 \, \mathsf{e}} + \frac{\mathsf{d}^{3/2} \, \mathsf{ArcTan} \left[ \frac{\sqrt{\mathsf{e}} \, \mathsf{x}}{\sqrt{\mathsf{d}}} \right]}{\mathsf{e}^{5/2}} \right] + \frac{1}{3} \, \mathsf{x}^3 \, \mathsf{Log} \big[ \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \big] + \mathsf{Log} \big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \big] \big) + \mathsf{f} \, \mathsf{x} \, \left( -\mathsf{p} \, \mathsf{Log} \big[ \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \big] + \mathsf{Log} \big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \big] \right) + \mathsf{f} \, \mathsf{x} \, \left( -\mathsf{p} \, \mathsf{Log} \big[ \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \big] + \mathsf{Log} \big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \big] \big)^2 + \mathsf{f} \, \mathsf{p}^2 \, \left[ \mathsf{x} \, \mathsf{Log} \big[ \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \big]^2 - \mathsf{Log} \big[ \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \big] + \mathsf{Log} \big[ \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \right)^{\mathsf{p}} \big] \big)^2 + \mathsf{f} \, \mathsf{p}^2 \, \left[ \mathsf{x} \, \mathsf{Log} \big[ \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \big]^2 - \mathsf{Log} \big[ \mathsf{d} + \mathsf{e} \, \mathsf{x}^2 \big] + \mathsf{Log} \big[ \mathsf{d} \, \mathsf{e} \, \mathsf{e} \, \mathsf{x}^2 \big] + \mathsf{Log} \big[ \mathsf{d} \, \mathsf{e} \, \mathsf{e} \, \mathsf{x}^2 \big] + \mathsf{Log} \big[ \mathsf{d} \, \mathsf{e} \, \mathsf{e} \, \mathsf{x}^2 \big] + \mathsf{Log} \big[ \mathsf{d} \, \mathsf{e} \, \mathsf{e}$$

Problem 341: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log\left[c\,\left(d+e\,x^2\right)^p\right]}{x\,\left(f+g\,x^2\right)}\,\mathrm{d}x$$

Optimal (type 4, 119 leaves, 8 steps):

$$\frac{\text{Log}\left[-\frac{e\,x^2}{d}\right]\,\text{Log}\left[c\,\left(d+e\,x^2\right)^p\right]}{2\,f} - \frac{\text{Log}\left[c\,\left(d+e\,x^2\right)^p\right]\,\text{Log}\left[\frac{e\,\left(f+g\,x^2\right)}{e\,f-d\,g}\right]}{2\,f} - \frac{p\,\text{PolyLog}\left[2,\,-\frac{g\,\left(d+e\,x^2\right)}{e\,f-d\,g}\right]}{2\,f} + \frac{p\,\text{PolyLog}\left[2,\,1+\frac{e\,x^2}{d}\right]}{2\,f}$$

Result (type 4, 663 leaves)

$$\begin{split} &-\frac{1}{2\,f}\left(2\,p\,\text{Log}[x]\,\,\text{Log}\Big[1-\frac{\mathrm{i}\,\sqrt{e}\,\,x}{\sqrt{d}}\Big]+2\,p\,\text{Log}[x]\,\,\text{Log}\Big[1+\frac{\mathrm{i}\,\sqrt{e}\,\,x}{\sqrt{d}}\Big]+\\ &p\,\text{Log}\Big[\frac{\mathrm{i}\,\,\sqrt{d}}{\sqrt{e}}+x\Big]\,\,\text{Log}\Big[\frac{\sqrt{e}\,\,\left(\sqrt{f}-\mathrm{i}\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}-\sqrt{d}\,\,\sqrt{g}}\Big]+p\,\text{Log}\Big[-\frac{\mathrm{i}\,\,\sqrt{d}}{\sqrt{e}}+x\Big]\,\,\text{Log}\Big[\frac{\sqrt{e}\,\,\left(\sqrt{f}-\mathrm{i}\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big]+\\ &p\,\text{Log}\Big[-\frac{\mathrm{i}\,\,\sqrt{d}}{\sqrt{e}}+x\Big]\,\,\text{Log}\Big[\frac{\sqrt{e}\,\,\left(\sqrt{f}+\mathrm{i}\,\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}-\sqrt{d}\,\,\sqrt{g}}\Big]+p\,\text{Log}\Big[\frac{\mathrm{i}\,\,\sqrt{d}}{\sqrt{e}}+x\Big]\,\,\text{Log}\Big[\frac{\sqrt{e}\,\,\left(\sqrt{f}+\mathrm{i}\,\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big]-\\ &2\,\text{Log}[x]\,\,\text{Log}\Big[c\,\,\left(d+e\,x^2\right)^p\Big]-p\,\text{Log}\Big[-\frac{\mathrm{i}\,\,\sqrt{d}}{\sqrt{e}}+x\Big]\,\,\text{Log}\Big[f+g\,x^2\Big]-p\,\text{Log}\Big[\frac{\mathrm{i}\,\,\sqrt{d}}{\sqrt{e}}+x\Big]\,\,\text{Log}\Big[f+g\,x^2\Big]+\\ &2\,\text{Log}\Big[c\,\,\left(d+e\,x^2\right)^p\Big]\,\,\text{Log}\Big[f+g\,x^2\Big]+2\,p\,\text{PolyLog}\Big[2,\,-\frac{\mathrm{i}\,\,\sqrt{e}\,\,x}{\sqrt{d}}\Big]+2\,p\,\text{PolyLog}\Big[2,\,\frac{\mathrm{i}\,\,\sqrt{e}\,\,x}{\sqrt{d}}\Big]+\\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}-\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big]+p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big]+p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] +p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,\mathrm{i}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,\sqrt{g}}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,\mathrm{i}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}+\sqrt{d}\,\,x\right)} \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,x\right)}{-\sqrt{e}\,\,x}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,x\right)}{-\sqrt{g}\,\,x}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,x}\Big] \\ &p\,\text{PolyLog}\Big[2,\,\frac{\sqrt{g}\,\,x}\Big] \\ &p\,\text{Po$$

Problem 342: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log\left[c\,\left(d+e\,x^2\right)^p\right]}{x^3\,\left(f+g\,x^2\right)}\,\mathrm{d}x$$

Optimal (type 4, 176 leaves, 12 steps):

$$\begin{split} &\frac{e\,p\,Log\,[\,x\,]}{d\,f} - \frac{e\,p\,Log\,\big[\,d + e\,\,x^2\,\big]}{2\,d\,f} - \frac{Log\,\big[\,c\,\,\big(\,d + e\,\,x^2\,\big)^{\,p}\,\big]}{2\,f\,x^2} - \frac{g\,Log\,\big[\,-\frac{e\,x^2}{d}\,\big]\,\,Log\,\big[\,c\,\,\big(\,d + e\,\,x^2\,\big)^{\,p}\,\big]}{2\,f^2} + \\ &\frac{g\,Log\,\big[\,c\,\,\big(\,d + e\,\,x^2\,\big)^{\,p}\,\big]\,\,Log\,\big[\,\frac{e\,\,(f + g\,\,x^2)}{e\,\,f - d\,\,g}\,\big]}{2\,f^2} + \frac{g\,p\,PolyLog\,\big[\,2\,,\,\,-\frac{g\,\,(d + e\,\,x^2)}{e\,\,f - d\,\,g}\,\big]}{2\,f^2} - \frac{g\,p\,PolyLog\,\big[\,2\,,\,\,1 + \frac{e\,x^2}{d}\,\big]}{2\,f^2} \end{split}$$

Result (type 4, 791 leaves):

$$\begin{split} &\frac{1}{2\,d\,f^2\,x^2} \left[ 2\,e\,f\,p\,x^2\,Log\,[x] + 2\,d\,g\,p\,x^2\,Log\,[x]\,\,Log\big[1 - \frac{i\,\sqrt{e}\,\,x}{\sqrt{d}}\big] + \\ &2\,d\,g\,p\,x^2\,Log\,[x]\,\,Log\,\Big[1 + \frac{i\,\sqrt{e}\,\,x}{\sqrt{d}}\Big] + d\,g\,p\,x^2\,Log\,\Big[\frac{i\,\sqrt{d}}{\sqrt{e}} + x\Big]\,\,Log\,\Big[\frac{\sqrt{e}\,\,\left(\sqrt{f}\,-i\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,-\sqrt{d}\,\,\sqrt{g}}\Big] + \\ &d\,g\,p\,x^2\,Log\,\Big[-\frac{i\,\sqrt{d}}{\sqrt{e}} + x\Big]\,\,Log\,\Big[\frac{\sqrt{e}\,\,\left(\sqrt{f}\,+i\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,-\sqrt{d}\,\,\sqrt{g}}\Big] + \\ &d\,g\,p\,x^2\,Log\,\Big[-\frac{i\,\sqrt{d}}{\sqrt{e}} + x\Big]\,\,Log\,\Big[\frac{\sqrt{e}\,\,\left(\sqrt{f}\,+i\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,-\sqrt{d}\,\,\sqrt{g}}\Big] + \\ &d\,g\,p\,x^2\,Log\,\Big[\frac{i\,\sqrt{d}}{\sqrt{e}} + x\Big]\,\,Log\,\Big[\frac{\sqrt{e}\,\,\left(\sqrt{f}\,+i\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,+\sqrt{d}\,\,\sqrt{g}}\Big] - e\,f\,p\,x^2\,Log\,\Big[d\,+e\,x^2\Big] - d\,f\,Log\,\Big[c\,\,\left(d\,+e\,x^2\right)^p\Big] - \\ &2\,d\,g\,x^2\,Log\,[x]\,\,Log\,\Big[c\,\,\left(d\,+e\,x^2\right)^p\Big] - d\,g\,p\,x^2\,Log\,\Big[-\frac{i\,\sqrt{d}}{\sqrt{e}} + x\Big]\,\,Log\,\Big[f\,+g\,x^2\Big] - \\ &d\,g\,p\,x^2\,Log\,\Big[\frac{i\,\sqrt{d}}{\sqrt{e}} + x\Big]\,\,Log\,\Big[f\,+g\,x^2\Big] + d\,g\,x^2\,Log\,\Big[c\,\,\left(d\,+e\,x^2\right)^p\Big]\,\,Log\,\Big[f\,+g\,x^2\Big] + \\ &2\,d\,g\,p\,x^2\,PolyLog\,\Big[2,\,-\frac{i\,\sqrt{e}\,\,x}{\sqrt{d}}\Big] + 2\,d\,g\,p\,x^2\,PolyLog\,\Big[2,\,\frac{i\,\sqrt{e}\,\,x}{\sqrt{d}}\Big] + \\ &d\,g\,p\,x^2\,PolyLog\,\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,-i\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}\,+\sqrt{d}\,\,\sqrt{g}}\Big] + d\,g\,p\,x^2\,PolyLog\,\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,-i\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,+\sqrt{d}\,\,\sqrt{g}}\Big] \Big] + \\ &d\,g\,p\,x^2\,PolyLog\,\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,+i\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}\,+\sqrt{d}\,\,\sqrt{g}}\Big] + d\,g\,p\,x^2\,PolyLog\,\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,+i\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,+\sqrt{d}\,\,\sqrt{g}}\Big] \Big] \\ &d\,g\,p\,x^2\,PolyLog\,\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,+i\,\sqrt{e}\,\,x\right)}{-\sqrt{e}\,\,\sqrt{f}\,+\sqrt{d}\,\,\sqrt{g}}\Big] \Big] + d\,g\,p\,x^2\,PolyLog\,\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,+i\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,+\sqrt{d}\,\,\sqrt{g}}\Big] \Big] \\ &d\,g\,p\,x^2\,PolyLog\,\Big[2,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,+i\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{g}\,\,\sqrt{g}\,\,x}\Big] \Big] \Big] \\ &d\,$$

Problem 351: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int\!\frac{Log\!\left[\left.c\,\left(d+e\,x^{2}\right)^{p}\right.\right]}{x\,\left(f+g\,x^{2}\right)^{2}}\,\mathrm{d}x$$

Optimal (type 4, 201 leaves, 12 steps):

$$-\frac{e\,p\,Log\!\left[d+e\,x^{2}\right]}{2\,f\,\left(e\,f-d\,g\right)} + \frac{Log\!\left[c\,\left(d+e\,x^{2}\right)^{p}\right]}{2\,f\,\left(f+g\,x^{2}\right)} + \frac{Log\!\left[-\frac{e\,x^{2}}{d}\right]\,Log\!\left[c\,\left(d+e\,x^{2}\right)^{p}\right]}{2\,f^{2}} + \frac{e\,p\,Log\!\left[f+g\,x^{2}\right]}{2\,f\,\left(e\,f-d\,g\right)} - \frac{Log\!\left[c\,\left(d+e\,x^{2}\right)^{p}\right]\,Log\!\left[\frac{e\,\left(f+g\,x^{2}\right)}{e\,f-d\,g}\right]}{2\,f^{2}} - \frac{p\,PolyLog\!\left[2,\,-\frac{g\,\left(d+e\,x^{2}\right)}{e\,f-d\,g}\right]}{2\,f^{2}} + \frac{p\,PolyLog\!\left[2,\,1+\frac{e\,x^{2}}{d}\right]}{2\,f^{2}}$$

Result (type 4, 1124 leaves):

$$\begin{split} &-\frac{1}{4\,f^2}\left[\frac{\mathrm{i}\,\sqrt{f}\,\,p\,\mathrm{Log}\left[-\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]}{-\mathrm{i}\,\sqrt{f}\,\,+\sqrt{g}\,\,x} - \frac{\mathrm{i}\,\sqrt{f}\,\,p\,\mathrm{Log}\left[\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]}{\mathrm{i}\,\sqrt{f}\,\,+\sqrt{g}\,\,x} + \frac{\mathrm{i}\,\sqrt{f}\,\,p\,\mathrm{Log}\left[\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]}{-\mathrm{i}\,\sqrt{f}\,\,+\sqrt{g}\,\,x} - \frac{\mathrm{i}\,\sqrt{f}\,\,p\,\mathrm{Log}\left[\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]}{\mathrm{i}\,\sqrt{f}\,\,+\sqrt{g}\,\,x} + \frac{\mathrm{i}\,\sqrt{f}\,\,p\,\mathrm{Log}\left[\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]}{-\mathrm{i}\,\sqrt{f}\,\,+\sqrt{g}\,\,x} - \frac{\mathrm{i}\,\sqrt{f}\,\,p\,\mathrm{Log}\left[\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]}{\mathrm{i}\,\sqrt{f}\,\,+\sqrt{g}\,\,x} + \frac{2\,f\,\,p\,\mathrm{Log}\left[\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]}{f\,+g\,x^2} + 4\,p\,\mathrm{Log}\left[x\right]\,\mathrm{Log}\left[1 - \frac{\mathrm{i}\,\sqrt{e}\,\,x}{\sqrt{d}}\right] + 4\,p\,\mathrm{Log}\left[x\right]\,\mathrm{Log}\left[1 + \frac{\mathrm{i}\,\sqrt{e}\,\,x}{\sqrt{d}}\right] + \\ 2\,p\,\mathrm{Log}\left[\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]\,\mathrm{Log}\left[\frac{\sqrt{e}\,\,\left(\sqrt{f}\,\,-\,\mathrm{i}\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,\,-\,\sqrt{d}\,\,\sqrt{g}}\right] + 2\,p\,\mathrm{Log}\left[-\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]\,\mathrm{Log}\left[\frac{\sqrt{e}\,\,\left(\sqrt{f}\,\,-\,\mathrm{i}\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,\,-\,\sqrt{d}\,\,\sqrt{g}}\right] + 2\,p\,\mathrm{Log}\left[\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]\,\mathrm{Log}\left[\frac{\sqrt{e}\,\,\left(\sqrt{f}\,\,+\,\mathrm{i}\,\sqrt{g}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,\,-\,\sqrt{d}\,\,\sqrt{g}}\right] + \\ 2\,p\,\mathrm{Log}\left[-\frac{\mathrm{i}\,\sqrt{d}}{\sqrt{e}}+x\right]\,\mathrm{Log}\left[\frac{\sqrt{e}\,\,\sqrt{f}\,\,-\,\sqrt{d}\,\,\sqrt{g}}{\sqrt{e}\,\,\sqrt{f}\,\,-\,\sqrt{d}\,\,\sqrt{g}}\right] - \frac{2\,f\,\mathrm{Log}\left[c\,\,\left(d\,+\,e\,x^2\right)^p\right]}{f\,+\,g\,x^2} - \\ 4\,\mathrm{Log}\left[x\right]\,\mathrm{Log}\left[c\,\,\left(d\,+\,e\,x^2\right)^p\right] - \frac{\sqrt{e}\,\,\sqrt{f}\,\,p\,\mathrm{Log}\left[f\,+\,g\,x^2\right]}{\sqrt{e}\,\,\sqrt{f}\,\,-\,\sqrt{d}\,\,\sqrt{g}} - \frac{\sqrt{e}\,\,\sqrt{f}\,\,p\,\mathrm{Log}\left[f\,+\,g\,x^2\right]}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} - \frac{2\,f\,\mathrm{Log}\left[f\,+\,g\,x^2\right]}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} - \frac{2\,p\,\mathrm{Log}\left[f\,+\,g\,x^2\right]}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} - \frac{2\,p\,\mathrm{Log}\left[f\,+\,g\,x^2\right]}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} - \frac{2\,p\,\mathrm{Log}\left[f\,+\,g\,x^2\right]}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} + x\right]\,\mathrm{Log}\left[f\,+\,g\,x^2\right] + 2\,p\,\mathrm{PolyLog}\left[2,\,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,-\,\mathrm{i}\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} \right] + \\ 2\,p\,\mathrm{PolyLog}\left[2,\,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,-\,\mathrm{i}\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} \right] + 2\,p\,\mathrm{PolyLog}\left[2,\,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,-\,\mathrm{i}\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} \right]} + 2\,p\,\mathrm{PolyLog}\left[2,\,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,-\,\mathrm{i}\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} \right] + 2\,p\,\mathrm{PolyLog}\left[2,\,\,\frac{\sqrt{g}\,\,\left(\sqrt{d}\,\,-\,\mathrm{i}\,\sqrt{e}\,\,x\right)}{\sqrt{e}\,\,\sqrt{f}\,\,+\,\sqrt{d}\,\,\sqrt{g}} \right]}$$

Problem 352: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log\left[c\,\left(d+e\,x^2\right)^p\right]}{x^3\,\left(f+g\,x^2\right)^2}\,\mathrm{d}x$$

Optimal (type 4, 251 leaves, 16 steps):

$$\begin{split} &\frac{e\,p\,Log\,[\,x\,]}{d\,f^2} - \frac{e\,p\,Log\,[\,d + e\,\,x^2\,]}{2\,d\,f^2} + \frac{e\,g\,p\,Log\,[\,d + e\,\,x^2\,]}{2\,f^2\,\left(\,e\,f - d\,g\right)} - \frac{Log\,[\,c\,\,\left(\,d + e\,\,x^2\,\right)^{\,p}\,]}{2\,f^2\,x^2} - \\ &\frac{g\,Log\,[\,c\,\,\left(\,d + e\,\,x^2\,\right)^{\,p}\,]}{2\,f^2\,\left(\,f + g\,\,x^2\,\right)} - \frac{g\,Log\,[\,-\,\frac{e\,x^2}{d}\,]\,\,Log\,[\,c\,\,\left(\,d + e\,\,x^2\,\right)^{\,p}\,]}{f^3} - \frac{e\,g\,p\,Log\,[\,f + g\,\,x^2\,]}{2\,f^2\,\left(\,e\,f - d\,g\right)} + \\ &\frac{g\,Log\,[\,c\,\,\left(\,d + e\,\,x^2\,\right)^{\,p}\,]\,\,Log\,[\,\frac{e\,\,(f + g\,x^2\,)}{e\,\,f - d\,g}\,]}{f^3} + \frac{g\,p\,PolyLog\,[\,2\,,\,\,-\,\frac{g\,\,(d + e\,x^2\,)}{e\,\,f - d\,g}\,]}{f^3} - \frac{g\,p\,PolyLog\,[\,2\,,\,\,1 + \frac{e\,x^2}{d}\,]}{f^3} \end{split}$$

Result (type 4, 1197 leaves):

$$\frac{1}{4\,f^3} \left( \frac{4\,e\,f\,p\,Log\left[ x \right]}{d} + \frac{i\,\sqrt{f}\,g\,p\,Log\left[ - \frac{i\,\sqrt{d}}{\sqrt{e}} + x \right]}{-i\,\sqrt{f} + \sqrt{g}\,x} - \frac{i\,\sqrt{f}\,g\,p\,Log\left[ - \frac{i\,\sqrt{d}}{\sqrt{e}} + x \right]}{i\,\sqrt{f} + \sqrt{g}\,x} + \frac{2\,f\,g\,p\,Log\left[ - \frac{i\,\sqrt{d}}{\sqrt{e}} + x \right]}{f + g\,x^2} + \frac{i\,\sqrt{f}\,g\,p\,Log\left[ \frac{i\,\sqrt{d}}{\sqrt{e}} + x \right]}{-i\,\sqrt{f} + \sqrt{g}\,x} - \frac{i\,\sqrt{f}\,g\,p\,Log\left[ \frac{i\,\sqrt{d}}{\sqrt{e}} + x \right]}{i\,\sqrt{f} + \sqrt{g}\,x} + \frac{2\,f\,g\,p\,Log\left[ \frac{i\,\sqrt{d}}{\sqrt{e}} + x \right]}{f + g\,x^2} + 8\,g\,p\,Log\left[ x \right]\,Log\left[ 1 - \frac{i\,\sqrt{e}\,x}{\sqrt{d}} \right] + \\ 8\,g\,p\,Log\left[ x \right]\,Log\left[ 1 + \frac{i\,\sqrt{e}\,x}{\sqrt{d}} \right] + 4\,g\,p\,Log\left[ \frac{i\,\sqrt{d}}{\sqrt{e}} + x \right]\,Log\left[ \frac{\sqrt{e}\,\left( \sqrt{f} - i\,\sqrt{g}\,x \right)}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} \right] + \\ 4\,g\,p\,Log\left[ - \frac{i\,\sqrt{d}}{\sqrt{e}} + x \right]\,Log\left[ \frac{\sqrt{e}\,\left( \sqrt{f} + i\,\sqrt{g}\,x \right)}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} \right] + \\ 4\,g\,p\,Log\left[ - \frac{i\,\sqrt{d}}{\sqrt{e}} + x \right]\,Log\left[ \frac{\sqrt{e}\,\left( \sqrt{f} + i\,\sqrt{g}\,x \right)}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} \right] - \frac{2\,e\,f\,p\,Log\left[ d + e\,x^2 \right]}{d} + \\ \frac{\sqrt{e}\,\sqrt{f}\,g\,p\,Log\left[ d + e\,x^2 \right]}{\sqrt{e}\,\sqrt{f} + \sqrt{d}\,\sqrt{g}} - \frac{2\,f\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,f\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}}} + \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}} - \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f} - \sqrt{d}\,\sqrt{g}}} + \frac{2\,g\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f}\,Log\left[ c\,\left( d + e\,x^2 \right)^p \right]} - \frac{2\,g\,Log\left[ e\,\left( e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f}\,Log\left[ e\,\left( e\,x^2 \right)^p \right]}} + \frac{2\,g\,Log\left[ e\,\left( e\,\left( e\,x^2 \right)^p \right]}{\sqrt{e}\,\sqrt{f}\,Log\left[ e\,\left( e\,\left( e\,x^2$$

