

# Mathematica 11.3 Integration Test Results

Test results for the 653 problems in "4.1.1.2 (g cos)^p (a+b sin)^m.m"

Problem 8: Result more than twice size of optimal antiderivative.

$$\int \sec(c + dx) (a + a \sin(c + dx)) \, dx$$

Optimal (type 3, 17 leaves, 2 steps):

$$-\frac{a \log[1 - \sin(c + dx)]}{d}$$

Result (type 3, 83 leaves):

$$-\frac{a \log[\cos(c + dx)]}{d} - \frac{a \log[\cos(\frac{c}{2} + \frac{dx}{2})] - \sin(\frac{c}{2} + \frac{dx}{2})}{d} + \frac{a \log[\cos(\frac{c}{2} + \frac{dx}{2})] + \sin(\frac{c}{2} + \frac{dx}{2})}{d}$$

Problem 10: Result more than twice size of optimal antiderivative.

$$\int \sec(c + dx)^3 (a + a \sin(c + dx)) \, dx$$

Optimal (type 3, 39 leaves, 4 steps):

$$\frac{a \operatorname{ArcTanh}[\sin(c + dx)]}{2 d} + \frac{a^2}{2 d (a - a \sin(c + dx))}$$

Result (type 3, 143 leaves):

$$-\frac{a \log[\cos(\frac{1}{2} (c + dx)) - \sin(\frac{1}{2} (c + dx))]}{2 d} + \frac{a \log[\cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx))]}{2 d} + \frac{a \sec(c + dx)^2}{2 d} + \frac{4 d (\cos(\frac{1}{2} (c + dx)) - \sin(\frac{1}{2} (c + dx)))^2}{a} - \frac{4 d (\cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx)))^2}{a}$$

Problem 12: Result more than twice size of optimal antiderivative.

$$\int \sec(c + dx)^5 (a + a \sin(c + dx)) \, dx$$

Optimal (type 3, 84 leaves, 4 steps):

$$\frac{3 a \operatorname{ArcTanh}[\sin[c+d x]]}{8 d} + \frac{a^3}{8 d (a - a \sin[c+d x])^2} +$$

$$\frac{a^2}{4 d (a - a \sin[c+d x])} - \frac{a^2}{8 d (a + a \sin[c+d x])}$$

Result (type 3, 207 leaves):

$$-\frac{3 a \log[\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)]]}{8 d} +$$

$$\frac{3 a \log[\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)]]}{8 d} + \frac{a \sec[c+d x]^4}{4 d} +$$

$$\frac{16 d \left(\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)]\right)^4}{a} + \frac{3 a}{16 d \left(\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)]\right)^2} -$$

$$\frac{16 d \left(\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)]\right)^4}{16 d \left(\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)]\right)^2}$$

Problem 20: Result more than twice size of optimal antiderivative.

$$\int \sec[c+d x]^2 (a + a \sin[c+d x])^2 dx$$

Optimal (type 3, 38 leaves, 3 steps):

$$-a^2 x + \frac{2 a^4 \cos[c+d x]}{d (a^2 - a^2 \sin[c+d x])}$$

Result (type 3, 101 leaves):

$$-\left(\left(a^2 \left((c+d x) \cos[\frac{1}{2} (c+d x)] - (4+c+d x) \sin[\frac{1}{2} (c+d x)]\right) (1+\sin[c+d x])^2\right) \right. \\ \left. \left(d \left(\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)]\right) \left(\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)]\right)^4\right)\right)$$

Problem 25: Result more than twice size of optimal antiderivative.

$$\int \sec[c+d x]^7 (a + a \sin[c+d x])^2 dx$$

Optimal (type 3, 109 leaves, 4 steps):

$$\frac{a^2 \operatorname{ArcTanh}[\sin[c+d x]]}{4 d} + \frac{a^5}{12 d (a - a \sin[c+d x])^3} +$$

$$\frac{a^4}{8 d (a - a \sin[c+d x])^2} + \frac{3 a^3}{16 d (a - a \sin[c+d x])} - \frac{a^3}{16 d (a + a \sin[c+d x])}$$

Result (type 3, 290 leaves):

$$\begin{aligned}
& \left( \left( -3 - 12 \log[\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)]] \right) \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^2 + \right. \\
& \quad 12 \log[\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)]] \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^2 + \\
& \quad 4 \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^2 + \frac{6 \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^2}{\left( \cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)] \right)^4} + \\
& \quad \left. \left( \cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)] \right)^6 \right) \left( a + a \sin[c + d x] \right)^2 \Bigg) / \\
& \quad \left( 48 d \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^6 \right)
\end{aligned}$$

**Problem 32: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + d x] (a + a \sin[c + d x])^3 \, dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a + a \sin[c + d x])^4}{4 a d}$$

Result (type 3, 47 leaves):

$$\frac{1}{32 d} a^3 (-28 \cos[2 (c + d x)] + \cos[4 (c + d x)] + 56 \sin[c + d x] - 8 \sin[3 (c + d x)])$$

**Problem 35: Result more than twice size of optimal antiderivative.**

$$\int \sec[c + d x]^3 (a + a \sin[c + d x])^3 \, dx$$

Optimal (type 3, 40 leaves, 3 steps):

$$\frac{a^3 \log[1 - \sin[c + d x]]}{d} + \frac{2 a^4}{d (a - a \sin[c + d x])}$$

Result (type 3, 92 leaves):

$$\begin{aligned}
& - \left( \left( 2 a^3 \left( -1 - \log[\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)]] + \log[\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)]] \right. \right. \right. \\
& \quad \left. \left. \left. \sin[c + d x] \right) \right) \Big/ \left( d \left( \cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)] \right)^2 \right) \right)
\end{aligned}$$

**Problem 41: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^5 (a + a \sin[c + d x])^8 \, dx$$

Optimal (type 3, 67 leaves, 3 steps):

$$\frac{4 (a + a \sin[c + d x])^{11}}{11 a^3 d} - \frac{(a + a \sin[c + d x])^{12}}{3 a^4 d} + \frac{(a + a \sin[c + d x])^{13}}{13 a^5 d}$$

Result (type 3, 139 leaves):

$$-\frac{1}{1757184 d} a^8 (4434144 \cos[2 (c + d x)] + 815100 \cos[4 (c + d x)] - 354640 \cos[6 (c + d x)] - 92664 \cos[8 (c + d x)] + 20592 \cos[10 (c + d x)] - 572 \cos[12 (c + d x)] - 8314020 \sin[c + d x] + 877591 \sin[3 (c + d x)] + 872157 \sin[5 (c + d x)] + 6006 \sin[7 (c + d x)] - 58630 \sin[9 (c + d x)] + 4485 \sin[11 (c + d x)] - 33 \sin[13 (c + d x)])$$

Problem 43: Result more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^3 (a + a \sin[c + d x])^8 dx$$

Optimal (type 3, 45 leaves, 3 steps):

$$\frac{(a + a \sin[c + d x])^{10}}{5 a^2 d} - \frac{(a + a \sin[c + d x])^{11}}{11 a^3 d}$$

Result (type 3, 109 leaves):

$$\frac{1}{56320 d} a^8 (-284240 \cos[2 (c + d x)] + 25080 \cos[6 (c + d x)] - 3520 \cos[8 (c + d x)] + 88 \cos[10 (c + d x)] + 461890 \sin[c + d x] - 106590 \sin[3 (c + d x)] - 31977 \sin[5 (c + d x)] + 11495 \sin[7 (c + d x)] - 715 \sin[9 (c + d x)] + 5 \sin[11 (c + d x)])$$

Problem 45: Result more than twice size of optimal antiderivative.

$$\int \cos[c + d x] (a + a \sin[c + d x])^8 dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a + a \sin[c + d x])^9}{9 a d}$$

Result (type 3, 97 leaves):

$$\frac{1}{2304 d} a^8 (-31824 \cos[2 (c + d x)] + 8568 \cos[4 (c + d x)] - 816 \cos[6 (c + d x)] + 18 \cos[8 (c + d x)] + 43758 \sin[c + d x] - 18564 \sin[3 (c + d x)] + 3060 \sin[5 (c + d x)] - 153 \sin[7 (c + d x)] + \sin[9 (c + d x)])$$

### Problem 49: Result more than twice size of optimal antiderivative.

$$\int \sec(c + dx)^4 (a + a \sin(c + dx))^8 dx$$

Optimal (type 3, 179 leaves, 8 steps) :

$$\begin{aligned} & \frac{1155 a^8 x}{8} - \frac{385 a^8 \cos(c + dx)^3}{4 d} + \frac{1155 a^8 \cos(c + dx) \sin(c + dx)}{8 d} + \frac{2 a^{15} \cos(c + dx)^{11}}{3 d (a - a \sin(c + dx))^7} - \\ & \frac{22 a^{13} \cos(c + dx)^9}{3 d (a - a \sin(c + dx))^5} - \frac{66 a^{14} \cos(c + dx)^7}{d (a^2 - a^2 \sin(c + dx))^3} - \frac{231 a^{16} \cos(c + dx)^5}{4 d (a^8 - a^8 \sin(c + dx))} \end{aligned}$$

Result (type 3, 465 leaves) :

$$\begin{aligned} & \frac{1155 (c + dx) (a + a \sin(c + dx))^8}{8 d (\cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx)))^{16}} - \frac{78 \cos(c + dx) (a + a \sin(c + dx))^8}{d (\cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx)))^{16}} + \\ & \frac{2 \cos(3 (c + dx)) (a + a \sin(c + dx))^8}{3 d (\cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx)))^{16}} + \left( 64 (a + a \sin(c + dx))^8 \right) / \\ & \left( 3 d \left( \cos(\frac{1}{2} (c + dx)) - \sin(\frac{1}{2} (c + dx)) \right)^2 \left( \cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx)) \right)^{16} \right) + \\ & \left( 128 \sin(\frac{1}{2} (c + dx)) (a + a \sin(c + dx))^8 \right) / \\ & \left( 3 d \left( \cos(\frac{1}{2} (c + dx)) - \sin(\frac{1}{2} (c + dx)) \right)^3 \left( \cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx)) \right)^{16} \right) - \\ & \left( 1024 \sin(\frac{1}{2} (c + dx)) (a + a \sin(c + dx))^8 \right) / \\ & \left( 3 d \left( \cos(\frac{1}{2} (c + dx)) - \sin(\frac{1}{2} (c + dx)) \right) \left( \cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx)) \right)^{16} \right) - \\ & \frac{31 (a + a \sin(c + dx))^8 \sin(2 (c + dx))}{4 d (\cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx)))^{16}} + \frac{(a + a \sin(c + dx))^8 \sin(4 (c + dx))}{32 d (\cos(\frac{1}{2} (c + dx)) + \sin(\frac{1}{2} (c + dx)))^{16}} \end{aligned}$$

### Problem 50: Result more than twice size of optimal antiderivative.

$$\int \sec(c + dx)^5 (a + a \sin(c + dx))^8 dx$$

Optimal (type 3, 110 leaves, 3 steps) :

$$\begin{aligned} & - \frac{80 a^8 \log[1 - \sin(c + dx)]}{d} - \frac{31 a^8 \sin(c + dx)}{d} - \frac{4 a^8 \sin(c + dx)^2}{d} - \\ & \frac{a^8 \sin(c + dx)^3}{3 d} + \frac{16 a^{10}}{d (a - a \sin(c + dx))^2} - \frac{80 a^9}{d (a - a \sin(c + dx))} \end{aligned}$$

Result (type 3, 341 leaves) :

$$\begin{aligned}
& \frac{2 \cos[2(c+d x)] (a+a \sin[c+d x])^8}{d (\cos[\frac{1}{2}(c+d x)] + \sin[\frac{1}{2}(c+d x)])^{16}} - \\
& \frac{160 \log[\cos[\frac{1}{2}(c+d x)] - \sin[\frac{1}{2}(c+d x)]] (a+a \sin[c+d x])^8}{d (\cos[\frac{1}{2}(c+d x)] + \sin[\frac{1}{2}(c+d x)])^{16}} + \left( 16 (a+a \sin[c+d x])^8 \right) / \\
& \left( d \left( \cos[\frac{1}{2}(c+d x)] - \sin[\frac{1}{2}(c+d x)] \right)^4 \left( \cos[\frac{1}{2}(c+d x)] + \sin[\frac{1}{2}(c+d x)] \right)^{16} \right) - \\
& \left( 80 (a+a \sin[c+d x])^8 \right) / \\
& \left( d \left( \cos[\frac{1}{2}(c+d x)] - \sin[\frac{1}{2}(c+d x)] \right)^2 \left( \cos[\frac{1}{2}(c+d x)] + \sin[\frac{1}{2}(c+d x)] \right)^{16} \right) - \\
& \frac{125 \sin[c+d x] (a+a \sin[c+d x])^8}{4 d (\cos[\frac{1}{2}(c+d x)] + \sin[\frac{1}{2}(c+d x)])^{16}} + \frac{(a+a \sin[c+d x])^8 \sin[3(c+d x)]}{12 d (\cos[\frac{1}{2}(c+d x)] + \sin[\frac{1}{2}(c+d x)])^{16}}
\end{aligned}$$

**Problem 57: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+d x]}{a+a \sin[c+d x]} \, dx$$

Optimal (type 3, 37 leaves, 4 steps):

$$\frac{\text{ArcTanh}[\sin[c+d x]]}{2 a d} - \frac{1}{2 d (a+a \sin[c+d x])}$$

Result (type 3, 126 leaves):

$$\begin{aligned}
& \left( -1 - \log[\cos[\frac{1}{2}(c+d x)] - \sin[\frac{1}{2}(c+d x)]] + \log[\cos[\frac{1}{2}(c+d x)] + \sin[\frac{1}{2}(c+d x)]] + \right. \\
& \left( -\log[\cos[\frac{1}{2}(c+d x)] - \sin[\frac{1}{2}(c+d x)]] + \log[\cos[\frac{1}{2}(c+d x)] + \sin[\frac{1}{2}(c+d x)]] \right) \\
& \left. \sin[c+d x] \right) / (2 a d (1 + \sin[c+d x]))
\end{aligned}$$

**Problem 58: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+d x]^2}{a+a \sin[c+d x]} \, dx$$

Optimal (type 3, 42 leaves, 3 steps):

$$-\frac{\sec[c+d x]}{3 d (a+a \sin[c+d x])} + \frac{2 \tan[c+d x]}{3 a d}$$

Result (type 3, 103 leaves):

$$\left( 2 \cos[c + dx] - 4 \cos[2(c + dx)] + 8 \sin[c + dx] + \sin[2(c + dx)] \right) / \\ \left( 12 a d \left( \cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right) \right. \\ \left. \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right) (1 + \sin[c + dx]) \right)$$

**Problem 59: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^3}{a + a \sin[c + dx]} dx$$

Optimal (type 3, 77 leaves, 4 steps):

$$\frac{3 \operatorname{ArcTanh}[\sin[c + dx]]}{8 a d} + \frac{1}{8 d (a - a \sin[c + dx])} - \frac{a}{8 d (a + a \sin[c + dx])^2} - \frac{1}{4 d (a + a \sin[c + dx])}$$

Result (type 3, 190 leaves):

$$- \left( \left( 2 + \frac{1}{\left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2} + \right. \right. \\ \left. \left. 3 \log\left[ \cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right] \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2 - \right. \\ \left. 3 \log\left[ \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right] \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2 - \right. \\ \left. \left. \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2 \right) / (8 d (a + a \sin[c + dx])) \right)$$

**Problem 61: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^5}{a + a \sin[c + dx]} dx$$

Optimal (type 3, 120 leaves, 4 steps):

$$\frac{5 \operatorname{ArcTanh}[\sin[c + dx]]}{16 a d} + \frac{a}{32 d (a - a \sin[c + dx])^2} + \frac{1}{8 d (a - a \sin[c + dx])} - \\ \frac{a^2}{24 d (a + a \sin[c + dx])^3} - \frac{3 a}{32 d (a + a \sin[c + dx])^2} - \frac{3}{16 d (a + a \sin[c + dx])}$$

Result (type 3, 267 leaves):

$$\frac{1}{96 d (a + a \sin[c + d x])} \left( -18 - \frac{4}{\left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^4} - \frac{9}{\left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2} - \right. \\ \left. 30 \log[\cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right]] \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2 + \right. \\ \left. 30 \log[\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]] \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2 + \right. \\ \left. \frac{3 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2}{\left( \cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right] \right)^4} + \frac{12 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2}{\left( \cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right] \right)^2} \right)$$

Problem 68: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^2}{(a + a \sin[c + d x])^2} dx$$

Optimal (type 3, 34 leaves, 2 steps):

$$-\frac{x}{a^2} - \frac{2 \cos[c + d x]}{d (a^2 + a^2 \sin[c + d x])}$$

Result (type 3, 75 leaves):

$$-\left( \left( \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^3 \right. \right. \\ \left. \left. \left( (c + d x) \cos\left[\frac{1}{2} (c + d x)\right] + (-4 + c + d x) \sin\left[\frac{1}{2} (c + d x)\right] \right) \right) \right) \Big/ \left( a^2 d (1 + \sin[c + d x])^2 \right)$$

Problem 70: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec[c + d x]}{(a + a \sin[c + d x])^2} dx$$

Optimal (type 3, 60 leaves, 4 steps):

$$\frac{\text{ArcTanh}[\sin[c + d x]]}{4 a^2 d} - \frac{1}{4 d (a + a \sin[c + d x])^2} - \frac{1}{4 d (a^2 + a^2 \sin[c + d x])}$$

Result (type 3, 139 leaves):

$$\begin{aligned}
& - \left( \left( 1 + \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 + \right. \right. \\
& \quad \left. \left. \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 - \right. \\
& \quad \left. \left. \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right) \right) / (4 \\
& \quad d (a + a \sin [c + d x])^2 \Big)
\end{aligned}$$

**Problem 72: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^3}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 3, 104 leaves, 4 steps):

$$\begin{aligned}
& \frac{\operatorname{ArcTanh}[\sin [c + d x]]}{4 a^2 d} - \frac{a}{12 d (a + a \sin [c + d x])^3} - \\
& \frac{1}{8 d (a + a \sin [c + d x])^2} + \frac{1}{16 d (a^2 - a^2 \sin [c + d x])} - \frac{3}{16 d (a^2 + a^2 \sin [c + d x])}
\end{aligned}$$

Result (type 3, 217 leaves):

$$\begin{aligned}
& - \left( \left( 6 + \frac{4}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + 9 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 + \right. \right. \\
& \quad 12 \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 - \\
& \quad 12 \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 - \\
& \quad \left. \left. \frac{3 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} \right) \right) / (48 d (a + a \sin [c + d x])^2)
\end{aligned}$$

**Problem 76: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^7}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 3, 23 leaves, 2 steps):

$$-\frac{(a - a \sin [c + d x])^4}{4 a^7 d}$$

Result (type 3, 48 leaves):

$$-\frac{1}{32 a^3 d} (-28 \cos [2 (c + d x)] + \cos [4 (c + d x)] + 8 (-7 \sin [c + d x] + \sin [3 (c + d x)]))$$

### Problem 80: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx]^3}{(a + a \sin[c + dx])^3} dx$$

Optimal (type 3, 39 leaves, 3 steps):

$$-\frac{\log[1 + \sin[c + dx]]}{a^3 d} - \frac{2}{d (a^3 + a^3 \sin[c + dx])}$$

Result (type 3, 89 leaves):

$$\begin{aligned} & \left( 2 \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right)^4 \right. \\ & \left. \left( -1 - \log \left[ \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right] \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right)^2 \right) \right) / (d \\ & (a + a \sin[c + dx])^3) \end{aligned}$$

### Problem 81: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx]^2}{(a + a \sin[c + dx])^3} dx$$

Optimal (type 3, 27 leaves, 1 step):

$$-\frac{\cos[c + dx]^3}{3 d (a + a \sin[c + dx])^3}$$

Result (type 3, 66 leaves):

$$\begin{aligned} & \left( \left( -3 \cos \left[ \frac{1}{2} (c + dx) \right] + \cos \left[ \frac{3}{2} (c + dx) \right] \right) \left( \cos \left[ \frac{1}{2} (c + dx) \right] + \sin \left[ \frac{1}{2} (c + dx) \right] \right)^3 \right) / \\ & (3 a^3 d (1 + \sin[c + dx])^3) \end{aligned}$$

### Problem 83: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec[c + dx]}{(a + a \sin[c + dx])^3} dx$$

Optimal (type 3, 82 leaves, 4 steps):

$$\begin{aligned} & \frac{\text{ArcTanh}[\sin[c + dx]]}{8 a^3 d} - \frac{1}{6 d (a + a \sin[c + dx])^3} - \\ & \frac{1}{8 a d (a + a \sin[c + dx])^2} - \frac{1}{8 d (a^3 + a^3 \sin[c + dx])} \end{aligned}$$

Result (type 3, 167 leaves):

$$\begin{aligned}
& - \left( \left( 4 + 3 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 + 3 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 + \right. \right. \\
& \quad 3 \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^6 - \\
& \quad \left. \left. 3 \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^6 \right) \right) / \\
& \quad \left( 24 d (a + a \sin [c + d x])^3 \right)
\end{aligned}$$

**Problem 88: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^8}{(a + a \sin [c + d x])^8} dx$$

Optimal (type 3, 127 leaves, 5 steps):

$$\begin{aligned}
& \frac{x}{a^8} - \frac{2 \cos [c + d x]^7}{7 a d (a + a \sin [c + d x])^7} + \frac{2 \cos [c + d x]^5}{5 a^3 d (a + a \sin [c + d x])^5} - \\
& \quad \frac{2 \cos [c + d x]^3}{3 a^2 d (a^2 + a^2 \sin [c + d x])^3} + \frac{2 \cos [c + d x]}{d (a^8 + a^8 \sin [c + d x])}
\end{aligned}$$

Result (type 3, 263 leaves):

$$\begin{aligned}
& \frac{1}{105 d (a + a \sin [c + d x])^8} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^9 \\
& \quad \left( 480 \sin \left[ \frac{1}{2} (c + d x) \right] - 240 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right. - \\
& \quad 1056 \sin \left[ \frac{1}{2} (c + d x) \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 + \\
& \quad 528 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 + 976 \sin \left[ \frac{1}{2} (c + d x) \right] \\
& \quad \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 - 488 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5 - \\
& \quad 704 \sin \left[ \frac{1}{2} (c + d x) \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^6 + \\
& \quad \left. 105 (c + d x) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^7 \right)
\end{aligned}$$

**Problem 90: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^6}{(a + a \sin [c + d x])^8} dx$$

Optimal (type 3, 58 leaves, 2 steps):

$$- \frac{\cos [c + d x]^7}{9 d (a + a \sin [c + d x])^8} - \frac{\cos [c + d x]^7}{63 a d (a + a \sin [c + d x])^7}$$

Result (type 3, 128 leaves):

$$-\left(\left(315 \cos\left[\frac{1}{2} (c+d x)\right] - 189 \cos\left[\frac{3}{2} (c+d x)\right] - 63 \cos\left[\frac{5}{2} (c+d x)\right] + 9 \cos\left[\frac{7}{2} (c+d x)\right] - 189 \sin\left[\frac{1}{2} (c+d x)\right] - 105 \sin\left[\frac{3}{2} (c+d x)\right] + 27 \sin\left[\frac{5}{2} (c+d x)\right] + \sin\left[\frac{9}{2} (c+d x)\right]\right)\right. \\ \left.\left(504 a^8 d \left(\cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right]\right)^9\right)\right)$$

Problem 101: Result more than twice size of optimal antiderivative.

$$\int \cos[c+d x]^7 \sqrt{a+a \sin[c+d x]} \, dx$$

Optimal (type 3, 97 leaves, 3 steps):

$$\frac{16 (a+a \sin[c+d x])^{9/2}}{9 a^4 d} - \frac{24 (a+a \sin[c+d x])^{11/2}}{11 a^5 d} + \\ \frac{12 (a+a \sin[c+d x])^{13/2}}{13 a^6 d} - \frac{2 (a+a \sin[c+d x])^{15/2}}{15 a^7 d}$$

Result (type 3, 1137 leaves):

$$\frac{35 \cos\left[\frac{d x}{2}\right] \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \sqrt{a (1 + \sin[c+d x])}}{64 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} - \\ \frac{35 \cos\left[\frac{3 d x}{2}\right] \left(\cos\left[\frac{3 c}{2}\right] - \sin\left[\frac{3 c}{2}\right]\right) \sqrt{a (1 + \sin[c+d x])}}{192 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\ \frac{21 \cos\left[\frac{5 d x}{2}\right] \left(\cos\left[\frac{5 c}{2}\right] + \sin\left[\frac{5 c}{2}\right]\right) \sqrt{a (1 + \sin[c+d x])}}{320 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} - \\ \frac{3 \cos\left[\frac{7 d x}{2}\right] \left(\cos\left[\frac{7 c}{2}\right] - \sin\left[\frac{7 c}{2}\right]\right) \sqrt{a (1 + \sin[c+d x])}}{64 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\ \frac{7 \cos\left[\frac{9 d x}{2}\right] \left(\cos\left[\frac{9 c}{2}\right] + \sin\left[\frac{9 c}{2}\right]\right) \sqrt{a (1 + \sin[c+d x])}}{576 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} - \\ \frac{7 \cos\left[\frac{11 d x}{2}\right] \left(\cos\left[\frac{11 c}{2}\right] - \sin\left[\frac{11 c}{2}\right]\right) \sqrt{a (1 + \sin[c+d x])}}{704 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\ \frac{\cos\left[\frac{13 d x}{2}\right] \left(\cos\left[\frac{13 c}{2}\right] + \sin\left[\frac{13 c}{2}\right]\right) \sqrt{a (1 + \sin[c+d x])}}{832 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)}$$

$$\begin{aligned}
& \frac{\cos\left[\frac{15d x}{2}\right] \left(\cos\left[\frac{15c}{2}\right] - \sin\left[\frac{15c}{2}\right]\right) \sqrt{a (1 + \sin[c + d x])}}{960 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{35 \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \sin\left[\frac{d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{64 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{35 \left(\cos\left[\frac{3c}{2}\right] + \sin\left[\frac{3c}{2}\right]\right) \sin\left[\frac{3d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{192 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{21 \left(\cos\left[\frac{5c}{2}\right] - \sin\left[\frac{5c}{2}\right]\right) \sin\left[\frac{5d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{320 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{3 \left(\cos\left[\frac{7c}{2}\right] + \sin\left[\frac{7c}{2}\right]\right) \sin\left[\frac{7d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{64 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{7 \left(\cos\left[\frac{9c}{2}\right] - \sin\left[\frac{9c}{2}\right]\right) \sin\left[\frac{9d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{576 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{7 \left(\cos\left[\frac{11c}{2}\right] + \sin\left[\frac{11c}{2}\right]\right) \sin\left[\frac{11d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{704 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{\left(\cos\left[\frac{13c}{2}\right] - \sin\left[\frac{13c}{2}\right]\right) \sin\left[\frac{13d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{832 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{\left(\cos\left[\frac{15c}{2}\right] + \sin\left[\frac{15c}{2}\right]\right) \sin\left[\frac{15d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{960 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)}
\end{aligned}$$

Problem 102: Result more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^6 \sqrt{a + a \sin[c + d x]} \, dx$$

Optimal (type 3, 127 leaves, 4 steps):

$$\begin{aligned}
& -\frac{256 a^4 \cos[c + d x]^7}{3003 d \left(a + a \sin[c + d x]\right)^{7/2}} - \frac{64 a^3 \cos[c + d x]^7}{429 d \left(a + a \sin[c + d x]\right)^{5/2}} - \\
& \frac{24 a^2 \cos[c + d x]^7}{143 d \left(a + a \sin[c + d x]\right)^{3/2}} - \frac{2 a \cos[c + d x]^7}{13 d \sqrt{a + a \sin[c + d x]}}
\end{aligned}$$

Result (type 3, 995 leaves):

$$\begin{aligned}
& - \frac{5 \cos\left[\frac{d x}{2}\right] \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \sqrt{a (1 + \sin[c + d x])}}{8 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{5 \cos\left[\frac{3 d x}{2}\right] \left(\cos\left[\frac{3 c}{2}\right] + \sin\left[\frac{3 c}{2}\right]\right) \sqrt{a (1 + \sin[c + d x])}}{32 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} - \\
& \frac{3 \cos\left[\frac{5 d x}{2}\right] \left(\cos\left[\frac{5 c}{2}\right] - \sin\left[\frac{5 c}{2}\right]\right) \sqrt{a (1 + \sin[c + d x])}}{32 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{3 \cos\left[\frac{7 d x}{2}\right] \left(\cos\left[\frac{7 c}{2}\right] + \sin\left[\frac{7 c}{2}\right]\right) \sqrt{a (1 + \sin[c + d x])}}{112 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} - \\
& \frac{\cos\left[\frac{9 d x}{2}\right] \left(\cos\left[\frac{9 c}{2}\right] - \sin\left[\frac{9 c}{2}\right]\right) \sqrt{a (1 + \sin[c + d x])}}{48 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{\cos\left[\frac{11 d x}{2}\right] \left(\cos\left[\frac{11 c}{2}\right] + \sin\left[\frac{11 c}{2}\right]\right) \sqrt{a (1 + \sin[c + d x])}}{352 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} - \\
& \frac{\cos\left[\frac{13 d x}{2}\right] \left(\cos\left[\frac{13 c}{2}\right] - \sin\left[\frac{13 c}{2}\right]\right) \sqrt{a (1 + \sin[c + d x])}}{416 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{5 \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \sin\left[\frac{d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{8 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{5 \left(\cos\left[\frac{3 c}{2}\right] - \sin\left[\frac{3 c}{2}\right]\right) \sin\left[\frac{3 d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{32 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{3 \left(\cos\left[\frac{5 c}{2}\right] + \sin\left[\frac{5 c}{2}\right]\right) \sin\left[\frac{5 d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{32 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{3 \left(\cos\left[\frac{7 c}{2}\right] - \sin\left[\frac{7 c}{2}\right]\right) \sin\left[\frac{7 d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{112 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{\left(\cos\left[\frac{9 c}{2}\right] + \sin\left[\frac{9 c}{2}\right]\right) \sin\left[\frac{9 d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{48 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} + \\
& \frac{\left(\cos\left[\frac{11 c}{2}\right] - \sin\left[\frac{11 c}{2}\right]\right) \sin\left[\frac{11 d x}{2}\right] \sqrt{a (1 + \sin[c + d x])}}{352 d \left(\cos\left[\frac{c}{2} + \frac{d x}{2}\right] + \sin\left[\frac{c}{2} + \frac{d x}{2}\right]\right)} +
\end{aligned}$$

$$\frac{\left(\cos\left[\frac{13c}{2}\right] + \sin\left[\frac{13c}{2}\right]\right) \sin\left[\frac{13dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{416d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)}$$

**Problem 108:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec[c + dx] \sqrt{a + a \sin[c + dx]} \, dx$$

Optimal (type 3, 40 leaves, 3 steps):

$$\frac{\sqrt{2} \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{d}$$

Result (type 3, 95 leaves):

$$-\left(\left(\left(2-2 \frac{i}{d}\right) (-1)^{1/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{3/4} \sec \left[\frac{d x}{4}\right]\left(\cos \left[\frac{1}{4} (2 c+d x)\right]+\sin \left[\frac{1}{4} (2 c+d x)\right]\right)\right]\right.\right. \\ \left.\left.\sqrt{a(1+\sin[c+dx])}\right)\right) \bigg/ \left(d\left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)\right)$$

**Problem 109:** Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c + dx]^2 \sqrt{a + a \sin[c + dx]} \, dx$$

Optimal (type 3, 72 leaves, 3 steps):

$$-\frac{\sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{\sqrt{2} d}+\frac{\sec [c+d x] \sqrt{a+a \sin [c+d x]}}{d}$$

Result (type 3, 106 leaves):

$$\frac{1}{d} \sec [c+d x] \\ \left(1-\left(1+\frac{i}{d}\right) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{3/4} \sec \left[\frac{d x}{4}\right]\left(\cos \left[\frac{1}{4} (2 c+d x)\right]-\sin \left[\frac{1}{4} (2 c+d x)\right]\right)\right]\right. \\ \left.\left(\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]\right)\right) \sqrt{a(1+\sin[c+dx])}$$

**Problem 110:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^3 \sqrt{a + a \sin[c + dx]} \, dx$$

Optimal (type 3, 95 leaves, 5 steps):

$$\frac{3 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{4 \sqrt{2} d}-\frac{3 a}{4 d \sqrt{a+a \sin[c+d x]}}+\frac{\operatorname{Sec}[c+d x]^2 \sqrt{a+a \sin[c+d x]}}{2 d}$$

Result (type 3, 271 leaves):

$$\left( \left( -2 - (3 - 3 \frac{i}{2}) (-1)^{1/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \operatorname{Sec}\left[\frac{d x}{4}\right]\right] \right. \right. \\ \left. \left. \left( \cos\left[\frac{1}{4} (2c + dx)\right] + \sin\left[\frac{1}{4} (2c + dx)\right] \right) \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right) + \right. \right. \\ \left. \left. \frac{2 \sin\left[\frac{d x}{2}\right] \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right)}{\left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2} (c + dx)\right] - \sin\left[\frac{1}{2} (c + dx)\right] \right)^2} + \right. \right. \\ \left. \left. \frac{\left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right)}{\left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2} (c + dx)\right] - \sin\left[\frac{1}{2} (c + dx)\right] \right)} \right) \right. \\ \left. \left. \sqrt{a (1 + \sin[c + dx])} \right) \right/ \left( 4 d \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right)^2 \right)$$

Problem 111: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^4 \sqrt{a+a \sin[c+d x]} \, dx$$

Optimal (type 3, 137 leaves, 5 steps):

$$\left. -\frac{5 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+d x]}{\sqrt{2} \sqrt{a+a \sin[c+d x]}\right]}{8 \sqrt{2} d} -\frac{5 a^2 \cos[c+d x]}{8 d (a+a \sin[c+d x])^{3/2}} + \right. \\ \left. \frac{5 a \operatorname{Sec}[c+d x]}{6 d \sqrt{a+a \sin[c+d x]}} + \frac{\operatorname{Sec}[c+d x]^3 \sqrt{a+a \sin[c+d x]}}{3 d} \right)$$

Result (type 3, 302 leaves):

$$\begin{aligned}
 & \left( \left( \frac{6 \sin\left[\frac{d x}{2}\right]}{\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]} - \frac{3 \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)}{\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]} - (15 + 15 i) \right. \right. \\
 & \quad \left( -1 \right)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \sec\left[\frac{d x}{4}\right] \left(\cos\left[\frac{1}{4} (2 c + d x)\right] - \sin\left[\frac{1}{4} (2 c + d x)\right]\right) \right] \\
 & \quad \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2 + \frac{4 \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^2}{\left(\cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right]\right)^3} + \\
 & \quad \left. \left. \frac{12 \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^2}{\cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right]} \right) \sqrt{a (1 + \sin[c + d x])} \right) / \\
 & \quad \left( 24 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^3 \right)
 \end{aligned}$$

Problem 112: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c + d x]^5 \sqrt{a + a \sin[c + d x]} \, dx$$

Optimal (type 3, 149 leaves, 7 steps):

$$\begin{aligned}
 & \frac{35 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{64 \sqrt{2} d} - \frac{35 a^2}{96 d \left(a + a \sin[c + d x]\right)^{3/2}} - \\
 & \frac{35 a}{64 d \sqrt{a + a \sin[c + d x]}} + \frac{7 a \sec[c + d x]^2}{16 d \sqrt{a + a \sin[c + d x]}} + \frac{\sec[c + d x]^4 \sqrt{a + a \sin[c + d x]}}{4 d}
 \end{aligned}$$

Result (type 3, 179 leaves):

$$\begin{aligned}
 & \left( \sqrt{a (1 + \sin[c + d x])} \left( (-420 + 420 i) (-1)^{1/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \sec\left[\frac{d x}{4}\right]\right] \right. \right. \\
 & \quad \left( \cos\left[\frac{1}{4} (2 c + d x)\right] + \sin\left[\frac{1}{4} (2 c + d x)\right] \right) \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^3 + \\
 & \quad \left. \left. (-102 - 70 \cos[2 (c + d x)] + 329 \sin[c + d x] + 105 \sin[3 (c + d x)]) \right) \right. \\
 & \quad \left( \cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right] \right)^4 \Big) / \\
 & \quad \left( 768 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^4 \right)
 \end{aligned}$$

Problem 113: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c + d x]^6 \sqrt{a + a \sin[c + d x]} \, dx$$

Optimal (type 3, 197 leaves, 7 steps):

$$\begin{aligned}
& -\frac{63 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{128 \sqrt{2} d} -\frac{63 a^2 \cos [c+d x]}{128 d (a+a \sin [c+d x])^{3/2}}-\frac{21 a^2 \sec [c+d x]}{80 d (a+a \sin [c+d x])^{3/2}}+ \\
& \frac{21 a \sec [c+d x]}{32 d \sqrt{a+a \sin [c+d x]}}+\frac{3 a \sec [c+d x]^3}{10 d \sqrt{a+a \sin [c+d x]}}+\frac{\sec [c+d x]^5 \sqrt{a+a \sin [c+d x]}}{5 d}
\end{aligned}$$

Result (type 3, 191 leaves):

$$\begin{aligned}
& \left(\sqrt{a(1+\sin[c+d x])}\left((-2520-2520 i)(-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right)(-1)^{3/4} \sec \left[\frac{d x}{4}\right]\right.\right.\right. \\
& \left.\left.\left.\left(\cos \left[\frac{1}{4}(2 c+d x)\right]-\sin \left[\frac{1}{4}(2 c+d x)\right]\right]\right)\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4+\right. \\
& \left.\left.\left.\left(649+1092 \cos [2(c+d x)]+315 \cos [4(c+d x)]+1572 \sin [c+d x]+420 \sin [3(c+d x)]\right)\right)\right.\right. \\
& \left.\left.\left.\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^5\right)\right) / \\
& \left(5120 d\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^5\right)
\end{aligned}$$

Problem 114: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^7 (a+a \sin [c+d x])^{3/2} d x$$

Optimal (type 3, 97 leaves, 3 steps):

$$\begin{aligned}
& \frac{16 (a+a \sin [c+d x])^{11/2}}{11 a^4 d}-\frac{24 (a+a \sin [c+d x])^{13/2}}{13 a^5 d}+ \\
& \frac{4 (a+a \sin [c+d x])^{15/2}}{5 a^6 d}-\frac{2 (a+a \sin [c+d x])^{17/2}}{17 a^7 d}
\end{aligned}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
& \frac{35 \cos\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{64 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{7 \cos\left[\frac{3}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{32 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
& \frac{7 \cos\left[\frac{5}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{160 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{\cos\left[\frac{7}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \\
& \frac{5 \cos\left[\frac{11}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{352 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{\cos\left[\frac{13}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{416 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \\
& \frac{\cos\left[\frac{15}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{640 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{\cos\left[\frac{17}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{2176 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
& \frac{35 \sin\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{64 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{7 (a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{3}{2}(c+dx)\right]}{32 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
& \frac{7 (a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{5}{2}(c+dx)\right]}{160 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{(a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{7}{2}(c+dx)\right]}{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
& \frac{5 (a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{11}{2}(c+dx)\right]}{352 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{(a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{13}{2}(c+dx)\right]}{416 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
& \frac{(a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{15}{2}(c+dx)\right]}{640 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{(a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{17}{2}(c+dx)\right]}{2176 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3}
\end{aligned}$$

Problem 115: Result more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^6 (a + a \sin[c+dx])^{3/2} dx$$

Optimal (type 3, 159 leaves, 5 steps):

$$\begin{aligned}
& - \frac{4096 a^5 \cos[c+dx]^7}{45045 d (a + a \sin[c+dx])^{7/2}} - \frac{1024 a^4 \cos[c+dx]^7}{6435 d (a + a \sin[c+dx])^{5/2}} - \\
& \frac{128 a^3 \cos[c+dx]^7}{715 d (a + a \sin[c+dx])^{3/2}} - \frac{32 a^2 \cos[c+dx]^7}{195 d \sqrt{a + a \sin[c+dx]}} - \frac{2 a \cos[c+dx]^7 \sqrt{a + a \sin[c+dx]}}{15 d}
\end{aligned}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
& -\frac{45 \cos\left[\frac{1}{2}(c+d x)\right] (a (1+\sin[c+d x]))^{3/2}}{64 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} + \frac{25 \cos\left[\frac{3}{2}(c+d x)\right] (a (1+\sin[c+d x]))^{3/2}}{192 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} - \\
& \frac{39 \cos\left[\frac{5}{2}(c+d x)\right] (a (1+\sin[c+d x]))^{3/2}}{320 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} + \frac{3 \cos\left[\frac{7}{2}(c+d x)\right] (a (1+\sin[c+d x]))^{3/2}}{448 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} - \\
& \frac{17 \cos\left[\frac{9}{2}(c+d x)\right] (a (1+\sin[c+d x]))^{3/2}}{576 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} - \frac{3 \cos\left[\frac{11}{2}(c+d x)\right] (a (1+\sin[c+d x]))^{3/2}}{704 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} - \\
& \frac{3 \cos\left[\frac{13}{2}(c+d x)\right] (a (1+\sin[c+d x]))^{3/2}}{832 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} - \frac{\cos\left[\frac{15}{2}(c+d x)\right] (a (1+\sin[c+d x]))^{3/2}}{960 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} + \\
& \frac{45 \sin\left[\frac{1}{2}(c+d x)\right] (a (1+\sin[c+d x]))^{3/2}}{64 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} + \frac{25 (a (1+\sin[c+d x]))^{3/2} \sin\left[\frac{3}{2}(c+d x)\right]}{192 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} + \\
& \frac{39 (a (1+\sin[c+d x]))^{3/2} \sin\left[\frac{5}{2}(c+d x)\right]}{320 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} + \frac{3 (a (1+\sin[c+d x]))^{3/2} \sin\left[\frac{7}{2}(c+d x)\right]}{448 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} + \\
& \frac{17 (a (1+\sin[c+d x]))^{3/2} \sin\left[\frac{9}{2}(c+d x)\right]}{576 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} - \frac{3 (a (1+\sin[c+d x]))^{3/2} \sin\left[\frac{11}{2}(c+d x)\right]}{704 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} + \\
& \frac{3 (a (1+\sin[c+d x]))^{3/2} \sin\left[\frac{13}{2}(c+d x)\right]}{832 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3} - \frac{(a (1+\sin[c+d x]))^{3/2} \sin\left[\frac{15}{2}(c+d x)\right]}{960 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3}
\end{aligned}$$

**Problem 121: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sec[c+d x] (a + a \sin[c+d x])^{3/2} \, dx$$

Optimal (type 3, 62 leaves, 4 steps):

$$\frac{2 \sqrt{2} a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{d} - \frac{2 a \sqrt{a+a \sin[c+d x]}}{d}$$

Result (type 3, 98 leaves):

$$-\left(\left(2\left(\left(2+2 \frac{1}{2}\right) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{1}{2}\right) (-1)^{1/4}\left(1+\tan\left[\frac{1}{4}(c+d x)\right]\right)\right]+\cos\left[\frac{1}{2}(c+d x)\right]+\right.\right.\right. \\
\left.\left.\left.\sin\left[\frac{1}{2}(c+d x)\right]\right)(a (1+\sin[c+d x]))^{3/2}\right) \Big/ \left(d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3\right)$$

**Problem 122: Result more than twice size of optimal antiderivative.**

$$\int \sec[c+d x]^2 (a + a \sin[c+d x])^{3/2} \, dx$$

Optimal (type 3, 26 leaves, 1 step):

$$\frac{2 a \operatorname{Sec}[c+d x] \sqrt{a+a \operatorname{Sin}[c+d x]}}{d}$$

Result (type 3, 67 leaves):

$$\left(2 (a (1+\sin[c+d x]))^{3/2}\right) / \left(d \left(\cos\left[\frac{1}{2} (c+d x)\right] - \sin\left[\frac{1}{2} (c+d x)\right]\right) \left(\cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right]\right)^3\right)$$

**Problem 123: Result unnecessarily involves imaginary or complex numbers.**

$$\int \operatorname{Sec}[c+d x]^3 (a+a \operatorname{Sin}[c+d x])^{3/2} dx$$

Optimal (type 3, 73 leaves, 4 steps):

$$\frac{a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} d} + \frac{\operatorname{Sec}[c+d x]^2 (a+a \operatorname{Sin}[c+d x])^{3/2}}{2 d}$$

Result (type 3, 134 leaves):

$$\left(a \left(\cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right] + (1+i) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4} (c+d x)\right]\right)\right] (-1 + \sin[c+d x])\right) \sqrt{a (1 + \sin[c+d x])}\right) / \left(2 d \left(\cos\left[\frac{1}{2} (c+d x)\right] - \sin\left[\frac{1}{2} (c+d x)\right]\right)^2 \left(\cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right]\right)\right)$$

**Problem 124: Result unnecessarily involves imaginary or complex numbers.**

$$\int \operatorname{Sec}[c+d x]^4 (a+a \operatorname{Sin}[c+d x])^{3/2} dx$$

Optimal (type 3, 107 leaves, 4 steps):

$$-\frac{a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sin}[c+d x]}}\right]}{2 \sqrt{2} d} + \frac{a \operatorname{Sec}[c+d x] \sqrt{a+a \operatorname{Sin}[c+d x]}}{2 d} + \frac{\operatorname{Sec}[c+d x]^3 (a+a \operatorname{Sin}[c+d x])^{3/2}}{3 d}$$

Result (type 3, 130 leaves):

$$\begin{aligned} & \frac{1}{d} \left( \frac{1}{12} + \frac{i}{12} \right) a \sec[c + d x]^3 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2 \\ & \sqrt{a (1 + \sin[c + d x])} \left( 6 (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4} (c + d x)\right]\right)\right] \right. \\ & \left. \left( \cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right] \right)^3 - (1 - i) (-5 + 3 \sin[c + d x]) \right) \end{aligned}$$

**Problem 125: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sec[c + d x]^5 (a + a \sin[c + d x])^{3/2} dx$$

Optimal (type 3, 127 leaves, 6 steps):

$$\begin{aligned} & \frac{15 a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{32 \sqrt{2} d} - \frac{15 a^2}{32 d \sqrt{a+a \sin[c+d x]}} + \\ & \frac{5 a \sec[c+d x]^2 \sqrt{a+a \sin[c+d x]}}{16 d} + \frac{\sec[c+d x]^4 (a+a \sin[c+d x])^{3/2}}{4 d} \end{aligned}$$

Result (type 3, 161 leaves):

$$\begin{aligned} & \frac{1}{d} \left( \frac{1}{128} + \frac{i}{128} \right) a \sec[c + d x]^4 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2 \\ & \sqrt{a (1 + \sin[c + d x])} \left( -60 (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4} (c + d x)\right]\right)\right] \right. \\ & \left. \left( \cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right] \right)^4 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right) + \right. \\ & \left. (1 - i) (-9 + 15 \cos[2 (c + d x)] + 40 \sin[c + d x]) \right) \end{aligned}$$

**Problem 126: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sec[c + d x]^6 (a + a \sin[c + d x])^{3/2} dx$$

Optimal (type 3, 169 leaves, 6 steps):

$$\begin{aligned} & -\frac{7 a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+d x]}{\sqrt{2} \sqrt{a+a \sin[c+d x]}}\right]}{16 \sqrt{2} d} - \frac{7 a^3 \cos[c+d x]}{16 d (a+a \sin[c+d x])^{3/2}} + \frac{7 a^2 \sec[c+d x]}{12 d \sqrt{a+a \sin[c+d x]}} + \\ & \frac{7 a \sec[c+d x]^3 \sqrt{a+a \sin[c+d x]}}{30 d} + \frac{\sec[c+d x]^5 (a+a \sin[c+d x])^{3/2}}{5 d} \end{aligned}$$

Result (type 3, 288 leaves):

$$\begin{aligned}
& \frac{1}{240 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5} \\
& \left( 30 \sin \left[ \frac{1}{2} (c + d x) \right] - 15 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) + (105 + 105 i) (-1)^{3/4} \right. \\
& \quad \left. \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan \left[ \frac{1}{4} (c + d x) \right] \right) \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 + \right. \\
& \quad \frac{24 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5} + \frac{40 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \\
& \quad \left. \frac{90 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2}{\cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right]} \right) (a (1 + \sin [c + d x]))^{3/2}
\end{aligned}$$

Problem 127: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^5 (a + a \sin [c + d x])^{5/2} \, dx$$

Optimal (type 3, 73 leaves, 3 steps):

$$\frac{8 (a + a \sin [c + d x])^{11/2}}{11 a^3 d} - \frac{8 (a + a \sin [c + d x])^{13/2}}{13 a^4 d} + \frac{2 (a + a \sin [c + d x])^{15/2}}{15 a^5 d}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
& \frac{45 \cos\left[\frac{1}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{64 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \frac{65 \cos\left[\frac{3}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{192 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{\cos\left[\frac{5}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{320 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \frac{5 \cos\left[\frac{7}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{64 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{5 \cos\left[\frac{9}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{192 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \frac{5 \cos\left[\frac{11}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{704 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{5 \cos\left[\frac{13}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{832 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \frac{\cos\left[\frac{15}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{960 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \\
& \frac{45 \sin\left[\frac{1}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{64 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \frac{65 (a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{3}{2}(c+d x)\right]}{192 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{(a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{5}{2}(c+d x)\right]}{320 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \frac{5 (a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{7}{2}(c+d x)\right]}{64 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{5 (a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{9}{2}(c+d x)\right]}{192 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \frac{5 (a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{11}{2}(c+d x)\right]}{704 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{5 (a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{13}{2}(c+d x)\right]}{832 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \frac{(a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{15}{2}(c+d x)\right]}{960 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^5}
\end{aligned}$$

Problem 128: Result more than twice size of optimal antiderivative.

$$\int \cos[c+d x]^4 (a + a \sin[c+d x])^{5/2} dx$$

Optimal (type 3, 159 leaves, 5 steps):

$$\begin{aligned}
& -\frac{4096 a^5 \cos[c+d x]^5}{15015 d (a + a \sin[c+d x])^{5/2}} - \frac{1024 a^4 \cos[c+d x]^5}{3003 d (a + a \sin[c+d x])^{3/2}} - \frac{128 a^3 \cos[c+d x]^5}{429 d \sqrt{a + a \sin[c+d x]}} - \\
& \frac{32 a^2 \cos[c+d x]^5 \sqrt{a + a \sin[c+d x]}}{143 d} - \frac{2 a \cos[c+d x]^5 (a + a \sin[c+d x])^{3/2}}{13 d}
\end{aligned}$$

Result (type 3, 757 leaves):

$$\begin{aligned}
& -\frac{9 \cos\left[\frac{1}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{8 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \frac{3 \cos\left[\frac{3}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{32 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{29 \cos\left[\frac{5}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{160 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \frac{5 \cos\left[\frac{7}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{112 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{\cos\left[\frac{9}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{48 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \frac{5 \cos\left[\frac{11}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{352 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \\
& \frac{\cos\left[\frac{13}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{416 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \frac{9 \sin\left[\frac{1}{2}(c+d x)\right] (a(1+\sin[c+d x]))^{5/2}}{8 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \\
& \frac{3 (a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{3}{2}(c+d x)\right]}{32 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \frac{29 (a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{5}{2}(c+d x)\right]}{160 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{5 (a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{7}{2}(c+d x)\right]}{112 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} + \frac{(a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{9}{2}(c+d x)\right]}{48 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \\
& \frac{5 (a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{11}{2}(c+d x)\right]}{352 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5} - \frac{(a(1+\sin[c+d x]))^{5/2} \sin\left[\frac{13}{2}(c+d x)\right]}{416 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5}
\end{aligned}$$

Problem 132: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c+d x] (a + a \sin[c+d x])^{5/2} \, dx$$

Optimal (type 3, 86 leaves, 5 steps):

$$\frac{4 \sqrt{2} a^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{d} - \frac{4 a^2 \sqrt{a+a \sin[c+d x]}}{d} - \frac{2 a (a+a \sin[c+d x])^{3/2}}{3 d}$$

Result (type 3, 126 leaves):

$$\begin{aligned}
& -\left(\left(\left(a(1+\sin[c+d x])\right)^{5/2} \left((24+24 \text{I}) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{\text{I}}{2}\right) (-1)^{1/4} \left(1+\tan\left[\frac{1}{4}(c+d x)\right]\right)\right]\right) + \right. \\
& \left. 15 \cos\left[\frac{1}{2}(c+d x)\right] - \cos\left[\frac{3}{2}(c+d x)\right] + 15 \sin\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{3}{2}(c+d x)\right]\right) / \\
& \left(3 d \left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^5\right)
\end{aligned}$$

Problem 134: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c+d x]^3 (a + a \sin[c+d x])^{5/2} \, dx$$

Optimal (type 3, 69 leaves, 4 steps):

$$-\frac{a^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{\sqrt{2} d}+\frac{a \sec [c+d x]^2 \left(a+a \sin[c+d x]\right)^{3/2}}{d}$$

Result (type 3, 138 leaves):

$$-\left(\left(a^2\left(-\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]+\left(1+\frac{i}{2}\right) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{1/4}\left(1+\tan \left[\frac{1}{4} (c+d x)\right]\right)\right](-1+\sin [c+d x])\right) \sqrt{a (1+\sin [c+d x])}\right) /\left(d \left(\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]\right)^2 \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)\right)$$

Problem 135: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^4 \left(a+a \sin [c+d x]\right)^{5/2} d x$$

Optimal (type 3, 30 leaves, 1 step):

$$\frac{2 a \sec [c+d x]^3 \left(a+a \sin [c+d x]\right)^{3/2}}{3 d}$$

Result (type 3, 69 leaves):

$$\left(2 \left(a \left(1+\sin [c+d x]\right)\right)^{5/2}\right) /\left(3 d \left(\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]\right)^3 \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^5\right)$$

Problem 136: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec [c+d x]^5 \left(a+a \sin [c+d x]\right)^{5/2} d x$$

Optimal (type 3, 103 leaves, 5 steps):

$$\frac{3 a^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{16 \sqrt{2} d}+\frac{3 a \sec [c+d x]^2 \left(a+a \sin [c+d x]\right)^{3/2}}{16 d}+\frac{\sec [c+d x]^4 \left(a+a \sin [c+d x]\right)^{5/2}}{4 d}$$

Result (type 3, 174 leaves):

$$\begin{aligned} & \left( a^2 \sqrt{a (1 + \sin(c + d x))} \left( 11 \cos\left(\frac{1}{2} (c + d x)\right) + 3 \cos\left(\frac{3}{2} (c + d x)\right) + \right. \right. \\ & \quad 11 \sin\left(\frac{1}{2} (c + d x)\right) + (3 + 3 i) (-1)^{1/4} \operatorname{ArcTan}\left(\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left(\frac{1}{4} (c + d x)\right)\right)\right) \\ & \quad \left. \left. (-3 + \cos[2 (c + d x)] + 4 \sin(c + d x)) - 3 \sin\left(\frac{3}{2} (c + d x)\right) \right) \right) / \\ & \left( 32 d \left( \cos\left(\frac{1}{2} (c + d x)\right) - \sin\left(\frac{1}{2} (c + d x)\right) \right)^4 \left( \cos\left(\frac{1}{2} (c + d x)\right) + \sin\left(\frac{1}{2} (c + d x)\right) \right) \right) \end{aligned}$$

**Problem 137: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sec(c + d x)^6 (a + a \sin(c + d x))^{5/2} dx$$

Optimal (type 3, 139 leaves, 5 steps):

$$\begin{aligned} & - \frac{a^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos(c+d x)}{\sqrt{2} \sqrt{a+a \sin(c+d x)}}\right]}{4 \sqrt{2} d} + \frac{a^2 \sec(c+d x) \sqrt{a+a \sin(c+d x)}}{4 d} + \\ & \frac{a \sec(c+d x)^3 (a+a \sin(c+d x))^{3/2}}{6 d} + \frac{\sec(c+d x)^5 (a+a \sin(c+d x))^{5/2}}{5 d} \end{aligned}$$

Result (type 3, 129 leaves):

$$\begin{aligned} & \left( \left( (15 + 15 i) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left(\frac{1}{4} (c + d x)\right)\right)\right] \right. \right. \\ & \quad \left. \left. \frac{89 - 15 \cos[2 (c + d x)] - 80 \sin(c + d x)}{2 \left(\cos\left(\frac{1}{2} (c + d x)\right) - \sin\left(\frac{1}{2} (c + d x)\right)\right)^5} \right) (a (1 + \sin(c + d x)))^{5/2} \right) / \\ & \left( 60 d \left( \cos\left(\frac{1}{2} (c + d x)\right) + \sin\left(\frac{1}{2} (c + d x)\right) \right)^5 \right) \end{aligned}$$

**Problem 138: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sec(c + d x)^7 (a + a \sin(c + d x))^{5/2} dx$$

Optimal (type 3, 159 leaves, 7 steps):

$$\begin{aligned} & \frac{35 a^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin(c+d x)}}{\sqrt{2} \sqrt{a}}\right]}{128 \sqrt{2} d} - \frac{35 a^3}{128 d \sqrt{a+a \sin(c+d x)}} + \frac{35 a^2 \sec(c+d x)^2 \sqrt{a+a \sin(c+d x)}}{192 d} + \\ & \frac{7 a \sec(c+d x)^4 (a+a \sin(c+d x))^{3/2}}{48 d} + \frac{\sec(c+d x)^6 (a+a \sin(c+d x))^{5/2}}{6 d} \end{aligned}$$

Result (type 3, 176 leaves):

$$\begin{aligned} & \frac{1}{d} \left( \frac{1}{3072} + \frac{i}{3072} \right) a^2 \sec[c + dx]^6 \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right)^4 \\ & \sqrt{a (1 + \sin[c + dx])} \left( -840 (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4} (c + dx)\right]\right)\right] \right. \\ & \left( \cos\left[\frac{1}{2} (c + dx)\right] - \sin\left[\frac{1}{2} (c + dx)\right] \right)^6 \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right) + \\ & (1 - i) (490 \cos[2 (c + dx)] + 791 \sin[c + dx] - 15 (10 + 7 \sin[3 (c + dx)])) \end{aligned}$$

**Problem 139: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx]^7 (a + a \sin[c + dx])^{7/2} \, dx$$

Optimal (type 3, 97 leaves, 3 steps):

$$\begin{aligned} & \frac{16 (a + a \sin[c + dx])^{15/2}}{15 a^4 d} - \frac{24 (a + a \sin[c + dx])^{17/2}}{17 a^5 d} + \\ & \frac{12 (a + a \sin[c + dx])^{19/2}}{19 a^6 d} - \frac{2 (a + a \sin[c + dx])^{21/2}}{21 a^7 d} \end{aligned}$$

Result (type 3, 1189 leaves):

$$\begin{aligned}
& \frac{91 \cos\left[\frac{1}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{128 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \frac{91 \cos\left[\frac{3}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{256 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \\
& \frac{7 \cos\left[\frac{5}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{1280 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \frac{43 \cos\left[\frac{7}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{448 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \\
& \frac{7 \cos\left[\frac{9}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{192 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \frac{7 \cos\left[\frac{11}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{512 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \\
& \frac{7 \cos\left[\frac{13}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{512 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} + \frac{7 \cos\left[\frac{15}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{3840 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \\
& \frac{7 \cos\left[\frac{17}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{4352 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} + \frac{7 \cos\left[\frac{19}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{9728 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} + \\
& \frac{\cos\left[\frac{21}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{10752 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} + \frac{91 \sin\left[\frac{1}{2} (c + d x)\right] (a (1 + \sin[c + d x]))^{7/2}}{128 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} + \\
& \frac{91 (a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{3}{2} (c + d x)\right]}{256 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \frac{7 (a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{5}{2} (c + d x)\right]}{1280 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} + \\
& \frac{43 (a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{7}{2} (c + d x)\right]}{448 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \frac{7 (a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{9}{2} (c + d x)\right]}{192 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} + \\
& \frac{7 (a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{11}{2} (c + d x)\right]}{512 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \frac{7 (a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{13}{2} (c + d x)\right]}{512 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \\
& \frac{7 (a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{15}{2} (c + d x)\right]}{3840 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \frac{7 (a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{17}{2} (c + d x)\right]}{4352 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} - \\
& \frac{7 (a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{19}{2} (c + d x)\right]}{9728 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7} + \frac{(a (1 + \sin[c + d x]))^{7/2} \sin\left[\frac{21}{2} (c + d x)\right]}{10752 d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^7}
\end{aligned}$$

**Problem 140: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^6 (a + a \sin[c + d x])^{7/2} dx$$

Optimal (type 3, 223 leaves, 7 steps):

$$\begin{aligned}
& -\frac{131072 a^7 \cos[c+d x]^7}{969969 d (a+a \sin[c+d x])^{7/2}} - \frac{32768 a^6 \cos[c+d x]^7}{138567 d (a+a \sin[c+d x])^{5/2}} - \frac{12288 a^5 \cos[c+d x]^7}{46189 d (a+a \sin[c+d x])^{3/2}} - \\
& -\frac{1024 a^4 \cos[c+d x]^7}{4199 d \sqrt{a+a \sin[c+d x]}} - \frac{64 a^3 \cos[c+d x]^7 \sqrt{a+a \sin[c+d x]}}{323 d} - \\
& \frac{48 a^2 \cos[c+d x]^7 (a+a \sin[c+d x])^{3/2}}{323 d} - \frac{2 a \cos[c+d x]^7 (a+a \sin[c+d x])^{5/2}}{19 d}
\end{aligned}$$

Result (type 3, 1081 leaves):

$$\begin{aligned}
& -\frac{143 \cos[\frac{1}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{128 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} + \frac{13 \cos[\frac{3}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{128 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \\
& -\frac{13 \cos[\frac{5}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{64 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \frac{23 \cos[\frac{7}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{448 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \\
& -\frac{7 \cos[\frac{9}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{192 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \frac{19 \cos[\frac{11}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{704 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} + \\
& -\frac{7 \cos[\frac{13}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{3328 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \frac{\cos[\frac{15}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{256 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} + \\
& +\frac{7 \cos[\frac{17}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{4352 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} + \frac{\cos[\frac{19}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{4864 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} + \\
& +\frac{143 \sin[\frac{1}{2} (c+d x)] (a (1+\sin[c+d x]))^{7/2}}{128 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} + \frac{13 (a (1+\sin[c+d x]))^{7/2} \sin[\frac{3}{2} (c+d x)]}{128 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} + \\
& -\frac{13 (a (1+\sin[c+d x]))^{7/2} \sin[\frac{5}{2} (c+d x)]}{64 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \frac{23 (a (1+\sin[c+d x]))^{7/2} \sin[\frac{7}{2} (c+d x)]}{448 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} + \\
& -\frac{7 (a (1+\sin[c+d x]))^{7/2} \sin[\frac{9}{2} (c+d x)]}{192 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \frac{19 (a (1+\sin[c+d x]))^{7/2} \sin[\frac{11}{2} (c+d x)]}{704 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \\
& -\frac{7 (a (1+\sin[c+d x]))^{7/2} \sin[\frac{13}{2} (c+d x)]}{3328 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \frac{(a (1+\sin[c+d x]))^{7/2} \sin[\frac{15}{2} (c+d x)]}{256 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} - \\
& +\frac{7 (a (1+\sin[c+d x]))^{7/2} \sin[\frac{17}{2} (c+d x)]}{4352 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7} + \frac{(a (1+\sin[c+d x]))^{7/2} \sin[\frac{19}{2} (c+d x)]}{4864 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^7}
\end{aligned}$$

Problem 141: Result more than twice size of optimal antiderivative.

$$\int \cos[c+d x]^5 (a+a \sin[c+d x])^{7/2} dx$$

Optimal (type 3, 73 leaves, 3 steps):

$$\frac{8 (a + a \sin[c + d x])^{13/2}}{13 a^3 d} - \frac{8 (a + a \sin[c + d x])^{15/2}}{15 a^4 d} + \frac{2 (a + a \sin[c + d x])^{17/2}}{17 a^5 d}$$

Result (type 3, 865 leaves):

$$\begin{aligned} & \frac{55 \cos[\frac{1}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}}{64 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} - \frac{11 \cos[\frac{3}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}}{24 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} - \\ & \frac{\cos[\frac{5}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}}{20 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} - \frac{3 \cos[\frac{7}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}}{32 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} - \\ & \frac{5 \cos[\frac{9}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}}{96 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} - \frac{\cos[\frac{13}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}}{104 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} + \\ & \frac{7 \cos[\frac{15}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}}{1920 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} + \frac{\cos[\frac{17}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}}{2176 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} + \\ & \frac{55 \sin[\frac{1}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}}{64 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} + \frac{11 (a (1 + \sin[c + d x]))^{7/2} \sin[\frac{3}{2} (c + d x)]}{24 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} - \\ & \frac{(a (1 + \sin[c + d x]))^{7/2} \sin[\frac{5}{2} (c + d x)]}{20 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} + \frac{3 (a (1 + \sin[c + d x]))^{7/2} \sin[\frac{7}{2} (c + d x)]}{32 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} - \\ & \frac{5 (a (1 + \sin[c + d x]))^{7/2} \sin[\frac{9}{2} (c + d x)]}{96 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} - \frac{(a (1 + \sin[c + d x]))^{7/2} \sin[\frac{13}{2} (c + d x)]}{104 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} - \\ & \frac{7 (a (1 + \sin[c + d x]))^{7/2} \sin[\frac{15}{2} (c + d x)]}{1920 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} + \frac{(a (1 + \sin[c + d x]))^{7/2} \sin[\frac{17}{2} (c + d x)]}{2176 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7} \end{aligned}$$

Problem 142: Result more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^4 (a + a \sin[c + d x])^{7/2} d x$$

Optimal (type 3, 191 leaves, 6 steps):

$$\begin{aligned} & - \frac{16384 a^6 \cos[c + d x]^5}{45045 d (a + a \sin[c + d x])^{5/2}} - \frac{4096 a^5 \cos[c + d x]^5}{9009 d (a + a \sin[c + d x])^{3/2}} - \\ & \frac{512 a^4 \cos[c + d x]^5}{1287 d \sqrt{a + a \sin[c + d x]}} - \frac{128 a^3 \cos[c + d x]^5 \sqrt{a + a \sin[c + d x]}}{429 d} - \\ & \frac{8 a^2 \cos[c + d x]^5 (a + a \sin[c + d x])^{3/2}}{39 d} - \frac{2 a \cos[c + d x]^5 (a + a \sin[c + d x])^{5/2}}{15 d} \end{aligned}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
 & - \frac{99 \cos\left[\frac{1}{2}(c+d x)\right] (a (1 + \sin[c+d x]))^{7/2}}{64 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7} + \frac{11 \cos\left[\frac{3}{2}(c+d x)\right] (a (1 + \sin[c+d x]))^{7/2}}{192 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7} - \\
 & 77 \cos\left[\frac{5}{2}(c+d x)\right] (a (1 + \sin[c+d x]))^{7/2} - \frac{43 \cos\left[\frac{7}{2}(c+d x)\right] (a (1 + \sin[c+d x]))^{7/2}}{448 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7} - \\
 & 320 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7 - \frac{17 \cos\left[\frac{11}{2}(c+d x)\right] (a (1 + \sin[c+d x]))^{7/2}}{704 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7} + \\
 & 576 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7 - \frac{\cos\left[\frac{15}{2}(c+d x)\right] (a (1 + \sin[c+d x]))^{7/2}}{960 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7} + \\
 & 7 \cos\left[\frac{13}{2}(c+d x)\right] (a (1 + \sin[c+d x]))^{7/2} + \frac{99 \sin\left[\frac{1}{2}(c+d x)\right] (a (1 + \sin[c+d x]))^{7/2}}{64 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7} + \frac{11 (a (1 + \sin[c+d x]))^{7/2} \sin\left[\frac{3}{2}(c+d x)\right]}{192 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7} + \\
 & 77 (a (1 + \sin[c+d x]))^{7/2} \sin\left[\frac{5}{2}(c+d x)\right] - \frac{43 (a (1 + \sin[c+d x]))^{7/2} \sin\left[\frac{7}{2}(c+d x)\right]}{448 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7} + \\
 & 320 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7 - \frac{17 (a (1 + \sin[c+d x]))^{7/2} \sin\left[\frac{11}{2}(c+d x)\right]}{704 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7} - \\
 & 576 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7 + \frac{(a (1 + \sin[c+d x]))^{7/2} \sin\left[\frac{15}{2}(c+d x)\right]}{960 d \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right)^7}
 \end{aligned}$$

Problem 143: Result more than twice size of optimal antiderivative.

$$\int \cos[c+d x]^3 (a + a \sin[c+d x])^{7/2} \, dx$$

Optimal (type 3, 49 leaves, 3 steps):

$$\frac{4 (a + a \sin[c+d x])^{11/2}}{11 a^2 d} - \frac{2 (a + a \sin[c+d x])^{13/2}}{13 a^3 d}$$

Result (type 3, 757 leaves):

$$\begin{aligned}
& \frac{9 \cos\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{8d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{21 \cos\left[\frac{3}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{32d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\
& \frac{5 \cos\left[\frac{5}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{32d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{\cos\left[\frac{7}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{16d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\
& \frac{\cos\left[\frac{9}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{16d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{7 \cos\left[\frac{11}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{352d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
& \frac{\cos\left[\frac{13}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{416d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{9 \sin\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{8d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
& \frac{21 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{3}{2}(c+dx)\right]}{32d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{5 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{5}{2}(c+dx)\right]}{32d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
& \frac{(a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{7}{2}(c+dx)\right]}{16d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{(a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{9}{2}(c+dx)\right]}{16d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\
& \frac{7 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{11}{2}(c+dx)\right]}{352d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{(a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{13}{2}(c+dx)\right]}{416d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7}
\end{aligned}$$

Problem 144: Result more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^2 (a + a \sin[c+dx])^{7/2} \, dx$$

Optimal (type 3, 159 leaves, 5 steps):

$$\begin{aligned}
& - \frac{4096 a^5 \cos[c+dx]^3}{3465 d (a + a \sin[c+dx])^{3/2}} - \\
& \frac{1024 a^4 \cos[c+dx]^3}{1155 d \sqrt{a + a \sin[c+dx]}} - \frac{128 a^3 \cos[c+dx]^3 \sqrt{a + a \sin[c+dx]}}{231 d} - \\
& \frac{32 a^2 \cos[c+dx]^3 (a + a \sin[c+dx])^{3/2}}{99 d} - \frac{2 a \cos[c+dx]^3 (a + a \sin[c+dx])^{5/2}}{11 d}
\end{aligned}$$

Result (type 3, 649 leaves):

$$\begin{aligned}
& - \frac{21 \cos\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{8d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} - \frac{\cos\left[\frac{3}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{8d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} - \\
& \frac{21 \cos\left[\frac{5}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{80d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} - \frac{19 \cos\left[\frac{7}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{112d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} + \\
& \frac{7 \cos\left[\frac{9}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{144d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} + \frac{\cos\left[\frac{11}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{176d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} + \\
& \frac{21 \sin\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{8d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} - \frac{(a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{3}{2}(c+dx)\right]}{8d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} + \\
& \frac{21 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{5}{2}(c+dx)\right]}{80d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} - \frac{19 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{7}{2}(c+dx)\right]}{112d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} - \\
& \frac{7 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{9}{2}(c+dx)\right]}{144d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7} + \frac{(a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{11}{2}(c+dx)\right]}{176d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7}
\end{aligned}$$

Problem 146: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c+dx] (a + a \sin[c+dx])^{7/2} \, dx$$

Optimal (type 3, 110 leaves, 6 steps):

$$\begin{aligned}
& \frac{8\sqrt{2} a^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+dx]}}{\sqrt{2} \sqrt{a}}\right]}{d} - \frac{8 a^3 \sqrt{a+a \sin[c+dx]}}{d} - \\
& \frac{4 a^2 (a+a \sin[c+dx])^{3/2}}{3 d} - \frac{2 a (a+a \sin[c+dx])^{5/2}}{5 d}
\end{aligned}$$

Result (type 3, 165 leaves):

$$\begin{aligned}
& - \left( \left( a^3 (1+\sin[c+dx])^3 \sqrt{a(1+\sin[c+dx])} \right. \right. \\
& \left. \left. \left( (480+480i)(-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{i}{2}\right)(-1)^{1/4}\right] \left(1+\tan\left[\frac{1}{4}(c+dx)\right]\right) \right. \right. + \\
& 330 \cos\left[\frac{1}{2}(c+dx)\right] - 35 \cos\left[\frac{3}{2}(c+dx)\right] - 3 \cos\left[\frac{5}{2}(c+dx)\right] + 330 \sin\left[\frac{1}{2}(c+dx)\right] + \\
& \left. \left. 35 \sin\left[\frac{3}{2}(c+dx)\right] - 3 \sin\left[\frac{5}{2}(c+dx)\right] \right) \right) \Big/ \left( 30d(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^7 \right)
\end{aligned}$$

Problem 148: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c+dx]^3 (a + a \sin[c+dx])^{7/2} \, dx$$

Optimal (type 3, 91 leaves, 5 steps):

$$-\frac{3 \sqrt{2} a^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{d} + \frac{3 a^3 \sqrt{a+a \sin[c+d x]}}{d} + \frac{a \sec [c+d x]^2 (a+a \sin[c+d x])^{5/2}}{d}$$

Result (type 3, 159 leaves):

$$\begin{aligned} & \left(a^3 \sqrt{a (1+\sin[c+d x])}\right. \\ & \left(3 \cos\left[\frac{1}{2} (c+d x)\right] + \cos\left[\frac{3}{2} (c+d x)\right] + 3 \sin\left[\frac{1}{2} (c+d x)\right] - (6+6 i) (-1)^{1/4}\right. \\ & \left.\operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4} (c+d x)\right]\right)\right] (-1+\sin[c+d x]) - \sin\left[\frac{3}{2} (c+d x)\right]\right) \Big/ \\ & \left(d \left(\cos\left[\frac{1}{2} (c+d x)\right] - \sin\left[\frac{1}{2} (c+d x)\right]\right)^2 \left(\cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right]\right)\right) \end{aligned}$$

Problem 150: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec [c+d x]^5 (a+a \sin[c+d x])^{7/2} \, dx$$

Optimal (type 3, 106 leaves, 5 steps):

$$-\frac{a^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{8 \sqrt{2} d} - \frac{a^2 \sec [c+d x]^2 (a+a \sin[c+d x])^{3/2}}{8 d} + \frac{a \sec [c+d x]^4 (a+a \sin[c+d x])^{5/2}}{2 d}$$

Result (type 3, 172 leaves):

$$\begin{aligned} & -\left(\left(a^3 \sqrt{a (1+\sin[c+d x])}\right. \left(-7 \cos\left[\frac{1}{2} (c+d x)\right] + \cos\left[\frac{3}{2} (c+d x)\right] -\right.\right. \\ & 7 \sin\left[\frac{1}{2} (c+d x)\right] + (1+i) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4} (c+d x)\right]\right)\right] \\ & \left.\left.\left(-3 + \cos[2 (c+d x)] + 4 \sin[c+d x]\right) - \sin\left[\frac{3}{2} (c+d x)\right]\right)\right) \Big/ \\ & \left(16 d \left(\cos\left[\frac{1}{2} (c+d x)\right] - \sin\left[\frac{1}{2} (c+d x)\right]\right)^4 \left(\cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right]\right)\right) \end{aligned}$$

Problem 151: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^6 (a+a \sin[c+d x])^{7/2} \, dx$$

Optimal (type 3, 30 leaves, 1 step):

$$\frac{2 a \sec[c + d x]^5 (a + a \sin[c + d x])^{5/2}}{5 d}$$

Result (type 3, 69 leaves):

$$\left( 2 (a (1 + \sin[c + d x]))^{7/2} \right) / \left( 5 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^7 \right)$$

Problem 152: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c + d x]^7 (a + a \sin[c + d x])^{7/2} \, dx$$

Optimal (type 3, 135 leaves, 6 steps):

$$\frac{5 a^{7/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{a + a \sin[c + d x]}}{\sqrt{2} \sqrt{a}} \right]}{64 \sqrt{2} d} + \frac{5 a^2 \sec[c + d x]^2 (a + a \sin[c + d x])^{3/2}}{64 d} + \frac{5 a \sec[c + d x]^4 (a + a \sin[c + d x])^{5/2}}{48 d} + \frac{\sec[c + d x]^6 (a + a \sin[c + d x])^{7/2}}{6 d}$$

Result (type 3, 205 leaves):

$$\begin{aligned} & \left( a^3 \sqrt{a (1 + \sin[c + d x])} \right. \\ & \left( 198 \cos \left[ \frac{1}{2} (c + d x) \right] + 85 \cos \left[ \frac{3}{2} (c + d x) \right] - 15 \cos \left[ \frac{5}{2} (c + d x) \right] - (60 + 60 \frac{i}{2}) (-1)^{1/4} \right. \\ & \quad \left. \operatorname{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \tan \left[ \frac{1}{4} (c + d x) \right] \right) \right] \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^6 + \right. \\ & \quad \left. 198 \sin \left[ \frac{1}{2} (c + d x) \right] - 85 \sin \left[ \frac{3}{2} (c + d x) \right] - 15 \sin \left[ \frac{5}{2} (c + d x) \right] \right) \Big/ \\ & \left( 768 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^6 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) \end{aligned}$$

Problem 153: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c + d x]^8 (a + a \sin[c + d x])^{7/2} \, dx$$

Optimal (type 3, 171 leaves, 6 steps):

$$\begin{aligned}
& - \frac{a^{7/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \cos(c+d x)}{\sqrt{2} \sqrt{a+a \sin(c+d x)}} \right]}{8 \sqrt{2} d} + \\
& \frac{a^3 \sec(c+d x) \sqrt{a+a \sin(c+d x)}}{8 d} + \frac{a^2 \sec(c+d x)^3 (a+a \sin(c+d x))^{3/2}}{12 d} + \\
& \frac{a \sec(c+d x)^5 (a+a \sin(c+d x))^{5/2}}{10 d} + \frac{\sec(c+d x)^7 (a+a \sin(c+d x))^{7/2}}{7 d}
\end{aligned}$$

Result (type 3, 139 leaves):

$$\begin{aligned}
& \left( (a (1 + \sin(c+d x)))^{7/2} \right. \\
& \left( (105 + 105 \frac{i}{2}) (-1)^{3/4} \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan \left[ \frac{1}{4} (c+d x) \right] \right) \right] + \right. \\
& \left. (2286 - 770 \cos(2 (c+d x)) - 2471 \sin(c+d x) + 105 \sin(3 (c+d x))) \right) / \\
& \left( 4 \left( \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right)^7 \right) \\
& \left. \left( 840 d \left( \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right)^7 \right)
\end{aligned}$$

Problem 154: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec(c+d x)^9 (a+a \sin(c+d x))^{7/2} dx$$

Optimal (type 3, 191 leaves, 8 steps):

$$\begin{aligned}
& \frac{315 a^{7/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{a+a \sin(c+d x)}}{\sqrt{2} \sqrt{a}} \right]}{2048 \sqrt{2} d} - \frac{315 a^4}{2048 d \sqrt{a+a \sin(c+d x)}} + \\
& \frac{105 a^3 \sec(c+d x)^2 \sqrt{a+a \sin(c+d x)}}{1024 d} + \frac{21 a^2 \sec(c+d x)^4 (a+a \sin(c+d x))^{3/2}}{256 d} + \\
& \frac{3 a \sec(c+d x)^6 (a+a \sin(c+d x))^{5/2}}{32 d} + \frac{\sec(c+d x)^8 (a+a \sin(c+d x))^{7/2}}{8 d}
\end{aligned}$$

Result (type 3, 735 leaves):

$$\begin{aligned}
& - \frac{(a (1 + \sin[c + d x]))^{7/2}}{16 d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^8} - \\
& \left( \left( \frac{315}{2048} + \frac{315 i}{2048} \right) (-1)^{1/4} \operatorname{ArcTan} \left( \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \sec[\frac{1}{4} (c + d x)] \right) \right. \\
& \left. \left( \cos[\frac{1}{4} (c + d x)] + \sin[\frac{1}{4} (c + d x)] \right) (a (1 + \sin[c + d x]))^{7/2} \right) / \\
& \left( d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7 \right) + (a (1 + \sin[c + d x]))^{7/2} / \\
& \left( 16 d (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^7 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7 \right) + \\
& (5 (a (1 + \sin[c + d x]))^{7/2}) / \\
& \left( 64 d (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^5 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7 \right) + \\
& (41 (a (1 + \sin[c + d x]))^{7/2}) / \\
& \left( 512 d (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^3 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7 \right) + \\
& (187 (a (1 + \sin[c + d x]))^{7/2}) / \\
& \left( 2048 d (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)]) (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7 \right) + \\
& \left( \sin[\frac{1}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2} \right) / \\
& \left( 8 d (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^8 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7 \right) + \\
& \left( 5 \sin[\frac{1}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2} \right) / \\
& \left( 32 d (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^6 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7 \right) + \\
& (41 \sin[\frac{1}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}) / \\
& \left( 256 d (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^4 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7 \right) + \\
& (187 \sin[\frac{1}{2} (c + d x)] (a (1 + \sin[c + d x]))^{7/2}) / \\
& \left( 1024 d (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^2 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^7 \right)
\end{aligned}$$

Problem 155: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c + d x]^{10} (a + a \sin[c + d x])^{7/2} \, dx$$

Optimal (type 3, 233 leaves, 8 steps):

$$\begin{aligned}
& -\frac{11 a^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{64 \sqrt{2} d} -\frac{11 a^5 \cos [c+d x]}{64 d (a+a \sin [c+d x])^{3/2}}+\frac{11 a^4 \sec [c+d x]}{48 d \sqrt{a+a \sin [c+d x]}}+ \\
& \frac{11 a^3 \sec [c+d x]^3 \sqrt{a+a \sin [c+d x]}}{120 d}+\frac{11 a^2 \sec [c+d x]^5 (a+a \sin [c+d x])^{3/2}}{140 d}+ \\
& \frac{11 a \sec [c+d x]^7 (a+a \sin [c+d x])^{5/2}}{126 d}+\frac{\sec [c+d x]^9 (a+a \sin [c+d x])^{7/2}}{9 d}
\end{aligned}$$

Result (type 3, 388 leaves):

$$\begin{aligned}
& \frac{1}{20160 d \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^9} \\
& \left(630 \sin \left[\frac{1}{2} (c+d x)\right]-315 \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)+\left(3465+3465 i\right) (-1)^{3/4}\right. \\
& \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{3/4} \left(-1+\tan \left[\frac{1}{4} (c+d x)\right]\right)\right] \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^2+ \\
& \frac{1120 \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]\right)^9}+\frac{1440 \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]\right)^7}+ \\
& \frac{1512 \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]\right)^5}+\frac{1680 \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]\right)^3}+ \\
& \left.\frac{3150 \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^2}{\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]}\right) \left(a (1+\sin [c+d x])\right)^{7/2}
\end{aligned}$$

Problem 161: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^2}{\sqrt{a+a \sin [c+d x]}} \, dx$$

Optimal (type 3, 30 leaves, 1 step):

$$-\frac{2 a \cos [c+d x]^3}{3 d (a+a \sin [c+d x])^{3/2}}$$

Result (type 3, 67 leaves):

$$-\left(\left(2 \left(\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]\right)^3 \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)\right) \middle/ \right. \\
\left.\left(3 d \sqrt{a (1+\sin [c+d x])}\right)\right)$$

**Problem 163: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec(c+dx)}{\sqrt{a+a \sin(c+dx)}} \, dx$$

Optimal (type 3, 60 leaves, 4 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin(c+dx)}}{\sqrt{2} \sqrt{a}}\right]}{\sqrt{2} \sqrt{a} d}-\frac{1}{d \sqrt{a+a \sin(c+dx)}}$$

Result (type 3, 76 leaves):

$$\begin{aligned} & \left(-1-\left(1+\frac{i}{2}\right)\left(-1\right)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(-1\right)^{1/4}\left(1+\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right]\right. \\ & \left.\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)\right) \bigg/ \left(d \sqrt{a(1+\sin(c+d x))}\right) \end{aligned}$$

**Problem 164: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec(c+dx)^2}{\sqrt{a+a \sin(c+dx)}} \, dx$$

Optimal (type 3, 102 leaves, 4 steps):

$$\begin{aligned} & -\frac{3 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos (c+d x)}{\sqrt{2} \sqrt{a+a \sin (c+d x)}}\right]}{4 \sqrt{2} \sqrt{a} d}-\frac{3 a \cos (c+d x)}{4 d\left(a+a \sin (c+d x)\right)^{3/2}}+\frac{\sec (c+d x)}{d \sqrt{a+a \sin (c+d x)}} \end{aligned}$$

Result (type 3, 118 leaves):

$$\begin{aligned} & -\left(\left(\sec (c+d x)\left(-1-\left(3+3 \frac{i}{2}\right)\left(-1\right)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(-1\right)^{3/4}\left(-1+\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right]\right.\right. \\ & \left.\left.\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^2-\right. \\ & \left.\left.3 \sin (c+d x)\right)\right) \bigg/ \left(4 d \sqrt{a(1+\sin(c+d x))}\right)\right) \end{aligned}$$

**Problem 165: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec(c+dx)^3}{\sqrt{a+a \sin(c+dx)}} \, dx$$

Optimal (type 3, 116 leaves, 6 steps):

$$\frac{5 \operatorname{ArcTanh} \left[ \frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}} \right]}{8 \sqrt{2} \sqrt{a} d} - \frac{5 a}{12 d (a+a \sin[c+d x])^{3/2}} -$$

$$\frac{5}{8 d \sqrt{a+a \sin[c+d x]}} + \frac{\operatorname{Sec}[c+d x]^2}{2 d \sqrt{a+a \sin[c+d x]}}$$

Result (type 3, 108 leaves):

$$\left( (-30 - 30 i) (-1)^{1/4} \operatorname{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} (c+d x) \right] \right) \right] \left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right) - \operatorname{Sec}[c+d x]^2 (11 + 15 \operatorname{Cos}[2 (c+d x)] - 20 \operatorname{Sin}[c+d x]) \right) / \left( 48 d \sqrt{a (1 + \operatorname{Sin}[c+d x])} \right)$$

Problem 166: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c+d x]^4}{\sqrt{a+a \sin[c+d x]}} \, dx$$

Optimal (type 3, 162 leaves, 6 steps):

$$-\frac{35 \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \operatorname{Cos}[c+d x]}{\sqrt{2} \sqrt{a+a \sin[c+d x]}} \right]}{64 \sqrt{2} \sqrt{a} d} - \frac{35 a \operatorname{Cos}[c+d x]}{64 d (a+a \sin[c+d x])^{3/2}} -$$

$$\frac{7 a \operatorname{Sec}[c+d x]}{24 d (a+a \sin[c+d x])^{3/2}} + \frac{35 \operatorname{Sec}[c+d x]}{48 d \sqrt{a+a \sin[c+d x]}} + \frac{\operatorname{Sec}[c+d x]^3}{3 d \sqrt{a+a \sin[c+d x]}}$$

Result (type 3, 117 leaves):

$$\left( (420 + 420 i) (-1)^{3/4} \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \operatorname{Tan} \left[ \frac{1}{4} (c+d x) \right] \right) \right] \left( \operatorname{Cos} \left[ \frac{1}{2} (c+d x) \right] + \operatorname{Sin} \left[ \frac{1}{2} (c+d x) \right] \right) + \operatorname{Sec}[c+d x]^3 (102 + 70 \operatorname{Cos}[2 (c+d x)] + 329 \operatorname{Sin}[c+d x] + 105 \operatorname{Sin}[3 (c+d x)]) \right) / \left( 768 d \sqrt{a (1 + \operatorname{Sin}[c+d x])} \right)$$

Problem 167: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c+d x]^5}{\sqrt{a+a \sin[c+d x]}} \, dx$$

Optimal (type 3, 175 leaves, 8 steps):

$$\frac{63 \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{128 \sqrt{2} \sqrt{a} d}-\frac{21 a}{64 d (a+a \sin[c+d x])^{3/2}}-\frac{9 a \sec [c+d x]^2}{40 d (a+a \sin[c+d x])^{3/2}}-$$

$$\frac{63}{128 d \sqrt{a+a \sin[c+d x]}}+\frac{63 \sec [c+d x]^2}{160 d \sqrt{a+a \sin[c+d x]}}+\frac{\sec [c+d x]^4}{4 d \sqrt{a+a \sin[c+d x]}}$$

Result (type 3, 130 leaves):

$$\left(\left(-315-315 \frac{i}{2}\right) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{1/4} \left(1+\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]\right)\right]\right.$$

$$\left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)-\frac{1}{8} \sec [c+d x]^4$$

$$\left.\left(649+1092 \cos [2 (c+d x)]+315 \cos [4 (c+d x)]-1572 \sin [c+d x]-420 \sin [3 (c+d x)]\right)\right)/$$

$$\left(640 d \sqrt{a (1+\sin [c+d x])}\right)$$

Problem 168: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sec [c+d x]^6}{\sqrt{a+a \sin [c+d x]}} dx$$

Optimal (type 3, 221 leaves, 8 steps):

$$\frac{231 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{512 \sqrt{2} \sqrt{a} d}-\frac{231 a \cos [c+d x]}{512 d (a+a \sin [c+d x])^{3/2}}-$$

$$\frac{77 a \sec [c+d x]}{320 d (a+a \sin [c+d x])^{3/2}}-\frac{11 a \sec [c+d x]^3}{60 d (a+a \sin [c+d x])^{3/2}}+$$

$$\frac{77 \sec [c+d x]}{128 d \sqrt{a+a \sin [c+d x]}}+\frac{11 \sec [c+d x]^3}{40 d \sqrt{a+a \sin [c+d x]}}+\frac{\sec [c+d x]^5}{5 d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 140 leaves):

$$\left(\left(3465+3465 \frac{i}{2}\right) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{3/4} \left(-1+\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]\right)\right]\right) \left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)+$$

$$\frac{1}{16} \sec [c+d x]^5 \left(11090+11352 \cos [2 (c+d x)]+2310 \cos [4 (c+d x)]+36850 \sin [c+d x]+17787 \sin [3 (c+d x)]+3465 \sin [5 (c+d x)]\right)\right)/\left(7680 d \sqrt{a (1+\sin [c+d x])}\right)$$

Problem 172: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^4}{(a+a \sin [c+d x])^{3/2}} dx$$

Optimal (type 3, 30 leaves, 1 step):

$$-\frac{2 a \cos[c+d x]^5}{5 d (a+a \sin[c+d x])^{5/2}}$$

Result (type 3, 69 leaves):

$$-\left(\left(2\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^5\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3\right)\right.\left.\left(5 d (a (1+\sin[c+d x]))^{3/2}\right)\right)$$

**Problem 174: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cos[c+d x]^2}{(a+a \sin[c+d x])^{3/2}} \, dx$$

Optimal (type 3, 76 leaves, 3 steps):

$$-\frac{2 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+d x]}{\sqrt{2} \sqrt{a+a \sin[c+d x]}}\right]}{a^{3/2} d}+\frac{2 \cos[c+d x]}{a d \sqrt{a+a \sin[c+d x]}}$$

Result (type 3, 100 leaves):

$$\left(2\left((2+2 \frac{i}{2}) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{3/4}\left(-1+\tan\left[\frac{1}{4}(c+d x)\right]\right)\right]+\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3\right)\right.\left.\left( d (a (1+\sin[c+d x]))^{3/2}\right)\right)$$

**Problem 176: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec[c+d x]}{(a+a \sin[c+d x])^{3/2}} \, dx$$

Optimal (type 3, 89 leaves, 5 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} a^{3/2} d}-\frac{1}{3 d (a+a \sin[c+d x])^{3/2}}-\frac{1}{2 a d \sqrt{a+a \sin[c+d x]}}$$

Result (type 3, 106 leaves):

$$\begin{aligned} & \left(-2-3\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2-\right. \\ & \left.(3+3 \frac{i}{2}) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{1/4}\left(1+\tan\left[\frac{1}{4}(c+d x)\right]\right)\right]\right. \\ & \left.\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^3\right)\right.\left.\left(6 d (a (1+\sin[c+d x]))^{3/2}\right)\right)$$

### Problem 177: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sec [c + d x]^2}{(a + a \sin [c + d x])^{3/2}} dx$$

Optimal (type 3, 134 leaves, 5 steps):

$$-\frac{15 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{32 \sqrt{2} a^{3/2} d}-\frac{15 \cos [c+d x]}{32 d (a+a \sin [c+d x])^{3/2}}-$$

$$\frac{\sec [c+d x]}{4 d (a+a \sin [c+d x])^{3/2}}+\frac{5 \sec [c+d x]}{8 a d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 224 leaves):

$$\left(-4+\frac{8 \sin \left[\frac{1}{2} (c+d x)\right]}{\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]}+\right.$$

$$14 \sin \left[\frac{1}{2} (c+d x)\right]\left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)-$$

$$7\left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^2+\left(15+15 \frac{i}{2}\right) (-1)^{3/4}$$

$$\operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right) (-1)^{3/4}\left(-1+\tan \left[\frac{1}{4} (c+d x)\right]\right)\right]\left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^3+$$

$$\left.\frac{8\left(\cos \left[\frac{1}{2} (c+d x)\right]+\sin \left[\frac{1}{2} (c+d x)\right]\right)^3}{\cos \left[\frac{1}{2} (c+d x)\right]-\sin \left[\frac{1}{2} (c+d x)\right]}\right) \bigg/ \left(32 d (a (1+\sin [c+d x]))^{3/2}\right)$$

### Problem 178: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sec [c + d x]^3}{(a + a \sin [c + d x])^{3/2}} dx$$

Optimal (type 3, 150 leaves, 7 steps):

$$\frac{7 \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{16 \sqrt{2} a^{3/2} d}-\frac{7}{24 d (a+a \sin [c+d x])^{3/2}}-$$

$$\frac{\sec [c+d x]^2}{5 d (a+a \sin [c+d x])^{3/2}}-\frac{7}{16 a d \sqrt{a+a \sin [c+d x]}}+\frac{7 \sec [c+d x]^2}{20 a d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 241 leaves):

$$\left( -40 - \frac{24}{(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^2} - 90 \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^2 - \right. \\ \left( 105 + 105 \frac{i}{2} \right) (-1)^{1/4} \operatorname{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \tan[\frac{1}{4}(c+dx)] \right) \right] \\ \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^3 + \frac{15 \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^3}{\cos[\frac{1}{2}(c+dx)] - \sin[\frac{1}{2}(c+dx)]} + \\ \left. \frac{30 \sin[\frac{1}{2}(c+dx)] \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^3}{\cos[\frac{1}{2}(c+dx)] - \sin[\frac{1}{2}(c+dx)]^2} \right) \Big/ \left( 240 d (a (1 + \sin[c+dx]))^{3/2} \right)$$

Problem 179: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sec[c+dx]^4}{(a + a \sin[c+dx])^{3/2}} dx$$

Optimal (type 3, 195 leaves, 7 steps):

$$- \frac{105 \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}} \right]}{256 \sqrt{2} a^{3/2} d} - \frac{105 \cos[c+dx]}{256 d (a + a \sin[c+dx])^{3/2}} - \frac{7 \sec[c+dx]}{32 d (a + a \sin[c+dx])^{3/2}} - \\ \frac{\sec[c+dx]^3}{6 d (a + a \sin[c+dx])^{3/2}} + \frac{35 \sec[c+dx]}{64 a d \sqrt{a + a \sin[c+dx]}} + \frac{\sec[c+dx]^3}{4 a d \sqrt{a + a \sin[c+dx]}}$$

Result (type 3, 334 leaves):

$$\frac{1}{768 d (a (1 + \sin[c+dx]))^{3/2}} \left( -68 + \frac{64 \sin[\frac{1}{2}(c+dx)]}{(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^3} - \right. \\ \left. \frac{32}{(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^2} + \frac{136 \sin[\frac{1}{2}(c+dx)]}{\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)]} + \right. \\ 246 \sin[\frac{1}{2}(c+dx)] \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right) - \\ 123 \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^2 + (315 + 315 \frac{i}{2}) (-1)^{3/4} \\ \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan[\frac{1}{4}(c+dx)] \right) \right] \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^3 + \\ \left. \frac{32 \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^3}{(\cos[\frac{1}{2}(c+dx)] - \sin[\frac{1}{2}(c+dx)])^3} + \frac{192 \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^3}{\cos[\frac{1}{2}(c+dx)] - \sin[\frac{1}{2}(c+dx)]} \right)$$

### Problem 180: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sec [c + d x]^5}{(a + a \sin [c + d x])^{3/2}} dx$$

Optimal (type 3, 211 leaves, 9 steps):

$$\begin{aligned} & \frac{99 \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{256 \sqrt{2} a^{3/2} d} - \frac{33}{128 d (a+a \sin [c+d x])^{3/2}} - \\ & \frac{99 \sec [c+d x]^2}{560 d (a+a \sin [c+d x])^{3/2}} - \frac{\sec [c+d x]^4}{7 d (a+a \sin [c+d x])^{3/2}} - \\ & \frac{99}{256 a d \sqrt{a+a \sin [c+d x]}} + \frac{99 \sec [c+d x]^2}{320 a d \sqrt{a+a \sin [c+d x]}} + \frac{11 \sec [c+d x]^4}{56 a d \sqrt{a+a \sin [c+d x]}} \end{aligned}$$

Result (type 3, 376 leaves):

$$\begin{aligned} & \frac{1}{8960 d (a (1 + \sin [c + d x]))^{3/2}} \\ & \left( -1120 - \frac{320}{(\cos [\frac{1}{2} (c + d x)] + \sin [\frac{1}{2} (c + d x)])^4} - \frac{672}{(\cos [\frac{1}{2} (c + d x)] + \sin [\frac{1}{2} (c + d x)])^2} - \right. \\ & 2800 \left( \cos [\frac{1}{2} (c + d x)] + \sin [\frac{1}{2} (c + d x)] \right)^2 - (3465 + 3465 i) (-1)^{1/4} \\ & \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4} (c + d x)\right]\right)\right] \left(\cos [\frac{1}{2} (c + d x)] + \sin [\frac{1}{2} (c + d x)]\right)^3 + \\ & 140 \left(\cos [\frac{1}{2} (c + d x)] + \sin [\frac{1}{2} (c + d x)]\right)^3 + \frac{665 \left(\cos [\frac{1}{2} (c + d x)] + \sin [\frac{1}{2} (c + d x)]\right)^3}{\cos [\frac{1}{2} (c + d x)] - \sin [\frac{1}{2} (c + d x)]} + \\ & 280 \sin [\frac{1}{2} (c + d x)] \left(\cos [\frac{1}{2} (c + d x)] + \sin [\frac{1}{2} (c + d x)]\right)^3 + \\ & \left. \left(\cos [\frac{1}{2} (c + d x)] - \sin [\frac{1}{2} (c + d x)]\right)^4 \right. \\ & \frac{1330 \sin [\frac{1}{2} (c + d x)] \left(\cos [\frac{1}{2} (c + d x)] + \sin [\frac{1}{2} (c + d x)]\right)^3}{\left(\cos [\frac{1}{2} (c + d x)] - \sin [\frac{1}{2} (c + d x)]\right)^2} \end{aligned}$$

### Problem 181: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sec [c + d x]^6}{(a + a \sin [c + d x])^{3/2}} dx$$

Optimal (type 3, 256 leaves, 9 steps):

$$\begin{aligned}
& -\frac{3003 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{8192 \sqrt{2} a^{3/2} d}-\frac{3003 \cos [c+d x]}{8192 d (a+a \sin [c+d x])^{3/2}}- \\
& \frac{1001 \sec [c+d x]}{5120 d (a+a \sin [c+d x])^{3/2}}-\frac{143 \sec [c+d x]^3}{960 d (a+a \sin [c+d x])^{3/2}}-\frac{\sec [c+d x]^5}{8 d (a+a \sin [c+d x])^{3/2}}+ \\
& \frac{1001 \sec [c+d x]}{2048 a d \sqrt{a+a \sin [c+d x]}}+\frac{143 \sec [c+d x]^3}{640 a d \sqrt{a+a \sin [c+d x]}}+\frac{13 \sec [c+d x]^5}{80 a d \sqrt{a+a \sin [c+d x]}}
\end{aligned}$$

Result (type 3, 444 leaves):

$$\begin{aligned}
& \frac{1}{122880 d (a (1+\sin [c+d x]))^{3/2}} \\
& \left( -8860 + \frac{3840 \sin \left[\frac{1}{2} (c+d x)\right]}{\left(\cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right]\right)^5} - \frac{1920}{\left(\cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right]\right)^4} + \right. \\
& \frac{9920 \sin \left[\frac{1}{2} (c+d x)\right]}{\left(\cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right]\right)^3} - \frac{4960}{\left(\cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right]\right)^2} + \\
& \frac{17720 \sin \left[\frac{1}{2} (c+d x)\right]}{\cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right]} + 32490 \sin \left[\frac{1}{2} (c+d x)\right] \\
& \left. \left( \cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right] \right) - 16245 \left( \cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right] \right)^2 + \right. \\
& \left( 45045 + 45045 i \right) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c+d x)\right]\right)\right] \\
& \left( \cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right] \right)^3 + \frac{1536 \left( \cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right] \right)^3}{\left( \cos \left[\frac{1}{2} (c+d x)\right] - \sin \left[\frac{1}{2} (c+d x)\right] \right)^5} + \\
& \frac{6400 \left( \cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right] \right)^3}{\left( \cos \left[\frac{1}{2} (c+d x)\right] - \sin \left[\frac{1}{2} (c+d x)\right] \right)^3} + \frac{28800 \left( \cos \left[\frac{1}{2} (c+d x)\right] + \sin \left[\frac{1}{2} (c+d x)\right] \right)^3}{\cos \left[\frac{1}{2} (c+d x)\right] - \sin \left[\frac{1}{2} (c+d x)\right]}
\end{aligned}$$

Problem 182: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^{10}}{(a+a \sin [c+d x])^{5/2}} d x$$

Optimal (type 3, 95 leaves, 3 steps):

$$-\frac{64 a^3 \cos [c+d x]^{11}}{2145 d (a+a \sin [c+d x])^{11/2}}-\frac{16 a^2 \cos [c+d x]^{11}}{195 d (a+a \sin [c+d x])^{9/2}}-\frac{2 a \cos [c+d x]^{11}}{15 d (a+a \sin [c+d x])^{7/2}}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
& - \frac{45 \cos\left[\frac{1}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5}{64 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{65 \cos\left[\frac{3}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5}{192 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{\cos\left[\frac{5}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5}{320 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{5 \cos\left[\frac{7}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5}{64 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{5 \cos\left[\frac{9}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5}{192 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{5 \cos\left[\frac{11}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5}{704 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{5 \cos\left[\frac{13}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5}{832 d (a (1 + \sin[c + d x]))^{5/2}} - \\
& \frac{\cos\left[\frac{15}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5}{960 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{45 \sin\left[\frac{1}{2}(c + d x)\right] \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5}{64 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{65 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5 \sin\left[\frac{3}{2}(c + d x)\right]}{192 d (a (1 + \sin[c + d x]))^{5/2}} - \\
& \frac{\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5 \sin\left[\frac{5}{2}(c + d x)\right]}{320 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{5 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5 \sin\left[\frac{7}{2}(c + d x)\right]}{64 d (a (1 + \sin[c + d x]))^{5/2}} - \\
& \frac{5 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5 \sin\left[\frac{9}{2}(c + d x)\right]}{192 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{5 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5 \sin\left[\frac{11}{2}(c + d x)\right]}{704 d (a (1 + \sin[c + d x]))^{5/2}} - \\
& \frac{5 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^5 \sin\left[\frac{13}{2}(c + d x)\right]}{832 d (a (1 + \sin[c + d x]))^{5/2}} -
\end{aligned}$$

$$\frac{(\cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)])^5 \sin[\frac{15}{2}(c+dx)]}{960d(a(1+\sin[c+dx]))^{5/2}}$$

Problem 183: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^9}{(a+a \sin[c+dx])^{5/2}} dx$$

Optimal (type 3, 121 leaves, 3 steps):

$$\begin{aligned} & \frac{32(a+a \sin[c+dx])^{5/2}}{5a^5d} - \frac{64(a+a \sin[c+dx])^{7/2}}{7a^6d} + \\ & \frac{16(a+a \sin[c+dx])^{9/2}}{3a^7d} - \frac{16(a+a \sin[c+dx])^{11/2}}{11a^8d} + \frac{2(a+a \sin[c+dx])^{13/2}}{13a^9d} \end{aligned}$$

Result (type 3, 757 leaves):

$$\begin{aligned}
& \frac{9 \cos\left[\frac{1}{2} (c + d x)\right] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5}{8 d (a (1 + \sin[c + d x]))^{5/2}} - \\
& \frac{3 \cos\left[\frac{3}{2} (c + d x)\right] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5}{32 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{29 \cos\left[\frac{5}{2} (c + d x)\right] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5}{160 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{5 \cos\left[\frac{7}{2} (c + d x)\right] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5}{112 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{\cos\left[\frac{9}{2} (c + d x)\right] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5}{48 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{5 \cos\left[\frac{11}{2} (c + d x)\right] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5}{352 d (a (1 + \sin[c + d x]))^{5/2}} - \\
& \frac{\cos\left[\frac{13}{2} (c + d x)\right] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5}{416 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{9 \sin\left[\frac{1}{2} (c + d x)\right] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5}{8 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{3 \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5 \sin\left[\frac{3}{2} (c + d x)\right]}{32 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{29 \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5 \sin\left[\frac{5}{2} (c + d x)\right]}{160 d (a (1 + \sin[c + d x]))^{5/2}} - \\
& \frac{5 \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5 \sin\left[\frac{7}{2} (c + d x)\right]}{112 d (a (1 + \sin[c + d x]))^{5/2}} + \\
& \frac{\left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5 \sin\left[\frac{9}{2} (c + d x)\right]}{48 d (a (1 + \sin[c + d x]))^{5/2}} - \\
& \frac{5 \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5 \sin\left[\frac{11}{2} (c + d x)\right]}{352 d (a (1 + \sin[c + d x]))^{5/2}} - \\
& \frac{\left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^5 \sin\left[\frac{13}{2} (c + d x)\right]}{416 d (a (1 + \sin[c + d x]))^{5/2}}
\end{aligned}$$

### Problem 186: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx]^6}{(a + a \sin[c + dx])^{5/2}} dx$$

Optimal (type 3, 30 leaves, 1 step):

$$-\frac{2 a \cos[c + dx]^7}{7 d (a + a \sin[c + dx])^{7/2}}$$

Result (type 3, 69 leaves):

$$-\left( \left( 2 \left( \cos\left[\frac{1}{2} (c + dx)\right] - \sin\left[\frac{1}{2} (c + dx)\right] \right)^7 \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right)^5 \right) \Big/ \left( 7 d (a (1 + \sin[c + dx]))^{5/2} \right)$$

### Problem 188: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos[c + dx]^4}{(a + a \sin[c + dx])^{5/2}} dx$$

Optimal (type 3, 108 leaves, 4 steps):

$$-\frac{4 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+d x]}{\sqrt{2} \sqrt{a+a \sin[c+d x]}}\right]}{a^{5/2} d} + \frac{2 \cos[c + dx]^3}{3 a d (a + a \sin[c + dx])^{3/2}} + \frac{4 \cos[c + dx]}{a^2 d \sqrt{a + a \sin[c + dx]}}$$

Result (type 3, 128 leaves):

$$\left( \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right)^5 \left( (24 + 24 i) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \operatorname{Tan}\left[\frac{1}{4} (c + dx)\right]\right)\right] + 15 \cos\left[\frac{1}{2} (c + dx)\right] - \cos\left[\frac{3}{2} (c + dx)\right] - 15 \sin\left[\frac{1}{2} (c + dx)\right] - \sin\left[\frac{3}{2} (c + dx)\right] \right) \Big/ \left( 3 d (a (1 + \sin[c + dx]))^{5/2} \right)$$

### Problem 190: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos[c + dx]^2}{(a + a \sin[c + dx])^{5/2}} dx$$

Optimal (type 3, 75 leaves, 3 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+d x]}{\sqrt{2} \sqrt{a+a \sin[c+d x]}}\right]}{\sqrt{2} a^{5/2} d} - \frac{\cos[c + dx]}{a d (a + a \sin[c + dx])^{3/2}}$$

Result (type 3, 108 leaves):

$$\begin{aligned}
& - \left( \left( \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right. \right. \\
& \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] + (1 + \frac{1}{2}) (-1)^{3/4} \operatorname{Arctanh} \left[ \left( \frac{1}{2} + \frac{1}{2} \right) (-1)^{3/4} \right. \right. \\
& \left. \left. \left( -1 + \tan \left[ \frac{1}{4} (c + d x) \right] \right] (1 + \sin [c + d x]) \right) \right) \Big/ \left( d (a (1 + \sin [c + d x]))^{5/2} \right)
\end{aligned}$$

**Problem 192: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c + d x]}{(a + a \sin [c + d x])^{5/2}} \, dx$$

Optimal (type 3, 113 leaves, 6 steps):

$$\begin{aligned}
& \frac{\operatorname{ArcTanh} \left[ \frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{2} \sqrt{a}} \right]}{4 \sqrt{2} a^{5/2} d} - \frac{1}{5 d (a + a \sin [c + d x])^{5/2}} - \\
& \frac{1}{6 a d (a + a \sin [c + d x])^{3/2}} - \frac{1}{4 a^2 d \sqrt{a + a \sin [c + d x]}}
\end{aligned}$$

Result (type 3, 131 leaves):

$$\begin{aligned}
& \left( -12 - 10 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 - 15 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 - \right. \\
& \left. (15 + 15 \frac{1}{2}) (-1)^{1/4} \operatorname{ArcTan} \left[ \left( \frac{1}{2} + \frac{1}{2} \right) (-1)^{1/4} \left( 1 + \tan \left[ \frac{1}{4} (c + d x) \right] \right) \right] \right. \\
& \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5 \right) \Big/ \left( 60 d (a (1 + \sin [c + d x]))^{5/2} \right)
\end{aligned}$$

**Problem 193: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c + d x]^2}{(a + a \sin [c + d x])^{5/2}} \, dx$$

Optimal (type 3, 167 leaves, 6 steps):

$$\begin{aligned}
& - \frac{35 \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}} \right]}{128 \sqrt{2} a^{5/2} d} - \frac{\sec [c + d x]}{6 d (a + a \sin [c + d x])^{5/2}} - \\
& \frac{35 \cos [c + d x]}{128 a d (a + a \sin [c + d x])^{3/2}} - \frac{7 \sec [c + d x]}{48 a d (a + a \sin [c + d x])^{3/2}} + \frac{35 \sec [c + d x]}{96 a^2 d \sqrt{a + a \sin [c + d x]}}
\end{aligned}$$

Result (type 3, 284 leaves):

$$\begin{aligned}
& \frac{1}{384 d (a (1 + \sin[c + d x]))^{5/2}} \left( -32 + \frac{64 \sin[\frac{1}{2} (c + d x)]}{\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)]} + \right. \\
& 88 \sin[\frac{1}{2} (c + d x)] \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right) - \\
& 44 \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^2 + 114 \sin[\frac{1}{2} (c + d x)] \\
& \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^3 - 57 \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^4 + \\
& (105 + 105 i) (-1)^{3/4} \operatorname{ArcTanh} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left( -1 + \tan[\frac{1}{4} (c + d x)] \right) \right] \\
& \left. \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^5 + \frac{48 \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^5}{\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)]} \right)
\end{aligned}$$

**Problem 194: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec[c + d x]^3}{(a + a \sin[c + d x])^{5/2}} dx$$

Optimal (type 3, 185 leaves, 8 steps):

$$\begin{aligned}
& \frac{9 \operatorname{ArcTanh} \left[ \frac{\sqrt{a + a \sin[c + d x]}}{\sqrt{2} \sqrt{a}} \right]}{32 \sqrt{2} a^{5/2} d} - \frac{\sec[c + d x]^2}{7 d (a + a \sin[c + d x])^{5/2}} - \frac{3}{16 a d (a + a \sin[c + d x])^{3/2}} - \\
& \frac{9 \sec[c + d x]^2}{70 a d (a + a \sin[c + d x])^{3/2}} - \frac{9}{32 a^2 d \sqrt{a + a \sin[c + d x]}} + \frac{9 \sec[c + d x]^2}{40 a^2 d \sqrt{a + a \sin[c + d x]}}
\end{aligned}$$

Result (type 3, 266 leaves):

$$\begin{aligned}
& \frac{1}{1120 d (a (1 + \sin[c + d x]))^{5/2}} \left( -112 - \frac{80}{\left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^2} - \right. \\
& 140 \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^2 - 280 \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^4 - \\
& (315 + 315 i) (-1)^{1/4} \operatorname{ArcTan} \left[ \left( \frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left( 1 + \tan[\frac{1}{4} (c + d x)] \right) \right] \\
& \left. \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^5 + \frac{35 \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^5}{\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)]} + \right. \\
& \left. \frac{70 \sin[\frac{1}{2} (c + d x)] \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^5}{\left( \cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)] \right)^2} \right)
\end{aligned}$$

### Problem 195: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sec^4(c + dx)}{(a + a \sin(c + dx))^{5/2}} \, dx$$

Optimal (type 3, 233 leaves, 8 steps):

$$\begin{aligned} & -\frac{1155 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos(c+d x)}{\sqrt{2} \sqrt{a+a \sin(c+d x)}}\right]}{4096 \sqrt{2} a^{5/2} d} - \frac{\sec^3(c + dx)}{8 d (a + a \sin(c + dx))^{5/2}} - \\ & \frac{1155 \cos(c + dx)}{4096 a d (a + a \sin(c + dx))^{3/2}} - \frac{77 \sec(c + dx)}{512 a d (a + a \sin(c + dx))^{3/2}} - \\ & \frac{11 \sec^3(c + dx)}{96 a d (a + a \sin(c + dx))^{3/2}} + \frac{385 \sec(c + dx)}{1024 a^2 d \sqrt{a + a \sin(c + dx)}} + \frac{11 \sec^3(c + dx)}{64 a^2 d \sqrt{a + a \sin(c + dx)}} \end{aligned}$$

Result (type 3, 394 leaves):

$$\begin{aligned} & \frac{1}{12288 d (a (1 + \sin(c + dx))^{5/2})} \\ & \left( -736 + \frac{768 \sin\left(\frac{1}{2} (c + dx)\right)}{\left(\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)\right)^3} - \frac{384}{\left(\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)\right)^2} + \right. \\ & \frac{1472 \sin\left(\frac{1}{2} (c + dx)\right)}{\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)} + 2072 \sin\left(\frac{1}{2} (c + dx)\right) \\ & \left. \left(\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)\right) - 1036 \left(\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)\right)^2 + \right. \\ & 3090 \sin\left(\frac{1}{2} (c + dx)\right) \left(\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)\right)^3 - \\ & 1545 \left(\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)\right)^4 + (3465 + 3465 i) (-1)^{3/4} \\ & \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left(\frac{1}{4} (c + dx)\right)\right)\right] \left(\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)\right)^5 + \\ & 256 \left(\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)\right)^5 + \frac{1920 \left(\cos\left(\frac{1}{2} (c + dx)\right) + \sin\left(\frac{1}{2} (c + dx)\right)\right)^5}{\cos\left(\frac{1}{2} (c + dx)\right) - \sin\left(\frac{1}{2} (c + dx)\right)} \end{aligned}$$

### Problem 197: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \cos(c + dx))^{5/2} (a + a \sin(c + dx)) \, dx$$

Optimal (type 4, 95 leaves, 4 steps):

$$-\frac{2 a (\cos[c+d x])^{7/2}}{7 d e} + \frac{6 a e^2 \sqrt{\cos[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (\cos[c+d x]), 2\right]}{5 d \sqrt{\cos[c+d x]}} + \frac{2 a e (\cos[c+d x])^{3/2} \sin[c+d x]}{5 d}$$

Result (type 5, 264 leaves):

$$\frac{1}{560 d \sqrt{\cos[c+d x]}} \left( a e^3 \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \left( -154 \cos[d x] - 182 \cos[2 c + d x] + 14 \cos[2 c + 3 d x] - 14 \cos[4 c + 3 d x] - 30 \sin[c] + 168 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] (\cos[d x] - i \sin[d x]) \sqrt{1 + \cos[2(c + d x)] + i \sin[2(c + d x)]} + 56 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] (\cos[d x] + i \sin[d x]) \sqrt{1 + \cos[2(c + d x)] + i \sin[2(c + d x)]} + 20 \sin[c + 2 d x] - 20 \sin[3 c + 2 d x] + 5 \sin[3 c + 4 d x] - 5 \sin[5 c + 4 d x] \right) \right)$$

Problem 199: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{\cos[c+d x]} (a + a \sin[c+d x]) \, dx$$

Optimal (type 4, 63 leaves, 3 steps):

$$-\frac{2 a (\cos[c+d x])^{3/2}}{3 d e} + \frac{2 a \sqrt{\cos[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (\cos[c+d x]), 2\right]}{d \sqrt{\cos[c+d x]}}$$

Result (type 5, 260 leaves):

$$\frac{1}{6 d \left( (1 + e^{2 i d x}) \cos[c] + i (-1 + e^{2 i d x}) \sin[c] \right)} \left( a \sqrt{\cos[c+d x]} \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] (\cos[d x] + i \sin[d x]) \left( -6 \cos[d x] - 6 \cos[2 c + d x] - 2 \sin[c] + 6 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] (\cos[d x] - i \sin[d x]) \sqrt{1 + \cos[2(c + d x)] + i \sin[2(c + d x)]} + 2 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] (\cos[d x] + i \sin[d x]) \sqrt{1 + \cos[2(c + d x)] + i \sin[2(c + d x)]} + \sin[c + 2 d x] - \sin[3 c + 2 d x] \right) \right)$$

Problem 201: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{a + a \sin[c + d x]}{(e \cos[c + d x])^{3/2}} dx$$

Optimal (type 4, 91 leaves, 4 steps):

$$\frac{2 a}{d e \sqrt{e \cos[c + d x]}} - \frac{2 a \sqrt{e \cos[c + d x]} \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{d e^2 \sqrt{\cos[c + d x]}} + \frac{2 a \sin[c + d x]}{d e \sqrt{e \cos[c + d x]}}$$

Result (type 5, 188 leaves):

$$\begin{aligned} & -\frac{1}{6 d e \sqrt{e \cos[c + d x]}} a \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \\ & \left( -6 (\cos[d x] + \sin[c]) + 3 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\ & \quad (\cos[d x] - i \sin[d x]) \sqrt{1 + \cos[2 (c + d x)] + i \sin[2 (c + d x)]} + \\ & \quad \left. \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\ & \quad \left. (\cos[d x] + i \sin[d x]) \sqrt{1 + \cos[2 (c + d x)] + i \sin[2 (c + d x)]} \right) \end{aligned}$$

Problem 203: Result unnecessarily involves higher level functions.

$$\int \frac{a + a \sin[c + d x]}{(e \cos[c + d x])^{7/2}} dx$$

Optimal (type 4, 126 leaves, 5 steps):

$$\begin{aligned} & \frac{2 a}{5 d e (e \cos[c + d x])^{5/2}} - \frac{6 a \sqrt{e \cos[c + d x]} \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 d e^4 \sqrt{\cos[c + d x]}} + \\ & \frac{2 a \sin[c + d x]}{5 d e (e \cos[c + d x])^{5/2}} + \frac{6 a \sin[c + d x]}{5 d e^3 \sqrt{e \cos[c + d x]}} \end{aligned}$$

Result (type 5, 160 leaves):

$$\begin{aligned} & \left( 2 a \sqrt{e \cos[c + d x]} (\cos[c + d x] - i \sin[c + d x]) \left( 3 i + \cos[c + d x] + 3 i \sqrt{1 + e^{2 i (c + d x)}} \right. \right. \\ & \quad \left. \left. \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)}\right] (-1 + \sin[c + d x]) - 2 i \sin[c + d x] \right) \right) / \\ & \left( 5 d e^4 \left( \cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right] \right)^3 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right) \right) \end{aligned}$$

Problem 210: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^2}{(e \cos[c + d x])^{5/2}} dx$$

Optimal (type 4, 89 leaves, 4 steps):

$$-\frac{2 a^2 \sqrt{\cos[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{3 d e^2 \sqrt{e \cos[c+d x]}} + \frac{4 a^4 \sqrt{e \cos[c+d x]}}{3 d e^3 (a^2 - a^2 \sin[c+d x])}$$

Result (type 4, 1198 leaves):

$$\begin{aligned} & \frac{\cos[c+d x]^3 \left( -\frac{2}{3} + \frac{4}{3 (\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])^2} \right) (a + a \sin[c+d x])^2}{d (e \cos[c+d x])^{5/2} (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^4} + \\ & \left( 2 \cos[c+d x]^2 \left( -\frac{\cos[\frac{1}{2} (c+d x)] \sqrt{\cos[c+d x]}}{3 (\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])} - \right. \right. \\ & \left. \left. \frac{\sqrt{\cos[c+d x]} \sin[\frac{1}{2} (c+d x)]}{3 (\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])} \right) (a + a \sin[c+d x])^2 \right. \\ & \left( \cos[c+d x] - 2 \sqrt{2} \cos[\frac{1}{4} (c+d x)]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1 + \cos[\frac{1}{2} (c+d x)]}} \right. \\ & \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right) \right) / \\ & \left( 3 d (e \cos[c+d x])^{5/2} \left( \cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)] \right)^4 \right. \\ & \left( \left( \sin[c+d x] \left( \cos[c+d x] - 2 \sqrt{2} \cos[\frac{1}{4} (c+d x)]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1 + \cos[\frac{1}{2} (c+d x)]}} \right. \right. \right. \\ & \left. \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right. \right. \\ & \left. \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right) \right) \right) / (3 \cos[c+d x]^{3/2}) + \\ & \frac{1}{3 \sqrt{\cos[c+d x]}} 2 \left( -\sin[c+d x] + \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1 + \cos[\frac{1}{2} (c+d x)]}} \right. \right. \end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{\operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right) \right) \\
& \left( \sqrt{2} \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} + \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right] \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], \right. \right. \\
& 17 - 12 \sqrt{2} \left. \sin \left[ \frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right. - \\
& \left. \left. \left( \sqrt{2} \cos \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \right. \\
& \left. \left. \left( \frac{(-2 + \sqrt{2}) \sin \left[ \frac{1}{2} (c + d x) \right]}{2 (1 + \cos \left[ \frac{1}{2} (c + d x) \right])} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]) \right. \right. \right. \right. \\
& \left. \left. \left. \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) \right) \right) \left/ \left( 2 \left( 1 + \cos \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) \right) \\
& \left. \left( \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right) \left/ \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \right) \right. - \\
& \left. \left. \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right) \right) \\
& \left( \sqrt{2 (3 - 2 \sqrt{2})} \sqrt{1 - \frac{\tan \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2 \sqrt{2}}} \right) \right) \right)
\end{aligned}$$

Problem 212: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin [c + d x])^2}{(e \cos [c + d x])^{9/2}} dx$$

Optimal (type 4, 114 leaves, 4 steps):

$$\frac{2 a^2 \sqrt{\cos[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{7 d e^4 \sqrt{e \cos[c+d x]}} + \frac{2 a^2 \sin[c+d x]}{7 d e^3 (e \cos[c+d x])^{3/2}} + \frac{4 (a^2 + a^2 \sin[c+d x])}{7 d e (e \cos[c+d x])^{7/2}}$$

Result (type 4, 1227 leaves):

$$\begin{aligned} & \left( \cos[c+d x]^5 \right. \\ & \left. \left( \frac{2}{7} + \frac{2}{7 (\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])^4} + \frac{2}{7 (\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])^2} \right. \right. \\ & \left. \left. (a + a \sin[c+d x])^2 \right) \right/ \left( d (e \cos[c+d x])^{9/2} \left( \cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)] \right)^4 \right) - \\ & \left( 2 \cos[c+d x]^4 \left( \frac{\cos[\frac{1}{2} (c+d x)] \sqrt{\cos[c+d x]}}{7 (\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])} + \frac{\sqrt{\cos[c+d x]} \sin[\frac{1}{2} (c+d x)]}{7 (\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])} \right) \right. \\ & \left. (a + a \sin[c+d x])^2 \right. \\ & \left. \left( \cos[c+d x] - 2 \sqrt{2} \cos[\frac{1}{4} (c+d x)]^2 \right. \right. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1 + \cos[\frac{1}{2} (c+d x)]}} \\ & \left. \left. \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right) \right) \right/ \\ & \left( 7 d (e \cos[c+d x])^{9/2} \left( \cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)] \right)^4 \right. \\ & \left. \left( - \left( \sin[c+d x] \left( \cos[c+d x] - 2 \sqrt{2} \cos[\frac{1}{4} (c+d x)]^2 \right. \right. \right. \right. \\ & \left. \left. \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1 + \cos[\frac{1}{2} (c+d x)]}} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], \right. \right. \right. \right. \\ & \left. \left. \left. \left. 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right) \right) \right/ (7 \cos[c+d x]^{3/2}) \right) - \end{aligned}$$

$$\begin{aligned}
& \frac{1}{7 \sqrt{\cos[c + d x]}} 2 \left( -\sin[c + d x] + \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right. \right. \\
& \left. \left. \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \tan[\frac{1}{4} (c + d x)] \right) \right) / \\
& \left( \sqrt{2} \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) + \sqrt{2} \cos[\frac{1}{4} (c + d x)] \\
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], \\
& 17 - 12 \sqrt{2}] \sin[\frac{1}{4} (c + d x)] \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} - \\
& \left( \sqrt{2} \cos[\frac{1}{4} (c + d x)]^2 \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \right. \\
& \left( \frac{(-2 + \sqrt{2}) \sin[\frac{1}{2} (c + d x)]}{2 (1 + \cos[\frac{1}{2} (c + d x)])} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]) \right. \right. \\
& \left. \left. \sin[\frac{1}{2} (c + d x)] \right) \right) / \left( 2 \left( 1 + \cos[\frac{1}{2} (c + d x)] \right)^2 \right) \\
& \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) / \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right) - \\
& \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) / \\
& \left( \sqrt{2 (3 - 2 \sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \right) \left. \right)
\end{aligned}$$

Problem 222: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^3}{(e \cos[c + d x])^{9/2}} dx$$

Optimal (type 4, 127 leaves, 5 steps):

$$-\frac{2 a^3 \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{21 d e^4 \sqrt{e \cos[c + d x]}} +$$

$$-\frac{4 a^5 \sqrt{e \cos[c + d x]}}{7 d e^5 (a - a \sin[c + d x])^2} - \frac{2 a^6 \sqrt{e \cos[c + d x]}}{21 d e^5 (a^3 - a^3 \sin[c + d x])}$$

Result (type 4, 1227 leaves):

$$\begin{aligned} & \left( \cos[c + d x]^5 \right. \\ & \left. - \frac{2}{21} + \frac{4}{7 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^4} - \frac{2}{21 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^2} \right. \\ & \left. (a + a \sin[c + d x])^3 \right) \Big/ \left( d (e \cos[c + d x])^{9/2} \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^6 \right) + \\ & \left( 2 \cos[c + d x]^4 \left( - \frac{\cos[\frac{1}{2} (c + d x)] \sqrt{\cos[c + d x]}}{21 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])} - \right. \right. \\ & \left. \left. \frac{\sqrt{\cos[c + d x]} \sin[\frac{1}{2} (c + d x)]}{21 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])} \right) (a + a \sin[c + d x])^3 \right. \\ & \left. \left( \cos[c + d x] - 2 \sqrt{2} \cos[\frac{1}{4} (c + d x)]^2 \right) \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right. \\ & \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) \Big/ \\ & \left( 21 d (e \cos[c + d x])^{9/2} \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^6 \right. \\ & \left. \left( \sin[c + d x] \left( \cos[c + d x] - 2 \sqrt{2} \cos[\frac{1}{4} (c + d x)]^2 \right) \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right) \right) \end{aligned}$$

$$\begin{aligned}
& \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left(\frac{1}{4}(c+d x)\right)}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \\
& \sqrt{3-2 \sqrt{2}-\tan\left(\frac{1}{4}(c+d x)\right)^2}\Bigg)\Bigg) \Bigg/ \left(21 \cos [(c+d x)]^{3/2}\right) + \\
& \frac{1}{21 \sqrt{\cos [(c+d x)]}} 2 \left(-\sin [(c+d x)]+\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}}\right. \\
& \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left(\frac{1}{4}(c+d x)\right)}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \tan\left[\frac{1}{4}(c+d x)\right]\Bigg) \Bigg) \\
& \left(\sqrt{2} \sqrt{3-2 \sqrt{2}-\tan\left(\frac{1}{4}(c+d x)\right)^2}\right) + \sqrt{2} \cos \left[\frac{1}{4}(c+d x)\right] \\
& \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left(\frac{1}{4}(c+d x)\right)}{\sqrt{3-2 \sqrt{2}}}\right],\right. \\
& 17-12 \sqrt{2}\Big] \sin \left[\frac{1}{4}(c+d x)\right] \sqrt{3-2 \sqrt{2}-\tan\left(\frac{1}{4}(c+d x)\right)^2}- \\
& \left.\left(\sqrt{2} \cos \left[\frac{1}{4}(c+d x)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left(\frac{1}{4}(c+d x)\right)}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]\right.\right. \\
& \left.\left(\frac{(-2+\sqrt{2}) \sin \left[\frac{1}{2}(c+d x)\right]}{2 \left(1+\cos \left[\frac{1}{2}(c+d x)\right]\right)}+\left((-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]\right)\right.\right. \\
& \left.\left.\sin \left[\frac{1}{2}(c+d x)\right]\right)\right) \Bigg/ \left(2 \left(1+\cos \left[\frac{1}{2}(c+d x)\right]\right)^2\right)\Bigg) \\
& \sqrt{3-2 \sqrt{2}-\tan\left(\frac{1}{4}(c+d x)\right)^2}\Bigg) \Bigg/ \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}}\Bigg)- \\
& \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \sqrt{3-2 \sqrt{2}-\tan\left(\frac{1}{4}(c+d x)\right)^2}\right)\Bigg)
\end{aligned}$$

$$\left( \sqrt{2 (3 - 2 \sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \right) \right)$$

Problem 230: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^4}{(e \cos[c + d x])^{9/2}} dx$$

Optimal (type 4, 127 leaves, 5 steps) :

$$\frac{10 a^4 \sqrt{\cos[c + d x]} \text{EllipticF}[\frac{1}{2} (c + d x), 2]}{21 d e^4 \sqrt{e \cos[c + d x]}} + \frac{4 a^7 (e \cos[c + d x])^{5/2}}{7 d e^7 (a - a \sin[c + d x])^3} - \frac{20 a^8 \sqrt{e \cos[c + d x]}}{21 d e^5 (a^4 - a^4 \sin[c + d x])}$$

Result (type 4, 1227 leaves) :

$$\begin{aligned} & \left( \cos[c + d x]^5 \right. \\ & \left( \frac{10}{21} + \frac{8}{7 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^4} - \frac{32}{21 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^2} \right. \\ & \left. (a + a \sin[c + d x])^4 \right) \Big/ \left( d (e \cos[c + d x])^{9/2} \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^8 \right) - \\ & \left( 10 \cos[c + d x]^4 \left( \frac{5 \cos[\frac{1}{2} (c + d x)] \sqrt{\cos[c + d x]}}{21 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])} + \right. \right. \\ & \left. \left. \frac{5 \sqrt{\cos[c + d x]} \sin[\frac{1}{2} (c + d x)]}{21 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])} \right) (a + a \sin[c + d x])^4 \right. \\ & \left( \cos[c + d x] - 2 \sqrt{2} \cos[\frac{1}{4} (c + d x)]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right. \\ & \left. \text{EllipticF}[\text{ArcSin}[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}], 17 - 12 \sqrt{2}] \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) \Big/ \end{aligned}$$

$$\begin{aligned}
& \left( 21 d (e \cos[c + d x])^{9/2} \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^8 \right. \\
& \left. - \left( \left( 5 \sin[c + d x] \left( \cos[c + d x] - 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \right. \right. \right. \right. \\
& \left. \left. \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], \right. \right. \right. \right. \\
& \left. \left. \left. \left. 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) \right) \right) \left. \right/ (21 \cos[c + d x]^{3/2}) - \\
& \frac{1}{21 \sqrt{\cos[c + d x]}} 10 \left( -\sin[c + d x] + \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]} \right. \right. \right. \\
& \left. \left. \left. \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \tan\left[\frac{1}{4} (c + d x)\right] \right) \right) \right) \left. \right/ \\
& \left( \sqrt{2} \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} + \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right] \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]} \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], \right. \\
& \left. 17 - 12 \sqrt{2}\right] \sin\left[\frac{1}{4} (c + d x)\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} - \\
& \left. \left( \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right. \\
& \left. \left( \frac{(-2 + \sqrt{2}) \sin\left[\frac{1}{2} (c + d x)\right]}{2 (1 + \cos\left[\frac{1}{2} (c + d x)\right])} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]) \right. \right. \right. \\
& \left. \left. \left. \sin\left[\frac{1}{2} (c + d x)\right] \right) \right) \right) \right/ \left( 2 \left( 1 + \cos\left[\frac{1}{2} (c + d x)\right] \right)^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \Bigg/ \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} - \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \Bigg/ \\
& \left( \sqrt{2 (3 - 2 \sqrt{2})} \sqrt{1 - \frac{\tan\left[\frac{1}{4} (c + d x)\right]^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2}{3 - 2 \sqrt{2}}} \right) \Bigg)
\end{aligned}$$

**Problem 232: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[c + d x])^4}{(e \cos[c + d x])^{13/2}} dx$$

Optimal (type 4, 169 leaves, 6 steps):

$$\begin{aligned}
& -\frac{2 a^4 \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{77 d e^6 \sqrt{e \cos[c + d x]}} + \frac{4 a^7 \sqrt{e \cos[c + d x]}}{11 d e^7 (a - a \sin[c + d x])^3} - \\
& \frac{2 a^8 \sqrt{e \cos[c + d x]}}{77 d e^7 (a^2 - a^2 \sin[c + d x])^2} - \frac{2 a^8 \sqrt{e \cos[c + d x]}}{77 d e^7 (a^4 - a^4 \sin[c + d x])}
\end{aligned}$$

Result (type 4, 1256 leaves):

$$\begin{aligned}
& \left( \cos[c + d x]^7 \right. \\
& \left. - \frac{2}{77} + \frac{4}{11 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^6} - \frac{2}{77 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^4} - \right. \\
& \left. \frac{2}{77 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^2} \right) (a + a \sin[c + d x])^4 \Bigg/ \\
& \left( d (e \cos[c + d x])^{13/2} \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^8 \right) + \\
& \left( 2 \cos[c + d x]^6 \left( -\frac{\cos[\frac{1}{2} (c + d x)] \sqrt{\cos[c + d x]}}{77 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])} - \right. \right. \\
& \left. \left. \frac{\sqrt{\cos[c + d x]} \sin[\frac{1}{2} (c + d x)]}{77 (\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])} \right) (a + a \sin[c + d x])^4 \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \cos[c + dx] - 2\sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \\
& \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) \right\} / \\
& \left( 77d \left(e \cos[c + dx]\right)^{13/2} \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^8 \right. \\
& \left( \sin[c + dx] \left( \cos[c + dx] - 2\sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \right. \\
& \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \\
& \left. \left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) \right) \right\} / (77 \cos[c + dx]^{3/2}) + \\
& \frac{1}{77\sqrt{\cos[c + dx]}} 2 \left( -\sin[c + dx] + \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \\
& \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \tan\left[\frac{1}{4}(c + dx)\right] \right) \right\} / \\
& \left( \sqrt{2} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} + \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right], \right. \\
& \left. 17 - 12\sqrt{2} \right] \sin\left[\frac{1}{4}(c + dx)\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} - \\
& \left. \left( \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{(-2 + \sqrt{2}) \sin[\frac{1}{2}(c + d x)]}{2(1 + \cos[\frac{1}{2}(c + d x)])} + \left( (-1 + \sqrt{2}) - (-2 + \sqrt{2}) \right) \cos[\frac{1}{2}(c + d x)] \right) \\
& \left. \sin[\frac{1}{2}(c + d x)] \right) \Big/ \left( 2 \left( 1 + \cos[\frac{1}{2}(c + d x)] \right)^2 \right) \\
& \sqrt{3 - 2\sqrt{2} - \tan[\frac{1}{4}(c + d x)]^2} \Bigg) \Bigg/ \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2}(c + d x)]}{1 + \cos[\frac{1}{2}(c + d x)]}} \right) - \\
& \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2}(c + d x)]}{1 + \cos[\frac{1}{2}(c + d x)]}} \sqrt{3 - 2\sqrt{2} - \tan[\frac{1}{4}(c + d x)]^2} \right) \Bigg/ \\
& \left( \sqrt{2(3 - 2\sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4}(c + d x)]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \tan[\frac{1}{4}(c + d x)]^2}{3 - 2\sqrt{2}}} \right) \Bigg) \Bigg)
\end{aligned}$$

**Problem 237: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \cos[c + d x])^{3/2}}{a + a \sin[c + d x]} \, dx$$

Optimal (type 4, 66 leaves, 3 steps):

$$\frac{2 e \sqrt{e \cos[c + d x]}}{a d} + \frac{2 e^2 \sqrt{\cos[c + d x]} \operatorname{EllipticF}[\frac{1}{2}(c + d x), 2]}{a d \sqrt{e \cos[c + d x]}}$$

Result (type 4, 1089 leaves):

$$\begin{aligned}
& \left( 2(e \cos[c + d x])^{3/2} \sec[c + d x]^2 \left( \cos[\frac{1}{2}(c + d x)] + \sin[\frac{1}{2}(c + d x)] \right)^2 \right. \\
& \left( \frac{\cos[\frac{1}{2}(c + d x)] \sqrt{\cos[c + d x]}}{\cos[\frac{1}{2}(c + d x)] + \sin[\frac{1}{2}(c + d x)]} - \frac{\sqrt{\cos[c + d x]} \sin[\frac{1}{2}(c + d x)]}{\cos[\frac{1}{2}(c + d x)] + \sin[\frac{1}{2}(c + d x)]} \right) \\
& \left( \cos[c + d x] + 2\sqrt{2} \cos[\frac{1}{4}(c + d x)]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2}(c + d x)]}{1 + \cos[\frac{1}{2}(c + d x)]}} \right. \\
& \left. \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan[\frac{1}{4}(c + d x)]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}] \sqrt{3 - 2\sqrt{2} - \tan[\frac{1}{4}(c + d x)]^2} \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left( d \left( a + a \sin(c + d x) \right) \left( \frac{1}{\cos(c + d x)^{3/2}} \sin(c + d x) \right. \right. \\
& \left. \left. + \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos(\frac{1}{2}(c + d x))}{1 + \cos(\frac{1}{2}(c + d x))}} \right. \right. \\
& \left. \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan(\frac{1}{4}(c + d x))}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \sqrt{3 - 2\sqrt{2} - \tan(\frac{1}{4}(c + d x))^2} \right] + \right. \\
& \left. \frac{1}{\sqrt{\cos(c + d x)}} 2 \left( -\sin(c + d x) - \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos(\frac{1}{2}(c + d x))}{1 + \cos(\frac{1}{2}(c + d x))}} \right. \right. \\
& \left. \left. \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan(\frac{1}{4}(c + d x))}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \tan(\frac{1}{4}(c + d x)) \right) \right. \\
& \left. \left( \sqrt{2} \sqrt{3 - 2\sqrt{2} - \tan(\frac{1}{4}(c + d x))^2} - \sqrt{2} \cos(\frac{1}{4}(c + d x)) \right. \right. \\
& \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos(\frac{1}{2}(c + d x))}{1 + \cos(\frac{1}{2}(c + d x))}} \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan(\frac{1}{4}(c + d x))}{\sqrt{3 - 2\sqrt{2}}} \right], \right. \right. \\
& \left. \left. 17 - 12\sqrt{2} \right] \sin(\frac{1}{4}(c + d x)) \sqrt{3 - 2\sqrt{2} - \tan(\frac{1}{4}(c + d x))^2} + \right. \\
& \left. \left( \sqrt{2} \cos(\frac{1}{4}(c + d x))^2 \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan(\frac{1}{4}(c + d x))}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \right. \right. \\
& \left. \left. + \left( \frac{(-2 + \sqrt{2}) \sin(\frac{1}{2}(c + d x))}{2(1 + \cos(\frac{1}{2}(c + d x)))} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos(\frac{1}{2}(c + d x))) \right. \right. \right. \right. \\
& \left. \left. \left. \left. \sin(\frac{1}{2}(c + d x)) \right) \right) \right) \right) \left( 2 \left( 1 + \cos(\frac{1}{2}(c + d x)) \right)^2 \right) \right) \\
& \left. \left( \sqrt{3 - 2\sqrt{2} - \tan(\frac{1}{4}(c + d x))^2} \right) \right) \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos(\frac{1}{2}(c + d x))}{1 + \cos(\frac{1}{2}(c + d x))}} \right) +
\end{aligned}$$

$$\left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2}(c + dx)]}{1 + \cos[\frac{1}{2}(c + dx)]}} \sqrt{3 - 2\sqrt{2} - \tan[\frac{1}{4}(c + dx)]^2} \right) / \left( \sqrt{2(3 - 2\sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4}(c + dx)]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \tan[\frac{1}{4}(c + dx)]^2}{3 - 2\sqrt{2}}} \right) \right)$$

**Problem 239: Result more than twice size of optimal antiderivative.**

$$\int \frac{1}{\sqrt{e \cos[c + dx]} (a + a \sin[c + dx])} dx$$

Optimal (type 4, 78 leaves, 3 steps):

$$\frac{2 \sqrt{\cos[c + dx]} \operatorname{EllipticF}[\frac{1}{2}(c + dx), 2]}{3 a d \sqrt{e \cos[c + dx]}} - \frac{2 \sqrt{e \cos[c + dx]}}{3 d e (a + a \sin[c + dx])}$$

Result (type 4, 1182 leaves):

$$\begin{aligned} & \left( \cos[c + dx] \left( \cos[\frac{1}{2}(c + dx)] + \sin[\frac{1}{2}(c + dx)] \right)^2 \right. \\ & \left. - \frac{2}{3} - \frac{2}{3 \left( \cos[\frac{1}{2}(c + dx)] + \sin[\frac{1}{2}(c + dx)] \right)^2} \right) / \\ & \left( d \sqrt{e \cos[c + dx]} (a + a \sin[c + dx]) \right) + \left( 2 \left( \cos[\frac{1}{2}(c + dx)] + \sin[\frac{1}{2}(c + dx)] \right)^2 \right. \\ & \left. - \frac{\cos[\frac{1}{2}(c + dx)] \sqrt{\cos[c + dx]}}{3 \left( \cos[\frac{1}{2}(c + dx)] + \sin[\frac{1}{2}(c + dx)] \right)} - \frac{\sqrt{\cos[c + dx]} \sin[\frac{1}{2}(c + dx)]}{3 \left( \cos[\frac{1}{2}(c + dx)] + \sin[\frac{1}{2}(c + dx)] \right)} \right) \\ & \left( \cos[c + dx] + 2\sqrt{2} \cos[\frac{1}{4}(c + dx)]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2}(c + dx)]}{1 + \cos[\frac{1}{2}(c + dx)]}} \right. \\ & \left. \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan[\frac{1}{4}(c + dx)]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}] \sqrt{3 - 2\sqrt{2} - \tan[\frac{1}{4}(c + dx)]^2} \right) / \\ & \left( 3 d \sqrt{e \cos[c + dx]} (a + a \sin[c + dx]) \left( \sin[c + dx] \left( \cos[c + dx] + 2\sqrt{2} \cos[\frac{1}{4}(c + dx)]^2 \right. \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \\
& \left. 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \Bigg) \Bigg/ (3 \cos[c + dx]^{3/2}) + \\
& \frac{1}{3\sqrt{\cos[c + dx]}} 2 \left( -\sin[c + dx] - \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \\
& \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \tan\left[\frac{1}{4}(c + dx)\right] \right) \Bigg/ \\
& \left( \sqrt{2} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) - \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] \\
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \\
& \left. 17 - 12\sqrt{2}\right] \sin\left[\frac{1}{4}(c + dx)\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} + \\
& \left( \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \\
& \left( \frac{(-2 + \sqrt{2}) \sin\left[\frac{1}{2}(c + dx)\right]}{2(1 + \cos\left[\frac{1}{2}(c + dx)\right])} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]) \right. \right. \\
& \left. \left. \sin\left[\frac{1}{2}(c + dx)\right] \right) \Bigg/ \left( 2 \left( 1 + \cos\left[\frac{1}{2}(c + dx)\right] \right)^2 \right) \Bigg) \\
& \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \Bigg/ \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right) + \\
& \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \\
& \left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) \Bigg/
\end{aligned}$$

$$\left( \sqrt{2 (3 - 2 \sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \right) \right)$$

**Problem 247: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \cos[c + d x])^{3/2}}{(a + a \sin[c + d x])^2} dx$$

Optimal (type 4, 83 leaves, 3 steps):

$$- \frac{2 e^2 \sqrt{\cos[c + d x]} \text{EllipticF}[\frac{1}{2} (c + d x), 2]}{3 a^2 d \sqrt{e \cos[c + d x]}} - \frac{4 e \sqrt{e \cos[c + d x]}}{3 d (a^2 + a^2 \sin[c + d x])}$$