Problem 359: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{Log\left[d+e\;x^2\right]}{1-x^2}\;\mathrm{d}x$$

Optimal (type 4, 217 leaves, 11 steps):

$$2 \operatorname{ArcTanh}[x] \operatorname{Log}\left[\frac{2}{1+x}\right] - \operatorname{ArcTanh}[x] \operatorname{Log}\left[\frac{2\left(\sqrt{-d} - \sqrt{e} \ x\right)}{\left(\sqrt{-d} - \sqrt{e}\ \right) \left(1+x\right)}\right] - \\ \operatorname{ArcTanh}[x] \operatorname{Log}\left[\frac{2\left(\sqrt{-d} + \sqrt{e} \ x\right)}{\left(\sqrt{-d} + \sqrt{e}\ \right) \left(1+x\right)}\right] + \operatorname{ArcTanh}[x] \operatorname{Log}\left[d + e \ x^2\right] - \operatorname{PolyLog}\left[2, \ 1 - \frac{2}{1+x}\right] + \\ \frac{1}{2} \operatorname{PolyLog}\left[2, \ 1 - \frac{2\left(\sqrt{-d} - \sqrt{e} \ x\right)}{\left(\sqrt{-d} - \sqrt{e}\ x\right) \left(1+x\right)}\right] + \frac{1}{2} \operatorname{PolyLog}\left[2, \ 1 - \frac{2\left(\sqrt{-d} + \sqrt{e} \ x\right)}{\left(\sqrt{-d} + \sqrt{e}\ x\right) \left(1+x\right)}\right]$$

Result (type 4, 468 leaves)

$$\frac{1}{2} \left( \text{Log} [1-x] \text{ Log} \Big[ -\frac{\text{i} \sqrt{d}}{\sqrt{e}} + x \Big] - \text{Log} \Big[ \frac{\sqrt{e} \left( -1 + x \right)}{\text{i} \sqrt{d} - \sqrt{e}} \Big] \text{ Log} \Big[ -\frac{\text{i} \sqrt{d}}{\sqrt{e}} + x \Big] - \\ \text{Log} [1+x] \text{ Log} \Big[ -\frac{\text{i} \sqrt{d}}{\sqrt{e}} + x \Big] + \text{Log} \Big[ -\frac{\text{i} \sqrt{e} \left( 1 + x \right)}{\sqrt{d} - \text{i} \sqrt{e}} \Big] \text{ Log} \Big[ -\frac{\text{i} \sqrt{d}}{\sqrt{e}} + x \Big] + \\ \text{Log} [1-x] \text{ Log} \Big[ \frac{\text{i} \sqrt{d}}{\sqrt{e}} + x \Big] - \text{Log} \Big[ \frac{\sqrt{e} \left( -1 + x \right)}{-\text{i} \sqrt{d} - \sqrt{e}} \Big] \text{ Log} \Big[ \frac{\text{i} \sqrt{d}}{\sqrt{e}} + x \Big] - \\ \text{Log} [1+x] \text{ Log} \Big[ \frac{\text{i} \sqrt{d}}{\sqrt{e}} + x \Big] + \text{Log} \Big[ \frac{\text{i} \sqrt{e} \left( 1 + x \right)}{\sqrt{d} + \text{i} \sqrt{e}} \Big] \text{ Log} \Big[ \frac{\text{i} \sqrt{d}}{\sqrt{e}} + x \Big] - \\ \text{Log} [1-x] \text{ Log} \Big[ d + e x^2 \Big] + \text{Log} [1+x] \text{ Log} \Big[ d + e x^2 \Big] - \text{PolyLog} \Big[ 2, \frac{\sqrt{d} - \text{i} \sqrt{e} x}{\sqrt{d} - \text{i} \sqrt{e}} \Big] + \\ \text{PolyLog} \Big[ 2, \frac{\sqrt{d} - \text{i} \sqrt{e} x}{\sqrt{d} + \text{i} \sqrt{e}} \Big] + \text{PolyLog} \Big[ 2, \frac{\sqrt{d} + \text{i} \sqrt{e} x}{\sqrt{d} - \text{i} \sqrt{e}} \Big] - \text{PolyLog} \Big[ 2, \frac{\sqrt{d} + \text{i} \sqrt{e} x}{\sqrt{d} + \text{i} \sqrt{e}} \Big] \right)$$

Problem 370: Unable to integrate problem.

$$\int \frac{Log\left[c\,\left(d+e\,x^n\right)^p\right]}{x\,\left(f+g\,x^{2\,n}\right)}\,\mathrm{d}x$$

Optimal (type 4, 266 leaves, 13 steps):

$$\frac{\text{Log} \left[ -\frac{e\,x^n}{d} \right] \, \text{Log} \left[ c \, \left( d + e\,x^n \right)^p \right]}{\text{f n}} - \frac{\text{Log} \left[ c \, \left( d + e\,x^n \right)^p \right] \, \text{Log} \left[ \frac{e \left( \sqrt{-f} - \sqrt{g}\,x^n \right)}{e \,\sqrt{-f} + d \,\sqrt{g}} \right]}{2 \, f \, n} - \frac{2 \, f \, n}{ \\ \frac{\text{Log} \left[ c \, \left( d + e\,x^n \right)^p \right] \, \text{Log} \left[ \frac{e \left( \sqrt{-f} + \sqrt{g}\,x^n \right)}{e \,\sqrt{-f} - d \,\sqrt{g}} \right]}{e \, \sqrt{-f} - d \,\sqrt{g}} - \frac{p \, \text{PolyLog} \left[ 2 \text{, } -\frac{\sqrt{g} \, \left( d + e\,x^n \right)}{e \, \sqrt{-f} - d \,\sqrt{g}} \right]}{2 \, f \, n} - \frac{p \, \text{PolyLog} \left[ 2 \text{, } 1 + \frac{e\,x^n}{d} \right]}{2 \, f \, n} - \frac{p \, \text{PolyLog} \left[ 2 \text{, } 1 + \frac{e\,x^n}{d} \right]}{f \, n}$$

Result (type 8, 29 leaves):

$$\int \frac{Log\left[\left.c\right.\left(d+e|x^{n}\right)^{p}\right]}{x\left.\left(f+g|x^{2|n}\right)\right.} \, \mathrm{d}x$$

### Problem 371: Unable to integrate problem.

$$\int \frac{Log\left[\left.c\right.\left(d+e\left.x^{n}\right)\right.^{p}\right]}{x\left.\left(f+g\left.x^{n}\right.\right)}\,\mathrm{d}x$$

Optimal (type 4, 121 leaves, 8 steps):

$$\begin{split} \frac{Log\left[-\frac{e\,x^{n}}{d}\right]\,Log\left[c\,\left(d+e\,x^{n}\right)^{\,p}\right]}{f\,n} &-\frac{Log\left[c\,\left(d+e\,x^{n}\right)^{\,p}\right]\,Log\left[\frac{e\,\left(f+g\,x^{n}\right)}{e\,f-d\,g}\right]}{f\,n} - \\ \frac{p\,PolyLog\left[2\,\text{, } -\frac{g\,\left(d+e\,x^{n}\right)}{e\,f-d\,g}\right]}{f\,n} &+\frac{p\,PolyLog\left[2\,\text{, } 1+\frac{e\,x^{n}}{d}\right]}{f\,n} \end{split}$$

Result (type 8, 27 leaves):

$$\int \frac{Log\left[\left.c\right.\left(d+e\,x^{n}\right)^{p}\right]}{x\,\left(f+g\,x^{n}\right)}\,\mathrm{d}x$$

## Problem 372: Unable to integrate problem.

$$\int \frac{Log\left[\left.c\right.\left(d+e|x^{n}\right)\right.^{p}\right]}{x\left.\left(f+g|x^{-n}\right)\right.} \; \mathrm{d}x$$

Optimal (type 4, 70 leaves, 5 steps):

$$\frac{Log\left[\left.c\left(d+e\,x^{n}\right)^{\,p}\right]\,Log\left[-\frac{e\,\left(g+f\,x^{n}\right)}{d\,f-e\,g}\right]}{f\,n}+\frac{p\,PolyLog\left[\left.2\text{, }\frac{f\,\left(d+e\,x^{n}\right)}{d\,f-e\,g}\right]}{f\,n}$$

Result (type 8, 29 leaves):

$$\int\!\frac{Log\!\left[\left.c\,\left(d+e\,x^{n}\right)^{\,p}\right.\right]}{x\,\left(f+g\,x^{-n}\right)}\;\mathrm{d}x$$

### Problem 373: Unable to integrate problem.

$$\int \frac{Log\left[\left.c\right.\left(d+e\,x^{n}\right)^{\,p}\right]}{x\,\left(f+g\,x^{-2\,n}\right)}\,\mathrm{d}x$$

Optimal (type 4, 221 leaves, 9 steps):

$$\frac{\text{Log}\left[c\,\left(d+e\,x^{n}\right)^{p}\right]\,\text{Log}\left[\frac{e\left(\sqrt{g}\,-\sqrt{-f}\,x^{n}\right)}{d\,\sqrt{-f}\,+e\,\sqrt{g}}\right]}{2\,f\,n}\,+\,\frac{\text{Log}\left[c\,\left(d+e\,x^{n}\right)^{p}\right]\,\text{Log}\left[-\frac{e\left(\sqrt{g}\,+\sqrt{-f}\,x^{n}\right)}{d\,\sqrt{-f}\,-e\,\sqrt{g}}\right]}{2\,f\,n}\,+\,\frac{p\,\text{PolyLog}\!\left[2\,\text{,}\,\frac{\sqrt{-f}\,\left(d+e\,x^{n}\right)}{d\,\sqrt{-f}\,+e\,\sqrt{g}}\right]}{2\,f\,n}\,+\,\frac{p\,\text{PolyLog}\!\left[2\,\text{,}\,\frac{\sqrt{-f}\,\left(d+e\,x^{n}\right)}{d\,\sqrt{-f}\,+e\,\sqrt{g}}\right]}{2\,f\,n}$$

#### Result (type 8, 29 leaves):

$$\int \frac{Log\left[\left.c\right.\left(d+e\,x^{n}\right)^{\,p}\right]}{x\,\left(f+g\,x^{-2\,n}\right)}\,\mathrm{d}x$$

### Problem 374: Unable to integrate problem.

$$\int\!\frac{Log\!\left[\left.c\,\left(d+e\,x^{n}\right)^{\,p}\right]}{x\,\left(f+g\,x^{2\,n}\right)^{\,2}}\,\mathrm{d}x$$

Optimal (type 4, 419 leaves, 19 steps):

$$\frac{\text{d}\,e\,\sqrt{g}\,\,p\,\text{ArcTan}\Big[\frac{\sqrt{g}\,\,x^{n}}{\sqrt{f}}\Big]}{2\,\,f^{3/2}\,\,\Big(e^{2}\,\,f+d^{2}\,g\Big)\,\,n} - \frac{e^{2}\,p\,\,\text{Log}\,[\,d+e\,\,x^{n}\,]}{2\,\,f\,\,\Big(e^{2}\,\,f+d^{2}\,g\Big)\,\,n} + \frac{\text{Log}\,[\,c\,\,\big(d+e\,\,x^{n}\,\big)^{\,p}\,\big]}{2\,\,f\,\,n\,\,\Big(f+g\,\,x^{2\,\,n}\,\Big)} + \frac{\text{Log}\,[\,c\,\,\big(d+e\,\,x^{n}\,\big)^{\,p}\,\big]}{f^{2}\,\,n} - \frac{\text{Log}\,[\,c\,\,\big(d+e\,\,x^{n}\,\big)^{\,p}\,\big]}{2\,\,f^{2}\,\,n} - \frac{\text{Log}\,[\,c\,\,\big(d+e\,\,x^{n}\,\big)^{\,p}\,\big]}{2\,\,f^{2}\,\,n} + \frac{\text{Log}\,[\,e\,\,\frac{e\,\,x^{n}\,\,g}\,\,x^{n}\,\big)}{e\,\,\sqrt{-f}\,\,d\,\,\sqrt{g}}\,\,\Big]}{2\,\,f^{2}\,\,n} + \frac{e^{2}\,p\,\,\text{Log}\,[\,f+g\,\,x^{2\,\,n}\,\big)}{4\,\,f\,\,\big(e^{2}\,\,f+d^{2}\,g\big)\,\,n} - \frac{p\,\,\text{PolyLog}\,[\,2\,,\,\,\frac{\sqrt{g}\,\,(d+e\,\,x^{n}\,\big)}{e\,\,\sqrt{-f}\,\,d\,\,\sqrt{g}}\,\,\big]}{2\,\,f^{2}\,\,n} + \frac{p\,\,\text{PolyLog}\,[\,2\,,\,\,1+\frac{e\,\,x^{n}}{d}\,\big]}{f^{2}\,\,n} + \frac{p\,\,\text{PolyLog}\,[\,2\,,\,\,1+\frac{e\,\,x^{n}}{d}\,\big]}{g^{2}\,\,n} + \frac{p\,\,x^{n}\,\,n}{q^{2}$$

Result (type 8, 29 leaves):

$$\int \frac{Log\left[\left.c\right.\left(d+e\,x^{n}\right)^{\,p}\right]}{x\,\left(f+g\,x^{2\,n}\right)^{\,2}}\;\mathrm{d}x$$

# Problem 375: Unable to integrate problem.

$$\int \frac{Log\left[\,c\,\left(d+e\,x^n\right)^{\,p}\,\right]}{x\,\left(\,f+g\,x^n\right)^{\,2}}\,\,\mathrm{d}x$$

Optimal (type 4, 204 leaves, 12 steps):

$$-\frac{e\,p\,Log\left[d+e\,x^{n}\right]}{f\left(e\,f-d\,g\right)\,n}+\frac{Log\left[c\,\left(d+e\,x^{n}\right)^{p}\right]}{f\,n\,\left(f+g\,x^{n}\right)}+\frac{Log\left[-\frac{e\,x^{n}}{d}\right]\,Log\left[c\,\left(d+e\,x^{n}\right)^{p}\right]}{f^{2}\,n}+\frac{e\,p\,Log\left[f+g\,x^{n}\right]}{f\left(e\,f-d\,g\right)\,n}-\frac{Log\left[c\,\left(d+e\,x^{n}\right)^{p}\right]\,Log\left[\frac{e\,\left(f+g\,x^{n}\right)}{e\,f-d\,g}\right]}{f^{2}\,n}-\frac{p\,PolyLog\left[2,\,-\frac{g\,\left(d+e\,x^{n}\right)}{e\,f-d\,g}\right]}{f^{2}\,n}+\frac{p\,PolyLog\left[2,\,1+\frac{e\,x^{n}}{d}\right]}{f^{2}\,n}$$

Result (type 8, 27 leaves):

$$\int\!\frac{Log\!\left[\left.c\,\left(d+e\,x^{n}\right)^{\,p}\right.\right]}{x\,\left(f+g\,x^{n}\right)^{\,2}}\,\mathrm{d}x$$

#### Problem 376: Unable to integrate problem.

$$\int \frac{Log\left[\left.c\,\left(d+e\,x^{n}\right)^{\,p}\right.\right]}{x\,\left(f+g\,x^{-n}\right)^{\,2}}\,\,\mathrm{d}x$$

Optimal (type 4, 156 leaves, 10 steps)

$$\frac{e \ g \ p \ Log \left[d+e \ x^n\right]}{f^2 \ \left(d \ f-e \ g\right) \ n} + \frac{g \ Log \left[c \ \left(d+e \ x^n\right)^p\right]}{f^2 \ n \ \left(g+f \ x^n\right)} - \frac{e \ g \ p \ Log \left[g+f \ x^n\right]}{f^2 \ \left(d \ f-e \ g\right) \ n} + \frac{Log \left[c \ \left(d+e \ x^n\right)^p\right] \ Log \left[-\frac{e \ \left(g+f \ x^n\right)}{d \ f-e \ g}\right]}{f^2 \ n} + \frac{p \ Poly Log \left[2, \ \frac{f \ \left(d+e \ x^n\right)}{d \ f-e \ g}\right]}{f^2 \ n}$$

Result (type 8, 29 leaves):

$$\int\!\frac{Log\!\left[\left.c\,\left(d+e\,x^{n}\right)^{p}\right.\right]}{x\,\left(f+g\,x^{-n}\right)^{2}}\,\mathrm{d}x$$

# Problem 377: Unable to integrate problem.

$$\int\!\frac{Log\!\left[\left.c\,\left(d+e\,x^{n}\right)^{p}\right.\right]}{x\,\left(f+g\,x^{-2\,n}\right)^{2}}\,\mathrm{d}x$$

Optimal (type 4, 377 leaves, 17 steps):

$$-\frac{d\,e\,\sqrt{g}\,\,p\,\text{ArcTan}\Big[\frac{\sqrt{f}\,\,x^{n}}{\sqrt{g}}\Big]}{2\,f^{3/2}\,\left(d^{2}\,f+e^{2}\,g\right)\,n} - \frac{e^{2}\,g\,p\,\text{Log}\,[\,d+e\,x^{n}\,]}{2\,f^{2}\,\left(d^{2}\,f+e^{2}\,g\right)\,n} + \frac{g\,\text{Log}\,[\,c\,\left(d+e\,x^{n}\right)^{\,p}\,]}{2\,f^{2}\,n\,\left(g+f\,x^{2\,n}\right)} + \frac{Log\,[\,c\,\left(d+e\,x^{n}\right)^{\,p}\,]}{2\,f^{2}\,n\,\left(g+f\,x^{2\,n}\right)} + \frac{Log\,[\,c\,\left(d+e\,x^{n}\right)^{\,p}\,]\,\text{Log}\,[\,-\frac{e\,\left(\sqrt{g}\,+\sqrt{-f}\,\,x^{n}\right)}{d\,\sqrt{-f}\,-e\,\sqrt{g}}\,]}{2\,f^{2}\,n} + \frac{e^{2}\,g\,p\,\text{Log}\,[\,g+f\,x^{2\,n}\,]}{2\,f^{2}\,n} + \frac{p\,\text{PolyLog}\,[\,2\,,\,\frac{\sqrt{-f}\,\left(d+e\,x^{n}\right)}{d\,\sqrt{-f}\,-e\,\sqrt{g}}\,]}{2\,f^{2}\,n} + \frac{p\,\text{PolyLog}\,[\,2\,,\,\frac{\sqrt{-f}\,\left(d+e\,x^{n}\right)}{d\,\sqrt{-f}\,+e\,\sqrt{g}}\,]}{2\,f^{2}\,n} + \frac{p\,\text{PolyLog}\,[\,2\,,\,\frac{\sqrt{-f}\,\left(d+e\,x^{n}\right)}{d\,\sqrt{-f}\,+e\,\sqrt{g}}\,]}{2\,f^{2}\,n}$$

Result (type 8, 29 leaves):

$$\int \frac{Log\left[\left.c\right.\left(d+e\,x^{n}\right)^{\,p}\right]}{x\,\left(f+g\,x^{-2\,n}\right)^{\,2}}\;\mathrm{d}x$$

## Problem 380: Unable to integrate problem.

$$\int \frac{Log\left[c\,\left(d+e\,x^{-n}\right)\,\right]}{x\,\left(c\,e-\,\left(1-c\,d\right)\,x^{n}\right)}\,\mathrm{d}x$$

Optimal (type 4, 26 leaves, 4 steps):

$$\frac{\text{PolyLog}\left[2,\ 1-c\ \left(d+e\ x^{-n}\right)\ \right]}{c\ e\ n}$$

Result (type 8, 35 leaves):

$$\int \frac{Log \left[ \left. c \, \left( d + e \, x^{-n} \right) \, \right]}{x \, \left( c \, e - \left( 1 - c \, d \right) \, x^n \right)} \, \mathrm{d}x$$

### Problem 392: Result more than twice size of optimal antiderivative.

$$\int\!\frac{Log\!\left[\,x^{-n}\,\left(\,a\,+\,x^{n}\,\right)\,\right]}{x}\;\mathrm{d}\,x$$

Optimal (type 4, 14 leaves, 2 steps):

Result (type 4, 51 leaves):

$$\frac{1}{2} \, \text{Log} \, \big[ \, x \, \big] \, \left( n \, \text{Log} \, \big[ \, x \, \big] \, + \, 2 \, \text{Log} \, \Big[ \, 1 \, + \, a \, x^{-n} \, \Big] \, - \, 2 \, \text{Log} \, \Big[ \, \frac{a \, + \, x^n}{a} \, \Big] \, \right) \, - \, \frac{\text{PolyLog} \, \big[ \, 2 \, , \, - \, \frac{x^n}{a} \, \big]}{n} \,$$

## Problem 397: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\mathsf{Log}\left[\frac{\mathsf{a}+\mathsf{b}\,\mathsf{x}^2}{\mathsf{x}^2}\right]}{\mathsf{c}+\mathsf{d}\,\mathsf{x}}\,\mathsf{d}\,\mathsf{x}$$

Optimal (type 4, 227 leaves, 14 steps):

$$\frac{\text{Log}\left[b + \frac{a}{x^2}\right] \, \text{Log}\left[c + d\,x\right]}{d} + \frac{2 \, \text{Log}\left[-\frac{d\,x}{c}\right] \, \text{Log}\left[c + d\,x\right]}{d} - \\ \frac{\text{Log}\left[\frac{d\left(\sqrt{-a} - \sqrt{b}\,x\right)}{\sqrt{b}\,\,c + \sqrt{-a}\,\,d}\right] \, \text{Log}\left[c + d\,x\right]}{d} - \frac{\text{Log}\left[-\frac{d\left(\sqrt{-a} + \sqrt{b}\,x\right)}{\sqrt{b}\,\,c - \sqrt{-a}\,\,d}\right] \, \text{Log}\left[c + d\,x\right]}{d} - \\ \frac{\text{PolyLog}\left[2, \, \frac{\sqrt{b}\,\,(c + d\,x)}{\sqrt{b}\,\,c - \sqrt{-a}\,\,d}\right]}{d} - \frac{\text{PolyLog}\left[2, \, \frac{\sqrt{b}\,\,(c + d\,x)}{\sqrt{b}\,\,c + \sqrt{-a}\,\,d}\right]}{d} + \frac{2 \, \text{PolyLog}\left[2, \, 1 + \frac{d\,x}{c}\right]}{d}$$

Result (type 4, 284 leaves):

$$\begin{split} &\frac{1}{d}\left[\text{Log}\left[b+\frac{a}{x^2}\right]\text{Log}\left[c+d\,x\right]+2\,\text{Log}\left[x\right]\,\text{Log}\left[c+d\,x\right]-\text{Log}\left[-\frac{\text{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,\text{Log}\left[c+d\,x\right]-\text{Log}\left[\frac{\text{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,\text{Log}\left[c+d\,x\right]-\text{Log}\left[\frac{\text{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,\text{Log}\left[\frac{\text{i}\,\sqrt{a}}{\sqrt{b}\,c-\text{i}\,\sqrt{a}\,d}\right]+\text{Log}\left[-\frac{\text{i}\,\sqrt{a}}{\sqrt{b}}+x\right]\,\text{Log}\left[\frac{\sqrt{b}\,\left(c+d\,x\right)}{\sqrt{b}\,c+\text{i}\,\sqrt{a}\,d}\right]-2\,\text{Log}\left[x\right]\,\text{Log}\left[1+\frac{d\,x}{c}\right]-2\,\text{PolyLog}\left[2,-\frac{d\,x}{c}\right]+\text{PolyLog}\left[2,\frac{d\,\left(\sqrt{a}\,-\text{i}\,\sqrt{b}\,x\right)}{\text{i}\,\sqrt{b}\,c+\sqrt{a}\,d}\right]+\text{PolyLog}\left[2,\frac{d\,\left(\sqrt{a}\,+\text{i}\,\sqrt{b}\,x\right)}{-\text{i}\,\sqrt{b}\,c+\sqrt{a}\,d}\right] \end{split}$$

#### Problem 411: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \log\left[c \left(d + e \sqrt{x}\right)^{n}\right]\right)^{2}}{x} dx$$

Optimal (type 4, 93 leaves, 5 steps):

$$\begin{split} &2\left(a+b\,\text{Log}\left[\,c\,\left(d+e\,\sqrt{x}\,\right)^{\,n}\,\right]\,\right)^{\,2}\,\text{Log}\left[\,-\,\frac{e\,\sqrt{x}}{d}\,\right]\,+\\ &4\,b\,n\,\left(a+b\,\text{Log}\left[\,c\,\left(d+e\,\sqrt{x}\,\right)^{\,n}\,\right]\,\right)\,\text{PolyLog}\left[\,2\,,\,1+\frac{e\,\sqrt{x}}{d}\,\right]\,-\,4\,b^{2}\,n^{2}\,\text{PolyLog}\left[\,3\,,\,1+\frac{e\,\sqrt{x}}{d}\,\right]\,. \end{split}$$

Result (type 4, 195 leaves):

$$\begin{split} &\left(\mathsf{a}-\mathsf{b}\,\mathsf{n}\,\mathsf{Log}\left[\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right]+\mathsf{b}\,\mathsf{Log}\left[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^\mathsf{n}\right]\right)^2\,\mathsf{Log}\left[\mathsf{x}\right]\,+\\ &2\,\mathsf{b}\,\mathsf{n}\,\left(\mathsf{a}-\mathsf{b}\,\mathsf{n}\,\mathsf{Log}\left[\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right]+\mathsf{b}\,\mathsf{Log}\left[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^\mathsf{n}\right]\right)\\ &\left(\left(\mathsf{Log}\left[\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right]-\mathsf{Log}\left[\mathsf{1}+\frac{\mathsf{e}\,\sqrt{\mathsf{x}}}{\mathsf{d}}\right]\right)\,\mathsf{Log}\left[\mathsf{x}\right]-2\,\mathsf{PolyLog}\left[\mathsf{2}\,,\,-\frac{\mathsf{e}\,\sqrt{\mathsf{x}}}{\mathsf{d}}\right]\right)\,+\\ &2\,\mathsf{b}^2\,\mathsf{n}^2\,\left(\mathsf{Log}\left[\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right]^2\,\mathsf{Log}\left[-\frac{\mathsf{e}\,\sqrt{\mathsf{x}}}{\mathsf{d}}\right]\right.\\ &\left.2\,\mathsf{Log}\left[\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right]\,\mathsf{PolyLog}\left[\mathsf{2}\,,\,\mathsf{1}+\frac{\mathsf{e}\,\sqrt{\mathsf{x}}}{\mathsf{d}}\right]-2\,\mathsf{PolyLog}\left[\mathsf{3}\,,\,\mathsf{1}+\frac{\mathsf{e}\,\sqrt{\mathsf{x}}}{\mathsf{d}}\right]\right) \end{split}$$

# Problem 418: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \log\left[c \left(d + e \sqrt{x}\right)^{n}\right]\right)^{3}}{x} dx$$

Optimal (type 4, 135 leaves, 6 steps):

$$\begin{split} &2\left(a+b\,\text{Log}\left[c\,\left(d+e\,\sqrt{x}\,\right)^n\right]\right)^3\,\text{Log}\left[-\frac{e\,\sqrt{x}}{d}\right] +\\ &6\,b\,n\,\left(a+b\,\text{Log}\left[c\,\left(d+e\,\sqrt{x}\,\right)^n\right]\right)^2\,\text{PolyLog}\left[2\,,\,1+\frac{e\,\sqrt{x}}{d}\right] -\\ &12\,b^2\,n^2\,\left(a+b\,\text{Log}\left[c\,\left(d+e\,\sqrt{x}\,\right)^n\right]\right)\,\text{PolyLog}\left[3\,,\,1+\frac{e\,\sqrt{x}}{d}\right] + 12\,b^3\,n^3\,\text{PolyLog}\left[4\,,\,1+\frac{e\,\sqrt{x}}{d}\right] \end{split}$$

#### Result (type 4, 333 leaves):

$$\begin{split} &\left(a-b\,n\,\text{Log}\left[d+e\,\sqrt{x}\,\right]+b\,\text{Log}\left[c\,\left(d+e\,\sqrt{x}\,\right)^n\right]\right)^3\,\text{Log}\left[x\right]+\\ &3\,b\,n\,\left(a-b\,n\,\text{Log}\left[d+e\,\sqrt{x}\,\right]+b\,\text{Log}\left[c\,\left(d+e\,\sqrt{x}\,\right)^n\right]\right)^2\\ &\left(\left(\text{Log}\left[d+e\,\sqrt{x}\,\right]-\text{Log}\left[1+\frac{e\,\sqrt{x}}{d}\right]\right)\,\text{Log}\left[x\right]-2\,\text{PolyLog}\left[2,\,-\frac{e\,\sqrt{x}}{d}\right]\right)+\\ &6\,b^2\,n^2\,\left(a-b\,n\,\text{Log}\left[d+e\,\sqrt{x}\,\right]+b\,\text{Log}\left[c\,\left(d+e\,\sqrt{x}\,\right)^n\right]\right)\,\left(\text{Log}\left[d+e\,\sqrt{x}\,\right]^2\,\text{Log}\left[-\frac{e\,\sqrt{x}}{d}\right]+\\ &2\,\text{Log}\left[d+e\,\sqrt{x}\,\right]\,\text{PolyLog}\left[2,\,1+\frac{e\,\sqrt{x}}{d}\right]-2\,\text{PolyLog}\left[3,\,1+\frac{e\,\sqrt{x}}{d}\right]\right)+\\ &2\,b^3\,n^3\,\left(\text{Log}\left[d+e\,\sqrt{x}\,\right]^3\,\text{Log}\left[-\frac{e\,\sqrt{x}}{d}\right]+3\,\text{Log}\left[d+e\,\sqrt{x}\,\right]^2\,\text{PolyLog}\left[2,\,1+\frac{e\,\sqrt{x}}{d}\right]-\\ &6\,\text{Log}\left[d+e\,\sqrt{x}\,\right]\,\text{PolyLog}\left[3,\,1+\frac{e\,\sqrt{x}}{d}\right]+6\,\text{PolyLog}\left[4,\,1+\frac{e\,\sqrt{x}}{d}\right]\right) \end{split}$$

### Problem 419: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \log\left[c \left(d + e \sqrt{x}\right)^{n}\right]\right)^{3}}{x^{2}} dx$$

Optimal (type 4, 263 leaves, 10 steps):

$$\frac{3 \, b \, e \, n \, \left(d + e \, \sqrt{x} \,\right) \, \left(a + b \, Log \left[c \, \left(d + e \, \sqrt{x} \,\right)^n\right]\right)^2}{d^2 \, \sqrt{x}} - \\ \frac{3 \, b \, e^2 \, n \, Log \left[1 - \frac{d}{d + e \, \sqrt{x}}\right] \, \left(a + b \, Log \left[c \, \left(d + e \, \sqrt{x} \,\right)^n\right]\right)^2}{d^2} - \\ \frac{\left(a + b \, Log \left[c \, \left(d + e \, \sqrt{x} \,\right)^n\right]\right)^3}{x} + \frac{6 \, b^2 \, e^2 \, n^2 \, \left(a + b \, Log \left[c \, \left(d + e \, \sqrt{x} \,\right)^n\right]\right) \, Log \left[-\frac{e \, \sqrt{x}}{d}\right]}{d^2} + \\ \frac{6 \, b^2 \, e^2 \, n^2 \, \left(a + b \, Log \left[c \, \left(d + e \, \sqrt{x} \,\right)^n\right]\right) \, PolyLog \left[2, \, \frac{d}{d + e \, \sqrt{x}}\right]}{d^2} + \\ \frac{6 \, b^3 \, e^2 \, n^3 \, PolyLog \left[2, \, 1 + \frac{e \, \sqrt{x}}{d}\right]}{d^2} + \frac{6 \, b^3 \, e^2 \, n^3 \, PolyLog \left[3, \, \frac{d}{d + e \, \sqrt{x}}\right]}{d^2}$$

Result (type 4, 536 leaves):

$$\begin{split} &\frac{1}{d^2\,x} \left( -3\,b\,d\,e\,n\,\sqrt{x} \; \left( a - b\,n\,Log \left[ d + e\,\sqrt{x} \; \right] + b\,Log \left[ c\, \left( d + e\,\sqrt{x} \; \right)^n \right] \right)^2 - \\ &3\,b\,d^2\,n\,Log \left[ d + e\,\sqrt{x} \; \right] \; \left( a - b\,n\,Log \left[ d + e\,\sqrt{x} \; \right] + b\,Log \left[ c\, \left( d + e\,\sqrt{x} \; \right)^n \right] \right)^2 + \\ &3\,b\,e^2\,n\,x\,Log \left[ d + e\,\sqrt{x} \; \right] \; \left( a - b\,n\,Log \left[ d + e\,\sqrt{x} \; \right] + b\,Log \left[ c\, \left( d + e\,\sqrt{x} \; \right)^n \right] \right)^2 - \\ &d^2\, \left( a - b\,n\,Log \left[ d + e\,\sqrt{x} \; \right] + b\,Log \left[ c\, \left( d + e\,\sqrt{x} \; \right)^n \right] \right)^3 - \\ &\frac{3}{2}\,b\,e^2\,n\,x\, \left( a - b\,n\,Log \left[ d + e\,\sqrt{x} \; \right] + b\,Log \left[ c\, \left( d + e\,\sqrt{x} \; \right)^n \right] \right)^2\,Log \left[ x \right] + \\ &3\,b^2\,n^2\, \left( a - b\,n\,Log \left[ d + e\,\sqrt{x} \; \right] + b\,Log \left[ c\, \left( d + e\,\sqrt{x} \; \right)^n \right] \right) \\ &\left( \left( d + e\,\sqrt{x} \; \right)\,Log \left[ d + e\,\sqrt{x} \; \right] + b\,Log \left[ c\, \left( d + e\,\sqrt{x} \; \right)^n \right] \right) \\ &\left( \left( d + e\,\sqrt{x} \; \right)\,Log \left[ d + e\,\sqrt{x} \; \right] \left( -2\,e\,\sqrt{x} \, + \left( -d + e\,\sqrt{x} \; \right)\,Log \left[ d + e\,\sqrt{x} \; \right] \right) - \\ &2\,e^2\,x\, \left( -1 + Log \left[ d + e\,\sqrt{x} \; \right] \right)\,Log \left[ -\frac{e\,\sqrt{x}}{d} \right] - 2\,e^2\,x\,PolyLog \left[ 2,\,1 + \frac{e\,\sqrt{x}}{d} \right] \right) \\ &b^3\,n^3\, \left( \left( d + e\,\sqrt{x} \; \right)\,Log \left[ d + e\,\sqrt{x} \; \right] \right)\,Log \left[ d + e\,\sqrt{x} \; \right]\,Log \left[ -\frac{e\,\sqrt{x}}{d} \right] - \\ &3\,e^2\,x\, \left( -2 + Log \left[ d + e\,\sqrt{x} \; \right] \right)\,Log \left[ d + e\,\sqrt{x} \; \right]\,Log \left[ -\frac{e\,\sqrt{x}}{d} \right] - \\ &6\,e^2\,x\, \left( -1 + Log \left[ d + e\,\sqrt{x} \; \right] \right)\,PolyLog \left[ 2,\,1 + \frac{e\,\sqrt{x}}{d} \right] + 6\,e^2\,x\,PolyLog \left[ 3,\,1 + \frac{e\,\sqrt{x}}{d} \right] \right) \right) \end{split}$$

Problem 432: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \log\left[c \left(d + \frac{e}{\sqrt{x}}\right)^{n}\right]\right)^{2}}{x} dx$$

Optimal (type 4, 93 leaves, 5 steps):

$$-2\left(a+b\,\text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^n\right]\right)^2\,\text{Log}\left[-\frac{e}{d\,\sqrt{x}}\right] -\\ 4\,b\,n\left(a+b\,\text{Log}\left[c\left(d+\frac{e}{\sqrt{x}}\right)^n\right]\right)\,\text{PolyLog}\left[2\text{, 1}+\frac{e}{d\,\sqrt{x}}\right] +4\,b^2\,n^2\,\text{PolyLog}\left[3\text{, 1}+\frac{e}{d\,\sqrt{x}}\right]$$

Result (type 4, 386 leaves):

$$\begin{split} &\left(a - b \, n \, Log\left[d + \frac{e}{\sqrt{x}}\right] + b \, Log\left[c\,\left(d + \frac{e}{\sqrt{x}}\right)^n\right]\right)^2 \, Log\left[x\right] + \\ &2 \, b \, n \, \left(a - b \, n \, Log\left[d + \frac{e}{\sqrt{x}}\right] + b \, Log\left[c\,\left(d + \frac{e}{\sqrt{x}}\right)^n\right]\right) \\ &\left(\left(Log\left[d + \frac{e}{\sqrt{x}}\right] - Log\left[1 + \frac{e}{d\,\sqrt{x}}\right]\right) \, Log\left[x\right] + 2 \, PolyLog\left[2, \, -\frac{e}{d\,\sqrt{x}}\right]\right) + \\ &\frac{1}{12} \, b^2 \, n^2 \left(24 \, Log\left[\frac{e}{d} + \sqrt{x}\right]^2 \, Log\left[-\frac{d\,\sqrt{x}}{e}\right] + 12 \, Log\left[d + \frac{e}{\sqrt{x}}\right]^2 \, Log\left[x\right] - 12 \, Log\left[\frac{e}{d} + \sqrt{x}\right]^2 \, Log\left[x\right] - \\ &24 \, Log\left[d + \frac{e}{\sqrt{x}}\right] \, Log\left[1 + \frac{d\,\sqrt{x}}{e}\right] \, Log\left[x\right] + 24 \, Log\left[\frac{e}{d} + \sqrt{x}\right] \, Log\left[1 + \frac{d\,\sqrt{x}}{e}\right] \, Log\left[x\right] + \\ &6 \, Log\left[d + \frac{e}{\sqrt{x}}\right] \, Log\left[x\right]^2 - 6 \, Log\left[1 + \frac{d\,\sqrt{x}}{e}\right] \, Log\left[x\right]^2 + Log\left[x\right]^3 + \\ &48 \, Log\left[\frac{e}{d} + \sqrt{x}\right] \, PolyLog\left[2, \, 1 + \frac{d\,\sqrt{x}}{e}\right] - 48 \, \left(Log\left[d + \frac{e}{\sqrt{x}}\right] - Log\left[\frac{e}{d} + \sqrt{x}\right]\right) \\ &PolyLog\left[2, \, -\frac{d\,\sqrt{x}}{e}\right] - 48 \, PolyLog\left[3, \, 1 + \frac{d\,\sqrt{x}}{e}\right] - 48 \, PolyLog\left[3, \, -\frac{d\,\sqrt{x}}{e}\right] \end{split}$$

Problem 438: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \log\left[c \left(d + \frac{e}{\sqrt{x}}\right)^{n}\right]\right)^{3}}{x} dx$$

Optimal (type 4, 135 leaves, 6 steps):

Result (type 4, 532 leaves):

$$\left( a - b \, n \, Log \left[ d + \frac{e}{\sqrt{x}} \right] + b \, Log \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^n \right] \right)^3 \, Log \left[ x \right] + \\ 3 \, b \, n \, \left( a - b \, n \, Log \left[ d + \frac{e}{\sqrt{x}} \right] + b \, Log \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^n \right] \right)^2 \\ \left( \left( \left[ Log \left[ d + \frac{e}{\sqrt{x}} \right] - Log \left[ 1 + \frac{e}{d\sqrt{x}} \right] \right) \, Log \left[ x \right] + 2 \, PolyLog \left[ 2 \, , \, - \frac{e}{d\sqrt{x}} \right] \right) + \\ 6 \, b^2 \, n^2 \, \left( a - b \, n \, Log \left[ d + \frac{e}{\sqrt{x}} \right] + b \, Log \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^n \right] \right) \left( Log \left[ \frac{e}{d} + \sqrt{x} \right]^2 Log \left[ - \frac{d\sqrt{x}}{e} \right] + \\ \frac{1}{2} \, Log \left[ d + \frac{e}{\sqrt{x}} \right]^2 \, Log \left[ x \right] - \frac{1}{2} \, Log \left[ \frac{e}{d} + \sqrt{x} \right]^2 \, Log \left[ x \right] - Log \left[ d + \frac{e}{\sqrt{x}} \right] \, Log \left[ 1 + \frac{d\sqrt{x}}{e} \right] \, Log \left[ x \right] + \\ Log \left[ \frac{e}{d} + \sqrt{x} \right] \, Log \left[ 1 + \frac{d\sqrt{x}}{e} \right] \, Log \left[ x \right] + \frac{1}{4} \, Log \left[ d + \frac{e}{\sqrt{x}} \right] \, Log \left[ x \right]^2 - \frac{1}{4} \, Log \left[ 1 + \frac{d\sqrt{x}}{e} \right] \, Log \left[ x \right]^2 + \\ \frac{Log \left[ x \right]^3}{24} + 2 \, Log \left[ \frac{e}{d} + \sqrt{x} \right] \, PolyLog \left[ 2 \, , \, 1 + \frac{d\sqrt{x}}{e} \right] - 2 \, \left[ Log \left[ d + \frac{e}{\sqrt{x}} \right] - Log \left[ \frac{e}{d} + \sqrt{x} \right] \right) \right) \\ PolyLog \left[ 2 \, , \, - \frac{d\sqrt{x}}{e} \right] - 2 \, PolyLog \left[ 3 \, , \, 1 + \frac{d\sqrt{x}}{e} \right] - 2 \, PolyLog \left[ 3 \, , \, - \frac{d\sqrt{x}}{e} \right] - \\ 2 \, b^3 \, n^3 \, \left( Log \left[ d + \frac{e}{\sqrt{x}} \right]^3 \, Log \left[ - \frac{e}{d\sqrt{x}} \right] + 3 \, Log \left[ d + \frac{e}{\sqrt{x}} \right]^2 \, PolyLog \left[ 2 \, , \, 1 + \frac{e}{d\sqrt{x}} \right] - \\ 6 \, Log \left[ d + \frac{e}{\sqrt{x}} \right] \, PolyLog \left[ 3 \, , \, 1 + \frac{e}{d\sqrt{x}} \right] + 6 \, PolyLog \left[ 4 \, , \, 1 + \frac{e}{d\sqrt{x}} \right] \right)$$

## Problem 453: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a+b \, Log\left[\, c \, \left(d+e \, x^{1/3}\right)^{\, n}\,\right]\,\right)^{\, 2}}{x} \, \mathrm{d}x$$

Optimal (type 4, 93 leaves, 5 steps):

$$3 \left(a + b Log \left[c \left(d + e x^{1/3}\right)^n\right]\right)^2 Log \left[-\frac{e x^{1/3}}{d}\right] + \\ 6 b n \left(a + b Log \left[c \left(d + e x^{1/3}\right)^n\right]\right) PolyLog \left[2, 1 + \frac{e x^{1/3}}{d}\right] - 6 b^2 n^2 PolyLog \left[3, 1 + \frac{e x^{1/3}}{d}\right]$$