Result (type 4, 1190 leaves):

$$\begin{aligned} & \left( (e \cos[c + d x])^{3/2} \sec[c + d x] \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^4 \right. \\ & \left. \left( \frac{2}{3} - \frac{4}{3 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^2} \right) \right) \Big/ (d (a + a \sin[c + d x])^2) - \\ & \left( 2 (e \cos[c + d x])^{3/2} \sec[c + d x]^2 \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^4 \right. \\ & \left. \left( - \frac{\cos[\frac{1}{2} (c + d x)] \sqrt{\cos[c + d x]}}{3 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])} + \frac{\sqrt{\cos[c + d x]} \sin[\frac{1}{2} (c + d x)]}{3 (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])} \right) \right) \\ & \left( \cos[c + d x] + 2 \sqrt{2} \cos[\frac{1}{4} (c + d x)]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right. \\ & \left. \text{EllipticF}[\text{ArcSin}[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}], 17 - 12 \sqrt{2}] \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) \Big/ \\ & \left( 3 d (a + a \sin[c + d x])^2 \left( - \left( \sin[c + d x] \left( \cos[c + d x] + 2 \sqrt{2} \cos[\frac{1}{4} (c + d x)]^2 \right. \right. \right. \right. \right. \\ & \left. \left. \left. \left. \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \text{EllipticF}[\text{ArcSin}[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}], \right. \right. \right. \right. \right. \right) \right) \end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{17 - 12 \sqrt{2}}{\sqrt{3 - 2 \sqrt{2}}} \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} \right) \right/ (3 \cos[c + d x]^{3/2}) - \\
& \frac{1}{3 \sqrt{\cos[c + d x]}} 2 \left( -\sin[c + d x] - \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left(\frac{1}{2} (c + d x)\right)}{1 + \cos\left(\frac{1}{2} (c + d x)\right)}} \right. \right. \\
& \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left(\frac{1}{4} (c + d x)\right)}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \tan\left(\frac{1}{4} (c + d x)\right) \right) \right/ \\
& \left( \sqrt{2} \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} - \sqrt{2} \cos\left(\frac{1}{4} (c + d x)\right) \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left(\frac{1}{2} (c + d x)\right)}{1 + \cos\left(\frac{1}{2} (c + d x)\right)}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left(\frac{1}{4} (c + d x)\right)}{\sqrt{3 - 2 \sqrt{2}}}\right], \right. \\
& \left. \left. 17 - 12 \sqrt{2}\right] \sin\left(\frac{1}{4} (c + d x)\right) \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} + \right. \\
& \left. \left( \sqrt{2} \cos\left(\frac{1}{4} (c + d x)\right)^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left(\frac{1}{4} (c + d x)\right)}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right. \right. \\
& \left. \left. \left( \frac{(-2 + \sqrt{2}) \sin\left(\frac{1}{2} (c + d x)\right)}{2 (1 + \cos\left(\frac{1}{2} (c + d x)\right))} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left(\frac{1}{2} (c + d x)\right) \right. \right. \right. \right. \\
& \left. \left. \left. \left. \sin\left(\frac{1}{2} (c + d x)\right) \right) \right/ \left( 2 \left( 1 + \cos\left(\frac{1}{2} (c + d x)\right) \right)^2 \right) \right) \right. \\
& \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} \right) \right/ \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left(\frac{1}{2} (c + d x)\right)}{1 + \cos\left(\frac{1}{2} (c + d x)\right)}} \right. \right. \\
& \left. \left. \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left(\frac{1}{2} (c + d x)\right)}{1 + \cos\left(\frac{1}{2} (c + d x)\right)}} \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} \right) \right/ \right. \\
& \left. \left. \left. \left( \sqrt{\frac{\tan\left(\frac{1}{4} (c + d x)\right)^2}{2 (3 - 2 \sqrt{2})}} \sqrt{1 - \frac{\tan\left(\frac{1}{4} (c + d x)\right)^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan\left(\frac{1}{4} (c + d x)\right)^2}{3 - 2 \sqrt{2}}} \right) \right) \right) \right)
\end{aligned}$$

### Problem 249: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos[c + d x]} (a + a \sin[c + d x])^2} dx$$

Optimal (type 4, 116 leaves, 4 steps):

$$\frac{2 \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{7 a^2 d \sqrt{e \cos[c + d x]}} - \frac{2 \sqrt{e \cos[c + d x]}}{7 d e (a + a \sin[c + d x])^2} - \frac{2 \sqrt{e \cos[c + d x]}}{7 d e (a^2 + a^2 \sin[c + d x])}$$

Result (type 4, 1209 leaves):

$$\begin{aligned} & \left( \cos[c + d x] \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^4 \right. \\ & \left. - \frac{2}{7} - \frac{2}{7 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^4} - \frac{2}{7 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2} \right) / \\ & \left( d \sqrt{e \cos[c + d x]} (a + a \sin[c + d x])^2 \right) + \left( 2 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^4 \right. \\ & \left. - \frac{\cos\left[\frac{1}{2} (c + d x)\right] \sqrt{\cos[c + d x]}}{7 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)} - \frac{\sqrt{\cos[c + d x]} \sin\left[\frac{1}{2} (c + d x)\right]}{7 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)} \right) \\ & \left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} \right. \\ & \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) / \\ & \left( 7 d \sqrt{e \cos[c + d x]} (a + a \sin[c + d x])^2 \left( \sin[c + d x] \left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \right. \right. \right. \\ & \left. \left. \left. - \frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], \right. \right. \\ & \left. \left. \left. 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) / (7 \cos[c + d x]^{3/2}) + \end{aligned}$$

$$\begin{aligned}
& \frac{1}{7 \sqrt{\cos[c+d x]}} 2 \left( -\sin[c+d x] - \left( \sqrt{\frac{-1+\sqrt{2} - (-2+\sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1+\cos[\frac{1}{2} (c+d x)]}} \right. \right. \\
& \left. \left. \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}] \tan[\frac{1}{4} (c+d x)] \right) \right) / \\
& \left( \sqrt{2} \sqrt{3-2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} - \sqrt{2} \cos[\frac{1}{4} (c+d x)] \right. \\
& \left. \sqrt{\frac{-1+\sqrt{2} - (-2+\sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1+\cos[\frac{1}{2} (c+d x)]}} \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3-2 \sqrt{2}}}\right], \right. \\
& \left. 17-12 \sqrt{2}] \sin[\frac{1}{4} (c+d x)] \sqrt{3-2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} + \right. \\
& \left. \left( \sqrt{2} \cos[\frac{1}{4} (c+d x)]^2 \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}] \right. \right. \\
& \left. \left( \frac{(-2+\sqrt{2}) \sin[\frac{1}{2} (c+d x)]}{2 (1+\cos[\frac{1}{2} (c+d x)])} + \left( (-1+\sqrt{2} - (-2+\sqrt{2}) \cos[\frac{1}{2} (c+d x)]) \right. \right. \right. \\
& \left. \left. \left. \sin[\frac{1}{2} (c+d x)] \right) \right) / \left( 2 \left( 1+\cos[\frac{1}{2} (c+d x)] \right)^2 \right) \right) \\
& \left. \sqrt{3-2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right) / \left( \sqrt{\frac{-1+\sqrt{2} - (-2+\sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1+\cos[\frac{1}{2} (c+d x)]}} \right) + \\
& \left( \sqrt{\frac{-1+\sqrt{2} - (-2+\sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1+\cos[\frac{1}{2} (c+d x)]}} \sqrt{3-2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right) / \\
& \left( \sqrt{2 (3-2 \sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4} (c+d x)]^2}{3-2 \sqrt{2}}} \sqrt{1 - \frac{(17-12 \sqrt{2}) \tan[\frac{1}{4} (c+d x)]^2}{3-2 \sqrt{2}}} \right) \left. \right) \left. \right)
\end{aligned}$$

Problem 259: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^{3/2}}{(a + a \sin[c + d x])^3} dx$$

Optimal (type 4, 118 leaves, 4 steps):

$$-\frac{2 e^2 \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{21 a^3 d \sqrt{e \cos[c + d x]}} -$$

$$\frac{4 e \sqrt{e \cos[c + d x]}}{7 a d (a + a \sin[c + d x])^2} + \frac{2 e \sqrt{e \cos[c + d x]}}{21 d (a^3 + a^3 \sin[c + d x])}$$

Result (type 4, 1217 leaves):

$$\left( (e \cos[c + d x])^{3/2} \sec[c + d x] \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^6 \right. \\ \left. \left( \frac{2}{21} - \frac{4}{7 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])^4} + \frac{2}{21 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])^2} \right) \right) / \\ \left( d (a + a \sin[c + d x])^3 \right) - \\ \left( 2 (e \cos[c + d x])^{3/2} \sec[c + d x]^2 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^6 \right. \\ \left. \left( -\frac{\cos\left[\frac{1}{2} (c + d x)\right] \sqrt{\cos[c + d x]}}{21 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])} + \frac{\sqrt{\cos[c + d x]} \sin\left[\frac{1}{2} (c + d x)\right]}{21 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])} \right) \right. \\ \left. \left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} \right. \right. \\ \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) / \\ \left( 21 d (a + a \sin[c + d x])^3 \left( -\left( \sin[c + d x] \left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. \left. 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) \right) / (21 \cos[c + d x]^{3/2}) \right) -$$

$$\begin{aligned}
& \frac{1}{21 \sqrt{\cos[c+d x]}} 2 \left( -\sin[c+d x] - \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1 + \cos[\frac{1}{2} (c+d x)]}} \right. \right. \\
& \left. \left. \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}] \tan[\frac{1}{4} (c+d x)] \right) \right) / \\
& \left( \sqrt{2} \sqrt{3-2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right) - \sqrt{2} \cos[\frac{1}{4} (c+d x)] \\
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1 + \cos[\frac{1}{2} (c+d x)]}} \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3-2 \sqrt{2}}}\right], \\
& 17-12 \sqrt{2}] \sin[\frac{1}{4} (c+d x)] \sqrt{3-2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} + \\
& \left( \sqrt{2} \cos[\frac{1}{4} (c+d x)]^2 \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c+d x)]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}] \right. \\
& \left( \frac{(-2 + \sqrt{2}) \sin[\frac{1}{2} (c+d x)]}{2 (1 + \cos[\frac{1}{2} (c+d x)])} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]) \right. \right. \\
& \left. \left. \sin[\frac{1}{2} (c+d x)] \right) \right) / \left( 2 \left( 1 + \cos[\frac{1}{2} (c+d x)] \right)^2 \right) \\
& \sqrt{3-2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right) / \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1 + \cos[\frac{1}{2} (c+d x)]}} \right) + \\
& \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c+d x)]}{1 + \cos[\frac{1}{2} (c+d x)]}} \sqrt{3-2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right) / \\
& \left( \sqrt{2 (3-2 \sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4} (c+d x)]^2}{3-2 \sqrt{2}}} \sqrt{1 - \frac{(17-12 \sqrt{2}) \tan[\frac{1}{4} (c+d x)]^2}{3-2 \sqrt{2}}} \right) \left. \right)
\end{aligned}$$

Problem 261: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos[c+d x]} (a + a \sin[c+d x])^3} dx$$

Optimal (type 4, 153 leaves, 5 steps):

$$\frac{\frac{10 \sqrt{\cos(c+dx)} \operatorname{EllipticF}\left(\frac{1}{2} (c+dx), 2\right)}{77 a^3 d \sqrt{e \cos(c+dx)}} - \frac{2 \sqrt{e \cos(c+dx)}}{11 d e (a+a \sin(c+dx))^3}}{\frac{10 \sqrt{e \cos(c+dx)}}{77 a d e (a+a \sin(c+dx))^2} - \frac{10 \sqrt{e \cos(c+dx)}}{77 d e (a^3+a^3 \sin(c+dx))}}$$

Result (type 4, 1236 leaves):

$$\begin{aligned}
& \left( \cos[c + dx] \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^6 \right. \\
& \left. - \frac{\frac{10}{77} - \frac{2}{11 \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^6}}{\frac{10}{77 \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4} - \frac{10}{77 \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2}} \right) \\
& \left. \left( d \sqrt{e \cos[c + dx]} (a + a \sin[c + dx])^3 \right) + \left( 10 \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^6 \right. \right. \\
& \left. \left. - \frac{5 \cos\left[\frac{1}{2}(c + dx)\right] \sqrt{\cos[c + dx]}}{77 \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)} - \frac{5 \sqrt{\cos[c + dx]} \sin\left[\frac{1}{2}(c + dx)\right]}{77 \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)} \right) \right. \\
& \left. \left( \cos[c + dx] + 2 \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \right. \\
& \left. \left. \text{EllipticF}[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) \right) \\
& \left( 77 d \sqrt{e \cos[c + dx]} (a + a \sin[c + dx])^3 \left( \left( 5 \sin[c + dx] \left( \cos[c + dx] + 2 \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right]^2 \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \text{EllipticF}[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) \right) \right) \left( 77 \cos[c + dx]^{3/2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{77 \sqrt{\cos[c + d x]}} 10 \left( -\sin[c + d x] - \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right. \right. \\
& \left. \left. \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \tan[\frac{1}{4} (c + d x)] \right) \right) / \\
& \left( \sqrt{2} \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) - \sqrt{2} \cos[\frac{1}{4} (c + d x)] \\
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], \\
& 17 - 12 \sqrt{2}] \sin[\frac{1}{4} (c + d x)] \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} + \\
& \left( \sqrt{2} \cos[\frac{1}{4} (c + d x)]^2 \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \right. \\
& \left( \frac{(-2 + \sqrt{2}) \sin[\frac{1}{2} (c + d x)]}{2 (1 + \cos[\frac{1}{2} (c + d x)])} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]) \right. \right. \\
& \left. \left. \sin[\frac{1}{2} (c + d x)] \right) \right) / \left( 2 \left( 1 + \cos[\frac{1}{2} (c + d x)] \right)^2 \right) \\
& \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) / \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right) + \\
& \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) / \\
& \left( \sqrt{2 (3 - 2 \sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \right) \left. \right) \left. \right)
\end{aligned}$$

Problem 267: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^{7/2}}{(a + a \sin[c + d x])^4} dx$$

Optimal (type 4, 120 leaves, 4 steps):

$$\frac{10 e^4 \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{21 a^4 d \sqrt{e \cos[c + d x]}} -$$

$$\frac{4 e (e \cos[c + d x])^{5/2}}{7 a d (a + a \sin[c + d x])^3} + \frac{20 e^3 \sqrt{e \cos[c + d x]}}{21 d (a^4 + a^4 \sin[c + d x])}$$

Result (type 4, 1219 leaves):

$$\left( (e \cos[c + d x])^{7/2} \sec[c + d x]^3 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^8 \right.$$

$$\left. \left( -\frac{10}{21} - \frac{8}{7 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])^4} + \frac{32}{21 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])^2} \right) \right) /$$

$$(d (a + a \sin[c + d x])^4) +$$

$$\left( 10 (e \cos[c + d x])^{7/2} \sec[c + d x]^4 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^8 \right.$$

$$\left. \left( \frac{5 \cos\left[\frac{1}{2} (c + d x)\right] \sqrt{\cos[c + d x]}}{21 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])} - \frac{5 \sqrt{\cos[c + d x]} \sin\left[\frac{1}{2} (c + d x)\right]}{21 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])} \right) \right)$$

$$\left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} \right.$$

$$\left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) /$$

$$\left( 21 d (a + a \sin[c + d x])^4 \left( 5 \sin[c + d x] \left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \right. \right. \right.$$

$$\left. \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) / (21 \cos[c + d x]^{3/2}) +$$

$$\begin{aligned}
& \frac{1}{21 \sqrt{\cos[c + d x]}} 10 \left( -\sin[c + d x] - \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right. \right. \\
& \left. \left. \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \tan[\frac{1}{4} (c + d x)] \right) \right) / \\
& \left( \sqrt{2} \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) - \sqrt{2} \cos[\frac{1}{4} (c + d x)] \\
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], \\
& 17 - 12 \sqrt{2}] \sin[\frac{1}{4} (c + d x)] \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} + \\
& \left( \sqrt{2} \cos[\frac{1}{4} (c + d x)]^2 \text{EllipticF}[\text{ArcSin}\left[\frac{\tan[\frac{1}{4} (c + d x)]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \right. \\
& \left( \frac{(-2 + \sqrt{2}) \sin[\frac{1}{2} (c + d x)]}{2 (1 + \cos[\frac{1}{2} (c + d x)])} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]) \right. \right. \\
& \left. \left. \sin[\frac{1}{2} (c + d x)] \right) \right) / \left( 2 \left( 1 + \cos[\frac{1}{2} (c + d x)] \right)^2 \right) \\
& \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) / \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \right) + \\
& \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos[\frac{1}{2} (c + d x)]}{1 + \cos[\frac{1}{2} (c + d x)]}} \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c + d x)]^2} \right) / \\
& \left( \sqrt{2 (3 - 2 \sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \right) \left. \right) \left. \right)
\end{aligned}$$

Problem 269: Result more than twice size of optimal antiderivative.

$$\int \frac{(\mathbf{e} \cos[c + d x])^{3/2}}{(\mathbf{a} + \mathbf{a} \sin[c + d x])^4} dx$$

Optimal (type 4, 154 leaves, 5 steps):

$$-\frac{2 \mathbf{e}^2 \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{77 \mathbf{a}^4 d \sqrt{\mathbf{e} \cos[c + d x]}} -$$

$$\frac{4 \mathbf{e} \sqrt{\mathbf{e} \cos[c + d x]}}{11 \mathbf{a} d (\mathbf{a} + \mathbf{a} \sin[c + d x])^3} + \frac{2 \mathbf{e} \sqrt{\mathbf{e} \cos[c + d x]}}{77 d (\mathbf{a}^2 + \mathbf{a}^2 \sin[c + d x])^2} + \frac{2 \mathbf{e} \sqrt{\mathbf{e} \cos[c + d x]}}{77 d (\mathbf{a}^4 + \mathbf{a}^4 \sin[c + d x])}$$

Result (type 4, 1244 leaves):

$$\left( (\mathbf{e} \cos[c + d x])^{3/2} \operatorname{Sec}[c + d x] \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^8 \right.$$

$$\left. \left( \frac{2}{77} - \frac{4}{11 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])^6} + \frac{2}{77 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])^4} + \right. \right.$$

$$\left. \left. \frac{2}{77 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])^2} \right) \right) / \left( d (\mathbf{a} + \mathbf{a} \sin[c + d x])^4 \right) -$$

$$\left( 2 (\mathbf{e} \cos[c + d x])^{3/2} \operatorname{Sec}[c + d x]^2 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^8 \right.$$

$$\left. \left( -\frac{\cos\left[\frac{1}{2} (c + d x)\right] \sqrt{\cos[c + d x]}}{77 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])} + \frac{\sqrt{\cos[c + d x]} \sin\left[\frac{1}{2} (c + d x)\right]}{77 (\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right])} \right) \right.$$

$$\left. \left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} \right. \right.$$

$$\left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) /$$

$$\left( 77 d (\mathbf{a} + \mathbf{a} \sin[c + d x])^4 \left( - \left( \sin[c + d x] \left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \right. \right. \right. \right. \right.$$

$$\left. \left. \left. \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], \right. \right. \right. \right. \right. \right)$$



### Problem 271: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos[c + d x]} (a + a \sin[c + d x])^4} dx$$

Optimal (type 4, 191 leaves, 6 steps):

$$\begin{aligned} & \frac{2 \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{33 a^4 d \sqrt{e \cos[c + d x]}} - \frac{2 \sqrt{e \cos[c + d x]}}{15 d e (a + a \sin[c + d x])^4} - \\ & \frac{14 \sqrt{e \cos[c + d x]}}{165 a d e (a + a \sin[c + d x])^3} - \frac{2 \sqrt{e \cos[c + d x]}}{33 d e (a^2 + a^2 \sin[c + d x])^2} - \frac{2 \sqrt{e \cos[c + d x]}}{33 d e (a^4 + a^4 \sin[c + d x])} \end{aligned}$$

Result (type 4, 1263 leaves):

$$\begin{aligned} & \left( \cos[c + d x] \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^8 \right. \\ & \left( -\frac{2}{33} - \frac{2}{15 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^8} - \frac{14}{165 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^6} - \right. \\ & \left. \left. \frac{2}{33 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^4} - \frac{2}{33 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2} \right) \right) / \\ & \left( d \sqrt{e \cos[c + d x]} (a + a \sin[c + d x])^4 \right) + \left( 2 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^8 \right. \\ & \left( \frac{\cos\left[\frac{1}{2} (c + d x)\right] \sqrt{\cos[c + d x]}}{33 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)} - \frac{\sqrt{\cos[c + d x]} \sin\left[\frac{1}{2} (c + d x)\right]}{33 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)} \right) \\ & \left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2} (c + d x)\right]}{1 + \cos\left[\frac{1}{2} (c + d x)\right]}} \right. \\ & \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) / \\ & \left( 33 d \sqrt{e \cos[c + d x]} (a + a \sin[c + d x])^4 \left( \sin[c + d x] \left( \cos[c + d x] + 2 \sqrt{2} \cos\left[\frac{1}{4} (c + d x)\right]^2 \right. \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \\
& \left. \frac{17 - 12\sqrt{2}}{\sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2}}\right] \Bigg/ (33 \cos[c + dx]^{3/2}) + \\
& \frac{1}{33\sqrt{\cos[c + dx]}} 2 \left( -\sin[c + dx] - \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \\
& \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \tan\left[\frac{1}{4}(c + dx)\right] \right) \Bigg/ \\
& \left( \sqrt{2} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} - \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \\
& \left. 17 - 12\sqrt{2}\right] \sin\left[\frac{1}{4}(c + dx)\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} + \right. \\
& \left. \left( \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \right. \\
& \left. \left( \frac{(-2 + \sqrt{2}) \sin\left[\frac{1}{2}(c + dx)\right]}{2(1 + \cos\left[\frac{1}{2}(c + dx)\right])} + \left( (-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]) \right. \right. \right. \\
& \left. \left. \left. \sin\left[\frac{1}{2}(c + dx)\right]\right) \Bigg/ \left( 2 \left( 1 + \cos\left[\frac{1}{2}(c + dx)\right] \right)^2 \right) \right) \\
& \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \Bigg/ \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right) + \\
& \left( \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \Bigg) \Bigg/
\end{aligned}$$

$$\left( \sqrt{2 (3 - 2 \sqrt{2})} \sqrt{1 - \frac{\tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan[\frac{1}{4} (c + d x)]^2}{3 - 2 \sqrt{2}}} \right) \right)$$

Problem 273: Result unnecessarily involves imaginary or complex numbers.

$$\int (e \cos[c + d x])^{3/2} \sqrt{a + a \sin[c + d x]} \, dx$$

Optimal (type 3, 236 leaves, 8 steps):

$$\begin{aligned} & -\frac{a (e \cos[c + d x])^{5/2}}{2 d e \sqrt{a + a \sin[c + d x]}} + \frac{3 e \sqrt{e \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{4 d} - \\ & \frac{3 e^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{4 d (1 + \cos[c + d x] + \sin[c + d x])} + \\ & \left( \frac{3 e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(4 d (1 + \cos[c + d x] + \sin[c + d x]))} \right) \end{aligned}$$

Result (type 3, 269 leaves):

$$\begin{aligned} & - \left( \left( \frac{1}{2} e e^{-i(c+d x)} \sqrt{e \cos[c + d x]} \left( -\frac{i}{2} \sqrt{1 + e^{2i(c+d x)}} - 2 e^{i(c+d x)} \sqrt{1 + e^{2i(c+d x)}} \right. \right. \right. + \\ & \left. \left. \left. 2 \frac{i}{2} e^{2i(c+d x)} \sqrt{1 + e^{2i(c+d x)}} + e^{3i(c+d x)} \sqrt{1 + e^{2i(c+d x)}} - 3 d e^{2i(c+d x)} x + \right. \right. \right. \\ & \left. \left. \left. 3 e^{2i(c+d x)} \operatorname{ArcSinh}\left[e^{i(c+d x)}\right] - 3 \frac{i}{2} e^{2i(c+d x)} \operatorname{Log}\left[1 + \sqrt{1 + e^{2i(c+d x)}}\right] \right) \right. \\ & \left. \sqrt{a (1 + \sin[c + d x])} \right) \left/ \left( 4 d \left( \frac{1}{2} + e^{i(c+d x)} \right) \sqrt{1 + e^{2i(c+d x)}} \right) \right) \end{aligned}$$

Problem 274: Result unnecessarily involves imaginary or complex numbers.

$$\int \sqrt{e \cos[c + d x]} \sqrt{a + a \sin[c + d x]} \, dx$$

Optimal (type 3, 194 leaves, 7 steps):

$$\begin{aligned} & -\frac{a (e \cos[c + d x])^{3/2}}{d e \sqrt{a + a \sin[c + d x]}} + \frac{\sqrt{e} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{d (1 + \cos[c + d x] + \sin[c + d x])} + \\ & \left( \frac{\sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(d (1 + \cos[c + d x] + \sin[c + d x]))} \right) \end{aligned}$$

Result (type 3, 195 leaves):

$$-\left(\left(\frac{1}{2} \sqrt{e \cos[c+d x]} \left(-\frac{1}{2} \sqrt{1+e^{2 \frac{1}{2} (c+d x)}}+e^{\frac{1}{2} (c+d x)} \sqrt{1+e^{2 \frac{1}{2} (c+d x)}}+\frac{i d e^{\frac{1}{2} (c+d x)} x+i e^{\frac{1}{2} (c+d x)} \operatorname{ArcSinh}\left[e^{\frac{1}{2} (c+d x)}\right]-e^{\frac{1}{2} (c+d x)} \operatorname{Log}\left[1+\sqrt{1+e^{2 \frac{1}{2} (c+d x)}}\right]\right)\right) \middle/ \left(d \left(\frac{1}{2}+e^{\frac{1}{2} (c+d x)}\right) \sqrt{1+e^{2 \frac{1}{2} (c+d x)}}\right)\right)$$

Problem 275: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sqrt{a+a \sin[c+d x]}}{\sqrt{e \cos[c+d x]}} \, dx$$

Optimal (type 3, 161 leaves, 6 steps) :

$$-\frac{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+d x]}}{\sqrt{e}}\right] \sqrt{1+\cos[c+d x]} \sqrt{a+a \sin[c+d x]}}{d \sqrt{e} (1+\cos[c+d x]+\sin[c+d x])} + \frac{\left(2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+d x]}{\sqrt{e \cos[c+d x]} \sqrt{1+\cos[c+d x]}}\right] \sqrt{1+\cos[c+d x]} \sqrt{a+a \sin[c+d x]}\right)}{(d \sqrt{e} (1+\cos[c+d x]+\sin[c+d x]))}$$

Result (type 3, 108 leaves) :

$$\left(\sqrt{1+e^{2 \frac{1}{2} (c+d x)}} \left(d x-\operatorname{ArcSinh}\left[e^{\frac{1}{2} (c+d x)}\right]+\frac{1}{2} \operatorname{Log}\left[1+\sqrt{1+e^{2 \frac{1}{2} (c+d x)}}\right]\right) \sqrt{a+\sin[c+d x]}\right) \middle/ (d \left(1-\frac{1}{2} e^{\frac{1}{2} (c+d x)}\right) \sqrt{e \cos[c+d x]})$$

Problem 280: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \cos[c+d x])^{5/2} (a+a \sin[c+d x])^{3/2} \, dx$$

Optimal (type 3, 319 leaves, 10 steps) :

$$-\frac{15 a^3 (e \cos[c+d x])^{7/2}}{32 d e (a+a \sin[c+d x])^{3/2}}+\frac{15 a^2 e (e \cos[c+d x])^{3/2}}{64 d \sqrt{a+a \sin[c+d x]}}- \frac{3 a^2 (e \cos[c+d x])^{7/2}}{8 d e \sqrt{a+a \sin[c+d x]}}-\frac{a (e \cos[c+d x])^{7/2} \sqrt{a+a \sin[c+d x]}}{4 d e}+ \frac{45 a e^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+d x]}}{\sqrt{e}}\right] \sqrt{1+\cos[c+d x]} \sqrt{a+\sin[c+d x]}}{64 d (1+\cos[c+d x]+\sin[c+d x])}+ \frac{\left(45 a e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+d x]}{\sqrt{e \cos[c+d x]} \sqrt{1+\cos[c+d x]}}\right] \sqrt{1+\cos[c+d x]} \sqrt{a+\sin[c+d x]}\right)}{(64 d (1+\cos[c+d x]+\sin[c+d x]))}$$

Result (type 4, 2816 leaves):

$$\begin{aligned}
 & \left( (\cos(c + d x))^5 \sec(c + d x)^2 (a (1 + \sin(c + d x)))^{3/2} \right. \\
 & \left( -\frac{3}{4} \cos\left[\frac{1}{2} (c + d x)\right] + \frac{3}{64} \cos\left[\frac{3}{2} (c + d x)\right] - \frac{1}{8} \cos\left[\frac{5}{2} (c + d x)\right] - \frac{1}{32} \cos\left[\frac{7}{2} (c + d x)\right] + \right. \\
 & \left. \frac{3}{4} \sin\left[\frac{1}{2} (c + d x)\right] + \frac{3}{64} \sin\left[\frac{3}{2} (c + d x)\right] + \frac{1}{8} \sin\left[\frac{5}{2} (c + d x)\right] - \frac{1}{32} \sin\left[\frac{7}{2} (c + d x)\right] \right) \Big) \Big) \\
 & \left( d \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^3 \right) + \left( 45 \sqrt{3 - 2 \sqrt{2}} (\cos(c + d x))^{5/2} \right. \\
 & \left. \sec(c + d x)^2 (a (1 + \sin(c + d x)))^{3/2} \right) \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \left( 1 + \tan\left[\frac{1}{4} (c + d x)\right]^2 \right) \\
 & \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
 & \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2} \\
 & \left( 2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \right) \\
 & \left( 4 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\
 & \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} + \right. \\
 & \left. 8 \text{EllipticPi}\left[-3 + 2 \sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right. \\
 & \left. \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\
 & \left. \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} + \sqrt{2} \left( \text{Log}\left[1 + \tan\left[\frac{1}{4} (c + d x)\right]^2\right] - \right. \right. \\
 & \left. \left. \text{Log}\left[2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4}\right]\right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \left( 1 - 6 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + \tan \left[ \frac{1}{4} (c + d x) \right]^4 \right) \right\} \Bigg/ \\
& \left( 128 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right. \\
& \left. \left( 4 \sec \left[ \frac{1}{4} (c + d x) \right]^2 - \right. \right. \\
& \left. \left. 3 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 - 52 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + \right. \right. \\
& \left. \left. 39 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 200 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^4 - \right. \right. \\
& \left. \left. 150 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^4 - 200 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^6 + \right. \right. \\
& \left. \left. 150 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^6 + 52 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^8 - \right. \right. \\
& \left. \left. 39 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^8 - 4 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^{10} + \right. \right. \\
& \left. \left. 3 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \right. \\
& \left. \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \right. \\
& \left. \left. \sqrt{1 - 3 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2 (3 - 2 \sqrt{2})} \sec \left[ \frac{1}{4} (c + d x) \right]^2} \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{4} (c + d x) \right]^3 \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \right. \\
& \left. \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \right. \\
& \left. \left. \sqrt{1 - 3 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec \left[ \frac{1}{4} (c + d x) \right]^2} \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{4} (c + d x) \right]^5 \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c+dx)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c+dx)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c+dx)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c+dx)\right)^2} - \\
& 6 \sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 4\sqrt{2} \sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 48 \sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 32\sqrt{2} \sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 84 \sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 56\sqrt{2} \sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 48 \sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 32\sqrt{2} \sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 6 \sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^8 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 4\sqrt{2} \sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^8 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 4\sqrt{3 - 2\sqrt{2}} \sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right) \\
& \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c+dx)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c+dx)\right)^2}{-3 + 2\sqrt{2}}}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c+dx)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c+dx)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{1 - 3 \tan\left(\frac{1}{4}(c+dx)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c+dx)\right)^2}{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4 - 4\sqrt{3-2\sqrt{2}} \sec\left(\frac{1}{4}(c+dx)\right)^2}} \\
& \tan\left(\frac{1}{4}(c+dx)\right)^3 \sqrt{\frac{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c+dx)\right)^2}{-3 + 2\sqrt{2}}} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c+dx)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c+dx)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c+dx)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{1 - 3 \tan\left(\frac{1}{4}(c+dx)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c+dx)\right)^2}{1 - 6 \tan\left(\frac{1}{4}(c+dx)\right)^2 + \tan\left(\frac{1}{4}(c+dx)\right)^4}} \Bigg)
\end{aligned}$$

Problem 281: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \cos[c+dx])^{3/2} (a + a \sin[c+dx])^{3/2} \, dx$$

Optimal (type 3, 278 leaves, 9 steps):

$$\begin{aligned}
& -\frac{7a^2 (e \cos[c+dx])^{5/2}}{12d e \sqrt{a + a \sin[c+dx]}} + \frac{7ae \sqrt{e \cos[c+dx]} \sqrt{a + a \sin[c+dx]}}{8d} - \\
& \frac{a (e \cos[c+dx])^{5/2} \sqrt{a + a \sin[c+dx]}}{3d e} - \\
& \frac{7ae^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+dx]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c+dx]} \sqrt{a + a \sin[c+dx]}}{8d (1 + \cos[c+dx] + \sin[c+dx])} + \\
& \left( \frac{7ae^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+dx]}{\sqrt{e \cos[c+dx]} \sqrt{1 + \cos[c+dx]}}\right] \sqrt{1 + \cos[c+dx]} \sqrt{a + a \sin[c+dx]}}{(8d (1 + \cos[c+dx] + \sin[c+dx]))} \right)
\end{aligned}$$

Result (type 4, 2810 leaves):

$$\begin{aligned}
& \left( (\mathbf{e} \cos[c + d x])^{3/2} \sec[c + d x] (a (1 + \sin[c + d x]))^{3/2} \left( \frac{5}{12} \cos\left[\frac{1}{2} (c + d x)\right] - \frac{3}{8} \cos\left[\frac{3}{2} (c + d x)\right] - \right. \right. \\
& \left. \left. \frac{1}{12} \cos\left[\frac{5}{2} (c + d x)\right] + \frac{5}{12} \sin\left[\frac{1}{2} (c + d x)\right] + \frac{3}{8} \sin\left[\frac{3}{2} (c + d x)\right] - \frac{1}{12} \sin\left[\frac{5}{2} (c + d x)\right] \right) \right) / \\
& \left( d \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^3 \right) - \left( 7 \sqrt{3 - 2 \sqrt{2}} (\mathbf{e} \cos[c + d x])^{3/2} \sec[c + d x] \right. \\
& \left. (a (1 + \sin[c + d x]))^{3/2} \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \left( 1 + \tan\left[\frac{1}{4} (c + d x)\right]^2 \right) \right. \\
& \left. \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\
& \left. \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\
& \left. \left( 2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \right) \right. \\
& \left. \left( 4 \text{EllipticF}[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \right. \\
& \left. \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} + \right. \right. \\
& \left. \left. 8 \text{EllipticPi}\left[-3 + 2 \sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right. \right. \\
& \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \right. \\
& \left. \left. \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} - \sqrt{2} \left( \text{Log}\left[1 + \tan\left[\frac{1}{4} (c + d x)\right]^2\right] - \right. \right. \right. \\
& \left. \left. \left. \text{Log}\left[2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4}\right]\right) \right) \right) / \\
& \left. \left( 1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4 \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( 16 d \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right. \\
& \left. - 4 \sec \left[ \frac{1}{4} (c + d x) \right]^2 + 3 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 + 52 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - \right. \\
& \left. 39 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 200 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^4 + \right. \\
& \left. 150 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^4 + 200 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^6 - \right. \\
& \left. 150 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^6 - 52 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^8 + \right. \\
& \left. 39 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^8 + 4 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^{10} - \right. \\
& \left. 3 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \right. \\
& \left. \tan \left[ \frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \\
& \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \\
& \left. \sqrt{1 - 3 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2 (3 - 2 \sqrt{2})} \sec \left[ \frac{1}{4} (c + d x) \right]^2} \right. \\
& \left. \tan \left[ \frac{1}{4} (c + d x) \right]^3 \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \\
& \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \\
& \left. \sqrt{1 - 3 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec \left[ \frac{1}{4} (c + d x) \right]^2} \right. \\
& \left. \tan \left[ \frac{1}{4} (c + d x) \right]^5 \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \\
& \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} + \\
& 6 \sec\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 4\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 48 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 32\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 84 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 56\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 48 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^6 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 32\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^6 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 6 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^8 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 4\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^8 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 4\sqrt{3 - 2\sqrt{2}} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right) \\
& \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} \\
& \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4 - 4\sqrt{3 - 2\sqrt{2}} \sec\left(\frac{1}{4}(c + d x)\right)^2} \\
& \tan\left(\frac{1}{4}(c + d x)\right)^3 \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} \\
& \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} \Bigg)
\end{aligned}$$

Problem 282: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{e \cos[c + d x]} (a + a \sin[c + d x])^{3/2} \, dx$$

Optimal (type 3, 243 leaves, 8 steps):

$$\begin{aligned}
& -\frac{5a^2 (e \cos[c + d x])^{3/2}}{4d e \sqrt{a + a \sin[c + d x]}} - \frac{a (e \cos[c + d x])^{3/2} \sqrt{a + a \sin[c + d x]}}{2d e} + \\
& \frac{5a \sqrt{e} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{4d (1 + \cos[c + d x] + \sin[c + d x])} + \\
& \left( \frac{5a \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]} \sqrt{1 + \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(4d (1 + \cos[c + d x] + \sin[c + d x]))} \right) /
\end{aligned}$$

Result (type 4, 2322 leaves):

$$\begin{aligned}
& \left( \sqrt{e \cos[c + d x]} (a (1 + \sin[c + d x]))^{3/2} \right. \\
& \left. \left( -\frac{3}{2} \cos\left[\frac{1}{2}(c + d x)\right] - \frac{1}{4} \cos\left[\frac{3}{2}(c + d x)\right] + \frac{3}{2} \sin\left[\frac{1}{2}(c + d x)\right] - \frac{1}{4} \sin\left[\frac{3}{2}(c + d x)\right] \right) \right) / \\
& \left( d \left( \cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( 25 \cos \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{e \cos [c + d x]} (a (1 + \sin [c + d x]))^{3/2} \left( \sqrt{2} \left( \log [\sec \left[ \frac{1}{4} (c + d x) \right]^2] - \right. \right. \right. \\
& \left. \left. \left. \log [2 + \sqrt{2}] \sqrt{\cos [c + d x] \sec \left[ \frac{1}{4} (c + d x) \right]^4 - 2 \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right. \\
& \left. \left. \left. \sqrt{\cos [c + d x] \sec \left[ \frac{1}{4} (c + d x) \right]^4 + 4 \text{EllipticF}[\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2}]} \right. \right. \\
& \left. \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2} + \right. \right. \right. \\
& 8 \text{EllipticPi}[-3 + 2 \sqrt{2}, -\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2}] \\
& \left. \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right) / \\
& \left( 64 d \sqrt{\cos [c + d x]} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^4 \right. \\
& \left( \frac{1}{16 \sqrt{\cos [c + d x]}} 5 \cos \left[ \frac{1}{4} (c + d x) \right] \sin \left[ \frac{1}{4} (c + d x) \right] \left( \sqrt{2} \left( \log [\sec \left[ \frac{1}{4} (c + d x) \right]^2] - \right. \right. \right. \\
& \left. \left. \left. \log [2 + \sqrt{2}] \sqrt{\cos [c + d x] \sec \left[ \frac{1}{4} (c + d x) \right]^4 - 2 \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right. \\
& \left. \left. \left. \sqrt{\cos [c + d x] \sec \left[ \frac{1}{4} (c + d x) \right]^4 + 4 \text{EllipticF}[\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2}]} \right. \right. \\
& \left. \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2} + \right. \right. \right. \\
& 8 \text{EllipticPi}[-3 + 2 \sqrt{2}, -\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2}] \\
& \left. \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right) - 
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{16 \cos[c + dx]^{3/2}} 5 \cos\left[\frac{1}{4} (c + dx)\right]^2 \sin[c + dx] \left( \sqrt{2} \left( \log[\sec\left[\frac{1}{4} (c + dx)\right]^2] - \right. \right. \\
& \left. \left. \log[2 + \sqrt{2} \sqrt{\cos[c + dx] \sec\left[\frac{1}{4} (c + dx)\right]^4} - 2 \tan\left[\frac{1}{4} (c + dx)\right]^2] \right) \right. \\
& \left. \sqrt{\cos[c + dx] \sec\left[\frac{1}{4} (c + dx)\right]^4 + 4 \text{EllipticF}[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + dx)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right],} \right. \\
& \left. \left. 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + dx)\right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + dx)\right]^2} + \right. \\
& \left. 8 \text{EllipticPi}\left[-3 + 2 \sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + dx)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right. \\
& \left. \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + dx)\right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + dx)\right]^2} \right) - \\
& \frac{1}{8 \sqrt{\cos[c + dx]}} 5 \cos\left[\frac{1}{4} (c + dx)\right]^2 \left( \left( \log[\sec\left[\frac{1}{4} (c + dx)\right]^2] - \log[ \right. \right. \\
& \left. \left. 2 + \sqrt{2} \sqrt{\cos[c + dx] \sec\left[\frac{1}{4} (c + dx)\right]^4} - 2 \tan\left[\frac{1}{4} (c + dx)\right]^2] \right) \right. \\
& \left. \left( -\sec\left[\frac{1}{4} (c + dx)\right]^4 \sin[c + dx] + \cos[c + dx] \sec\left[\frac{1}{4} (c + dx)\right]^4 \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4} (c + dx)\right] \right) \right) \Big/ \left( \sqrt{2} \sqrt{\cos[c + dx] \sec\left[\frac{1}{4} (c + dx)\right]^4} \right) + \\
& \left( (-3 + 2 \sqrt{2}) \text{EllipticF}[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + dx)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \right. \\
& \left. \left. \sec\left[\frac{1}{4} (c + dx)\right]^2 \tan\left[\frac{1}{4} (c + dx)\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + dx)\right]^2} \right) \Big/ \right. \\
& \left. \left( \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + dx)\right]^2} + 2 (-3 + 2 \sqrt{2}) \text{EllipticPi}\left[-3 + 2 \sqrt{2}, \right. \right. \right. \\
& \left. \left. \left. 17 - 12 \sqrt{2}\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}] \sec \left[\frac{1}{4}(c+d x)\right]^2 \tan \left[\frac{1}{4}(c+d x)\right] \\
& \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\Bigg) \Bigg/ \left(\sqrt{1+\left(-3+2 \sqrt{2}\right) \tan \left[\frac{1}{4}(c+d x)\right]^2}\right) - \\
& \left(\text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sec \left[\frac{1}{4}(c+d x)\right]^2 \tan \left[\frac{1}{4}(c+d x)\right]\right. \\
& \left.\sqrt{1+\left(-3+2 \sqrt{2}\right) \tan \left[\frac{1}{4}(c+d x)\right]^2}\right) \Bigg/ \left(\sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right) - \\
& \left(2 \text{EllipticPi}\left[-3+2 \sqrt{2},-\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]\right. \\
& \left.\sec \left[\frac{1}{4}(c+d x)\right]^2 \tan \left[\frac{1}{4}(c+d x)\right] \sqrt{1+\left(-3+2 \sqrt{2}\right) \tan \left[\frac{1}{4}(c+d x)\right]^2}\right) \Bigg/ \\
& \left(\sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right) + \left(\sec \left[\frac{1}{4}(c+d x)\right]^2\right. \\
& \left.\sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2} \sqrt{1+\left(-3+2 \sqrt{2}\right) \tan \left[\frac{1}{4}(c+d x)\right]^2}\right) \Bigg/ \\
& \left(\sqrt{3-2 \sqrt{2}} \sqrt{1-\frac{\tan \left[\frac{1}{4}(c+d x)\right]^2}{3-2 \sqrt{2}}} \sqrt{1-\frac{\left(17-12 \sqrt{2}\right) \tan \left[\frac{1}{4}(c+d x)\right]^2}{3-2 \sqrt{2}}}\right) - \\
& \left(2 \sec \left[\frac{1}{4}(c+d x)\right]^2 \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right. \\
& \left.\sqrt{1+\left(-3+2 \sqrt{2}\right) \tan \left[\frac{1}{4}(c+d x)\right]^2}\right) \Bigg/ \left(\sqrt{3-2 \sqrt{2}} \sqrt{1-\frac{\tan \left[\frac{1}{4}(c+d x)\right]^2}{3-2 \sqrt{2}}}\right. \\
& \left.\sqrt{1-\frac{\left(17-12 \sqrt{2}\right) \tan \left[\frac{1}{4}(c+d x)\right]^2}{3-2 \sqrt{2}}}\left(1-\frac{\left(-3+2 \sqrt{2}\right) \tan \left[\frac{1}{4}(c+d x)\right]^2}{3-2 \sqrt{2}}\right)\right) + 
\end{aligned}$$

$$\begin{aligned}
& \sqrt{2} \sqrt{\cos[c+d x] \sec[\frac{1}{4} (c+d x)]^4} \left( \frac{1}{2} \tan[\frac{1}{4} (c+d x)] - \left( -\sec[\frac{1}{4} (c+d x)]^2 \tan[\frac{1}{4} (c+d x)]^4 \right. \right. \\
& \left. \left. + \left( -\sec[\frac{1}{4} (c+d x)]^4 \sin[c+d x] + \cos[c+d x] \sec[\frac{1}{4} (c+d x)]^4 \tan[\frac{1}{4} (c+d x)] \right) \right) \right) / \left( \sqrt{2} \sqrt{\cos[c+d x] \sec[\frac{1}{4} (c+d x)]^4} \right) \right) / \\
& \left( 2 + \sqrt{2} \sqrt{\cos[c+d x] \sec[\frac{1}{4} (c+d x)]^4} - 2 \tan[\frac{1}{4} (c+d x)]^2 \right) \right) \right)
\end{aligned}$$

**Problem 283: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(\mathbf{a} + \mathbf{a} \sin[c+d x])^{3/2}}{\sqrt{\mathbf{e} \cos[c+d x]}} dx$$

Optimal (type 3, 198 leaves, 7 steps):

$$\begin{aligned}
& -\frac{a \sqrt{e \cos[c+d x]} \sqrt{a + a \sin[c+d x]}}{d e} - \\
& \frac{3 a \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c+d x]} \sqrt{a + a \sin[c+d x]}}{d \sqrt{e} (1 + \cos[c+d x] + \sin[c+d x])} + \\
& \left( 3 a \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+d x]}{\sqrt{e \cos[c+d x]} \sqrt{1 + \cos[c+d x]}}\right] \sqrt{1 + \cos[c+d x]} \sqrt{a + a \sin[c+d x]} \right) / \\
& (d \sqrt{e} (1 + \cos[c+d x] + \sin[c+d x]))
\end{aligned}$$

Result (type 4, 2750 leaves):

$$\begin{aligned}
& \left( \cos[c+d x] \left( -\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)] \right) (a (1 + \sin[c+d x]))^{3/2} \right) / \\
& \left( d \sqrt{e \cos[c+d x]} \left( \cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)] \right)^3 - \right. \\
& \left. \left( 3 \sqrt{3 - 2 \sqrt{2}} \cos[c+d x] (a (1 + \sin[c+d x]))^{3/2} \sqrt{3 - 2 \sqrt{2} - \tan[\frac{1}{4} (c+d x)]^2} \right. \right. \\
& \left. \left. \left( 1 + \tan[\frac{1}{4} (c+d x)]^2 \right) \sqrt{\frac{-3 + 2 \sqrt{2} + \tan[\frac{1}{4} (c+d x)]^2}{-3 + 2 \sqrt{2}}} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2} \\
& \left( 2 - 2 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4} \right) \\
& \left( 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right. \\
& \left. \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4} + \right. \\
& \left. 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \\
& \left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} \right. \\
& \left. \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4} - \sqrt{2} \left( \operatorname{Log}\left[1 + \tan\left[\frac{1}{4}(c + dx)\right]^2\right] - \right. \right. \\
& \left. \left. \operatorname{Log}\left[2 - 2 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4}\right]\right) \right. \\
& \left. \left( 1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4 \right) \right) \Bigg) \\
2d\sqrt{e \cos(c + dx)} \left( \cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right) \left( \cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^3 \\
& \left( -4 \sec\left[\frac{1}{4}(c + dx)\right]^2 + 3\sqrt{2} \sec\left[\frac{1}{4}(c + dx)\right]^2 + 52 \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^2 - \right. \\
& \left. 39\sqrt{2} \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 200 \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^4 + \right.
\end{aligned}$$

$$\begin{aligned}
& 150 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^4 + 200 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^6 - \\
& 150 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^6 - 52 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^8 + \\
& 39 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^8 + 4 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^{10} - \\
& 3 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec\left[\frac{1}{4} (c + d x)\right]^2 \\
& \tan\left[\frac{1}{4} (c + d x)\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2 (3 - 2 \sqrt{2})} \sec\left[\frac{1}{4} (c + d x)\right]^2} \\
& \tan\left[\frac{1}{4} (c + d x)\right]^3 \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec\left[\frac{1}{4} (c + d x)\right]^2} \\
& \tan\left[\frac{1}{4} (c + d x)\right]^5 \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2 +} \\
& 6 \sec\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} - \\
& 4 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} -
\end{aligned}$$

$$\begin{aligned}
& 48 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 32 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 84 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 56 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 48 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 32 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 6 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 4 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \\
& \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}}
\end{aligned}$$

$$\sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \sqrt{\frac{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4}}$$

**Problem 284: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sin[c + d x])^{3/2}}{(e \cos[c + d x])^{3/2}} dx$$

Optimal (type 3, 210 leaves, 7 steps):

$$\frac{4 a \sqrt{a + a \sin[c + d x]}}{d e \sqrt{e \cos[c + d x]}} - \frac{2 a^2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{d e^{3/2} (a + a \cos[c + d x] + a \sin[c + d x])} - \left( \frac{2 a^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]} \sqrt{1 + \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(d e^{3/2} (a + a \cos[c + d x] + a \sin[c + d x]))} \right)$$

Result (type 4, 2727 leaves):

$$\begin{aligned} & \left( 4 \cos[c + d x]^2 (a (1 + \sin[c + d x]))^{3/2} \right) \Big/ \left( d (e \cos[c + d x])^{3/2} \right. \\ & \left. \left( \cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right) \left( \cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) - \\ & \left( \sqrt{3 - 2\sqrt{2}} \cos[c + d x]^2 (a (1 + \sin[c + d x]))^{3/2} \right) \sqrt{\frac{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2}{3 - 2\sqrt{2}}} \\ & \left( 1 + \tan\left(\frac{1}{4}(c + d x)\right)^2 \right) \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\ & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\ & \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} \end{aligned}$$

$$\begin{aligned}
& \left( 2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \right) \\
& \left( 4 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\
& \quad \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} + \right. \\
& \quad \left. 8 \text{EllipticPi}\left[-3 + 2 \sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right. \\
& \quad \left. \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\
& \quad \left. \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} + \sqrt{2} \left( \text{Log}\left[1 + \tan\left[\frac{1}{4} (c + d x)\right]^2\right] - \right. \right. \\
& \quad \left. \left. \text{Log}\left[2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4}\right]\right) \right. \\
& \quad \left. \left( 1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4 \right) \right) \Bigg) \\
& \left( d (e \cos(c + d x))^{3/2} \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^4 \right. \\
& \quad \left( 4 \sec\left[\frac{1}{4} (c + d x)\right]^2 - 3 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 - 52 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \right. \\
& \quad \left. 39 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 200 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^4 - \right. \\
& \quad \left. 150 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^4 - 200 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^6 + \right. \\
& \quad \left. 150 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^6 + 52 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^8 - \right. \\
& \quad \left. 39 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^8 - 4 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^{10} + \right. \\
& \quad \left. 3 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec\left[\frac{1}{4} (c + d x)\right]^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2\left(3-2\sqrt{2}\right)}\sec\left(\frac{1}{4}(c+dx)\right)^2} \\
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^3}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2\left(3-2\sqrt{2}\right)}\sec\left(\frac{1}{4}(c+dx)\right)^2} \\
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^5}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}- \\
& 6\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}+ \\
& 4\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}+ \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2\tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}- \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2\tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}- \\
& \dots
\end{aligned}$$

$$\begin{aligned}
& 84 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 56 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 48 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 32 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 6 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 4 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \\
& \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}
\end{aligned}$$

$$\sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \Bigg)$$

**Problem 289: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (e \cos[c + d x])^{3/2} (a + a \sin[c + d x])^{5/2} \, dx$$

Optimal (type 3, 323 leaves, 10 steps):

$$\begin{aligned} & \frac{77 a^3 (e \cos[c + d x])^{5/2}}{96 d e \sqrt{a + a \sin[c + d x]}} + \frac{77 a^2 e \sqrt{e \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{64 d} - \\ & \frac{11 a^2 (e \cos[c + d x])^{5/2} \sqrt{a + a \sin[c + d x]}}{24 d e} - \\ & \frac{77 a^2 e^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{64 d (1 + \cos[c + d x] + \sin[c + d x])} + \\ & \left( \frac{77 a^2 e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]} \sqrt{1 + \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(64 d (1 + \cos[c + d x] + \sin[c + d x]))} - \frac{a (e \cos[c + d x])^{5/2} (a + a \sin[c + d x])^{3/2}}{4 d e} \right) \Bigg) \end{aligned}$$

Result (type 4, 2838 leaves):

$$\begin{aligned} & \left( (e \cos[c + d x])^{3/2} \sec[c + d x] (a (1 + \sin[c + d x]))^{5/2} \right. \\ & \left( \frac{5}{12} \cos\left[\frac{1}{2} (c + d x)\right] - \frac{35}{64} \cos\left[\frac{3}{2} (c + d x)\right] - \frac{5}{24} \cos\left[\frac{5}{2} (c + d x)\right] + \frac{1}{32} \cos\left[\frac{7}{2} (c + d x)\right] + \right. \\ & \left. \frac{5}{12} \sin\left[\frac{1}{2} (c + d x)\right] + \frac{35}{64} \sin\left[\frac{3}{2} (c + d x)\right] - \frac{5}{24} \sin\left[\frac{5}{2} (c + d x)\right] - \frac{1}{32} \sin\left[\frac{7}{2} (c + d x)\right] \right) \Bigg) \\ & \left( d \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^5 \right) - \left( 77 \sqrt{3 - 2 \sqrt{2}} (e \cos[c + d x])^{3/2} \right. \\ & \left. \sec[c + d x] (a (1 + \sin[c + d x]))^{5/2} \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2 \left(1 + \tan\left[\frac{1}{4} (c + d x)\right]^2\right)} \right. \\ & \left. \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\ & \left. \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \end{aligned}$$

$$\begin{aligned}
& \left( 2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \right) \\
& \left( 4 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\
& \quad \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} + \right. \\
& \quad \left. 8 \text{EllipticPi}\left[-3 + 2 \sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right. \\
& \quad \left. \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\
& \quad \left. \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} - \sqrt{2} \left( \text{Log}\left[1 + \tan\left[\frac{1}{4} (c + d x)\right]^2\right] - \right. \right. \\
& \quad \left. \left. \text{Log}\left[2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4}\right]\right) \right. \\
& \quad \left. \left( 1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4 \right) \right) \Bigg) \\
& \left( 128 d \left( \cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right] \right) \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^5 \right. \\
& \quad \left. \left( -4 \sec\left[\frac{1}{4} (c + d x)\right]^2 + 3 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 + 52 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^2 - \right. \right. \\
& \quad \left. \left. 39 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 200 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^4 + \right. \right. \\
& \quad \left. \left. 150 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^4 + 200 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^6 - \right. \right. \\
& \quad \left. \left. 150 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^6 - 52 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^8 + \right. \right. \\
& \quad \left. \left. 39 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^8 + 4 \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^{10} - \right. \right. \\
& \quad \left. \left. 3 \sqrt{2} \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec\left[\frac{1}{4} (c + d x)\right]^2 \right. \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2\left(3-2\sqrt{2}\right)}\sec\left(\frac{1}{4}(c+dx)\right)^2} \\
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^3}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2\left(3-2\sqrt{2}\right)}\sec\left(\frac{1}{4}(c+dx)\right)^2} \\
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^5}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2} + \\
& 6\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 4\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2\tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2\tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} +
\end{aligned}$$

$$\begin{aligned}
& 84 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - \\
& 56 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - \\
& 48 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 6 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - \\
& 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}
\end{aligned}$$

$$\left. \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \right)$$

**Problem 290: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{e \cos[c + d x]} (a + a \sin[c + d x])^{5/2} dx$$

Optimal (type 3, 286 leaves, 9 steps):

$$\begin{aligned} & -\frac{15 a^3 (e \cos[c + d x])^{3/2}}{8 d e \sqrt{a + a \sin[c + d x]}} - \frac{3 a^2 (e \cos[c + d x])^{3/2} \sqrt{a + a \sin[c + d x]}}{4 d e} + \\ & \frac{15 a^2 \sqrt{e} \operatorname{ArcSinh}\left[\frac{\sqrt{e} \cos[c + d x]}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{8 d (1 + \cos[c + d x] + \sin[c + d x])} + \\ & \left( \frac{15 a^2 \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e} \cos[c + d x]}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{8 d (1 + \cos[c + d x] + \sin[c + d x])} - \frac{a (e \cos[c + d x])^{3/2} (a + a \sin[c + d x])^{3/2}}{3 d e} \right) \end{aligned}$$

Result (type 4, 2350 leaves):

$$\begin{aligned} & \left( \sqrt{e \cos[c + d x]} (a (1 + \sin[c + d x]))^{5/2} \right. \\ & \left. \left( -\frac{29}{12} \cos\left[\frac{1}{2} (c + d x)\right] - \frac{5}{8} \cos\left[\frac{3}{2} (c + d x)\right] + \frac{1}{12} \cos\left[\frac{5}{2} (c + d x)\right] + \frac{29}{12} \sin\left[\frac{1}{2} (c + d x)\right] - \right. \right. \\ & \left. \left. \frac{5}{8} \sin\left[\frac{3}{2} (c + d x)\right] - \frac{1}{12} \sin\left[\frac{5}{2} (c + d x)\right] \right) \right) \Big/ \left( d \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^5 \right) - \\ & \left( 225 \cos\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{e \cos[c + d x]} (a (1 + \sin[c + d x]))^{5/2} \left( \sqrt{2} \left( \operatorname{Log}[\sec\left[\frac{1}{4} (c + d x)\right]^2] - \right. \right. \right. \right. \\ & \left. \left. \left. \left. \operatorname{Log}[2 + \sqrt{2}] \sqrt{\cos[c + d x] \sec\left[\frac{1}{4} (c + d x)\right]^4 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) \right. \\ & \left. \left. \left. \left. \sqrt{\cos[c + d x] \sec\left[\frac{1}{4} (c + d x)\right]^4 + 4 \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}]} \right. \right. \right. \\ & \left. \left. \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} + \right. \right. \right. \right) \end{aligned}$$

$$\begin{aligned}
& 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \\
& \left. \left( \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) \right) / \\
& \left( 256 d \sqrt{\operatorname{Cos}[c + d x]} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^6 \right. \\
& \left( \frac{1}{32 \sqrt{\operatorname{Cos}[c + d x]}} 15 \operatorname{Cos}\left[\frac{1}{4}(c + d x)\right] \operatorname{Sin}\left[\frac{1}{4}(c + d x)\right] \left( \sqrt{2} \left( \operatorname{Log}[\operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2] - \right. \right. \right. \\
& \left. \left. \left. \operatorname{Log}[2 + \sqrt{2}] \sqrt{\operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 - 2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) \right. \right. \\
& \left. \left. \sqrt{\operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 + 4 \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \right. \right. \\
& \left. \left. \left. 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} + \right. \right. \\
& \left. \left. 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \right. \\
& \left. \left. \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) - \right. \\
& \left. \frac{1}{32 \operatorname{Cos}[c + d x]^{3/2}} 15 \operatorname{Cos}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Sin}[c + d x] \left( \sqrt{2} \left( \operatorname{Log}[\operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2] - \right. \right. \right. \\
& \left. \left. \left. \operatorname{Log}[2 + \sqrt{2}] \sqrt{\operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 - 2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) \right. \right. \\
& \left. \left. \sqrt{\operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 + 4 \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \right. \right. \\
& \left. \left. \left. 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} + \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 8 \operatorname{EllipticPi}[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}] \\
& \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \\
& \frac{1}{16\sqrt{\operatorname{Cos}[c + d x]}} 15 \operatorname{Cos}\left[\frac{1}{4}(c + d x)\right]^2 \left( \left( \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2\right] - \operatorname{Log}\left[ \right. \right. \right. \\
& \left. \left. \left. 2 + \sqrt{2} \sqrt{\operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 - 2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right] \right) \\
& \left. \left( -\operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 \operatorname{Sin}[c + d x] + \operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \right) \right) \Big/ \left( \sqrt{2} \sqrt{\operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4} \right) + \\
& \left( (-3 + 2\sqrt{2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \\
& \left. \left. \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) \Big/ \\
& \left( \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right. + \left. \left( 2(-3 + 2\sqrt{2}) \operatorname{EllipticPi}[-3 + 2\sqrt{2}, \right. \right. \\
& \left. \left. -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \right. \right. \\
& \left. \left. \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) \Big/ \left( \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) - \\
& \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \right. \\
& \left. \left. \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) \Big/ \left( \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) - 
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \operatorname{EllipticPi} \left[ -3 + 2\sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right) / \\
& \quad \left( \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} + \left( \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \right. \right. \\
& \quad \left. \left. \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right) / \right. \\
& \quad \left. \left( \sqrt{3 - 2\sqrt{2}} \sqrt{1 - \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}}} \right) - \right. \\
& \quad \left. \left( 2 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right. \right. \\
& \quad \left. \left. \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right) / \left( \sqrt{3 - 2\sqrt{2}} \sqrt{1 - \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}}} \right. \right. \\
& \quad \left. \left. \sqrt{1 - \frac{(17 - 12\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}}} \left( 1 - \frac{(-3 + 2\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}} \right) \right) + \right. \\
& \quad \left. \sqrt{2} \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^4} \left( \frac{1}{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] - \left( -\operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] + \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right] \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^4 \right. \right. \\
& \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \right) / \left( \sqrt{2} \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^4} \right) \right) / \\
& \quad \left( 2 + \sqrt{2} \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^4 - 2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right) \right)
\end{aligned}$$

Problem 291: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^{5/2}}{\sqrt{e \cos[c + d x]}} \, dx$$

Optimal (type 3, 247 leaves, 8 steps) :

$$\begin{aligned} & - \frac{7 a^2 \sqrt{e \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{4 d e} - \\ & \frac{21 a^2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{4 d \sqrt{e} (1 + \cos[c + d x] + \sin[c + d x])} + \\ & \left( 21 a^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]} \sqrt{1 + \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]} \right) / \\ & \left( 4 d \sqrt{e} (1 + \cos[c + d x] + \sin[c + d x]) \right) - \frac{a \sqrt{e \cos[c + d x]} (a + a \sin[c + d x])^{3/2}}{2 d e} \end{aligned}$$

Result (type 4, 2782 leaves) :

$$\begin{aligned} & \left( \cos[c + d x] (a (1 + \sin[c + d x]))^{5/2} \right. \\ & \left. \left( -\frac{5}{2} \cos\left[\frac{1}{2} (c + d x)\right] + \frac{1}{4} \cos\left[\frac{3}{2} (c + d x)\right] - \frac{5}{2} \sin\left[\frac{1}{2} (c + d x)\right] - \frac{1}{4} \sin\left[\frac{3}{2} (c + d x)\right] \right) \right) / \\ & \left( d \sqrt{e \cos[c + d x]} \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^5 \right) - \\ & \left( 21 \sqrt{3 - 2 \sqrt{2}} \cos[c + d x] (a (1 + \sin[c + d x]))^{5/2} \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\ & \left. \left( 1 + \tan\left[\frac{1}{4} (c + d x)\right]^2 \right) \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\ & \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\ & \left. \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\ & \left. \left( 2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \right) \right. \\ & \left. \left( 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right) \end{aligned}$$

$$\begin{aligned}
& \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left(\frac{1}{4}(c + d x)\right)}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \\
& \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left(\frac{1}{4}(c + d x)\right)^2} \\
& \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \sqrt{2} \left( \operatorname{Log}\left[1 + \tan\left(\frac{1}{4}(c + d x)\right)^2\right] - \right. \\
& \left. \operatorname{Log}\left[2 - 2 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \sqrt{2} \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4}\right] \right) \\
& \left. \left( 1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4 \right) \right) / \\
& \left( 8 d \sqrt{e \cos(c + d x)} \left( \cos\left(\frac{1}{2}(c + d x)\right) - \sin\left(\frac{1}{2}(c + d x)\right) \right) \left( \cos\left(\frac{1}{2}(c + d x)\right) + \sin\left(\frac{1}{2}(c + d x)\right) \right)^5 \right. \\
& \left( -4 \sec\left(\frac{1}{4}(c + d x)\right)^2 + 3\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 + 52 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 - \right. \\
& 39\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 200 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 + \\
& 150\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 + 200 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^6 - \\
& 150\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^6 - 52 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^8 + \\
& 39\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^8 + 4 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^{10} - \\
& 3\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^{10} + 2 \sqrt{2(3 - 2\sqrt{2})} \sec\left(\frac{1}{4}(c + d x)\right)^2 \\
& \tan\left(\frac{1}{4}(c + d x)\right) \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} - 12 \sqrt{2(3 - 2\sqrt{2})} \sec\left(\frac{1}{4}(c + d x)\right)^2 \\
& \tan\left(\frac{1}{4}(c + d x)\right)^3 \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} + 2 \sqrt{2(3 - 2\sqrt{2})} \sec\left(\frac{1}{4}(c + d x)\right)^2 \\
& \tan\left(\frac{1}{4}(c + d x)\right)^5 \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} + \\
& 6 \sec\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 4\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 48 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 32\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 84 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 56\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} -
\end{aligned}$$

$$\begin{aligned}
& 48 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 6 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - \\
& 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} \Bigg)
\end{aligned}$$

Problem 292: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^{5/2}}{(e \cos[c + d x])^{3/2}} \, dx$$

Optimal (type 3, 239 leaves, 8 steps):

$$\begin{aligned} & \frac{5 a^3 (e \cos[c + d x])^{3/2}}{d e^3 \sqrt{a + a \sin[c + d x]}} - \frac{5 a^2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{d e^{3/2} (1 + \cos[c + d x] + \sin[c + d x])} - \\ & \left( \frac{5 a^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(d e^{3/2} (1 + \cos[c + d x] + \sin[c + d x]))} + \frac{4 a (a + a \sin[c + d x])^{3/2}}{d e \sqrt{e \cos[c + d x]}} \right) \end{aligned}$$

Result (type 4, 2753 leaves):

$$\begin{aligned} & \left( \cos[c + d x]^2 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \frac{8}{\cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right]} - \sin\left[\frac{1}{2} (c + d x)\right] \right) \right. \\ & \left. (a (1 + \sin[c + d x]))^{5/2} \right) \Big/ \left( d (e \cos[c + d x])^{3/2} \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^5 \right) - \\ & \left( 5 \sqrt{3 - 2 \sqrt{2}} \cos[c + d x]^2 (a (1 + \sin[c + d x]))^{5/2} \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\ & \left. \left( 1 + \tan\left[\frac{1}{4} (c + d x)\right]^2 \right) \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\ & \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\ & \left. \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\ & \left. \left( 2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \right) \right. \\ & \left. \left( 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \right. \\ & \left. \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} + \right. \right. \end{aligned}$$

$$\begin{aligned}
& 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \\
& \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4} + \sqrt{2} \left( \operatorname{Log}\left[1 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2\right] - \right. \\
& \left. \operatorname{Log}\left[2 - 2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4}\right] \right) \\
& \left. \left( 1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4 \right) \right) / \\
& \left( 2 d (e \operatorname{Cos}[c + d x])^{3/2} \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^6 \right. \\
& \left( 4 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 - 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 - 52 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \right. \\
& 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + 200 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4 - \\
& 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4 - 200 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^6 + \\
& 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^6 + 52 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^8 - \\
& 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^8 - 4 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^{10} + \\
& 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^{10} + 2 \sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - 12 \sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2}
\end{aligned}$$

$$\begin{aligned}
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^3}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2} + 2\sqrt{2(3-2\sqrt{2})} \sec\left(\frac{1}{4}(c+dx)\right)^2 \\
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^5}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2} - \\
& 6\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 4\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 84\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 56\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} -
\end{aligned}$$

$$\begin{aligned}
& 6 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right] \\
& \sqrt{3 - 2 \sqrt{2}} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^3 \sqrt{3 - 2 \sqrt{2}} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} \Bigg)
\end{aligned}$$

Problem 293: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^{5/2}}{(e \cos[c + d x])^{5/2}} dx$$

Optimal (type 3, 204 leaves, 7 steps):

$$\begin{aligned}
& \frac{2 a^2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c+d x]}}{\sqrt{e}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{d e^{5/2} (1+\cos [c+d x]+\sin [c+d x])} - \\
& \left(2 a^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c+d x]}{\sqrt{e \cos [c+d x]}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}\right) / \\
& \left(d e^{5/2} (1+\cos [c+d x]+\sin [c+d x])\right) + \frac{4 a (a+a \sin [c+d x])^{3/2}}{3 d e (e \cos [c+d x])^{3/2}}
\end{aligned}$$

Result (type 4, 2795 leaves):

$$\begin{aligned}
& \left(\cos [c+d x]^3 \left(\frac{4}{3 (\cos [\frac{1}{2} (c+d x)] - \sin [\frac{1}{2} (c+d x)])} + \frac{8 \sin [\frac{1}{2} (c+d x)]}{3 (\cos [\frac{1}{2} (c+d x)] - \sin [\frac{1}{2} (c+d x)])^2}\right) \right. \\
& \left. (a (1+\sin [c+d x]))^{5/2}\right) / \left(d (e \cos [c+d x])^{5/2} (\cos [\frac{1}{2} (c+d x)] + \sin [\frac{1}{2} (c+d x)])^5\right) + \\
& \left(\sqrt{3-2 \sqrt{2}} \cos [c+d x]^3 (a (1+\sin [c+d x]))^{5/2} \sqrt{\frac{-3+2 \sqrt{2}+\tan [\frac{1}{4} (c+d x)]^2}{-3+2 \sqrt{2}}}\right. \\
& \left(\tan [\frac{1}{4} (c+d x)]^2\right) \sqrt{\frac{-3+2 \sqrt{2}+\tan [\frac{1}{4} (c+d x)]^2}{-3+2 \sqrt{2}}} \\
& \sqrt{\frac{-3+2 \sqrt{2}+17 \tan [\frac{1}{4} (c+d x)]^2-12 \sqrt{2} \tan [\frac{1}{4} (c+d x)]^2}{-3+2 \sqrt{2}}} \\
& \sqrt{1-3 \tan [\frac{1}{4} (c+d x)]^2+2 \sqrt{2} \tan [\frac{1}{4} (c+d x)]^2} \\
& \left(2-2 \tan [\frac{1}{4} (c+d x)]^2+\sqrt{2} \sqrt{1-6 \tan [\frac{1}{4} (c+d x)]^2+\tan [\frac{1}{4} (c+d x)]^4}\right) \\
& \left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan [\frac{1}{4} (c+d x)]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan [\frac{1}{4} (c+d x)]^2}\right. \\
& \left.\sqrt{1+\left(-3+2 \sqrt{2}\right) \tan [\frac{1}{4} (c+d x)]^2} \sqrt{1-6 \tan [\frac{1}{4} (c+d x)]^2+\tan [\frac{1}{4} (c+d x)]^4} + \right. \\
& \left. 8 \operatorname{EllipticPi}\left[-3+2 \sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan [\frac{1}{4} (c+d x)]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]\right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left(\frac{1}{4}(c + d x)\right)^2} \\
& \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \sqrt{2} \left( \log\left[1 + \tan\left(\frac{1}{4}(c + d x)\right)^2\right] - \right. \\
& \left. \log\left[2 - 2 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \sqrt{2} \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4}\right] \right) \\
& \left. \left( 1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4 \right) \right) / \\
& \left( d (e \cos(c + d x))^{5/2} \left( \cos\left(\frac{1}{2}(c + d x)\right) - \sin\left(\frac{1}{2}(c + d x)\right) \right) \right. \\
& \left( \cos\left(\frac{1}{2}(c + d x)\right) + \sin\left(\frac{1}{2}(c + d x)\right) \right)^5 \\
& \left( -4 \sec\left(\frac{1}{4}(c + d x)\right)^2 + 3\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 + 52 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 - \right. \\
& 39\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 200 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 + \\
& 150\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 + 200 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^6 - \\
& 150\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^6 - 52 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^8 + \\
& 39\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^8 + 4 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^{10} - \\
& 3\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^{10} + 2 \sqrt{2(3 - 2\sqrt{2})} \sec\left(\frac{1}{4}(c + d x)\right)^2 \\
& \tan\left(\frac{1}{4}(c + d x)\right) \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12 \sqrt{2(3 - 2\sqrt{2})} \sec\left(\frac{1}{4}(c + d x)\right)^2}
\end{aligned}$$

$$\begin{aligned}
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^3}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2} + 2\sqrt{2(3-2\sqrt{2})} \sec\left(\frac{1}{4}(c+dx)\right)^2 \\
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^5}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2} + \\
& 6\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 4\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 84\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 56\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} +
\end{aligned}$$

$$\begin{aligned}
& 6 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 4 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \\
& \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} \Bigg)
\end{aligned}$$