Result (type 4, 195 leaves):

$$\begin{split} &\left(\mathsf{a} - \mathsf{b} \, \mathsf{n} \, \mathsf{Log} \Big[ \, \mathsf{d} + \mathsf{e} \, \, \mathsf{x}^{1/3} \, \Big] \, + \mathsf{b} \, \mathsf{Log} \Big[ \, \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \, \mathsf{x}^{1/3} \right)^{\, \mathsf{n}} \, \Big] \, \right)^{\, \mathsf{2}} \, \mathsf{Log} \big[ \mathsf{x} \big] \, + \\ & 2 \, \mathsf{b} \, \mathsf{n} \, \left( \mathsf{a} - \mathsf{b} \, \mathsf{n} \, \mathsf{Log} \Big[ \, \mathsf{d} + \mathsf{e} \, \, \mathsf{x}^{1/3} \big] \, + \mathsf{b} \, \mathsf{Log} \Big[ \, \mathsf{c} \, \left( \mathsf{d} + \mathsf{e} \, \, \mathsf{x}^{1/3} \right)^{\, \mathsf{n}} \, \Big] \, \right) \\ & \left( \left( \mathsf{Log} \Big[ \, \mathsf{d} + \mathsf{e} \, \, \mathsf{x}^{1/3} \big] \, - \mathsf{Log} \Big[ \, \mathsf{1} + \frac{\mathsf{e} \, \, \mathsf{x}^{1/3}}{\mathsf{d}} \, \Big] \, \right) \, \mathsf{Log} \big[ \mathsf{x} \big] \, - \, \mathsf{3} \, \mathsf{PolyLog} \Big[ \, \mathsf{2} \, , \, \, - \frac{\mathsf{e} \, \, \mathsf{x}^{1/3}}{\mathsf{d}} \, \Big] \, + \, \mathsf{3} \, \, \mathsf{b}^{2} \, \, \mathsf{n}^{2} \\ & \left( \mathsf{Log} \Big[ \, \mathsf{d} + \mathsf{e} \, \, \mathsf{x}^{1/3} \big]^{\, 2} \, \mathsf{Log} \Big[ \, - \frac{\mathsf{e} \, \, \mathsf{x}^{1/3}}{\mathsf{d}} \, \Big] \, + \, \mathsf{2} \, \mathsf{Log} \Big[ \, \mathsf{d} + \mathsf{e} \, \, \mathsf{x}^{1/3} \, \Big] \, \, \mathsf{PolyLog} \Big[ \, \mathsf{2} \, , \, \, \, \mathsf{1} + \frac{\mathsf{e} \, \, \mathsf{x}^{1/3}}{\mathsf{d}} \, \Big] \, - \, \mathsf{2} \, \mathsf{PolyLog} \Big[ \, \mathsf{3} \, , \, \, \, \mathsf{1} + \frac{\mathsf{e} \, \, \mathsf{x}^{1/3}}{\mathsf{d}} \, \Big] \, \right) \end{split}$$

Problem 460: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a+b \, Log\left[c\, \left(d+e\, x^{1/3}\right)^n\right]\right)^3}{x} \, \mathrm{d}x$$

Optimal (type 4, 135 leaves, 6 steps):

$$3 \left( a + b \log \left[ c \left( d + e x^{1/3} \right)^n \right] \right)^3 \log \left[ -\frac{e x^{1/3}}{d} \right] + \\ 9 b n \left( a + b \log \left[ c \left( d + e x^{1/3} \right)^n \right] \right)^2 PolyLog \left[ 2, 1 + \frac{e x^{1/3}}{d} \right] - \\ 18 b^2 n^2 \left( a + b \log \left[ c \left( d + e x^{1/3} \right)^n \right] \right) PolyLog \left[ 3, 1 + \frac{e x^{1/3}}{d} \right] + 18 b^3 n^3 PolyLog \left[ 4, 1 + \frac{e x^{1/3}}{d} \right]$$

Result (type 4, 333 leaves):

Problem 473: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a+b \, Log\left[\, c \, \left(d+e \, x^{2/3}\right)^{\, n}\,\right]\,\right)^{\, 2}}{x} \, \mathrm{d}x$$

Optimal (type 4, 95 leaves, 5 steps):

$$\begin{split} &\frac{3}{2} \, \left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{2/3} \right)^n \right] \right)^2 \, \text{Log} \left[ -\frac{e \, x^{2/3}}{d} \right] \, + \\ &- 3 \, b \, n \, \left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{2/3} \right)^n \right] \right) \, \text{PolyLog} \left[ 2 \, , \, 1 + \frac{e \, x^{2/3}}{d} \right] - 3 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e \, x^{2/3}}{d} \right] \end{split}$$

Result (type 4, 199 leaves):

$$\begin{split} &\left(a-b\,n\,\text{Log}\left[d+e\,x^{2/3}\right]+b\,\text{Log}\left[c\,\left(d+e\,x^{2/3}\right)^{n}\right]\right)^{2}\,\text{Log}\left[x\right]\,+\\ &2\,b\,n\,\left(a-b\,n\,\text{Log}\left[d+e\,x^{2/3}\right]+b\,\text{Log}\left[c\,\left(d+e\,x^{2/3}\right)^{n}\right]\right)\\ &\left(\left[\text{Log}\left[d+e\,x^{2/3}\right]-\text{Log}\left[1+\frac{e\,x^{2/3}}{d}\right]\right)\,\text{Log}\left[x\right]-\frac{3}{2}\,\text{PolyLog}\!\left[2,\,-\frac{e\,x^{2/3}}{d}\right]\right)+\frac{3}{2}\,b^{2}\,n^{2}\\ &\left(\text{Log}\left[d+e\,x^{2/3}\right]^{2}\,\text{Log}\left[-\frac{e\,x^{2/3}}{d}\right]+2\,\text{Log}\!\left[d+e\,x^{2/3}\right]\,\text{PolyLog}\!\left[2,\,1+\frac{e\,x^{2/3}}{d}\right]-2\,\text{PolyLog}\!\left[3,\,1+\frac{e\,x^{2/3}}{d}\right]\right) \end{split}$$

### Problem 483: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a+b \; Log\left[\, c \; \left(d+e \; x^{2/3}\right)^{\, n}\,\right]\,\right)^{\, 3}}{x} \; \mathrm{d}x$$

Optimal (type 4, 139 leaves, 6 steps):

$$\begin{split} &\frac{3}{2} \left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{2/3} \right)^n \right] \right)^3 \, \text{Log} \left[ - \frac{e \, x^{2/3}}{d} \right] \, + \\ &\frac{9}{2} \, b \, n \, \left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{2/3} \right)^n \right] \right)^2 \, \text{PolyLog} \left[ 2 \, , \, 1 + \frac{e \, x^{2/3}}{d} \right] \, - \\ &9 \, b^2 \, n^2 \, \left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{2/3} \right)^n \right] \right) \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e \, x^{2/3}}{d} \right] \, + 9 \, b^3 \, n^3 \, \text{PolyLog} \left[ 4 \, , \, 1 + \frac{e \, x^{2/3}}{d} \right] \end{split}$$

#### Result (type 4, 339 leaves):

## Problem 500: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a+b\, \text{Log}\left[\,c\, \left(d+\frac{e}{x^{1/3}}\,\right)^{\,n}\,\right]\,\right)^{\,2}}{x}\, \text{d}\, x$$

Optimal (type 4, 93 leaves, 5 steps):

$$-3 \left( a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{x^{1/3}} \right)^n \right] \right)^2 \, \text{Log} \left[ -\frac{e}{d \, x^{1/3}} \right] - \\ 6 \, b \, n \, \left( a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{x^{1/3}} \right)^n \right] \right) \, \text{PolyLog} \left[ 2 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, n^2 \, \text{PolyLog} \left[ 3 \, , \, 1 + \frac{e}{d \, x^{1/3}} \right] + 6 \, b^2 \, n^2 \, n^$$

Result (type 4, 389 leaves):

$$\begin{split} \left(a - b \, n \, \text{Log} \Big[d + \frac{e}{x^{1/3}}\Big] + b \, \text{Log} \Big[c \, \left(d + \frac{e}{x^{1/3}}\right)^n\Big] \right)^2 \, \text{Log} \big[x\big] + \\ 2 \, b \, n \, \left(a - b \, n \, \text{Log} \Big[d + \frac{e}{x^{1/3}}\Big] + b \, \text{Log} \Big[c \, \left(d + \frac{e}{x^{1/3}}\right)^n\Big] \right) \\ \left(\left(\text{Log} \Big[d + \frac{e}{x^{1/3}}\Big] - \text{Log} \Big[1 + \frac{e}{d \, x^{1/3}}\Big] \right) \, \text{Log} \big[x\big] + 3 \, \text{PolyLog} \Big[2 \, , \, -\frac{e}{d \, x^{1/3}}\Big] \right) + 3 \, b^2 \, n^2 \\ \left(2 \, \text{Log} \Big[\frac{e}{d} + x^{1/3}\Big] \, \text{PolyLog} \Big[2 \, , \, 1 + \frac{d \, x^{1/3}}{e}\Big] - 2 \, \left(\text{Log} \Big[d + \frac{e}{x^{1/3}}\Big] - \text{Log} \Big[\frac{e}{d} + x^{1/3}\Big] \right) \, \text{PolyLog} \Big[2 \, , \, -\frac{d \, x^{1/3}}{e}\Big] + \\ \frac{1}{81} \, \left(81 \, \text{Log} \Big[\frac{e}{d} + x^{1/3}\Big]^2 \, \text{Log} \Big[-\frac{d \, x^{1/3}}{e}\Big] + 27 \, \text{Log} \Big[d + \frac{e}{x^{1/3}}\Big]^2 \, \text{Log} \big[x\big] - \\ 27 \, \text{Log} \Big[\frac{e}{d} + x^{1/3}\Big]^2 \, \text{Log} \big[x\big] - 54 \, \text{Log} \Big[d + \frac{e}{x^{1/3}}\Big] \, \text{Log} \big[1 + \frac{d \, x^{1/3}}{e}\Big] \, \text{Log} \big[x\big] + \\ 54 \, \text{Log} \Big[\frac{e}{d} + x^{1/3}\Big] \, \text{Log} \big[1 + \frac{d \, x^{1/3}}{e}\Big] \, \text{Log} \big[x\big] + 9 \, \text{Log} \big[d + \frac{e}{x^{1/3}}\Big] \, \text{Log} \big[x\big]^2 - \\ 9 \, \text{Log} \Big[1 + \frac{d \, x^{1/3}}{e}\Big] \, \text{Log} \big[x\big]^2 + \text{Log} \big[x\big]^3 - 162 \, \text{PolyLog} \big[3 \, , \, 1 + \frac{d \, x^{1/3}}{e}\Big] - 162 \, \text{PolyLog} \big[3 \, , \, -\frac{d \, x^{1/3}}{e}\Big] \Big) \bigg) \bigg) \end{split}$$

Problem 505: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \, Log \left[c \, \left(d + \frac{e}{x^{1/3}}\right)^n\right]\right)^3}{x} \, dx$$

Optimal (type 4, 135 leaves, 6 steps):

$$\begin{split} &-3\left(a+b\,\text{Log}\Big[\,c\,\left(d+\frac{e}{x^{1/3}}\right)^n\,\Big]\,\right)^3\,\text{Log}\Big[\,-\frac{e}{d\,x^{1/3}}\,\Big]\,\,-\\ &9\,b\,n\,\left(a+b\,\text{Log}\Big[\,c\,\left(d+\frac{e}{x^{1/3}}\right)^n\,\Big]\,\right)^2\,\text{PolyLog}\Big[\,2\,,\,\,1+\frac{e}{d\,x^{1/3}}\,\Big]\,\,+\\ &18\,b^2\,n^2\,\left(a+b\,\text{Log}\Big[\,c\,\left(d+\frac{e}{x^{1/3}}\right)^n\,\Big]\,\right)\,\text{PolyLog}\Big[\,3\,,\,\,1+\frac{e}{d\,x^{1/3}}\,\Big]\,-\,18\,b^3\,n^3\,\text{PolyLog}\Big[\,4\,,\,\,1+\frac{e}{d\,x^{1/3}}\,\Big] \end{split}$$

Result (type 4, 527 leaves):

$$\begin{split} &\left(a-b\,n\,\text{Log}\left[d+\frac{e}{x^{1/3}}\right]+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^n\right]\right)^3\,\text{Log}\left[x\right] +\\ &3\,b\,n\,\left(a-b\,n\,\text{Log}\left[d+\frac{e}{x^{1/3}}\right]+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^n\right]\right)^2\\ &\left(\left(\text{Log}\left[d+\frac{e}{x^{1/3}}\right]-\text{Log}\left[1+\frac{e}{d\,x^{1/3}}\right]\right)\,\text{Log}\left[x\right]+3\,\text{PolyLog}\left[2,-\frac{e}{d\,x^{1/3}}\right]\right)+\\ &9\,b^2\,n^2\,\left(a-b\,n\,\text{Log}\left[d+\frac{e}{x^{1/3}}\right]+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^n\right]\right)\\ &\left(2\,\text{Log}\left[\frac{e}{d}+x^{1/3}\right]\,\text{PolyLog}\left[2,\,1+\frac{d\,x^{1/3}}{e}\right]-2\,\left(\text{Log}\left[d+\frac{e}{x^{1/3}}\right]-\text{Log}\left[\frac{e}{d}+x^{1/3}\right]\right)\,\text{PolyLog}\left[2,\,-\frac{d\,x^{1/3}}{e}\right]+\\ &\frac{1}{81}\left(81\,\text{Log}\left[\frac{e}{d}+x^{1/3}\right]^2\,\text{Log}\left[-\frac{d\,x^{1/3}}{e}\right]+27\,\text{Log}\left[d+\frac{e}{x^{1/3}}\right]^2\,\text{Log}\left[x\right]-27\,\text{Log}\left[\frac{e}{d}+x^{1/3}\right]^2\,\text{Log}\left[x\right]-\\ &54\,\text{Log}\left[d+\frac{e}{x^{1/3}}\right]\,\text{Log}\left[1+\frac{d\,x^{1/3}}{e}\right]\,\text{Log}\left[x\right]+54\,\text{Log}\left[\frac{e}{d}+x^{1/3}\right]\,\text{Log}\left[1+\frac{d\,x^{1/3}}{e}\right]\,\text{Log}\left[x\right]+\\ &9\,\text{Log}\left[d+\frac{e}{x^{1/3}}\right]\,\text{Log}\left[x\right]^2-9\,\text{Log}\left[1+\frac{d\,x^{1/3}}{e}\right]\,\text{Log}\left[x\right]^2+\text{Log}\left[x\right]^3-\\ &162\,\text{PolyLog}\left[3,\,1+\frac{d\,x^{1/3}}{e}\right]-162\,\text{PolyLog}\left[3,\,-\frac{d\,x^{1/3}}{e}\right]\right)\right)-\\ &3\,b^3\,n^3\left(\text{Log}\left[d+\frac{e}{x^{1/3}}\right]^3\,\text{Log}\left[-\frac{e}{d\,x^{1/3}}\right]+3\,\text{Log}\left[d+\frac{e}{x^{1/3}}\right]^2\,\text{PolyLog}\left[2,\,1+\frac{e}{d\,x^{1/3}}\right]-\\ &6\,\text{Log}\left[d+\frac{e}{x^{1/3}}\right]\,\text{PolyLog}\left[3,\,1+\frac{e}{d\,x^{1/3}}\right]+6\,\text{PolyLog}\left[4,\,1+\frac{e}{d\,x^{1/3}}\right]\right) \end{split}$$

Problem 518: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \operatorname{Log}\left[c \left(d + \frac{e}{x^{2/3}}\right)^{n}\right]\right)^{2}}{x} dx$$

Optimal (type 4, 95 leaves, 5 steps):

$$-\frac{3}{2} \left( a + b \log \left[ c \left( d + \frac{e}{x^{2/3}} \right)^n \right] \right)^2 \log \left[ -\frac{e}{d x^{2/3}} \right] - \\ 3 b n \left( a + b \log \left[ c \left( d + \frac{e}{x^{2/3}} \right)^n \right] \right) \text{PolyLog} \left[ 2, 1 + \frac{e}{d x^{2/3}} \right] + 3 b^2 n^2 \text{PolyLog} \left[ 3, 1 + \frac{e}{d x^{2/3}} \right]$$

Result (type 4, 1701 leaves):

$$\begin{split} &\left(a - b \, n \, Log \Big[d + \frac{e}{x^{2/3}}\Big] + b \, Log \Big[c \, \left(d + \frac{e}{x^{2/3}}\right)^n\Big]\right)^2 \, Log [x] \, + \\ &2 \, b \, n \, \left(a - b \, n \, Log \Big[d + \frac{e}{x^{2/3}}\Big] + b \, Log \Big[c \, \left(d + \frac{e}{x^{2/3}}\right)^n\Big]\right) \\ & \left(\left(Log \Big[d + \frac{e}{x^{2/3}}\Big] - Log \Big[1 + \frac{e}{d \, x^{2/3}}\Big]\right) \, Log [x] + \frac{3}{2} \, PolyLog \Big[2, -\frac{e}{d \, x^{2/3}}\Big]\right) + \\ & 3 \, b^2 \, n^2 \, \left(Log \Big[-\frac{\dot{\mathbb{1}} \, \sqrt{e}}{\sqrt{d}} + x^{1/3}\Big]^2 \, Log \Big[-\frac{\dot{\mathbb{1}} \, \sqrt{d} \, x^{1/3}}{\sqrt{e}}\Big] + 2 \, Log \Big[-\frac{\dot{\mathbb{1}} \, \sqrt{e}}{\sqrt{d}} + x^{1/3}\Big] \, Log \Big[\frac{\dot{\mathbb{1}} \, \sqrt{e}}{\sqrt{d}} + x^{1/3}\Big] \end{split}$$

$$\begin{split} & \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{3/3}}{\sqrt{e}} \Big] + \text{Log} \Big[ 1 - \frac{i \sqrt{d} \ x^{3/3}}{\sqrt{e}} \Big] \left( 2 \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{3/3} \Big] + \text{Log} \Big[ 1 - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] \right) \\ & \left( \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] - \text{Log} \Big[ \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] \right) + \text{Log} \Big[ \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] \text{Log} \Big[ \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] + \\ & 2 \text{Log} \Big[ \frac{\sqrt{e} - i \sqrt{d} \ x^{1/3}}{\sqrt{e} + i \sqrt{d} \ x^{1/3}} \Big] \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] \left( - \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] + \text{Log} \Big[ \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] \right) + \\ & \text{Log} \Big[ \frac{\sqrt{e} - i \sqrt{d} \ x^{1/3}}{\sqrt{e} + i \sqrt{d} \ x^{1/3}} \Big]^2 \left( \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] + \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] - \text{Log} \Big[ - \frac{2x^{1/3}}{\sqrt{d}} + x^{1/3} \Big] \right) + \\ & \frac{1}{3} \left( - \text{Log} \Big[ d + \frac{e}{x^{2/3}} \Big] + \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{e}} + x^{1/3} \Big] + \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] + \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] - 2 \text{Log} \Big[ x \Big] + \frac{4 \text{Log} \Big[ x \Big]^3}{\sqrt{e}} + x^{1/3} \Big] + \\ & 2 \text{Log} \Big[ \frac{i \sqrt{e} - i \sqrt{d} \ x^{1/3}}{\sqrt{e} + i \sqrt{d} \ x^{1/3}} \Big] + \text{PolyLog} \Big[ 2, \frac{i \sqrt{e} + i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] + \\ & 2 \text{Log} \Big[ \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] \text{PolyLog} \Big[ 2, 1 - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] + \\ & 2 \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] \text{PolyLog} \Big[ 2, 1 + \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] + \\ & 2 \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] - \text{Log} \Big[ \frac{\sqrt{e} - i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] + \\ & 2 \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] - \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{e}} + i \sqrt{d} \ x^{1/3} \Big] - \\ & 2 \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] + \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{e}} + i \sqrt{d} \ x^{1/3} \Big] - \\ & 2 \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] + 2 \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] - \\ & 2 \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] + 2 \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] - \\ & 2 \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] + 2 \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] - \\ & 2 \text{Log} \Big[ - \frac{i \sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] + 2 \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/3}}{\sqrt{e}} \Big] - 2 \text{Log} \Big[ - \frac{i \sqrt{d} \ x^{1/$$

$$6 \, \text{Log} \, [\text{x}] \, \text{PolyLog} \, \Big[ \, 2 \, , \, - \, \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \, \Big] \, - \, 6 \, \text{Log} \, [\text{x}] \, \, \text{PolyLog} \, \Big[ \, 2 \, , \, \, \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \, \Big] \, + \, \\ 18 \, \text{PolyLog} \, \Big[ \, 3 \, , \, - \, \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \, \Big] \, + \, 18 \, \text{PolyLog} \, \Big[ \, 3 \, , \, \, \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \, \Big] \, \Bigg)$$

#### Problem 523: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b Log\left[c \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^2}{x^2} dx$$

Optimal (type 4, 361 leaves, 19 steps):

$$-\frac{8 \ b^{2} \ n^{2}}{9 \ x} + \frac{32 \ b^{2} \ d \ n^{2}}{3 \ e \ x^{1/3}} + \frac{32 \ b^{2} \ d^{3/2} \ n^{2} \ ArcTan \Big[\frac{\sqrt{d} \ x^{1/3}}{\sqrt{e}}\Big]}{3 \ e^{3/2}} + \frac{4 \ \dot{\mathbb{1}} \ b^{2} \ d^{3/2} \ n^{2} \ ArcTan \Big[\frac{\sqrt{d} \ x^{1/3}}{\sqrt{e}}\Big]^{2}}{e^{3/2}} - \frac{8 \ b^{2} \ d^{3/2} \ n^{2} \ ArcTan \Big[\frac{\sqrt{d} \ x^{1/3}}{\sqrt{e}}\Big] \ Log \Big[2 - \frac{2 \sqrt{e}}{\sqrt{e} - \dot{\mathbb{1}} \sqrt{d} \ x^{1/3}}\Big]}{\sqrt{e} - \dot{\mathbb{1}} \sqrt{d} \ x^{1/3}} + \frac{4 \ b \ n \ \Big(a + b \ Log \Big[c \ \Big(d + \frac{e}{x^{2/3}}\Big)^{n}\Big]\Big)}{3 \ x} - \frac{4 \ b \ d^{3/2} \ n \ ArcTan \Big[\frac{\sqrt{d} \ x^{1/3}}{\sqrt{e}}\Big] \ \Big(a + b \ Log \Big[c \ \Big(d + \frac{e}{x^{2/3}}\Big)^{n}\Big]\Big)}{e^{3/2}} - \frac{4 \ b \ d^{3/2} \ n \ ArcTan \Big[\frac{\sqrt{d} \ x^{1/3}}{\sqrt{e}}\Big] \ \Big(a + b \ Log \Big[c \ \Big(d + \frac{e}{x^{2/3}}\Big)^{n}\Big]\Big)}{e^{3/2}} - \frac{4 \ \dot{\mathbb{1}} \ b^{2} \ d^{3/2} \ n^{2} \ PolyLog \Big[2, -1 + \frac{2 \sqrt{e}}{\sqrt{e} - \dot{\mathbb{1}} \sqrt{d} \ x^{1/3}}\Big]}{e^{3/2}}$$