Problem 294: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin(c + d x))^{5/2}}{(e \cos(c + d x))^{7/2}} dx$$

Optimal (type 3, 36 leaves, 1 step):

$$\frac{2 (a + a \sin(c + d x))^{5/2}}{5 d e (e \cos(c + d x))^{5/2}}$$

Result (type 3, 87 leaves):

$$\frac{2 a^2 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \sqrt{a (1 + \sin [c + d x])}}{5 d e^3 \sqrt{e \cos [c + d x]} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2}$$

Problem 298: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{5/2}}{\sqrt{a + a \sin [c + d x]}} dx$$

Optimal (type 3, 244 leaves, 8 steps):

$$\begin{aligned} & - \frac{a (e \cos [c + d x])^{7/2}}{2 d e (a + a \sin [c + d x])^{3/2}} + \frac{e (e \cos [c + d x])^{3/2}}{4 d \sqrt{a + a \sin [c + d x]}} + \\ & \frac{3 e^{5/2} \operatorname{ArcSinh} \left[ \frac{\sqrt{e \cos [c + d x]}}{\sqrt{e}} \right] \sqrt{1 + \cos [c + d x]} \sqrt{a + a \sin [c + d x]}}{4 d (a + a \cos [c + d x] + a \sin [c + d x])} + \\ & \left( \frac{3 e^{5/2} \operatorname{ArcTan} \left[ \frac{\sqrt{e} \sin [c + d x]}{\sqrt{e \cos [c + d x]} \sqrt{1 + \cos [c + d x]}} \right] \sqrt{1 + \cos [c + d x]} \sqrt{a + a \sin [c + d x]}}{(4 d (a + a \cos [c + d x] + a \sin [c + d x]))} \right) \end{aligned}$$

Result (type 4, 2305 leaves):

$$\begin{aligned} & \left( (e \cos [c + d x])^{5/2} \sec [c + d x]^2 \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\ & \left. \left( -\frac{1}{2} \cos \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{4} \cos \left[ \frac{3}{2} (c + d x) \right] + \frac{1}{2} \sin \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{4} \sin \left[ \frac{3}{2} (c + d x) \right] \right) \right) / \\ & \left( d \sqrt{a (1 + \sin [c + d x])} \right) - \\ & \left( 9 \cos \left[ \frac{1}{4} (c + d x) \right]^2 (e \cos [c + d x])^{5/2} \left( \sqrt{2} \left( \operatorname{Log} [\sec \left[ \frac{1}{4} (c + d x) \right]^2] - \right. \right. \right. \\ & \left. \left. \left. \operatorname{Log} [2 + \sqrt{2}] \sqrt{\cos [c + d x] \sec \left[ \frac{1}{4} (c + d x) \right]^4 - 2 \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right. \\ & \left. \sqrt{\cos [c + d x] \sec \left[ \frac{1}{4} (c + d x) \right]^4 + 4 \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right]} \right. \\ & \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2} + \right) \end{aligned}$$

$$\begin{aligned}
& 8 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right],17-12 \sqrt{2}\right] \\
& \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2} \sqrt{1+\left(-3+2 \sqrt{2}\right) \operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2}\Bigg)\Bigg) \\
& \left(\frac{1}{16 \sqrt{\cos [c+d x]}} 3 \cos \left[\frac{1}{4} (c+d x)\right] \sin \left[\frac{1}{4} (c+d x)\right]\right. \\
& \left.\left(\sqrt{2} \left(\operatorname{Log}\left[\sec \left[\frac{1}{4} (c+d x)\right]^2\right]-\operatorname{Log}\left[2+\sqrt{2}\right] \sqrt{\cos [c+d x] \sec \left[\frac{1}{4} (c+d x)\right]^4-2 \operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2}\right)\right. \\
& \left.\sqrt{\cos [c+d x] \sec \left[\frac{1}{4} (c+d x)\right]^4+4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right],\right.\right. \\
& \left.\left.17-12 \sqrt{2}\right]\sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2} \sqrt{1+\left(-3+2 \sqrt{2}\right) \operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2}+8 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right],17-12 \sqrt{2}\right]\right. \\
& \left.\left(\sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2} \sqrt{1+\left(-3+2 \sqrt{2}\right) \operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2}\right)-\frac{1}{16 \cos [c+d x]^{3/2}} 3 \cos \left[\frac{1}{4} (c+d x)\right]^2 \sin [c+d x]\right. \\
& \left.\left(\sqrt{2} \left(\operatorname{Log}\left[\sec \left[\frac{1}{4} (c+d x)\right]^2\right]-\operatorname{Log}\left[2+\sqrt{2}\right] \sqrt{\cos [c+d x] \sec \left[\frac{1}{4} (c+d x)\right]^4-2 \operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2}\right)\right. \\
& \left.\left.\sqrt{\cos [c+d x] \sec \left[\frac{1}{4} (c+d x)\right]^4+4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right],\right.\right. \\
& \left.\left.17-12 \sqrt{2}\right]\sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2} \sqrt{1+\left(-3+2 \sqrt{2}\right) \operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]^2}+8 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4} (c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right],17-12 \sqrt{2}\right]\right)\right)\right)
\end{aligned}$$

$$\begin{aligned}
& 8 \operatorname{EllipticPi}[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}] \\
& \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \\
& \frac{1}{8\sqrt{\operatorname{Cos}[c + d x]}} 3 \operatorname{Cos}\left[\frac{1}{4}(c + d x)\right]^2 \left( \left( \operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2\right] - \operatorname{Log}\left[2 + \sqrt{2} \sqrt{\operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 - 2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2}\right] \right. \right. \\
& \left. \left. \left( -\operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 \operatorname{Sin}[c + d x] + \operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]\right) \right) \right) \Big/ \left( \sqrt{2} \sqrt{\operatorname{Cos}[c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4} \right) + \\
& \left( (-3 + 2\sqrt{2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \\
& \left. \left. \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) \right) \Big/ \\
& \left( \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) + \left( 2(-3 + 2\sqrt{2}) \operatorname{EllipticPi}[-3 + 2\sqrt{2}, \right. \\
& \left. -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \right. \\
& \left. \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) \Big/ \left( \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) - \\
& \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \right. \\
& \left. \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) \Big/ \left( \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \right) - 
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \operatorname{EllipticPi} \left[ -3 + 2\sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right) / \\
& \quad \left( \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} + \left( \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \right. \right. \\
& \quad \left. \left. \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right) / \right. \\
& \quad \left. \left( \sqrt{3 - 2\sqrt{2}} \sqrt{1 - \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}}} \right) - \right. \\
& \quad \left. \left( 2 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right. \right. \\
& \quad \left. \left. \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right) / \left( \sqrt{3 - 2\sqrt{2}} \sqrt{1 - \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}}} \right. \right. \\
& \quad \left. \left. \sqrt{1 - \frac{(17 - 12\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}}} \left( 1 - \frac{(-3 + 2\sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2\sqrt{2}} \right) \right) + \right. \\
& \quad \left. \sqrt{2} \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^4} \left( \frac{1}{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] - \left( -\operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] + \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right] \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^4 \right. \right. \\
& \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \right) / \left( \sqrt{2} \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^4} \right) \right) / \\
& \quad \left( 2 + \sqrt{2} \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^4 - 2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right) \right)
\end{aligned}$$

Problem 299: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(\mathbf{e} \cos[c + d x])^{3/2}}{\sqrt{a + a \sin[c + d x]}} dx$$

Optimal (type 3, 200 leaves, 7 steps) :

$$\begin{aligned} & \frac{e \sqrt{e \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{a d} - \\ & \frac{e^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{a d (1 + \cos[c + d x] + \sin[c + d x])} + \\ & \left( \frac{e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]} \sqrt{1 + \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(a d (1 + \cos[c + d x] + \sin[c + d x]))} \right) \end{aligned}$$

Result (type 4, 2723 leaves) :

$$\begin{aligned} & \frac{(\mathbf{e} \cos[c + d x])^{3/2} \sec[c + d x] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^2}{d \sqrt{a (1 + \sin[c + d x])}} - \\ & \left( \sqrt{3 - 2 \sqrt{2}} (\mathbf{e} \cos[c + d x])^{3/2} \sec[c + d x] \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right) \right. \\ & \left. \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \left(1 + \tan\left[\frac{1}{4} (c + d x)\right]^2\right) \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\ & \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\ & \left. \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\ & \left. \left(2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4}\right) \right. \\ & \left. \left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \right. \\ & \left. \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} + \right. \right. \end{aligned}$$

$$\begin{aligned}
& 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \\
& \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4} - \sqrt{2} \left( \operatorname{Log}\left[1 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2\right] - \right. \\
& \left. \operatorname{Log}\left[2 - 2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4}\right] \right) \\
& \left. \left( 1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4 \right) \right) / \\
& \left( 2 d \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \sqrt{a (1 + \operatorname{Sin}[c + d x])} \right. \\
& \left( -4 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 + 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 + 52 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - \right. \\
& 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - 200 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4 + \\
& 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4 + 200 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^6 - \\
& 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^6 - 52 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^8 + \\
& 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^8 + 4 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^{10} - \\
& 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^{10} + 2 \sqrt{2 (3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - 12 \sqrt{2 (3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2}
\end{aligned}$$

$$\begin{aligned}
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^3}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2} + 2\sqrt{2(3-2\sqrt{2})} \sec\left(\frac{1}{4}(c+dx)\right)^2 \\
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^5}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2} + \\
& 6\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 4\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 84\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 56\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} +
\end{aligned}$$

$$\begin{aligned}
& 6 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 4 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \\
& \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} \Bigg)
\end{aligned}$$

Problem 300: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{e \cos [c + d x]}}{\sqrt{a + a \sin [c + d x]}} \, dx$$

Optimal (type 3, 169 leaves, 6 steps):

$$\frac{2 \sqrt{e} \operatorname{ArcSinh}\left[\frac{\sqrt{e} \cos [c+d x]}{\sqrt{e}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{d (a+a \cos [c+d x]+a \sin [c+d x])} +$$

$$\left(\frac{2 \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c+d x]}{\sqrt{e} \cos [c+d x]}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{(d (a+a \cos [c+d x]+a \sin [c+d x]))}\right)$$

Result (type 4, 2607 leaves):

$$\left(\sqrt{3-2 \sqrt{2}} \sqrt{e \cos [c+d x]} \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4} (c+d x)\right]^2} \left(1+\tan \left[\frac{1}{4} (c+d x)\right]^2\right)\right.$$

$$\sqrt{\frac{-3+2 \sqrt{2}+\tan \left[\frac{1}{4} (c+d x)\right]^2}{-3+2 \sqrt{2}}} \sqrt{\frac{-3+2 \sqrt{2}+17 \tan \left[\frac{1}{4} (c+d x)\right]^2-12 \sqrt{2} \tan \left[\frac{1}{4} (c+d x)\right]^2}{-3+2 \sqrt{2}}}$$

$$\sqrt{1-3 \tan \left[\frac{1}{4} (c+d x)\right]^2+2 \sqrt{2} \tan \left[\frac{1}{4} (c+d x)\right]^2}$$

$$\left.2-2 \tan \left[\frac{1}{4} (c+d x)\right]^2+\sqrt{2} \sqrt{1-6 \tan \left[\frac{1}{4} (c+d x)\right]^2+\tan \left[\frac{1}{4} (c+d x)\right]^4}\right)$$

$$\left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4} (c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4} (c+d x)\right]^2}\right.$$

$$\sqrt{1+\left(-3+2 \sqrt{2}\right) \tan \left[\frac{1}{4} (c+d x)\right]^2} \sqrt{1-6 \tan \left[\frac{1}{4} (c+d x)\right]^2+\tan \left[\frac{1}{4} (c+d x)\right]^4} +$$

$$8 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4} (c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]$$

$$\sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4} (c+d x)\right]^2} \sqrt{1+\left(-3+2 \sqrt{2}\right) \tan \left[\frac{1}{4} (c+d x)\right]^2}$$

$$\sqrt{1-6 \tan \left[\frac{1}{4} (c+d x)\right]^2+\tan \left[\frac{1}{4} (c+d x)\right]^4}+\sqrt{2} \left(\operatorname{Log}\left[1+\tan \left[\frac{1}{4} (c+d x)\right]^2\right]-\right.$$

$$\left.\operatorname{Log}\left[2-2 \tan \left[\frac{1}{4} (c+d x)\right]^2+\sqrt{2}\right] \sqrt{1-6 \tan \left[\frac{1}{4} (c+d x)\right]^2+\tan \left[\frac{1}{4} (c+d x)\right]^4}\right)$$

$$\begin{aligned}
& \left. \left( 1 - 6 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + \tan \left[ \frac{1}{4} (c + d x) \right]^4 \right) \right) \Bigg/ \left( d \sqrt{a (1 + \sin [c + d x])} \right) \\
& \left( 4 \sec \left[ \frac{1}{4} (c + d x) \right]^2 - 3 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 - 52 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + \right. \\
& \quad 39 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 200 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^4 - \\
& \quad 150 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^4 - 200 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^6 + \\
& \quad 150 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^6 + 52 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^8 - \\
& \quad 39 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^8 - 4 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^{10} + \\
& \quad 3 \sqrt{2} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec \left[ \frac{1}{4} (c + d x) \right]^2 \\
& \quad \tan \left[ \frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{1 - 3 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2 (3 - 2 \sqrt{2})} \sec \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \quad \tan \left[ \frac{1}{4} (c + d x) \right]^3 \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{1 - 3 \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \quad \tan \left[ \frac{1}{4} (c + d x) \right]^5 \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} - \\
& 6 \sec\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 4\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 48 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 32\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 84 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 56\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 48 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^6 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 32\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^6 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 6 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^8 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 4\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^8 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 4\sqrt{3 - 2\sqrt{2}} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right) \\
& \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} \\
& \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4 - 4\sqrt{3 - 2\sqrt{2}} \sec\left(\frac{1}{4}(c + d x)\right)^2} \\
& \tan\left(\frac{1}{4}(c + d x)\right)^3 \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} \\
& \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} \Bigg)
\end{aligned}$$

Problem 305: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^{7/2}}{(a + a \sin[c + d x])^{3/2}} dx$$

Optimal (type 3, 247 leaves, 8 steps):

$$\begin{aligned}
& \frac{e (e \cos[c + d x])^{5/2}}{2 a d \sqrt{a + a \sin[c + d x]}} + \frac{5 e^3 \sqrt{e \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{4 a^2 d} - \\
& \frac{5 e^{7/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{4 a^2 d (1 + \cos[c + d x] + \sin[c + d x])} + \\
& \left( \frac{5 e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]} \sqrt{1 + \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(4 a^2 d (1 + \cos[c + d x] + \sin[c + d x]))} \right)
\end{aligned}$$

Result (type 4, 2786 leaves):

$$\begin{aligned}
& \left( (e \cos[c + d x])^{7/2} \sec[c + d x]^3 \left( \cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^3 \right. \\
& \left. \left( \frac{3}{2} \cos\left[\frac{1}{2}(c + d x)\right] + \frac{1}{4} \cos\left[\frac{3}{2}(c + d x)\right] + \frac{3}{2} \sin\left[\frac{1}{2}(c + d x)\right] - \frac{1}{4} \sin\left[\frac{3}{2}(c + d x)\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( d \left( a \left( 1 + \sin(c + d x) \right) \right)^{3/2} \right) - \left( 5 \sqrt{3 - 2 \sqrt{2}} \left( e \cos(c + d x) \right)^{7/2} \sec(c + d x)^3 \right. \\
& \left( \cos\left(\frac{1}{2}(c + d x)\right) + \sin\left(\frac{1}{2}(c + d x)\right) \right)^3 \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \left( 1 + \tan\left(\frac{1}{4}(c + d x)\right)^2 \right) \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2 \sqrt{2}}} \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12 \sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2 \sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} \\
& \left( 2 - 2 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \sqrt{2} \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} \right) \\
& \left( 4 \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\tan\left(\frac{1}{4}(c + d x)\right)}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \right. \\
& \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \right. \\
& \left. 8 \text{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\text{ArcSin} \left[ \frac{\tan\left(\frac{1}{4}(c + d x)\right)}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \\
& \left. \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left(\frac{1}{4}(c + d x)\right)^2} \right. \\
& \left. \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \sqrt{2} \left( \text{Log} \left[ 1 + \tan\left(\frac{1}{4}(c + d x)\right)^2 \right] - \right. \right. \\
& \left. \left. \text{Log} \left[ 2 - 2 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \sqrt{2} \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} \right] \right) \right. \\
& \left. \left( 1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4 \right) \right) \Bigg) \\
& \left( 8 d \left( \cos\left(\frac{1}{2}(c + d x)\right) - \sin\left(\frac{1}{2}(c + d x)\right) \right) \left( a \left( 1 + \sin(c + d x) \right) \right)^{3/2} \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -4 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 + 3 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 + 52 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - \right. \\
& \quad 39 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 200 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 + \\
& \quad 150 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 + 200 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 - \\
& \quad 150 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 - 52 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 + \\
& \quad 39 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 + 4 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^{10} - \\
& \quad 3 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \\
& \quad \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2 (3 - 2 \sqrt{2})} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \quad \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2 (3 - 2 \sqrt{2})} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \quad \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^5 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \quad \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + }
\end{aligned}$$

$$\begin{aligned}
& 6 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 4 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 48 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 32 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 84 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 56 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 48 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 32 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 6 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \\
& 4 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - 4 \sqrt{3 - 2\sqrt{2}} \sec\left(\frac{1}{4}(c + d x)\right)^2 \\
& \tan\left(\frac{1}{4}(c + d x)\right)^3 \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} \\
& \left. \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} \right)
\end{aligned}$$

Problem 306: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^{5/2}}{(a + a \sin[c + d x])^{3/2}} dx$$

Optimal (type 3, 215 leaves, 7 steps):

$$\begin{aligned}
& \frac{e (e \cos[c + d x])^{3/2}}{a d \sqrt{a + a \sin[c + d x]}} + \frac{3 e^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{d (a^2 + a^2 \cos[c + d x] + a^2 \sin[c + d x])} + \\
& \left. \left( \frac{3 e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(d (a^2 + a^2 \cos[c + d x] + a^2 \sin[c + d x]))} \right) \right)
\end{aligned}$$

Result (type 4, 2726 leaves):

$$\begin{aligned}
& \left( (e \cos[c + d x])^{5/2} \sec[c + d x]^2 \left( \cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right) \right. \\
& \left. \left( \cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) \Big/ \left( d (a (1 + \sin[c + d x]))^{3/2} \right) + \\
& \left. \left( 3 \sqrt{3 - 2\sqrt{2}} (e \cos[c + d x])^{5/2} \sec[c + d x]^2 \left( \cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right. \right. \\
& \left. \left. \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \left( 1 + \tan\left(\frac{1}{4}(c + d x)\right)^2 \right) \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \right) \right)
\end{aligned}$$



$$\begin{aligned}
& 3\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^{10} + 2\sqrt{2\left(3-2\sqrt{2}\right)} \sec\left[\frac{1}{4}(c+dx)\right]^2 \\
& \tan\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2\left(3-2\sqrt{2}\right)}\sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2\left(3-2\sqrt{2}\right)}\sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2-} \\
& 6\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
& 4\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
& 48\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
& 32\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} -
\end{aligned}$$

$$\begin{aligned}
& 84 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 56 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 48 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - \\
& 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - \\
& 6 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}
\end{aligned}$$

$$\sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \Bigg)$$

**Problem 307: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(\cos[c + d x])^{3/2}}{(\sin[c + d x])^{3/2}} \, dx$$

Optimal (type 3, 236 leaves, 8 steps):

$$\begin{aligned} & - \frac{2 (\cos[c + d x])^{5/2}}{d e (\sin[c + d x])^{3/2}} - \frac{2 e \sqrt{\cos[c + d x]} \sqrt{\sin[c + d x]}}{a^2 d} + \\ & \frac{2 e^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{\cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{\sin[c + d x]}}{a^2 d (1 + \cos[c + d x] + \sin[c + d x])} - \\ & \left( \frac{2 e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{\cos[c + d x]} \sqrt{1 + \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{\sin[c + d x]}}{(a^2 d (1 + \cos[c + d x] + \sin[c + d x]))} \right) \Bigg) \end{aligned}$$

Result (type 4, 2723 leaves):

$$\begin{aligned} & - \left( \left( 4 (\cos[c + d x])^{3/2} \sec[c + d x] \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^2 \right) \Big/ \right. \\ & \left. \left( d (a (1 + \sin[c + d x]))^{3/2} \right) \right) + \\ & \left( \sqrt{3 - 2 \sqrt{2}} (\cos[c + d x])^{3/2} \sec[c + d x] \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^3 \right. \\ & \left. \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \left( 1 + \tan\left[\frac{1}{4} (c + d x)\right]^2 \right) \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\ & \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \right. \\ & \left. \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2} \right. \\ & \left. \left( 2 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \right) \right) \end{aligned}$$

$$\begin{aligned}
& \left( 4 \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \right. \\
& \quad \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} + \right. \\
& \quad 8 \operatorname{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \\
& \quad \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \\
& \quad \left. \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} - \sqrt{2} \left( \operatorname{Log} \left[ 1 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 \right] - \right. \right. \\
& \quad \left. \left. \operatorname{Log} \left[ 2 - 2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4} \right] \right) \right. \\
& \quad \left. \left( 1 - 6 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 \right) \right) \Bigg) \Bigg/ \\
& \left( d \left( \operatorname{Cos} \left[ \frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[ \frac{1}{2} (c + d x) \right] \right) (a (1 + \operatorname{Sin} [c + d x]))^{3/2} \right. \\
& \quad \left( -4 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 + 3 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 + 52 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - \right. \\
& \quad \left. 39 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2 - 200 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 + \right. \\
& \quad \left. 150 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^4 + 200 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 - \right. \\
& \quad \left. 150 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^6 - 52 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 + \right. \\
& \quad \left. 39 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^8 + 4 \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^{10} - \right. \\
& \quad \left. 3 \sqrt{2} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \operatorname{Sec} \left[ \frac{1}{4} (c + d x) \right]^2 \right. \\
& \quad \left. \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[ \frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2 \left(3 - 2\sqrt{2}\right)} \sec\left(\frac{1}{4}(c + d x)\right)^2} \\
& \tan\left(\frac{1}{4}(c + d x)\right)^3 \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2 \left(3 - 2\sqrt{2}\right)} \sec\left(\frac{1}{4}(c + d x)\right)^2} \\
& \tan\left(\frac{1}{4}(c + d x)\right)^5 \sqrt{3 - 2\sqrt{2} - \tan\left(\frac{1}{4}(c + d x)\right)^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left(\frac{1}{4}(c + d x)\right)^2 - 12\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left(\frac{1}{4}(c + d x)\right)^2 + 2\sqrt{2} \tan\left(\frac{1}{4}(c + d x)\right)^2} + \\
& 6 \sec\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 4\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} - \\
& 48 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 32\sqrt{2} \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^2 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} + \\
& 84 \sec\left(\frac{1}{4}(c + d x)\right)^2 \tan\left(\frac{1}{4}(c + d x)\right)^4 \sqrt{1 - 6 \tan\left(\frac{1}{4}(c + d x)\right)^2 + \tan\left(\frac{1}{4}(c + d x)\right)^4} -
\end{aligned}$$

$$\begin{aligned}
& 56\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
& 48 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
& 32\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
& 6 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
& 4\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
& 4\sqrt{3-2\sqrt{2}} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right] \\
& \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2} + 17\tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} - 4\sqrt{3-2\sqrt{2}} \sec\left[\frac{1}{4}(c+dx)\right]^2 \\
& \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2} + 17\tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} \Bigg)
\end{aligned}$$

Problem 313: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^{9/2}}{(a + a \sin[c + d x])^{5/2}} dx$$

Optimal (type 3, 261 leaves, 9 steps):

$$\begin{aligned} & \frac{e (e \cos[c + d x])^{7/2}}{2 a d (a + a \sin[c + d x])^{3/2}} + \frac{7 e^3 (e \cos[c + d x])^{3/2}}{4 a^2 d \sqrt{a + a \sin[c + d x]}} + \\ & \frac{21 e^{9/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{4 d (a^3 + a^3 \cos[c + d x] + a^3 \sin[c + d x])} + \\ & \left( \frac{21 e^{9/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + d x]}{\sqrt{e \cos[c + d x]}}\right] \sqrt{1 + \cos[c + d x]} \sqrt{a + a \sin[c + d x]}}{(4 d (a^3 + a^3 \cos[c + d x] + a^3 \sin[c + d x]))} \right) \end{aligned}$$

Result (type 4, 2330 leaves):

$$\begin{aligned} & \left( (e \cos[c + d x])^{9/2} \operatorname{Sec}[c + d x]^4 \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^5 \right. \\ & \left. \left( \frac{5}{2} \cos\left[\frac{1}{2} (c + d x)\right] - \frac{1}{4} \cos\left[\frac{3}{2} (c + d x)\right] - \frac{5}{2} \sin\left[\frac{1}{2} (c + d x)\right] - \frac{1}{4} \sin\left[\frac{3}{2} (c + d x)\right] \right) \right) \Big/ \\ & \left( d (a (1 + \sin[c + d x]))^{5/2} \right) - \left( 441 \cos\left[\frac{1}{4} (c + d x)\right]^2 (e \cos[c + d x])^{9/2} \right. \\ & \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)^4 \sqrt{2} \left( \operatorname{Log}[\operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2] - \right. \\ & \left. \left. \operatorname{Log}[2 + \sqrt{2}] \sqrt{\cos[c + d x] \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^4 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right. \\ & \left. \sqrt{\cos[c + d x] \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^4 + 4 \operatorname{EllipticF}[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}]} \right. \\ & \left. \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} + \right. \\ & \left. 8 \operatorname{EllipticPi}\left[-3 + 2 \sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \right) \end{aligned}$$

$$\begin{aligned}
& \left. \left( \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left(\frac{1}{4} (c + d x)\right)^2} \right) \right) / \\
& \left( 64 d \cos[c + d x]^{9/2} (a (1 + \sin[c + d x]))^{5/2} \right. \\
& \left( \frac{1}{16 \sqrt{\cos[c + d x]}} 21 \cos\left(\frac{1}{4} (c + d x)\right) \sin\left(\frac{1}{4} (c + d x)\right) \left( \sqrt{2} \left( \log[\sec\left(\frac{1}{4} (c + d x)\right)^2] - \right. \right. \right. \right. \\
& \left. \left. \left. \left. \log[2 + \sqrt{2} \sqrt{\cos[c + d x] \sec\left(\frac{1}{4} (c + d x)\right)^4} - 2 \tan\left(\frac{1}{4} (c + d x)\right)^2] \right) \right) \right. \\
& \left. \sqrt{\cos[c + d x] \sec\left(\frac{1}{4} (c + d x)\right)^4} + 4 \text{EllipticF}[\text{ArcSin}\left(\frac{\tan\left(\frac{1}{4} (c + d x)\right)}{\sqrt{3 - 2 \sqrt{2}}}\right), \right. \\
& 17 - 12 \sqrt{2}] \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left(\frac{1}{4} (c + d x)\right)^2} + \\
& 8 \text{EllipticPi}\left[-3 + 2 \sqrt{2}, -\text{ArcSin}\left(\frac{\tan\left(\frac{1}{4} (c + d x)\right)}{\sqrt{3 - 2 \sqrt{2}}}\right), 17 - 12 \sqrt{2}\right] \\
& \left. \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left(\frac{1}{4} (c + d x)\right)^2} \right) - \\
& \frac{1}{16 \cos[c + d x]^{3/2}} 21 \cos\left(\frac{1}{4} (c + d x)\right)^2 \sin[c + d x] \left( \sqrt{2} \left( \log[\sec\left(\frac{1}{4} (c + d x)\right)^2] - \right. \right. \\
& \left. \left. \log[2 + \sqrt{2} \sqrt{\cos[c + d x] \sec\left(\frac{1}{4} (c + d x)\right)^4} - 2 \tan\left(\frac{1}{4} (c + d x)\right)^2] \right) \right. \\
& \left. \sqrt{\cos[c + d x] \sec\left(\frac{1}{4} (c + d x)\right)^4} + 4 \text{EllipticF}[\text{ArcSin}\left(\frac{\tan\left(\frac{1}{4} (c + d x)\right)}{\sqrt{3 - 2 \sqrt{2}}}\right), \right. \\
& 17 - 12 \sqrt{2}] \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left(\frac{1}{4} (c + d x)\right)^2} + \\
& 8 \text{EllipticPi}\left[-3 + 2 \sqrt{2}, -\text{ArcSin}\left(\frac{\tan\left(\frac{1}{4} (c + d x)\right)}{\sqrt{3 - 2 \sqrt{2}}}\right), 17 - 12 \sqrt{2}\right]
\end{aligned}$$

$$\begin{aligned}
& \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} - \\
& \frac{1}{8 \sqrt{\cos[c + d x]}} 21 \cos\left[\frac{1}{4} (c + d x)\right]^2 \left( \left( \left( \log[\sec\left[\frac{1}{4} (c + d x)\right]^2] - \log\left[ \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. 2 + \sqrt{2} \sqrt{\cos[c + d x] \sec\left[\frac{1}{4} (c + d x)\right]^4 - 2 \tan\left[\frac{1}{4} (c + d x)\right]^2} \right] \right) \right. \right. \\
& \left. \left. \left. \left. \left. \left. \left( -\sec\left[\frac{1}{4} (c + d x)\right]^4 \sin[c + d x] + \cos[c + d x] \sec\left[\frac{1}{4} (c + d x)\right]^4 \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. \left. \tan\left[\frac{1}{4} (c + d x)\right] \right) \right) \right/ \left( \sqrt{2} \sqrt{\cos[c + d x] \sec\left[\frac{1}{4} (c + d x)\right]^4} \right) + \right. \\
& \left( (-3 + 2 \sqrt{2}) \text{EllipticF}[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \right. \\
& \left. \left. \left. \left. \left. \left. \left. \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right/ \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. \left. \left( \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) + \left( 2 (-3 + 2 \sqrt{2}) \text{EllipticPi}[-3 + 2 \sqrt{2}, \right. \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. \left. \left. -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right] \right) \right/ \left( \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) - \right. \right. \right. \\
& \left( \text{EllipticF}[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \sec\left[\frac{1}{4} (c + d x)\right]^2 \tan\left[\frac{1}{4} (c + d x)\right] \right. \\
& \left. \left. \left. \left. \left. \left. \left. \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) \right/ \left( \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \right) - \right. \right. \right. \right. \right. \right. \right. \\
& \left( 2 \text{EllipticPi}[-3 + 2 \sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}] \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \frac{\sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right] \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2}}{\sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2}} + \left( \frac{\sec \left[ \frac{1}{4} (c + d x) \right]^2}{\sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2}} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2}} \right) \right) \right. \\
& \left. \left( \sqrt{3 - 2 \sqrt{2}} \sqrt{1 - \frac{\tan \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2 \sqrt{2}}} \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2 \sqrt{2}}} \right) - \right. \\
& \left. \left( 2 \sec \left[ \frac{1}{4} (c + d x) \right]^2 \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right. \right. \\
& \left. \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2} \right) \right) \right. \\
& \left. \left( \sqrt{3 - 2 \sqrt{2}} \sqrt{1 - \frac{\tan \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2 \sqrt{2}}} \right. \right. \\
& \left. \left. \sqrt{1 - \frac{(17 - 12 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2 \sqrt{2}}} \left( 1 - \frac{(-3 + 2 \sqrt{2}) \tan \left[ \frac{1}{4} (c + d x) \right]^2}{3 - 2 \sqrt{2}} \right) \right) + \right. \\
& \left. \left. \sqrt{2} \sqrt{\cos [c + d x] \sec \left[ \frac{1}{4} (c + d x) \right]^4} \left( \frac{1}{2} \tan \left[ \frac{1}{4} (c + d x) \right] - \left( -\sec \left[ \frac{1}{4} (c + d x) \right]^2 \tan \left[ \frac{1}{4} (c + d x) \right] + \left( -\sec \left[ \frac{1}{4} (c + d x) \right]^4 \sin [c + d x] + \cos [c + d x] \sec \left[ \frac{1}{4} (c + d x) \right]^4 \tan \left[ \frac{1}{4} (c + d x) \right] \right) \right) \right) \right) \right. \\
& \left. \left( \sqrt{2} \sqrt{\cos [c + d x] \sec \left[ \frac{1}{4} (c + d x) \right]^4} \right) \right) \right) \right) \right)
\end{aligned}$$

Problem 314: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(\cos(c+dx))^7}{(\sin(c+dx))^5} dx$$

Optimal (type 3, 239 leaves, 8 steps):

$$\begin{aligned} & -\frac{4e(\cos(c+dx))^{5/2}}{a(\sin(c+dx))^{3/2}} - \frac{5e^3\sqrt{\cos(c+dx)}\sqrt{a+\sin(c+dx)}}{a^3d} + \\ & \frac{5e^{7/2}\operatorname{ArcSinh}\left[\frac{\sqrt{\cos(c+dx)}}{\sqrt{e}}\right]\sqrt{1+\cos(c+dx)}\sqrt{a+\sin(c+dx)}}{a^3d(1+\cos(c+dx)+\sin(c+dx))} - \\ & \left(\frac{5e^{7/2}\operatorname{ArcTan}\left[\frac{\sqrt{e}\sin(c+dx)}{\sqrt{\cos(c+dx)}\sqrt{1+\cos(c+dx)}}\right]\sqrt{1+\cos(c+dx)}\sqrt{a+\sin(c+dx)}}{(a^3d(1+\cos(c+dx)+\sin(c+dx)))}\right) \end{aligned}$$

Result (type 4, 2779 leaves):

$$\begin{aligned} & \left( (\cos(c+dx))^{7/2} \sec(c+dx)^3 \left( \cos\left(\frac{1}{2}(c+dx)\right) + \sin\left(\frac{1}{2}(c+dx)\right) \right)^5 \right. \\ & \left. - \cos\left(\frac{1}{2}(c+dx)\right) - \sin\left(\frac{1}{2}(c+dx)\right) - \frac{8}{\cos\left(\frac{1}{2}(c+dx)\right) + \sin\left(\frac{1}{2}(c+dx)\right)} \right) \Big/ \\ & \left( d(a(1+\sin(c+dx)))^{5/2} \right) + \left( 5\sqrt{3-2\sqrt{2}}(\cos(c+dx))^{7/2} \sec(c+dx)^3 \right. \\ & \left. \left( \cos\left(\frac{1}{2}(c+dx)\right) + \sin\left(\frac{1}{2}(c+dx)\right) \right)^5 \sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2} \left( 1+\tan\left(\frac{1}{4}(c+dx)\right)^2 \right) \right. \\ & \left. \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \right. \\ & \left. \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2} \right. \\ & \left. \left( 2-2\tan\left(\frac{1}{4}(c+dx)\right)^2+\sqrt{2}\sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} \right) \right. \\ & \left. \left( 4\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left(\frac{1}{4}(c+dx)\right)}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2} \right. \right. \\ & \left. \left. \sqrt{1+\left(-3+2\sqrt{2}\right)\tan\left(\frac{1}{4}(c+dx)\right)^2} \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \right. \right. \end{aligned}$$

$$\begin{aligned}
& 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \\
& \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4} - \sqrt{2} \left( \operatorname{Log}\left[1 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2\right] - \right. \\
& \left. \operatorname{Log}\left[2 - 2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4}\right] \right) \\
& \left. \left( 1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4 \right) \right) / \\
& \left( 2 d \left( \operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \right) (a (1 + \operatorname{Sin}(c + d x)))^{5/2} \right. \\
& \left( -4 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 + 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 + 52 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - \right. \\
& 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - 200 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4 + \\
& 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^4 + 200 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^6 - \\
& 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^6 - 52 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^8 + \\
& 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^8 + 4 \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^{10} - \\
& 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^{10} + 2 \sqrt{2 (3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2}{-3 + 2\sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]^2 - 12 \sqrt{2 (3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2}
\end{aligned}$$

$$\begin{aligned}
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^3}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2(3-2\sqrt{2})}\sec\left(\frac{1}{4}(c+dx)\right)^2}{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}} \\
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^5}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2+}{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}} - \\
& 6\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{\frac{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}} - \\
& 4\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{\frac{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}} - \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{\frac{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}} + \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{\frac{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}} + \\
& 84\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{\frac{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}} - \\
& 56\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{\frac{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}} - \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{\frac{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}} + \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{\frac{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4}} +
\end{aligned}$$

$$\begin{aligned}
& 6 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - \\
& 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\
& 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} \Bigg)
\end{aligned}$$

Problem 315: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(\operatorname{e} \operatorname{Cos}[c + d x])^{5/2}}{(\operatorname{a} + \operatorname{a} \operatorname{Sin}[c + d x])^{5/2}} \operatorname{d}x$$

Optimal (type 3, 218 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{4 e (\cos[c+d x])^{3/2}}{3 a d (\sin[c+d x])^{3/2}} - \frac{2 e^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+d x]}}{\sqrt{e}}\right] \sqrt{1+\cos[c+d x]} \sqrt{a+a \sin[c+d x]}}{d (a^3+a^3 \cos[c+d x]+a^3 \sin[c+d x])} - \\
 & \left( \frac{2 e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+d x]}{\sqrt{e \cos[c+d x]} \sqrt{1+\cos[c+d x]}}\right] \sqrt{1+\cos[c+d x]} \sqrt{a+a \sin[c+d x]}}{(d (a^3+a^3 \cos[c+d x]+a^3 \sin[c+d x]))} \right) /
 \end{aligned}$$

Result (type 4, 2766 leaves):

$$\begin{aligned}
 & \left( (\cos[c+d x])^{5/2} \sec[c+d x]^2 \left( \cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right] \right)^5 \right. \\
 & \left. \left( \frac{8 \sin\left[\frac{1}{2} (c+d x)\right]}{3 (\cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right])^2} - \frac{4}{3 (\cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right])} \right) \right) / \\
 & (d (a (1+\sin[c+d x]))^{5/2}) - \left( \sqrt{3-2 \sqrt{2}} (\cos[c+d x])^{5/2} \sec[c+d x]^2 \right. \\
 & \left. \left( \cos\left[\frac{1}{2} (c+d x)\right] + \sin\left[\frac{1}{2} (c+d x)\right] \right)^4 \sqrt{3-2 \sqrt{2}-\tan\left[\frac{1}{4} (c+d x)\right]^2} \left( 1+\tan\left[\frac{1}{4} (c+d x)\right]^2 \right) \right. \\
 & \left. \sqrt{\frac{-3+2 \sqrt{2}+\tan\left[\frac{1}{4} (c+d x)\right]^2}{-3+2 \sqrt{2}}} \sqrt{\frac{-3+2 \sqrt{2}+17 \tan\left[\frac{1}{4} (c+d x)\right]^2-12 \sqrt{2} \tan\left[\frac{1}{4} (c+d x)\right]^2}{-3+2 \sqrt{2}}} \right. \\
 & \left. \sqrt{1-3 \tan\left[\frac{1}{4} (c+d x)\right]^2+2 \sqrt{2} \tan\left[\frac{1}{4} (c+d x)\right]^2} \right. \\
 & \left. \left( 2-2 \tan\left[\frac{1}{4} (c+d x)\right]^2+\sqrt{2} \sqrt{1-6 \tan\left[\frac{1}{4} (c+d x)\right]^2+\tan\left[\frac{1}{4} (c+d x)\right]^4} \right) \right. \\
 & \left. \left( 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan\left[\frac{1}{4} (c+d x)\right]^2} \right. \right. \\
 & \left. \left. \sqrt{1+\left(-3+2 \sqrt{2}\right) \tan\left[\frac{1}{4} (c+d x)\right]^2} \sqrt{1-6 \tan\left[\frac{1}{4} (c+d x)\right]^2+\tan\left[\frac{1}{4} (c+d x)\right]^4} + \right. \right. \\
 & \left. \left. 8 \operatorname{EllipticPi}\left[-3+2 \sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4} (c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \right. \right. \\
 & \left. \left. \sqrt{3-2 \sqrt{2}-\tan\left[\frac{1}{4} (c+d x)\right]^2} \sqrt{1+\left(-3+2 \sqrt{2}\right) \tan\left[\frac{1}{4} (c+d x)\right]^2} \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - 6 \tan\left(\frac{1}{4} (c + d x)\right)^2 + \tan\left(\frac{1}{4} (c + d x)\right)^4} + \sqrt{2} \left( \log\left[1 + \tan\left(\frac{1}{4} (c + d x)\right)^2\right] - \right. \\
& \left. \log\left[2 - 2 \tan\left(\frac{1}{4} (c + d x)\right)^2 + \sqrt{2} \sqrt{1 - 6 \tan\left(\frac{1}{4} (c + d x)\right)^2 + \tan\left(\frac{1}{4} (c + d x)\right)^4}\right] \right) \\
& \left. \left(1 - 6 \tan\left(\frac{1}{4} (c + d x)\right)^2 + \tan\left(\frac{1}{4} (c + d x)\right)^4\right) \right) / \left( d (a (1 + \sin(c + d x)))^{5/2} \right. \\
& \left. \left(4 \sec\left(\frac{1}{4} (c + d x)\right)^2 - 3 \sqrt{2} \sec\left(\frac{1}{4} (c + d x)\right)^2 - 52 \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^2 + \right. \right. \\
& \left. \left. 39 \sqrt{2} \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^2 + 200 \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^4 - \right. \right. \\
& \left. \left. 150 \sqrt{2} \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^4 - 200 \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^6 + \right. \right. \\
& \left. \left. 150 \sqrt{2} \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^6 + 52 \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^8 - \right. \right. \\
& \left. \left. 39 \sqrt{2} \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^8 - 4 \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^{10} + \right. \right. \\
& \left. \left. 3 \sqrt{2} \sec\left(\frac{1}{4} (c + d x)\right)^2 \tan\left(\frac{1}{4} (c + d x)\right)^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec\left(\frac{1}{4} (c + d x)\right)^2 \right. \right. \\
& \left. \left. \tan\left(\frac{1}{4} (c + d x)\right) \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left(\frac{1}{4} (c + d x)\right)^2}{-3 + 2 \sqrt{2}}} \right. \right. \\
& \left. \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left(\frac{1}{4} (c + d x)\right)^2 - 12 \sqrt{2} \tan\left(\frac{1}{4} (c + d x)\right)^2}{-3 + 2 \sqrt{2}}} \right. \right. \\
& \left. \left. \sqrt{1 - 3 \tan\left(\frac{1}{4} (c + d x)\right)^2 + 2 \sqrt{2} \tan\left(\frac{1}{4} (c + d x)\right)^2} - 12 \sqrt{2 (3 - 2 \sqrt{2})} \sec\left(\frac{1}{4} (c + d x)\right)^2 \right. \right. \\
& \left. \left. \tan\left(\frac{1}{4} (c + d x)\right)^3 \sqrt{3 - 2 \sqrt{2} - \tan\left(\frac{1}{4} (c + d x)\right)^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left(\frac{1}{4} (c + d x)\right)^2}{-3 + 2 \sqrt{2}}} \right. \right. \\
& \left. \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left(\frac{1}{4} (c + d x)\right)^2 - 12 \sqrt{2} \tan\left(\frac{1}{4} (c + d x)\right)^2}{-3 + 2 \sqrt{2}}} \right. \right. \\
& \left. \left. \sqrt{1 - 3 \tan\left(\frac{1}{4} (c + d x)\right)^2 + 2 \sqrt{2} \tan\left(\frac{1}{4} (c + d x)\right)^2} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \sec\left(\frac{1}{4} (c + d x)\right)^2 \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{\tan\left(\frac{1}{4}(c+dx)\right)^5}{\sqrt{3-2\sqrt{2}-\tan\left(\frac{1}{4}(c+dx)\right)^2}} \sqrt{\frac{-3+2\sqrt{2}+\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left(\frac{1}{4}(c+dx)\right)^2-12\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left(\frac{1}{4}(c+dx)\right)^2+2\sqrt{2}\tan\left(\frac{1}{4}(c+dx)\right)^2} - \\
& 6\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 4\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^2 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 84\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 56\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^4 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 48\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 32\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^6 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} - \\
& 6\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^8 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 4\sqrt{2}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)^8 \sqrt{1-6\tan\left(\frac{1}{4}(c+dx)\right)^2+\tan\left(\frac{1}{4}(c+dx)\right)^4} + \\
& 4\sqrt{3-2\sqrt{2}}\sec\left(\frac{1}{4}(c+dx)\right)^2 \tan\left(\frac{1}{4}(c+dx)\right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} - 4 \sqrt{3 - 2 \sqrt{2}} \sec\left[\frac{1}{4} (c + d x)\right]^2 \\
& \tan\left[\frac{1}{4} (c + d x)\right]^3 \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan\left[\frac{1}{4} (c + d x)\right]^2 - 12 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2}{-3 + 2 \sqrt{2}}} \\
& \sqrt{1 - 3 \tan\left[\frac{1}{4} (c + d x)\right]^2 + 2 \sqrt{2} \tan\left[\frac{1}{4} (c + d x)\right]^2} \\
& \sqrt{1 - 6 \tan\left[\frac{1}{4} (c + d x)\right]^2 + \tan\left[\frac{1}{4} (c + d x)\right]^4} \Bigg)
\end{aligned}$$

Problem 327: Attempted integration timed out after 120 seconds.

$$\int (e \cos[c + d x])^p (a + a \sin[c + d x])^8 dx$$

Optimal (type 5, 95 leaves, 2 steps):

$$\begin{aligned}
& -\frac{1}{d e (1+p)} 2^{\frac{17}{2} + \frac{p}{2}} a^8 (\cos[c + d x])^{1+p} \\
& \text{Hypergeometric2F1}\left[\frac{1}{2} (-15 - p), \frac{1 + p}{2}, \frac{3 + p}{2}, \frac{1}{2} (1 - \sin[c + d x])\right] (1 + \sin[c + d x])^{\frac{1}{2} (-1-p)}
\end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 328: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos[c + d x])^p (a + a \sin[c + d x])^3 dx$$

Optimal (type 5, 95 leaves, 2 steps):

$$-\frac{1}{d e (1+p)} 2^{\frac{7+p}{2}} a^3 (e \cos[c + d x])^{1+p} \\ \text{Hypergeometric2F1}\left[\frac{1}{2} (-5-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1-\sin[c + d x])\right] (1+\sin[c + d x])^{\frac{1}{2} (-1-p)}$$

Result (type 5, 462 leaves):

$$\frac{1}{d (\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^6} \pm 2^{-3-p} (e^{-i (c+d x)} + e^{i (c+d x)})^p (1 + e^{2 i (c+d x)})^{-p} \cos[c + d x]^{-p} \\ \left( e \cos[c + d x] \right)^p \left( -\frac{i e^{-3 i (c+d x)} \text{Hypergeometric2F1}\left[-\frac{3}{2} - \frac{p}{2}, -p, -\frac{1}{2} - \frac{p}{2}, -e^{2 i (c+d x)}\right]}{3+p} - \right. \\ \frac{6 e^{-2 i (c+d x)} \text{Hypergeometric2F1}\left[-1 - \frac{p}{2}, -p, -\frac{p}{2}, -e^{2 i (c+d x)}\right]}{2+p} + \\ \frac{15 i e^{-i (c+d x)} \text{Hypergeometric2F1}\left[-\frac{1}{2} - \frac{p}{2}, -p, \frac{1}{2} - \frac{p}{2}, -e^{2 i (c+d x)}\right]}{1+p} - \\ \frac{15 i e^{i (c+d x)} \text{Hypergeometric2F1}\left[\frac{1}{2} - \frac{p}{2}, -p, \frac{3}{2} - \frac{p}{2}, -e^{2 i (c+d x)}\right]}{-1+p} - \\ \frac{6 e^{2 i (c+d x)} \text{Hypergeometric2F1}\left[1 - \frac{p}{2}, -p, 2 - \frac{p}{2}, -e^{2 i (c+d x)}\right]}{-2+p} + \\ \frac{i e^{3 i (c+d x)} \text{Hypergeometric2F1}\left[\frac{3}{2} - \frac{p}{2}, -p, \frac{5}{2} - \frac{p}{2}, -e^{2 i (c+d x)}\right]}{-3+p} + \\ \left. \frac{20 \text{Hypergeometric2F1}\left[-p, -\frac{p}{2}, 1 - \frac{p}{2}, -e^{2 i (c+d x)}\right]}{p} \right) (a + a \sin[c + d x])^3$$

Problem 329: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos[c + d x])^p (a + a \sin[c + d x])^2 dx$$

Optimal (type 5, 95 leaves, 2 steps):

$$-\frac{1}{d e (1+p)} 2^{\frac{5+p}{2}} a^2 (e \cos[c+d x])^{1+p} \\ \text{Hypergeometric2F1}\left[\frac{1}{2} (-3-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1-\sin[c+d x])\right] (1+\sin[c+d x])^{\frac{1}{2} (-1-p)}$$

Result (type 5, 351 leaves):

$$\frac{1}{d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^4} 2^{-2-p} (e^{-\frac{i}{2} (c+d x)} + e^{\frac{i}{2} (c+d x)})^p (1 + e^{2 \frac{i}{2} (c+d x)})^{-p} \cos[c+d x]^{-p} \\ \left( (e \cos[c+d x])^p \left( -\frac{\frac{i}{2} e^{-2 \frac{i}{2} (c+d x)} \text{Hypergeometric2F1}\left[-1-\frac{p}{2}, -p, -\frac{p}{2}, -e^{2 \frac{i}{2} (c+d x)}\right]}{2+p} - \right. \right. \\ \left. \left. \frac{4 e^{-\frac{i}{2} (c+d x)} \text{Hypergeometric2F1}\left[-\frac{1}{2}-\frac{p}{2}, -p, \frac{1}{2}-\frac{p}{2}, -e^{2 \frac{i}{2} (c+d x)}\right]}{1+p} + \right. \right. \\ \left. \left. \frac{4 e^{\frac{i}{2} (c+d x)} \text{Hypergeometric2F1}\left[\frac{1}{2}-\frac{p}{2}, -p, \frac{3}{2}-\frac{p}{2}, -e^{2 \frac{i}{2} (c+d x)}\right]}{-1+p} - \right. \right. \\ \left. \left. \frac{i e^{2 \frac{i}{2} (c+d x)} \text{Hypergeometric2F1}\left[1-\frac{p}{2}, -p, 2-\frac{p}{2}, -e^{2 \frac{i}{2} (c+d x)}\right]}{-2+p} + \right. \right. \\ \left. \left. \frac{6 i \text{Hypergeometric2F1}\left[-p, -\frac{p}{2}, 1-\frac{p}{2}, -e^{2 \frac{i}{2} (c+d x)}\right]}{p} \right) (a + a \sin[c+d x])^2 \right)$$

Problem 330: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos[c+d x])^p (a + a \sin[c+d x]) \, dx$$

Optimal (type 5, 93 leaves, 2 steps):

$$-\frac{1}{d e (1+p)} 2^{\frac{3+p}{2}} a (e \cos[c+d x])^{1+p} \\ \text{Hypergeometric2F1}\left[\frac{1}{2} (-1-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1-\sin[c+d x])\right] (1+\sin[c+d x])^{\frac{1}{2} (-1-p)}$$

Result (type 5, 266 leaves):

$$\frac{1}{d (-1+p) p (1+p) (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^2} \\ 2^{-1-p} a (1 + e^{2 \frac{i}{2} (c+d x)})^{-1-p} (e^{-\frac{i}{2} (c+d x)} (1 + e^{2 \frac{i}{2} (c+d x)})^{1+p} \cos[c+d x]^{-p} (e \cos[c+d x])^p \\ \left( -(-1+p) p \text{Hypergeometric2F1}\left[\frac{1}{2} (-1-p), -p, \frac{1-p}{2}, -e^{2 \frac{i}{2} (c+d x)}\right] + \right. \\ \left. e^{\frac{i}{2} (c+d x)} (1+p) \left( e^{\frac{i}{2} (c+d x)} p \text{Hypergeometric2F1}\left[\frac{1-p}{2}, -p, \frac{3-p}{2}, -e^{2 \frac{i}{2} (c+d x)}\right] + \right. \right. \\ \left. \left. 2 \frac{i}{2} (-1+p) \text{Hypergeometric2F1}\left[-p, -\frac{p}{2}, 1-\frac{p}{2}, -e^{2 \frac{i}{2} (c+d x)}\right] \right) \right) (1+\sin[c+d x])$$

### Problem 331: Unable to integrate problem.

$$\int \frac{(\mathbf{e} \cos[c + d x])^p}{a + a \sin[c + d x]} dx$$

Optimal (type 5, 95 leaves, 2 steps):

$$-\frac{1}{a d e (1+p)} 2^{\frac{1}{2}+\frac{p}{2}} (\mathbf{e} \cos[c + d x])^{1+p}$$

$$\text{Hypergeometric2F1}\left[\frac{3-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1-\sin[c + d x])\right] (1+\sin[c + d x])^{\frac{1}{2}(-1-p)}$$

Result (type 8, 25 leaves):

$$\int \frac{(\mathbf{e} \cos[c + d x])^p}{(a + a \sin[c + d x])^2} dx$$

### Problem 332: Unable to integrate problem.

$$\int \frac{(\mathbf{e} \cos[c + d x])^p}{(a + a \sin[c + d x])^2} dx$$

Optimal (type 5, 93 leaves, 2 steps):

$$-\frac{1}{a^2 d e (1+p)} 2^{\frac{1}{2}(-3+p)} (\mathbf{e} \cos[c + d x])^{1+p}$$

$$\text{Hypergeometric2F1}\left[\frac{5-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1-\sin[c + d x])\right] (1+\sin[c + d x])^{\frac{1}{2}(-1-p)}$$

Result (type 8, 25 leaves):

$$\int \frac{(\mathbf{e} \cos[c + d x])^p}{(a + a \sin[c + d x])^2} dx$$

### Problem 333: Unable to integrate problem.

$$\int \frac{(\mathbf{e} \cos[c + d x])^p}{(a + a \sin[c + d x])^3} dx$$

Optimal (type 5, 93 leaves, 2 steps):

$$-\frac{1}{a^3 d e (1+p)} 2^{\frac{1}{2}(-5+p)} (\mathbf{e} \cos[c + d x])^{1+p}$$

$$\text{Hypergeometric2F1}\left[\frac{7-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1-\sin[c + d x])\right] (1+\sin[c + d x])^{\frac{1}{2}(-1-p)}$$

Result (type 8, 25 leaves):

$$\int \frac{(\mathbf{e} \cos[c + d x])^p}{(a + a \sin[c + d x])^3} dx$$

### Problem 334: Unable to integrate problem.

$$\int \frac{(\mathbf{e} \cos[c + d x])^p}{(\mathbf{a} + \mathbf{a} \sin[c + d x])^8} dx$$

Optimal (type 5, 93 leaves, 2 steps):

$$-\frac{1}{a^8 d e (1+p)} 2^{\frac{1}{2} (-15+p)} (\mathbf{e} \cos[c + d x])^{1+p}$$

$$\text{Hypergeometric2F1}\left[\frac{17-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin[c + d x])\right] (1 + \sin[c + d x])^{\frac{1}{2} (-1-p)}$$

Result (type 8, 25 leaves):

$$\int \frac{(\mathbf{e} \cos[c + d x])^p}{(\mathbf{a} + \mathbf{a} \sin[c + d x])^8} dx$$

### Problem 335: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (\mathbf{e} \cos[c + d x])^p (\mathbf{a} + \mathbf{a} \sin[c + d x])^{7/2} dx$$

Optimal (type 5, 103 leaves, 3 steps):

$$-\left( \left( 2^{4+\frac{p}{2}} a^4 (\mathbf{e} \cos[c + d x])^{1+p} \text{Hypergeometric2F1}\left[\frac{1}{2} (-6-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin[c + d x])\right] \right. \right.$$

$$\left. \left. (1 + \sin[c + d x])^{-p/2} \right) \right/ \left( d e (1+p) \sqrt{a + a \sin[c + d x]} \right)$$

Result (type 5, 629 leaves):

$$\begin{aligned}
& \frac{1}{d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^7} \\
& \left( 1 + \frac{1}{2} \right) 2^{-3-p} e^{i p (c+d x)} \left( e^{-i (c+d x)} + e^{i (c+d x)} \right)^p \left( 1 + e^{2 i (c+d x)} \right)^{-p} \cos [c + d x]^{-p} \left( e \cos [c + d x] \right)^p \\
& \left( \frac{1}{7+2p} e^{-\frac{1}{2} i (7+2p) (c+d x)} \text{Hypergeometric2F1} \left[ -\frac{7}{4} - \frac{p}{2}, -p, -\frac{3}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \right. \\
& \frac{1}{5+2p} 7 i e^{-\frac{1}{2} i (5+2p) (c+d x)} \text{Hypergeometric2F1} \left[ -\frac{5}{4} - \frac{p}{2}, -p, -\frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\
& \frac{1}{3+2p} 21 e^{-\frac{1}{2} i (3+2p) (c+d x)} \text{Hypergeometric2F1} \left[ -\frac{3}{4} - \frac{p}{2}, -p, \frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\
& \frac{1}{1+2p} 35 i e^{-\frac{1}{2} i (1+2p) (c+d x)} \text{Hypergeometric2F1} \left[ -\frac{1}{4} - \frac{p}{2}, -p, \frac{3}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\
& \frac{1}{-1+2p} 35 e^{-\frac{1}{2} i (-1+2p) (c+d x)} \text{Hypergeometric2F1} \left[ \frac{1}{4} - \frac{p}{2}, -p, \frac{5}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\
& \frac{1}{-3+2p} 21 i e^{\frac{1}{2} i (3-2p) (c+d x)} \text{Hypergeometric2F1} \left[ \frac{3}{4} - \frac{p}{2}, -p, \frac{7}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\
& \frac{1}{-5+2p} 7 e^{\frac{1}{2} i (5-2p) (c+d x)} \text{Hypergeometric2F1} \left[ \frac{5}{4} - \frac{p}{2}, -p, \frac{9}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\
& \left. \frac{1}{-7+2p} i e^{-\frac{1}{2} i (-7+2p) (c+d x)} \text{Hypergeometric2F1} \left[ \frac{7}{4} - \frac{p}{2}, -p, \frac{11}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] \right) \\
& (a (1 + \sin [c + d x]))^{7/2}
\end{aligned}$$

Problem 336: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + a \sin [c + d x])^{5/2} dx$$

Optimal (type 5, 103 leaves, 3 steps):

$$\begin{aligned}
& - \left( \left( 2^{3+\frac{p}{2}} a^3 (e \cos [c + d x])^{1+p} \text{Hypergeometric2F1} \left[ \frac{1}{2} (-4 - p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [c + d x]) \right] \right. \right. \\
& \left. \left. (1 + \sin [c + d x])^{-p/2} \right) \right) \left/ \left( d e (1 + p) \sqrt{a + a \sin [c + d x]} \right) \right.
\end{aligned}$$

Result (type 5, 504 leaves):

$$\begin{aligned}
 & -\frac{1}{d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^5} \\
 & \left( 1 - \frac{1}{2} \right) 2^{-3-p} e^{i p (c+d x)} \left( e^{-i (c+d x)} + e^{i (c+d x)} \right)^p \left( 1 + e^{2 i (c+d x)} \right)^{-p} \cos [c + d x]^{-p} (e \cos [c + d x])^p \\
 & \left( -\frac{1}{5+2p} 2 e^{-\frac{1}{2} i (5+2p) (c+d x)} \text{Hypergeometric2F1} \left[ -\frac{5}{4} - \frac{p}{2}, -p, -\frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \right. \\
 & \frac{1}{3+2p} 10 i e^{-\frac{1}{2} i (3+2p) (c+d x)} \text{Hypergeometric2F1} \left[ -\frac{3}{4} - \frac{p}{2}, -p, \frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\
 & \frac{1}{1+2p} 20 e^{-\frac{1}{2} i (1+2p) (c+d x)} \text{Hypergeometric2F1} \left[ -\frac{1}{4} - \frac{p}{2}, -p, \frac{3}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\
 & \frac{1}{-1+2p} 20 i e^{\frac{1}{2} i (1-2p) (c+d x)} \text{Hypergeometric2F1} \left[ \frac{1}{4} - \frac{p}{2}, -p, \frac{5}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\
 & \frac{1}{-3+2p} 10 e^{\frac{1}{2} i (3-2p) (c+d x)} \text{Hypergeometric2F1} \left[ \frac{3}{4} - \frac{p}{2}, -p, \frac{7}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\
 & \left. -\frac{1}{-5+2p} 2 i e^{-\frac{1}{2} i (-5+2p) (c+d x)} \text{Hypergeometric2F1} \left[ \frac{5}{4} - \frac{p}{2}, -p, \frac{9}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] \right) \\
 & (a (1 + \sin [c + d x]))^{5/2}
 \end{aligned}$$

**Problem 337:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + a \sin [c + d x])^{3/2} \, dx$$

Optimal (type 5, 103 leaves, 3 steps) :

$$\begin{aligned}
 & - \left( \left( 2^{2+\frac{p}{2}} a^2 (e \cos [c + d x])^{1+p} \text{Hypergeometric2F1} \left[ \frac{1}{2} (-2-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [c + d x]) \right] \right. \right. \\
 & \left. \left. (1 + \sin [c + d x])^{-p/2} \right) \Big/ \left( d e (1+p) \sqrt{a + a \sin [c + d x]} \right) \right)
 \end{aligned}$$

Result (type 5, 378 leaves) :

$$\begin{aligned}
 & -\frac{1}{d \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} \\
 & \left( 1 + \frac{1}{2} \right) 2^{-2-p} e^{i p (c+d x)} \left( e^{-i (c+d x)} + e^{i (c+d x)} \right)^p \left( 1 + e^{2 i (c+d x)} \right)^{-p} \cos [c + d x]^{-p} (e \cos [c + d x])^p \\
 & \left( \frac{1}{3+2p} 2 e^{-\frac{1}{2} i (3+2p) (c+d x)} \text{Hypergeometric2F1} \left[ -\frac{3}{4} - \frac{p}{2}, -p, \frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \right. \\
 & \frac{1}{1+2p} 6 i e^{-\frac{1}{2} i (1+2p) (c+d x)} \text{Hypergeometric2F1} \left[ -\frac{1}{4} - \frac{p}{2}, -p, \frac{3}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\
 & \frac{1}{-1+2p} 6 e^{\frac{1}{2} i (1-2p) (c+d x)} \text{Hypergeometric2F1} \left[ \frac{1}{4} - \frac{p}{2}, -p, \frac{5}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\
 & \left. \frac{1}{-3+2p} 2 i e^{-\frac{1}{2} i (-3+2p) (c+d x)} \text{Hypergeometric2F1} \left[ \frac{3}{4} - \frac{p}{2}, -p, \frac{7}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] \right) \\
 & (a (1 + \sin [c + d x]))^{3/2}
 \end{aligned}$$

**Problem 338:** Result unnecessarily involves complex numbers and more than

twice size of optimal antiderivative.

$$\int (e \cos[c + dx])^p \sqrt{a + a \sin[c + dx]} \, dx$$

Optimal (type 5, 97 leaves, 3 steps):

$$-\left( \left( 2^{1+\frac{p}{2}} a (e \cos[c + dx])^{1+p} \text{Hypergeometric2F1}\left[-\frac{p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin[c + dx])\right] (1 + \sin[c + dx])^{-p/2} \right) \right) \Big/ \left( d e (1 + p) \sqrt{a + a \sin[c + dx]} \right)$$

Result (type 5, 310 leaves):

$$\frac{1}{d (-1 + 2 p) (1 + 2 p) \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right) (1 + \frac{i}{2}) 2^{-p} e^{-\frac{1}{2} \frac{i}{2} d x} \cos[c + dx]^{-p} (e \cos[c + dx])^p \left( e^{\frac{i}{2} d x} (1 + 2 p) \text{Hypergeometric2F1}\left[\frac{1}{4} (1 - 2 p), -p, \frac{1}{4} (5 - 2 p), -e^{2 \frac{i}{2} d x} (\cos[c] + \frac{i}{2} \sin[c])^2\right] \left( \cos\left[\frac{c}{2}\right] + \frac{i}{2} \sin\left[\frac{c}{2}\right] \right) + (-1 + 2 p) \text{Hypergeometric2F1}\left[\frac{1}{4} (-1 - 2 p), -p, \frac{1}{4} (3 - 2 p), -e^{2 \frac{i}{2} d x} (\cos[c] + \frac{i}{2} \sin[c])^2\right] \left( \frac{i}{2} \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right) \left( e^{-\frac{i}{2} d x} ((1 + e^{2 \frac{i}{2} d x}) \cos[c] + \frac{i}{2} (-1 + e^{2 \frac{i}{2} d x}) \sin[c])^p \right) (1 + e^{2 \frac{i}{2} d x} \cos[2c] + \frac{i}{2} e^{2 \frac{i}{2} d x} \sin[2c])^{-p} \sqrt{a (1 + \sin[c + dx])}}$$

Problem 340: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + dx])^p}{(a + a \sin[c + dx])^{3/2}} \, dx$$

Optimal (type 5, 102 leaves, 3 steps):

$$-\left( \left( 2^{-1+\frac{p}{2}} (e \cos[c + dx])^{1+p} \text{Hypergeometric2F1}\left[\frac{4-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin[c + dx])\right] (1 + \sin[c + dx])^{1-\frac{p}{2}} \right) \right) \Big/ \left( d e (1 + p) (a + a \sin[c + dx])^{3/2} \right)$$

Result (type 5, 228 leaves):

$$\frac{1}{a d p (-4 + p^2) \sqrt{2 - 2 \sin[c + d x]} (a (1 + \sin[c + d x]))^{3/2}}$$

$$2^{-1+\frac{p}{2}} \cos[c + d x] (e \cos[c + d x])^p (1 - \sin[c + d x])^{-p/2}$$

$$\left( 4 a p (2 + p) \text{Hypergeometric2F1}\left[\frac{1}{2} (-1 - p), \frac{1}{2} (-2 + p), \frac{p}{2}, \frac{1}{2} (1 + \sin[c + d x]) \right] + \right.$$

$$( -2 + p) (1 + \sin[c + d x])$$

$$\left( 2 a (2 + p) \text{Hypergeometric2F1}\left[\frac{1}{2} (-1 - p), \frac{p}{2}, \frac{2 + p}{2}, \frac{1}{2} (1 + \sin[c + d x]) \right] + \right.$$

$$\left. a p \text{Hypergeometric2F1}\left[\frac{1 - p}{2}, \frac{2 + p}{2}, \frac{4 + p}{2}, \frac{1}{2} (1 + \sin[c + d x]) \right] (1 + \sin[c + d x]) \right)$$

Problem 341: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^p}{(a + a \sin[c + d x])^{5/2}} \, dx$$

Optimal (type 5, 105 leaves, 3 steps):

$$- \left( \left( 2^{-2+\frac{p}{2}} (e \cos[c + d x])^{1+p} \text{Hypergeometric2F1}\left[\frac{6 - p}{2}, \frac{1 + p}{2}, \frac{3 + p}{2}, \frac{1}{2} (1 - \sin[c + d x]) \right] \right. \right.$$

$$\left. \left. (1 + \sin[c + d x])^{1-\frac{p}{2}} \right) \right/ \left( a d e (1 + p) (a + a \sin[c + d x])^{3/2} \right)$$

Result (type 5, 304 leaves):

$$\frac{1}{a^4 d (-4 + p) (-2 + p) p (2 + p) \sqrt{2 - 2 \sin[c + d x]} (1 + \sin[c + d x])^3}$$

$$2^{-2+\frac{p}{2}} \cos[c + d x] (e \cos[c + d x])^p (1 - \sin[c + d x])^{-p/2} \sqrt{a (1 + \sin[c + d x])}$$

$$\left( 8 a p (-4 + p^2) \text{Hypergeometric2F1}\left[\frac{1}{2} (-1 - p), \frac{1}{2} (-4 + p), \frac{1}{2} (-2 + p), \frac{1}{2} (1 + \sin[c + d x]) \right] + \right.$$

$$( -4 + p) (1 + \sin[c + d x]) \left( 4 a p (2 + p) \text{Hypergeometric2F1}\left[\frac{1}{2} (-1 - p), \right. \right.$$

$$\left. \left. \frac{1}{2} (-2 + p), \frac{p}{2}, \frac{1}{2} (1 + \sin[c + d x]) \right] + (-2 + p) (1 + \sin[c + d x]) \right)$$

$$\left( 2 a (2 + p) \text{Hypergeometric2F1}\left[\frac{1}{2} (-1 - p), \frac{p}{2}, \frac{2 + p}{2}, \frac{1}{2} (1 + \sin[c + d x]) \right] + \right.$$

$$\left. a p \text{Hypergeometric2F1}\left[\frac{1 - p}{2}, \frac{2 + p}{2}, \frac{4 + p}{2}, \frac{1}{2} (1 + \sin[c + d x]) \right] (1 + \sin[c + d x]) \right)$$

Problem 343: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^7 (a + a \sin[c + d x])^m \, dx$$

Optimal (type 3, 109 leaves, 3 steps):

$$\frac{8 (a + a \sin[c + d x])^{4+m}}{a^4 d (4+m)} - \frac{12 (a + a \sin[c + d x])^{5+m}}{a^5 d (5+m)} +$$

$$\frac{6 (a + a \sin[c + d x])^{6+m}}{a^6 d (6+m)} - \frac{(a + a \sin[c + d x])^{7+m}}{a^7 d (7+m)}$$

Result (type 3, 796 leaves):

$$\frac{1}{d} (a (1 + \sin[c + d x]))^m \left( \frac{6144 + 1084 m + 117 m^2 + 5 m^3}{16 (4+m) (5+m) (6+m) (7+m)} + \right.$$

$$\left( (29400 + 2578 m + 171 m^2 + 5 m^3) \left( -\frac{1}{128} \operatorname{Cos}[c + d x] + \frac{1}{128} \operatorname{Sin}[c + d x] \right) \right) /$$

$$((4+m) (5+m) (6+m) (7+m)) +$$

$$\left( (29400 + 2578 m + 171 m^2 + 5 m^3) \left( \frac{1}{128} \operatorname{Cos}[c + d x] + \frac{1}{128} \operatorname{Sin}[c + d x] \right) \right) /$$

$$((4+m) (5+m) (6+m) (7+m)) +$$

$$\left( (804 m + 109 m^2 + 5 m^3) \left( \frac{3}{64} \operatorname{Cos}[2 (c + d x)] - \frac{3}{64} \operatorname{Sin}[2 (c + d x)] \right) \right) /$$

$$((4+m) (5+m) (6+m) (7+m)) +$$

$$\left( (804 m + 109 m^2 + 5 m^3) \left( \frac{3}{64} \operatorname{Cos}[2 (c + d x)] + \frac{3}{64} \operatorname{Sin}[2 (c + d x)] \right) \right) /$$

$$((4+m) (5+m) (6+m) (7+m)) +$$

$$\left( (1960 + 1070 m + 93 m^2 + 3 m^3) \left( -\frac{3}{128} \operatorname{Cos}[3 (c + d x)] + \frac{3}{128} \operatorname{Sin}[3 (c + d x)] \right) \right) /$$

$$((4+m) (5+m) (6+m) (7+m)) +$$

$$\left( (1960 + 1070 m + 93 m^2 + 3 m^3) \left( \frac{3}{128} \operatorname{Cos}[3 (c + d x)] + \frac{3}{128} \operatorname{Sin}[3 (c + d x)] \right) \right) /$$

$$((4+m) (5+m) (6+m) (7+m)) +$$

$$\frac{(44 m + 17 m^2 + m^3) \left( \frac{3}{32} \operatorname{Cos}[4 (c + d x)] - \frac{3}{32} \operatorname{Sin}[4 (c + d x)] \right)}{(4+m) (5+m) (6+m) (7+m)} +$$

$$\frac{(44 m + 17 m^2 + m^3) \left( \frac{3}{32} \operatorname{Cos}[4 (c + d x)] + \frac{3}{32} \operatorname{Sin}[4 (c + d x)] \right)}{(4+m) (5+m) (6+m) (7+m)} +$$

$$\left( (294 + 103 m + 5 m^2) \left( -\frac{1}{128} \operatorname{Cos}[5 (c + d x)] + \frac{1}{128} \operatorname{Sin}[5 (c + d x)] \right) \right) /$$

$$((5+m) (6+m) (7+m)) + \frac{(294 + 103 m + 5 m^2) \left( \frac{1}{128} \operatorname{Cos}[5 (c + d x)] + \frac{1}{128} \operatorname{Sin}[5 (c + d x)] \right)}{(5+m) (6+m) (7+m)} +$$

$$\frac{\frac{1}{64} m \operatorname{Cos}[6 (c + d x)] - \frac{1}{64} m \operatorname{Sin}[6 (c + d x)]}{(6+m) (7+m)} + \frac{\frac{1}{64} m \operatorname{Cos}[6 (c + d x)] + \frac{1}{64} m \operatorname{Sin}[6 (c + d x)]}{(6+m) (7+m)} +$$

$$\left. \frac{-\frac{1}{128} \operatorname{Cos}[7 (c + d x)] + \frac{1}{128} \operatorname{Sin}[7 (c + d x)]}{7+m} + \frac{\frac{1}{128} \operatorname{Cos}[7 (c + d x)] + \frac{1}{128} \operatorname{Sin}[7 (c + d x)]}{7+m} \right)$$

Problem 347: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sec [c + dx] \left( a + a \sin [c + dx] \right)^m dx$$

Optimal (type 5, 40 leaves, 2 steps):

$$\frac{1}{2 d m} \text{Hypergeometric2F1}[1, m, 1+m, \frac{1}{2} (1 + \text{Sin}[c + d x])] (a + a \text{Sin}[c + d x])^m$$

### Result (type 6, 7227 leaves):

$$\left( d \left( \cos \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] - \sin \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] \right) \right)$$

$$\begin{aligned}
& \left( \cos \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + d x \right) \right] + \right. \\
& \left. \sin \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + d x \right) \right] \right) \\
& \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) \left( \frac{1}{2 \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^2} \right. \\
& \csc \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] \left( \frac{1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2} \right)^{2m} \\
& \left( - \left( \left( 2 \operatorname{AppellF1} \left[ 1, 1 - 2m, 2m, 2, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \right. \right. \\
& \left. \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^4 \right) \right/ \left( -2 \operatorname{AppellF1} \left[ 1, 1 - 2m, 2m, 2, \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + \left( 2m \operatorname{AppellF1} \left[ 2, \right. \right. \\
& \left. \left. 1 - 2m, 1 + 2m, 3, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + \right. \\
& \left. \left( -1 + 2m \right) \operatorname{AppellF1} \left[ 2, 2 - 2m, 2m, 3, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) + \\
& \left( \left( 1 + m \right) \operatorname{AppellF1} \left[ 1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \\
& \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \left( -1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^2 \right) \right/ \\
& \left( \left( 1 + 2m \right) \left( -2 \left( 1 + m \right) \operatorname{AppellF1} \left[ 1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \\
& \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + \left( \operatorname{AppellF1} \left[ 2 + 2m, 2m, 2, 3 + 2m, \right. \right. \right. \\
& \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + \left( \operatorname{AppellF1} \left[ 2 + 2m, 2m, 2, 3 + 2m, \right. \right. \right. \\
& \left. \left. \frac{1}{2} - \frac{1}{2} \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + \right. \\
& \left. m \operatorname{AppellF1} \left[ 2 + 2m, 1 + 2m, 1, 3 + 2m, \frac{1}{2} - \frac{1}{2} \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \\
& \left. \left. 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \left( -1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) \right) \right) - \\
& \frac{1}{2 \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)} \cot \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] \csc \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \\
& \left( \frac{1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2} \right)^{2m} \\
& \left( - \left( \left( 2 \operatorname{AppellF1} \left[ 1, 1 - 2m, 2m, 2, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \right. \right. \\
& \left. \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^4 \right) \right) \right/ \left( -2 \operatorname{AppellF1} \left[ 1, 1 - 2m, 2m, 2, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \right)
\end{aligned}$$



$$\begin{aligned}
& \left( (1+m) \operatorname{AppellF1}[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]]^2, \right. \\
& \quad \left. 1 - \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) \left( -1 + \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right)^2 \Big/ \\
& \left( (1+2m) \left( -2 (1+m) \operatorname{AppellF1}[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]]^2, \right. \right. \\
& \quad \left. \left. 1 - \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) + \left( \operatorname{AppellF1}[2+2m, 2m, 2, 3+2m, \right. \right. \\
& \quad \left. \left. \frac{1}{2} - \frac{1}{2} \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]]^2, 1 - \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) + \right. \\
& \quad \left. m \operatorname{AppellF1}[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]]^2, \right. \\
& \quad \left. \left. 1 - \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) \left( -1 + \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) \right) \Big) + \\
& \frac{1}{1 - \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2} \cot[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \left( \frac{1 - \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]]^2}{1 + \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2} \right)^{2m} \\
& \left( - \left( \left( 2 \operatorname{AppellF1}[1, 1-2m, 2m, 2, \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2, -\tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2] \right. \right. \right. \\
& \quad \left. \left. \left. \sec[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^3 \right) \Big/ \left( -2 \operatorname{AppellF1}[1, 1-2m, 2m, \right. \right. \\
& \quad \left. \left. 2, \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2, -\tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) + \left( 2m \operatorname{AppellF1}[2, \right. \right. \\
& \quad \left. \left. 1-2m, 1+2m, 3, \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2, -\tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) + \right. \\
& \quad \left. \left. (-1+2m) \operatorname{AppellF1}[2, 2-2m, 2m, 3, \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2, \right. \right. \\
& \quad \left. \left. -\tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) \Big) - \\
& \left( 2 \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^4 \left( -\frac{1}{2} m \operatorname{AppellF1}[2, 1-2m, 1+2m, 3, \right. \right. \\
& \quad \left. \left. \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2, -\tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) \right. \\
& \quad \left. \left. \sec[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)] + \frac{1}{4} (1-2m) \right. \\
& \quad \left. \left. \operatorname{AppellF1}[2, 2-2m, 2m, 3, \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2, -\tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2] \right) \right. \\
& \quad \left. \left. \sec[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)] \right) \right) \Big/ \\
& \left( -2 \operatorname{AppellF1}[1, 1-2m, 2m, 2, \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2, -\tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2] \right. \\
& \quad \left. \left. + \left( 2m \operatorname{AppellF1}[2, 1-2m, 1+2m, 3, \tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan[\frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]^2 \right) + (-1+2m) \operatorname{AppellF1}[2, 2-2m, 2m, 3, \tan[\right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)]]^2 \right) \right) \right)
\end{aligned}$$







$$\begin{aligned}
& \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, 1 - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2] + \\
& m \text{AppellF1}\left[2 + 2m, 1 + 2m, 1, 3 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], \\
& 1 - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2] \left(-1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2 \Big) \Big) \Big) \Big)
\end{aligned}$$

**Problem 348:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^3 (a + a \sin[c + dx])^m dx$$

Optimal (type 5, 47 leaves, 2 steps):

$$-\frac{1}{4d(1-m)} a \text{Hypergeometric2F1}\left[2, -1+m, m, \frac{1}{2} (1 + \sin[c + dx])\right] (a + a \sin[c + dx])^{-1+m}$$

Result (type 6, 27 160 leaves): Display of huge result suppressed!