Result (type 4, 797 leaves):

$$\begin{split} \frac{1}{9\,e^{3/2}\,x} \left[ 6\,b\,n \left[ -6\,d^{3/2}\,x\,\mathsf{ArcTan} \Big[ \frac{\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] + \sqrt{e}\,\, \left( 2\,e - 6\,d\,x^{2/3} - 3\,e\,\mathsf{Log} \Big[ d + \frac{e}{x^{2/3}} \Big] \right) \right) \right] \\ & \left( a - b\,n\,\mathsf{Log} \Big[ d + \frac{e}{x^{2/3}} \Big] + b\,\mathsf{Log} \Big[ c\,\, \left( d + \frac{e}{x^{2/3}} \right)^n \Big] \right) - \\ & 9\,e^{3/2}\,\, \left( a - b\,n\,\mathsf{Log} \Big[ d + \frac{e}{x^{2/3}} \Big] + b\,\mathsf{Log} \Big[ c\,\, \left( d + \frac{e}{x^{2/3}} \right)^n \Big] \right)^2 + \\ & b^2\,n^2 \left( - 8\,e^{3/2} + 96\,d\,\sqrt{e}\,\,x^{2/3} + 96\,d^{3/2}\,x\,\mathsf{ArcTan} \Big[ \frac{\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] + 12\,e^{3/2}\,\mathsf{Log} \Big[ d + \frac{e}{x^{2/3}} \Big] - \\ & 36\,d\,\sqrt{e}\,\,x^{2/3}\,\mathsf{Log} \Big[ d + \frac{e}{x^{2/3}} \Big] - 36\,d^{3/2}\,x\,\mathsf{ArcTan} \Big[ \frac{\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] \,\mathsf{Log} \Big[ d + \frac{e}{x^{2/3}} \Big] - \\ & 9\,e^{3/2}\,\mathsf{Log} \Big[ d + \frac{e}{x^{2/3}} \Big]^2 + 36\,d^{3/2}\,x\,\mathsf{ArcTan} \Big[ \frac{\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] \,\mathsf{Log} \Big[ -\frac{i\,\sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] + \\ & 9\,i\,d^{3/2}\,x\,\mathsf{Log} \Big[ -\frac{i\,\sqrt{e}}{\sqrt{d}} + x^{1/3} \Big]^2 + 36\,d^{3/2}\,x\,\mathsf{ArcTan} \Big[ \frac{\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] \,\mathsf{Log} \Big[ \frac{i\,\sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] - \\ & 9\,i\,d^{3/2}\,x\,\mathsf{Log} \Big[ \frac{i\,\sqrt{e}}{\sqrt{d}} + x^{1/3} \Big]^2 - 18\,i\,d^{3/2}\,x\,\mathsf{Log} \Big[ -\frac{i\,\sqrt{e}}{\sqrt{d}} + x^{1/3} \Big] \,\mathsf{Log} \Big[ \frac{1}{2} - \frac{i\,\sqrt{d}\,\,x^{1/3}}{2\,\sqrt{e}} \Big] + \\ & 18\,i\,d^{3/2}\,x\,\mathsf{Log} \Big[ 1 - \frac{i\,\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] \,\mathsf{Log} \Big[ 1 - \frac{i\,\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] + \\ & 18\,i\,d^{3/2}\,x\,\mathsf{Log} \Big[ 1 - \frac{i\,\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] \,\mathsf{Log} \Big[ 1 - \frac{i\,\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] - 18\,i\,d^{3/2}\,x\,\mathsf{PolyLog} \Big[ 2 - \frac{i\,\sqrt{d}\,\,x^{1/3}}{2\,\sqrt{e}} \Big] - \\ & 36\,i\,d^{3/2}\,x\,\mathsf{PolyLog} \Big[ 2 - \frac{i\,\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] + 36\,i\,d^{3/2}\,x\,\mathsf{PolyLog} \Big[ 2 - \frac{i\,\sqrt{d}\,\,x^{1/3}}{\sqrt{e}} \Big] \Big] \Big) \Big) \Big) \Big) \\ \end{aligned}$$

Problem 526: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\left(a + b \, \text{Log}\left[c \, \left(d + \frac{e}{x^{2/3}}\right)^n\right]\right)^3}{x} \, dx$$

Optimal (type 4, 139 leaves, 6 steps):

$$\begin{split} &-\frac{3}{2}\left(a+b\,\text{Log}\!\left[c\,\left(d+\frac{e}{x^{2/3}}\right)^n\right]\right)^3\,\text{Log}\!\left[-\frac{e}{d\,x^{2/3}}\right] - \\ &-\frac{9}{2}\,b\,n\,\left(a+b\,\text{Log}\!\left[c\,\left(d+\frac{e}{x^{2/3}}\right)^n\right]\right)^2\,\text{PolyLog}\!\left[2\,,\,1+\frac{e}{d\,x^{2/3}}\right] + \\ &-9\,b^2\,n^2\,\left(a+b\,\text{Log}\!\left[c\,\left(d+\frac{e}{x^{2/3}}\right)^n\right]\right)\,\text{PolyLog}\!\left[3\,,\,1+\frac{e}{d\,x^{2/3}}\right] - 9\,b^3\,n^3\,\text{PolyLog}\!\left[4\,,\,1+\frac{e}{d\,x^{2/3}}\right] \end{split}$$

Result (type 4, 1841 leaves):

$$\left( a - b \, n \, \log \left[ d + \frac{e}{x^{2/3}} \right] + b \, \log \left[ c \, \left( d + \frac{e}{x^{2/3}} \right)^n \right] \right)^3 \, \log \left[ x \right] + \\ 3 \, b \, n \, \left[ a - b \, n \, \log \left[ d + \frac{e}{x^{2/3}} \right] + b \, \log \left[ c \, \left( d + \frac{e}{x^{2/3}} \right)^n \right] \right]^2 \\ = \left( \left( \log \left[ d + \frac{e}{x^{2/3}} \right] - \log \left[ 1 + \frac{e}{d \, x^{2/3}} \right] \right) \, \log \left[ x \right] + \frac{3}{2} \, Polytog \left[ 2, -\frac{e}{d \, x^{2/3}} \right] \right) + \\ 9 \, b^2 \, n^2 \, \left[ a - b \, n \, \log \left[ d + \frac{e}{x^{2/3}} \right] + b \, \log \left[ c \, \left( d + \frac{e}{x^{2/3}} \right)^n \right] \right) \\ = \left( \log \left[ -\frac{i \, \sqrt{e}}{\sqrt{d}} + x^{1/3} \right]^2 \, \log \left[ -\frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] + 2 \, \log \left[ -\frac{i \, \sqrt{e}}{\sqrt{d}} + x^{1/3} \right] \, \log \left[ \frac{i \, \sqrt{e}}{\sqrt{d}} + x^{1/3} \right] \right) \\ = \left( \log \left[ -\frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] + \log \left[ 1 \, \frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] + \log \left[ \frac{i \, \sqrt{e}}{\sqrt{d}} + x^{1/3} \right] + \log \left[ 1 \, \frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] \right) + \log \left[ \frac{i \, \sqrt{d}}{\sqrt{e}} + x^{1/3} \right] + \log \left[ 1 \, \frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] \right) \\ = \left( \log \left[ -\frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] + \log \left[ \frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] + \log \left[ \frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] \right) + \log \left[ \frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] + \log \left[ \frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] \right) \\ = \left( \log \left[ \frac{\sqrt{e} - i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] \right) \left[ \log \left[ -\frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] + \log \left[ -\frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] \right] + \log \left[ \frac{2 \, x^{1/3}}{\sqrt{e}} \right] \right) + \log \left[ \frac{2 \, x^{1/3}}{\sqrt{e}} \right] \right] \\ = \left( \log \left[ i \, \frac{e}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \right] \right) \left[ -polytog \left[ 2, \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \right] \right] + \log \left[ \frac{2 \, x^{1/3}}{\sqrt{e}} \right] + \log \left[ \frac{i \, \sqrt{d}}{\sqrt{e}} \, x^{1/3} \right] \right] \right] \\ = \left( \log \left[ i \, \frac{e}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \right] \right) \left[ -polytog \left[ 2, \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \right] \right] + \log \left[ \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \right] \right) + \log \left[ \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \right] \right) \left[ \log \left[ \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \right] \right] + \log \left[ \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \right] \right] + \log \left[ \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \, x^{1/3} \right] \right] + \log \left[ \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \, x^{1/3} \, x^{1/3} \right] + \log \left[ \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \, x^{1/3} \, x^{1/3} \right] \right] + \log \left[ \frac{i \, \sqrt{e}}{\sqrt{e}} \, x^{1/3} \, x^{1/3} \, x^{1/3} \, x^{1/3} \, x^{1/3} \,$$

$$\begin{split} & 2 \, \text{PolyLog} \Big[ 3 , \, \frac{\text{i} \, \sqrt{e} \, + \sqrt{d} \, \, x^{1/3}}{\text{i} \, \sqrt{e} \, - \sqrt{d} \, \, x^{1/3}} \Big] \, - 2 \, \text{PolyLog} \Big[ 3 , \, \frac{\text{i} \, \sqrt{e} \, + \sqrt{d} \, \, x^{1/3}}{-\text{i} \, \sqrt{e} \, + \sqrt{d} \, \, x^{1/3}} \Big] \, - \\ & 4 \, \text{PolyLog} \Big[ 3 , \, 1 - \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \Big] \, - 4 \, \text{PolyLog} \Big[ 3 , \, 1 + \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \Big] \, - \\ & \frac{2}{9} \left( \left| \text{Log} \left[ \frac{\text{i} \, \sqrt{e}}{\sqrt{d}} + x^{1/3} \right] - \text{Log} \left[ 1 - \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \right] \right) \, \text{Log} [x]^2 \, + \\ & \left( \text{Log} \left[ - \frac{\text{i} \, \sqrt{e}}{\sqrt{d}} + x^{1/3} \right] - \text{Log} \left[ 1 + \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \right] \right) \, \text{Log} [x]^2 \, - \\ & 6 \, \text{Log} [x] \, \text{PolyLog} \Big[ 2 , \, - \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \Big] \, - 6 \, \text{Log} [x] \, \text{PolyLog} \Big[ 2 , \, \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \Big] \, + \\ & 18 \, \text{PolyLog} \Big[ 3 , \, - \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \Big] \, + 18 \, \text{PolyLog} \Big[ 3 , \, \frac{\text{i} \, \sqrt{d} \, \, x^{1/3}}{\sqrt{e}} \Big] \Big) \bigg) \bigg] \, - \\ & \frac{3}{2} \, \text{b}^3 \, \text{n}^3 \, \left( \text{Log} \Big[ \text{d} + \frac{e}{x^{2/3}} \Big]^3 \, \text{Log} \Big[ - \frac{e}{d \, x^{2/3}} \Big] \, + 3 \, \text{Log} \Big[ \text{d} + \frac{e}{x^{2/3}} \Big]^2 \, \text{PolyLog} \Big[ 2 , \, 1 + \frac{e}{d \, x^{2/3}} \Big] \, - \\ & 6 \, \text{Log} \Big[ \text{d} + \frac{e}{x^{2/3}} \Big] \, \text{PolyLog} \Big[ 3 , \, 1 + \frac{e}{d \, x^{2/3}} \Big] \, + 6 \, \text{PolyLog} \Big[ 4 , \, 1 + \frac{e}{d \, x^{2/3}} \Big] \bigg) \end{split}$$

### Problem 538: Unable to integrate problem.

$$\int x^3 \left( a + b \operatorname{Log} \left[ c \left( d + e \sqrt{x} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 907 leaves, 27 steps):

$$\begin{split} &\frac{1}{c^4\,e^8} 2^{-2\,\,(1+p)}\,\,e^{-\frac{4\,a}{b}}\,\text{Gamma} \left[1+p\,\text{,}\, -\frac{4\,\left(a+b\,\text{Log} \left[c\,\left(d+e\,\sqrt{x}\,\right)^2\right]\right)}{b}\right] \\ &\left(a+b\,\text{Log} \left[c\,\left(d+e\,\sqrt{x}\,\right)^2\right]\right)^p \left(-\frac{a+b\,\text{Log} \left[c\,\left(d+e\,\sqrt{x}\,\right)^2\right]}{b}\right)^{-p} - \\ &\left(2^{1+p}\times7^{-p}\,d\,e^{-\frac{7\,a}{2\,b}}\left(d+e\,\sqrt{x}\,\right)^7\,\text{Gamma} \left[1+p\,\text{,}\, -\frac{7\,\left(a+b\,\text{Log} \left[c\,\left(d+e\,\sqrt{x}\,\right)^2\right]\right)}{2\,b}\right] \\ &\left(a+b\,\text{Log} \left[c\,\left(d+e\,\sqrt{x}\,\right)^2\right]\right)^p \left(-\frac{a+b\,\text{Log} \left[c\,\left(d+e\,\sqrt{x}\,\right)^2\right]}{b}\right)^{-p}\right) \middle/ \left(e^8\,\left(c\,\left(d+e\,\sqrt{x}\,\right)^2\right)^{7/2}\right) + \\ &\frac{1}{c^3\,e^8} 7\times 3^{-p}\,d^2\,e^{-\frac{3\,a}{b}}\,\text{Gamma} \left[1+p\,\text{,}\, -\frac{3\,\left(a+b\,\text{Log} \left[c\,\left(d+e\,\sqrt{x}\,\right)^2\right]\right)}{b}\right] \\ &\left(a+b\,\text{Log} \left[c\,\left(d+e\,\sqrt{x}\,\right)^2\right]\right)^p \left(-\frac{a+b\,\text{Log} \left[c\,\left(d+e\,\sqrt{x}\,\right)^2\right]\right)^{-p}}{b}\right) - \end{split}$$

$$\left[ 7 \times 2^{1+p} \times 5^{-p} \, d^3 \, e^{-\frac{5\pi}{2b}} \left( d + e \, \sqrt{x} \, \right)^5 \, \mathsf{Gamma} \left[ 1 + \mathsf{p}, \, -\frac{5 \, \left( a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)}{2 \, b} \right] \right]$$
 
$$\left( a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)^p \left( -\frac{a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right]}{b} \right)^{-p} \right) / \left( e^8 \, \left( c \, \left( d + e \, \sqrt{x} \, \right)^2 \right)^{5/2} \right) + \frac{1}{c^2 \, e^8} \, \mathsf{35} \cdot 2^{-1-p} \, d^4 \, e^{-\frac{2\pi}{b}} \, \mathsf{Gamma} \left[ 1 + \mathsf{p}, \, -\frac{2 \, \left( a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)}{b} \right] \right)$$
 
$$\left( a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)^p \left( -\frac{a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)^{-p} - \frac{3 \, \left( a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)}{2 \, b} \right)$$
 
$$\left( a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)^p \left( -\frac{a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)^{-p} \right) / \left( e^8 \, \left( c \, \left( d + e \, \sqrt{x} \, \right)^2 \right)^{3/2} \right) + \frac{1}{c \, e^8} \, \mathsf{7} \, d^6 \, e^{-\frac{\pi}{b}} \, \mathsf{Gamma} \left[ 1 + \mathsf{p}, \, -\frac{a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right) \right)^p \left( -\frac{a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right]}{b} \right) \left( a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)^p \right)$$
 
$$\left( a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)^{-p} - \left( 2^{1+p} \, d^7 \, e^{-\frac{\pi}{2b}} \left( d + e \, \sqrt{x} \, \right) \, \mathsf{Gamma} \left[ 1 + \mathsf{p}, \, -\frac{a + b \, \mathsf{Log} \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right]}{2 \, b} \right) \right)$$

Result (type 8, 26 leaves):

$$\int x^3 \left( a + b \log \left[ c \left( d + e \sqrt{x} \right)^2 \right] \right)^p dx$$

## Problem 539: Unable to integrate problem.

$$\int x^2 \left( a + b \log \left[ c \left( d + e \sqrt{x} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 677 leaves, 21 steps):

$$\begin{split} &\frac{1}{c^3\,e^6}3^{-1-p}\,e^{-\frac{3\,s}{b}}\,\mathsf{Gamma}\big[1+p,\,-\frac{3\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)}{b} \Big] \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)^p \left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]}{b}\right)^{-p} - \\ &\left(2^{1+p}\times 5^{-p}\,d\,e^{-\frac{5\,s}{2\,b}}\,\left(d+e\,\sqrt{x}\,\right)^5\,\mathsf{Gamma}\big[1+p,\,-\frac{5\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)}{2\,b}\right] \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)^p \left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]}{b}\right)^{-p} \right) \bigg/ \left(e^6\,\left(c\,\left(d+e\,\sqrt{x}\,\right)^2\right)^{5/2}\right) + \\ &\frac{1}{c^2\,e^6}5\times 2^{-p}\,d^2\,e^{-\frac{3\,s}{b}}\,\mathsf{Gamma}\big[1+p,\,-\frac{2\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)}{b}\right] \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)^p \left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]}{b}\right)^{-p} - \\ &\left[5\times 2^{2+p}\times 3^{-1-p}\,d^3\,e^{-\frac{1\,s}{2\,b}}\,\left(d+e\,\sqrt{x}\,\right)^3\,\mathsf{Gamma}\big[1+p,\,-\frac{3\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)}{2\,b}\right] \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)^p \left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]}{b}\right) \bigg/ \left(e^6\,\left(c\,\left(d+e\,\sqrt{x}\,\right)^2\right)^{3/2}\right) + \\ &\frac{1}{c\,e^6}5\,d^4\,e^{-\frac{3\,s}{b}}\,\mathsf{Gamma}\big[1+p,\,-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]}{b}\right] \left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)^p \\ &\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]}{b}\right)^{-p} - \left(2^{1+p}\,d^5\,e^{-\frac{3\,s}{2\,b}}\,\left(d+e\,\sqrt{x}\,\right)^2\right) \bigg|^{-p}\right) \bigg/ \left(e^6\,\sqrt{c\,\left(d+e\,\sqrt{x}\,\right)^2}\right) \right] \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)^p \left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]}{b}\right)^{-p} \right) \bigg/ \left(e^6\,\sqrt{c\,\left(d+e\,\sqrt{x}\,\right)^2}\right) \bigg|^{-p} \right) \bigg/ \left(e^6\,\sqrt{c\,\left(d+e\,\sqrt{x}\,\right)^2}\right) \bigg|^{-p} \right. \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)^{-p} - \left(2^{1+p}\,d^5\,e^{-\frac{3\,s}{2\,b}}\,\left(d+e\,\sqrt{x}\,\right)^2\right) \bigg|^{-p} \right) \bigg/ \left(e^6\,\sqrt{c\,\left(d+e\,\sqrt{x}\,\right)^2}\right) \bigg|^{-p} \bigg|^{-p} \right. \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,\sqrt{x}\,\right)^2\big]\right)^{-p} - \left(2^{1+p}\,d^5\,e^{-\frac{3\,s}{2\,b}}\,\left(d+e\,\sqrt{x}\,\right)^2\right) \bigg|^{-p} \bigg$$

$$\int x^2 \left( a + b \, Log \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)^p \, dx$$

Problem 540: Unable to integrate problem.

$$\int x \left( a + b \operatorname{Log} \left[ c \left( d + e \sqrt{x} \right)^{2} \right] \right)^{p} dx$$

Optimal (type 4, 445 leaves, 15 steps):

$$\begin{split} &\frac{1}{c^2\,e^4} 2^{-1-p}\,e^{-\frac{2\,a}{b}}\,\mathsf{Gamma}\,\big[1+p,-\frac{2\,\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]\right)}{\mathsf{b}} \\ &\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]\right)^p \left(-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]}{\mathsf{b}}\right)^{-p} - \\ &\left(2^{1+p}\times 3^{-p}\,\mathsf{d}\,e^{-\frac{3\,a}{2\,b}}\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^3\,\mathsf{Gamma}\,\big[1+p,-\frac{3\,\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]\right)}{2\,\mathsf{b}}\right] \\ &\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]\right)^p \left(-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]}{\mathsf{b}}\right)^{-p} \right) \left/\left(\mathsf{e}^4\left(\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\right)^{3/2}\right) + \\ &\frac{1}{\mathsf{c}\,\mathsf{e}^4} 3\,\mathsf{d}^2\,e^{-\frac{a}{b}}\,\mathsf{Gamma}\big[1+p,-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]}{\mathsf{b}}\right] \left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]\right)^p \\ &\left(-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]}{\mathsf{b}}\right)^{-p} - \left(2^{1+p}\,\mathsf{d}^3\,e^{-\frac{a}{2\,b}}\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)\,\mathsf{Gamma}\big[1+p,-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]}{2\,\mathsf{b}}\right) \\ &\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]\right)^p \left(-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]}{\mathsf{b}}\right)^{-p} \right) / \left(\mathsf{e}^4\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2}\right) \right)^p \right) \\ &\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]\right)^p \left(-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]}{\mathsf{b}}\right)^{-p} \right) / \left(\mathsf{e}^4\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2}\right) \right)^{-p} \right) \\ &\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]\right)^{-p} \left(-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]}{\mathsf{b}}\right)^{-p} \right) / \left(\mathsf{e}^4\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2}\right)^{-p} \right) \\ &\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]\right)^{-p} \left(-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2\big]}{\mathsf{b}}\right)^{-p} \right) / \left(\mathsf{e}^4\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2}\right)^{-p} \right) \\ &\left(\mathsf{e}^4\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}}\,\right)^2}\right)^{-p} \right)^{-p} \left(\mathsf{e}^4\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{c}}\,\right)^2}\right)^{-p} \right) / \left(\mathsf{e}^4\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{c}\,\right)^2}\right)^2}\right)^{-p} \right) / \left(\mathsf{e}^4\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{c}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{c}\,\left(\mathsf{$$

Result (type 8, 24 leaves):

$$\int x \left( a + b \operatorname{Log} \left[ c \left( d + e \sqrt{x} \right)^{2} \right] \right)^{p} dx$$

Problem 541: Unable to integrate problem.