**Problem 349:** Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^5 (a + a \sin[c + dx])^m dx$$

Optimal (type 5, 51 leaves, 2 steps):

$$-\frac{1}{8d(2-m)} a^2 \text{Hypergeometric2F1}\left[3, -2+m, -1+m, \frac{1}{2} (1 + \sin[c + dx])\right] (a + a \sin[c + dx])^{-2+m}$$

Result (type 5, 443 leaves):

$$\begin{aligned}
& -\frac{1}{32 d} \left( \operatorname{Sec} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^m \left( a + a \operatorname{Sin} [c + d x] \right)^m \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{-m} \\
& \left( -\frac{1}{m} 6 \left( 1 + \operatorname{Cot} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^m \operatorname{Hypergeometric2F1} [m, m, 1+m, -\operatorname{Cot} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2] - \right. \\
& \left. \frac{1}{1+m} 4 \operatorname{Cot} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \left( 1 + \operatorname{Cot} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^m \right. \\
& \left. \operatorname{Hypergeometric2F1} [m, 1+m, 2+m, -\operatorname{Cot} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2] - \frac{1}{2+m} \operatorname{Cot} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^4 \right. \\
& \left. \left( 1 + \operatorname{Cot} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^m \operatorname{Hypergeometric2F1} [m, 2+m, 3+m, -\operatorname{Cot} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2] + \right. \\
& \left. \frac{4}{-1 + m} \left( -1 - \operatorname{Tan} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 + \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^m \right) \right. \\
& \left. \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^4 + \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^m \right) - \right. \\
& \left. m \left( \operatorname{Tan} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 + \operatorname{Tan} \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - d x \right) \right]^4 \right) \right) \Big/ \left( (-2+m) (-1+m) \right) \right)
\end{aligned}$$

Problem 350: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^4 \left( a + a \sin [c + d x] \right)^m dx$$

Optimal (type 5, 83 leaves, 3 steps):

$$-\frac{1}{5 d} 2^{\frac{5+m}{2}} a^2 \cos[c+d x]^5 \text{Hypergeometric2F1}\left[\frac{5}{2}, -\frac{3}{2}-m, \frac{7}{2}, \frac{1}{2} (1-\sin[c+d x])\right] \\ (1+\sin[c+d x])^{-\frac{1}{2}-m} (a+a \sin[c+d x])^{-2+m}$$

Result (type 6, 9362 leaves):

$$\begin{aligned}
& - \left( \left( 3072 \cos[c + d x]^4 (a + a \sin[c + d x])^m \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right] \right. \right. \\
& \left. \left. \left( 1 - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right)^{2(2+m)} \left( \frac{1}{1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2} \right)^{9+2m} \right. \\
& \left. \left( \left( \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \right. \right. \\
& \left. \left. \left( 1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right)^2 \right) \right/ \left( 3 \text{AppellF1}\left[\frac{1}{2}, -2(2+m), \right. \right. \\
& \left. \left. 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] - \right. \\
& \left. \left. 2 \left( 2(2+m) \text{AppellF1}\left[\frac{3}{2}, -3-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left( 1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right)^2 \right) \right) \right)
\end{aligned}$$



$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(4+m), \frac{5}{2}, \right. \\
& \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \\
& \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \\
& \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] / \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+ \right. \right. \\
& \left. \left. 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] - \right. \\
& \left. 2\left(2(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(5+m), \frac{5}{2}, \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) + \right. \\
& \left. \left(2 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \right) / \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] + \right. \\
& \left. 4\left((2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \right. \\
& \left. \left. \left. \frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) - \right. \\
& \left. 3072(2+m) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \right. \\
& \left. \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)^{-1+2(2+m)} \right. \\
& \left. \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2}\right)^{9+2m} \right. \\
& \left. \left(\left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \right. \right. \right. \\
& \left. \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)^2\right) / \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+ \right. \right. \right. \right. \\
& \left. \left. \left. \left. 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] - \right. \right. \right. \right. \\
& \left. \left. \left. \left. 2\left(2(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] + (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(4+m), \frac{5}{2}, \right. \right. \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]\right)\right)\right)\right)
\end{aligned}$$



$$\begin{aligned}
& \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
& \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] / \left(3\text{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+ \right. \right. \\
& \left. \left. 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \left. 2\left(2(2+m)\text{AppellF1}\left[\frac{3}{2}, -3-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (9+2m)\text{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(5+m), \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \left(2\text{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)\right) / \\
& \left(-3\text{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 4\left((2+m)\text{AppellF1}\left[\frac{3}{2}, -3-2m, \right. \right. \right. \\
& \left. \left. \left. 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \left. (4+m)\text{AppellF1}\left[\frac{3}{2}, -2(2+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \\
& 3072 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{2(2+m)} \\
& \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}\right)^{9+2m} \\
& \left(\left(\text{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \\
& \left. \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)\right)\right) / \\
& \left(3\text{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \left. 2\left(2(2+m)\text{AppellF1}\left[\frac{3}{2}, -3-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (7+2m)\text{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(4+m), \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) +
\end{aligned}$$



$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 9+2m, \frac{5}{2}, \right. \\
& \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \\
& \left(2\left(-\frac{1}{3}(4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 1+2(4+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]\right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] - \frac{1}{3} \right. \\
& \left. (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(2+m), 2(4+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \\
& \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \Big/ \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 2\right. \right. \\
& \left. \left. (4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \right. \\
& \left. 4\left((2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 9+2m, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2\right) - \\
& \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \\
& \left. \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)^2 \left(-\left(2(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, 7+2m, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) + \right. \\
& \left. (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(4+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, \right. \\
& \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \\
& 3\left(-\frac{1}{6}(7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, \right. \\
& \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] - \\
& \frac{1}{3}(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(2+m), 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, \\
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] - 2 \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \left(2(2+m) \left(-\frac{3}{10}(7+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -3-2m, \right. \right. \right. \\
& \left. \left. \left. 8+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \right. \\
& \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \frac{3}{10}(-3-2m)\right)
\end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{5}{2}, -2 - 2m, 7 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\right.\right. \\
& \left.\left. -\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 + \\
& (7 + 2m) \left(-\frac{3}{5}(4 + m) \text{AppellF1}\left[\frac{5}{2}, -2(2 + m), 1 + 2(4 + m), \frac{7}{2}, \tan\left[\frac{1}{4}\right.\right.\right. \\
& \left.\left.\left. -\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
& \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{3}{5}(2 + m) \text{AppellF1}\left[\frac{5}{2}, 1 - 2(2 + m), \right. \right. \\
& \left. \left. 2(4 + m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right) \Big) \\
& \Big( 3 \text{AppellF1}\left[\frac{1}{2}, -2(2 + m), 7 + 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
& \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2 \left( 2(2 + m) \text{AppellF1}\left[\frac{3}{2}, -3 - 2m, \right. \right. \\
& \left. \left. 7 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \left. (7 + 2m) \text{AppellF1}\left[\frac{3}{2}, -2(2 + m), 2(4 + m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big)^2 - \\
& \Big( \text{AppellF1}\left[\frac{1}{2}, -2(2 + m), 9 + 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
& \left( -\left( 2(2 + m) \text{AppellF1}\left[\frac{3}{2}, -3 - 2m, 9 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (9 + 2m) \text{AppellF1}\left[\frac{3}{2}, -2(2 + m), \right. \right. \\
& \left. \left. 2(5 + m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 3 \left( -\frac{1}{6}(9 + 2m) \right. \\
& \left. \text{AppellF1}\left[\frac{3}{2}, -2(2 + m), 10 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \right. \\
& \left. \frac{1}{3}(2 + m) \text{AppellF1}\left[\frac{3}{2}, 1 - 2(2 + m), 9 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) - 2 \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left( 2(2 + m) \left( -\frac{3}{10}(9 + 2m) \text{AppellF1}\left[\frac{5}{2}, -3 - 2m, \right. \right. \right. \\
& \left. \left. \left. 10 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{10} (-3 - 2m) \\
& \operatorname{AppellF1}\left[\frac{5}{2}, -2 - 2m, 9 + 2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\right.\right. \\
& \left.\left.\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \\
& (9 + 2m) \left(-\frac{3}{5} (5 + m) \operatorname{AppellF1}\left[\frac{5}{2}, -2 (2 + m), 1 + 2 (5 + m), \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\right.\right.\right. \\
& \left.\left.\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{3}{5} (2 + m) \operatorname{AppellF1}\left[\frac{5}{2}, 1 - 2 (2 + m), \right. \\
& 2 (5 + m), \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
& \left.\left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right)\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2 (2 + m), 9 + 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] - 2 \left(2 (2 + m) \operatorname{AppellF1}\left[\frac{3}{2}, -3 - 2m, \right. \right. \\
& 9 + 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \\
& (9 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2 (2 + m), 2 (5 + m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 - \\
& \left(2 \operatorname{AppellF1}\left[\frac{1}{2}, -2 (2 + m), 2 (4 + m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \\
& \left(2 \left((2 + m) \operatorname{AppellF1}\left[\frac{3}{2}, -3 - 2m, 8 + 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (4 + m) \operatorname{AppellF1}\left[\frac{3}{2}, -2 (2 + m), \right. \right. \\
& 9 + 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
& \left.\left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) - 3\right. \right. \\
& \left.\left. - \frac{1}{3} (4 + m) \operatorname{AppellF1}\left[\frac{3}{2}, -2 (2 + m), 1 + 2 (4 + m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \\
& \frac{1}{3} (2 + m) \operatorname{AppellF1}\left[\frac{3}{2}, 1 - 2 (2 + m), 2 (4 + m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) + 4
\end{aligned}$$

Problem 351: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c + dx]^2 (a + a \sin [c + dx])^m dx$$

Optimal (type 5, 81 leaves, 3 steps):

$$-\frac{1}{3 d} 2^{\frac{3}{2}+m} a \cos [c+d x]^3 \text{Hypergeometric2F1}\left[\frac{3}{2},-\frac{1}{2}-m,\frac{5}{2},\frac{1}{2} \left(1-\sin [c+d x]\right)\right] \\ (1+\sin [c+d x])^{-\frac{1}{2}-m} (a+a \sin [c+d x])^{-1+m}$$

Result (type 6, 6167 leaves):

$$- \left( \left( 192 \left( \cos \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{5+2m} \cos [c + dx]^2 \right)$$

$$\begin{aligned}
& \left( a + a \sin[c + d x] \right)^m \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] \left( 1 - \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{2(1+m)} \\
& \left( - \left( \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \right. \\
& \left. \left( 3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] - \right. \\
& \left. 2 \left( 2(1+m) \text{AppellF1}\left[\frac{3}{2}, -1-2m, 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (5+2m) \text{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) + \\
& \left( \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \\
& \left. \sec\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) \Big/ \left( 3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \right. \right. \\
& \left. \left. \frac{3}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] - \right. \\
& \left. 4 \left( (1+m) \text{AppellF1}\left[\frac{3}{2}, -1-2m, 4+2m, \frac{5}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (2+m) \text{AppellF1}\left[\frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) \Big) \Big/ \\
& \left( d \left( 48 \cos\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^8 \left( \cos\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{2m} \left( 1 - \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{2(1+m)} \right. \right. \\
& \left. \left. - \left( \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \Big/ \left( 3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] - 2 \left( 2(1+m) \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \left. \left. \left. -1-2m, 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + \right. \\
& \left. \left. (5+2m) \text{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) + \\
& \left( \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \sec\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) \Big/ \left( 3 \text{AppellF1}\left[\frac{1}{2}, -2 \right. \right. \\
& \left. \left. (1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] - \right.
\end{aligned}$$

$$\begin{aligned}
& 4 \left( (1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, -1-2m, 4+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \tan \left[ \right. \right. \\
& \quad \left. \left. \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) - \\
& 96 (5+2m) \left( \cos \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{4+2m} \sin \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \\
& \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(1+m)} \\
& \left( - \left( \operatorname{AppellF1} \left[ \frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 2 \left( 2(1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \\
& \quad \left. \left. -1-2m, 5+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \quad \left. \left. (5+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( \operatorname{AppellF1} \left[ \frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -2 \right. \right. \\
& \quad \left. \left. (1+m), 2(2+m), \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad \left. 4 \left( (1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, -1-2m, 4+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \tan \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) - \\
& 192 (1+m) \cos \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^6 \left( \cos \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2m} \\
& \sin \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \\
& \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-1+2(1+m)} \\
& \left( - \left( \operatorname{AppellF1} \left[ \frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 2 \left( 2(1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \\
& \quad \left. \left. -1-2m, 5+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& -1 - 2m, 5 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] + \\
& (5 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
& \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) + \\
& \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1 - 2m, \right. \right. \\
& \left. \left. 4 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \left. (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 5 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) + \\
192 & \left(\cos\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{5+2m} \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \\
& \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{2(1+m)} \\
& \left(-\left(\left(-\frac{1}{6}(5 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 6 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) - \frac{1}{3} \right. \\
& \left. (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1 - 2(1+m), 5 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 5 + 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2 \left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1 - 2m, \right. \right. \\
& \left. \left. 5 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \left. (5 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) + \\
& \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) /
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 4 \left( (1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, -1-2m, \right. \right. \right. \\
& \quad \left. \left. \left. 4+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \quad \left. \left. \left. (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \left( -\frac{1}{3} (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, -2(1+m), 1+2(2+m), \right. \right. \right. \\
& \quad \left. \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] - \frac{1}{3} (1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 1-2(1+m), \right. \right. \\
& \quad \left. \left. 2(2+m), \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \right) \Big/ \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (2+m) \operatorname{AppellF1} \left[ \frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( \operatorname{AppellF1} \left[ \frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \left( - \left( 2(1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, -1-2m, 5+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (5+2m) \operatorname{AppellF1} \left[ \frac{3}{2}, -2(1+m), \right. \right. \right. \\
& \quad \left. \left. \left. 2(3+m), \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right. \\
& \quad \left. \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] + 3 \left( -\frac{1}{6} (5+2m) \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, -2(1+m), 6+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \right) - \right. \\
& \quad \left. \frac{1}{3} (1+m) \operatorname{AppellF1} \left[ \frac{3}{2}, 1-2(1+m), 5+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \right) - 2
\end{aligned}$$

$$\begin{aligned}
& \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(2(1+m) \left(-\frac{3}{10}(5+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, \right.\right.\right. \\
& \quad \left.\left.\left.6+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
& \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{10}(-1-2m) \operatorname{AppellF1}\left[\right.\right. \\
& \quad \left.\left.\frac{5}{2}, -2m, 5+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
& \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) + \\
& \quad \left.(5+2m) \left(-\frac{3}{5}(3+m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 1+2(3+m), \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\right.\right.\right. \\
& \quad \left.\left.\left.(-c + \frac{\pi}{2} - dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right. \\
& \quad \left.\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right.\right. \\
& \quad \left.\left.2(3+m), \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
& \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right)\Big) \\
& \quad \left.\left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right.\right. \\
& \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right.\right.\right. \\
& \quad \left.\left.\left.5+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \quad \left.(5+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2 - \\
& \quad \left.\left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right.\right. \\
& \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right. \\
& \quad \left.\left.\left(-2\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 4+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right.\right. \right.\right. \\
& \quad \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), \right.\right.\right. \\
& \quad \left.\left.\left.5+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \right. \\
& \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 3\left(-\frac{1}{3}(2+m) \right. \right. \\
& \quad \left.\left.\operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 1+2(2+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right. \right. \\
& \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) - \right.
\end{aligned}$$

Problem 352: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sec^2(c + dx) (a + a \sin(c + dx))^m dx$$

Optimal (type 5, 73 leaves, 3 steps):

$$\frac{1}{d} 2^{-\frac{1}{2}+m} \text{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{3}{2}-m, \frac{1}{2}, \frac{1}{2} (1-\sin[c+dx])\right] \sec[c+dx] (1+\sin[c+dx])^{\frac{1}{2}-m} (a+a \sin[c+dx])^m$$

Result (type 6, 12061 leaves):

$$\begin{aligned}
 & - \left( \left( \text{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] (a + a \sin[c + d x])^m \right. \right. \\
 & \left. \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{2(-1+m)} \left( \frac{1}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2} \right)^{2m} \right. \\
 & \left( - \left( \left( 5 \text{AppellF1} \left[ -\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) / \right. \\
 & \left. \left( \text{AppellF1} \left[ -\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] - \right. \\
 & \left. 4 \left( m \text{AppellF1} \left[ \frac{1}{2}, 2-2m, 1+2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (-1+m) \text{AppellF1} \left[ \frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \right. \right. \\
 & \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) + \\
 & \left( 15 \text{AppellF1} \left[ \frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \\
 & \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) / \\
 & \left( \text{AppellF1} \left[ \frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] - \right. \\
 & \left. \left. \frac{4}{3} \left( m \text{AppellF1} \left[ \frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (-1+m) \text{AppellF1} \left[ \frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) + \\
 & \left( 25 \text{AppellF1} \left[ \frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \\
 & \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^4 \right) / \\
 & \left( 5 \text{AppellF1} \left[ \frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] - \right. \\
 & \left. 4 \left( m \text{AppellF1} \left[ \frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (-1+m) \text{AppellF1} \left[ \frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \right. \right. \\
 & \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) + \\
 & \left( 7 \text{AppellF1} \left[ \frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \\
 & \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^6 \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( 7 \text{AppellF1} \left[ \frac{5}{2}, 2 - 2m, 2m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& 4 \left( m \text{AppellF1} \left[ \frac{7}{2}, 2 - 2m, 1 + 2m, \frac{9}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1 + m) \text{AppellF1} \left[ \frac{7}{2}, 3 - 2m, 2m, \frac{9}{2}, \right. \\
& \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \Bigg) \\
& \left( 20d \left( \cos \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] - \sin \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] \right)^2 \right. \\
& \left( \cos \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] + \sin \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] \right)^2 \\
& \left. \left( -\frac{1}{20} (-1 + m) \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right. \right. \\
& \left. \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-1+2(-1+m)} \left( \frac{1}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{2m} \right. \\
& \left. \left( - \left( \left( 5 \text{AppellF1} \left[ -\frac{1}{2}, 2 - 2m, 2m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right) \Big/ \left( \text{AppellF1} \left[ -\frac{1}{2}, 2 - 2m, 2m, \frac{1}{2}, \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 4 \left( m \text{AppellF1} \left[ \frac{1}{2}, \right. \right. \\
& \left. \left. 2 - 2m, 1 + 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \left. \left. (-1 + m) \text{AppellF1} \left[ \frac{1}{2}, 3 - 2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 15 \text{AppellF1} \left[ \frac{1}{2}, 2 - 2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \Big/ \\
& \left( \text{AppellF1} \left[ \frac{1}{2}, 2 - 2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \left. \frac{4}{3} \left( m \text{AppellF1} \left[ \frac{3}{2}, 2 - 2m, 1 + 2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1 + m) \text{AppellF1} \left[ \frac{3}{2}, 3 - 2m, 2m, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( 25 \operatorname{AppellF1} \left[ \frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^4 \right) / \\
& \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad 4 \left( m \operatorname{AppellF1} \left[ \frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1+m) \operatorname{AppellF1} \left[ \frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 7 \operatorname{AppellF1} \left[ \frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^6 \right) / \\
& \left( 7 \operatorname{AppellF1} \left[ \frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad 4 \left( m \operatorname{AppellF1} \left[ \frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1+m) \operatorname{AppellF1} \left[ \frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \tan \left[ \right. \right. \\
& \quad \left. \left. \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) - \\
& \frac{1}{80} \csc \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(-1+m)} \\
& \quad \left( \frac{1}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{2m} \\
& \quad \left( - \left( \left( 5 \operatorname{AppellF1} \left[ -\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \left( \operatorname{AppellF1} \left[ -\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 4 \left( m \operatorname{AppellF1} \left[ \frac{1}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 2-2m, 1+2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \quad \left. \left. \left. (-1+m) \operatorname{AppellF1} \left[ \frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right. \\
& \quad \left( 15 \operatorname{AppellF1} \left[ \frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( \text{AppellF1} \left[ \frac{1}{2}, 2 - 2m, 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad \left. \frac{4}{3} \left( m \text{AppellF1} \left[ \frac{3}{2}, 2 - 2m, 1 + 2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1 + m) \text{AppellF1} \left[ \frac{3}{2}, 3 - 2m, 2m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 25 \text{AppellF1} \left[ \frac{3}{2}, 2 - 2m, 2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^4 \right) / \\
& \left( 5 \text{AppellF1} \left[ \frac{3}{2}, 2 - 2m, 2m, \frac{5}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad \left. 4 \left( m \text{AppellF1} \left[ \frac{5}{2}, 2 - 2m, 1 + 2m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1 + m) \text{AppellF1} \left[ \frac{5}{2}, 3 - 2m, 2m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 7 \text{AppellF1} \left[ \frac{5}{2}, 2 - 2m, 2m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^6 \right) / \\
& \left( 7 \text{AppellF1} \left[ \frac{5}{2}, 2 - 2m, 2m, \frac{7}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad \left. 4 \left( m \text{AppellF1} \left[ \frac{7}{2}, 2 - 2m, 1 + 2m, \frac{9}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1 + m) \text{AppellF1} \left[ \frac{7}{2}, 3 - 2m, 2m, \frac{9}{2}, \tan \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) - \\
& \frac{1}{20} m \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(-1+m)} \\
& \left( \frac{1}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{1+2m} \\
& \left( - \left( \left( 5 \text{AppellF1} \left[ -\frac{1}{2}, 2 - 2m, 2m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \left( \text{AppellF1} \left[ -\frac{1}{2}, 2 - 2m, 2m, \frac{1}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 4 \left( m \text{AppellF1} \left[ \frac{1}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 2 - 2m, 1 + 2m, \frac{3}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right.
\end{aligned}$$

$$\begin{aligned}
& (-1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) + \\
& \left( 15 \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \Big/ \\
& \left( \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \quad \left. \frac{4}{3} \left( m \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \left( 25 \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4\right) \Big/ \\
& \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \quad \left. 4 \left( m \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \left( 7 \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^6\right) \Big/ \\
& \left( 7 \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \quad \left. 4 \left( m \operatorname{AppellF1}\left[\frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \tan\left[\right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \frac{1}{20} \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left( 1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^{2(-1+m)} \\
& \left( \frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2} \right)^{2m}
\end{aligned}$$







$$\begin{aligned}
& \frac{3}{2}, 4 - 2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right)\right)\right) / \\
& \left(\text{AppellF1}\left[-\frac{1}{2}, 2 - 2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& 4 \left(m \text{AppellF1}\left[\frac{1}{2}, 2 - 2m, 1 + 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\right. \right. \\
& \left.\left. \left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1 + m) \text{AppellF1}\left[\frac{1}{2}, 3 - 2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]^2 - \\
& \left(15 \text{AppellF1}\left[\frac{1}{2}, 2 - 2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(-\frac{1}{3}m \text{AppellF1}\left[\frac{3}{2}, 2 - 2m, 1 + 2m, \right. \right. \\
& \left.\left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{1}{6}(2 - 2m) \\
& \text{AppellF1}\left[\frac{3}{2}, 3 - 2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{2}{3}\left(m \text{AppellF1}\left[\frac{3}{2}, 2 - 2m, 1 + 2m, \right. \right. \\
& \left.\left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1 + m) \text{AppellF1}\left[\right. \right. \\
& \left.\left. \frac{3}{2}, 3 - 2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{4}{3}\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
& \left(m\left(-\frac{3}{10}(1 + 2m) \text{AppellF1}\left[\frac{5}{2}, 2 - 2m, 2 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left.\left.\left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\right. \right. \right. \\
& \left.\left.\left. \frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{10}(2 - 2m) \text{AppellF1}\left[\frac{5}{2}, 3 - 2m, 1 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\right. \right. \right. \\
& \left.\left.\left. \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + (-1 + m)\left(-\frac{3}{5}m \text{AppellF1}\left[\frac{5}{2}, 3 - 2m, \right. \right. \\
& \left.\left. 1 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{10}(3 - 2m) \text{AppellF1}\left[\right. \right. \\
& \left.\left. \frac{5}{2}, 4 - 2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]
\end{aligned}$$





Problem 353: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sec [c + dx]^4 (a + a \sin [c + dx])^m dx$$

Optimal (type 5, 83 leaves, 3 steps):

$$\frac{1}{3 \, a \, d} \, 2^{-\frac{3+m}{2}} \, \text{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{5}{2}-m, -\frac{1}{2}, \frac{1}{2} \left(1-\sin[c+dx]\right)\right] \, \sec[c+dx]^3 \left(1+\sin[c+dx]\right)^{\frac{1}{2}-m} \left(a+a\sin[c+dx]\right)^{1+m}$$

### Result (type 6, 3545 leaves):

$$\begin{aligned}
& \left( \text{AppellF1} \left[ -\frac{3}{2}, 4 - 2m, -7 + 2m, -\frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \left. \cos \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - dx \right) \right]^{2m} \csc \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^{13} \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] (a + a \sin [c + dx])^m \right) / \\
& \left( 192d \left( -1 + \cot \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^4 \left( 2 (-7 + 2m) \text{AppellF1} \left[ -\frac{1}{2}, 4 - 2m, \right. \right. \right. \\
& \left. \left. \left. -6 + 2m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + 4 (-2 + m) \right. \right. \\
& \left. \left. \text{AppellF1} \left[ -\frac{1}{2}, 5 - 2m, -7 + 2m, \frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \right. \\
& \left. \left. \text{AppellF1} \left[ -\frac{3}{2}, 4 - 2m, -7 + 2m, -\frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \left. \cot \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \left( \cos \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] - \sin \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] \right)^4 \\
& \left( \cos \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] + \sin \left[ \frac{\pi}{4} + \frac{1}{2} \left( c - \frac{\pi}{2} + dx \right) \right] \right)^4 \\
& \left( \left( 13 \text{AppellF1} \left[ -\frac{3}{2}, 4 - 2m, -7 + 2m, -\frac{1}{2}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \\
& \left. \left. \cos \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - dx \right) \right]^{2m} \csc \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^{13} \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] (a + a \sin [c + dx])^m \right) / \right.
\end{aligned}$$



$$\begin{aligned}
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] + \text{AppellF1}\left[-\frac{3}{2}, 4-2m, -7+2m, \right. \\
& \left. -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) - \\
& \left(\cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{2m} \csc\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^{13} \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right. \\
& \left. \left(-\frac{3}{2}(-7+2m) \text{AppellF1}\left[-\frac{1}{2}, 4-2m, -6+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right) / \\
& \left(192\left(-1 + \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^4 \left(2(-7+2m) \text{AppellF1}\left[-\frac{1}{2}, 4-2m, \right. \right. \right. \\
& \left. \left. \left. -6+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \right. \\
& \left. \left. \left. 4(-2+m) \text{AppellF1}\left[-\frac{1}{2}, 5-2m, -7+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] + \text{AppellF1}\left[-\frac{3}{2}, 4-2m, -7+2m, -\frac{1}{2}, \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)\right) + \right. \right. \right. \\
& \left(\text{AppellF1}\left[-\frac{3}{2}, 4-2m, -7+2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \right. \\
& \left. \cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{2m} \csc\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^{13} \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) \left(-\frac{1}{2} \text{AppellF1}\left[ \right. \right. \right. \\
& \left. \left. \left. -\frac{3}{2}, 4-2m, -7+2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \right. \\
& \left. \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \csc\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 + \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \right. \right. \\
& \left. \left(-\frac{3}{2}(-7+2m) \text{AppellF1}\left[-\frac{1}{2}, 4-2m, -6+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) + \right. \right. \right. \\
& \left. \frac{3}{2}(4-2m) \text{AppellF1}\left[-\frac{1}{2}, 5-2m, -7+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) + \right. \right. \right. \\
& \left. 2(-7+2m)\left(\frac{1}{2}(-6+2m) \text{AppellF1}\left[\frac{1}{2}, 4-2m, -5+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) - \right. \right. \right. \\
& \left. \frac{1}{2}(4-2m) \text{AppellF1}\left[\frac{1}{2}, 5-2m, -6+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. 
\end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \\
& 4(-2+m)\left(\frac{1}{2}(-7+2m)\text{AppellF1}\left[\frac{1}{2}, 5-2m, -6+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right. \\
& \left.\left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) - \\
& \frac{1}{2}(5-2m)\text{AppellF1}\left[\frac{1}{2}, 6-2m, -7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2, \right.\right. \\
& \left.\left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right) / \\
& \left(192\left(-1+\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)^4\left(2(-7+2m)\text{AppellF1}\left[-\frac{1}{2}, 4-2m, -6+2m, \right.\right. \right. \\
& \left.\left.\left. \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 + \right.\right. \right. \\
& \left.\left.\left. 4(-2+m)\text{AppellF1}\left[-\frac{1}{2}, 5-2m, -7+2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2, \right.\right. \right.\right. \right. \\
& \left.\left.\left.\left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \text{AppellF1}\left[-\frac{3}{2}, 4-2m, -7+2m, -\frac{1}{2}, \right.\right. \right.\right. \right. \\
& \left.\left.\left.\left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2\right)\right)\right)
\end{aligned}$$

Problem 354: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \cos[c + dx])^{5/2} (a + a \sin[c + dx])^m dx$$

Optimal (type 5, 88 leaves, 3 steps):

$$\begin{aligned}
& -\frac{1}{7de} 2^{\frac{11}{4}+m} a \left(e \cos[c + dx]\right)^{7/2} \text{Hypergeometric2F1}\left[\frac{7}{4}, -\frac{3}{4}-m, \frac{11}{4}, \frac{1}{2}(1-\sin[c + dx])\right] \\
& (1+\sin[c + dx])^{-\frac{3}{4}-m} (a + a \sin[c + dx])^{-1+m}
\end{aligned}$$

Result (type 6, 32 821 leaves): Display of huge result suppressed!

Problem 355: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \cos[c + dx])^{3/2} (a + a \sin[c + dx])^m dx$$

Optimal (type 5, 88 leaves, 3 steps):

$$\begin{aligned}
& -\frac{1}{5de} 2^{\frac{9}{4}+m} a \left(e \cos[c + dx]\right)^{5/2} \text{Hypergeometric2F1}\left[\frac{5}{4}, -\frac{1}{4}-m, \frac{9}{4}, \frac{1}{2}(1-\sin[c + dx])\right] \\
& (1+\sin[c + dx])^{-\frac{1}{4}-m} (a + a \sin[c + dx])^{-1+m}
\end{aligned}$$

Result (type 6, 13 703 leaves):



$$\begin{aligned}
& \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \Big) + \\
& \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right], -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right] \Big) \Big/ \\
& \left( -9 \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \\
& \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right], -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right] + \\
& 2 \left( 4 (2 + m) \text{AppellF1} \left[ \frac{9}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{13}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right], \right. \right. \\
& \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right] + (1 + 4m) \text{AppellF1} \left[ \frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan \left[ \right. \right. \\
& \left. \left. \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right], -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \Big) \Big) \Big) \Big) \Big/ \\
& \left( 5d \cos [c + dx]^{3/2} \left( \frac{64}{5} m \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right. \right. \\
& \left. \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right]^2 \right)^{-1+2m} \right. \\
& \left. \left( \frac{1}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right]^2} \right)^{3+2m} \right. \\
& \left. \sqrt{\frac{\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right]^3}{\left( 1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right]^2 \right)^2}} \right. \\
& \left( \left( 25 \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right], -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right]^2 \right. \right. \\
& \left. \left( 1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right]^2 \right) \right) \Big/ \left( -5 \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2} - 2m, \right. \right. \\
& \left. \left. 3 + 2m, \frac{5}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right] + \right. \\
& \left. 2 \left( (6 + 4m) \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right], \right. \right. \right. \\
& \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right] + (1 + 4m) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \\
& \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right) + \\
& \left( 25 \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right)^2 \right] \right] \right) \Big)
\end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)\Big/ \\
& \left(5 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] - \right. \\
& 2 \left(4(2+m) \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \\
& \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (1+4m) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \\
& \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \\
& 9 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \left(-\left(\text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \right. \\
& \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)\Big/ \\
& \left(-9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, \right. \\
& \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) + 2 \left((6+4m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \\
& \left. 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \\
& (1+4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, \\
& \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\Big) + \\
& \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\Big) \Big/ \\
& \left(-9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, \right. \\
& \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) + 2 \left(4(2+m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \\
& \left. 5 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \\
& (1+4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, \\
& \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\Big) \Big) + \\
& \frac{32}{5} (3 + 2m) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \\
& \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)^{2m} \\
& \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2}\right)^{4+2m}
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2}} \\
& \left( \left( 25 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right. \right. \\
& \left. \left. \left( 1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) \Big/ \left( -5 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \right. \\
& \left. 2 \left( (6 + 4m) \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + (1 + 4m) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \left( 25 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right. \\
& \left. \left( 5 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - \right. \\
& \left. \left. 2 \left( 4(2 + m) \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + (1 + 4m) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \right. \\
& \left. 9 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left( - \left( \left( \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \left( 1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) \Big/ \right. \right. \\
& \left. \left. \left( -9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + 2 \left( (6 + 4m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \right. \right. \right. \\
& \left. \left. \left. (1 + 4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \right. \\
& \left. \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right/ \right. \\
& \left. \left( -9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right. \right)
\end{aligned}$$

$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2]+2\left(4(2+m) \operatorname{AppellF1}\left[\frac{9}{4},-\frac{1}{2}-2 m,\right.\right. \\
& \left.\left.5+2 m,\frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+ \right. \\
& \left.(1+4 m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2 m, 4+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\Big)- \\
& \frac{1}{5 \sqrt{\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^3}{\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^2}}} 32\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^{2 m} \\
& \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2}\right)^{3+2 m} \\
& \left(\left(\frac{1}{4} \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2-\frac{3}{4} \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right) / \right. \\
& \left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^2-\left(\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\right.\right. \\
& \left.\left.\left(\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^3\right)\right) / \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^3\right) \\
& \left(\left(25 \operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2 m, 3+2 m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right.\right. \\
& \left.\left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\right) / \left(-5 \operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2 m,\right.\right. \\
& \left.\left.3+2 m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+ \right. \\
& \left.2\left(\left(6+4 m\right) \operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2 m, 4+2 m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right. \right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+\left(1+4 m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2 m, 3+2 m, \frac{9}{4},\right.\right. \\
& \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)+ \right. \\
& \left.\left(25 \operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2 m, 4+2 m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right. \right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\right) / \left(5 \operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2 m, 4+2 m,\right.\right. \right. \\
& \left.\left.\left.\frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]- \right. \\
& \left.2\left(4(2+m) \operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2 m, 5+2 m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right. \right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+\left(1+4 m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2 m, 4+2 m, \frac{9}{4},\right.\right. \\
& \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)+ \right.
\end{aligned}$$

$$\begin{aligned}
& 9 \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left( - \left( \left( \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \left( 1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) \right) / \\
& \quad \left( -9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + 2 \left( (6 + 4m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \\
& \quad \left. \left. 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \right. \\
& \quad \left. (1 + 4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \text{AppellF1}\left[\frac{5}{4}, \right. \\
& \quad \left. -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] / \\
& \quad \left( -9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + 2 \left( 4 (2 + m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \\
& \quad \left. \left. 5 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \right. \\
& \quad \left. (1 + 4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) - \\
& \quad \frac{64}{5} \left( 1 - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^{2m} \left( \frac{1}{1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2} \right)^{3+2m} \\
& \quad \sqrt{\frac{\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right] - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2}} \\
& \quad \left( \left( 25 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right] \right) / \right. \\
& \quad \left( 2 \left( -5 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + 2 \left( (6 + 4m) \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
& \quad \left. \left. \left. 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \right. \\
& \quad \left. (1 + 4m) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right) \\
\end{aligned}$$



$$\begin{aligned}
& \left(1 + 4m\right) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
& \quad \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) + \\
& \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] / \\
& \left(-9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 2 \left(4(2+m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \\
& \quad \left. \left. 5 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \quad \left.\left(1 + 4m\right) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) - \\
& \left(25 \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \\
& \left(\left((6 + 4m) \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1 + 4m) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 5 \left(-\frac{1}{10}(3 + 2m) \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \right. \right. \\
& \quad \left. \left. \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
& \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{1}{10}\left(-\frac{1}{2} - 2m\right) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
& \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) + 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left((6 + 4m) \right. \\
& \quad \left. \left(-\frac{5}{18}(4 + 2m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \right. \\
& \quad \left. \left. \frac{5}{18}\left(-\frac{1}{2} - 2m\right) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) + \right. \\
& \quad \left. (1 + 4m) \left(-\frac{5}{18}(3 + 2m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right)
\end{aligned}$$





$$\begin{aligned}
& \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2, -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] + \\
& \left( -\frac{5}{18} (4+2m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 5+2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \sec\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] + \right. \\
& \quad \left. \frac{5}{18} \left( -\frac{1}{2} - 2m \right) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \sec\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \right) / \\
& \left( -9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4+2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] + 2 \left( 4 (2+m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
& \quad \left. \left. \left. 5+2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \right) + \\
& \quad \left( (1+4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \right) \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] + \\
& \left( \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3+2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \right) \left( \left( (6+4m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 4+2m, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \frac{13}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \right) + \\
& \quad \left( (1+4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3+2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \right) \sec\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] - \\
& 9 \left( -\frac{5}{18} (3+2m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \sec\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \right) + \\
& \quad \left. \frac{5}{18} \left( -\frac{1}{2} - 2m \right) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3+2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \sec\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \right) + \\
& 2 \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \left( (6+4m) \left( -\frac{9}{26} (4+2m) \text{AppellF1}\left[\frac{13}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. 5+2m, \frac{17}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right. \\
& \quad \left. -\tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \right) \sec\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right] + \frac{9}{26} \left( -\frac{1}{2} - 2m \right) \right. \\
& \quad \left. \text{AppellF1}\left[\frac{13}{4}, \frac{1}{2} - 2m, 4+2m, \frac{17}{4}, \tan\left[\frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right)^2\right]\right] \right)
\end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + (1+4m) \left(-\frac{9}{26} (3+2m) \text{AppellF1}\left[\frac{13}{4}, \frac{1}{2} - 2m, \right.\right. \\
& \left.\left. 4+2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{9}{26}\left(\frac{1}{2} - 2m\right) \text{AppellF1}\left[\frac{13}{4}, \frac{3}{2} - 2m, 3+2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right) \\
& \left. \left( -9 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 2 \left( (6+4m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right.\right. \right. \\
& \left. \left. \left. 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \left. \left. \left. (1+4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^2 - \\
& \left( \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \left. \left( \left( 4(2+m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 5+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1+4m) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, \right.\right. \right. \\
& \left. \left. \left. 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right. \\
& \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \right. \\
& \left. 9 \left( -\frac{5}{18} (4+2m) \text{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 5+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) + \right. \\
& \left. \frac{5}{18} \left(-\frac{1}{2} - 2m\right) \text{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) + \right. \\
& \left. 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left( 4(2+m) \left( -\frac{9}{26} (5+2m) \text{AppellF1}\left[\frac{13}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \right. \\
& \left. \left. \left. \left. 6+2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \right. \right. \\
& \left. \left. \left. \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{9}{26} \left(-\frac{1}{2} - 2m\right) \right) \right) \right)
\end{aligned}$$

Problem 356: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{e \cos(c + dx)} \left(a + a \sin(c + dx)\right)^m dx$$

Optimal (type 5, 88 leaves, 3 steps):

$$-\frac{1}{3 d e} 2^{\frac{7}{4}+m} a \left(e \cos [c+d x]\right)^{3/2} \text{Hypergeometric2F1}\left[\frac{3}{4}, \frac{1}{4}-m, \frac{7}{4}, \frac{1}{2} \left(1-\sin [c+d x]\right)\right] \\ \left(1+\sin [c+d x]\right)^{\frac{1}{4}-m} \left(a+a \sin [c+d x]\right)^{-1+m}$$

Result (type 6, 3061 leaves):

$$-\left(\left(28 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 2+2m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right.\right. \\ \left.\left.\operatorname{Cos}\left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx\right)\right]^{2m} \sqrt{\operatorname{Cos}[c+dx]} \sqrt{e \operatorname{Cos}[c+dx]}\right)\right)$$





$$\begin{aligned}
& \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
& \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + (1 + 4m) \left(-\frac{7}{22} (2 + 2m) \operatorname{AppellF1}\left[\frac{11}{4},\right.\right. \\
& \left.\left.\frac{1}{2} - 2m, 3 + 2m, \frac{15}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
& \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{7}{22} \left(\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\right.\right. \\
& \left.\left.\frac{11}{4}, \frac{3}{2} - 2m, 2 + 2m, \frac{15}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
& \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right)\right) / \\
& \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \left.6 \left(4 (1 + m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{11}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right.\right. \right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2} - 2m, 2 + 2m, \frac{11}{4}, \operatorname{Tan}\left[\right.\right.\right. \\
& \left.\left.\left.\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)\right)\right)
\end{aligned}$$

Problem 357: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin [c + d x])^m}{\sqrt{e \cos [c + d x]}} dx$$

Optimal (type 5, 86 leaves, 3 steps):

$$-\frac{1}{d e} 2^{\frac{5}{4}+m} a \sqrt{e \cos [c+d x]} \text{Hypergeometric2F1}\left[\frac{1}{4}, \frac{3}{4}-m, \frac{5}{4}, \frac{1}{2} (1-\sin [c+d x])\right] \\ (1+\sin [c+d x])^{\frac{3}{4}-m} (a+a \sin [c+d x])^{-1+m}$$

### Result (type 6, 3947 leaves):

$$\begin{aligned}
& - \left( \left( 10 \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \left. \cos \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - dx \right) \right]^{2m} \sqrt{\cos [c + dx]} \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 (a + a \sin [c + dx])^m \right. \\
& \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \Big/ \left( d \sqrt{e \cos [c + dx]} \left( -1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right. \\
& \left. \left( -8m \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{9}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \left. (2 - 8m) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2} - 2m, 2m, \frac{9}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \left. 5 \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right)
\end{aligned}$$





$$\begin{aligned}
& \left( 10 \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \cos \left[ \frac{1}{2} \left( -c + \frac{\pi}{2} - dx \right) \right]^{2m} \sqrt{\cos[c + dx]} \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right. \\
& \quad \left( -8m \left( \frac{5}{18} (1+2m) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2} - 2m, 2+2m, \frac{13}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 - \frac{5}{18} \right. \right. \\
& \quad \left. \left. \left( \frac{1}{2} - 2m \right) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2} - 2m, 1+2m, \frac{13}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right. \\
& \quad \left. (2-8m) \left( \frac{5}{9}m \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2} - 2m, 1+2m, \frac{13}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 - \frac{5}{18} \right. \right. \\
& \quad \left. \left. \left( \frac{3}{2} - 2m \right) \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right. \\
& \quad \left. \frac{5}{2} \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] + 5 \left( \frac{1}{5}m \operatorname{AppellF1} \left[ \frac{5}{4}, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{2} - 2m, 1+2m, \frac{9}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 - \frac{1}{10} \left( \frac{1}{2} - 2m \right) \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2} - 2m, 2m, \frac{9}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \Big/ \\
& \quad \left( \left( -1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \left( -8m \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2} - 2m, 1+2m, \frac{9}{4}, \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. \left. (2-8m) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2} - 2m, 2m, \frac{9}{4}, \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + 5 \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \right. \right. \right. \\
& \quad \left. \left. \left. \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) \right)
\end{aligned}$$

Problem 358: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^m}{(e \cos[c + d x])^{3/2}} dx$$

Optimal (type 5, 82 leaves, 3 steps):

$$\left( \frac{3}{4}^{1+m} \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{5}{4}-m, \frac{3}{4}, \frac{1}{2} (1 - \sin[c + d x])\right] \right. \\ \left. (1 + \sin[c + d x])^{\frac{1-m}{4}} (a + a \sin[c + d x])^m \right) / (d e \sqrt{e \cos[c + d x]})$$

Result (type 6, 10902 leaves):

$$- \left( \left( \cot\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right] (a + a \sin[c + d x])^m \left(1 - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right)^{2(-1+m)} \right. \right. \\ \left. \left. \left( \frac{1}{1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2} \right)^{-1+2m} \sqrt{\frac{\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right] - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right)^2}} \right. \right. \\ \left. \left. \left( \left( 63 \text{AppellF1}\left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \right) / \right. \right. \\ \left. \left. \left( -3 \text{AppellF1}\left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] + \right. \right. \\ \left. \left. 2 \left( 4m \text{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \right. \\ \left. \left. \left. -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] + (-3 + 4m) \text{AppellF1}\left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \right. \right. \\ \left. \left. \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right) + \right. \right. \\ \left. \left. \left( 98 \text{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \right. \right. \\ \left. \left. \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right) / \right. \right. \\ \left. \left. \left( 7 \text{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] - \right. \right. \\ \left. \left. 2 \left( 4m \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \right. \\ \left. \left. \left. -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] + (-3 + 4m) \text{AppellF1}\left[\frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \right. \right. \\ \left. \left. \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right) + \right. \right. \\ \left. \left. \left( 33 \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \right. \right. \\ \left. \left. \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^4\right) / \right)$$

$$\begin{aligned}
& \left( 11 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& 2 \left( 4m \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{3}{2} - 2m, 1+2m, \frac{15}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3+4m) \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \right. \\
& \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \Bigg) \\
& \left( 21d \left( e \cos[c+dx] \right)^{3/2} \left( -\frac{1}{42} (-1+2m) \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right. \right. \\
& \left. \left. \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(-1+m)} \left( \frac{1}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{2m} \right. \\
& \left. \left. \sqrt{\frac{\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^3}{\left( 1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \right) \right. \\
& \left. \left( \left( 63 \operatorname{AppellF1} \left[ -\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right. \\
& \left. \left. \left( -3 \operatorname{AppellF1} \left[ -\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. dx \right) \right]^2 \right] + 2 \left( 4m \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 1+2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \left. \left. \left. \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3+4m) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \right. \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right. \\
& \left. \left. \left( 98 \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \\
& \left. \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) \right. \\
& \left. \left( 7 \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \left. \left. 2 \left( 4m \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 1+2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3+4m) \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \right. \right. \\
& \left. \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 33 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^4 \right) / \\
& \left( 11 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad 2 \left( 4m \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{3}{2} - 2m, 1+2m, \frac{15}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3+4m) \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) - \\
& \frac{1}{21} (-1+m) \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-1+2(-1+m)} \\
& \left( \frac{1}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{-1+2m} \\
& \sqrt{\frac{\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^3}{\left( 1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \\
& \left( \left( 63 \operatorname{AppellF1} \left[ -\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \right. \\
& \quad \left. \left( -3 \operatorname{AppellF1} \left[ -\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. + 2 \left( 4m \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 1+2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3+4m) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 98 \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \\
& \left( 7 \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad \left. 2 \left( 4m \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 1+2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3+4m) \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 33 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^4\right] \Big/ \\
& \left(11 \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] - \right. \\
& 2 \left(4m \text{AppellF1}\left[\frac{11}{4}, \frac{3}{2} - 2m, 1+2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (-3+4m) \text{AppellF1}\left[\frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\Big) - \\
& \frac{1}{84} \csc\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)^{2(-1+m)} \\
& \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]}\right)^{-1+2m} \\
& \sqrt{\frac{\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^3\right]}{\left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)^2}} \\
& \left(\left(63 \text{AppellF1}\left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)\right. \right. \\
& \left. \left. -3 \text{AppellF1}\left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] + 2 \left(4m \text{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 1+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (-3+4m) \text{AppellF1}\left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \right. \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) + \\
& \left(98 \text{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \Big/ \\
& \left(7 \text{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) - \right. \\
& 2 \left(4m \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 1+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (-3+4m) \text{AppellF1}\left[\frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \right. \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) + \\
& \left(33 \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^4\right]\right) \Big/
\end{aligned}$$

$$\begin{aligned}
& \left( 11 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad 2 \left( 4m \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{3}{2} - 2m, 1+2m, \frac{15}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3+4m) \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \frac{1}{42} \sqrt{\frac{\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^3}{\left( 1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \cot \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \\
& \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(-1+m)} \\
& \left( \frac{1}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{-1+2m} \\
& \left( \left( 63 \operatorname{AppellF1} \left[ -\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \left( -3 \operatorname{AppellF1} \left[ -\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + 2 \left( 4m \operatorname{AppellF1} \left[ \frac{3}{4}, \right. \right. \\
& \quad \left. \left. \frac{3}{2} - 2m, 1+2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \quad \left. (-3+4m) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 98 \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \\
& \left( 7 \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \quad \left. 2 \left( 4m \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 1+2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3+4m) \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \tan \left[ \right. \right. \\
& \quad \left. \left. \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 33 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^4 \right) / \left( 11 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^4 \right] \right)
\end{aligned}$$

$$\begin{aligned}
& \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2]-2\left(4 m \operatorname{AppellF1}\left[\frac{11}{4},\right.\right. \\
& \left.\left.\frac{3}{2}-2 m, 1+2 m, \frac{15}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+ \right. \\
& \left.(-3+4 m) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{5}{2}-2 m, 2 m, \frac{15}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\Big) \\
& \left(\left(\frac{1}{4} \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2-\frac{3}{4} \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\right. \\
& \left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^2-\right. \\
& \left.\left(\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\left(\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]-\right.\right.\right. \\
& \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^3\right)\right)\right)\Big/\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^3\Big)+ \\
& \frac{1}{21} \operatorname{Cot}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^{2(-1+m)} \\
& \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2}\right)^{-1+2 m} \\
& \sqrt{\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^3}{\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^2}} \\
& \left(\left(63\left(\frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2}-2 m, 1+2 m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right.\right.\right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]-\frac{1}{6}\right. \\
& \left.\left(\frac{3}{2}-2 m\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{5}{2}-2 m, 2 m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\right)\Big) \\
& \left.\left(-3 \operatorname{AppellF1}\left[-\frac{1}{4}, \frac{3}{2}-2 m, 2 m, \frac{3}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-\right.\right.\right.\right. \\
& \left.\left.\left.d x\right)\right]^2\right]+2\left(4 m \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2}-2 m, 1+2 m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+(-3+4 m) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{5}{2}-2 m, 2 m, \frac{7}{4},\right.\right. \\
& \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)+ \\
& \left(49 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2}-2 m, 2 m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right. \\
& \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\right)\right)
\end{aligned}$$



$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\right)\right)\right) / \\
& \left(11 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}-2 m, 2 m, \frac{11}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]-\right. \\
& 2\left(4 m \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2}-2 m, 1+2 m, \frac{15}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+(-3+4 m) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{5}{2}-2 m, 2 m, \frac{15}{4},\right.\right. \\
& \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)- \\
& \left(63 \operatorname{AppellF1}\left[-\frac{1}{4}, \frac{3}{2}-2 m, 2 m, \frac{3}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right. \\
& \left(\left(4 m \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2}-2 m, 1+2 m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right. \\
& \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+(-3+4 m) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{5}{2}-2 m,\right.\right. \\
& \left.\left.2 m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\right] \\
& \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]-3\left(\frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{4},\right.\right. \\
& \left.\left.\frac{3}{2}-2 m, 1+2 m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right. \\
& \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]-\frac{1}{6}\left(\frac{3}{2}-2 m\right) \operatorname{AppellF1}\left[\right.\right. \\
& \left.\left.\frac{3}{4}, \frac{5}{2}-2 m, 2 m, \frac{7}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right. \\
& \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\right)+2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \\
& \left(4 m\left(-\frac{3}{14}(1+2 m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}-2 m, 2+2 m, \frac{11}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,\right.\right.\right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right) \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-\right.\right. \\
& \left.\left.d x\right)\right]+\frac{3}{14}\left(\frac{3}{2}-2 m\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{5}{2}-2 m, 1+2 m, \frac{11}{4}, \operatorname{Tan}\left[\frac{1}{4}\right.\right. \\
& \left.\left.\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \\
& \left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\right)+(-3+4 m)\left(-\frac{3}{7} m \operatorname{AppellF1}\left[\frac{7}{4}, \frac{5}{2}-2 m,\right.\right. \\
& \left.\left.1+2 m, \frac{11}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right. \\
& \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\right]+\frac{3}{14}\left(\frac{5}{2}-2 m\right) \operatorname{AppellF1}\left[\right.\right. \\
& \left.\left.\frac{7}{4}, \frac{7}{2}-2 m, 2 m, \frac{11}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]\right. \\
& \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\right)\right)\right)\right) / 
\end{aligned}$$

$$\begin{aligned}
& \left( -3 \operatorname{AppellF1} \left[ -\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + 2 \left( 4m \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 1 + 2m, \right. \right. \\
& \quad \left. \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \\
& \quad \left( -3 + 4m \right) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \\
& \quad \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2 - \\
& \left( 98 \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \left( - \left( 4m \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{11}{4}, \right. \right. \right. \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3 + 4m) \operatorname{AppellF1} \left[ \right. \\
& \quad \left. \frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \\
& \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] + 7 \left( -\frac{3}{7}m \operatorname{AppellF1} \left[ \frac{7}{4}, \right. \right. \\
& \quad \left. \frac{3}{2} - 2m, 1 + 2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \\
& \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] + \frac{3}{14} \left( \frac{3}{2} - 2m \right) \operatorname{AppellF1} \left[ \right. \\
& \quad \left. \frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \\
& \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \left) - 2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right. \\
& \left( 4m \left( -\frac{7}{22} (1 + 2m) \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{3}{2} - 2m, 2 + 2m, \frac{15}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] + \frac{7}{22} \left( \frac{3}{2} - 2m \right) \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{5}{2} - 2m, \right. \right. \\
& \quad \left. \left. 1 + 2m, \frac{15}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \right) + (-3 + 4m) \right. \\
& \left( -\frac{7}{11}m \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{15}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] + \frac{7}{22} \left( \frac{5}{2} - 2m \right) \operatorname{AppellF1} \left[ \frac{11}{4}, \frac{7}{2} - 2m, \right. \right. \\
& \quad \left. \left. 2m, \frac{15}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right)
\end{aligned}$$



Problem 359: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin [c + d x])^m}{(e \cos [c + d x])^{5/2}} dx$$

Optimal (type 5, 85 leaves, 3 steps):

$$\left( 2^{\frac{1}{4}+\mathfrak{m}} \text{Hypergeometric2F1}\left[ -\frac{3}{4}, \frac{7}{4}-\mathfrak{m}, \frac{1}{4}, \frac{1}{2} (1 - \text{Sin}[c + d x]) \right] \right. \\ \left. (1 + \text{Sin}[c + d x])^{\frac{3}{4}-\mathfrak{m}} (a + a \text{Sin}[c + d x])^{\mathfrak{m}} \right) \Big/ \left( 3 d e (e \text{Cos}[c + d x])^{3/2} \right)$$

Result (type 6, 16 046 leaves):

$$\begin{aligned}
& - \left( \left( a + a \sin [c + d x] \right)^m \left( 1 - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{-3+2m} \right. \\
& \left. \left( \frac{1}{1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2} \right)^{-1+2m} \sqrt{\frac{\tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^3}{\left( 1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^2}} \right. \\
& \left. \left( \left( 195 \text{AppellF1} \left[ -\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left( 1 + \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{-1+2m} \right)^{-1+2m} \right)^{-1+2m} \right)^{-1+2m}
\end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \Big/ \\
& \left( \text{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] - \right. \\
& 2 \left( 4m \text{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 1+2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (-5+4m) \text{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \right) + \\
& \left( 11700 \text{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \right) / \\
& \left( 5 \text{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] - \right. \\
& 2 \left( 4m \text{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 1+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (-5+4m) \text{AppellF1}\left[\frac{5}{4}, \frac{7}{2} - 2m, 2m, \frac{9}{4}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \right) + \\
& \left( 6318 \text{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \right. \\
& \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \right) / \\
& \left( 9 \text{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] - \right. \\
& 2 \left( 4m \text{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 1+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (-5+4m) \text{AppellF1}\left[\frac{9}{4}, \frac{7}{2} - 2m, 2m, \frac{13}{4}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \right) + \\
& \left( 3380 \text{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \right. \\
& \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^4\right] \right) / \\
& \left( 13 \text{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] - \right. \\
& 2 \left( 4m \text{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 1+2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + (-5+4m) \text{AppellF1}\left[\frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \right) + \\
& \left( 765 \text{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( 17 \operatorname{AppellF1} \left[ \frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& 2 \left( 4m \operatorname{AppellF1} \left[ \frac{17}{4}, \frac{5}{2} - 2m, 1+2m, \frac{21}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-5+4m) \operatorname{AppellF1} \left[ \frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \right. \\
& \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) / \\
& \left( 2340d \left( e \cos(c+dx) \right)^{5/2} \left( -\frac{1}{4680} (-1+2m) \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \right. \right. \\
& \left. \left. \left( 1 - \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-3+2m} \left( \frac{1}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{2m} \right. \\
& \left. \left. \sqrt{\frac{\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] - \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^3}{\left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \right. \right. \\
& \left. \left. \left( \left( 195 \operatorname{AppellF1} \left[ -\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right]^2 \right) \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \left( \operatorname{AppellF1} \left[ -\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \right. \right. \right. \\
& \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 2 \left( 4m \operatorname{AppellF1} \left[ \frac{1}{4}, \right. \right. \right. \\
& \left. \left. \left. \frac{5}{2} - 2m, 1+2m, \frac{5}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \left. \left. \left. (-5+4m) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \left( 11700 \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \left. \left. \left. \frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \\
& \left( 5 \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
& \left. 2 \left( 4m \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{5}{2} - 2m, 1+2m, \frac{9}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \left. \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-5+4m) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{7}{2} - 2m, \right. \right. \right. \\
& \left. \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& 2 \mathfrak{m}, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \Big) \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) + \left(6318 \text{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2\mathfrak{m}, 2\mathfrak{m}, \frac{9}{4}, \right. \right. \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) \Big/ \\
& \left(9 \text{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2\mathfrak{m}, 2\mathfrak{m}, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& 2 \left(4\mathfrak{m} \text{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2\mathfrak{m}, 1 + 2\mathfrak{m}, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] + (-5 + 4\mathfrak{m}) \text{AppellF1}\left[\frac{9}{4}, \frac{7}{2} - 2\mathfrak{m}, 2\mathfrak{m}, \frac{13}{4}, \tan\left[\frac{1}{4}\right. \right. \\
& \left. \left. \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) + \\
& \left(3380 \text{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2\mathfrak{m}, 2\mathfrak{m}, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4\Big) \Big/ \\
& \left(13 \text{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2\mathfrak{m}, 2\mathfrak{m}, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] - 2 \left(4\mathfrak{m} \text{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2\mathfrak{m}, 1 + 2\mathfrak{m}, \frac{17}{4}, \right. \right. \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] + (-5 + 4\mathfrak{m}) \text{AppellF1}\left[\frac{13}{4}, \frac{7}{2} - 2\mathfrak{m}, 2\mathfrak{m}, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \Big) \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) + \left(765 \text{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2\mathfrak{m}, 2\mathfrak{m}, \frac{17}{4}, \right. \right. \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^6\Big) \Big/ \\
& \left(17 \text{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2\mathfrak{m}, 2\mathfrak{m}, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] - 2 \left(4\mathfrak{m} \text{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2\mathfrak{m}, 1 + 2\mathfrak{m}, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] + \\
& (-5 + 4\mathfrak{m}) \text{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2\mathfrak{m}, 2\mathfrak{m}, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\Big) \Big) - \\
& \frac{1}{4680} (-3 + 2\mathfrak{m}) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \\
& \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{-4+2\mathfrak{m}}
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{1}{1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2} \right)^{-1+2m} \\
& \sqrt{\frac{\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right] - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2}} \\
& \left( - \left( \left( 195 \operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. - \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \cot\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) \left/ \left( \operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, \right. \right. \right. \\
& \left. \left. \left. 2m, \frac{1}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - 2 \left( 4m \operatorname{AppellF1}\left[\frac{1}{4}, \right. \right. \right. \\
& \left. \left. \left. \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \right. \\
& \left. \left. \left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) + \left( 11700 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \left/ \right. \\
& \left. \left( 5 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - \right. \\
& \left. \left. 2 \left( 4m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + (-5 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{7}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \left( 6318 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \left/ \right. \\
& \left. \left( 9 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - \right. \\
& \left. \left. 2 \left( 4m \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + (-5 + 4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{7}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \left( 3380 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^4 \right) \left/ \right. \left( 13 \operatorname{AppellF1}\left[\frac{9}{4}, \right. \right. \right. \\
& \left. \left. \left. \frac{7}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^4, -\tan\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx\right)\right]^4 \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] - \\
& 2 \left( 4m \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \operatorname{AppellF1}\left[\frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. \frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \left( 765 \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^6 \right) / \\
& \left( 17 \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2 \left( 4m \operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 1 + 2m, \right. \right. \\
& \left. \left. \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \left. \left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) + \\
& \frac{1}{4680 \sqrt{\frac{\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2}}} \left( 1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^{-3+2m} \\
& \left( \frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2} \right)^{-1+2m} \\
& \left( - \left( \left( 195 \operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) / \left( \operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, \right. \right. \right. \\
& \left. \left. \left. 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - 2 \left( 4m \operatorname{AppellF1}\left[\frac{1}{4}, \right. \right. \right. \\
& \left. \left. \left. \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \right. \\
& \left. \left. \left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) + \left( 11700 \operatorname{AppellF1}\left[ \right. \right. \right. \\
& \left. \left. \left. \frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) / \\
& \left( 5 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - \right.
\end{aligned}$$



$$\begin{aligned}
& \left( \left( \frac{1}{4} \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 - \frac{3}{4} \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) \Big/ \\
& \quad \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^2 - \\
& \quad \left( \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] \left( \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] - \right. \right. \\
& \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^3 \right) \Big/ \left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^3 \right) + \\
& \frac{1}{2340} \left( 1 - \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^{-3+2m} \left( \frac{1}{1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2} \right)^{-1+2m} \\
& \sqrt{\frac{\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] - \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^3}{\left( 1 + \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right)^2}} \\
& \left( \left( 195 \operatorname{AppellF1} \left[ -\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] \operatorname{Csc} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) \Big/ \\
& \quad \left( 2 \left( \operatorname{AppellF1} \left[ -\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] - 2 \left( 4m \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{5}{2} - 2m, 1+2m, \frac{5}{4}, \right. \right. \\
& \quad \left. \left. \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (-5+4m) \operatorname{AppellF1} \left[ \right. \\
& \quad \left. \left. \frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \\
& \quad \left( \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) - \left( 195 \operatorname{Cot} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right. \\
& \quad \left. \left( 3m \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{5}{2} - 2m, 1+2m, \frac{5}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] - \right. \\
& \quad \left. \left. \frac{3}{2} \left( \frac{5}{2} - 2m \right) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right] \right) \right) \Big/ \\
& \quad \left( \operatorname{AppellF1} \left[ -\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] - \right. \\
& \quad \left. 2 \left( 4m \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{5}{2} - 2m, 1+2m, \frac{5}{4}, \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \\
& \quad \left. \left. -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (-5+4m) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan} \left[ \right. \right. \\
& \quad \left. \left. \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2, -\operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \operatorname{Tan} \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - d x \right) \right]^2 \right) +
\end{aligned}$$



$$\begin{aligned}
& \left( 3380 \text{AppellF1} \left[ \frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^3 \right) / \\
& \left( 13 \text{AppellF1} \left[ \frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 2 \left( 4m \text{AppellF1} \left[ \frac{13}{4}, \frac{5}{2} - 2m, 1+2m, \right. \right. \\
& \quad \left. \left. \frac{17}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \quad \left. \left. (-5+4m) \text{AppellF1} \left[ \frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 3380 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^4 \left( -\frac{9}{13}m \text{AppellF1} \left[ \frac{13}{4}, \frac{5}{2} - 2m, 1+2m, \frac{17}{4}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
& \quad \left. \left. \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right. \\
& \quad \left. \left. \frac{9}{26} \left( \frac{5}{2} - 2m \right) \text{AppellF1} \left[ \frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right] \right) \right) / \\
& \left( 13 \text{AppellF1} \left[ \frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 2 \left( 4m \text{AppellF1} \left[ \frac{13}{4}, \frac{5}{2} - 2m, 1+2m, \right. \right. \\
& \quad \left. \left. \frac{17}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \quad \left. \left. (-5+4m) \text{AppellF1} \left[ \frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
& \left( 2295 \text{AppellF1} \left[ \frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^5 \right) / \\
& \left( 2 \left( 17 \text{AppellF1} \left[ \frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 2 \left( 4m \text{AppellF1} \left[ \frac{17}{4}, \frac{5}{2} - 2m, 1+2m, \right. \right. \right. \\
& \quad \left. \left. \frac{21}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, - \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
& \quad \left. \left. (-5+4m) \text{AppellF1} \left[ \frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \tan \left[ \frac{1}{4} \left( -c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right) \right)
\end{aligned}$$