$$\int \left( a + b \log \left[ c \left( d + e \sqrt{x} \right)^{2} \right] \right)^{p} dx$$

Optimal (type 4, 213 leaves, 9 steps):

$$\begin{split} &\frac{1}{c\,e^2}e^{-\frac{a}{b}}\,\mathsf{Gamma}\,\big[1+p\,,\,-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\,c\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}\,}\right)^2\big]}{\mathsf{b}}\,\bigg]\\ &\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\,c\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}\,}\right)^2\big]\,\right)^p\,\left(-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\,c\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}\,}\right)^2\big]}{\mathsf{b}}\right)^{-p}\,-\\ &\left[2^{1+p}\,\mathsf{d}\,\,e^{-\frac{a}{2\,b}}\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}\,}\right)\,\mathsf{Gamma}\,\big[\,1+p\,,\,-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\,c\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}\,}\right)^2\big]}{2\,\mathsf{b}}\,\right]\,\left(\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\,c\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}\,}\right)^2\big]\right)^p\\ &\left(-\frac{\mathsf{a}+\mathsf{b}\,\mathsf{Log}\big[\,c\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}\,}\right)^2\big]}{\mathsf{b}}\right)^{-p}\right)\bigg/\left(e^2\,\sqrt{c\,\left(\mathsf{d}+\mathsf{e}\,\sqrt{\mathsf{x}\,}\right)^2}\right) \end{split}$$

$$\int \left( a + b \, Log \left[ c \, \left( d + e \, \sqrt{x} \, \right)^2 \right] \right)^p \, dx$$

#### Problem 553: Unable to integrate problem.

$$\int \frac{\left(a + b \log\left[c \left(d + \frac{e}{\sqrt{x}}\right)^{2}\right]\right)^{p}}{x^{2}} dx$$

Optimal (type 4, 213 leaves, 9 steps):

$$\begin{split} &-\frac{1}{c\,e^2}e^{-\frac{a}{b}}\,\text{Gamma}\,\big[1+p\text{,}\,-\frac{a+b\,\text{Log}\,\big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\big]}{b}\big]\\ &-\left(a+b\,\text{Log}\,\big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\big]\right)^p\left(-\frac{a+b\,\text{Log}\,\big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\big]}{b}\right)^{-p}+\\ &\left(2^{1+p}\,d\,e^{-\frac{a}{2\,b}}\left(d+\frac{e}{\sqrt{x}}\right)\,\text{Gamma}\,\big[1+p\text{,}\,-\frac{a+b\,\text{Log}\,\big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\big]}{2\,b}\big]\\ &\left(a+b\,\text{Log}\,\big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\big]\right)^p\left(-\frac{a+b\,\text{Log}\,\big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\big]}{b}\right)^{-p}\right)\bigg/\left(e^2\,\sqrt{c\,\left(d+\frac{e}{\sqrt{x}}\right)^2}\right) \end{split}$$

Result (type 8, 26 leaves):

$$\int \frac{\left(a + b \log \left[c \left(d + \frac{e}{\sqrt{x}}\right)^{2}\right]\right)^{p}}{x^{2}} dx$$

### Problem 554: Unable to integrate problem.

$$\int \frac{\left(a + b \, Log\left[c \, \left(d + \frac{e}{\sqrt{x}}\right)^2\right]\right)^p}{x^4} \, dx$$

Optimal (type 4, 676 leaves, 21 steps):

$$\begin{split} &-\frac{1}{c^3\,e^6}3^{-1-p}\,e^{-\frac{1a}{b}}\,\mathsf{Gamma}\Big[1+p,\,-\frac{3\left(a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right)\Big]}{b}\Big]\\ &-\left(a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\Big)^p\left[-\frac{a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right]^{-p}+\\ &-\left(2^{1+p}\times 5^{-p}\,d\,e^{-\frac{3a}{23}}\,\left(d+\frac{e}{\sqrt{x}}\right)^5\,\mathsf{Gamma}\Big[1+p,\,-\frac{5\left(a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{2\,b}\Big]\\ &-\left(a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\Big)^p\left[-\frac{a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right]^{-p}\Big]/\left(e^6\left(c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right)^{5/2}\right)-\\ &-\frac{1}{c^2\,e^6}5\times 2^{-p}\,d^2\,e^{-\frac{2a}{b}}\,\mathsf{Gamma}\Big[1+p,\,-\frac{2\left(a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)}{b}\Big]\\ &-\left(a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p\left[-\frac{a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right]^{-p}+\\ &-\left(5\times 2^{2+p}\times 3^{-1-p}\,d^3\,e^{-\frac{2a}{2b}}\left(d+\frac{e}{\sqrt{x}}\right)^3\right)\right)^p\left[-\frac{a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right]^{-p}\Big]/\left(e^6\left(c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right)^{3/2}\right)-\\ &-\frac{1}{c\,e^6}5\,d^4\,e^{-\frac{a}{b}}\,\mathsf{Gamma}\Big[1+p,\,-\frac{a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{b}\right]\left(a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right)^p\right)^p\\ &-\left(-\frac{a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right)^2\right)^{-p}+\left(2^{1+p}\,d^5\,e^{-\frac{a}{2b}}\,\left(d+\frac{e}{\sqrt{x}}\right)\,\mathsf{Gamma}\Big[1+p,\,-\frac{a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]}{2\,b}\right]\\ &-\left(a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right)^p\right)^p\left[-\frac{a+b\,\mathsf{Log}\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right]^{-p}}{b}\right]/\left(e^6\sqrt{c}\left(d+\frac{e}{\sqrt{x}}\right)^2\right)^2\end{split}$$

$$\int \frac{\left(a+b\, Log\left[c\, \left(d+\frac{e}{\sqrt{x}}\right)^2\right]\right)^p}{x^4}\, \mathrm{d}x$$

#### Problem 555: Unable to integrate problem.

$$\int \frac{\left(a + b Log\left[c \left(d + \frac{e}{\sqrt{x}}\right)^{2}\right]\right)^{p}}{x^{6}} dx$$

Optimal (type 4, 1141 leaves, 33 steps):

$$\begin{split} &-\frac{1}{c^5\,e^{10}}5^{-1-p}\,e^{-\frac{5a}{b}}\,\mathsf{Gamma}\,\Big[1+p,\,-\frac{5\,\left(a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]\right)}{b}\Big]\\ &-\left(a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]}{b}\right)^{-p}+\\ &\left(2^{1+p}\times 9^{-p}\,d\,e^{-\frac{9a}{2b}}\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]}{2\,b}\right)^{-p}\right)\bigg/\left(e^{10}\,\left(c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big)\right)\\ &-\left(a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]}{b}\right)^{-p}\right)\bigg/\left(e^{10}\,\left(c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\right)^{9/2}\right)-\\ &-\frac{1}{c^4\,e^{10}}9\times 4^{-p}\,d^2\,e^{-\frac{4a}{b}}\,\mathsf{Gamma}\,\Big[1+p,\,-\frac{4\,\left(a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]\right)}{b}\right)\\ &-\left(a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]\right)^p\bigg(-\frac{a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]}{b}\right)^{-p}+\\ &-\frac{3\times 2^{3+p}\times 7^{-p}\,d^3\,e^{-\frac{2a}{2b}}\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]\right)^p\bigg(-\frac{a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]}{b}\right)^{-p}\bigg/\left(e^{10}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]\right)^{-p}\bigg)-\\ &-\frac{1}{c^3\,e^{10}}14\times 3^{1-p}\,d^4\,e^{-\frac{3a}{b}}\,\mathsf{Gamma}\,\Big[1+p,\,-\frac{3\,\left(a+b\,\mathsf{Log}\,\Big[c\,\left(d+\frac{e}{\sqrt{x}}\right)^2\,\Big]\right)}{b}\right)^{-p}+\\ &-\frac{1}{c^3\,e^{10}}14\times 3^{1-p}\,d^4\,e^{-\frac{3a}{b}}\,\mathsf{Gamma}\,\Big[1+p,\,-\frac{3}{b}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3a}{b}}\,e^{-\frac{3$$

$$\left[ 63 \times 2^{2+p} \times 5^{-1-p} \, d^5 \, e^{-\frac{5a}{2b}} \left( d + \frac{e}{\sqrt{x}} \right)^5 \, \text{Gamma} \left[ 1 + p_{\text{\tiny $p$}} - \frac{5 \left( a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right] \right)}{2 \, b} \right]$$
 
$$\left( a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right] \right)^p \left( - \frac{a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right]}{b} \right)^{-p} \right) / \left( e^{1\theta} \left( c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right)^{5/2} \right) - \frac{1}{c^2 \, e^{1\theta}} 21 \times 2^{1-p} \, d^6 \, e^{-\frac{2b}{b}} \, \text{Gamma} \left[ 1 + p_{\text{\tiny $p$}} - \frac{2 \, \left( a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right] \right)}{b} \right]$$
 
$$\left( a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right] \right)^p \left( - \frac{a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right] \right)^{-p} + \frac{2b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right]}{b} \right)^{-p} \right)$$
 
$$\left( a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right] \right)^p \left( - \frac{a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right] \right)^{-p} \right) / \left( e^{1\theta} \left( c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right)^{3/2} \right) - \frac{1}{c \, e^{1\theta}} 9 \, d^8 \, e^{-\frac{e}{b}} \, \text{Gamma} \left[ 1 + p_{\text{\tiny $p$}} - \frac{a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right] \right)$$
 
$$\left( - \frac{a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right]}{b} \right)^{-p} + \left( 2^{1+p} \, d^9 \, e^{-\frac{e}{2b}} \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right) \right)^{-p} \right) / \left( e^{1\theta} \, \sqrt{c \, \left( d + \frac{e}{\sqrt{x}} \right)^2} \right)$$
 
$$\left( a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right] \right)^p - \frac{a + b \, \text{Log} \left[ c \, \left( d + \frac{e}{\sqrt{x}} \right)^2 \right]}{b} \right)^{-p} \right) / \left( e^{1\theta} \, \sqrt{c \, \left( d + \frac{e}{\sqrt{x}} \right)^2} \right)$$

$$\int \frac{\left(a + b \, Log \left[c \, \left(d + \frac{e}{\sqrt{x}}\right)^2\right]\right)^p}{x^6} \, dx$$

## Problem 562: Unable to integrate problem.

$$\int x^3 \left(a + b \operatorname{Log}\left[c \left(d + e x^{1/3}\right)^2\right]\right)^p dx$$

Optimal (type 4, 1363 leaves, 39 steps):

$$\frac{1}{c^{6} e^{12}} 2^{-2-p} \times 3^{-p} e^{-\frac{6a}{b}} \operatorname{Gamma} \left[ 1 + p, -\frac{6 \left( a + b \operatorname{Log} \left[ c \left( d + e x^{1/3} \right)^{2} \right] \right)}{b} \right]$$

$$\left(a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]\right)^p \left(-\frac{a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]}{b}\right)^{-p} - \left(3 \left[\frac{2}{11}\right]^p d \, e^{-\frac{114}{2}} \left(d + e \, x^{1/3}\right)^{13} \, \mathsf{Gamma} \left[1 + p, \, -\frac{11 \left(a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]\right)}{2b}\right] \right)$$
 
$$\left(a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]\right)^p \left(-\frac{a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]\right)^{-p} \right) / \left(e^{12} \left(c \left(d + e \, x^{1/3}\right)^2\right)^{11/2}\right) + \frac{1}{2c^5 \, e^{12}} \, 33 \times 5^{-p} \, d^2 \, e^{-\frac{52}{2}} \, \mathsf{Gamma} \left[1 + p, \, -\frac{5 \left(a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]\right)}{b}\right) - \frac{1}{2b}$$
 
$$\left(a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]\right)^p \left(-\frac{a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]}{b}\right)^{-p} - \frac{5 \left(a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]\right)}{2b} \right)$$
 
$$\left(a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]\right)^p \left(-\frac{a + b \log \left[c \left(d + e \, x^{1/3}\right)^2\right]}{b}\right)^{-p} \right) / \left(e^{12} \left(c \left(d + e \, x^{1/3}\right)^2\right)^{9/2}\right) + \frac{1}{c^4 \, e^{12}} \, 495 \cdot 2^{-2 \, (1 + p)} \, d^4 \, e^{-\frac{4 \, e^4 \, e^4$$

$$\left(a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]\right)^p \left(-\frac{a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]}{b}\right)^{-p} - \left[55 \left(\frac{2}{3}\right)^p d^9 \, e^{-\frac{3a}{2b}} \left(d + e \, x^{1/3}\right)^3 \, \text{Gamma} \left[1 + p\right], -\frac{3 \, \left(a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]\right)}{2 \, b}\right]$$
 
$$\left(a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]\right)^p \left(-\frac{a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]}{b}\right)^{-p} \right) / \left(e^{12} \left(c \, \left(d + e \, x^{1/3}\right)^2\right)^{3/2}\right) + \frac{1}{2 \, c \, e^{12}} 33 \, d^{10} \, e^{-\frac{a}{b}} \, \text{Gamma} \left[1 + p\right], -\frac{a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]}{b}\right] \left(a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]\right)^p$$
 
$$\left(-\frac{a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]}{b}\right)^{-p} - \frac{a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]}{2 \, b}\right]$$
 
$$\left(a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]\right)^p \left(-\frac{a + b \, \text{Log} \left[c \, \left(d + e \, x^{1/3}\right)^2\right]}{b}\right)^{-p} \right) / \left(e^{12} \, \sqrt{c \, \left(d + e \, x^{1/3}\right)^2}\right)$$

$$\int x^3 \left(a + b \operatorname{Log}\left[c \left(d + e x^{1/3}\right)^2\right]\right)^p dx$$

# Problem 563: Unable to integrate problem.

$$\int x^2 \left( a + b \log \left[ c \left( d + e x^{1/3} \right)^2 \right] \right)^p dx$$

Optimal (type 4, 1035 leaves, 30 steps):

$$\left( 2^p \times 3^{-1-2\,p} \, e^{-\frac{9\,a}{2\,b}} \, \left( d + e \, x^{1/3} \right)^9 \, \text{Gamma} \left[ 1 + p \text{,} \, - \frac{9 \, \left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right] \right)}{2 \, b} \right]$$
 
$$\left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right] \right)^p \left( - \frac{a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right]}{b} \right)^{-p} \right) / \left( e^9 \, \left( c \, \left( d + e \, x^{1/3} \right)^2 \right)^{9/2} \right) - \frac{1}{c^4 \, e^9} 3 \times 4^{-p} \, d \, e^{-\frac{4\,a}{b}} \, \text{Gamma} \left[ 1 + p \text{,} \, - \frac{4 \, \left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right] \right)}{b} \right]$$
 
$$\left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right] \right)^p \left( - \frac{a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right]}{b} \right)^{-p} + \frac{3 \, \left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right] \right)}{2 \, b} \right)$$
 
$$\left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right] \right)^p \left( - \frac{a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right]}{b} \right)^{-p} \right) / \left( e^9 \, \left( c \, \left( d + e \, x^{1/3} \right)^2 \right)^{7/2} \right) - \frac{3 \, \left( a + b \, \text{Log} \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right] \right)^{-p}}{b} \right)$$

$$\begin{split} &\frac{1}{c^3\,e^3}28\times 3^{-p}\,d^3\,e^{-\frac{3\,s}{b}}\,\mathsf{Gamma}\,\big[1+p,-\frac{3\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]\right)}{b}\big]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]}{b}\right)^{-p}+\\ &\left(21\times 2^{1+p}\times 5^{-p}\,d^4\,e^{-\frac{5\,s}{2\,b}}\,\left(d+e\,x^{1/3}\right)^5\,\mathsf{Gamma}\,\big[1+p,-\frac{5\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]\right)}{2\,b}\big]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]}{b}\right)^{-p}\right)\bigg/\left(e^{9}\,\left(c\,\left(d+e\,x^{1/3}\right)^2\right)\right)\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]}{b}\right)^{-p}+\\ &\left(7\times 2^{2+p}\times 3^{-p}\,d^6\,e^{-\frac{3\,s}{2\,b}}\,\left(d+e\,x^{1/3}\right)^3\,\mathsf{Gamma}\,\big[1+p,-\frac{3\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]\right)}{2\,b}\right)\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]}{b}\right)^{-p}\right)\bigg/\left(e^9\,\left(c\,\left(d+e\,x^{1/3}\right)^2\right)^{3/2}\right)-\\ &\frac{1}{c\,e^3}12\,d^7\,e^{-\frac{a}{b}}\,\mathsf{Gamma}\,\big[1+p,-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]}{b}\right]\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]\right)^p\\ &\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]}{b}\right)^{-p}+\\ &\left(3\times 2^p\,d^3\,e^{-\frac{a}{2\,b}}\,\left(d+e\,x^{1/3}\right)^3\,\mathsf{Gamma}\,\big[1+p,-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]}{2\,b}\right)^{-p}\right)\bigg/\left(e^9\,\sqrt{c\,\left(d+e\,x^{1/3}\right)^2}\right)\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^3\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^2\big]}{2\,b}\right)^{-p}\bigg)\bigg/\left(e^9\,\sqrt{c\,\left(d+e\,x^{1/3}\right)^2}\right)\bigg)\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^3\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^3\big]}{2\,b}\right)^{-p}\bigg)\bigg/\left(e^9\,\sqrt{c\,\left(d+e\,x^{1/3}\right)^2}\right)\bigg)\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^3\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^3\big]}{2\,b}\right)^{-p}\bigg)\bigg/\left(e^9\,\sqrt{c\,\left(d+e\,x^{1/3}\right)^2}\right)\bigg)$$

$$\int x^2 \left( a + b \, Log \left[ c \, \left( d + e \, x^{1/3} \right)^2 \right] \right)^p \, dx$$

## Problem 564: Unable to integrate problem.

$$\int x \left(a + b Log \left[c \left(d + e x^{1/3}\right)^{2}\right]\right)^{p} dx$$

Optimal (type 4, 673 leaves, 21 steps):

$$\begin{split} &\frac{1}{2\,c^{3}\,e^{6}}3^{-p}\,e^{-\frac{3z}{b}}\,\mathsf{Gamma}\big[1+p,\,-\frac{3\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)}{b}\big]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}-\\ &\left(3\,\left(\frac{2}{5}\right)^{p}\,d\,e^{-\frac{5z}{2b}}\,\left(d+e\,x^{1/3}\right)^{5}\,\mathsf{Gamma}\big[1+p,\,-\frac{5\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)}{2\,b}\big]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right)\bigg/\left(e^{6}\left(c\,\left(d+e\,x^{1/3}\right)^{2}\right)^{5/2}\right)+\\ &\frac{1}{c^{2}\,e^{6}}15\times2^{-1-p}\,d^{2}\,e^{-\frac{2z}{b}}\,\mathsf{Gamma}\big[1+p,\,-\frac{2\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)}{b}\big]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}-\\ &\left(5\times2^{1+p}\times3^{-p}\,d^{3}\,e^{-\frac{3z}{2b}}\,\left(d+e\,x^{1/3}\right)^{3}\,\mathsf{Gamma}\big[1+p,\,-\frac{3\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)}{2\,b}\right)\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right/\left(e^{6}\left(c\,\left(d+e\,x^{1/3}\right)^{2}\right)^{3/2}\right)+\\ &\frac{1}{2\,c\,e^{6}}15\,d^{4}\,e^{-\frac{z}{b}}\,\mathsf{Gamma}\big[1+p,\,-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right]\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\\ &\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}-\\ &\left(3\times2^{p}\,d^{5}\,e^{-\frac{z}{2b}}\,\left(d+e\,x^{1/3}\right)^{2}\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right/\left(e^{6}\left(c\,\left(d+e\,x^{1/3}\right)^{2}\right)\right) \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right/\left(e^{6}\left(c\,\left(d+e\,x^{1/3}\right)^{2}\right)^{2}\right) \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right) \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right) \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right) \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right) \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right) \\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{1/3}\right)^{2}\big]}{b}\right)^{-p}\right) \\ &$$

$$\int x \left(a + b Log \left[c \left(d + e x^{1/3}\right)^{2}\right]\right)^{p} dx$$

# Problem 565: Unable to integrate problem.

$$\int \left(a + b \operatorname{Log}\left[c \left(d + e x^{1/3}\right)^{2}\right]\right)^{p} dx$$

Optimal (type 4, 338 leaves, 12 steps):

$$\begin{split} &\left(\frac{2}{3}\right)^{p} \, e^{-\frac{3\,a}{2\,b}} \, \left(d + e \, x^{1/3}\right)^{3} \, \text{Gamma} \left[1 + p_{\text{\tiny J}} - \frac{3\, \left(a + b \, \text{Log} \left[c\, \left(d + e \, x^{1/3}\right)^{2}\right]\right)}{2\, b} \right] \\ & \left(a + b \, \text{Log} \left[c\, \left(d + e \, x^{1/3}\right)^{2}\right]\right)^{p} \left(-\frac{a + b \, \text{Log} \left[c\, \left(d + e \, x^{1/3}\right)^{2}\right]}{b}\right)^{-p} \right) \bigg/ \, \left(e^{3} \, \left(c\, \left(d + e \, x^{1/3}\right)^{2}\right)^{3/2}\right) - \frac{1}{c\, e^{3}} 3 \, d \, e^{-\frac{a}{b}} \, \text{Gamma} \left[1 + p_{\text{\tiny J}} - \frac{a + b \, \text{Log} \left[c\, \left(d + e \, x^{1/3}\right)^{2}\right]}{b}\right] \, \left(a + b \, \text{Log} \left[c\, \left(d + e \, x^{1/3}\right)^{2}\right]\right)^{p} \\ & \left(-\frac{a + b \, \text{Log} \left[c\, \left(d + e \, x^{1/3}\right)^{2}\right]}{b}\right)^{-p} + \frac{3 + b \, \text{Log} \left[c\, \left(d + e \, x^{1/3}\right)^{2}\right]}{2\, b} \\ & \left(a + b \, \text{Log} \left[c\, \left(d + e \, x^{1/3}\right)^{2}\right]\right)^{p} \left(-\frac{a + b \, \text{Log} \left[c\, \left(d + e \, x^{1/3}\right)^{2}\right]}{b}\right)^{-p} \right) \bigg/ \left(e^{3} \, \sqrt{c\, \left(d + e \, x^{1/3}\right)^{2}}\right) \end{split}$$

$$\left[\left(a+b \, \mathsf{Log}\left[c\, \left(d+e \, x^{1/3}\right)^2\right]\right)^p \, \mathrm{d}x\right]$$