$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \\
& \left(765 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^6 \left(-\frac{13}{17} m \operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{21}{4}, \right.\right.\right. \\
& \left.\left.\left. \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]\right. \\
& \left.\left.\left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \right.\right.\right. \\
& \left.\left.\left. \frac{13}{34} \left(\frac{5}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right], \right.\right.\right. \\
& \left.\left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right)\right) / \\
& \left(17 \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \right. \\
& \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2\right] - 2 \left(4m \operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 1 + 2m, \right.\right. \\
& \left.\left. \frac{21}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2\right] + \right. \\
& \left.\left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \right. \\
& \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] + \right. \\
& \left(195 \operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \right. \\
& \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \operatorname{Cot}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \right. \\
& \left(3m \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \right. \\
& \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] - \right. \\
& \left.\frac{3}{2} \left(\frac{5}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \right. \\
& \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] - \right. \\
& \left(4m \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \right. \\
& \left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] + (-5 + 4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, \right.\right. \\
& \left.\left. 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right) \\
& \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right] - 2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \\
& \left(4m \left(-\frac{1}{10} (1 + 2m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2 + 2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right. \right. \right. \\
& \left.\left.\left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)^2\right]^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right] + \frac{1}{10}\left(\frac{5}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{7}{2} - 2m, \right. \\
& \left. 1 + 2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \\
& \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right] + (-5 + 4m) \\
& \left(-\frac{1}{5}m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{7}{2} - 2m, 1 + 2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right. \\
& \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right] + \frac{1}{10}\left(\frac{7}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{9}{2} - 2m, \right. \right. \\
& \left. \left. 2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]\right)\right)\right) \\
& \left(\operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] - 2\left(4m \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 1 + 2m, \right. \right. \\
& \left. \left. \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] + \right. \\
& \left. \left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right]\right) \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right. \\
& \left. \left. - \right. \right. \\
& \left(11700 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \left(-\left(4m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{9}{4}, \right. \right. \right. \\
& \left. \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] + (-5 + 4m) \operatorname{AppellF1}\left[\right. \right. \right. \\
& \left. \left. \left. \frac{5}{4}, \frac{7}{2} - 2m, 2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right]\right) \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right] + 5\left(-\frac{1}{5}m \operatorname{AppellF1}\left[\frac{5}{4}, \right. \right. \right. \\
& \left. \left. \left. \frac{5}{2} - 2m, 1 + 2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right]\right. \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right] + \frac{1}{10}\left(\frac{5}{2} - 2m\right) \operatorname{AppellF1}\left[\right. \right. \right. \\
& \left. \left. \left. \frac{5}{4}, \frac{7}{2} - 2m, 2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right]\right. \right. \\
& \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]\right) - 2\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2 \\
& \left(4m \left(-\frac{5}{18} (1 + 2m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2 + 2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - d x\right)\right]^2\right]\right) \right)
\end{aligned}$$





$$\begin{aligned}
& \frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
& \left(4m\left(-\frac{13}{34}(1+2m)\operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 2+2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right.\right.\right. \\
& \left.\left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right. \\
& \left.\left.\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{13}{34}\left(\frac{5}{2} - 2m\right)\operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m,\right.\right. \\
& \left.\left.1+2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
& \left.\sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) + (-5+4m) \\
& \left(-\frac{13}{17}m\operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 1+2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right.\right. \\
& \left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right. \\
& \left.\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{13}{34}\left(\frac{7}{2} - 2m\right)\operatorname{AppellF1}\left[\frac{17}{4}, \frac{9}{2} - 2m,\right.\right. \\
& \left.\left.2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
& \left.\sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right)\Bigg) \\
& \left(13\operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right.\right. \\
& \left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2\left(4m\operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 1+2m,\right.\right. \\
& \left.\left.\frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \left.\left.(-5+4m)\operatorname{AppellF1}\left[\frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right.\right. \\
& \left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2 - \\
& \left(765\operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right.\right. \\
& \left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^6 \\
& \left.\left(-\left(4m\operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 1+2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right.\right. \right. \\
& \left.\left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5+4m)\operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m,\right.\right. \\
& \left.\left.2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 17\left(-\frac{13}{17}m\operatorname{AppellF1}\left[\frac{17}{4},\right.\right. \\
& \left.\left.\frac{9}{2} - 2m, 2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right)
\end{aligned}$$

Problem 371: Result more than twice size of optimal antiderivative.

$$\int (e \cos[c + d x])^{-3-2m} (a + a \sin[c + d x])^m dx$$

Optimal (type 5, 70 leaves, 3 steps):

$$\frac{1}{4 a d e (1+m)} (e \cos[c + d x])^{-2(1+m)} \text{Hypergeometric2F1}[2, -1-m, -m, \frac{1}{2} (1 - \sin[c + d x])] (a + a \sin[c + d x])^{1+m}$$

Result (type 5, 206 leaves):

$$\begin{aligned} & \frac{1}{8 d e^3 m (-1+m^2)} (e \cos[c + d x])^{-2m} \left( \sec[\frac{1}{4} (2c - \pi + 2d x)]^2 \right)^{-m} (a (1 + \sin[c + d x]))^m \\ & \left( 2 (-1+m^2) \text{Hypergeometric2F1}[-m, -m, 1-m, -\tan[\frac{1}{4} (2c - \pi + 2d x)]^2] + \right. \\ & (-1+m) m \csc[\frac{1}{4} (2c - \pi + 2d x)]^2 \left( \sec[\frac{1}{4} (2c - \pi + 2d x)]^2 \right)^m + m (1+m) \\ & \left. \text{Hypergeometric2F1}[1-m, -m, 2-m, -\tan[\frac{1}{4} (2c - \pi + 2d x)]^2] \tan[\frac{1}{4} (2c - \pi + 2d x)]^2 \right) \end{aligned}$$

Problem 372: Result more than twice size of optimal antiderivative.

$$\int (e \cos[c + d x])^{4-2m} (a + a \sin[c + d x])^m dx$$

Optimal (type 5, 89 leaves, 4 steps):

$$\begin{aligned} & \frac{1}{5 d e} 2^{\frac{5}{2}-m} (e \cos[c + d x])^{5-2m} \text{Hypergeometric2F1}[\frac{5}{2}, \frac{1}{2} (-3+2m), \frac{7}{2}, \frac{1}{2} (1+\sin[c + d x])] \\ & (1 - \sin[c + d x])^{-\frac{5}{2}+m} (a + a \sin[c + d x])^m \end{aligned}$$

Result (type 5, 200 leaves):

$$\begin{aligned} & -\frac{1}{d (-1+2m)} \\ & 32 e^4 (e \cos[c + d x])^{-2m} \left( \text{Hypergeometric2F1}[\frac{1}{2}-m, 3-m, \frac{3}{2}-m, -\tan[\frac{1}{4} (2c - \pi + 2d x)]^2] - \right. \\ & 2 \text{Hypergeometric2F1}[\frac{1}{2}-m, 4-m, \frac{3}{2}-m, -\tan[\frac{1}{4} (2c - \pi + 2d x)]^2] + \\ & \left. \text{Hypergeometric2F1}[\frac{1}{2}-m, 5-m, \frac{3}{2}-m, -\tan[\frac{1}{4} (2c - \pi + 2d x)]^2] \right) \\ & \left( \sec[\frac{1}{4} (2c - \pi + 2d x)]^2 \right)^{-m} (a (1 + \sin[c + d x]))^m \tan[\frac{1}{4} (2c - \pi + 2d x)] \end{aligned}$$

Problem 375: Result more than twice size of optimal antiderivative.

$$\int (e \cos[c + d x])^{-2-2m} (a + a \sin[c + d x])^m dx$$

Optimal (type 5, 87 leaves, 4 steps):

$$-\frac{1}{d e} 2^{-\frac{1}{2}-m} (e \cos[c+d x])^{-1-2 m} \text{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1}{2} (3+2 m), \frac{1}{2}, \frac{1}{2} (1+\sin[c+d x])\right] \\ (1-\sin[c+d x])^{\frac{1}{2}+m} (a+a \sin[c+d x])^m$$

Result (type 5, 186 leaves):

$$\frac{1}{2 d e^2 (-1+4 m^2)} (e \cos[c+d x])^{-2 m} \text{Cot}\left[\frac{1}{4} (2 c+\pi+2 d x)\right] \left((-1+2 m) \text{Cot}\left[\frac{1}{4} (2 c-\pi+2 d x)\right]^2 \text{Hypergeometric2F1}\left[-\frac{1}{2}-m, -m, \frac{1}{2}-m, -\tan\left[\frac{1}{4} (2 c-\pi+2 d x)\right]^2\right] + (1+2 m) \text{Hypergeometric2F1}\left[\frac{1}{2}-m, -m, \frac{3}{2}-m, -\tan\left[\frac{1}{4} (2 c-\pi+2 d x)\right]^2\right]\right) \\ \left(\sec\left[\frac{1}{4} (2 c-\pi+2 d x)\right]^2\right)^{-m} (a (1+\sin[c+d x]))^m$$

Problem 380: Result more than twice size of optimal antiderivative.

$$\int \sec[c+d x]^3 (a+b \sin[c+d x]) \, dx$$

Optimal (type 3, 41 leaves, 3 steps):

$$\frac{a \text{ArcTanh}[\sin[c+d x]]}{2 d} + \frac{\sec[c+d x]^2 (b+a \sin[c+d x])}{2 d}$$

Result (type 3, 83 leaves):

$$\frac{1}{2 d} \left( a \left( -\log[\cos[\frac{1}{2} (c+d x)]] - \sin[\frac{1}{2} (c+d x)] \right) + \log[\cos[\frac{1}{2} (c+d x)]] + \sin[\frac{1}{2} (c+d x)] \right) + b \sec[c+d x]^2 + a \sec[c+d x] \tan[c+d x]$$

Problem 381: Result more than twice size of optimal antiderivative.

$$\int \sec[c+d x]^5 (a+b \sin[c+d x]) \, dx$$

Optimal (type 3, 61 leaves, 4 steps):

$$\frac{3 a \text{ArcTanh}[\sin[c+d x]]}{8 d} + \frac{\sec[c+d x]^4 (b+a \sin[c+d x])}{4 d} + \frac{3 a \sec[c+d x] \tan[c+d x]}{8 d}$$

Result (type 3, 207 leaves):

$$\begin{aligned}
 & -\frac{3 a \operatorname{Log}[\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)]]}{8 d} + \\
 & \frac{3 a \operatorname{Log}[\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)]]}{8 d} + \frac{b \operatorname{Sec}[\cos[\frac{1}{2} (c+d x)]]^4}{4 d} + \\
 & \frac{a}{16 d (\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])^4} + \frac{3 a}{16 d (\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])^2} - \\
 & \frac{16 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^4}{16 d (\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^2}
 \end{aligned}$$

Problem 389: Result more than twice size of optimal antiderivative.

$$\int \cos[c+d x] (a+b \sin[c+d x])^2 \, dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(\mathbf{a} + \mathbf{b} \sin[c+d x])^3}{3 b d}$$

Result (type 3, 46 leaves):

$$\frac{a^2 \sin[c+d x]}{d} + \frac{a b \sin[c+d x]^2}{d} + \frac{b^2 \sin[c+d x]^3}{3 d}$$

Problem 391: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[\cos[c+d x]]^3 (a+b \sin[c+d x])^2 \, dx$$

Optimal (type 3, 59 leaves, 3 steps):

$$\frac{(\mathbf{a}^2 - \mathbf{b}^2) \operatorname{Arctanh}[\sin[c+d x]]}{2 d} + \frac{\operatorname{Sec}[\cos[c+d x]]^2 (\mathbf{b} + \mathbf{a} \sin[c+d x]) (\mathbf{a} + \mathbf{b} \sin[c+d x])}{2 d}$$

Result (type 3, 139 leaves):

$$\begin{aligned}
 & \frac{1}{4 d} \left( 2 (-a^2 + b^2) \operatorname{Log}[\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)]] + \right. \\
 & 2 (a^2 - b^2) \operatorname{Log}[\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)]] + \\
 & \left. \frac{(\mathbf{a} + \mathbf{b})^2}{(\cos[\frac{1}{2} (c+d x)] - \sin[\frac{1}{2} (c+d x)])^2} - \frac{(\mathbf{a} - \mathbf{b})^2}{(\cos[\frac{1}{2} (c+d x)] + \sin[\frac{1}{2} (c+d x)])^2} \right)
 \end{aligned}$$

### Problem 392: Result more than twice size of optimal antiderivative.

$$\int \sec(c + dx)^5 (a + b \sin(c + dx))^2 dx$$

Optimal (type 3, 99 leaves, 4 steps):

$$\frac{(3a^2 - b^2) \operatorname{ArcTanh}[\sin(c + dx)]}{8d} + \frac{\sec(c + dx)^4 (b + a \sin(c + dx)) (a + b \sin(c + dx))}{4d} + \frac{\sec(c + dx)^2 (2ab + (3a^2 - b^2) \sin(c + dx))}{8d}$$

Result (type 3, 219 leaves):

$$\begin{aligned} \frac{1}{16d} \left( & 2(-3a^2 + b^2) \operatorname{Log}[\cos(\frac{1}{2}(c + dx)) - \sin(\frac{1}{2}(c + dx))] + \right. \\ & 2(3a^2 - b^2) \operatorname{Log}[\cos(\frac{1}{2}(c + dx)) + \sin(\frac{1}{2}(c + dx))] + \\ & \frac{(a + b)^2}{(\cos(\frac{1}{2}(c + dx)) - \sin(\frac{1}{2}(c + dx)))^4} + \frac{3a^2 + 2ab - b^2}{(\cos(\frac{1}{2}(c + dx)) - \sin(\frac{1}{2}(c + dx)))^2} - \\ & \left. \frac{(a - b)^2}{(\cos(\frac{1}{2}(c + dx)) + \sin(\frac{1}{2}(c + dx)))^4} + \frac{-3a^2 + 2ab + b^2}{(\cos(\frac{1}{2}(c + dx)) + \sin(\frac{1}{2}(c + dx)))^2} \right) \end{aligned}$$

### Problem 402: Result more than twice size of optimal antiderivative.

$$\int \cos(c + dx) (a + b \sin(c + dx))^3 dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a + b \sin(c + dx))^4}{4bd}$$

Result (type 3, 67 leaves):

$$\frac{a^3 \sin(c + dx)}{d} + \frac{3a^2 b \sin(c + dx)^2}{2d} + \frac{ab^2 \sin(c + dx)^3}{d} + \frac{b^3 \sin(c + dx)^4}{4d}$$

### Problem 405: Result more than twice size of optimal antiderivative.

$$\int \sec(c + dx)^5 (a + b \sin(c + dx))^3 dx$$

Optimal (type 3, 94 leaves, 4 steps):

$$\frac{3 a (a^2 - b^2) \operatorname{ArcTanh}[\sin[c + d x]]}{8 d} + \frac{3 a \sec[c + d x]^2 (b + a \sin[c + d x]) (a + b \sin[c + d x])}{8 d} + \frac{\sec[c + d x]^3 (a + b \sin[c + d x])^3 \tan[c + d x]}{4 d}$$

Result (type 3, 213 leaves):

$$\begin{aligned} & \frac{1}{16 d} \left( -6 a (a^2 - b^2) \operatorname{Log}[\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)]] + \right. \\ & 6 a (a^2 - b^2) \operatorname{Log}[\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)]] + \\ & \frac{(a + b)^3}{(\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^4} + \frac{3 (a - b) (a + b)^2}{(\cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)])^2} - \\ & \frac{(a - b)^3}{(\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^4} - \frac{3 (a - b)^2 (a + b)}{(\cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)])^2} \Big) \end{aligned}$$

Problem 413: Result more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^5 (a + b \sin[c + d x])^8 dx$$

Optimal (type 3, 144 leaves, 3 steps):

$$\begin{aligned} & \frac{(a^2 - b^2)^2 (a + b \sin[c + d x])^9}{9 b^5 d} - \frac{2 a (a^2 - b^2) (a + b \sin[c + d x])^{10}}{5 b^5 d} + \\ & \frac{2 (3 a^2 - b^2) (a + b \sin[c + d x])^{11}}{11 b^5 d} - \frac{a (a + b \sin[c + d x])^{12}}{3 b^5 d} + \frac{(a + b \sin[c + d x])^{13}}{13 b^5 d} \end{aligned}$$

Result (type 3, 572 leaves):

$$\begin{aligned} & \frac{1}{26357760 d} (-205920 (80 a^7 b + 168 a^5 b^3 + 70 a^3 b^5 + 5 a b^7) \cos[2 (c + d x)] - \\ & 25740 (256 a^7 b + 224 a^5 b^3 - 5 a b^7) \cos[4 (c + d x)] - 1098240 a^7 b \cos[6 (c + d x)] + \\ & 3843840 a^5 b^3 \cos[6 (c + d x)] + 2402400 a^3 b^5 \cos[6 (c + d x)] + 171600 a b^7 \cos[6 (c + d x)] + \\ & 1441440 a^5 b^3 \cos[8 (c + d x)] - 51480 a b^7 \cos[8 (c + d x)] - 288288 a^3 b^5 \cos[10 (c + d x)] - \\ & 20592 a b^7 \cos[10 (c + d x)] + 8580 a b^7 \cos[12 (c + d x)] + 16473600 a^8 \sin[c + d x] + \\ & 57657600 a^6 b^2 \sin[c + d x] + 43243200 a^4 b^4 \sin[c + d x] + 7207200 a^2 b^6 \sin[c + d x] + \\ & 128700 b^8 \sin[c + d x] + 2745600 a^8 \sin[3 (c + d x)] - 3843840 a^6 b^2 \sin[3 (c + d x)] - \\ & 9609600 a^4 b^4 \sin[3 (c + d x)] - 2402400 a^2 b^6 \sin[3 (c + d x)] - 53625 b^8 \sin[3 (c + d x)] + \\ & 329472 a^8 \sin[5 (c + d x)] - 6918912 a^6 b^2 \sin[5 (c + d x)] - 5765760 a^4 b^4 \sin[5 (c + d x)] - \\ & 720720 a^2 b^6 \sin[5 (c + d x)] - 6435 b^8 \sin[5 (c + d x)] - 1647360 a^6 b^2 \sin[7 (c + d x)] + \\ & 1029600 a^4 b^4 \sin[7 (c + d x)] + 514800 a^2 b^6 \sin[7 (c + d x)] + 12870 b^8 \sin[7 (c + d x)] - \\ & 800800 a^4 b^4 \sin[9 (c + d x)] + 80080 a^2 b^6 \sin[9 (c + d x)] - 1430 b^8 \sin[9 (c + d x)] - \\ & 65520 a^2 b^6 \sin[11 (c + d x)] - 1755 b^8 \sin[11 (c + d x)] + 495 b^8 \sin[13 (c + d x)]) \end{aligned}$$

### Problem 414: Result more than twice size of optimal antiderivative.

$$\int \cos[c + dx]^3 (a + b \sin[c + dx])^8 \, dx$$

Optimal (type 3, 77 leaves, 3 steps):

$$-\frac{(a^2 - b^2) (a + b \sin[c + dx])^9}{9 b^3 d} + \frac{a (a + b \sin[c + dx])^{10}}{5 b^3 d} - \frac{(a + b \sin[c + dx])^{11}}{11 b^3 d}$$

Result (type 3, 438 leaves):

$$\begin{aligned} & \frac{1}{506880 d} (-7920 (64 a^7 b + 168 a^5 b^3 + 84 a^3 b^5 + 7 a b^7) \cos[2 (c + d x)] - \\ & 15840 (8 a^7 b - 7 a^3 b^5 - a b^7) \cos[4 (c + d x)] + 147840 a^5 b^3 \cos[6 (c + d x)] + \\ & 73920 a^3 b^5 \cos[6 (c + d x)] + 3960 a b^7 \cos[6 (c + d x)] - 27720 a^3 b^5 \cos[8 (c + d x)] - \\ & 3960 a b^7 \cos[8 (c + d x)] + 792 a b^7 \cos[10 (c + d x)] + 380160 a^8 \sin[c + d x] + \\ & 1774080 a^6 b^2 \sin[c + d x] + 1663200 a^4 b^4 \sin[c + d x] + 332640 a^2 b^6 \sin[c + d x] + \\ & 6930 b^8 \sin[c + d x] + 42240 a^8 \sin[3 (c + d x)] - 295680 a^6 b^2 \sin[3 (c + d x)] - \\ & 554400 a^4 b^4 \sin[3 (c + d x)] - 147840 a^2 b^6 \sin[3 (c + d x)] - 3630 b^8 \sin[3 (c + d x)] - \\ & 177408 a^6 b^2 \sin[5 (c + d x)] - 110880 a^4 b^4 \sin[5 (c + d x)] + 495 b^8 \sin[5 (c + d x)] + \\ & 79200 a^4 b^4 \sin[7 (c + d x)] + 23760 a^2 b^6 \sin[7 (c + d x)] + 495 b^8 \sin[7 (c + d x)] - \\ & 6160 a^2 b^6 \sin[9 (c + d x)] - 275 b^8 \sin[9 (c + d x)] + 45 b^8 \sin[11 (c + d x)]) \end{aligned}$$

### Problem 465: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sec[c + dx]}{(a + b \sin[c + dx])^8} \, dx$$

Optimal (type 3, 385 leaves, 4 steps):

$$\begin{aligned} & -\frac{\log[1 - \sin[c + dx]]}{2 (a + b)^8 d} + \frac{\log[1 + \sin[c + dx]]}{2 (a - b)^8 d} - \\ & \frac{8 a b (a^2 + b^2) (a^4 + 6 a^2 b^2 + b^4) \log[a + b \sin[c + dx]]}{(a^2 - b^2)^8 d} + \frac{b}{7 (a^2 - b^2) d (a + b \sin[c + dx])^7} + \\ & \frac{a b}{3 (a^2 - b^2)^2 d (a + b \sin[c + dx])^6} + \frac{b (3 a^2 + b^2)}{5 (a^2 - b^2)^3 d (a + b \sin[c + dx])^5} + \\ & \frac{a b (a^2 + b^2)}{(a^2 - b^2)^4 d (a + b \sin[c + dx])^4} + \frac{b (5 a^4 + 10 a^2 b^2 + b^4)}{3 (a^2 - b^2)^5 d (a + b \sin[c + dx])^3} + \\ & \frac{a b (3 a^2 + b^2) (a^2 + 3 b^2)}{(a^2 - b^2)^6 d (a + b \sin[c + dx])^2} + \frac{b (7 a^6 + 35 a^4 b^2 + 21 a^2 b^4 + b^6)}{(a^2 - b^2)^7 d (a + b \sin[c + dx])} \end{aligned}$$

Result (type 3, 847 leaves):

$$\begin{aligned}
& \frac{16 \operatorname{Im} \left( a^7 b + 7 a^5 b^3 + 7 a^3 b^5 + a b^7 \right) (c + d x)}{(a - b)^8 (a + b)^8 d} + \frac{1}{(a - b)^8 d} \\
& \pm \operatorname{ArcTan} \left[ \operatorname{Csc} [c + d x] \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right. \\
& \left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right] - \frac{1}{(a + b)^8 d} \operatorname{ArcTan} \left[ \operatorname{Csc} [c + d x] \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right] - \\
& \frac{\operatorname{Log} \left[ \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right]}{2 (a + b)^8 d} + \frac{\operatorname{Log} \left[ \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right]}{2 (a - b)^8 d} - \\
& \frac{8 (a^7 b + 7 a^5 b^3 + 7 a^3 b^5 + a b^7) \operatorname{Log} [a + b \sin [c + d x]]}{(a^2 - b^2)^8 d} + \\
& \frac{1}{3360 (a^2 - b^2)^7 d (a + b \sin [c + d x])^7} \\
& (46176 a^{12} b + 368176 a^{10} b^3 + 1198292 a^8 b^5 + 1066342 a^6 b^7 + 403302 a^4 b^9 + 20066 a^2 b^{11} + 2286 b^{13} - \\
& 249648 a^{10} b^3 \cos [2 (c + d x)] - 1190224 a^8 b^5 \cos [2 (c + d x)] - 1321089 a^6 b^7 \cos [2 (c + d x)] - \\
& 527429 a^4 b^9 \cos [2 (c + d x)] - 35539 a^2 b^{11} \cos [2 (c + d x)] - 2471 b^{13} \cos [2 (c + d x)] + \\
& 51100 a^8 b^5 \cos [4 (c + d x)] + 239610 a^6 b^7 \cos [4 (c + d x)] + 137690 a^4 b^9 \cos [4 (c + d x)] + \\
& 14350 a^2 b^{11} \cos [4 (c + d x)] + 770 b^{13} \cos [4 (c + d x)] - 735 a^6 b^7 \cos [6 (c + d x)] - \\
& 3675 a^4 b^9 \cos [6 (c + d x)] - 2205 a^2 b^{11} \cos [6 (c + d x)] - 105 b^{13} \cos [6 (c + d x)] + \\
& 229152 a^{11} b^2 \sin [c + d x] + 1230376 a^9 b^4 \sin [c + d x] + 2302916 a^7 b^6 \sin [c + d x] + \\
& 1297156 a^5 b^8 \sin [c + d x] + 255276 a^3 b^{10} \sin [c + d x] + 7364 a b^{12} \sin [c + d x] - \\
& 149240 a^9 b^4 \sin [3 (c + d x)] - 692370 a^7 b^6 \sin [3 (c + d x)] - 506170 a^5 b^8 \sin [3 (c + d x)] - \\
& 127190 a^3 b^{10} \sin [3 (c + d x)] - 3430 a b^{12} \sin [3 (c + d x)] + 9450 a^7 b^6 \sin [5 (c + d x)] + \\
& 45570 a^5 b^8 \sin [5 (c + d x)] + 24990 a^3 b^{10} \sin [5 (c + d x)] + 630 a b^{12} \sin [5 (c + d x)])
\end{aligned}$$

Problem 466: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec} [c + d x]^3}{(a + b \sin [c + d x])^8} d x$$

Optimal (type 3, 527 leaves, 4 steps):

$$\begin{aligned}
& - \frac{(a+9b) \operatorname{Log}[1 - \operatorname{Sin}[c + d x]]}{4 (a+b)^9 d} + \frac{(a-9b) \operatorname{Log}[1 + \operatorname{Sin}[c + d x]]}{4 (a-b)^9 d} + \\
& \frac{8 a b^3 (15 a^6 + 63 a^4 b^2 + 45 a^2 b^4 + 5 b^6) \operatorname{Log}[a + b \operatorname{Sin}[c + d x]]}{(a^2 - b^2)^9 d} - \\
& \frac{b (7 a^2 + 9 b^2)}{14 (a^2 - b^2)^2 d (a + b \operatorname{Sin}[c + d x])^7} - \frac{\operatorname{Sec}[c + d x]^2 (b - a \operatorname{Sin}[c + d x])}{2 (a^2 - b^2) d (a + b \operatorname{Sin}[c + d x])^7} - \\
& \frac{a b (3 a^2 + 13 b^2)}{6 (a^2 - b^2)^3 d (a + b \operatorname{Sin}[c + d x])^6} - \frac{b (5 a^4 + 50 a^2 b^2 + 9 b^4)}{10 (a^2 - b^2)^4 d (a + b \operatorname{Sin}[c + d x])^5} - \\
& \frac{a b (a^4 + 20 a^2 b^2 + 11 b^4)}{2 (a^2 - b^2)^5 d (a + b \operatorname{Sin}[c + d x])^4} - \frac{b (3 a^6 + 115 a^4 b^2 + 129 a^2 b^4 + 9 b^6)}{6 (a^2 - b^2)^6 d (a + b \operatorname{Sin}[c + d x])^3} - \\
& \frac{a b (a^6 + 77 a^4 b^2 + 147 a^2 b^4 + 31 b^6)}{2 (a^2 - b^2)^7 d (a + b \operatorname{Sin}[c + d x])^2} - \frac{b (a^8 + 196 a^6 b^2 + 574 a^4 b^4 + 244 a^2 b^6 + 9 b^8)}{2 (a^2 - b^2)^8 d (a + b \operatorname{Sin}[c + d x])}
\end{aligned}$$

Result (type 3, 1237 leaves):

$$\begin{aligned}
& - \frac{16 i (15 a^7 b^3 + 63 a^5 b^5 + 45 a^3 b^7 + 5 a b^9) (c + d x)}{(a - b)^9 (a + b)^9 d} + \frac{1}{2 (a - b)^9 d} \\
& i (a - 9 b) \operatorname{ArcTan}[\operatorname{Csc}[c + d x] \left( \cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)] \right) \\
& \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)] + \frac{1}{2 (a + b)^9 d} i (-a - 9 b) \operatorname{ArcTan}[ \\
& \operatorname{Csc}[c + d x] \left( \cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)] \right) \left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)] + \\
& \frac{(-a - 9 b) \log[\left( \cos[\frac{1}{2} (c + d x)] - \sin[\frac{1}{2} (c + d x)] \right)^2]}{4 (a + b)^9 d} + \\
& \frac{(a - 9 b) \log[\left( \cos[\frac{1}{2} (c + d x)] + \sin[\frac{1}{2} (c + d x)] \right)^2]}{4 (a - b)^9 d} + \\
& \frac{8 (15 a^7 b^3 + 63 a^5 b^5 + 45 a^3 b^7 + 5 a b^9) \log[a + b \sin[c + d x]]}{(a^2 - b^2)^9 d} + \\
& \frac{1}{26880 (a^2 - b^2)^8 d (a + b \sin[c + d x])^7} \\
& \sec[c + d x]^2 (-60480 a^{14} b - 2155120 a^{12} b^3 - 10531096 a^{10} b^5 - 18656885 a^8 b^7 - \\
& 11704100 a^6 b^9 - 2859110 a^4 b^{11} - 153820 a^2 b^{13} - 5469 b^{15} - 47040 a^{14} b \cos[2 (c + d x)] - \\
& 2190400 a^{12} b^3 \cos[2 (c + d x)] - 3544396 a^{10} b^5 \cos[2 (c + d x)] + \\
& 128224 a^8 b^7 \cos[2 (c + d x)] + 4162744 a^6 b^9 \cos[2 (c + d x)] + 1322704 a^4 b^{11} \cos[2 (c + d x)] + \\
& 171764 a^2 b^{13} \cos[2 (c + d x)] - 3600 b^{15} \cos[2 (c + d x)] + 58800 a^{12} b^3 \cos[4 (c + d x)] + \\
& 6695640 a^{10} b^5 \cos[4 (c + d x)] + 17845324 a^8 b^7 \cos[4 (c + d x)] + \\
& 11544064 a^6 b^9 \cos[4 (c + d x)] + 2887864 a^4 b^{11} \cos[4 (c + d x)] + \\
& 96264 a^2 b^{13} \cos[4 (c + d x)] + 9324 b^{15} \cos[4 (c + d x)] - 8820 a^{10} b^5 \cos[6 (c + d x)] - \\
& 1410080 a^8 b^7 \cos[6 (c + d x)] - 3831800 a^6 b^9 \cos[6 (c + d x)] - \\
& 1515920 a^4 b^{11} \cos[6 (c + d x)] - 109620 a^2 b^{13} \cos[6 (c + d x)] - 5040 b^{15} \cos[6 (c + d x)] + \\
& 105 a^8 b^7 \cos[8 (c + d x)] + 20580 a^6 b^9 \cos[8 (c + d x)] + 60270 a^4 b^{11} \cos[8 (c + d x)] + \\
& 25620 a^2 b^{13} \cos[8 (c + d x)] + 945 b^{15} \cos[8 (c + d x)] + 13440 a^{15} \sin[c + d x] - \\
& 164640 a^{13} b^2 \sin[c + d x] - 5702480 a^{11} b^4 \sin[c + d x] - 20202406 a^9 b^6 \sin[c + d x] - \\
& 24081736 a^7 b^8 \sin[c + d x] - 9935716 a^5 b^{10} \sin[c + d x] - 1391096 a^3 b^{12} \sin[c + d x] - \\
& 36806 a b^{14} \sin[c + d x] - 70560 a^{13} b^2 \sin[3 (c + d x)] - 5955320 a^{11} b^4 \sin[3 (c + d x)] - \\
& 15658566 a^9 b^6 \sin[3 (c + d x)] - 13417656 a^7 b^8 \sin[3 (c + d x)] - \\
& 3705156 a^5 b^{10} \sin[3 (c + d x)] - 326816 a^3 b^{12} \sin[3 (c + d x)] - 3206 a b^{14} \sin[3 (c + d x)] + \\
& 29400 a^{11} b^4 \sin[5 (c + d x)] + 4071970 a^9 b^6 \sin[5 (c + d x)] + 10871560 a^7 b^8 \sin[5 (c + d x)] + \\
& 5210380 a^5 b^{10} \sin[5 (c + d x)] + 875280 a^3 b^{12} \sin[5 (c + d x)] + \\
& 15330 a b^{14} \sin[5 (c + d x)] - 1470 a^9 b^6 \sin[7 (c + d x)] - 262920 a^7 b^8 \sin[7 (c + d x)] - \\
& 737940 a^5 b^{10} \sin[7 (c + d x)] - 283080 a^3 b^{12} \sin[7 (c + d x)] - 4830 a b^{14} \sin[7 (c + d x)])
\end{aligned}$$

Problem 495: Result more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^3 (a + b \sin[c + d x])^{5/2} \, dx$$

Optimal (type 3, 83 leaves, 3 steps):

$$-\frac{2 (a^2 - b^2) (a + b \sin[c + d x])^{7/2}}{7 b^3 d} + \frac{4 a (a + b \sin[c + d x])^{9/2}}{9 b^3 d} - \frac{2 (a + b \sin[c + d x])^{11/2}}{11 b^3 d}$$

Result (type 3, 198 leaves):

$$\left( -2 a^2 (64 a^4 - 780 a^2 b^2 - 705 b^4) \sqrt{1 + \frac{b \sin[c + d x]}{a}} \left( -1 + \sqrt{1 + \frac{b \sin[c + d x]}{a}} \right) + b (a + b \sin[c + d x]) (8 a b (3 a^2 - 136 b^2) \cos[2 (c + d x)] - 322 a b^3 \cos[4 (c + d x)] + 2 (32 a^4 + 1698 a^2 b^2 + 279 b^4) \sin[c + d x] + b^2 (452 a^2 - 81 b^2) \sin[3 (c + d x)] - 63 b^4 \sin[5 (c + d x)]) \right) / (5544 b^3 d \sqrt{a + b \sin[c + d x]})$$

Problem 497: Result more than twice size of optimal antiderivative.

$$\int \sec[c + d x] (a + b \sin[c + d x])^{5/2} \, dx$$

Optimal (type 3, 117 leaves, 7 steps):

$$-\frac{(a - b)^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \sin[c+d x]}}{\sqrt{a-b}}\right]}{d} + \frac{(a + b)^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \sin[c+d x]}}{\sqrt{a+b}}\right]}{d} - \frac{4 a b \sqrt{a + b \sin[c + d x]}}{d} - \frac{2 b (a + b \sin[c + d x])^{3/2}}{3 d}$$

Result (type 3, 286 leaves):

$$\begin{aligned} & \frac{1}{6 d} \left( -\frac{(6 a^3 - 18 a^2 b + 11 a b^2 - 6 b^3) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \sin[c+d x]}}{\sqrt{a-b}}\right]}{\sqrt{a-b}} + \right. \\ & \left( \sqrt{-a-b} \sqrt{-a+b} (6 a^3 + 18 a^2 b + 11 a b^2 + 6 b^3) \operatorname{ArcTanh}\left[\frac{\sqrt{a+b \sin[c+d x]}}{\sqrt{a+b}}\right] - \right. \\ & b \left( 7 a b \sqrt{-a+b} \sqrt{a+b} \operatorname{ArcTan}\left[\frac{\sqrt{a+b \sin[c+d x]}}{\sqrt{-a-b}}\right] + \right. \\ & \left. \sqrt{-(a+b)^2} \left( -7 a b \operatorname{ArcTan}\left[\frac{\sqrt{a+b \sin[c+d x]}}{\sqrt{-a+b}}\right] + 4 \sqrt{-a+b} \right. \right. \\ & \left. \left. \sqrt{a+b \sin[c+d x]} (7 a + b \sin[c+d x]) \right) \right) \Bigg) / \left( \sqrt{-a+b} \sqrt{-(a+b)^2} \right) \end{aligned}$$

Problem 574: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + dx])^{11/2}}{a + b \sin[c + dx]} dx$$

Optimal (type 4, 531 leaves, 15 steps):

$$\begin{aligned} & - \frac{(-a^2 + b^2)^{9/4} e^{11/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c + dx]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{11/2} d} - \frac{(-a^2 + b^2)^{9/4} e^{11/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c + dx]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{11/2} d} + \\ & \frac{2 e (e \cos[c + dx])^{9/2}}{9 b d} + \left(2 a (21 a^4 - 49 a^2 b^2 + 33 b^4) e^6 \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2} (c + dx), 2\right]\right) / \\ & \left(21 b^6 d \sqrt{e \cos[c + dx]}\right) - \frac{a (a^2 - b^2)^3 e^6 \sqrt{\cos[c + dx]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + dx), 2\right]}{b^6 (a^2 - b (b - \sqrt{-a^2 + b^2})) d \sqrt{e \cos[c + dx]}} - \\ & \frac{a (a^2 - b^2)^3 e^6 \sqrt{\cos[c + dx]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + dx), 2\right]}{b^6 (a^2 - b (b + \sqrt{-a^2 + b^2})) d \sqrt{e \cos[c + dx]}} - \\ & \frac{2 e^3 (e \cos[c + dx])^{5/2} (7 (a^2 - b^2) - 5 a b \sin[c + dx])}{35 b^3 d} + \\ & \frac{2 e^5 \sqrt{e \cos[c + dx]} (21 (a^2 - b^2)^2 - a b (7 a^2 - 12 b^2) \sin[c + dx])}{21 b^5 d} \end{aligned}$$

Result (type 6, 2235 leaves):

$$\begin{aligned} & \frac{1}{1680 b^4 d \cos[c + dx]^{11/2}} \\ & (e \cos[c + dx])^{11/2} \left( - \frac{1}{\sqrt{1 - \cos[c + dx]^2} (a + b \sin[c + dx])} 2 (280 a^4 - 636 a^2 b^2 + 721 b^4) \right. \\ & \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \left( 5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \\ & \left. \left. \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \sqrt{\cos[c + dx]} \right) / \left( \sqrt{1 - \cos[c + dx]^2} \right. \\ & \left. \left( 5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - 2 \right. \right. \\ & \left. \left( 2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right. \\ & \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) \\ & \left( a^2 + b^2 (-1 + \cos[c + dx]^2) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \end{aligned}$$

$$\begin{aligned}
& \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \right. \\
& \left. \operatorname{Log} \left[ \sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] - \right. \\
& \left. \operatorname{Log} \left[ \sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] \right) \\
& \frac{1}{\sin[c+d x] + \frac{1}{\sqrt{1 - \cos[c+d x]^2} (-1 + 2 \cos[c+d x]^2) (a + b \sin[c+d x])}} \\
& \left( 840 a^4 - 1764 a^2 b^2 + 959 b^4 \right) \left( a + b \sqrt{1 - \cos[c+d x]^2} \right) \\
& \cos[2(c+d x)] \\
& \left( \frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \\
& b^{3/2} (-a^2+b^2)^{3/4} \\
& \left( \frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \frac{4 \sqrt{\cos[c+d x]}}{b} + \\
& \left( 10 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos[c+d x]} \right) / \\
& \left( \sqrt{1 - \cos[c+d x]^2} \left( 5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) (a^2 + b^2 (-1 + \cos[c+d x]^2)) \right) - \\
& \left( 36 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right. \\
& \left. \cos[c+d x]^{5/2} \right) / \left( 5 \sqrt{1 - \cos[c+d x]^2} \right. \\
& \left. \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \\
& \left. \left. \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) \\
& \left( a^2 + b^2 (-1 + \cos[c+d x]^2) \right) + \left( \left( \frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[ \sqrt{-a^2+b^2} - \right. \right. \\
& \left. \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] \right) / \left( b^{3/2} (-a^2+b^2)^{3/4} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( \left( \frac{1}{4} - \frac{\frac{1}{4}}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + \left( 1 + \frac{1}{4} \right) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} \right] + \right. \\
& \left. \left. \frac{1}{4} b \cos[c + d x] \right) \right/ \left( b^{3/2} (-a^2 + b^2)^{3/4} \right) \sin[c + d x] - \right. \\
& \left. \frac{1}{(1 - \cos[c + d x]^2) (a + b \sin[c + d x])^2} \left( -392 a^3 b + 722 a b^3 \right) \right. \\
& \left. \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \right. \\
& \left. \left( 5 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + d x]} \sqrt{1 - \cos[c + d x]^2} \right) \right/ \\
& \left. \left( -5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \right) + \\
& \left. \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \right. \\
& \left. \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] + \right. \right. \right. \\
& \left. \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \right) \right/ \\
& \left. \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + d x]^2 \right) + \frac{1}{d} \\
& (e \cos[c + d x])^{11/2} \sec[c + d x]^5 \left( \frac{(-9 a^2 + 14 b^2) \cos[2 (c + d x)]}{45 b^3} + \right. \\
& \left. \frac{\cos[4 (c + d x)]}{36 b} - \right. \\
& \left. \frac{a (28 a^2 - 51 b^2) \sin[c + d x]}{42 b^4} + \right. \\
& \left. \frac{a \sin[3 (c + d x)]}{14 b^2} \right)
\end{aligned}$$

Problem 575: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^{9/2}}{a + b \sin[c + d x]} dx$$

Optimal (type 4, 446 leaves, 14 steps):

$$\begin{aligned} & \frac{(-a^2 + b^2)^{7/4} e^{9/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{9/2} d} - \frac{(-a^2 + b^2)^{7/4} e^{9/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{9/2} d} + \\ & \frac{2 e (e \cos[c + d x])^{7/2}}{7 b d} - \frac{2 a (5 a^2 - 8 b^2) e^4 \sqrt{e \cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 b^4 d \sqrt{\cos[c + d x]}} + \\ & \frac{a (a^2 - b^2)^2 e^5 \sqrt{\cos[c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{b^5 (b - \sqrt{-a^2 + b^2}) d \sqrt{e \cos[c + d x]}} + \\ & \frac{a (a^2 - b^2)^2 e^5 \sqrt{\cos[c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{b^5 (b + \sqrt{-a^2 + b^2}) d \sqrt{e \cos[c + d x]}} - \\ & \frac{2 e^3 (e \cos[c + d x])^{3/2} (5 (a^2 - b^2) - 3 a b \sin[c + d x])}{15 b^3 d} \end{aligned}$$

Result (type 6, 1228 leaves):

$$\begin{aligned} & -\frac{1}{5 b^3 d \cos[c + d x]^{9/2}} (e \cos[c + d x])^{9/2} \\ & \left( \frac{1}{12 \sqrt{1 - \cos[c + d x]^2} (a + b \sin[c + d x])} (2 a^2 b - 5 b^3) \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \right. \\ & \left( - \left( \left( 56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \right. \right. \right. \right. \\ & \left. \left. \left. \left. \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \cos[c + d x]^{3/2} \right) \right. \left. \left( \sqrt{1 - \cos[c + d x]^2} \right. \right. \\ & \left. \left. \left( 7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] - \right. \right. \\ & \left. \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\ & \left. \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\ & \left. \left. \left. \cos[c + d x]^2 \right) \left( a^2 + b^2 (-1 + \cos[c + d x]^2) \right) \right) \right) - \end{aligned}$$

$$\begin{aligned}
& \left( (3 + 3 \text{i}) \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \operatorname{Log} \left[ \sqrt{-a^2 + b^2} - (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] + \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] \right] \right) \Big/ \left( \sqrt{b} (-a^2 + b^2)^{1/4} \right) \sin[c + d x] - \\
& \frac{1}{(1 - \cos[c + d x]^2) (a + b \sin[c + d x])} 2 (5 a^3 - 8 a b^2) \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \\
& \left( 7 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right. \right. \\
& \left. \left. \cos[c + d x]^{3/2} \sqrt{1 - \cos[c + d x]^2} \right] \Big/ \\
& \left( 3 \left( -7 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + 2 \right. \right. \\
& \left. \left. \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \Big) + \\
& \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] - \operatorname{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \right) \Big/ \\
& \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[c + d x]^2 + \frac{1}{d} \\
& (e \cos[c + d x])^{9/2} \sec[c + d x]^4 \left( \frac{(-28 a^2 + 37 b^2) \cos[c + d x]}{42 b^3} + \right. \\
& \left. \frac{\cos[3(c + d x)]}{14 b} + \right. \\
& \left. \left. \frac{a \sin[2(c + d x)]}{5 b^2} \right) \right)
\end{aligned}$$

Problem 576: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(\cos(c+dx))^7}{a+b \sin(c+dx)} \, dx$$

Optimal (type 4, 461 leaves, 14 steps):

$$\begin{aligned} & - \frac{(-a^2 + b^2)^{5/4} e^{7/2} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\cos(c+dx)}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{b^{7/2} d} - \frac{(-a^2 + b^2)^{5/4} e^{7/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\cos(c+dx)}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{b^{7/2} d} + \\ & \frac{2 e (\cos(c+dx))^{5/2}}{5 b d} - \frac{2 a (3 a^2 - 4 b^2) e^4 \sqrt{\cos(c+dx)} \operatorname{EllipticF} \left[ \frac{1}{2} (c+dx), 2 \right]}{3 b^4 d \sqrt{e \cos(c+dx)}} + \\ & \frac{a (a^2 - b^2)^2 e^4 \sqrt{\cos(c+dx)} \operatorname{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+dx), 2 \right]}{b^4 (a^2 - b (b - \sqrt{-a^2 + b^2})) d \sqrt{e \cos(c+dx)}} + \\ & \frac{a (a^2 - b^2)^2 e^4 \sqrt{\cos(c+dx)} \operatorname{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+dx), 2 \right]}{b^4 (a^2 - b (b + \sqrt{-a^2 + b^2})) d \sqrt{e \cos(c+dx)}} - \\ & \frac{2 e^3 \sqrt{e \cos(c+dx)} (3 (a^2 - b^2) - a b \sin(c+dx))}{3 b^3 d} \end{aligned}$$

Result (type 6, 2155 leaves):

$$\begin{aligned} & \frac{(\cos(c+dx))^{7/2} \operatorname{Sec}(c+dx)^3 \left( \frac{\cos(2(c+dx))}{5b} + \frac{2a \sin(c+dx)}{3b^2} \right)}{d} - \\ & \frac{1}{60 b^2 d \cos(c+dx)^{7/2}} (\cos(c+dx))^{7/2} \\ & \left( - \frac{1}{\sqrt{1 - \cos(c+dx)^2} (a + b \sin(c+dx))} 2 (10 a^2 - 27 b^2) \left( a + b \sqrt{1 - \cos(c+dx)^2} \right) \right. \\ & \left( \left( 5 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos(c+dx)^2, \frac{b^2 \cos(c+dx)^2}{-a^2 + b^2} \right] \sqrt{\cos(c+dx)} \right) \right. \\ & \left. \left( 5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos(c+dx)^2, \frac{b^2 \cos(c+dx)^2}{-a^2 + b^2} \right] - 2 \right. \\ & \left. \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos(c+dx)^2, \frac{b^2 \cos(c+dx)^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \\ & \left. \left. \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos(c+dx)^2, \frac{b^2 \cos(c+dx)^2}{-a^2 + b^2} \right] \right) \cos(c+dx)^2 \right) \\ & \left( a^2 + b^2 (-1 + \cos(c+dx)^2) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \end{aligned}$$

$$\begin{aligned}
& \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \right. \\
& \left. \operatorname{Log} \left[ \sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] - \right. \\
& \left. \operatorname{Log} \left[ \sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] \right) \\
& \frac{1}{\sin[c+d x] + \frac{\sqrt{1-\cos[c+d x]^2} (-1+2 \cos[c+d x]^2) (a+b \sin[c+d x])}{(30 a^2 - 33 b^2) \left( a + b \sqrt{1-\cos[c+d x]^2} \right) \cos[2 (c+d x)]}} - \\
& \frac{\left( \frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2+b^2)^{3/4}} - \\
& \frac{\left( \frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2+b^2)^{3/4}} + \frac{4 \sqrt{\cos[c+d x]}}{b} + \\
& \left( 10 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos[c+d x]} \right) / \\
& \left( \sqrt{1-\cos[c+d x]^2} \left( 5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) (a^2 + b^2 (-1 + \cos[c+d x]^2)) \right) - \\
& \left( 36 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right. \\
& \left. \cos[c+d x]^{5/2} \right) / \left( 5 \sqrt{1-\cos[c+d x]^2} \right. \\
& \left. \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \\
& \left. \left. \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) \\
& \left. (a^2 + b^2 (-1 + \cos[c+d x]^2)) \right) + \left( \left( \frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[ \sqrt{-a^2+b^2} - \right. \right. \\
& \left. \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] \right) / \left( b^{3/2} (-a^2+b^2)^{3/4} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \left( \frac{1}{4} - \frac{\frac{1}{2}}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + \left( 1 + \frac{1}{2} \right) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} \right] + \right. \right. \\
& \left. \left. \frac{\frac{1}{2} b \cos[c + d x]}{\left( b^{3/2} (-a^2 + b^2)^{3/4} \right)} \right) \operatorname{Sin}[c + d x] + \right. \\
& \left. \frac{1}{(1 - \cos[c + d x]^2) (a + b \sin[c + d x])} 28 a b \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \right. \\
& \left. \left( 5 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + d x]} \sqrt{1 - \cos[c + d x]^2} \right) \right. \\
& \left. \left( \left( -5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \right. \\
& \left. \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \right) + \\
& \left. \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \right. \\
& \left. \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] + \right. \right. \right. \\
& \left. \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \right) \right. \\
& \left. \left. \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \operatorname{Sin}[c + d x]^2 \right) \right)
\end{aligned}$$

Problem 577: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^{5/2}}{a + b \sin[c + d x]} dx$$

Optimal (type 4, 384 leaves, 13 steps):

$$\begin{aligned}
& \frac{\left(-a^2 + b^2\right)^{3/4} e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{b^{5/2} d} - \frac{\left(-a^2 + b^2\right)^{3/4} e^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{b^{5/2} d} + \\
& \frac{2 e \left(e \cos[c+d x]\right)^{3/2}}{3 b d} + \frac{2 a e^2 \sqrt{e \cos[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{b^2 d \sqrt{\cos[c+d x]}} - \\
& \frac{a \left(a^2 - b^2\right) e^3 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{b^3 \left(b - \sqrt{-a^2+b^2}\right) d \sqrt{e \cos[c+d x]}} - \\
& \frac{a \left(a^2 - b^2\right) e^3 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{b^3 \left(b + \sqrt{-a^2+b^2}\right) d \sqrt{e \cos[c+d x]}}
\end{aligned}$$

Result (type 6, 1151 leaves):

$$\begin{aligned}
& \frac{2 \left(e \cos[c+d x]\right)^{5/2} \operatorname{Sec}[c+d x]}{3 b d} + \frac{1}{b d \cos[c+d x]^{5/2}} \\
& \left(e \cos[c+d x]\right)^{5/2} \left( \frac{1}{12 \sqrt{1 - \cos[c+d x]^2} (a + b \sin[c+d x])} - b \left(a + b \sqrt{1 - \cos[c+d x]^2}\right) \right. \\
& \left. - \left( \left( 56 a \left(a^2 - b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] \cos[c+d x]^{3/2} \right) \right. \\
& \left. \left( \sqrt{1 - \cos[c+d x]^2} \left( 7 \left(a^2 - b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] - 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] + \left(-a^2 + b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] \right) \cos[c+d x]^2 \right) \left( a^2 + b^2 (-1 + \cos[c+d x]^2) \right) \right) \\
& \left( (3 + 3 \text{i}) \left( 2 \operatorname{ArcTan}\left[1 - \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1 + \text{i}) \sqrt{b} (-a^2+b^2)^{1/4}\right] \right. \\
& \left. + \sqrt{\cos[c+d x]} + \text{i} b \cos[c+d x]\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1 + \text{i}) \sqrt{b} (-a^2+b^2)^{1/4}\right] \right. \\
& \left. + \sqrt{\cos[c+d x]} + \text{i} b \cos[c+d x]\right) \right) \left( \sqrt{b} (-a^2+b^2)^{1/4} \right) \sin[c+d x] - \\
& \frac{1}{(1 - \cos[c+d x]^2) (a + b \sin[c+d x])} 2 a \left(a + b \sqrt{1 - \cos[c+d x]^2}\right) \\
& \left( 7 b \left(a^2 - b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \cos[(c+dx)^{3/2} \sqrt{1 - \cos[(c+dx)^2]} \right) \right/ \\
& \left( 3 \left( -7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2 + b^2} \right] + \right. \right. \\
& \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2 + b^2} \right] \right) \right) \\
& \left. \left( \cos[(c+dx)^2] (a^2 + b^2 (-1 + \cos[(c+dx)^2])) \right) \right. \\
& \left. \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[(c+dx)]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[(c+dx)]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \right. \\
& \left. \left. \left. \text{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[(c+dx)]} + b \cos[(c+dx)] \right] - \right. \right. \right. \\
& \left. \left. \left. \text{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[(c+dx)]} + b \cos[(c+dx)] \right] \right) \right) \right/ \\
& \left. \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[(c+dx)^2] \right)
\end{aligned}$$

Problem 578: Result unnecessarily involves higher level functions.

$$\int \frac{(e \cos[(c+dx)]^{3/2})}{a + b \sin[(c+dx)]} dx$$

Optimal (type 4, 397 leaves, 13 steps):

$$\begin{aligned}
& - \frac{(-a^2 + b^2)^{1/4} e^{3/2} \text{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos[(c+dx)]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{b^{3/2} d} - \frac{(-a^2 + b^2)^{1/4} e^{3/2} \text{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos[(c+dx)]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{b^{3/2} d} + \\
& \frac{2 e \sqrt{e \cos[(c+dx)]}}{b d} + \frac{2 a e^2 \sqrt{\cos[(c+dx)]} \text{EllipticF} \left[ \frac{1}{2} (c+dx), 2 \right]}{b^2 d \sqrt{e \cos[(c+dx)]}} - \\
& \frac{a (a^2 - b^2) e^2 \sqrt{\cos[(c+dx)]} \text{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+dx), 2 \right]}{b^2 (a^2 - b (b - \sqrt{-a^2 + b^2})) d \sqrt{e \cos[(c+dx)]}} - \\
& \frac{a (a^2 - b^2) e^2 \sqrt{\cos[(c+dx)]} \text{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+dx), 2 \right]}{b^2 (a^2 - b (b + \sqrt{-a^2 + b^2})) d \sqrt{e \cos[(c+dx)]}}
\end{aligned}$$

Result (type 6, 624 leaves):

$$\begin{aligned}
& \frac{1}{20 d \cos[c + d x]^{3/2} \sqrt{1 - \cos[c + d x]^2} (a + b \sin[c + d x])} \\
& (e \cos[c + d x])^{3/2} \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \\
& \left( - \left( \left( 72 a (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \cos[c + d x]^{5/2} \right) \right. \right. \\
& \left( \sqrt{1 - \cos[c + d x]^2} \left( 9 (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] - \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (-a^2 + b^2) \text{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \right) + \\
& \frac{1}{b^{3/2}} (5 - 5 \text{i}) \left( 2 (-a^2 + b^2)^{1/4} \text{ArcTan} \left[ 1 - \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 (-a^2 + b^2)^{1/4} \right. \\
& \left. \text{ArcTan} \left[ 1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + (4 + 4 \text{i}) \sqrt{b} \sqrt{\cos[c + d x]} + (-a^2 + b^2)^{1/4} \right. \\
& \left. \text{Log} \left[ \sqrt{-a^2 + b^2} - (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] - (-a^2 + b^2)^{1/4} \right. \\
& \left. \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] \right) \sin[c + d x]
\end{aligned}$$

Problem 579: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{e \cos[c + d x]}}{a + b \sin[c + d x]} \, dx$$

Optimal (type 4, 292 leaves, 9 steps):

$$\begin{aligned}
& \frac{\sqrt{e} \text{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right] - \sqrt{e} \text{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{\sqrt{b} (-a^2 + b^2)^{1/4} d} + \\
& \frac{a e \sqrt{\cos[c + d x]} \text{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{b (b - \sqrt{-a^2 + b^2}) d \sqrt{e \cos[c + d x]}} + \\
& \frac{a e \sqrt{\cos[c + d x]} \text{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{b (b + \sqrt{-a^2 + b^2}) d \sqrt{e \cos[c + d x]}}
\end{aligned}$$

Result (type 6, 565 leaves):

$$\begin{aligned}
& \frac{1}{12 d \sqrt{\cos[c + d x]} \sqrt{1 - \cos[c + d x]^2} (a + b \sin[c + d x])} \\
& \sqrt{e \cos[c + d x]} \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \\
& \left( - \left( \left( 56 a (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \cos[c + d x]^{3/2} \right) \right. \right. \\
& \left( \sqrt{1 - \cos[c + d x]^2} \left( 7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] - \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (-a^2 + b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \cos[c + d x]^2 \right) \\
& \left. \left( a^2 + b^2 (-1 + \cos[c + d x]^2) \right) \right) - \left( (3 + 3 \text{i}) \left( 2 \text{ArcTan} \left[ 1 - \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \right. \right. \\
& \left. \left. 2 \text{ArcTan} \left[ 1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \right. \right. \\
& \left. \left. \text{Log} \left[ \sqrt{-a^2 + b^2} - (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] + \right. \right. \\
& \left. \left. \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] \right) \right) \\
& \left. \left( \sqrt{b} (-a^2 + b^2)^{1/4} \right) \sin[c + d x] \right)
\end{aligned}$$

Problem 580: Result unnecessarily involves higher level functions.

$$\int \frac{1}{\sqrt{e \cos[c + d x]} (a + b \sin[c + d x])} \, dx$$

Optimal (type 4, 299 leaves, 9 steps):

$$\begin{aligned}
& - \frac{\sqrt{b} \text{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{(-a^2 + b^2)^{3/4} d \sqrt{e}} - \frac{\sqrt{b} \text{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{(-a^2 + b^2)^{3/4} d \sqrt{e}} + \\
& \frac{a \sqrt{\cos[c + d x]} \text{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{\left( a^2 - b \left( b - \sqrt{-a^2 + b^2} \right) \right) d \sqrt{e \cos[c + d x]}} + \\
& \frac{a \sqrt{\cos[c + d x]} \text{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{\left( a^2 - b \left( b + \sqrt{-a^2 + b^2} \right) \right) d \sqrt{e \cos[c + d x]}}
\end{aligned}$$

Result (type 6, 567 leaves):

$$\begin{aligned}
& - \frac{1}{d \sqrt{e \cos[c + d x]} \sqrt{1 - \cos[c + d x]^2} (a + b \sin[c + d x])} \\
& \frac{2 \sqrt{\cos[c + d x]} \left( a + b \sqrt{1 - \cos[c + d x]^2} \right)}{\left( 5 a (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] \sqrt{\cos[c + d x]} \right) /} \\
& \left( \sqrt{1 - \cos[c + d x]^2} \left( 5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] - \right. \right. \\
& 2 \left( 2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] + \right. \\
& \left. \left. \left. (-a^2 + b^2) \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] \right) \cos[c + d x]^2 \right) \\
& \left( a^2 + b^2 (-1 + \cos[c + d x]^2) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
& \left( 2 \text{ArcTan}\left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \text{ArcTan}\left[1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}}\right] + \right. \\
& \left. \left. \left. \text{Log}\left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + i b \cos[c + d x]\right] - \right. \right. \right. \\
& \left. \left. \left. \text{Log}\left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + i b \cos[c + d x]\right]\right) \right) \sin[c + d x]
\end{aligned}$$

Problem 581: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos[c + d x])^{3/2} (a + b \sin[c + d x])} dx$$

Optimal (type 4, 411 leaves, 13 steps):

$$\begin{aligned}
& \frac{b^{3/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right] - b^{3/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{(-a^2 + b^2)^{5/4} d e^{3/2}} - \\
& \frac{2 a \sqrt{e \cos[c + d x]} \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{(a^2 - b^2) d e^2 \sqrt{\cos[c + d x]}} - \\
& \frac{a b \sqrt{\cos[c + d x]} \text{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{(a^2 - b^2) (b - \sqrt{-a^2 + b^2}) d e \sqrt{e \cos[c + d x]}} - \\
& \frac{a b \sqrt{\cos[c + d x]} \text{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{(a^2 - b^2) (b + \sqrt{-a^2 + b^2}) d e \sqrt{e \cos[c + d x]}} - \frac{2 (b - a \sin[c + d x])}{(a^2 - b^2) d e \sqrt{e \cos[c + d x]}}
\end{aligned}$$

Result (type 6, 1186 leaves):

$$\begin{aligned}
& \frac{2 \cos(c + dx) (-b + a \sin(c + dx))}{(a^2 - b^2) d (\epsilon \cos(c + dx))^{3/2}} - \frac{1}{(a - b) (a + b) d (\epsilon \cos(c + dx))^{3/2}} \\
& \cos(c + dx)^{3/2} \left( \frac{1}{12 \sqrt{1 - \cos(c + dx)^2} (a + b \sin(c + dx))} (a^2 + b^2) \left( a + b \sqrt{1 - \cos(c + dx)^2} \right) \right. \\
& \left. - \left( \left( 56 a (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos(c + dx)^2, \frac{b^2 \cos(c + dx)^2}{-a^2 + b^2} \right] \cos(c + dx)^{3/2} \right) \right. \right. \\
& \left( \sqrt{1 - \cos(c + dx)^2} \left( 7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos(c + dx)^2, \right. \right. \right. \\
& \left. \left. \frac{b^2 \cos(c + dx)^2}{-a^2 + b^2} \right] - 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos(c + dx)^2, \right. \right. \\
& \left. \left. \frac{b^2 \cos(c + dx)^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos(c + dx)^2, \right. \right. \\
& \left. \left. \frac{b^2 \cos(c + dx)^2}{-a^2 + b^2} \right] \right) \cos(c + dx)^2 \right) \left( a^2 + b^2 (-1 + \cos(c + dx)^2) \right) \right) - \\
& \left( (3 + 3 i) \left( 2 \text{ArcTan} \left[ 1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos(c + dx)}}{(-a^2 + b^2)^{1/4}} \right] - 2 \text{ArcTan} \left[ \right. \right. \right. \\
& \left. \left. \left. 1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos(c + dx)}}{(-a^2 + b^2)^{1/4}} \right] - \text{Log} \left[ \sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
& \left. \left. \sqrt{\cos(c + dx)} + i b \cos(c + dx) \right] + \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
& \left. \left. \sqrt{\cos(c + dx)} + i b \cos(c + dx) \right] \right) \right) \left/ \left( \sqrt{b} (-a^2 + b^2)^{1/4} \right) \right. \sin(c + dx) - \\
& \frac{1}{(1 - \cos(c + dx)^2) (a + b \sin(c + dx))} 2 a b \left( a + b \sqrt{1 - \cos(c + dx)^2} \right) \\
& \left( \left( 7 b (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos(c + dx)^2, \frac{b^2 \cos(c + dx)^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \cos(c + dx)^{3/2} \sqrt{1 - \cos(c + dx)^2} \right) \right/ \\
& \left( 3 \left( -7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos(c + dx)^2, \frac{b^2 \cos(c + dx)^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. + 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos(c + dx)^2, \frac{b^2 \cos(c + dx)^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. + (a^2 - b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos(c + dx)^2, \frac{b^2 \cos(c + dx)^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos(c + dx)^2 \right) \left( a^2 + b^2 (-1 + \cos(c + dx)^2) \right) \right) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos(c + dx)}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos(c + dx)}}{(a^2 - b^2)^{1/4}} \right] \right. \right. \\
& \left. \left. + \right. \right)
\end{aligned}$$

$$\left. \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin [c + d x]^2 \right) \left. \left( \begin{aligned} & \log \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] - \\ & \log \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \end{aligned} \right) \right) /$$

Problem 582: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos [c + d x])^{5/2} (a + b \sin [c + d x])} dx$$

Optimal (type 4, 434 leaves, 13 steps):

$$\begin{aligned}
& -\frac{b^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{\left(-a^2+b^2\right)^{7/4} d e^{5/2}}-\frac{b^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{\left(-a^2+b^2\right)^{7/4} d e^{5/2}}+ \\
& \frac{2 a \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{3 \left(a^2-b^2\right) d e^2 \sqrt{e \cos [c+d x]}}- \\
& a b^2 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]- \\
& \left(a^2-b^2\right) \left(a^2-b \left(b-\sqrt{-a^2+b^2}\right)\right) d e^2 \sqrt{e \cos [c+d x]}- \\
& a b^2 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]-\frac{2 \left(b-a \sin [c+d x]\right)}{3 \left(a^2-b^2\right) d e \left(e \cos [c+d x]\right)^{3/2}}
\end{aligned}$$

Result (type 6, 1192 leaves):

$$\begin{aligned}
 & \frac{2 \cos[c + dx] (-b + a \sin[c + dx])}{3 (a^2 - b^2) d (\epsilon \cos[c + dx])^{5/2}} + \\
 & \frac{1}{3 (a - b) (a + b) d (\epsilon \cos[c + dx])^{5/2}} \cos[c + dx]^{5/2} \left( -\frac{1}{\sqrt{1 - \cos[c + dx]^2}} \frac{1}{(a + b \sin[c + dx])} \right. \\
 & 2 (a^2 - 3 b^2) \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \left( 5 a (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \\
 & \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \left. \right] \sqrt{\cos[c + dx]} \left. \right) \left/ \left( \sqrt{1 - \cos[c + dx]^2} \right. \right. \\
 & \left. \left( 5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - 2 \right. \right. \\
 & \left. \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right)
 \end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] \cos[c + dx]^2 \\
& \left( a^2 + b^2 (-1 + \cos[c + dx]^2) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
& \left( 2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}}\right] + \right. \\
& \left. \log\left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + i b \cos[c + dx]\right] - \right. \\
& \left. \log\left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + i b \cos[c + dx]\right] \right) \\
& \sin[c + dx] - \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 2 a b \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( 5 b (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] \right. \\
& \left. \sqrt{\cos[c + dx]} \sqrt{1 - \cos[c + dx]^2} \right) / \\
& \left( \left( -5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] \right) \right. \\
& \left. \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \\
& \left( a \left( -2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}}\right] - \right. \right. \\
& \left. \left. \log\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx]\right] + \right. \right. \\
& \left. \left. \log\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx]\right] \right) \right) / \\
& \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + dx]^2
\end{aligned}$$

Problem 583: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos[c + dx])^{7/2} (a + b \sin[c + dx])} dx$$

Optimal (type 4, 486 leaves, 14 steps):

$$\begin{aligned}
& \frac{b^{7/2} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{(-a^2+b^2)^{9/4} d e^{7/2}} - \frac{b^{7/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{(-a^2+b^2)^{9/4} d e^{7/2}} - \\
& \frac{2 a (3 a^2 - 8 b^2) \sqrt{e \cos[c+d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c+d x), 2 \right]}{5 (a^2 - b^2)^2 d e^4 \sqrt{\cos[c+d x]}} + \\
& a b^3 \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right] \\
& + (a^2 - b^2)^2 \left( b - \sqrt{-a^2+b^2} \right) d e^3 \sqrt{e \cos[c+d x]} \\
& \frac{a b^3 \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{(a^2 - b^2)^2 \left( b + \sqrt{-a^2+b^2} \right) d e^3 \sqrt{e \cos[c+d x]}} - \\
& \frac{2 (b - a \sin[c+d x])}{5 (a^2 - b^2) d e (\sin[c+d x])^{5/2}} + \frac{2 (5 b^3 + a (3 a^2 - 8 b^2) \sin[c+d x])}{5 (a^2 - b^2)^2 d e^3 \sqrt{e \cos[c+d x]}}
\end{aligned}$$

Result (type 6, 1275 leaves) :

$$\begin{aligned}
& - \frac{1}{5 (a-b)^2 (a+b)^2 d (\cos[c+d x])^{7/2}} \\
& \cos[c+d x]^{7/2} \left( \frac{1}{12 \sqrt{1 - \cos[c+d x]^2} (a+b \sin[c+d x])} (3 a^4 - 8 a^2 b^2 - 5 b^4) \right. \\
& \left( a+b \sqrt{1 - \cos[c+d x]^2} \right) \left( - \left( \left( 56 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \cos[c+d x]^{3/2} \right) \right/ \left( \sqrt{1 - \cos[c+d x]^2} \right. \\
& \left. \left( 7 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - \right. \\
& \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. \left. (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \right) \\
& \left. \cos[c+d x]^2 \left( a^2 + b^2 (-1 + \cos[c+d x]^2) \right) \right) \right) - \\
& \left( (3 + 3 \text{i}) \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ \right. \right. \right. \\
& \left. \left. \left. 1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[ \sqrt{-a^2+b^2} - (1 + \text{i}) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c+d x]} + \text{i} b \cos[c+d x] \right] + \operatorname{Log} \left[ \sqrt{-a^2+b^2} + (1 + \text{i}) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c+d x]} \right] \right) \right)
\end{aligned}$$

Problem 584: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{11/2}}{(a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 543 leaves, 15 steps):

$$\begin{aligned}
& -\frac{9 a (-a^2 + b^2)^{5/4} e^{11/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{11/2} d} - \frac{9 a (-a^2 + b^2)^{5/4} e^{11/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{11/2} d} - \\
& \frac{3 (21 a^4 - 28 a^2 b^2 + 5 b^4) e^6 \sqrt{\cos[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{7 b^6 d \sqrt{\cos[c+d x]}} + \\
& \left( \frac{9 a^2 (a^2 - b^2)^2 e^6 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+d x), 2\right]}{b - \sqrt{-a^2 + b^2}} \right) / \\
& \left( 2 b^6 \left(a^2 - b \left(b - \sqrt{-a^2 + b^2}\right)\right) d \sqrt{\cos[c+d x]}\right) + \\
& \left( \frac{9 a^2 (a^2 - b^2)^2 e^6 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+d x), 2\right]}{b + \sqrt{-a^2 + b^2}} \right) / \\
& \left( 2 b^6 \left(a^2 - b \left(b + \sqrt{-a^2 + b^2}\right)\right) d \sqrt{\cos[c+d x]}\right) + \\
& \frac{9 e^3 (e \cos[c+d x])^{5/2} (7 a - 5 b \sin[c+d x])}{35 b^3 d} - \frac{e (e \cos[c+d x])^{9/2}}{b d (a + b \sin[c+d x])} - \\
& \frac{3 e^5 \sqrt{e \cos[c+d x]} (21 a (a^2 - b^2) - b (7 a^2 - 5 b^2) \sin[c+d x])}{7 b^5 d}
\end{aligned}$$