#### Problem 575: Unable to integrate problem.

$$\int x^3 \left(a + b \operatorname{Log}\left[c \left(d + e x^{2/3}\right)^2\right]\right)^p dx$$

Optimal (type 4, 675 leaves, 21 steps):

$$\begin{split} &\frac{1}{4\,c^3\,e^6}3^{-p}\,e^{-\frac{3\,s}{b}}\,\mathsf{Gamma}\big[1+p,\,-\frac{3\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)}{b}\Big]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]}{b}\right)^{-p}-\\ &\left(3\times2^{-1+p}\times5^{-p}\,d\,e^{-\frac{2\,s}{2\,b}}\,\left(d+e\,x^{2/3}\right)^5\,\mathsf{Gamma}\big[1+p,\,-\frac{5\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)}{2\,b}\Big]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]}{b}\right)^{-p}\right/\left(e^6\,\left(c\,\left(d+e\,x^{2/3}\right)^2\right)^{5/2}\right)+\\ &\frac{1}{c^2\,e^6}15\times2^{-2-p}\,d^2\,e^{-\frac{2\,s}{b}}\,\mathsf{Gamma}\big[1+p,\,-\frac{2\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)}{b}\Big]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)^{-p}-\\ &\frac{5\,\left(\frac{2}{3}\right)^p\,d^3\,e^{-\frac{3\,s}{2\,b}}\,\left(d+e\,x^{2/3}\right)^3\,\mathsf{Gamma}\big[1+p,\,-\frac{3\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)}{2\,b}\Big]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]}{b}\right)^{-p}\right/\left(e^6\,\left(c\,\left(d+e\,x^{2/3}\right)^2\right)^{3/2}\right)+\\ &\frac{1}{4\,c\,e^6}15\,d^4\,e^{-\frac{s}{b}}\,\mathsf{Gamma}\big[1+p,\,-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]}{b}\right]\,\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)^p\\ &\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]}{b}\right)^{-p}-\\ &\left(3\times2^{-1+p}\,d^3\,e^{-\frac{s}{a\,b}}\,\left(d+e\,x^{2/3}\right)^2\right)\,\mathsf{Gamma}\big[1+p,\,-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]}{2\,b}\right]\\ &\left(a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]\right)^p\left(-\frac{a+b\,\mathsf{Log}\big[c\,\left(d+e\,x^{2/3}\right)^2\big]}{b}\right)^{-p}\right/\left(e^6\,\sqrt{c\,\left(d+e\,x^{2/3}\right)^2}\right) \end{aligned}$$

$$\int x^3 \left(a + b \, Log \left[c \, \left(d + e \, x^{2/3}\right)^2\right]\right)^p \, dx$$

## Problem 576: Unable to integrate problem.

$$\int x \left(a + b \, \text{Log} \left[ \, c \, \left(d + e \, x^{2/3} \right)^{\, 2} \, \right] \, \right)^{\, p} \, \text{d} x$$

Optimal (type 4, 347 leaves, 12 steps):

$$\left( 2^{-1+p} \times 3^{-p} \ e^{-\frac{3a}{2b}} \ \left( d + e \ x^{2/3} \right)^3 \ \mathsf{Gamma} \left[ 1 + p \text{, } -\frac{3 \ \left( a + b \ \mathsf{Log} \left[ c \ \left( d + e \ x^{2/3} \right)^2 \right] \right)}{2 \ b} \right]$$
 
$$\left( a + b \ \mathsf{Log} \left[ c \ \left( d + e \ x^{2/3} \right)^2 \right] \right)^p \left( -\frac{a + b \ \mathsf{Log} \left[ c \ \left( d + e \ x^{2/3} \right)^2 \right]}{b} \right)^{-p} \right) \bigg/ \left( e^3 \ \left( c \ \left( d + e \ x^{2/3} \right)^2 \right)^{3/2} \right) - \frac{1}{2 \ c \ e^3} 3 \ d \ e^{-\frac{a}{b}} \ \mathsf{Gamma} \left[ 1 + p \text{, } -\frac{a + b \ \mathsf{Log} \left[ c \ \left( d + e \ x^{2/3} \right)^2 \right]}{b} \right] \left( a + b \ \mathsf{Log} \left[ c \ \left( d + e \ x^{2/3} \right)^2 \right] \right)^p$$
 
$$\left( -\frac{a + b \ \mathsf{Log} \left[ c \ \left( d + e \ x^{2/3} \right)^2 \right]}{b} \right)^{-p} + \frac{3 \ \mathsf{Log} \left[ c \ \left( d + e \ x^{2/3} \right)^2 \right]}{2 \ b} \right)$$
 
$$\left( a + b \ \mathsf{Log} \left[ c \ \left( d + e \ x^{2/3} \right)^2 \right] \right)^p \left( -\frac{a + b \ \mathsf{Log} \left[ c \ \left( d + e \ x^{2/3} \right)^2 \right]}{b} \right)^{-p} \right) / \left( e^3 \ \sqrt{c \ \left( d + e \ x^{2/3} \right)^2} \right)^{-p} \right)$$

$$\int x \left(a + b \operatorname{Log}\left[c \left(d + e x^{2/3}\right)^{2}\right]\right)^{p} dx$$

#### Problem 591: Unable to integrate problem.

$$\int \frac{\left(a + b \log \left[c \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p}{x^2} \, dx$$

Optimal (type 4, 339 leaves, 12 steps):

$$\begin{split} &-\left(\left(\left(\frac{2}{3}\right)^{p} e^{-\frac{3a}{2b}} \left(d+\frac{e}{x^{1/3}}\right)^{3} \mathsf{Gamma}\left[1+p,-\frac{3\left(a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)}{2\,b}\right] \\ &-\left(a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)^{p} \left(-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]}{b}\right)^{-p} \right) \middle/\left(e^{3}\left(c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right)^{3/2}\right)\right) + \\ &-\frac{1}{c\,e^{3}} 3\, d\, e^{-\frac{a}{b}} \, \mathsf{Gamma}\left[1+p,-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]}{b}\right] \, \left(a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)^{p} \\ &-\left(-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]}{b}\right)^{-p} - \\ &-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]}{b} \, \mathsf{Gamma}\left[1+p,-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]}{2\,b}\right] \\ &-\left(a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)^{p} \left(-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]}{b}\right)^{-p} \middle/\left(e^{3} \, \sqrt{c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}}\right) \\ &-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right) \\ &-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right) \\ &-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right) \\ &-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right) \\ &-\frac{a+b \, \mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1$$

$$\int \frac{\left(a+b \, Log\left[c\, \left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p}{x^2} \, dx$$

## Problem 592: Unable to integrate problem.

$$\int \frac{\left(a + b \, Log\left[c \, \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p}{x^3} \, dx$$

Optimal (type 4, 673 leaves, 21 steps):

$$\begin{split} &-\frac{1}{2\,c^3\,e^6}3^{-p}\,e^{\frac{-3\,x}{4}}\,\mathsf{Gamma}\left[1+p,\,-\frac{3\,\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)}{b}\right]\\ &-\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}\\ &+\left(3\,\left(\frac{2}{5}\right)^p\,d\,\,e^{-\frac{2\,x}{2\,3}}\,\left(d+\frac{e}{x^{1/3}}\right)^5\,\mathsf{Gamma}\left[1+p,\,-\frac{5\,\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)}{2\,b}\right]\\ &-\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^{-p}\right)\bigg/\left(e^6\left(c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right)^{5/2}\right)-\\ &-\frac{1}{c^2\,e^6}15\times2^{-1-p}\,d^2\,e^{-\frac{2\,x}{3}}\,\mathsf{Gamma}\left[1+p,\,-\frac{2\,\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)}{b}\right]\\ &-\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^{-p}\\ &-\frac{b}{b}\\ &-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)\\ &-\frac{2\,b}{b}\\ &-\frac{1}{2\,c\,e^6}15\,d^4\,e^{-\frac{2\,x}{3}}\,\mathsf{Gamma}\left[1+p,\,-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^{-p}\right/\left(e^6\left(c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right)^{3/2}\right)-\\ &-\frac{1}{2\,c\,e^6}15\,d^4\,e^{-\frac{2\,x}{3}}\,\mathsf{Gamma}\left[1+p,\,-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]}{b}\right]\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right)^p\right)\\ &-\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^{-p}+\left\{3\times2^p\,d^5\,e^{-\frac{2\,x}{3}}\left(d+\frac{e}{x^{1/3}}\right)\,\mathsf{Gamma}\left[1+p,\,-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]}{2\,b}\right]\right)\\ &-\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^{-p}\right)\\ &-\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^{-p}+\left\{3\times2^p\,d^5\,e^{-\frac{2\,x}{3}}\left(d+\frac{e}{x^{1/3}}\right)\,\mathsf{Gamma}\left[1+p,\,-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]}{2\,b}\right)\right]\\ &-\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}\right)\\ &-\left(\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}\left(\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p}\right)\\ &-\left(\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right)^{-p}}{b}\right)^{-p}\left(\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right)}{b}\right)^{-p}}\right)\\ &-\left(\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right)^{-p}}{b}\right)^{-p}\left(\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right)^{-p}}{b}\right)^{-p}}\right)\\ &-\left(\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right)^{-p}}{b}\right)^{-p}\left(\frac{a+b\,\mathsf{Log}$$

$$\int \frac{\left(a+b \ Log\left[\, c \ \left(d+\frac{e}{x^{1/3}}\right)^{\, 2}\,\right]\,\right)^{\, p}}{x^3} \ \mathrm{d}\, x$$

### Problem 593: Unable to integrate problem.

$$\int \frac{\left(a+b \, Log\left[c\, \left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p}{x^4} \, dx$$

Optimal (type 4, 1036 leaves, 30 steps):

$$-\left[\left(2^{p}\times3^{-1\cdot2\,p}\,e^{-\frac{9z}{2\,b}}\left(d+\frac{e}{x^{1/3}}\right)^{9}\,\mathsf{Gamma}\left[1+p,-\frac{9\,\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right)\right)}{2\,b}\right]\right]\\ =\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]}{b}\right)^{-p}\right)\bigg/\left(e^{9}\left(c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right)^{9/2}\right)\bigg)+\\ =\frac{1}{c^{4}\,e^{9}}3\times4^{-p}\,d\,e^{-\frac{4z}{b}}\,\mathsf{Gamma}\left[1+p,-\frac{4\,\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)}{b}\right]\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)^{p}-\\ =\frac{1}{c^{4}\,e^{9}}3\times4^{-p}\,d\,e^{-\frac{4z}{b}}\,\mathsf{Gamma}\left[1+p,-\frac{7\,\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)}{b}\right]\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)^{p}-\\ =\frac{1}{c^{3}\,e^{9}}\times7^{-p}\,d^{2}\,e^{-\frac{7z}{2\,b}}\left(d+\frac{e}{x^{1/3}}\right)^{2}\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]}{b}\right)^{-p}\right/\left(e^{9}\left(c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right)^{7/2}\right)+\\ =\frac{1}{c^{3}\,e^{9}}28\times3^{-p}\,d^{3}\,e^{-\frac{3z}{b}}\,\mathsf{Gamma}\left[1+p,-\frac{3\,\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)}{b}\right]\\ =\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)^{p}\left(-\frac{a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]}{b}\right)^{-p}-\\ =\frac{1}{c^{3}\,e^{9}}21\times2^{1+p}\times5^{-p}\,d^{4}\,e^{-\frac{5z}{2b}}\left(d+\frac{e}{x^{1/3}}\right)^{5}\,\mathsf{Gamma}\left[1+p,-\frac{5\,\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)}{2\,b}\right]\\ =\frac{1}{c^{3}\,e^{9}}21\times2^{1+p}\,d^{5}\,e^{-\frac{7z}{2b}}\,\mathsf{Gamma}\left[1+p,-\frac{2\,\left(a+b\,\mathsf{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^{2}\right]\right)}{b}\right]$$

$$\begin{split} &\left(a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{3/3}}\right)^2\right]}{b}\right)^{-p} - \\ &\left(7\times2^{2+p}\times3^{-p}\,d^6\,e^{-\frac{3\,a}{2\,b}}\left(d+\frac{e}{x^{1/3}}\right)^3\,\text{Gamma}\left[1+p,\,-\frac{3\,\left(a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)}{2\,b}\right] \\ &\left(a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{3/3}}\right)^2\right]}{b}\right)^{-p} \right) \bigg/ \left(e^9\left(c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right)^{3/2}\right) + \\ &\frac{1}{c\,e^9}12\,d^7\,e^{-\frac{a}{b}}\,\text{Gamma}\left[1+p,\,-\frac{a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{3/3}}\right)^2\right]}{b}\right] \left(a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p \\ &\left(-\frac{a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{3/3}}\right)^2\right]}{b}\right)^{-p} - \\ &\left(3\times2^p\,d^8\,e^{-\frac{a}{2\,b}}\left(d+\frac{e}{x^{1/3}}\right)\,\text{Gamma}\left[1+p,\,-\frac{a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]}{2\,b}\right] \\ &\left(a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]\right)^p \left(-\frac{a+b\,\text{Log}\left[c\,\left(d+\frac{e}{x^{1/3}}\right)^2\right]}{b}\right)^{-p} \right) \bigg/ \left(e^9\,\sqrt{c\,\left(d+\frac{e}{x^{1/3}}\right)^2}\right) \end{split}$$

$$\int \frac{\left(a + b \, \text{Log}\left[c \, \left(d + \frac{e}{x^{1/3}}\right)^2\right]\right)^p}{x^4} \, dx$$

# Problem 619: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\,[\,f\,x^p\,]\,\,\text{Log}\,[\,1+e\,x^m\,]}{x}\,\text{d}\,x$$

Optimal (type 4, 33 leaves, 2 steps):

$$-\frac{\text{Log[fx}^p] \text{ PolyLog[2, -ex}^m]}{\text{m}} + \frac{\text{p PolyLog[3, -ex}^m]}{\text{m}^2}$$

Result (type 4, 160 leaves):

$$\begin{split} &\frac{1}{6\,m^2} \left( -\,m^3\,p\, \text{Log}\,[\,x\,]^{\,3} \,-\, 3\,\,m^2\,p\, \text{Log}\,[\,x\,]^{\,2}\, \text{Log}\,\big[\,\frac{e + x^{-m}}{e}\,\big] \,+\, \\ &3\,m^2\,p\, \text{Log}\,[\,x\,]^{\,2}\, \text{Log}\,\big[\,1 + e\, x^m\,\big] \,-\, 6\,m\,p\, \text{Log}\,[\,x\,]\, \text{Log}\,\big[\,-e\, x^m\,\big]\, \text{Log}\,\big[\,1 + e\, x^m\,\big] \,+\, \\ &6\,m\, \text{Log}\,\big[\,-e\, x^m\,\big]\, \text{Log}\,\big[\,f\, x^p\,\big]\, \text{Log}\,\big[\,1 + e\, x^m\,\big] \,+\, 6\,m\,p\, \text{Log}\,[\,x\,]\, \text{PolyLog}\,\big[\,2 \,,\, -\, \frac{x^{-m}}{e}\,\big] \,+\, \\ &6\,m\, \left( -\,p\, \text{Log}\,[\,x\,] \,+\, \text{Log}\,\big[\,f\, x^p\,\big] \,\right)\, \text{PolyLog}\,\big[\,2 \,,\, 1 + e\, x^m\,\big] \,+\, 6\,p\, \text{PolyLog}\,\big[\,3 \,,\, -\, \frac{x^{-m}}{e}\,\big] \,\end{split}$$

Problem 620: Result more than twice size of optimal antiderivative.

$$\int \frac{x^{-1+m} Log[fx^p]^2}{d+ex^m} dx$$

Optimal (type 4, 75 leaves, 3 steps):

$$\frac{\text{Log}[\texttt{f}\, x^p]^2\, \text{Log}\big[\texttt{1} + \frac{e\, x^m}{d}\big]}{e\, m} + \frac{2\, p\, \text{Log}[\texttt{f}\, x^p]\,\, \text{PolyLog}\big[\texttt{2}, -\frac{e\, x^m}{d}\big]}{e\, m^2} - \frac{2\, p^2\, \text{PolyLog}\big[\texttt{3}, -\frac{e\, x^m}{d}\big]}{e\, m^3}$$

Result (type 4, 210 leaves):

$$\begin{split} &\frac{1}{3\,e\,m^3} \left( \text{m}^3\,p^2\,\text{Log}[\,x\,]^{\,3} + 3\,\text{m}^2\,p^2\,\text{Log}[\,x\,]^{\,2}\,\text{Log}\big[\,1 + \frac{d\,x^{-m}}{e}\,\big] - 3\,\text{m}^2\,p^2\,\text{Log}[\,x\,]^{\,2}\,\text{Log}\big[\,d + e\,x^{m}\,\big] + \\ &- 6\,\text{m}\,p^2\,\text{Log}[\,x\,]\,\,\text{Log}\big[\,- \frac{e\,x^{m}}{d}\,\big]\,\,\text{Log}\big[\,d + e\,x^{m}\,\big] - 6\,\text{m}\,p\,\,\text{Log}\big[\,- \frac{e\,x^{m}}{d}\,\big]\,\,\text{Log}\big[\,f\,x^{p}\,\big]\,\,\text{Log}\big[\,d + e\,x^{m}\,\big] + \\ &- 3\,\text{m}^2\,\text{Log}\big[\,f\,x^{p}\,\big]^{\,2}\,\,\text{Log}\big[\,d + e\,x^{m}\,\big] - 6\,\text{m}\,p^2\,\,\text{Log}[\,x\,]\,\,\text{PolyLog}\big[\,2 \,, \, - \frac{d\,x^{-m}}{e}\,\big] + \\ &- 6\,\text{m}\,p\,\,\big(\,p\,\,\text{Log}[\,x\,] - \text{Log}\big[\,f\,x^{p}\,\big]\,\big)\,\,\text{PolyLog}\big[\,2 \,, \, 1 + \frac{e\,x^{m}}{d}\,\big] - 6\,p^2\,\,\text{PolyLog}\big[\,3 \,, \, - \frac{d\,x^{-m}}{e}\,\big]\,\big) \end{split}$$

Problem 621: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\,[\,f\,x^p\,]^{\,3}\,\left(\,a\,+\,b\,\,\text{Log}\,\left[\,c\,\,\left(\,d\,+\,e\,\,x^m\,\right)^{\,n}\,\right]\,\right)}{x}\,\,\mathrm{d}x$$

Optimal (type 4, 161 leaves, 6 steps):

$$\begin{split} &\frac{\text{Log}\, [\, f\, x^p \,]^{\, 4}\, \left(a + b\, \text{Log}\, \left[\, c\, \left(d + e\, x^m \,\right)^n \,\right]\, \right)}{4\, p} - \frac{b\, n\, \text{Log}\, [\, f\, x^p \,]^{\, 4}\, \text{Log}\, \left[\, 1 + \frac{e\, x^m}{d} \,\right]}{4\, p} - \\ &\frac{b\, n\, \text{Log}\, [\, f\, x^p \,]^{\, 3}\, \text{PolyLog}\, \left[\, 2\, ,\, -\frac{e\, x^m}{d} \,\right]}{m} + \frac{3\, b\, n\, p\, \text{Log}\, [\, f\, x^p \,]^{\, 2}\, \text{PolyLog}\, \left[\, 3\, ,\, -\frac{e\, x^m}{d} \,\right]}{m^2} - \\ &\frac{6\, b\, n\, p^2\, \text{Log}\, [\, f\, x^p \,]\, \, \text{PolyLog}\, \left[\, 4\, ,\, -\frac{e\, x^m}{d} \,\right]}{m^3} + \frac{6\, b\, n\, p^3\, \text{PolyLog}\, \left[\, 5\, ,\, -\frac{e\, x^m}{d} \,\right]}{m^4} \end{split}$$

Result (type 4, 659 leaves):

$$\begin{split} &-\frac{3}{10}\,b\,m\,n\,p^3\,Log[x]^5 + \frac{3}{4}\,b\,m\,n\,p^2\,Log[x]^4\,Log[f\,x^p] - \\ &-\frac{1}{2}\,b\,m\,n\,p\,Log[x]^3\,Log[f\,x^p]^2 + \frac{a\,Log[f\,x^p]^4}{4\,p} - \frac{3}{4}\,b\,n\,p^3\,Log[x]^4\,Log[1 + \frac{d\,x^{-m}}{e}] + \\ &2\,b\,n\,p^2\,Log[x]^3\,Log[f\,x^p]\,Log[1 + \frac{d\,x^{-m}}{e}] - \frac{3}{2}\,b\,n\,p\,Log[x]^2\,Log[f\,x^p]^2\,Log[1 + \frac{d\,x^{-m}}{e}] + \\ &b\,n\,p^3\,Log[x]^4\,Log[d\,+\,e\,x^m] - \frac{b\,n\,p^3\,Log[x]^3\,Log[-\frac{e\,x^e}{d}]\,Log[d\,+\,e\,x^m]}{m} - \\ &3\,b\,n\,p^2\,Log[x]^3\,Log[f\,x^p]\,Log[d\,+\,e\,x^m] + \frac{3\,b\,n\,p^2\,Log[x]^2\,Log[-\frac{e\,x^e}{d}]\,Log[f\,x^p]\,Log[d\,+\,e\,x^m]}{m} + \\ &3\,b\,n\,p\,Log[x]^2\,Log[f\,x^p]^2\,Log[d\,+\,e\,x^m] - \frac{3\,b\,n\,p\,Log[x]\,Log[-\frac{e\,x^e}{d}]\,Log[f\,x^p]^2\,Log[d\,+\,e\,x^m]}{m} - \\ &b\,n\,Log[x]\,Log[f\,x^p]^3\,Log[d\,+\,e\,x^m] + \frac{b\,n\,Log[-\frac{e\,x^e}{d}]\,Log[f\,x^p]^3\,Log[d\,+\,e\,x^m]}{m} - \\ &\frac{1}{4}\,b\,p^3\,Log[x]^4\,Log[c\,(d\,+\,e\,x^m)^n] + b\,p^2\,Log[x]^3\,Log[f\,x^p]\,Log[c\,(d\,+\,e\,x^m)^n] - \\ &\frac{3}{2}\,b\,p\,Log[x]^2\,Log[f\,x^p]^2\,Log[c\,(d\,+\,e\,x^m)^n] + b\,Log[x]\,Log[f\,x^p]^3\,Log[c\,(d\,+\,e\,x^m)^n] + \\ &\frac{1}{b}\,b\,n\,p\,Log[x]\,\left(p^2\,Log[x]^2 - 3\,p\,Log[x]\,Log[f\,x^p] + 3\,Log[f\,x^p]^2\right)\,PolyLog[2, -\frac{d\,x^{-m}}{e}] - \\ &\frac{b\,n\,\left(p\,Log[x] - Log[f\,x^p]\right)^3\,PolyLog[2, 1 + \frac{e\,x^e}{d}]}{m} + \frac{3\,b\,n\,p\,Log[f\,x^p]^2\,PolyLog[3, -\frac{d\,x^m}{e}]}{m^2} + \\ &\frac{6\,b\,n\,p^2\,Log[f\,x^p]\,PolyLog[4, -\frac{d\,x^m}{e}]}{m^3} + \frac{6\,b\,n\,p^3\,PolyLog[5, -\frac{d\,x^m}{e}]}{m^4} \\ &\frac{6\,b\,n\,p^3\,PolyLog[5, -\frac{d\,x^m}{e}]}{m^4} + \frac{6\,b\,n\,p^3\,PolyLog[5, -\frac$$

# Problem 622: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}[fx^p]^2 \left(a + b \text{Log}\left[c \left(d + e x^m\right)^n\right]\right)}{x} dx$$

Optimal (type 4, 132 leaves, 5 steps):

$$\frac{\text{Log} \left[\text{f} \, x^p\right]^3 \, \left(\text{a} + \text{b} \, \text{Log} \left[\text{c} \, \left(\text{d} + \text{e} \, x^m\right)^n\right]\right)}{3 \, p} - \frac{\text{b} \, \text{n} \, \text{Log} \left[\text{f} \, x^p\right]^3 \, \text{Log} \left[\text{1} + \frac{\text{e} \, x^m}{\text{d}}\right]}{3 \, p} - \frac{\text{b} \, \text{n} \, \text{Log} \left[\text{f} \, x^p\right]^3 \, \text{Log} \left[\text{1} + \frac{\text{e} \, x^m}{\text{d}}\right]}{3 \, p} - \frac{\text{b} \, \text{n} \, \text{Log} \left[\text{f} \, x^p\right]^3 \, \text{PolyLog} \left[\text{3} \, , \, -\frac{\text{e} \, x^m}{\text{d}}\right]}{\text{m}^2} - \frac{\text{2} \, \text{b} \, \text{n} \, \text{p}^2 \, \text{PolyLog} \left[\text{4} \, , \, -\frac{\text{e} \, x^m}{\text{d}}\right]}{\text{m}^3}$$

Result (type 4, 456 leaves):

$$\begin{split} &\frac{1}{4}\,b\,m\,n\,p^2\,Log[x]^4 - \frac{1}{3}\,b\,m\,n\,p\,Log[x]^3\,Log\big[f\,x^p\big] + \frac{a\,Log[f\,x^p]^3}{3\,p} + \\ &\frac{2}{3}\,b\,n\,p^2\,Log[x]^3\,Log\big[1 + \frac{d\,x^{-m}}{e}\big] - b\,n\,p\,Log[x]^2\,Log\big[f\,x^p\big]\,Log\big[1 + \frac{d\,x^{-m}}{e}\big] - \\ &b\,n\,p^2\,Log[x]^3\,Log\big[d + e\,x^m\big] + \frac{b\,n\,p^2\,Log[x]^2\,Log\big[-\frac{e\,x^n}{d}\big]\,Log[d + e\,x^m\big]}{m} + \\ &2\,b\,n\,p\,Log[x]^2\,Log\big[f\,x^p\big]\,Log\big[d + e\,x^m\big] - \frac{2\,b\,n\,p\,Log[x]\,Log\big[-\frac{e\,x^m}{d}\big]\,Log[f\,x^p]\,Log[d + e\,x^m\big]}{m} - \\ &b\,n\,Log[x]\,Log\big[f\,x^p\big]^2\,Log\big[d + e\,x^m\big] + \frac{b\,n\,Log\big[-\frac{e\,x^m}{d}\big]\,Log[f\,x^p]^2\,Log[d + e\,x^m\big]}{m} + \\ &\frac{1}{3}\,b\,p^2\,Log[x]^3\,Log\big[c\,\left(d + e\,x^m\right)^n\big] - b\,p\,Log[x]^2\,Log\big[f\,x^p\big]\,Log\big[c\,\left(d + e\,x^m\right)^n\big] + \\ &b\,Log[x]\,Log\big[f\,x^p\big]^2\,Log\big[c\,\left(d + e\,x^m\right)^n\big] - \frac{b\,n\,p\,Log[x]\,\left(p\,Log[x] - 2\,Log[f\,x^p]\right)\,PolyLog\big[2,\,-\frac{d\,x^n}{e}\big]}{m} + \\ &\frac{b\,n\,\left(-p\,Log[x] + Log[f\,x^p]\right)^2\,PolyLog\big[2,\,1 + \frac{e\,x^m}{d}\big]}{m} + \\ &\frac{2\,b\,n\,p\,Log[f\,x^p]\,PolyLog\big[3,\,-\frac{d\,x^n}{e}\big]}{m^2} + \frac{2\,b\,n\,p^2\,PolyLog\big[4,\,-\frac{d\,x^n}{e}\big]}{m^3} \end{split}$$

#### Problem 623: Result more than twice size of optimal antiderivative.

$$\int \frac{\text{Log}\,[\,f\,x^p\,]\,\,\left(\,a\,+\,b\,\,\text{Log}\,\left[\,c\,\,\left(\,d\,+\,e\,\,x^m\,\right)^{\,n}\,\right]\,\right)}{x}\,\,\text{d}\,x$$

Optimal (type 4, 102 leaves, 4 steps):

$$\frac{\text{Log}\left[\text{f}\,x^{p}\right]^{2}\,\left(\text{a}+\text{b}\,\text{Log}\left[\text{c}\,\left(\text{d}+\text{e}\,x^{\text{m}}\right)^{n}\right]\right)}{2\,p}-\frac{\text{b}\,\text{n}\,\text{Log}\left[\text{f}\,x^{p}\right]^{2}\,\text{Log}\left[1+\frac{\text{e}\,x^{\text{m}}}{\text{d}}\right]}{2\,p}-\frac{\text{b}\,\text{n}\,\text{Log}\left[\text{f}\,x^{p}\right]^{2}\,\text{Log}\left[1+\frac{\text{e}\,x^{\text{m}}}{\text{d}}\right]}{2\,p}-\frac{\text{b}\,\text{n}\,\text{p}\,\text{PolyLog}\left[3,-\frac{\text{e}\,x^{\text{m}}}{\text{d}}\right]}{\text{m}^{2}}-\frac{\text{b}\,\text{n}\,\text{p}\,\text{PolyLog}\left[3,-\frac{\text{e}\,x^{\text{m}}}{\text{d}}\right]}{\text{m}^{2}}$$

Result (type 4, 265 leaves):

$$\begin{split} &-\frac{1}{6}\,b\,m\,n\,p\,Log\,[\,x\,]^{\,3}\,+\,\frac{a\,Log\,[\,f\,x^{p}\,]^{\,2}}{2\,p}\,-\,\frac{1}{2}\,b\,n\,p\,Log\,[\,x\,]^{\,2}\,Log\,[\,1\,+\,\frac{d\,x^{-m}}{e}\,]\,\,+\,b\,n\,p\,Log\,[\,x\,]^{\,2}\,Log\,[\,d\,+\,e\,x^{m}\,]\,\,-\,\\ &\frac{b\,n\,p\,Log\,[\,x\,]\,\,Log\,[\,-\,\frac{e\,x^{m}}{d}\,]\,\,Log\,[\,d\,+\,e\,x^{m}\,]}{m}\,\,-\,b\,n\,Log\,[\,x\,]\,\,Log\,[\,f\,x^{p}\,]\,\,Log\,[\,d\,+\,e\,x^{m}\,]\,\,+\,\\ &\frac{b\,n\,Log\,[\,-\,\frac{e\,x^{m}}{d}\,]\,\,Log\,[\,f\,x^{p}\,]\,\,Log\,[\,d\,+\,e\,x^{m}\,]}{m}\,\,-\,\frac{1}{2}\,b\,p\,Log\,[\,x\,]^{\,2}\,Log\,[\,c\,\,(\,d\,+\,e\,x^{m}\,)^{\,n}\,]\,\,+\,\\ &\frac{b\,n\,p\,Log\,[\,x\,]\,\,Log\,[\,f\,x^{p}\,]\,\,Log\,[\,c\,\,(\,d\,+\,e\,x^{m}\,)^{\,n}\,]\,\,+\,\frac{b\,n\,p\,Log\,[\,x\,]\,\,PolyLog\,[\,2\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m}\,\,-\,\\ &\frac{b\,n\,(\,p\,Log\,[\,x\,]\,\,-\,Log\,[\,f\,x^{p}\,]\,)\,\,PolyLog\,[\,2\,,\,\,1\,+\,\frac{e\,x^{m}}{d}\,]}{m}\,\,+\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^{-m}}{e}\,]}{m^{\,2}}\,\,-\,\frac{b\,n\,p\,PolyLog\,[\,3\,,\,\,-\,\frac{d\,x^$$

#### Problem 628: Unable to integrate problem.

$$\left\lceil Log \left[ c \left( d + e \left( f + g x \right)^{p} \right)^{q} \right] dx \right]$$

Optimal (type 5, 76 leaves, 3 steps):

$$-\frac{\text{e p q } \left(\text{f + g x}\right)^{\text{1+p}} \text{ Hypergeometric} 2\text{F1}\left[\text{1, 1} + \frac{1}{p}, \text{ 2} + \frac{1}{p}, -\frac{\text{e } (\text{f+g x})^{\text{p}}}{\text{d}}\right]}{\text{d g } \left(\text{1 + p}\right)}}{\text{f }} + \frac{\left(\text{f + g x}\right) \text{ Log}\left[\text{c } \left(\text{d + e } \left(\text{f + g x}\right)^{\text{p}}\right)^{\text{q}}\right]}{\text{g}}$$

Result (type 8, 18 leaves):

$$\int Log \left[ c \left( d + e \left( f + g x \right)^{p} \right)^{q} \right] dx$$

# Problem 636: Result more than twice size of optimal antiderivative.

$$\int \left( a + b \log \left[ c \left( d + \frac{e}{f + g x} \right)^{p} \right] \right)^{4} dx$$

Optimal (type 4, 221 leaves, 8 steps):

$$\frac{4 \, b \, e \, p \, Log \Big[ -\frac{e}{d \, (f+g \, x)} \Big] \, \left(a + b \, Log \Big[ c \, \left(d + \frac{e}{f+g \, x} \right)^p \Big] \right)^3}{d \, g} + \frac{\left(e + d \, \left(f + g \, x\right)\right) \, \left(a + b \, Log \Big[ c \, \left(d + \frac{e}{f+g \, x} \right)^p \Big] \right)^4}{d \, g} - \frac{12 \, b^2 \, e \, p^2 \, \left(a + b \, Log \Big[ c \, \left(d + \frac{e}{f+g \, x} \right)^p \Big] \right)^2 \, PolyLog \Big[ 2 \, , \, 1 + \frac{e}{d \, (f+g \, x)} \Big]}{d \, g} + \frac{24 \, b^3 \, e \, p^3 \, \left(a + b \, Log \Big[ c \, \left(d + \frac{e}{f+g \, x} \right)^p \Big] \right) \, PolyLog \Big[ 3 \, , \, 1 + \frac{e}{d \, (f+g \, x)} \Big]}{d \, g} - \frac{24 \, b^4 \, e \, p^4 \, PolyLog \Big[ 4 \, , \, 1 + \frac{e}{d \, (f+g \, x)} \Big]}{d \, g}$$

Result (type 4, 732 leaves):

$$\begin{split} &\frac{1}{d\,g}\left(-4\,b\,p\left(d\,f\,Log\,[f+g\,x]-\left(e+d\,f\right)\,Log\,[e+d\,f+d\,g\,x]-d\,g\,x\,Log\,\Big[\frac{e+d\,f+d\,g\,x}{f+g\,x}\Big]\right) \\ &\left(a-b\,p\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]+b\,Log\,\Big[c\,\left(d+\frac{e}{f+g\,x}\right)^p\Big]\right)^3+\\ &d\,g\,x\,\left(a-b\,p\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]+b\,Log\,\Big[c\,\left(d+\frac{e}{f+g\,x}\right)^p\Big]\right)^4+\\ &6\,b^2\,p^2\,\left(a-b\,p\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]+b\,Log\,\Big[c\,\left(d+\frac{e}{f+g\,x}\right)^p\Big]\right)^2+\\ &\left(d\,f\,Log\,\Big[\frac{f}{g}+x\Big]^2+\left(e+d\,f\right)\,Log\,\Big[\frac{e+d\,f+d\,g\,x}{d\,g}\Big]^2+d\,g\,x\,Log\,\Big[\frac{e+d\,f+d\,g\,x}{f+g\,x}\Big]^2-2\,\left(d\,f\,Log\,[f+g\,x]-e^{-2}\right)^p\Big]\right)^2-\\ &\left(e+d\,f\right)\,Log\,\Big[e+d\,f+d\,g\,x\Big]\right)\left(Log\,\Big[\frac{f}{g}+x\Big]-Log\,\Big[\frac{e+d\,f+d\,g\,x}{d\,g}\Big]+Log\,\Big[\frac{e+d\,f+d\,g\,x}{f+g\,x}\Big]\right)-\\ &2\,\left(e+d\,f\right)\,\left(Log\,\Big[\frac{f}{g}+x\Big]\,Log\,\Big[\frac{e+d\,f+d\,g\,x}{e}\Big]+PolyLog\,\Big[2,\,-\frac{d\,(f+g\,x)}{e}\Big]\right)-\\ &2\,d\,f\left(Log\,\Big[-\frac{d\,(f+g\,x)}{g}\Big]\,Log\,\Big[\frac{e+d\,f+d\,g\,x}{d\,g}\Big]+PolyLog\,\Big[2,\,-\frac{e+d\,f+d\,g\,x}{e}\Big]\right)\right)+\\ &4\,b^3\,p^3\,\Big[a-b\,p\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]+b\,Log\,\Big[c\,\Big(d+\frac{e}{f+g\,x}\Big)^p\Big]\right)\\ &\left(Log\,\Big[d+\frac{e}{f+g\,x}\Big]^2\Big[-3\,e\,Log\,\Big[-\frac{e}{d\,f+d\,g\,x}\Big]+\left(e+d\,f+d\,g\,x\right)\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]\right)-\\ &6\,e\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]\,PolyLog\,\Big[2,\,1+\frac{e}{d\,f+d\,g\,x}\Big]+6\,e\,PolyLog\,\Big[3,\,1+\frac{e}{d\,f+d\,g\,x}\Big]\right)-\\ &b^4\,p^4\,\Big(4\,e\,Log\,\Big[-\frac{e}{d\,f+d\,g\,x}\Big]\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]^3-e\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]^4-\\ &d\,(f+g\,x)\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]^4+12\,e\,Log\,\Big[d+\frac{e}{f+g\,x}\Big]^2\,PolyLog\,\Big[2,\,1+\frac{e}{d\,f+d\,g\,x}\Big]\Big)\Big) \end{split}$$

Problem 637: Result more than twice size of optimal antiderivative.

$$\int \left( a + b \, \text{Log} \left[ \, c \, \left( d + \frac{e}{f + g \, x} \right)^p \, \right] \, \right)^3 \, \text{d} \, x$$

Optimal (type 4, 168 leaves, 7 steps):

$$-\frac{3 \text{ be p Log} \left[-\frac{e}{d \text{ } (f+g \text{ } x)}\right] \left(a+b \text{ Log} \left[c \left(d+\frac{e}{f+g \text{ } x}\right)^p\right]\right)^2}{d \text{ } g} + \frac{\left(e+d \left(f+g \text{ } x\right)\right) \left(a+b \text{ Log} \left[c \left(d+\frac{e}{f+g \text{ } x}\right)^p\right]\right)^3}{d \text{ } g} - \frac{6 \text{ } b^2 \text{ } e \text{ } p^2 \left(a+b \text{ Log} \left[c \left(d+\frac{e}{f+g \text{ } x}\right)^p\right]\right) \text{ PolyLog} \left[2\text{, } 1+\frac{e}{d \text{ } (f+g \text{ } x)}\right]} + \frac{6 \text{ } b^3 \text{ } e \text{ } p^3 \text{ PolyLog} \left[3\text{, } 1+\frac{e}{d \text{ } (f+g \text{ } x)}\right]}{d \text{ } g}$$

Result (type 4, 441 leaves):

$$\begin{split} &\frac{1}{d\,g}\left(3\,b\,d\,p\,\left(f+g\,x\right)\,Log\Big[d+\frac{e}{f+g\,x}\Big]\,\left(a-b\,p\,Log\Big[d+\frac{e}{f+g\,x}\Big]+b\,Log\Big[c\,\left(d+\frac{e}{f+g\,x}\right)^{P}\Big]\right)^{2}+\\ &d\,\left(f+g\,x\right)\left(a-b\,p\,Log\Big[d+\frac{e}{f+g\,x}\Big]+b\,Log\Big[c\,\left(d+\frac{e}{f+g\,x}\right)^{P}\Big]\right)^{3}+\\ &3\,b\,e\,p\,\left(a-b\,p\,Log\Big[d+\frac{e}{f+g\,x}\Big]+b\,Log\Big[c\,\left(d+\frac{e}{f+g\,x}\right)^{P}\Big]\right)^{2}\,Log\Big[e+d\,\left(f+g\,x\right)\Big]+\\ &3\,b^{2}\,p^{2}\left(a-b\,p\,Log\Big[d+\frac{e}{f+g\,x}\Big]+b\,Log\Big[c\,\left(d+\frac{e}{f+g\,x}\right)^{P}\Big]\right)\left(d\,\left(f+g\,x\right)\,Log\Big[d+\frac{e}{f+g\,x}\Big]^{2}+\\ &e\,\left(Log\Big[\frac{e}{d}+f+g\,x\Big]^{2}+2\left(Log\,[f+g\,x]-Log\Big[\frac{e}{d}+f+g\,x\Big]+Log\Big[d+\frac{e}{f+g\,x}\Big]\right)Log\Big[\\ &e+d\,\left(f+g\,x\right)\Big]-2\left(Log\,[f+g\,x]\,Log\Big[1+\frac{d\,\left(f+g\,x\right)}{e}\Big]+PolyLog\Big[2,-\frac{d\,\left(f+g\,x\right)}{e}\Big]\right)\Big)\Big)+\\ &b^{3}\,p^{3}\left(Log\Big[d+\frac{e}{f+g\,x}\Big]^{2}\left(-3\,e\,Log\Big[-\frac{e}{d\,f+d\,g\,x}\Big]+\left(e+d\,f+d\,g\,x\right)Log\Big[d+\frac{e}{f+g\,x}\Big]\right)-\\ &6\,e\,Log\Big[d+\frac{e}{f+g\,x}\Big]PolyLog\Big[2,1+\frac{e}{d\,f+d\,g\,x}\Big]+6\,e\,PolyLog\Big[3,1+\frac{e}{d\,f+d\,g\,x}\Big]\Big)\Big) \end{split}$$

#### Problem 638: Result more than twice size of optimal antiderivative.

$$\int \left( a + b \, \text{Log} \left[ \, c \, \left( d + \frac{e}{f + g \, x} \right)^p \, \right] \, \right)^2 \, \text{d} \, x$$

Optimal (type 4, 115 leaves, 5 steps):

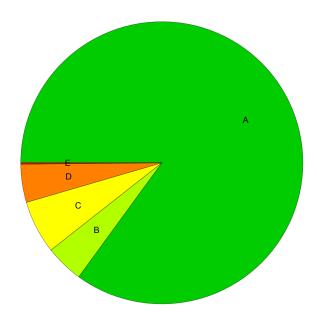
$$-\frac{2 \, b \, e \, p \, Log\left[-\frac{e}{d \, (f+g \, x)}\right] \, \left(a+b \, Log\left[c \, \left(d+\frac{e}{f+g \, x}\right)^p\right]\right)}{d \, g} + \\ -\frac{\left(e+d \, \left(f+g \, x\right)\right) \, \left(a+b \, Log\left[c \, \left(d+\frac{e}{f+g \, x}\right)^p\right]\right)^2}{d \, g} - \frac{2 \, b^2 \, e \, p^2 \, PolyLog\left[2, \, 1+\frac{e}{d \, (f+g \, x)}\right]}{d \, g}$$

Result (type 4, 250 leaves):

$$\begin{split} \frac{1}{d\,g} \left( d\, \left( f + g\, x \right) \, \left( a - b\, p\, Log \Big[ d + \frac{e}{f + g\, x} \Big] + b\, Log \Big[ c\, \left( d + \frac{e}{f + g\, x} \right)^p \Big] \right)^2 + \\ 2\, b\, p\, \left( a - b\, p\, Log \Big[ d + \frac{e}{f + g\, x} \Big] + b\, Log \Big[ c\, \left( d + \frac{e}{f + g\, x} \right)^p \Big] \right) \\ \left( d\, \left( f + g\, x \right) \, Log \Big[ d + \frac{e}{f + g\, x} \Big] + e\, Log \Big[ e + d\, \left( f + g\, x \right) \, \Big] \right) + b^2\, p^2 \left( d\, \left( f + g\, x \right) \, Log \Big[ d + \frac{e}{f + g\, x} \Big]^2 + e\, Log \Big[ e + d\, \left( f + g\, x \right) \, - Log \Big[ \frac{e}{d} + f + g\, x \Big] + Log \Big[ d + \frac{e}{f + g\, x} \Big] \right) \\ Log \Big[ e + d\, \left( f + g\, x \right) \, \Big] - 2\, \left( Log \big[ f + g\, x \big] \, Log \Big[ 1 + \frac{d\, \left( f + g\, x \right)}{e} \right] + PolyLog \Big[ 2, \, -\frac{d\, \left( f + g\, x \right)}{e} \Big] \right) \Big] \bigg) \bigg) \bigg) \end{split}$$

# **Summary of Integration Test Results**

#### 641 integration problems



- A 545 optimal antiderivatives
- B 28 more than twice size of optimal antiderivatives
- C 39 unnecessarily complex antiderivatives
- D 28 unable to integrate problems
- E 1 integration timeouts