Result (type 6, 2230 leaves):

$$\begin{aligned}
& -\frac{1}{70 b^5 d \cos[c+d x]^{11/2}} (\cos[c+d x])^{11/2} \\
& - \left( -\frac{1}{\sqrt{1 - \cos[c+d x]^2} (a + b \sin[c+d x])} 2 (70 a^3 b - 93 a b^3) \left(a + b \sqrt{1 - \cos[c+d x]^2}\right) \right. \\
& \left( \left( 5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2 + b^2}\right] \sqrt{\cos[c+d x]}\right) / \right. \\
& \left( \sqrt{1 - \cos[c+d x]^2} \left( 5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2 + b^2}\right] - 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \\
& \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \\
& \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2 + b^2}\right] \right) \cos[c+d x]^2 \left( a^2 + b^2 (-1 + \cos[c+d x]^2) \right) \right) - \\
& \frac{1}{(-a^2 + b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \left( 2 \operatorname{ArcTan}\left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2 + b^2)^{1/4}}\right] - \right. \\
& \left. 2 \operatorname{ArcTan}\left[1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2 + b^2)^{1/4}}\right] + \operatorname{Log}\left[\sqrt{-a^2 + b^2} - \right. \right. \\
& \left. \left. (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c+d x]}\right] + i b \cos[c+d x]\right] - \operatorname{Log}\left[\sqrt{-a^2 + b^2} + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( 1 + \frac{i}{2} \right) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + \frac{i}{2} b \cos[c + dx] \right) \right\} \sin[c + dx] + \\
& \frac{1}{\sqrt{1 - \cos[c + dx]^2} (-1 + 2 \cos[c + dx]^2) (a + b \sin[c + dx])} \\
& (140 a^3 b - 147 a b^3) \\
& \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \cos[2(c + dx)] \\
& \left( \frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}} \right] \\
& \frac{b^{3/2} (-a^2 + b^2)^{3/4}}{b^{3/2} (-a^2 + b^2)^{3/4}} - \\
& \left( \frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}} \right] \\
& + \frac{4 \sqrt{\cos[c + dx]}}{b} + \\
& \left( 10 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \sqrt{\cos[c + dx]} \right) / \\
& \left( \sqrt{1 - \cos[c + dx]^2} \left( 5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) - \\
& \left( 36 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \\
& \left. \cos[c + dx]^{5/2} \right) / \left( 5 \sqrt{1 - \cos[c + dx]^2} \right. \\
& \left. \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - 2 \right. \right. \\
& \left. \left. \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right. \right. \\
& \left. \left. \left. \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) \\
& (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \left( \left( \frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[ \sqrt{-a^2 + b^2} - \right. \right. \\
& \left. \left. \left( 1 + \frac{i}{2} \right) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + \frac{i}{2} b \cos[c + dx] \right] \right) / \left( b^{3/2} (-a^2 + b^2)^{3/4} \right) - \\
& \left( \left( \frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + \left( 1 + \frac{i}{2} \right) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + \right. \right. \\
& \left. \left. \left( 1 - \frac{i}{2} \right) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + \frac{i}{2} b \cos[c + dx] \right] \right) / \left( b^{3/2} (-a^2 + b^2)^{3/4} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{\frac{1}{2} b \cos[c + d x]}{\left(1 - \cos[c + d x]^2\right) \left(a + b \sin[c + d x]\right)} \right/ \left( b^{3/2} \left(-a^2 + b^2\right)^{3/4} \right) \sin[c + d x] - \\
& \frac{1}{\left(a + b \sqrt{1 - \cos[c + d x]^2}\right)} 2 \left(35 a^4 - 126 a^2 b^2 + 75 b^4\right) \\
& \left( \left(5 b \left(a^2 - b^2\right) \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + d x]} \sqrt{1 - \cos[c + d x]^2}\right) / \\
& \left( \left(-5 \left(a^2 - b^2\right) \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] + 2 \right. \right. \\
& \left. \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] + \right. \right. \\
& \left. \left. \left(a^2 - b^2\right) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right]\right) \right. \\
& \left. \cos[c + d x]^2\right) \left(a^2 + b^2 \left(-1 + \cos[c + d x]^2\right)\right) + \\
& \left. \left(a \left(-2 \text{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{\left(a^2 - b^2\right)^{1/4}}\right] + 2 \text{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{\left(a^2 - b^2\right)^{1/4}}\right]\right) - \right. \\
& \left. \left.\log\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} \left(a^2 - b^2\right)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x]\right] + \log\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} \left(a^2 - b^2\right)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x]\right]\right)\right/ \\
& \left. \left(4 \sqrt{2} \sqrt{b} \left(a^2 - b^2\right)^{3/4}\right) \sin[c + d x]^2\right) + \frac{1}{d} \\
& \left. \left(e \cos[c + d x]\right)^{11/2} \sec[c + d x]^5 \left(\frac{2 a \cos[2 (c + d x)]}{5 b^3} - \right. \right. \\
& \left. \left. \frac{(-28 a^2 + 17 b^2) \sin[c + d x]}{14 b^4} - \right. \right. \\
& \left. \left. \frac{(-a^2 + b^2)^2}{b^5 (a + b \sin[c + d x])} - \right. \right. \\
& \left. \left. \frac{\sin[3 (c + d x)]}{14 b^2}\right)\right)
\end{aligned}$$

## Problem 585: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^{9/2}}{(a + b \sin[c + d x])^2} dx$$

Optimal (type 4, 459 leaves, 14 steps):

$$\begin{aligned} & \frac{7 a (-a^2 + b^2)^{3/4} e^{9/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{2 b^{9/2} d} - \frac{7 a (-a^2 + b^2)^{3/4} e^{9/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{2 b^{9/2} d} + \\ & \frac{7 (5 a^2 - 3 b^2) e^4 \sqrt{e \cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 b^4 d \sqrt{\cos[c + d x]}} - \\ & \frac{7 a^2 (a^2 - b^2) e^5 \sqrt{\cos[c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{2 b^5 (b - \sqrt{-a^2 + b^2}) d \sqrt{e \cos[c + d x]}} - \\ & \frac{7 a^2 (a^2 - b^2) e^5 \sqrt{\cos[c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{2 b^5 (b + \sqrt{-a^2 + b^2}) d \sqrt{e \cos[c + d x]}} + \\ & \frac{7 e^3 (e \cos[c + d x])^{3/2} (5 a - 3 b \sin[c + d x])}{15 b^3 d} - \frac{e (e \cos[c + d x])^{7/2}}{b d (a + b \sin[c + d x])} \end{aligned}$$

Result (type 6, 1229 leaves):

$$\begin{aligned} & \frac{1}{10 b^3 d \cos[c + d x]^{9/2}} \\ & 7 (e \cos[c + d x])^{9/2} \left( \frac{1}{6 \sqrt{1 - \cos[c + d x]^2} (a + b \sin[c + d x])} a b \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \right. \\ & \left( - \left( \left( 56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] \cos[c + d x]^{3/2} \right) \right. \right. \\ & \left( \sqrt{1 - \cos[c + d x]^2} \left( 7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \right. \right. \right. \\ & \left. \left. \left. \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c + d x]^2, \right. \right. \right. \\ & \left. \left. \left. \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c + d x]^2, \right. \right. \right. \\ & \left. \left. \left. \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \cos[c + d x]^2 \right) \left( a^2 + b^2 (-1 + \cos[c + d x]^2) \right) \right) - \\ & \left( (3 + 3 i) \left( 2 \operatorname{ArcTan}\left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4}\right] \right) \right. \end{aligned}$$

Problem 586: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{7/2}}{(a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 473 leaves, 14 steps):

$$\begin{aligned}
& -\frac{5 a (-a^2 + b^2)^{1/4} e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{7/2} d} - \frac{5 a (-a^2 + b^2)^{1/4} e^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{7/2} d} + \\
& \frac{5 (3 a^2 - b^2) e^4 \sqrt{\cos[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{3 b^4 d \sqrt{e \cos[c+d x]}} - \\
& \frac{5 a^2 (a^2 - b^2) e^4 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^4 (a^2 - b (b - \sqrt{-a^2+b^2})) d \sqrt{e \cos[c+d x]}} - \\
& \frac{5 a^2 (a^2 - b^2) e^4 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^4 (a^2 - b (b + \sqrt{-a^2+b^2})) d \sqrt{e \cos[c+d x]}} + \\
& \frac{5 e^3 \sqrt{e \cos[c+d x]} (3 a - b \sin[c+d x])}{3 b^3 d} - \frac{e (e \cos[c+d x])^{5/2}}{b d (a + b \sin[c+d x])}
\end{aligned}$$

Result (type 6, 2156 leaves):

$$\begin{aligned}
& \frac{(e \cos[c+d x])^{7/2} \sec[c+d x]^3 \left(-\frac{2 \sin[c+d x]}{3 b^2} + \frac{a^2-b^2}{b^3 (a+b \sin[c+d x])}\right)}{d} + \\
& \frac{1}{6 b^3 d \cos[c+d x]^{7/2}} (e \cos[c+d x])^{7/2} \left(-\frac{1}{\sqrt{1-\cos[c+d x]^2} (a+b \sin[c+d x])}\right) \\
& 8 a b \left(a + b \sqrt{1 - \cos[c+d x]^2}\right) \left( \left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\
& \left. \left. \left. \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos[c+d x]}\right) \Big/ \left(\sqrt{1-\cos[c+d x]^2}\right. \\
& \left. \left. \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] - 2\right. \right. \\
& \left. \left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] + (-a^2+b^2)\right. \right. \\
& \left. \left. \left.\operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right]\right) \cos[c+d x]^2\right) \\
& \left. \left. \left.(a^2 + b^2 (-1 + \cos[c+d x]^2)\right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8}\right) \sqrt{b}\right) \\
& \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right]\right. + \\
& \left. \left.\operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]}\right] + i b \cos[c+d x]\right] - \\
& \left. \left.\operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]}\right] + i b \cos[c+d x]\right)\right)
\end{aligned}$$

$$\begin{aligned}
& \frac{\sin[c + dx] + \frac{1}{\sqrt{1 - \cos[c + dx]^2} (-1 + 2 \cos[c + dx]^2) (a + b \sin[c + dx])}}{6 a b \left(a + b \sqrt{1 - \cos[c + dx]^2}\right) \cos[2 (c + d x)]} \\
& \left( \frac{\left(\frac{1}{2} - \frac{i}{2}\right) (-2 a^2 + b^2) \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right]}{b^{3/2} (-a^2 + b^2)^{3/4}} - \right. \\
& \left. \frac{\left(\frac{1}{2} - \frac{i}{2}\right) (-2 a^2 + b^2) \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right]}{b^{3/2} (-a^2 + b^2)^{3/4}} + \frac{4 \sqrt{\cos[c + dx]}}{b} + \right. \\
& \left. \left(10 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] \sqrt{\cos[c + dx]}\right) / \right. \\
& \left. \left(\sqrt{1 - \cos[c + dx]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right]\right) \cos[c + dx]^2\right) (a^2 + b^2 (-1 + \cos[c + dx]^2))\right) - \\
& \left(36 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] \right. \\
& \left. \cos[c + dx]^{5/2}\right) / \left(5 \sqrt{1 - \cos[c + dx]^2} \right. \\
& \left. \left(9 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] - \right. \right. \\
& \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right]\right) \cos[c + dx]^2\right) \\
& \left. (a^2 + b^2 (-1 + \cos[c + dx]^2))\right) + \left( \left(\frac{1}{2} - \frac{i}{4}\right) (-2 a^2 + b^2) \operatorname{Log}\left[\sqrt{-a^2 + b^2} - \right. \right. \\
& \left. \left.(1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]}\right. \right. + i b \cos[c + dx]\right) / \left(b^{3/2} (-a^2 + b^2)^{3/4}\right) - \\
& \left. \left(\left(\frac{1}{4} - \frac{i}{4}\right) (-2 a^2 + b^2) \operatorname{Log}\left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]}\right. \right. \right. \\
& \left. \left. \left. + i b \cos[c + dx]\right]\right) / \left(b^{3/2} (-a^2 + b^2)^{3/4}\right)\right) \sin[c + dx] - 
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 2 (3 a^2 - 5 b^2) \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( \left( 5 b (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + dx]} \sqrt{1 - \cos[c + dx]^2} \right) \right. \\
& \left( \left( -5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
& \left. \left. \log \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] + \right. \right. \\
& \left. \left. \log \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] \right) \right) \right) \right. \\
& \left. \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + dx]^2 \right)
\end{aligned}$$

**Problem 587: Result unnecessarily involves higher level functions.**

$$\int \frac{(e \cos[c + dx])^{5/2}}{(a + b \sin[c + dx])^2} dx$$

Optimal (type 4, 390 leaves, 13 steps):

$$\begin{aligned}
& \frac{3 a e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{5/2} (-a^2+b^2)^{1/4} d} - \frac{3 a e^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{5/2} (-a^2+b^2)^{1/4} d} - \\
& \frac{3 e^2 \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{b^2 d \sqrt{\cos [c+d x]}} + \\
& \frac{3 a^2 e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^3 (b-\sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}} + \\
& \frac{3 a^2 e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^3 (b+\sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}} - \frac{e (e \cos [c+d x])^{3/2}}{b d (a+b \sin [c+d x])}
\end{aligned}$$

Result (type 6, 617 leaves):

$$\begin{aligned}
& -\frac{(e \cos [c+d x])^{5/2} \sec [c+d x]}{b d (a+b \sin [c+d x])} + \\
& \frac{1}{b d \cos [c+d x]^{5/2} (1-\cos [c+d x]^2) (a+b \sin [c+d x])} 3 (e \cos [c+d x])^{5/2} \\
& \left( a+b \sqrt{1-\cos [c+d x]^2} \right) \left( \left( 7 b (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \cos [c+d x]^{3/2} \sqrt{1-\cos [c+d x]^2} \right) / \\
& \left( 3 \left( -7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \\
& \left. \cos [c+d x]^2 \right) (a^2+b^2 (-1+\cos [c+d x]^2)) \Big) + \\
& \left( a \left( -2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}}\right] + \right. \right. \\
& \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right] - \right. \right. \\
& \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right] \right) \right) / \\
& \left( 4 \sqrt{2} b^{3/2} (a^2-b^2)^{1/4} \right) \sin [c+d x]^2
\end{aligned}$$

Problem 588: Result unnecessarily involves higher level functions.

$$\int \frac{(e \cos(c + d x))^{3/2}}{(a + b \sin(c + d x))^2} dx$$

Optimal (type 4, 404 leaves, 13 steps):

$$\begin{aligned} & -\frac{a e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos(c+d x)}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{3/2} (-a^2+b^2)^{3/4} d} - \\ & \frac{a e^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos(c+d x)}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{3/2} (-a^2+b^2)^{3/4} d} - \frac{e^2 \sqrt{\cos(c+d x)} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{b^2 d \sqrt{e \cos(c+d x)}} + \\ & \frac{a^2 e^2 \sqrt{\cos(c+d x)} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^2 \left(a^2-b \left(b-\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos(c+d x)}} + \\ & \frac{a^2 e^2 \sqrt{\cos(c+d x)} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^2 \left(a^2-b \left(b+\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos(c+d x)}} - \frac{e \sqrt{e \cos(c+d x)}}{b d \left(a+b \sin(c+d x)\right)} \end{aligned}$$

Result (type 6, 614 leaves):

$$\begin{aligned}
& - \frac{(\mathbf{e} \cos[c + d x])^{3/2} \sec[c + d x]}{b d (a + b \sin[c + d x])} + \\
& \frac{1}{b d \cos[c + d x]^{3/2} (1 - \cos[c + d x]^2) (a + b \sin[c + d x])} (\mathbf{e} \cos[c + d x])^{3/2} \\
& \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \left( \left( 5 b (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \sqrt{\cos[c + d x]} \sqrt{1 - \cos[c + d x]^2} \right) / \\
& \left( \left( -5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \\
& \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \right) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
& \left. \left. \log \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] + \right. \right. \\
& \left. \left. \log \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \right) / \\
& \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + d x]^2
\end{aligned}$$

Problem 589: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{e \cos[c + d x]}}{(a + b \sin[c + d x])^2} dx$$

Optimal (type 4, 422 leaves, 13 steps):

$$\begin{aligned}
& -\frac{a \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 \sqrt{b} (-a^2+b^2)^{5/4} d} + \\
& \frac{a \sqrt{e} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 \sqrt{b} (-a^2+b^2)^{5/4} d} + \frac{\sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{(a^2-b^2) d \sqrt{\cos [c+d x]}} + \\
& \frac{a^2 e \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b (a^2-b^2) \left(b-\sqrt{-a^2+b^2}\right) d \sqrt{e \cos [c+d x]}} + \\
& \frac{a^2 e \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b (a^2-b^2) \left(b+\sqrt{-a^2+b^2}\right) d \sqrt{e \cos [c+d x]}} + \frac{b (e \cos [c+d x])^{3/2}}{(a^2-b^2) d e (a+b \sin [c+d x])}
\end{aligned}$$

Result (type 6, 1182 leaves):

$$\begin{aligned}
& -\frac{b \cos [c+d x] \sqrt{e \cos [c+d x]}}{(-a^2+b^2) d (a+b \sin [c+d x])} + \frac{1}{2 (a-b) (a+b) d \sqrt{\cos [c+d x]}} \\
& \sqrt{e \cos [c+d x]} \left( \frac{1}{6 \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} a \left( a+b \sqrt{1-\cos [c+d x]^2} \right) \right. \\
& \left. - \left( \left( 56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \cos [c+d x]^{3/2} \right) \right. \\
& \left. \left( \sqrt{1-\cos [c+d x]^2} \left( 7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2 \right) \left( a^2+b^2 (-1+\cos [c+d x]^2) \right) \right) - \\
& \left( (3+3 \text{i}) \left( 2 \operatorname{ArcTan}\left[1-\frac{(1+\text{i}) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1+\frac{(1+\text{i}) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2}-(1+\text{i}) \sqrt{b} (-a^2+b^2)^{1/4}\right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos [c+d x]}+\text{i} b \cos [c+d x]\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2}+(1+\text{i}) \sqrt{b} (-a^2+b^2)^{1/4}\right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos [c+d x]}+\text{i} b \cos [c+d x]\right]\right) \right) \left/ \left(\sqrt{b} (-a^2+b^2)^{1/4}\right)\right) \sin [c+d x] - \\
& \frac{1}{(1-\cos [c+d x]^2) (a+b \sin [c+d x])} 2 b \left( a+b \sqrt{1-\cos [c+d x]^2} \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 7b(a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \quad \left. \left. \cos[c + dx]^{3/2} \sqrt{1 - \cos[c + dx]^2} \right) \right) / \\
& \quad \left( 3 \left( -7(a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \quad \left. \left. 2 \left( 2b^2 \text{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \quad \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \right. \\
& \quad \left. \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \\
& \quad \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
& \quad \left. \left. \log \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] - \right. \right. \\
& \quad \left. \left. \log \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] \right) \right) / \\
& \quad \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[c + dx]^2
\end{aligned}$$

Problem 590: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos[c + dx]} (a + b \sin[c + dx])^2} dx$$

Optimal (type 4, 429 leaves, 13 steps):

$$\begin{aligned}
& \frac{3a\sqrt{b} \text{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos[c + dx]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{2(-a^2 + b^2)^{7/4} d \sqrt{e}} + \\
& \frac{3a\sqrt{b} \text{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos[c + dx]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{2(-a^2 + b^2)^{7/4} d \sqrt{e}} - \frac{\sqrt{\cos[c + dx]} \text{EllipticF} \left[ \frac{1}{2} (c + dx), 2 \right]}{(a^2 - b^2) d \sqrt{e \cos[c + dx]}} + \\
& \frac{3a^2 \sqrt{\cos[c + dx]} \text{EllipticPi} \left[ \frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + dx), 2 \right]}{2(a^2 - b^2) (a^2 - b (b - \sqrt{-a^2 + b^2})) d \sqrt{e \cos[c + dx]}} + \\
& \frac{3a^2 \sqrt{\cos[c + dx]} \text{EllipticPi} \left[ \frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + dx), 2 \right]}{2(a^2 - b^2) (a^2 - b (b + \sqrt{-a^2 + b^2})) d \sqrt{e \cos[c + dx]}} + \frac{b \sqrt{e \cos[c + dx]}}{(a^2 - b^2) d e (a + b \sin[c + dx])}
\end{aligned}$$

Result (type 6, 1181 leaves):

$$\begin{aligned}
& \frac{b \cos[c + dx]}{(a^2 - b^2) d \sqrt{e \cos[c + dx]} (a + b \sin[c + dx])} + \\
& \frac{1}{2 (a - b) (a + b) d \sqrt{e \cos[c + dx]}} \sqrt{\cos[c + dx]} \left( -\frac{1}{\sqrt{1 - \cos[c + dx]^2}} \frac{1}{(a + b \sin[c + dx])} \right. \\
& 4 a \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \left( \left( 5 a (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\
& \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \left. \right) \sqrt{\cos[c + dx]} \left. \right) \left/ \left( \sqrt{1 - \cos[c + dx]^2} \right. \right. \\
& \left( 5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - 2 \right. \\
& \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \\
& \left. \text{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \\
& \left. \left( a^2 + b^2 (-1 + \cos[c + dx]^2) \right) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
& \left( 2 \text{ArcTan} \left[ 1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \text{ArcTan} \left[ 1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}} \right] + \right. \\
& \left. \text{Log} \left[ \sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] - \right. \\
& \left. \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] \right) \\
& \sin[c + dx] + \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 2 b \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( 5 b (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \\
& \left. \sqrt{\cos[c + dx]} \sqrt{1 - \cos[c + dx]^2} \right) \left/ \right. \\
& \left( \left( -5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \\
& \cos[c + dx]^2 \left( a^2 + b^2 (-1 + \cos[c + dx]^2) \right) \right) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
& \left. \left. \right. \right)
\end{aligned}$$

Problem 591: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos [c + d x])^{3/2} (a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 492 leaves, 14 steps):

$$\begin{aligned}
& -\frac{5 a b^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 \left(-a^2+b^2\right)^{9/4} d e^{3/2}}+\frac{5 a b^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 \left(-a^2+b^2\right)^{9/4} d e^{3/2}}- \\
& \frac{\left(2 a^2+3 b^2\right) \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{\left(a^2-b^2\right)^2 d e^2 \sqrt{\cos [c+d x]}}- \\
& \frac{5 a^2 b \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 \left(a^2-b^2\right)^2 \left(b-\sqrt{-a^2+b^2}\right) d e \sqrt{e \cos [c+d x]}}- \\
& \frac{5 a^2 b \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 \left(a^2-b^2\right)^2 \left(b+\sqrt{-a^2+b^2}\right) d e \sqrt{e \cos [c+d x]}}+ \\
& \frac{b}{\left(a^2-b^2\right) d e \sqrt{e \cos [c+d x]} \left(a+b \sin [c+d x]\right)}-\frac{5 a b-\left(2 a^2+3 b^2\right) \sin [c+d x]}{\left(a^2-b^2\right)^2 d e \sqrt{e \cos [c+d x]}}
\end{aligned}$$

Result (type 6, 1260 leaves):

$$\begin{aligned}
 & -\frac{1}{2 \sqrt{2} (a-b)^2 (a+b)^2 d \left(e \cos [c+d x]\right)^{3/2}} \\
 & \cos [c+d x]^{3/2} \left( \frac{1}{12 \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} (2 a^3 + 8 a b^2) \right. \\
 & \left( a+b \sqrt{1-\cos [c+d x]^2} \right) \left( - \left( \left( 56 a (a^2-b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2 \right] \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right) \cos [c+d x]^{3/2} \right) \Big/ \left( \sqrt{1-\cos [c+d x]^2} \right. \\
 & \left. \left( 7 (a^2-b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - \right. \right.
 \end{aligned}$$



$$(e \cos[c + d x])^{3/2}$$

Problem 592: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos[c + d x])^{5/2} (a + b \sin[c + d x])^2} \, dx$$

Optimal (type 4, 514 leaves, 14 steps):

$$\begin{aligned} & \frac{7 a b^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 (-a^2+b^2)^{11/4} d e^{5/2}} + \frac{7 a b^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 (-a^2+b^2)^{11/4} d e^{5/2}} + \\ & \frac{(2 a^2+5 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{3 (a^2-b^2)^2 d e^2 \sqrt{e \cos[c+d x]}} - \\ & \frac{7 a^2 b^2 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 (a^2-b^2)^2 (a^2-b (b-\sqrt{-a^2+b^2})) d e^2 \sqrt{e \cos[c+d x]}} - \\ & \frac{7 a^2 b^2 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 (a^2-b^2)^2 (a^2-b (b+\sqrt{-a^2+b^2})) d e^2 \sqrt{e \cos[c+d x]}} + \\ & \frac{b}{(a^2-b^2) d e (e \cos[c+d x])^{3/2} (a+b \sin[c+d x])} - \frac{7 a b - (2 a^2+5 b^2) \sin[c+d x]}{3 (a^2-b^2)^2 d e (e \cos[c+d x])^{3/2}} \end{aligned}$$

Result (type 6, 1258 leaves):

$$\begin{aligned} & \frac{1}{6 (a-b)^2 (a+b)^2 d (e \cos[c+d x])^{5/2}} \cos[c+d x]^{5/2} \\ & \left( -\frac{1}{\sqrt{1-\cos[c+d x]^2}} \frac{2 (2 a^3-16 a b^2)}{(a+b \sin[c+d x])} \left( a+b \sqrt{1-\cos[c+d x]^2} \right) \right. \\ & \left( \left( 5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos[c+d x]} \right) \right. \\ & \left. \left( \sqrt{1-\cos[c+d x]^2} \right. \right. \\ & \left. \left( 5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - 2 \right. \\ & \left. \left( 2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \\ & \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) \end{aligned}$$

$$\begin{aligned}
& \left( a^2 + b^2 (-1 + \cos[c + d x]^2) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
& \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \right. \\
& \left. \operatorname{Log} \left[ \sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] - \right. \\
& \left. \operatorname{Log} \left[ \sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] \right) \\
& \frac{\sin[c+d x] - \frac{1}{(1-\cos[c+d x]^2) (a+b \sin[c+d x])}}{2 (2 a^2 b + 5 b^3) \left( a + b \sqrt{1-\cos[c+d x]^2} \right)} \\
& \left( \left( 5 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c+d x]} \sqrt{1-\cos[c+d x]^2} \right) / \\
& \left( \left( -5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \right. \\
& \left. \cos[c+d x]^2 \right) \left( a^2 + b^2 (-1 + \cos[c+d x]^2) \right) + \\
& \left. \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c+d x]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c+d x]}}{(a^2-b^2)^{1/4}} \right] - \right. \right. \\
& \left. \left. \operatorname{Log} \left[ \sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[c+d x]} + b \cos[c+d x] \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[ \sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[c+d x]} + b \cos[c+d x] \right] \right) \right) / \\
& \left. \left( 4 \sqrt{2} \sqrt{b} (a^2-b^2)^{3/4} \right) \sin[c+d x]^2 \right) + \\
& \left( \cos[c+d x]^3 \left( -\frac{b^3}{(a^2-b^2)^2 (a+b \sin[c+d x])} + \right. \right. \\
& \left. \left. \frac{2 \sec[c+d x]^2 (-2 a b + a^2 \sin[c+d x] + b^2 \sin[c+d x])}{3 (a^2-b^2)^2} \right) \right) / (d) \\
& (e \cos[c+d x])^{5/2}
\end{aligned}$$

Problem 593: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos[c + dx])^{7/2} (a + b \sin[c + dx])^2} dx$$

Optimal (type 4, 574 leaves, 15 steps):

$$\begin{aligned} & - \frac{9 a b^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c + dx]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{2 (-a^2 + b^2)^{13/4} d e^{7/2}} + \frac{9 a b^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c + dx]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{2 (-a^2 + b^2)^{13/4} d e^{7/2}} - \\ & \frac{3 (2 a^4 - 10 a^2 b^2 - 7 b^4) \sqrt{e \cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2} (c + dx), 2\right]}{5 (a^2 - b^2)^3 d e^4 \sqrt{\cos[c + dx]}} + \\ & \frac{9 a^2 b^3 \sqrt{\cos[c + dx]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + dx), 2\right]}{2 (a^2 - b^2)^3 (b - \sqrt{-a^2 + b^2}) d e^3 \sqrt{e \cos[c + dx]}} + \\ & \frac{9 a^2 b^3 \sqrt{\cos[c + dx]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + dx), 2\right]}{2 (a^2 - b^2)^3 (b + \sqrt{-a^2 + b^2}) d e^3 \sqrt{e \cos[c + dx]}} - \\ & \frac{b}{(a^2 - b^2) d e (e \cos[c + dx])^{5/2} (a + b \sin[c + dx])} - \\ & \frac{9 a b - (2 a^2 + 7 b^2) \sin[c + dx]}{5 (a^2 - b^2)^2 d e (e \cos[c + dx])^{5/2}} + \frac{3 (15 a b^3 + (2 a^4 - 10 a^2 b^2 - 7 b^4) \sin[c + dx])}{5 (a^2 - b^2)^3 d e^3 \sqrt{e \cos[c + dx]}} \end{aligned}$$

Result (type 6, 1343 leaves):

$$\begin{aligned} & - \frac{1}{10 (a - b)^3 (a + b)^3 d (e \cos[c + dx])^{7/2}} \\ & 3 \cos[c + dx]^{7/2} \left( \frac{1}{12 \sqrt{1 - \cos[c + dx]^2} (a + b \sin[c + dx])} \right. \\ & (2 a^5 - 10 a^3 b^2 - 22 a b^4) \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \left( - \left( \left( 56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \right. \right. \right. \right. \\ & \left. \left. \left. \left. \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \cos[c + dx]^{3/2} \right) \right) \left( \sqrt{1 - \cos[c + dx]^2} \right. \\ & \left. \left( 7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - \right. \right. \\ & \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\ & \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \right) \\ & \left. \cos[c + dx]^2 \right) \left( a^2 + b^2 (-1 + \cos[c + dx]^2) \right) \left. \right) - \end{aligned}$$

$$\begin{aligned}
& \left( (3 + 3 \text{i}) \left( 2 \text{ArcTan} \left[ 1 - \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \text{ArcTan} \left[ 1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \text{Log} \left[ \sqrt{-a^2 + b^2} - (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] + \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] \right] \right) \Big/ \left( \sqrt{b} (-a^2 + b^2)^{1/4} \right) \sin[c + d x] - \\
& \frac{1}{(1 - \cos[c + d x]^2) (a + b \sin[c + d x])} 2 (2 a^4 b - 10 a^2 b^3 - 7 b^5) \\
& \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \\
& \left( \left( 7 b (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \cos[c + d x]^{3/2} \sqrt{1 - \cos[c + d x]^2} \right) \Big/ \right. \\
& \left. \left( 3 \left( -7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + 2 \right. \right. \\
& \left. \left. \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \Big) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
& \left. \left. \text{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] - \text{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \right) \Big/ \\
& \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[c + d x]^2 + \left( \cos[c + d x]^4 \right. \\
& \left. \left( \frac{b^5 \cos[c + d x]}{(a^2 - b^2)^3 (a + b \sin[c + d x])} + \frac{2 \sec[c + d x]^3 (-2 a b + a^2 \sin[c + d x] + b^2 \sin[c + d x])}{5 (a^2 - b^2)^2} \right. \right. \\
& \left. \left. \frac{1}{5 (a^2 - b^2)^3} \right. \right. \\
& \left. \left. 2 \sec[c + d x] \right. \right. \\
& \left. \left. (20 a b^3 + 3 a^4 \sin[c + d x] - 15 a^2 b^2 \sin[c + d x] - \right. \right.
\end{aligned}$$

$$8 b^4 \sin(c + d x) \Bigg) \Bigg) \Bigg/ \left( d \left( e \cos(c + d x) \right)^{7/2} \right)$$

Problem 594: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{13/2}}{(a + b \sin [c + d x])^3} dx$$

Optimal (type 4, 575 leaves, 15 steps):

$$\begin{aligned}
& \frac{11 \left(9 a^4 - 11 a^2 b^2 + 2 b^4\right) e^{13/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 b^{13/2} (-a^2+b^2)^{1/4} d} + \\
& \frac{11 \left(9 a^4 - 11 a^2 b^2 + 2 b^4\right) e^{13/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 b^{13/2} (-a^2+b^2)^{1/4} d} + \\
& \frac{11 a \left(45 a^2 - 37 b^2\right) e^6 \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{20 b^6 d \sqrt{\cos [c+d x]}} - \\
& \left(11 a \left(9 a^4 - 11 a^2 b^2 + 2 b^4\right) e^7 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
& \left(8 b^7 \left(b - \sqrt{-a^2+b^2}\right) d \sqrt{e \cos [c+d x]}\right) - \\
& \left(11 a \left(9 a^4 - 11 a^2 b^2 + 2 b^4\right) e^7 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
& \left(8 b^7 \left(b + \sqrt{-a^2+b^2}\right) d \sqrt{e \cos [c+d x]}\right) - \\
& \frac{e \left(e \cos [c+d x]\right)^{11/2}}{2 b d \left(a + b \sin [c+d x]\right)^2} - \frac{11 e^3 \left(e \cos [c+d x]\right)^{7/2} \left(9 a + 2 b \sin [c+d x]\right)}{28 b^3 d \left(a + b \sin [c+d x]\right)} + \\
& \frac{11 e^5 \left(e \cos [c+d x]\right)^{3/2} \left(5 \left(9 a^2 - 2 b^2\right) - 27 a b \sin [c+d x]\right)}{60 b^5 d}
\end{aligned}$$

### Result (type 6, 1326 leaves):

$$\frac{1}{40 b^5 d \cos[c + d x]^{13/2}} 11 \left( e \cos[c + d x] \right)^{13/2} \left( \frac{1}{12 \sqrt{1 - \cos[c + d x]^2} (a + b \sin[c + d x])} (18 a^2 b - 10 b^3) \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \right. \\ \left. - \left( \left( 56 a (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \cos[c + d x]^{3/2} \right) \right. \right. \\ \left. \left. \left( \sqrt{1 - \cos[c + d x]^2} \left( 7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \right. \right. \right. \right. \right. \\ \left. \left. \left. \left. \left. \left. \right] \right] \right] \right] \right)$$



$$\begin{aligned}
& \frac{\cos[3(c+dx)]}{14b^3} + \\
& \frac{-a^4 \cos[c+dx] + 2a^2 b^2 \cos[c+dx] - b^4 \cos[c+dx]}{2b^5 (a+b \sin[c+dx])^2} + \\
& \frac{19(a^3 \cos[c+dx] - a b^2 \cos[c+dx])}{4b^5 (a+b \sin[c+dx])} - \\
& \frac{3a \sin[2(c+dx)]}{5b^4}
\end{aligned}$$

Problem 595: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c+dx])^{11/2}}{(a+b \sin[c+dx])^3} dx$$

Optimal (type 4, 589 leaves, 15 steps):

$$\begin{aligned}
& \frac{9(7a^4 - 9a^2b^2 + 2b^4)e^{11/2} \operatorname{ArcTan}\left[\frac{\sqrt{b}\sqrt{e \cos[c+dx]}}{(-a^2+b^2)^{1/4}\sqrt{e}}\right]}{8b^{11/2}(-a^2+b^2)^{3/4}d} + \\
& \frac{9(7a^4 - 9a^2b^2 + 2b^4)e^{11/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b}\sqrt{e \cos[c+dx]}}{(-a^2+b^2)^{1/4}\sqrt{e}}\right]}{8b^{11/2}(-a^2+b^2)^{3/4}d} + \\
& \frac{3a(21a^2 - 13b^2)e^6\sqrt{\cos[c+dx]}\operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{4b^6d\sqrt{e \cos[c+dx]}} - \\
& \left(9a(7a^4 - 9a^2b^2 + 2b^4)e^6\sqrt{\cos[c+dx]}\operatorname{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+dx), 2\right]\right) / \\
& \left(8b^6\left(a^2 - b\left(b - \sqrt{-a^2+b^2}\right)\right)d\sqrt{e \cos[c+dx]}\right) - \\
& \left(9a(7a^4 - 9a^2b^2 + 2b^4)e^6\sqrt{\cos[c+dx]}\operatorname{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+dx), 2\right]\right) / \\
& \left(8b^6\left(a^2 - b\left(b + \sqrt{-a^2+b^2}\right)\right)d\sqrt{e \cos[c+dx]}\right) - \\
& \frac{e(e \cos[c+dx])^{9/2}}{2b d (a+b \sin[c+dx])^2} - \frac{9e^3(e \cos[c+dx])^{5/2}(7a+2b \sin[c+dx])}{20b^3 d (a+b \sin[c+dx])} + \\
& \frac{3e^5\sqrt{e \cos[c+dx]}}{4b^5 d} (3(7a^2 - 2b^2) - 7ab \sin[c+dx])
\end{aligned}$$

Result (type 6, 2224 leaves):

$$\frac{1}{d}(e \cos[c+dx])^{11/2} \operatorname{Sec}[c+dx]^5$$

$$\begin{aligned}
& \left( -\frac{\cos[2(c+dx)]}{5b^3} - \frac{2a \sin[c+dx]}{b^4} - \frac{(-a^2+b^2)^2}{2b^5 (a+b \sin[c+dx])^2} + \frac{17a(a^2-b^2)}{4b^5 (a+b \sin[c+dx])} \right) + \\
& \frac{1}{40b^5 d \cos[c+dx]^{11/2}} 3 (\cos[c+dx])^{11/2} \\
& \left( -\frac{1}{\sqrt{1-\cos[c+dx]^2} (a+b \sin[c+dx])} 2 (30a^2b - 16b^3) \left( a+b \sqrt{1-\cos[c+dx]^2} \right) \right. \\
& \left( \left( 5a(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \sqrt{\cos[c+dx]} \right) / \right. \\
& \left( \sqrt{1-\cos[c+dx]^2} \right. \\
& \left( 5(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] - 2 \right. \\
& \left. \left( 2b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \\
& \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \right) \cos[c+dx]^2 \right) \\
& \left. (a^2+b^2 (-1+\cos[c+dx]^2)) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
& \left( 2 \operatorname{ArcTan}\left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}}\right] + \right. \\
& \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+dx]} + i b \cos[c+dx]\right] - \right. \\
& \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+dx]} + i b \cos[c+dx]\right] \right) \\
& \frac{1}{\sin[c+dx] + \frac{1}{\sqrt{1-\cos[c+dx]^2} (-1+2\cos[c+dx]^2) (a+b \sin[c+dx])}} \\
& (40a^2b - 14b^3) \left( a+b \sqrt{1-\cos[c+dx]^2} \right) \cos[2(c+dx)] \\
& \left( \frac{1}{2} - \frac{i}{2} \right) (-2a^2+b^2) \operatorname{ArcTan}\left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}}\right] \\
& \left. \frac{b^{3/2} (-a^2+b^2)^{3/4}}{\right. \\
& \left. \left( \frac{1}{2} - \frac{i}{2} \right) (-2a^2+b^2) \operatorname{ArcTan}\left[1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}}\right] \right. \\
& \left. \left. + \frac{4\sqrt{\cos[c+dx]}}{b} \right) + \right. \\
& \left. \left( 10a(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \sqrt{\cos[c+dx]}\right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{1 - \cos[c + dx]^2} \left( 5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) - \\
& \left( 36 a (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \\
& \left. \cos[c + dx]^{5/2} \right) \Big/ \left( 5 \sqrt{1 - \cos[c + dx]^2} \right. \\
& \left. \left( 9 (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right. \\
& \left. \left. \text{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) \\
& \left. (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \left( \left( \frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \text{Log} \left[ \sqrt{-a^2 + b^2} - \right. \right. \\
& \left. \left. (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] \right) \Big/ \left( b^{3/2} (-a^2 + b^2)^{3/4} \right) - \\
& \left. \left( \left( \frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + \right. \right. \right. \\
& \left. \left. \left. i b \cos[c + dx] \right] \right) \Big/ \left( b^{3/2} (-a^2 + b^2)^{3/4} \right) \right) \sin[c + dx] - \\
& \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 2 (25 a^3 - 37 a b^2) \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( \left( 5 b (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + dx]} \sqrt{1 - \cos[c + dx]^2} \right) \Big/ \\
& \left( \left( -5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \Big) +
\end{aligned}$$

$$\left. \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c+d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c+d x]}}{(a^2 - b^2)^{1/4}} \right] - \operatorname{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c+d x]} + b \cos[c+d x] \right] + \operatorname{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c+d x]} + b \cos[c+d x] \right] \right) \right) \right) \right/ \\ \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c+d x]^2$$

Problem 596: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c+d x])^{9/2}}{(a + b \sin[c+d x])^3} dx$$

Optimal (type 4, 483 leaves, 14 steps):

$$\frac{7 (5 a^2 - 2 b^2) e^{9/2} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{8 b^{9/2} (-a^2 + b^2)^{1/4} d} - \frac{7 (5 a^2 - 2 b^2) e^{9/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{8 b^{9/2} (-a^2 + b^2)^{1/4} d} - \frac{35 a e^4 \sqrt{e \cos[c+d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{4 b^4 d \sqrt{\cos[c+d x]}} + \\ \left( 7 a (5 a^2 - 2 b^2) e^5 \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right] \right) \left/ \right. \\ \left( 8 b^5 \left( b - \sqrt{-a^2 + b^2} \right) d \sqrt{e \cos[c+d x]} \right) + \\ \left( 7 a (5 a^2 - 2 b^2) e^5 \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right] \right) \left/ \right. \\ \left( 8 b^5 \left( b + \sqrt{-a^2 + b^2} \right) d \sqrt{e \cos[c+d x]} \right) - \\ \frac{e (e \cos[c+d x])^{7/2}}{2 b d (a + b \sin[c+d x])^2} - \frac{7 e^3 (e \cos[c+d x])^{3/2} (5 a + 2 b \sin[c+d x])}{12 b^3 d (a + b \sin[c+d x])}$$

Result (type 6, 1231 leaves):

$$\frac{1}{d} (e \cos[c+d x])^{9/2} \operatorname{Sec}[c+d x]^4 \\ \left( -\frac{2 \cos[c+d x]}{3 b^3} + \frac{a^2 \cos[c+d x] - b^2 \cos[c+d x]}{2 b^3 (a + b \sin[c+d x])^2} - \frac{11 a \cos[c+d x]}{4 b^3 (a + b \sin[c+d x])} \right) - \\ \frac{1}{8 b^3 d \cos[c+d x]^{9/2}} 7 (e \cos[c+d x])^{9/2}$$

$$\begin{aligned}
& \left( \frac{1}{6 \sqrt{1 - \cos[c + dx]^2} (a + b \sin[c + dx])} b \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \right. \\
& \left. - \left( \left( 56 a (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \cos[c + dx]^{3/2} \right) \right. \right. \\
& \left. \left( \sqrt{1 - \cos[c + dx]^2} \left( 7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c + dx]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c + dx]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) \right) - \\
& \left( (3 + 3 i) \left( 2 \text{ArcTan} \left[ 1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \text{ArcTan} \left[ \right. \right. \right. \\
& \left. \left. \left. 1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}} \right] - \text{Log} \left[ \sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] + \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] \right) \right) \right. \left. \left( \sqrt{b} (-a^2 + b^2)^{1/4} \right) \right) \sin[c + dx] - \\
& \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 10 a \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( \left( 7 b (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \cos[c + dx]^{3/2} \sqrt{1 - \cos[c + dx]^2} \right) \right. \\
& \left( 3 \left( -7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
& \left. \left. \text{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] - \right. \right. \\
& \left. \left. \text{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] \right) \right) \right)
\end{aligned}$$

$$\left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin [c + d x]^2 \right)$$

**Problem 597: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(e \cos [c + d x])^{7/2}}{(a + b \sin [c + d x])^3} \, dx$$

Optimal (type 4, 497 leaves, 14 steps):

$$\begin{aligned} & - \frac{5 (3 a^2 - 2 b^2) e^{7/2} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{8 b^{7/2} (-a^2 + b^2)^{3/4} d} - \\ & \frac{5 (3 a^2 - 2 b^2) e^{7/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{8 b^{7/2} (-a^2 + b^2)^{3/4} d} - \frac{15 a e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{4 b^4 d \sqrt{e \cos [c + d x]}} + \\ & \left( 5 a (3 a^2 - 2 b^2) e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right] \right) / \\ & \left( 8 b^4 \left( a^2 - b \left( b - \sqrt{-a^2 + b^2} \right) \right) d \sqrt{e \cos [c + d x]} \right) + \\ & \left( 5 a (3 a^2 - 2 b^2) e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right] \right) / \\ & \left( 8 b^4 \left( a^2 - b \left( b + \sqrt{-a^2 + b^2} \right) \right) d \sqrt{e \cos [c + d x]} \right) - \\ & \frac{e (e \cos [c + d x])^{5/2}}{2 b d (a + b \sin [c + d x])^2} - \frac{5 e^3 \sqrt{e \cos [c + d x]} (3 a + 2 b \sin [c + d x])}{4 b^3 d (a + b \sin [c + d x])} \end{aligned}$$

Result (type 6, 2154 leaves):

$$\begin{aligned} & \frac{(e \cos [c + d x])^{7/2} \operatorname{Sec} [c + d x]^3 \left( \frac{a^2 - b^2}{2 b^3 (a + b \sin [c + d x])^2} - \frac{9 a}{4 b^3 (a + b \sin [c + d x])} \right)}{d} - \\ & \frac{1}{8 b^3 d \cos [c + d x]^{7/2}} (e \cos [c + d x])^{7/2} \left( - \frac{1}{\sqrt{1 - \cos [c + d x]^2} (a + b \sin [c + d x])} \right. \\ & \left. 12 b \left( a + b \sqrt{1 - \cos [c + d x]^2} \right) \left( 5 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\ & \left. \left. \left. \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \sqrt{\cos [c + d x]} \right) / \left( \sqrt{1 - \cos [c + d x]^2} \right. \\ & \left. \left. \left. \left( 5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] - 2 \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
& \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \\
& \quad \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
& \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \right. \\
& \quad \left. \operatorname{Log} \left[ \sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] - \right. \\
& \quad \left. \operatorname{Log} \left[ \sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] \right) \\
& \frac{1}{\sin[c+d x] + \frac{1}{\sqrt{1-\cos[c+d x]^2} (-1+2 \cos[c+d x]^2) (a+b \sin[c+d x])}} \\
& 4 b \left( a+b \sqrt{1-\cos[c+d x]^2} \right) \cos[2 (c+d x)] - \\
& \left( \frac{1}{2} - \frac{i}{2} \right) (-2 a^2+b^2) \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \\
& \quad \frac{b^{3/2} (-a^2+b^2)^{3/4}}{\left( \frac{1}{2} - \frac{i}{2} \right) (-2 a^2+b^2) \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right]} + \frac{4 \sqrt{\cos[c+d x]}}{b} + \\
& \left( 10 a (a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos[c+d x]} \right) / \\
& \left( \sqrt{1-\cos[c+d x]^2} \left( 5 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \quad \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \\
& \quad \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \\
& \quad \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) (a^2+b^2 (-1+\cos[c+d x]^2)) - \\
& \left( 36 a (a^2-b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right. \\
& \quad \left. \cos[c+d x]^{5/2} \right) / \left( 5 \sqrt{1-\cos[c+d x]^2} \right. \\
& \quad \left. \left( 9 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - \right. \right. \\
& \quad \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \left( \frac{1}{4} - \frac{\frac{1}{2}}{4} \right) \left( -2 a^2 + b^2 \right) \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + \left( 1 + \frac{1}{2} \right) \sqrt{b} \left( -a^2 + b^2 \right)^{1/4} \sqrt{\cos [c + d x]} \right] + \frac{1}{2} b \cos [c + d x] \right) \right) \Big/ \left( b^{3/2} \left( -a^2 + b^2 \right)^{3/4} \right) - \\
& \left. \left( \left( \frac{1}{4} - \frac{\frac{1}{2}}{4} \right) \left( -2 a^2 + b^2 \right) \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + \left( 1 + \frac{1}{2} \right) \sqrt{b} \left( -a^2 + b^2 \right)^{1/4} \sqrt{\cos [c + d x]} \right] + \right. \right. \\
& \left. \left. \frac{1}{2} b \cos [c + d x] \right) \right) \Big/ \left( b^{3/2} \left( -a^2 + b^2 \right)^{3/4} \right) \right] \sin [c + d x] - \\
& \frac{1}{(1 - \cos [c + d x]^2) (a + b \sin [c + d x])} 14 a \left( a + b \sqrt{1 - \cos [c + d x]^2} \right) \\
& \left( \left( 5 b \left( a^2 - b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos [c + d x]} \sqrt{1 - \cos [c + d x]^2} \right) \Big/ \right. \\
& \left. \left( \left( -5 \left( a^2 - b^2 \right) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. \left( a^2 - b^2 \right) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right. \right. \\
& \left. \left. \cos [c + d x]^2 \right) \left( a^2 + b^2 \left( -1 + \cos [c + d x]^2 \right) \right) \right) + \\
& \left. \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{\left( a^2 - b^2 \right)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{\left( a^2 - b^2 \right)^{1/4}} \right] \right) - \right. \\
& \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} \left( a^2 - b^2 \right)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} \left( a^2 - b^2 \right)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \right) \right) \Big/ \\
& \left. \left( 4 \sqrt{2} \sqrt{b} \left( a^2 - b^2 \right)^{3/4} \right) \sin [c + d x]^2 \right)
\end{aligned}$$

Problem 598: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{5/2}}{(a + b \sin [c + d x])^3} dx$$

Optimal (type 4, 505 leaves, 14 steps):

$$\begin{aligned}
 & \frac{3 (a^2 - 2 b^2) e^{5/2} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 b^{5/2} (-a^2+b^2)^{5/4} d} - \\
 & \frac{3 (a^2 - 2 b^2) e^{5/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 b^{5/2} (-a^2+b^2)^{5/4} d} + \frac{3 a e^2 \sqrt{e \cos [c+d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c+d x), 2 \right]}{4 b^2 (a^2-b^2) d \sqrt{\cos [c+d x]}} - \\
 & \left( 3 a (a^2 - 2 b^2) e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\
 & \left( 8 b^3 (a^2 - b^2) \left( b - \sqrt{-a^2+b^2} \right) d \sqrt{e \cos [c+d x]} \right) - \\
 & \left( 3 a (a^2 - 2 b^2) e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\
 & \left( 8 b^3 (a^2 - b^2) \left( b + \sqrt{-a^2+b^2} \right) d \sqrt{e \cos [c+d x]} \right) - \\
 & \frac{e (e \cos [c+d x])^{3/2}}{2 b d (a+b \sin [c+d x])^2} + \frac{3 a e (e \cos [c+d x])^{3/2}}{4 b (a^2-b^2) d (a+b \sin [c+d x])}
 \end{aligned}$$

Result (type 6, 1225 leaves):

$$\begin{aligned}
 & \frac{1}{d} (e \cos [c+d x])^{5/2} \operatorname{Sec} [c+d x]^2 \left( -\frac{\cos [c+d x]}{2 b (a+b \sin [c+d x])^2} - \frac{3 a \cos [c+d x]}{4 b (-a^2+b^2) (a+b \sin [c+d x])} \right) + \\
 & \frac{1}{8 (a-b) b (a+b) d \cos [c+d x]^{5/2}} \\
 & 3 (e \cos [c+d x])^{5/2} \left( \frac{1}{6 \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} b \left( a+b \sqrt{1-\cos [c+d x]^2} \right) \right. \\
 & \left. - \left( \left( 56 a (a^2-b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \cos [c+d x]^{3/2} \right) / \right. \\
 & \left. \left( \sqrt{1-\cos [c+d x]^2} \left( 7 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2 \left( a^2+b^2 (-1+\cos [c+d x]^2) \right) \right) \right) - \\
 & \left( (3+3 i) \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[ \sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \frac{\sqrt{\cos[c + dx]} + i b \cos[c + dx]}{\sqrt{\cos[c + dx]} + i b \cos[c + dx]} \Bigg) \Bigg/ \left( \sqrt{b} (-a^2 + b^2)^{1/4} \right) \sin[c + dx] - \\
& \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 2 a \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( \left( 7 b (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \cos[c + dx]^{3/2} \sqrt{1 - \cos[c + dx]^2} \right) \Bigg/ \right. \\
& \left. \left( 3 \left( -7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \left. \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] \right. \right. \\
& \left. \left. \log \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] - \right. \right. \\
& \left. \left. \log \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] \right) \right) \Bigg/ \\
& \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[c + dx]^2
\end{aligned}$$

Problem 599: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{3/2}}{(a + b \sin [c + d x])^3} dx$$

Optimal (type 4, 519 leaves, 14 steps):

$$\begin{aligned}
& \frac{(a^2 + 2b^2) e^{3/2} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 b^{3/2} (-a^2+b^2)^{7/4} d} + \\
& \frac{(a^2 + 2b^2) e^{3/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 b^{3/2} (-a^2+b^2)^{7/4} d} - \frac{a e^2 \sqrt{\cos[c+d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c+d x), 2 \right]}{4 b^2 (a^2-b^2) d \sqrt{e \cos[c+d x]}} + \\
& \frac{a (a^2 + 2b^2) e^2 \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{8 b^2 (a^2-b^2) (a^2-b (b-\sqrt{-a^2+b^2})) d \sqrt{e \cos[c+d x]}} + \\
& \frac{a (a^2 + 2b^2) e^2 \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{8 b^2 (a^2-b^2) (a^2-b (b+\sqrt{-a^2+b^2})) d \sqrt{e \cos[c+d x]}} - \\
& \frac{e \sqrt{e \cos[c+d x]}}{2 b d (a+b \sin[c+d x])^2} + \frac{a e \sqrt{e \cos[c+d x]}}{4 b (a^2-b^2) d (a+b \sin[c+d x])}
\end{aligned}$$

Result (type 6, 1211 leaves):

$$\begin{aligned}
& \frac{1}{d} (e \cos[c+d x])^{3/2} \operatorname{Sec}[c+d x] \left( -\frac{1}{2 b (a+b \sin[c+d x])^2} - \frac{a}{4 b (-a^2+b^2) (a+b \sin[c+d x])} \right) - \\
& \frac{1}{8 (a-b) b (a+b) d \cos[c+d x]^{3/2}} \\
& (e \cos[c+d x])^{3/2} \left( \frac{1}{\sqrt{1-\cos[c+d x]^2} (a+b \sin[c+d x])} 4 b \left( a+b \sqrt{1-\cos[c+d x]^2} \right) \right. \\
& \left( \left( 5 a (a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos[c+d x]} \right) / \right. \\
& \left( \sqrt{1-\cos[c+d x]^2} \left( 5 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) \right) - \\
& \frac{1}{(-a^2+b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \right. \\
& \left. 2 \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \right. \\
& \left. \operatorname{Log} \left[ \sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] - \right.
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] \Bigg) \\
& \sin[c + dx] - \frac{1}{(1 - \cos[c + dx]^2)^2 (a + b \sin[c + dx])} 2 a \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( \left( 5 b (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + dx]} \sqrt{1 - \cos[c + dx]^2} \right) \Bigg) \\
& \left( \left( -5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \\
& \cos[c + dx]^2 \Bigg) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \Bigg) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] \right) - \right. \\
& \text{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] + \\
& \text{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] \Bigg) \Bigg) \\
& \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + dx]^2
\end{aligned}$$

Problem 600: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{e \cos [c + d x]}}{(a + b \sin [c + d x])^3} dx$$

Optimal (type 4, 514 leaves, 14 steps):

$$\begin{aligned}
& \frac{(3 a^2 + 2 b^2) \sqrt{e} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 \sqrt{b} (-a^2+b^2)^{9/4} d} - \\
& \frac{(3 a^2 + 2 b^2) \sqrt{e} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 \sqrt{b} (-a^2+b^2)^{9/4} d} + \frac{5 a \sqrt{e \cos[c+d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c+d x), 2 \right]}{4 (a^2-b^2)^2 d \sqrt{\cos[c+d x]}} + \\
& \frac{a (3 a^2 + 2 b^2) e \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{8 b (a^2-b^2)^2 (b-\sqrt{-a^2+b^2}) d \sqrt{e \cos[c+d x]}} + \\
& \frac{a (3 a^2 + 2 b^2) e \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{8 b (a^2-b^2)^2 (b+\sqrt{-a^2+b^2}) d \sqrt{e \cos[c+d x]}} + \\
& \frac{b (\operatorname{e} \cos[c+d x])^{3/2}}{2 (a^2-b^2) d e (a+b \sin[c+d x])^2} + \frac{5 a b (\operatorname{e} \cos[c+d x])^{3/2}}{4 (a^2-b^2)^2 d e (a+b \sin[c+d x])}
\end{aligned}$$

Result (type 6, 1232 leaves):

$$\begin{aligned}
& \frac{\sqrt{e \cos[c+d x]} \left( \frac{b \cos[c+d x]}{2 (a^2-b^2) (a+b \sin[c+d x])^2} + \frac{5 a b \cos[c+d x]}{4 (a^2-b^2)^2 (a+b \sin[c+d x])} \right)}{d} + \\
& \frac{1}{8 (a-b)^2 (a+b)^2 d \sqrt{\cos[c+d x]}} \sqrt{e \cos[c+d x]} \\
& \left( \frac{1}{12 \sqrt{1-\cos[c+d x]^2} (a+b \sin[c+d x])} (8 a^2 + 2 b^2) \left( a + b \sqrt{1-\cos[c+d x]^2} \right) \right. \\
& \left. - \left( \left( 56 a (a^2-b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \cos[c+d x]^{3/2} \right) \right. \\
& \left. \left( \sqrt{1-\cos[c+d x]^2} \left( 7 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) \right) - \\
& \left( (3+3 i) \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[ \sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \\
& \left. \left. \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] + \operatorname{Log} \left[ \sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \\
& \left. \left. \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] \right)
\end{aligned}$$

Problem 601: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos [c + d x]}} \frac{1}{(a + b \sin [c + d x])^3} dx$$

Optimal (type 4, 520 leaves, 14 steps):

$$\begin{aligned}
& -\frac{3 \sqrt{b} (5 a^2 + 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 (-a^2+b^2)^{11/4} d \sqrt{e}} - \\
& \frac{3 \sqrt{b} (5 a^2 + 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 (-a^2+b^2)^{11/4} d \sqrt{e}} - \frac{7 a \sqrt{\cos[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{4 (a^2-b^2)^2 d \sqrt{e \cos[c+d x]}} + \\
& \frac{3 a (5 a^2 + 2 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{8 (a^2-b^2)^2 (a^2-b (b-\sqrt{-a^2+b^2})) d \sqrt{e \cos[c+d x]}} + \\
& \frac{3 a (5 a^2 + 2 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{8 (a^2-b^2)^2 (a^2-b (b+\sqrt{-a^2+b^2})) d \sqrt{e \cos[c+d x]}} + \\
& \frac{b \sqrt{e \cos[c+d x]}}{2 (a^2-b^2) d e (a+b \sin[c+d x])^2} + \frac{7 a b \sqrt{e \cos[c+d x]}}{4 (a^2-b^2)^2 d e (a+b \sin[c+d x])}
\end{aligned}$$

Result (type 6, 1226 leaves):

$$\begin{aligned}
& \frac{\cos[c+d x] \left( \frac{b}{2 (a^2-b^2) (a+b \sin[c+d x])^2} + \frac{7 a b}{4 (a^2-b^2)^2 (a+b \sin[c+d x])} \right)}{d \sqrt{e \cos[c+d x]}} + \\
& \frac{1}{8 (a-b)^2 (a+b)^2 d \sqrt{e \cos[c+d x]}} \sqrt{\cos[c+d x]} \left( -\frac{1}{\sqrt{1-\cos[c+d x]^2}} (a+b \sin[c+d x]) \right. \\
& \left. 2 (8 a^2 + 6 b^2) \left( a+b \sqrt{1-\cos[c+d x]^2} \right) \left( 5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\
& \left. \left. \left. \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos[c+d x]} \right) \Big/ \left( \sqrt{1-\cos[c+d x]^2} \right. \\
& \left. \left( 5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - 2 \right. \right. \\
& \left. \left. \left( 2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \\
& \left. \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) \\
& \left. (a^2+b^2 (-1+\cos[c+d x]^2) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
& \left( 2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right] \right. + \\
& \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x]\right] - \right. \\
& \left. \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x]\right]\right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sin[c + dx] + \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 14 a b \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( \left( 5 b (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + dx]} \sqrt{1 - \cos[c + dx]^2} \right) \Big/ \\
& \left( \left( -5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \\
& \cos[c + dx]^2 \Big) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \Big) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
& \text{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] + \\
& \left. \left. \text{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] \right) \right) \Big/ \\
& \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + dx]^2
\end{aligned}$$

Problem 602: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos[c + dx])^{3/2} (a + b \sin[c + dx])^3} dx$$

Optimal (type 4, 596 leaves, 15 steps):

$$\begin{aligned}
& \frac{5 b^{3/2} (7 a^2 + 2 b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 (-a^2+b^2)^{13/4} d e^{3/2}} - \frac{5 b^{3/2} (7 a^2 + 2 b^2) \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 (-a^2+b^2)^{13/4} d e^{3/2}} - \\
& \frac{a (8 a^2 + 37 b^2) \sqrt{e \cos[c+d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c+d x), 2 \right]}{4 (a^2-b^2)^3 d e^2 \sqrt{\cos[c+d x]}} - \\
& \left( 5 a b (7 a^2 + 2 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\
& \left( 8 (a^2-b^2)^3 \left( b - \sqrt{-a^2+b^2} \right) d e \sqrt{e \cos[c+d x]} \right) - \\
& \left( 5 a b (7 a^2 + 2 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\
& \left( 8 (a^2-b^2)^3 \left( b + \sqrt{-a^2+b^2} \right) d e \sqrt{e \cos[c+d x]} \right) + \\
& \frac{b}{2 (a^2-b^2) d e \sqrt{e \cos[c+d x]} (a+b \sin[c+d x])^2} + \\
& \frac{9 a b}{4 (a^2-b^2)^2 d e \sqrt{e \cos[c+d x]} (a+b \sin[c+d x])} - \frac{5 b (7 a^2 + 2 b^2) - a (8 a^2 + 37 b^2) \sin[c+d x]}{4 (a^2-b^2)^3 d e \sqrt{e \cos[c+d x]}}
\end{aligned}$$

Result (type 6, 1316 leaves):

$$\begin{aligned}
& - \frac{1}{8 (a-b)^3 (a+b)^3 d (\cos[c+d x])^{3/2}} \\
& \cos[c+d x]^{3/2} \left( \frac{1}{12 \sqrt{1 - \cos[c+d x]^2} (a+b \sin[c+d x])} (8 a^4 + 72 a^2 b^2 + 10 b^4) \right. \\
& \left( a + b \sqrt{1 - \cos[c+d x]^2} \right) \left( - \left( \left( 56 a (a^2-b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2 \right] \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right) \cos[c+d x]^{3/2} \right) / \left( \sqrt{1 - \cos[c+d x]^2} \right. \\
& \left( 7 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - \right. \\
& \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. (-a^2+b^2) \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \\
& \left. \cos[c+d x]^2 \left( a^2+b^2 (-1 + \cos[c+d x]^2) \right) \right) - \\
& \left( (3+3 \text{i}) \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1+\text{i}) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ \right. \right. \right. \\
& \left. \left. \left. 1 + \frac{(1+\text{i}) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[ \sqrt{-a^2+b^2} - (1+\text{i}) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \\
& \left. \left. \left. \right] \right)
\end{aligned}$$

$$\begin{aligned}
& \frac{\sqrt{\cos[c + dx]} + i b \cos[c + dx]}{\left(1 - \cos[c + dx]^2\right) (a + b \sin[c + dx])} \frac{2 (8 a^3 b + 37 a b^3) \left(a + b \sqrt{1 - \cos[c + dx]^2}\right)}{\left(\sqrt{b} (-a^2 + b^2)^{1/4}\right) \sin[c + dx]} - \\
& \left( \left( 7 b (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] \right. \right. \\
& \left. \left. \cos[c + dx]^{3/2} \sqrt{1 - \cos[c + dx]^2} \right) \right/ \\
& \left( 3 \left( -7 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] + 2 \right. \right. \\
& \left. \left( 2 b^2 \text{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2}\right] \right) \right. \\
& \left. \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \\
& \left( a \left( -2 \text{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}}\right] + 2 \text{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}}\right] \right. \right. \\
& \left. \left. \log\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]}\right] + b \cos[c + dx] \right) - \right. \\
& \left. \left. \log\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]}\right] + b \cos[c + dx] \right) \right) \right/ \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[c + dx]^2 \right) + \\
& \left( \cos[c + dx]^2 \left( -\frac{b^3 \cos[c + dx]}{2 (a^2 - b^2)^2 (a + b \sin[c + dx])^2} - \frac{13 a b^3 \cos[c + dx]}{4 (a^2 - b^2)^3 (a + b \sin[c + dx])} \right) \right. \right. \\
& \left. \left. \frac{1}{(a^2 - b^2)^3} \right) \right. \\
& \left. 2 \sec[c + dx] \right. \\
& \left. \left( -3 a^2 b - b^3 + a^3 \sin[c + dx] + 3 a b^2 \sin[c + dx] \right) \right) \right) \right/ \left( d (e \right. \\
& \left. \cos[c + dx])^{3/2} \right)
\end{aligned}$$

Problem 603: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos [c + d x])^{5/2} (a + b \sin [c + d x])^3} dx$$

Optimal (type 4, 614 leaves, 15 steps):

$$\begin{aligned}
 & -\frac{7 b^{5/2} (9 a^2 + 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 (-a^2+b^2)^{15/4} d e^{5/2}} - \frac{7 b^{5/2} (9 a^2 + 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 (-a^2+b^2)^{15/4} d e^{5/2}} + \\
 & \frac{a (8 a^2 + 69 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{12 (a^2-b^2)^3 d e^2 \sqrt{e \cos[c+d x]}} - \\
 & \left(7 a b^2 (9 a^2 + 2 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
 & \left(8 (a^2-b^2)^3 \left(a^2-b \left(b-\sqrt{-a^2+b^2}\right)\right) d e^2 \sqrt{e \cos[c+d x]}\right) - \\
 & \left(7 a b^2 (9 a^2 + 2 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
 & \left(8 (a^2-b^2)^3 \left(a^2-b \left(b+\sqrt{-a^2+b^2}\right)\right) d e^2 \sqrt{e \cos[c+d x]}\right) + \\
 & \frac{b}{2 (a^2-b^2) d e (\cos[c+d x])^{3/2} (a+b \sin[c+d x])^2} + \\
 & \frac{11 a b}{4 (a^2-b^2)^2 d e (\cos[c+d x])^{3/2} (a+b \sin[c+d x])} - \\
 & \frac{7 b (9 a^2 + 2 b^2) - a (8 a^2 + 69 b^2) \sin[c+d x]}{12 (a^2-b^2)^3 d e (\cos[c+d x])^{3/2}}
 \end{aligned}$$

Result (type 6, 1308 leaves):

$$\begin{aligned}
 & \frac{1}{24 (a-b)^3 (a+b)^3 d (\cos[c+d x])^{5/2}} \cos[c+d x]^{5/2} \\
 & \left( -\frac{1}{\sqrt{1-\cos[c+d x]^2}} \frac{2 (8 a^4 - 120 a^2 b^2 - 42 b^4) \left(a+b \sqrt{1-\cos[c+d x]^2}\right)}{(a+b \sin[c+d x])} \right. \\
 & \left( 5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos[c+d x]}\right) / \\
 & \left( \sqrt{1-\cos[c+d x]^2} \right. \\
 & \left( 5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] - 2 \right. \\
 & \left( 2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] + (-a^2+b^2) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right]\right) \cos[c+d x]^2 \\
 & \left. \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8}\right) \sqrt{b} \right)
 \end{aligned}$$

$$\begin{aligned}
& \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + \right. \\
& \quad \left. \operatorname{Log} \left[ \sqrt{-a^2 + b^2} - (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] - \right. \\
& \quad \left. \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] \right) \\
& \quad \frac{\sin[c + d x] - \frac{1}{(1 - \cos[c + d x]^2) (a + b \sin[c + d x])}}{2 (8 a^3 b + 69 a b^3) \left( a + b \sqrt{1 - \cos[c + d x]^2} \right)} \\
& \quad \left( \left( 5 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \quad \left. \left. \sqrt{\cos[c + d x]} \sqrt{1 - \cos[c + d x]^2} \right) / \right. \\
& \quad \left( \left( -5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \quad \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
& \quad \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \right) + \\
& \quad \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
& \quad \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] + \right. \right. \\
& \quad \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \right) / \\
& \quad \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + d x]^2 + \\
& \quad \left( \cos[c + d x]^3 \left( -\frac{b^3}{2 (a^2 - b^2)^2 (a + b \sin[c + d x])^2} - \right. \right. \\
& \quad \left. \left. \frac{15 a b^3}{4 (a^2 - b^2)^3 (a + b \sin[c + d x])} + \right. \right. \\
& \quad \left. \left. \frac{1}{3 (a^2 - b^2)^3} \right. \right. \\
& \quad \left. \left. 2 \sec[c + d x]^2 \right. \right. \\
& \quad \left. \left. (-3 a^2 b - b^3 + a^3 \sin[c + d x] + 3 a b^2 \sin[c + d x]) \right) \right) / \left( d (e \cos[c + d x])^{5/2} \right)
\end{aligned}$$

Problem 604: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(\cos[c+dx])^{7/2} (\sin[c+dx])^3} dx$$

Optimal (type 4, 685 leaves, 16 steps):

$$\begin{aligned} & \frac{9 b^{7/2} (11 a^2 + 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 (-a^2+b^2)^{17/4} d e^{7/2}} - \frac{9 b^{7/2} (11 a^2 + 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 (-a^2+b^2)^{17/4} d e^{7/2}} \\ & \left(3 a (8 a^4 - 64 a^2 b^2 - 139 b^4) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2} (c+dx), 2\right]\right) / \\ & \left(20 (a^2 - b^2)^4 d e^4 \sqrt{\cos[c+dx]}\right) + \\ & \left(9 a b^3 (11 a^2 + 2 b^2) \sqrt{\cos[c+dx]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+dx), 2\right]\right) / \\ & \left(8 (a^2 - b^2)^4 \left(b - \sqrt{-a^2 + b^2}\right) d e^3 \sqrt{\cos[c+dx]}\right) + \\ & \left(9 a b^3 (11 a^2 + 2 b^2) \sqrt{\cos[c+dx]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+dx), 2\right]\right) / \\ & \left(8 (a^2 - b^2)^4 \left(b + \sqrt{-a^2 + b^2}\right) d e^3 \sqrt{\cos[c+dx]}\right) + \\ & \frac{b}{2 (a^2 - b^2) d e (\cos[c+dx])^{5/2} (\sin[c+dx])^2} + \\ & \frac{13 a b}{4 (a^2 - b^2)^2 d e (\cos[c+dx])^{5/2} (\sin[c+dx])} - \\ & \frac{9 b (11 a^2 + 2 b^2) - a (8 a^2 + 109 b^2) \sin[c+dx]}{20 (a^2 - b^2)^3 d e (\cos[c+dx])^{5/2}} + \\ & \frac{3 (15 b^3 (11 a^2 + 2 b^2) + a (8 a^4 - 64 a^2 b^2 - 139 b^4) \sin[c+dx])}{20 (a^2 - b^2)^4 d e^3 \sqrt{\cos[c+dx]}} \end{aligned}$$

Result (type 6, 1408 leaves):

$$\begin{aligned} & -\frac{1}{40 (a-b)^4 (a+b)^4 d (\cos[c+dx])^{7/2}} \\ & -\frac{3 \cos[c+dx]^{7/2} \left(\frac{1}{12 \sqrt{1 - \cos[c+dx]^2} (\sin[c+dx])}\right)}{\left(8 a^6 - 64 a^4 b^2 - 304 a^2 b^4 - 30 b^6\right) \left(a + b \sqrt{1 - \cos[c+dx]^2}\right)} \\ & \left(-\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2 + b^2}\right]\right)\right) \end{aligned}$$



Problem 605: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{15/2}}{(a + b \sin [c + d x])^4} dx$$

Optimal (type 4, 671 leaves, 16 steps):

$$\begin{aligned}
& \frac{39 a (11 a^4 - 17 a^2 b^2 + 6 b^4) e^{15/2} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{16 b^{15/2} (-a^2+b^2)^{3/4} d} + \\
& \frac{39 a (11 a^4 - 17 a^2 b^2 + 6 b^4) e^{15/2} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{16 b^{15/2} (-a^2+b^2)^{3/4} d} + \\
& \left( 13 (231 a^4 - 203 a^2 b^2 + 20 b^4) e^8 \sqrt{\cos [c+d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c+d x), 2 \right] \right) / \\
& \left( 56 b^8 d \sqrt{e \cos [c+d x]} \right) - \\
& \left( 39 a^2 (11 a^4 - 17 a^2 b^2 + 6 b^4) e^8 \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\
& \left( 16 b^8 \left( a^2 - b \left( b - \sqrt{-a^2+b^2} \right) \right) d \sqrt{e \cos [c+d x]} \right) - \\
& \left( 39 a^2 (11 a^4 - 17 a^2 b^2 + 6 b^4) e^8 \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\
& \left( 16 b^8 \left( a^2 - b \left( b + \sqrt{-a^2+b^2} \right) \right) d \sqrt{e \cos [c+d x]} \right) - \\
& \frac{e (e \cos [c+d x])^{13/2}}{3 b d (a+b \sin [c+d x])^3} - \frac{13 e^3 (e \cos [c+d x])^{9/2} (11 a + 4 b \sin [c+d x])}{84 b^3 d (a+b \sin [c+d x])^2} - \\
& \frac{39 e^5 (e \cos [c+d x])^{5/2} (77 a^2 - 20 b^2 + 22 a b \sin [c+d x])}{280 b^5 d (a+b \sin [c+d x])} + \frac{1}{56 b^7 d} \\
& 13 e^7 \sqrt{e \cos [c+d x]} (21 a (11 a^2 - 6 b^2) - b (77 a^2 - 20 b^2) \sin [c+d x])
\end{aligned}$$

Result (type 6, 2302 leaves):

$$\begin{aligned}
& \frac{1}{560 b^7 d \cos [c+d x]^{15/2}} (e \cos [c+d x])^{15/2} \\
& \left( - \frac{1}{\sqrt{1 - \cos [c+d x]^2} (a+b \sin [c+d x])} 2 (4410 a^3 b - 3418 a b^3) \left( a + b \sqrt{1 - \cos [c+d x]^2} \right) \right. \\
& \left( \left( 5 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos [c+d x]} \right) / \right. \\
& \left. \left( \sqrt{1 - \cos [c+d x]^2} \right. \right. \\
& \left. \left( 5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - 2 \right. \\
& \left. \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \\
& \left. \left. \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \left( a^2 + b^2 (-1 + \cos[c + d x]^2) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left( \frac{1}{8} - \frac{\frac{1}{2}}{8} \right) \sqrt{b} \\
& \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1 + \frac{1}{2}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1 + \frac{1}{2}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + \right. \\
& \left. \operatorname{Log} \left[ \sqrt{-a^2 + b^2} - (1 + \frac{1}{2}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \frac{1}{2} b \cos[c + d x] \right] - \right. \\
& \left. \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + (1 + \frac{1}{2}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \frac{1}{2} b \cos[c + d x] \right] \right) \\
& \frac{1}{\sin[c + d x] + \frac{1}{\sqrt{1 - \cos[c + d x]^2} (-1 + 2 \cos[c + d x]^2) (a + b \sin[c + d x])}} \\
& \left( 5600 a^3 b - 3472 a b^3 \right) \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \cos[2 (c + d x)] \\
& \left( \frac{1}{2} - \frac{\frac{1}{2}}{2} \right) \left( -2 a^2 + b^2 \right) \operatorname{ArcTan} \left[ 1 - \frac{(1 + \frac{1}{2}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \\
& \frac{b^{3/2} (-a^2 + b^2)^{3/4}}{\left( \frac{1}{2} - \frac{\frac{1}{2}}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[ 1 + \frac{(1 + \frac{1}{2}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right]} + \frac{4 \sqrt{\cos[c + d x]}}{b} + \\
& \left( 10 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \sqrt{\cos[c + d x]} \right) / \\
& \left( \sqrt{1 - \cos[c + d x]^2} \left( 5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) - \\
& \left( 36 a (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right. \\
& \left. \cos[c + d x]^{5/2} \right) / \left( 5 \sqrt{1 - \cos[c + d x]^2} \right. \\
& \left. \left( 9 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] - \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right. \\
& \left. \left. \operatorname{AppellF1} \left[ \frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \cos[c + d x]^2 \right) \\
& \left( a^2 + b^2 (-1 + \cos[c + d x]^2) \right) + \left( \left( \frac{1}{4} - \frac{\frac{1}{2}}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[ \sqrt{-a^2 + b^2} - \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \left( \left( 1 + \frac{i}{4} \right) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \frac{i}{4} b \cos[c + d x] \right) \right/ \left( b^{3/2} (-a^2 + b^2)^{3/4} \right) - \\
& \left. \left( \left( \frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \text{Log} \left[ \sqrt{-a^2 + b^2} + \left( 1 + \frac{i}{4} \right) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} \right] + \right. \right. \\
& \left. \left. \frac{i}{4} b \cos[c + d x] \right) \right/ \left( b^{3/2} (-a^2 + b^2)^{3/4} \right) \right) \sin[c + d x] - \\
& \frac{1}{(1 - \cos[c + d x]^2) (a + b \sin[c + d x])} 2 (3815 a^4 - 6251 a^2 b^2 + 1300 b^4) \\
& \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \\
& \left( \left( 5 b (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + d x]} \sqrt{1 - \cos[c + d x]^2} \right) \right/ \\
& \left( \left( -5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \\
& \cos[c + d x]^2 \left( a^2 + b^2 (-1 + \cos[c + d x]^2) \right) \right) + \\
& \left. \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
& \text{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] + \\
& \left. \left. \text{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \right) \right/ \\
& \left. \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + d x]^2 \right) + \frac{1}{d} \\
& (e \cos[c + d x])^{15/2} \sec[c + d x]^7 \left( -\frac{4 a \cos[2 (c + d x)]}{5 b^5} + \right. \\
& \frac{(-280 a^2 + 79 b^2) \sin[c + d x]}{42 b^6} - \\
& \left. \frac{(-a^2 + b^2)^3}{3 b^7 (a + b \sin[c + d x])^3} \right)
\end{aligned}$$

$$\begin{aligned} & \frac{37 a (a^2 - b^2)^2}{12 b^7 (a + b \sin[c + d x])^2} + \\ & \frac{(-a^2 + b^2) (-393 a^2 + 76 b^2)}{24 b^7 (a + b \sin[c + d x])} + \\ & \frac{\sin[3 (c + d x)]}{14 b^4} \end{aligned}$$

**Problem 606: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(e \cos[c + d x])^{13/2}}{(a + b \sin[c + d x])^4} dx$$

Optimal (type 4, 557 leaves, 15 steps):

$$\begin{aligned} & \frac{77 a (3 a^2 - 2 b^2) e^{13/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{16 b^{13/2} (-a^2 + b^2)^{1/4} d} - \frac{77 a (3 a^2 - 2 b^2) e^{13/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{16 b^{13/2} (-a^2 + b^2)^{1/4} d} - \\ & \frac{77 (15 a^2 - 4 b^2) e^6 \sqrt{e \cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{40 b^6 d \sqrt{\cos[c + d x]}} + \\ & \left(77 a^2 (3 a^2 - 2 b^2) e^7 \sqrt{\cos[c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]\right) / \\ & \left(16 b^7 \left(b - \sqrt{-a^2 + b^2}\right) d \sqrt{e \cos[c + d x]}\right) + \\ & \left(77 a^2 (3 a^2 - 2 b^2) e^7 \sqrt{\cos[c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]\right) / \\ & \left(16 b^7 \left(b + \sqrt{-a^2 + b^2}\right) d \sqrt{e \cos[c + d x]}\right) - \\ & \frac{e (e \cos[c + d x])^{11/2}}{3 b d (a + b \sin[c + d x])^3} - \frac{11 e^3 (e \cos[c + d x])^{7/2} (9 a + 4 b \sin[c + d x])}{60 b^3 d (a + b \sin[c + d x])^2} - \\ & \frac{77 e^5 (e \cos[c + d x])^{3/2} (15 a^2 - 4 b^2 + 6 a b \sin[c + d x])}{120 b^5 d (a + b \sin[c + d x])} \end{aligned}$$

Result (type 6, 1331 leaves):

$$\begin{aligned} & -\frac{1}{80 b^5 d \cos[c + d x]^{13/2}} \\ & 77 (e \cos[c + d x])^{13/2} \left( \frac{1}{2 \sqrt{1 - \cos[c + d x]^2} (a + b \sin[c + d x])} a b \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \right. \\ & \left. - \left( \left( 56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
& \left. \cos[(c+dx)^{3/2}] \right/ \left( \sqrt{1 - \cos[(c+dx)^2]} \left( 7(a^2-b^2) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2+b^2} \right] - 2 \left( 2b^2 \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2+b^2} \right] + (-a^2+b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2+b^2} \right] \right) \cos[(c+dx)^2] \left( a^2+b^2 (-1+\cos[(c+dx)^2]) \right) \right) \right) - \\
& \left( (3+3i) \left( 2 \text{ArcTan}\left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[(c+dx)^2]}}{(-a^2+b^2)^{1/4}}\right] - 2 \text{ArcTan}\left[1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[(c+dx)^2]}}{(-a^2+b^2)^{1/4}}\right] - \text{Log}\left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b}(-a^2+b^2)^{1/4}\right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[(c+dx)^2]} + i b \cos[(c+dx)^2]\right] + \text{Log}\left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b}(-a^2+b^2)^{1/4}\right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[(c+dx)^2]} + i b \cos[(c+dx)^2]\right] \right) \right) \left/ \left( \sqrt{b} (-a^2+b^2)^{1/4} \right) \right. \sin[(c+dx)^2] - \\
& \frac{1}{(1-\cos[(c+dx)^2]) (a+b \sin[(c+dx)^2])} 2 (15a^2-4b^2) \left( a+b \sqrt{1-\cos[(c+dx)^2]} \right) \\
& \left( 7b(a^2-b^2) \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2+b^2} \right] \right. \\
& \left. \cos[(c+dx)^{3/2} \sqrt{1-\cos[(c+dx)^2]}\right) \left/ \right. \\
& \left( 3 \left( -7(a^2-b^2) \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2+b^2} \right] + 2 \right. \right. \\
& \left. \left( 2b^2 \text{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. \left. (a^2-b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[(c+dx)^2], \frac{b^2 \cos[(c+dx)^2]}{-a^2+b^2} \right] \right) \right. \\
& \left. \cos[(c+dx)^2] \left( a^2+b^2 (-1+\cos[(c+dx)^2]) \right) \right) + \\
& \left( a \left( -2 \text{ArcTan}\left[1 - \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[(c+dx)^2]}}{(a^2-b^2)^{1/4}}\right] + 2 \text{ArcTan}\left[1 + \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[(c+dx)^2]}}{(a^2-b^2)^{1/4}}\right] + \right. \right. \\
& \left. \left. \text{Log}\left[\sqrt{a^2-b^2} - \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[(c+dx)^2]} + b \cos[(c+dx)^2]\right] - \text{Log}\left[\sqrt{a^2-b^2} + \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[(c+dx)^2]} + b \cos[(c+dx)^2]\right] \right) \right) \right/ \\
& \left( 4\sqrt{2}b^{3/2}(a^2-b^2)^{1/4} \right) \sin[(c+dx)^2] + \frac{1}{d} \\
& (e \cos[(c+dx)])^{13/2} \sec[(c+dx)]^6 \left( -\frac{8a \cos[(c+dx)]}{3b^5} + \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{-a^4 \cos[c+d x] + 2 a^2 b^2 \cos[c+d x] - b^4 \cos[c+d x]}{3 b^5 (a+b \sin[c+d x])^3} + \\
& \frac{9 (a^3 \cos[c+d x] - a b^2 \cos[c+d x])}{4 b^5 (a+b \sin[c+d x])^2} + \\
& \frac{-71 a^2 \cos[c+d x] + 20 b^2 \cos[c+d x]}{8 b^5 (a+b \sin[c+d x])} + \\
& \frac{\sin[2 (c+d x)]}{5 b^4}
\end{aligned}$$

Problem 607: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c+d x])^{11/2}}{(a+b \sin[c+d x])^4} \, dx$$

Optimal (type 4, 571 leaves, 15 steps):

$$\begin{aligned}
& -\frac{15 a (7 a^2 - 6 b^2) e^{11/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{11/2} (-a^2+b^2)^{3/4} d} - \frac{15 a (7 a^2 - 6 b^2) e^{11/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{11/2} (-a^2+b^2)^{3/4} d} - \\
& \frac{5 (21 a^2 - 4 b^2) e^6 \sqrt{\cos[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{8 b^6 d \sqrt{e \cos[c+d x]}} + \\
& \left(15 a^2 (7 a^2 - 6 b^2) e^6 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
& \left(16 b^6 \left(a^2 - b \left(b - \sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos[c+d x]}\right) + \\
& \left(15 a^2 (7 a^2 - 6 b^2) e^6 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
& \left(16 b^6 \left(a^2 - b \left(b + \sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos[c+d x]}\right) - \\
& \frac{e (e \cos[c+d x])^{9/2}}{3 b d (a+b \sin[c+d x])^3} - \frac{e^3 (e \cos[c+d x])^{5/2} (7 a + 4 b \sin[c+d x])}{4 b^3 d (a+b \sin[c+d x])^2} - \\
& \frac{5 e^5 \sqrt{e \cos[c+d x]} (21 a^2 - 4 b^2 + 14 a b \sin[c+d x])}{8 b^5 d (a+b \sin[c+d x])}
\end{aligned}$$

Result (type 6, 2220 leaves):

$$\begin{aligned}
& \frac{1}{d} (e \cos[c+d x])^{11/2} \operatorname{Sec}[c+d x]^5 \left( \frac{2 \sin[c+d x]}{3 b^4} - \right. \\
& \left. \frac{(-a^2+b^2)^2}{3 b^5 (a+b \sin[c+d x])^3} + \frac{25 a (a^2-b^2)}{12 b^5 (a+b \sin[c+d x])^2} + \frac{-165 a^2+52 b^2}{24 b^5 (a+b \sin[c+d x])} \right) -
\end{aligned}$$



$$\begin{aligned}
& \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \Big] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \right. \\
& \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \Big] \Big) \cos[c+d x]^2 \Big) \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) \Big) - \\
& \left( 36 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right. \\
& \left. \cos[c+d x]^{5/2} \right) \Big/ \left( 5 \sqrt{1-\cos[c+d x]^2} \right. \\
& \left. \left( 9 (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) \\
& \left. \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) \right) + \left( \left( \frac{1}{4} - \frac{i}{4} \right) (-2 a^2+b^2) \operatorname{Log}\left[\sqrt{-a^2+b^2} - \right. \right. \\
& \left. \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x] \right] \right) \Big/ \left( b^{3/2} (-a^2+b^2)^{3/4} \right) - \\
& \left. \left( \left( \frac{1}{4} - \frac{i}{4} \right) (-2 a^2+b^2) \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + \right. \right. \right. \\
& \left. \left. \left. i b \cos[c+d x] \right] \right) \Big/ \left( b^{3/2} (-a^2+b^2)^{3/4} \right) \right) \sin[c+d x] - \\
& \frac{1}{(1-\cos[c+d x]^2) (a+b \sin[c+d x])} 2 (41 a^2 - 20 b^2) \left( a + b \sqrt{1-\cos[c+d x]^2} \right) \\
& \left( \left( 5 b (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c+d x]} \sqrt{1-\cos[c+d x]^2} \right) \Big/ \\
& \left( \left( -5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \right. \\
& \left. \left. \cos[c+d x]^2 \right) \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) \right) + \\
& \left( a \left( -2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c+d x]}}{(a^2-b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c+d x]}}{(a^2-b^2)^{1/4}}\right] \right) - \right. \\
& \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[c+d x]} + b \cos[c+d x] \right] + \right. \right.
\end{aligned}$$

Problem 608: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{9/2}}{(a + b \sin [c + d x])^4} dx$$

Optimal (type 4, 591 leaves, 15 steps):

$$\begin{aligned}
& \frac{7 a \left(5 a^2 - 6 b^2\right) e^{9/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{9/2} (-a^2+b^2)^{5/4} d} - \frac{7 a \left(5 a^2 - 6 b^2\right) e^{9/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{9/2} (-a^2+b^2)^{5/4} d} + \\
& \frac{7 \left(5 a^2 - 4 b^2\right) e^4 \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{8 b^4 (a^2-b^2) d \sqrt{\cos [c+d x]}} - \\
& \left(7 a^2 \left(5 a^2 - 6 b^2\right) e^5 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
& \left(16 b^5 (a^2-b^2) \left(b - \sqrt{-a^2+b^2}\right) d \sqrt{e \cos [c+d x]}\right) - \\
& \left(7 a^2 \left(5 a^2 - 6 b^2\right) e^5 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
& \left(16 b^5 (a^2-b^2) \left(b + \sqrt{-a^2+b^2}\right) d \sqrt{e \cos [c+d x]}\right) - \frac{e \left(e \cos [c+d x]\right)^{7/2}}{3 b d \left(a + b \sin [c+d x]\right)^3} + \\
& \frac{7 \left(5 a^2 - 4 b^2\right) e^3 \left(e \cos [c+d x]\right)^{3/2}}{8 b^3 (a^2-b^2) d \left(a + b \sin [c+d x]\right)} - \frac{7 e^3 \left(e \cos [c+d x]\right)^{3/2} \left(5 a + 4 b \sin [c+d x]\right)}{12 b^3 d \left(a + b \sin [c+d x]\right)^2}
\end{aligned}$$

### Result (type 6, 1294 leaves):

$$\begin{aligned}
& \frac{1}{d} \left( e \cos [c + dx] \right)^{9/2} \sec^4 [c + dx] \left( \frac{a^2 \cos [c + dx] - b^2 \cos [c + dx]}{3 b^3 (a + b \sin [c + dx])^3} - \frac{5 a \cos [c + dx]}{4 b^3 (a + b \sin [c + dx])^2} + \right. \\
& \left. \frac{-19 a^2 \cos [c + dx] + 12 b^2 \cos [c + dx]}{8 b^3 (-a^2 + b^2) (a + b \sin [c + dx])} \right) + \frac{1}{16 (a - b) b^3 (a + b) d \cos [c + dx]^{9/2}} \\
& 7 \left( e \cos [c + dx] \right)^{9/2} \left( \frac{1}{6 \sqrt{1 - \cos [c + dx]^2} (a + b \sin [c + dx])} a b \left( a + b \sqrt{1 - \cos [c + dx]^2} \right) \right. \\
& \left. - \left( \left( 56 a (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c + dx]^2, \frac{b^2 \cos [c + dx]^2}{-a^2 + b^2} \right] \cos [c + dx]^{3/2} \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{1 - \cos[c + dx]^2} \left( 7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c + dx]^2, \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) - \\
& \left( (3 + 3 i) \left( 2 \text{ArcTan} \left[ 1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \text{ArcTan} \left[ \right. \right. \right. \\
& \left. \left. \left. 1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}} \right] - \text{Log} \left[ \sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
& \left. \left. \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] + \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
& \left. \left. \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] \right) \right) \left/ \left( \sqrt{b} (-a^2 + b^2)^{1/4} \right) \right) \sin[c + dx] - \\
& \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 2 (5 a^2 - 4 b^2) \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( \left( 7 b (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \cos[c + dx]^{3/2} \sqrt{1 - \cos[c + dx]^2} \right) \right) \left/ \right. \\
& \left( 3 \left( -7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \\
& \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
& \left. \left. \text{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] - \right. \right. \\
& \left. \left. \text{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] \right) \right) \left/ \right. \\
& \left. \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[c + dx]^2 \right)
\end{aligned}$$

Problem 609: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^{7/2}}{(a + b \sin[c + d x])^4} dx$$

Optimal (type 4, 597 leaves, 15 steps):

$$\begin{aligned} & -\frac{5 a (a^2 - 2 b^2) e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{7/2} (-a^2+b^2)^{7/4} d} - \frac{5 a (a^2 - 2 b^2) e^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{7/2} (-a^2+b^2)^{7/4} d} + \\ & \frac{5 (3 a^2 - 4 b^2) e^4 \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{24 b^4 (a^2 - b^2) d \sqrt{e \cos[c + d x]}} - \\ & \left(5 a^2 (a^2 - 2 b^2) e^4 \sqrt{\cos[c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]\right) / \\ & \left(16 b^4 (a^2 - b^2) \left(a^2 - b \left(b - \sqrt{-a^2 + b^2}\right)\right) d \sqrt{e \cos[c + d x]}\right) - \\ & \left(5 a^2 (a^2 - 2 b^2) e^4 \sqrt{\cos[c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]\right) / \\ & \left(16 b^4 (a^2 - b^2) \left(a^2 - b \left(b + \sqrt{-a^2 + b^2}\right)\right) d \sqrt{e \cos[c + d x]}\right) - \frac{e (e \cos[c + d x])^{5/2}}{3 b d (a + b \sin[c + d x])^3} - \\ & \frac{5 (3 a^2 - 4 b^2) e^3 \sqrt{e \cos[c + d x]}}{24 b^3 (a^2 - b^2) d (a + b \sin[c + d x])} + \frac{5 e^3 \sqrt{e \cos[c + d x]} (3 a + 4 b \sin[c + d x])}{12 b^3 d (a + b \sin[c + d x])^2} \end{aligned}$$

Result (type 6, 1263 leaves):

$$\begin{aligned} & \frac{1}{d} (e \cos[c + d x])^{7/2} \operatorname{Sec}[c + d x]^3 \\ & \left( \frac{a^2 - b^2}{3 b^3 (a + b \sin[c + d x])^3} - \frac{13 a}{12 b^3 (a + b \sin[c + d x])^2} + \frac{-33 a^2 + 28 b^2}{24 b^3 (-a^2 + b^2) (a + b \sin[c + d x])} \right) + \\ & \frac{1}{48 (a - b) b^3 (a + b) d \cos[c + d x]^{7/2}} \\ & 5 (e \cos[c + d x])^{7/2} \left( -\frac{1}{\sqrt{1 - \cos[c + d x]^2} (a + b \sin[c + d x])} 4 a b \left(a + b \sqrt{1 - \cos[c + d x]^2}\right) \right. \\ & \left. \left( 5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] \sqrt{\cos[c + d x]}\right) \right) / \\ & \left( \sqrt{1 - \cos[c + d x]^2} \left( 5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] - 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2}\right] \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
& \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \Big) \cos[c + dx]^2 \Big) \left( a^2 + b^2 \left( -1 + \cos[c + dx]^2 \right) \right) \Big) - \\
& \frac{1}{(-a^2 + b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}} \right] - \right. \\
& \left. 2 \operatorname{ArcTan} \left[ 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}} \right] + \operatorname{Log} \left[ \sqrt{-a^2 + b^2} - (1+i) \sqrt{b} \right. \right. \\
& \left. \left. (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] - \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + (1+i) \sqrt{b} \right. \right. \\
& \left. \left. \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + i b \cos[c + dx] \right] \right) \Big) \sin[c + dx] - \\
& \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 2 (3 a^2 - 4 b^2) \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( \left( 5 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + dx]} \sqrt{1 - \cos[c + dx]^2} \right) \Big/ \right. \\
& \left. \left( \left( -5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \right. \right. \\
& \left. \left. \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) + \\
& \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
& \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] \right) \right) \Big/ \\
& \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + dx]^2 \Big)
\end{aligned}$$

Problem 610: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + dx])^{5/2}}{(a + b \sin[c + dx])^4} dx$$

Optimal (type 4, 574 leaves, 15 steps):

$$\begin{aligned}
& -\frac{a (a^2 - 6 b^2) e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{5/2} (-a^2+b^2)^{9/4} d} + \frac{a (a^2 - 6 b^2) e^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{5/2} (-a^2+b^2)^{9/4} d} + \\
& \frac{(a^2 + 4 b^2) e^2 \sqrt{e \cos[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{8 b^2 (a^2 - b^2)^2 d \sqrt{\cos[c+d x]}} - \\
& \frac{a^2 (a^2 - 6 b^2) e^3 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{16 b^3 (a^2 - b^2)^2 \left(b - \sqrt{-a^2+b^2}\right) d \sqrt{e \cos[c+d x]}} - \\
& \frac{a^2 (a^2 - 6 b^2) e^3 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{16 b^3 (a^2 - b^2)^2 \left(b + \sqrt{-a^2+b^2}\right) d \sqrt{e \cos[c+d x]}} - \frac{e (e \cos[c+d x])^{3/2}}{3 b d (a+b \sin[c+d x])^3} + \\
& \frac{a e (e \cos[c+d x])^{3/2}}{4 b (a^2 - b^2) d (a+b \sin[c+d x])^2} + \frac{(a^2 + 4 b^2) e (e \cos[c+d x])^{3/2}}{8 b (a^2 - b^2)^2 d (a+b \sin[c+d x])}
\end{aligned}$$

Result (type 6, 1286 leaves) :

$$\begin{aligned}
& \frac{1}{d} (e \cos[c+d x])^{5/2} \operatorname{Sec}[c+d x]^2 \left( -\frac{\cos[c+d x]}{3 b (a+b \sin[c+d x])^3} - \frac{a \cos[c+d x]}{4 b (-a^2+b^2) (a+b \sin[c+d x])^2} + \right. \\
& \left. \frac{a^2 \cos[c+d x] + 4 b^2 \cos[c+d x]}{8 b (-a^2+b^2)^2 (a+b \sin[c+d x])} \right) + \frac{1}{16 (a-b)^2 b (a+b)^2 d \cos[c+d x]^{5/2}} \\
& (e \cos[c+d x])^{5/2} \left( \frac{1}{6 \sqrt{1-\cos[c+d x]^2} (a+b \sin[c+d x])} - 5 a b \left(a+b \sqrt{1-\cos[c+d x]^2}\right) \right. \\
& \left. - \left( \left( 56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2}\right] \cos[c+d x]^{3/2} \right) / \right. \\
& \left. \left( \sqrt{1-\cos[c+d x]^2} \left( 7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) (a^2 + b^2 (-1 + \cos[c+d x]^2)) \right) - \\
& \left( (3 + 3 \frac{i}{2}) \left( 2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4}\right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c+d x]} + i b \cos[c+d x]\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4}\right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c+d x]}\right]\right)
\end{aligned}$$

Problem 611: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{3/2}}{(a + b \sin [c + d x])^4} dx$$

Optimal (type 4, 592 leaves, 15 steps):

$$\begin{aligned}
& -\frac{a (a^2 + 6 b^2) e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{3/2} (-a^2+b^2)^{11/4} d} - \frac{a (a^2 + 6 b^2) e^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{3/2} (-a^2+b^2)^{11/4} d} - \\
& \frac{(3 a^2 + 4 b^2) e^2 \sqrt{\cos[c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{24 b^2 (a^2-b^2)^2 d \sqrt{e \cos[c+d x]}} + \\
& \frac{a^2 (a^2 + 6 b^2) e^2 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{16 b^2 (a^2-b^2)^2 (a^2-b (b-\sqrt{-a^2+b^2})) d \sqrt{e \cos[c+d x]}} + \\
& \frac{a^2 (a^2 + 6 b^2) e^2 \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{16 b^2 (a^2-b^2)^2 (a^2-b (b+\sqrt{-a^2+b^2})) d \sqrt{e \cos[c+d x]}} - \frac{e \sqrt{e \cos[c+d x]}}{3 b d (a+b \sin[c+d x])^3} + \\
& \frac{a e \sqrt{e \cos[c+d x]}}{12 b (a^2-b^2) d (a+b \sin[c+d x])^2} + \frac{(3 a^2 + 4 b^2) e \sqrt{e \cos[c+d x]}}{24 b (a^2-b^2)^2 d (a+b \sin[c+d x])}
\end{aligned}$$

Result (type 6, 1263 leaves):

$$\begin{aligned}
& \frac{1}{d} (e \cos[c+d x])^{3/2} \operatorname{Sec}[c+d x] \left( -\frac{1}{3 b (a+b \sin[c+d x])^3} - \right. \\
& \left. \frac{a}{12 b (-a^2+b^2) (a+b \sin[c+d x])^2} + \frac{3 a^2 + 4 b^2}{24 b (-a^2+b^2)^2 (a+b \sin[c+d x])} \right) - \\
& \frac{1}{48 (a-b)^2 b (a+b)^2 d \cos[c+d x]^{3/2}} (e \cos[c+d x])^{3/2} \left( \frac{1}{\sqrt{1-\cos[c+d x]^2} (a+b \sin[c+d x])} \right. \\
& \left. 28 a b \left( a+b \sqrt{1-\cos[c+d x]^2} \right) \left( \left( 5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos[c+d x]} \right) \right) \left( \sqrt{1-\cos[c+d x]^2} \right. \\
& \left. \left( 5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \cos[c+d x]^2 \right) \right. \\
& \left. \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
& \left( 2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+d x]}}{(-a^2+b^2)^{1/4}}\right] + \right. \\
& \left. \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+d x]} + i b \cos[c+d x]\right] \right) - 
\end{aligned}$$

$$\begin{aligned}
& \text{Log} \left[ \sqrt{-a^2 + b^2} + (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + dx]} + \text{i} b \cos[c + dx] \right] \Bigg) \\
& \sin[c + dx] - \frac{1}{(1 - \cos[c + dx]^2) (a + b \sin[c + dx])} 2 (3 a^2 + 4 b^2) \\
& \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \\
& \left( \left( 5 b (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos[c + dx]} \sqrt{1 - \cos[c + dx]^2} \right) \Bigg) \\
& \left( \left( -5 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
& 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (a^2 - b^2) \right. \\
& \left. \left. \text{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) \\
& (a^2 + b^2 (-1 + \cos[c + dx]^2)) \Bigg) + \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
& 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - \text{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \right. \\
& \left. \left. \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] + \text{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \right. \right. \\
& \left. \left. \sqrt{\cos[c + dx]} + b \cos[c + dx] \right] \right) \Bigg) \Bigg/ \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + dx]^2
\end{aligned}$$

Problem 612: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{e \cos [c + d x]}}{(a + b \sin [c + d x])^4} dx$$

Optimal (type 4, 579 leaves, 15 steps):

$$\begin{aligned}
& - \frac{5 a (a^2 + 2 b^2) \sqrt{e} \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{16 \sqrt{b} (-a^2 + b^2)^{13/4} d} + \frac{5 a (a^2 + 2 b^2) \sqrt{e} \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{16 \sqrt{b} (-a^2 + b^2)^{13/4} d} + \\
& \frac{(11 a^2 + 4 b^2) \sqrt{e \cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{8 (a^2 - b^2)^3 d \sqrt{\cos [c + d x]}} + \\
& \left( 5 a^2 (a^2 + 2 b^2) e \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right] \right) / \\
& \left( 16 b (a^2 - b^2)^3 \left( b - \sqrt{-a^2 + b^2} \right) d \sqrt{e \cos [c + d x]} \right) + \\
& \left( 5 a^2 (a^2 + 2 b^2) e \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right] \right) / \\
& \left( 16 b (a^2 - b^2)^3 \left( b + \sqrt{-a^2 + b^2} \right) d \sqrt{e \cos [c + d x]} \right) + \frac{b (e \cos [c + d x])^{3/2}}{3 (a^2 - b^2) d e (a + b \sin [c + d x])^3} + \\
& \frac{3 a b (e \cos [c + d x])^{3/2}}{4 (a^2 - b^2)^2 d e (a + b \sin [c + d x])^2} + \frac{b (11 a^2 + 4 b^2) (e \cos [c + d x])^{3/2}}{8 (a^2 - b^2)^3 d e (a + b \sin [c + d x])}
\end{aligned}$$

Result (type 6, 1294 leaves):

$$\begin{aligned}
& \frac{1}{d} \sqrt{e \cos[c + dx]} \left( \frac{b \cos[c + dx]}{3 (a^2 - b^2) (a + b \sin[c + dx])^3} + \right. \\
& \left. \frac{3 a b \cos[c + dx]}{4 (a^2 - b^2)^2 (a + b \sin[c + dx])^2} - \frac{-11 a^2 b \cos[c + dx] - 4 b^3 \cos[c + dx]}{8 (a^2 - b^2)^3 (a + b \sin[c + dx])} \right) + \\
& \frac{1}{16 (a - b)^3 (a + b)^3 d \sqrt{\cos[c + dx]}} \\
& \left( \frac{1}{12 \sqrt{1 - \cos[c + dx]^2} (a + b \sin[c + dx])} (16 a^3 + 14 a b^2) \left( a + b \sqrt{1 - \cos[c + dx]^2} \right) \right. \\
& \left. \left( - \left( \left( 56 a (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \cos[c + dx]^{3/2} \right) \right. \right. \\
& \left. \left( \sqrt{1 - \cos[c + dx]^2} \left( 7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] - 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c + dx]^2, \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos[c + dx]^2}{-a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) (a^2 + b^2 (-1 + \cos[c + dx]^2)) \right) \right) - \\
& \left( (3 + 3 \frac{1}{2}) \left( 2 \text{ArcTan} \left[ 1 - \frac{(1 + \frac{1}{2}) \sqrt{b} \sqrt{\cos[c + dx]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \text{ArcTan} \left[ \right. \right. \right. \\
& \left. \left. \left. \frac{b \sqrt{1 - \cos[c + dx]^2}}{a^2 + b^2} \right] \right) \cos[c + dx]^2 \right) \cos[c + dx]^2
\end{aligned}$$

$$\begin{aligned}
& 1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \Big] - \log \left[ \sqrt{-a^2 + b^2} - (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \\
& \left. \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] + \log \left[ \sqrt{-a^2 + b^2} + (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \\
& \left. \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] \Bigg] \Bigg) \Bigg/ \left( \sqrt{b} (-a^2 + b^2)^{1/4} \right) \sin[c + d x] - \\
& \frac{1}{(1 - \cos[c + d x]^2) (a + b \sin[c + d x])} 2 (11 a^2 b + 4 b^3) \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \\
& \left( \left( 7 b (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \cos[c + d x]^{3/2} \sqrt{1 - \cos[c + d x]^2} \right) \Bigg/ \right. \\
& \left. \left( 3 \left( -7 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. 2 \left( 2 b^2 \text{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \text{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \Bigg) + \\
& \left. \left( a \left( -2 \text{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \right. \\
& \left. \left. \log \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] - \right. \right. \\
& \left. \left. \log \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \right) \Bigg) \Bigg/ \\
& \left. \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[c + d x]^2 \right)
\end{aligned}$$

Problem 613: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos[c + d x]} (a + b \sin[c + d x])^4} \, dx$$

Optimal (type 4, 593 leaves, 15 steps):

$$\begin{aligned}
& \frac{7 a \sqrt{b} (5 a^2 + 6 b^2) \operatorname{ArcTan} \left[ \frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{16 (-a^2+b^2)^{15/4} d \sqrt{e}} + \frac{7 a \sqrt{b} (5 a^2 + 6 b^2) \operatorname{ArcTanh} \left[ \frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{16 (-a^2+b^2)^{15/4} d \sqrt{e}} - \\
& \frac{(57 a^2 + 20 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c+d x), 2 \right]}{24 (a^2-b^2)^3 d \sqrt{e \cos[c+d x]}} + \\
& \left( 7 a^2 (5 a^2 + 6 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\
& \left( 16 (a^2-b^2)^3 \left( a^2 - b \left( b - \sqrt{-a^2+b^2} \right) \right) d \sqrt{e \cos[c+d x]} \right) + \\
& \left( 7 a^2 (5 a^2 + 6 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi} \left[ \frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\
& \left( 16 (a^2-b^2)^3 \left( a^2 - b \left( b + \sqrt{-a^2+b^2} \right) \right) d \sqrt{e \cos[c+d x]} \right) + \frac{b \sqrt{e \cos[c+d x]}}{3 (a^2-b^2) d e (a+b \sin[c+d x])^3} + \\
& \frac{11 a b \sqrt{e \cos[c+d x]}}{12 (a^2-b^2)^2 d e (a+b \sin[c+d x])^2} + \frac{b (57 a^2 + 20 b^2) \sqrt{e \cos[c+d x]}}{24 (a^2-b^2)^3 d e (a+b \sin[c+d x])}
\end{aligned}$$

Result (type 6, 1276 leaves):

$$\begin{aligned}
& \left( \cos[c+d x] \left( \frac{b}{3 (a^2-b^2) (a+b \sin[c+d x])^3} + \right. \right. \\
& \left. \left. \frac{11 a b}{12 (a^2-b^2)^2 (a+b \sin[c+d x])^2} + \frac{b (57 a^2 + 20 b^2)}{24 (a^2-b^2)^3 (a+b \sin[c+d x])} \right) \right) / \\
& \left( d \sqrt{e \cos[c+d x]} \right) + \frac{1}{48 (a-b)^3 (a+b)^3 d \sqrt{e \cos[c+d x]}} \sqrt{\cos[c+d x]} \\
& \left( - \frac{1}{\sqrt{1-\cos[c+d x]^2}} \frac{1}{(a+b \sin[c+d x])} \right. \\
& \left. \left( 5 a (a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos[c+d x]} \right) \right) / \\
& \left( \sqrt{1-\cos[c+d x]^2} \right. \\
& \left. \left( 5 (a^2-b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - 2 \right. \right. \\
& \left. \left. \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \\
& \left. \left. \left. \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \cos[c+d x]^2 \right) \\
& \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left( \frac{1}{8} - \frac{i}{8} \right) \sqrt{b}
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] + \right. \\
& \quad \left. \operatorname{Log} \left[ \sqrt{-a^2 + b^2} - (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] - \right. \\
& \quad \left. \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] \right) \\
& \quad \frac{\sin[c + d x] - \frac{1}{(1 - \cos[c + d x]^2) (a + b \sin[c + d x])}}{2 (-57 a^2 b - 20 b^3) \left( a + b \sqrt{1 - \cos[c + d x]^2} \right)} \\
& \quad \left( \left( 5 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \quad \left. \left. \sqrt{\cos[c + d x]} \sqrt{1 - \cos[c + d x]^2} \right) / \right. \\
& \quad \left( \left( -5 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \quad \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1} \left[ \frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
& \quad \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \right) + \\
& \quad \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
& \quad \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] + \right. \right. \\
& \quad \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \right) / \\
& \quad \left( 4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin[c + d x]^2
\end{aligned}$$

Problem 614: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos[c + d x])^{3/2} (a + b \sin[c + d x])^4} dx$$

Optimal (type 4, 674 leaves, 16 steps):

$$\begin{aligned}
& - \frac{15 a b^{3/2} (7 a^2 + 6 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 (-a^2+b^2)^{17/4} d e^{3/2}} + \frac{15 a b^{3/2} (7 a^2 + 6 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 (-a^2+b^2)^{17/4} d e^{3/2}} - \\
& \frac{(16 a^4 + 151 a^2 b^2 + 28 b^4) \sqrt{e \cos[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{8 (a^2-b^2)^4 d e^2 \sqrt{\cos[c+d x]}} - \\
& \left(15 a^2 b (7 a^2 + 6 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
& \left(16 (a^2-b^2)^4 \left(b-\sqrt{-a^2+b^2}\right) d e \sqrt{e \cos[c+d x]}\right) - \\
& \left(15 a^2 b (7 a^2 + 6 b^2) \sqrt{\cos[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) / \\
& \left(16 (a^2-b^2)^4 \left(b+\sqrt{-a^2+b^2}\right) d e \sqrt{e \cos[c+d x]}\right) + \\
& \frac{b}{3 (a^2-b^2) d e \sqrt{e \cos[c+d x]} (a+b \sin[c+d x])^3} + \\
& \frac{13 a b}{12 (a^2-b^2)^2 d e \sqrt{e \cos[c+d x]} (a+b \sin[c+d x])^2} + \\
& \frac{b (89 a^2 + 28 b^2)}{24 (a^2-b^2)^3 d e \sqrt{e \cos[c+d x]} (a+b \sin[c+d x])} - \\
& \frac{15 a b (7 a^2 + 6 b^2) - (16 a^4 + 151 a^2 b^2 + 28 b^4) \sin[c+d x]}{8 (a^2-b^2)^4 d e \sqrt{e \cos[c+d x]}}
\end{aligned}$$

Result (type 6, 1390 leaves):

$$\begin{aligned}
& - \frac{1}{16 (a-b)^4 (a+b)^4 d (\cos[c+d x])^{3/2}} \\
& \cos[c+d x]^{3/2} \left( \frac{1}{12 \sqrt{1-\cos[c+d x]^2} (a+b \sin[c+d x])} (16 a^5 + 256 a^3 b^2 + 118 a b^4) \right. \\
& \left( a+b \sqrt{1-\cos[c+d x]^2} \right) \left( - \left( \left( 56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \cos[c+d x]^{3/2} \right) / \left( \sqrt{1-\cos[c+d x]^2} \right. \right. \\
& \left. \left. \left( 7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] - \right. \right. \\
& \left. \left. \left. 2 \left( 2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c+d x]^2, \frac{b^2 \cos[c+d x]^2}{-a^2+b^2} \right] \right) \right) \\
& \left. \cos[c+d x]^2 \right) \left( a^2+b^2 (-1+\cos[c+d x]^2) \right) \right) - 
\end{aligned}$$

$$\begin{aligned}
& \left( (3 + 3 \text{i}) \left( 2 \operatorname{ArcTan} \left[ 1 - \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[ 1 + \frac{(1 + \text{i}) \sqrt{b} \sqrt{\cos[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \operatorname{Log} \left[ \sqrt{-a^2 + b^2} - (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] + \operatorname{Log} \left[ \sqrt{-a^2 + b^2} + (1 + \text{i}) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \right. \\
& \left. \left. \left. \sqrt{\cos[c + d x]} + \text{i} b \cos[c + d x] \right] \right] \right) \Big/ \left( \sqrt{b} (-a^2 + b^2)^{1/4} \right) \sin[c + d x] - \\
& \frac{1}{(1 - \cos[c + d x]^2) (a + b \sin[c + d x])} 2 (16 a^4 b + 151 a^2 b^3 + 28 b^5) \\
& \left( a + b \sqrt{1 - \cos[c + d x]^2} \right) \\
& \left( \left( 7 b (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
& \left. \left. \cos[c + d x]^{3/2} \sqrt{1 - \cos[c + d x]^2} \right) \Big/ \right. \\
& \left. \left( 3 \left( -7 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + 2 \right. \right. \\
& \left. \left. 2 b^2 \operatorname{AppellF1} \left[ \frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c + d x]^2, \frac{b^2 \cos[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
& \left. \cos[c + d x]^2 \right) (a^2 + b^2 (-1 + \cos[c + d x]^2)) \Big) + \\
& \left( a \left( -2 \operatorname{ArcTan} \left[ 1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[ 1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] - \right. \right. \\
& \left. \left. \operatorname{Log} \left[ \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos[c + d x]} + b \cos[c + d x] \right] \right) \Big/ \left( 4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin[c + d x]^2 \right) + \\
& \left( \cos[c + d x]^2 \left( -\frac{b^3 \cos[c + d x]}{3 (a^2 - b^2)^2 (a + b \sin[c + d x])^3} - \frac{7 a b^3 \cos[c + d x]}{4 (a^2 - b^2)^3 (a + b \sin[c + d x])^2} + \right. \right. \\
& \left. \left. \frac{-55 a^2 b^3 \cos[c + d x] - 12 b^5 \cos[c + d x]}{8 (a^2 - b^2)^4 (a + b \sin[c + d x])} + \right. \right. \\
& \left. \left. \frac{1}{(a^2 - b^2)^4} \right. \right. \\
& \left. \left. 2 \operatorname{Sec}[c + d x] \right. \right. \\
& \left. \left. (-4 a^3 b - 4 a b^3 + a^4 \sin[c + d x] + 6 a^2 b^2 \sin[c + d x]) + \right. \right. \\
\end{aligned}$$

$$\frac{b^4 \sin(c + dx)}{\left(d \left(e \cos(c + dx)\right)^{3/2}\right)}$$

## Problem 615: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{c \cos [e + f x]} \sqrt{a + b \sin [e + f x]}} dx$$

Optimal (type 4, 183 leaves, 2 steps):

$$\left. \begin{aligned}
 & 2\sqrt{2} \left( -a + b \right)^{1/4} \sqrt{c \cos[e + fx]} \\
 & \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\left( a + b \right)^{1/4} \sqrt{\frac{1 + \cos[e + fx] + \sin[e + fx]}{1 + \cos[e + fx] - \sin[e + fx]}}}{\left( -a + b \right)^{1/4}} \right], -1 \right] \sqrt{\frac{a + b \sin[e + fx]}{(a - b) (1 - \sin[e + fx])}} \\
 & \left( a + b \right)^{1/4} c f \sqrt{\frac{1 + \cos[e + fx] + \sin[e + fx]}{1 + \cos[e + fx] - \sin[e + fx]}} \sqrt{a + b \sin[e + fx]}
 \end{aligned} \right\}$$

### Result (type 4. 4001 leaves):

$$\begin{aligned}
& - \left( \left( 4 \cos \left[ \frac{1}{2} (e + fx) \right]^2 \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan \left[ \frac{1}{2} (e + fx) \right])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (e + fx) \right])}} \right], -1 \right] \right. \right. \\
& \left. \left. \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right) \left( 1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan \left[ \frac{1}{2} (e + fx) \right]}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (e + fx) \right])}} \right. \right. \\
& \left. \left. \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan \left[ \frac{1}{2} (e + fx) \right]}{(-a + b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (e + fx) \right])}} \right) \right) \Big/ \left( f \sqrt{\cos [e + fx]} \right) \\
& \sqrt{c \cos [e + fx]} (a + b \sin [e + fx]) \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan \left[ \frac{1}{2} (e + fx) \right])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (e + fx) \right])}} \\
& - \left( \left( 2 \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan \left[ \frac{1}{2} (e + fx) \right])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[ \frac{1}{2} (e + fx) \right])}} \right], -1 \right] \right.
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e + fx)\right]}{(a - b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}} \\
& \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e + fx)\right]}{(-a + b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}} \Bigg) \\
& \left( \sqrt{\cos[e + fx]} \sqrt{a + b \sin[e + fx]} \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) \left( 1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}{(a - b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}} \right) - \\
& \left( 2 \operatorname{EllipticF}[\operatorname{ArcSin}\left[\sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) \left( 1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}{(a - b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}}\right], -1] \right. \\
& \left. \left( 1 + \tan\left[\frac{1}{2}(e + fx)\right] \right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e + fx)\right]}{(a - b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}} \right. \\
& \left. \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e + fx)\right]}{(-a + b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}} \right) \Bigg) \\
& \left( \sqrt{\cos[e + fx]} \sqrt{a + b \sin[e + fx]} \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) \left( 1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}{(a - b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}} \right) + \\
& \left( 2 b \cos\left[\frac{1}{2}(e + fx)\right]^2 \sqrt{\cos[e + fx]} \operatorname{EllipticF}[\right. \\
& \left. \operatorname{ArcSin}\left[\sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) \left( 1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}{(a - b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}}\right], -1] \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right) \right. \\
& \left. \left( 1 + \tan\left[\frac{1}{2}(e + fx)\right] \right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e + fx)\right]}{(a - b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}} \right. \\
& \left. \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e + fx)\right]}{(-a + b + \sqrt{-a^2 + b^2}) \left( -1 + \tan\left[\frac{1}{2}(e + fx)\right] \right)}} \right) \Bigg)
\end{aligned}$$

$$\begin{aligned}
& \left( (a+b \sin[e+f x])^{3/2} \sqrt{\frac{(-a-b+\sqrt{-a^2+b^2}) (1+\tan[\frac{1}{2} (e+f x)])}{(a-b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}} \right) + \\
& \left( 4 \cos[\frac{1}{2} (e+f x)] \text{EllipticF}[\text{ArcSin}\left[\sqrt{\frac{(-a-b+\sqrt{-a^2+b^2}) (1+\tan[\frac{1}{2} (e+f x)])}{(a-b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}}\right], \right. \\
& \quad \left. -1\right] \sin[\frac{1}{2} (e+f x)] \left(-1+\tan[\frac{1}{2} (e+f x)]\right) \\
& \quad \left(1+\tan[\frac{1}{2} (e+f x)]\right) \sqrt{\frac{b-\sqrt{-a^2+b^2}+a \tan[\frac{1}{2} (e+f x)]}{(a-b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}} \\
& \quad \left. -\frac{b+\sqrt{-a^2+b^2}+a \tan[\frac{1}{2} (e+f x)]}{(-a+b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}\right) / \\
& \left( \sqrt{\cos[e+f x]} \sqrt{a+b \sin[e+f x]} \sqrt{\frac{(-a-b+\sqrt{-a^2+b^2}) (1+\tan[\frac{1}{2} (e+f x)])}{(a-b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}} \right) - \\
& \left( 2 \cos[\frac{1}{2} (e+f x)]^2 \text{EllipticF}[\text{ArcSin}\left[\sqrt{\frac{(-a-b+\sqrt{-a^2+b^2}) (1+\tan[\frac{1}{2} (e+f x)])}{(a-b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}}\right], \right. \\
& \quad \left. -1\right] \sin[e+f x] \left(-1+\tan[\frac{1}{2} (e+f x)]\right) \\
& \quad \left(1+\tan[\frac{1}{2} (e+f x)]\right) \sqrt{\frac{b-\sqrt{-a^2+b^2}+a \tan[\frac{1}{2} (e+f x)]}{(a-b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}} \\
& \quad \left. -\frac{b+\sqrt{-a^2+b^2}+a \tan[\frac{1}{2} (e+f x)]}{(-a+b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}\right) / \\
& \left( \cos[e+f x]^{3/2} \sqrt{a+b \sin[e+f x]} \sqrt{\frac{(-a-b+\sqrt{-a^2+b^2}) (1+\tan[\frac{1}{2} (e+f x)])}{(a-b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}} \right) + \\
& \left( 2 \cos[\frac{1}{2} (e+f x)]^2 \text{EllipticF}[\text{ArcSin}\left[\sqrt{\frac{(-a-b+\sqrt{-a^2+b^2}) (1+\tan[\frac{1}{2} (e+f x)])}{(a-b+\sqrt{-a^2+b^2}) (-1+\tan[\frac{1}{2} (e+f x)])}}\right], \right.
\end{aligned}$$

$$\begin{aligned}
& -1 \left[ \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right) \left( 1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right) \right. \\
& \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan \left[ \frac{1}{2} (e + fx) \right]}{\left( a - b + \sqrt{-a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)}} \\
& \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan \left[ \frac{1}{2} (e + fx) \right]}{\left( -a + b + \sqrt{-a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)}} \\
& \left( \frac{\left( -a - b + \sqrt{-a^2 + b^2} \right) \sec \left[ \frac{1}{2} (e + fx) \right]^2}{2 \left( a - b + \sqrt{-a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)} - \right. \\
& \left. \left( \left( -a - b + \sqrt{-a^2 + b^2} \right) \sec \left[ \frac{1}{2} (e + fx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right) \right) \right) / \\
& \left( 2 \left( a - b + \sqrt{-a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)^2 \right) \Bigg) / \\
& \left( \sqrt{\cos [e + fx]} \sqrt{a + b \sin [e + fx]} \left( \frac{\left( -a - b + \sqrt{-a^2 + b^2} \right) \left( 1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)}{\left( a - b + \sqrt{-a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)} \right)^{3/2} \right. \\
& \left( 2 \left( a - b + \sqrt{-a^2 + b^2} \right) \cos \left[ \frac{1}{2} (e + fx) \right]^2 \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)^2 \right. \\
& \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan \left[ \frac{1}{2} (e + fx) \right]}{\left( a - b + \sqrt{-a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)}} \\
& \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan \left[ \frac{1}{2} (e + fx) \right]}{\left( -a + b + \sqrt{-a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)}} \\
& \left( \frac{\left( -a - b + \sqrt{-a^2 + b^2} \right) \sec \left[ \frac{1}{2} (e + fx) \right]^2}{2 \left( a - b + \sqrt{-a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)} - \right. \\
& \left. \left( \left( -a - b + \sqrt{-a^2 + b^2} \right) \sec \left[ \frac{1}{2} (e + fx) \right]^2 \left( 1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right) \right) \right) / \\
& \left( 2 \left( a - b + \sqrt{-a^2 + b^2} \right) \left( -1 + \tan \left[ \frac{1}{2} (e + fx) \right] \right)^2 \right) \Bigg) / \left( \left( -a - b + \sqrt{-a^2 + b^2} \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\cos[e + fx]} \sqrt{a + b \sin[e + fx]} \sqrt{1 - \frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan[\frac{1}{2} (e + fx)])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])}} \\
& \sqrt{1 + \frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan[\frac{1}{2} (e + fx)])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])}} - \\
& \left( 2 \cos[\frac{1}{2} (e + fx)]^2 \text{EllipticF}[\text{ArcSin}\left[ \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan[\frac{1}{2} (e + fx)])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])}} \right], \right. \\
& \left. -1 \right] \left( -1 + \tan[\frac{1}{2} (e + fx)] \right) \left( 1 + \tan[\frac{1}{2} (e + fx)] \right) \\
& \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan[\frac{1}{2} (e + fx)]}{(-a + b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])}} \\
& \left( \frac{a \sec[\frac{1}{2} (e + fx)]^2}{2 (a - b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])} - \right. \\
& \left. \frac{\sec[\frac{1}{2} (e + fx)]^2 (b - \sqrt{-a^2 + b^2} + a \tan[\frac{1}{2} (e + fx)])}{2 (a - b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])^2} \right) / \\
& \left( \sqrt{\cos[e + fx]} \sqrt{a + b \sin[e + fx]} \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan[\frac{1}{2} (e + fx)])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])}} \right. \\
& \left. \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan[\frac{1}{2} (e + fx)]}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])}} \right) - \\
& \left( 2 \cos[\frac{1}{2} (e + fx)]^2 \text{EllipticF}[\text{ArcSin}\left[ \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan[\frac{1}{2} (e + fx)])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])}} \right], \right. \\
& \left. -1 \right] \left( -1 + \tan[\frac{1}{2} (e + fx)] \right) \left( 1 + \tan[\frac{1}{2} (e + fx)] \right) \\
& \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan[\frac{1}{2} (e + fx)]}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan[\frac{1}{2} (e + fx)])}}
\end{aligned}$$

$$\begin{aligned}
& \left( -\frac{a \operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2}{2 \left(-a + b + \sqrt{-a^2 + b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)} + \right. \\
& \left. \frac{\operatorname{Sec}\left[\frac{1}{2} (e + f x)\right]^2 \left(b + \sqrt{-a^2 + b^2} + a \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)}{2 \left(-a + b + \sqrt{-a^2 + b^2}\right) \left(-1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)^2} \right) / \\
& \left( \sqrt{\operatorname{Cos}[e + f x]} \sqrt{a + b \operatorname{Sin}[e + f x]} \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)}{(a - b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)}} \right. \\
& \left. \left. \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]}{(-a + b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2} (e + f x)\right]\right)}} \right) \right)
\end{aligned}$$

Problem 617: Result unnecessarily involves imaginary or complex numbers.

$$\int (e \operatorname{Cos}[c + d x])^p (a + b \operatorname{Sin}[c + d x])^2 dx$$

Optimal (type 5, 157 leaves, 3 steps):

$$\begin{aligned}
& -\frac{a b (3 + p) (e \operatorname{Cos}[c + d x])^{1+p}}{d e (1 + p) (2 + p)} - \\
& \left( (b^2 + a^2 (2 + p)) (e \operatorname{Cos}[c + d x])^{1+p} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \operatorname{Cos}[c + d x]^2\right] \right. \\
& \left. \operatorname{Sin}[c + d x]\right) / \left( d e (1 + p) (2 + p) \sqrt{\operatorname{Sin}[c + d x]^2} \right) - \frac{b (e \operatorname{Cos}[c + d x])^{1+p} (a + b \operatorname{Sin}[c + d x])}{d e (2 + p)}
\end{aligned}$$

Result (type 5, 288 leaves):

$$\begin{aligned}
& \frac{1}{d (1 + p) \sqrt{\operatorname{Sin}[c + d x]^2}} \\
& (e \operatorname{Cos}[c + d x])^p \left( \frac{1}{-1 + p} 2^{-p} a b \left(1 + e^{2 \frac{i}{2} (c + d x)}\right)^{-1-p} \left(e^{-\frac{i}{2} (c + d x)} \left(1 + e^{2 \frac{i}{2} (c + d x)}\right)\right)^{1+p} \right. \\
& \left. \operatorname{Cos}[c + d x]^{-p} \left( -(-1 + p) \operatorname{Hypergeometric2F1}\left[\frac{1}{2} (-1 - p), -p, \frac{1 - p}{2}, -e^{2 \frac{i}{2} (c + d x)}\right] + \right. \right. \\
& \left. \left. e^{2 \frac{i}{2} (c + d x)} (1 + p) \operatorname{Hypergeometric2F1}\left[\frac{1 - p}{2}, -p, \frac{3 - p}{2}, -e^{2 \frac{i}{2} (c + d x)}\right]\right) \sqrt{\operatorname{Sin}[c + d x]^2} \right. \\
& \left. - \frac{1}{2} b^2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1 + p}{2}, \frac{3 + p}{2}, \operatorname{Cos}[c + d x]^2\right] \operatorname{Sin}[2 (c + d x)] \right. \\
& \left. - \frac{1}{2} a^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1 + p}{2}, \frac{3 + p}{2}, \operatorname{Cos}[c + d x]^2\right] \operatorname{Sin}[2 (c + d x)] \right)
\end{aligned}$$

Problem 618: Result unnecessarily involves complex numbers and more than

twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + b \sin [c + d x]) dx$$

Optimal (type 5, 97 leaves, 2 steps):

$$-\frac{b (e \cos[c + d x])^{1+p}}{d e (1+p)} -$$

$$\left( a (e \cos[c + d x])^{1+p} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \cos[c + d x]^2\right] \sin[c + d x] \right) /$$

$$\left( d e (1+p) \sqrt{\sin[c + d x]^2} \right)$$

### Result (type 5, 233 leaves):

$$\frac{1}{2 d (1+p)} \left( \begin{array}{l} \left( e \cos[c + d x] \right)^p \left( \frac{1}{-1+p} 2^{-p} b \left( 1 + e^{2 i (c+d x)} \right)^{-1-p} \left( e^{-i (c+d x)} \left( 1 + e^{2 i (c+d x)} \right) \right)^{1+p} \cos[c + d x]^{-p} \right. \\ \left. - \left( -1+p \right) \text{Hypergeometric2F1} \left[ \frac{1}{2} \left( -1-p \right), -p, \frac{1-p}{2}, -e^{2 i (c+d x)} \right] + e^{2 i (c+d x)} \left( 1+p \right) \text{Hypergeometric2F1} \left[ \frac{1-p}{2}, -p, \frac{3-p}{2}, -e^{2 i (c+d x)} \right] \right) - a \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \cos[c + d x]^2 \right] \sin[2 (c + d x)] \end{array} \right) \sqrt{\sin[c + d x]^2}$$

## Problem 619: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^p}{a + b \sin [c + d x]} dx$$

Optimal (type 6, 158 leaves, 1 step):

$$-\frac{1}{b d (1-p)} e \text{AppellF1}\left[1-p, \frac{1-p}{2}, \frac{1-p}{2}, 2-p, \frac{a+b}{a+b \sin[c+d x]}, \frac{a-b}{a+b \sin[c+d x]}\right] \\ (e \cos[c+d x])^{-1+p} \left(-\frac{b (1-\sin[c+d x])}{a+b \sin[c+d x]}\right)^{\frac{1-p}{2}} \left(\frac{b (1+\sin[c+d x])}{a+b \sin[c+d x]}\right)^{\frac{1-p}{2}}$$

### Result (type 6, 6000 leaves):

$$\begin{aligned} & \left( a^2 (e \cos(c + d x))^p \tan(c + d x) (1 + \tan(c + d x)^2)^{-\frac{p}{2}} \left( b \tan(c + d x) + a \sqrt{1 + \tan(c + d x)^2} \right) \right. \\ & \left. - \left( \left( 3 a \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan(c + d x)^2, \left( -1 + \frac{b^2}{a^2} \right) \tan(c + d x)^2 \right] \sqrt{1 + \tan(c + d x)^2} \right) \right. \right. \\ & \left. \left. - 3 a^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan(c + d x)^2, \left( -1 + \frac{b^2}{a^2} \right) \tan(c + d x)^2 \right] + \left( 2 (a^2 - b^2) \right. \right. \right. \\ & \left. \left. \left. - 3 a^2 \tan(c + d x) \left( 1 + \tan(c + d x)^2 \right)^{-\frac{p}{2}} \left( b \tan(c + d x) + a \sqrt{1 + \tan(c + d x)^2} \right) \right) \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
& \text{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + a^2 p \text{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \tan[c+d x]^2\Big) + \\
& \left(2 b \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+d x]^2, \frac{(-a^2 + b^2) \tan[c+d x]^2}{a^2}\right] \tan[c+d x]\right) \Big/ \\
& \left(-4 a^2 \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + \right. \\
& \left. \left(2 (a^2 - b^2) \text{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + a^2 (1+p) \right. \right. \\
& \left. \left. \text{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right]\right) \tan[c+d x]^2\right) \Big) \Big/ \\
& \left(d (a + b \sin[c+d x]) \left(a + \frac{b \tan[c+d x]}{\sqrt{1 + \tan[c+d x]^2}}\right) (-b^2 \tan[c+d x]^2 + \right. \\
& \left. a^2 (1 + \tan[c+d x]^2)) \right. \\
& \left. - \frac{1}{\left(a + \frac{b \tan[c+d x]}{\sqrt{1 + \tan[c+d x]^2}}\right) (-b^2 \tan[c+d x]^2 + a^2 (1 + \tan[c+d x]^2))^2} \right. \\
& a^2 \tan[c+d x] (2 a^2 \sec[c+d x]^2 \tan[c+d x] - 2 b^2 \sec[c+d x]^2 \tan[c+d x]) \\
& (1 + \tan[c+d x]^2)^{-1-\frac{p}{2}} \left(b \tan[c+d x] + a \sqrt{1 + \tan[c+d x]^2}\right) \\
& \left(-\left(3 a \text{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \right. \right. \\
& \left. \left. \sqrt{1 + \tan[c+d x]^2}\right) \Big/ \left(-3 a^2 \text{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+d x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + \left(2 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[c+d x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + a^2 p \text{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[c+d x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \tan[c+d x]^2\right) \Big) + \\
& \left(2 b \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+d x]^2, \frac{(-a^2 + b^2) \tan[c+d x]^2}{a^2}\right] \tan[c+d x]\right) \Big/ \\
& \left(-4 a^2 \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + \right. \\
& \left. \left(2 (a^2 - b^2) \text{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + \right. \right. \\
\end{aligned}$$

$$\begin{aligned}
& a^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[c+d x]^2, \right. \\
& \quad \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \tan[c+d x]^2\Big) + \\
& \frac{1}{\left(a + \frac{b \tan[c+d x]}{\sqrt{1+\tan[c+d x]^2}}\right) \left(-b^2 \tan[c+d x]^2 + a^2 (1+\tan[c+d x]^2)\right)} \\
& \left(1 + \tan[c+d x]^2\right)^{-1-\frac{p}{2}} \left(b \sec[c+d x]^2 + \frac{a \sec[c+d x]^2 \tan[c+d x]}{\sqrt{1+\tan[c+d x]^2}}\right) \\
& \left(-\left(3 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \right. \right. \\
& \quad \left.\left. \sqrt{1+\tan[c+d x]^2}\right) \right/ \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+d x]^2, \right. \right. \\
& \quad \left.\left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \\
& \quad \left.\left. -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, \right. \right. \\
& \quad \left.\left. 1, \frac{5}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \tan[c+d x]^2\right) \right) + \\
& \left(2 b \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+d x]^2, \frac{(-a^2 + b^2) \tan[c+d x]^2}{a^2}\right] \tan[c+d x]\right) \Big/ \\
& \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + \right. \\
& \quad \left.a^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[c+d x]^2, \right. \right. \\
& \quad \left.\left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \tan[c+d x]^2\right) - \\
& \frac{1}{\left(a + \frac{b \tan[c+d x]}{\sqrt{1+\tan[c+d x]^2}}\right)^2 \left(-b^2 \tan[c+d x]^2 + a^2 (1+\tan[c+d x]^2)\right)} \\
& a^2 \tan[c+d x] \left(1 + \tan[c+d x]^2\right)^{-1-\frac{p}{2}} \\
& \left(-\frac{b \sec[c+d x]^2 \tan[c+d x]^2}{(1+\tan[c+d x]^2)^{3/2}} + \frac{b \sec[c+d x]^2}{\sqrt{1+\tan[c+d x]^2}}\right) \\
& \left(b \tan[c+d x] + a \sqrt{1+\tan[c+d x]^2}\right) \\
& \left(-\left(3 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \right. \right. \\
& \quad \left.\left. \sqrt{1+\tan[c+d x]^2}\right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \sqrt{1 + \tan[c + dx]^2} \right) \Big/ \left( -3 a^2 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + dx]^2, \right. \right. \\
& \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \left( 2 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \\
& \left. \left. -\tan[c + dx]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + a^2 p \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, \right. \right. \\
& \left. \left. 1, \frac{5}{2}, -\tan[c + dx]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \right) \tan[c + dx]^2 \right) + \\
& \left( 2 b \operatorname{AppellF1} \left[ 1, \frac{1+p}{2}, 1, 2, -\tan[c + dx]^2, \frac{(-a^2 + b^2) \tan[c + dx]^2}{a^2} \right] \tan[c + dx] \right) \Big/ \\
& \left( -4 a^2 \operatorname{AppellF1} \left[ 1, \frac{1+p}{2}, 1, 2, -\tan[c + dx]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \right. \\
& \left( 2 (a^2 - b^2) \operatorname{AppellF1} \left[ 2, \frac{1+p}{2}, 2, 3, -\tan[c + dx]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \right. \\
& \left. a^2 (1+p) \operatorname{AppellF1} \left[ 2, \frac{3+p}{2}, 1, 3, -\tan[c + dx]^2, \right. \right. \\
& \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \right) \tan[c + dx]^2 \Big) + \\
& \frac{1}{\left( a + \frac{b \tan[c + dx]}{\sqrt{1 + \tan[c + dx]^2}} \right) \left( -b^2 \tan[c + dx]^2 + a^2 (1 + \tan[c + dx]^2) \right)} \\
& 2 a^2 \left( -1 - \frac{p}{2} \right) \sec[c + dx]^2 \\
& \tan[c + dx]^2 (1 + \tan[c + dx]^2)^{-2 - \frac{p}{2}} \\
& \left( b \tan[c + dx] + a \sqrt{1 + \tan[c + dx]^2} \right) \\
& \left( - \left( \left( 3 a \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + dx]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \right. \right. \right. \\
& \left. \left. \left. \sqrt{1 + \tan[c + dx]^2} \right) \Big/ \left( -3 a^2 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + dx]^2, \right. \right. \right. \\
& \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \left( 2 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \\
& \left. \left. -\tan[c + dx]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + a^2 p \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, \right. \right. \\
& \left. \left. 1, \frac{5}{2}, -\tan[c + dx]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] \right) \tan[c + dx]^2 \right) + \\
& \left( 2 b \operatorname{AppellF1} \left[ 1, \frac{1+p}{2}, 1, 2, -\tan[c + dx]^2, \frac{(-a^2 + b^2) \tan[c + dx]^2}{a^2} \right] \tan[c + dx] \right) \Big/ \\
& \left( -4 a^2 \operatorname{AppellF1} \left[ 1, \frac{1+p}{2}, 1, 2, -\tan[c + dx]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \right. \\
& \left( 2 (a^2 - b^2) \operatorname{AppellF1} \left[ 2, \frac{1+p}{2}, 2, 3, -\tan[c + dx]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + dx]^2 \right] + \right.
\end{aligned}$$



$$\begin{aligned}
& -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\Big] + \left(2 \left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \right. \right. \\
& \left. \left. \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right] + a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, \right. \right. \\
& \left. \left. 1, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right]\right)\Big) - \\
& \left(3 a \left(-\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right] \right. \right. \\
& \left. \left. \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] + \frac{2}{3} \left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left.-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]\right) \sqrt{1+\operatorname{Tan}[c+d x]^2}\Big)\Big/ \\
& \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right] + \left(2 \left(a^2-b^2\right) \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right] + a^2 p \operatorname{AppellF1}\left[\right. \right. \right. \\
& \left. \left. \left.\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right]\right) \operatorname{Tan}[c+d x]^2\right) + \\
& \left(2 b \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[c+d x]^2, \frac{(-a^2+b^2) \operatorname{Tan}[c+d x]^2}{a^2}\right] \operatorname{Sec}[c+d x]^2\right)\Big/ \\
& \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right] + \right. \\
& \left(2 \left(a^2-b^2\right) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right] + a^2 \right. \\
& \left. (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right]\right) \\
& \operatorname{Tan}[c+d x]^2\Big) + \left(2 b \operatorname{Tan}[c+d x] \left(\frac{1}{a^2} (-a^2+b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, \right. \right. \right. \\
& \left. \left. 3, -\operatorname{Tan}[c+d x]^2, \frac{(-a^2+b^2) \operatorname{Tan}[c+d x]^2}{a^2}\right] \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] - \right. \right. \\
& \left. \left. \frac{1}{2} (1+p) \operatorname{AppellF1}\left[2, 1+\frac{1+p}{2}, 1, 3, -\operatorname{Tan}[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \frac{(-a^2+b^2) \operatorname{Tan}[c+d x]^2}{a^2}\right] \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x]\right)\right)\Big/ \\
& \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right] + \right. \\
& \left(2 \left(a^2-b^2\right) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\operatorname{Tan}[c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right] + \right. \\
& \left. a^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\operatorname{Tan}[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left. \left(-1+\frac{b^2}{a^2}\right) \operatorname{Tan}[c+d x]^2\right]\right) \operatorname{Tan}[c+d x]^2\Big)
\end{aligned}$$

$$\begin{aligned}
& \left( 3 a \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \sqrt{1 + \operatorname{Tan}[c + d x]^2} \right. \\
& \left( 2 \left( 2 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] + \right. \right. \\
& \left. a^2 p \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \right) \\
& \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] - 3 a^2 \left( -\frac{1}{3} p \operatorname{AppellF1} \left[ \frac{3}{2}, 1 + \frac{p}{2}, 1, \frac{5}{2}, \right. \right. \\
& \left. \left. -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] + \right. \\
& \left. \frac{2}{3} \left( -1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \right. \\
& \left. \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] \right) + \operatorname{Tan}[c + d x]^2 \left( 2 (a^2 - b^2) \left( -\frac{3}{5} p \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
& \left. \left. 1 + \frac{p}{2}, 2, \frac{7}{2}, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \operatorname{Sec}[c + d x]^2 \right. \\
& \left. \operatorname{Tan}[c + d x] + \frac{12}{5} \left( -1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{p}{2}, 3, \frac{7}{2}, -\operatorname{Tan}[c + d x]^2, \right. \right. \\
& \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] \right) + a^2 p \left( \frac{6}{5} \left( -1 + \frac{b^2}{a^2} \right) \right. \\
& \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2+p}{2}, 2, \frac{7}{2}, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \right. \\
& \left. \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] - \frac{3}{5} (2 + p) \operatorname{AppellF1} \left[ \frac{5}{2}, 1 + \frac{2+p}{2}, 1, \frac{7}{2}, \right. \right. \\
& \left. \left. -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] \right) \right) \right) \Big) \\
& \left( -3 a^2 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] + \right. \\
& \left. \left( 2 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] + \right. \right. \\
& \left. a^2 p \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[c + d x]^2, \right. \right. \\
& \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \operatorname{Tan}[c + d x]^2 \right)^2 - \\
& \left( 2 b \operatorname{AppellF1} \left[ 1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[c + d x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[c + d x]^2}{a^2} \right] \operatorname{Tan}[c + d x] \right. \\
& \left. \left( 2 \left( 2 (a^2 - b^2) \operatorname{AppellF1} \left[ 2, \frac{1+p}{2}, 2, 3, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] + \right. \right. \right. \\
& \left. \left. a^2 (1 + p) \operatorname{AppellF1} \left[ 2, \frac{3+p}{2}, 1, 3, -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \right) \right. \\
& \left. \operatorname{Sec}[c + d x]^2 \operatorname{Tan}[c + d x] - 4 a^2 \left( \left( -1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[ 2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \\
& \left. \left. \left. -\operatorname{Tan}[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c + d x]^2 \right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2 \sec[c + dx]^2 \tan[c + dx] - \\
& \frac{1}{2} (1+p) \operatorname{AppellF1}\left[2, 1 + \frac{1+p}{2}, 1, 3, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] \\
& \sec[c + dx]^2 \tan[c + dx] + \tan[c + dx]^2 \left(2 (a^2 - b^2) \left(\frac{8}{3} \left(-1 + \frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[3, \frac{1+p}{2}, 3, 4, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] \sec[c + dx]^2\right.\right. \\
& \left.\left. \tan[c + dx] - \frac{2}{3} (1+p) \operatorname{AppellF1}\left[3, 1 + \frac{1+p}{2}, 2, 4, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] \sec[c + dx]^2 \tan[c + dx]\right) + a^2 (1+p) \left(\frac{4}{3} \left(-1 + \frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[3, \frac{3+p}{2}, 2, 4, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right]\right. \\
& \left. \sec[c + dx]^2 \tan[c + dx] - \frac{2}{3} (3+p) \operatorname{AppellF1}\left[3, 1 + \frac{3+p}{2}, 1, 4, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right]\right)\right) \Bigg) \\
& \left( -4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + \right. \\
& \left. \left( 2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + \right. \right. \\
& \left. \left. a^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right]^2 \right) \tan[c + dx]^2 \right) \Bigg)
\end{aligned}$$

Problem 620: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + dx])^p}{(a + b \sin[c + dx])^2} dx$$

Optimal (type 6, 170 leaves, 1 step):

$$\begin{aligned}
& - \left( \left( e \operatorname{AppellF1}\left[2 - p, \frac{1-p}{2}, \frac{1-p}{2}, 3 - p, \frac{a + b}{a + b \sin[c + dx]}, \frac{a - b}{a + b \sin[c + dx]}\right] (e \cos[c + dx])^{-1+p} \right. \right. \\
& \left. \left. \left( - \frac{b (1 - \sin[c + dx])}{a + b \sin[c + dx]}\right)^{\frac{1-p}{2}} \left( \frac{b (1 + \sin[c + dx])}{a + b \sin[c + dx]}\right)^{\frac{1-p}{2}} \right) \Bigg/ (b d (2 - p) (a + b \sin[c + dx])) \right)
\end{aligned}$$

Result (type 6, 6875 leaves):

$$\begin{aligned}
& \left( a^2 (e \cos[c + d x])^p \tan[c + d x] (1 + \tan[c + d x]^2)^{-p/2} \right. \\
& \left( \left( 3 (a^2 + b^2) \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \right) / \right. \\
& \left( \left( -3 a^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \left. \left. \left( 2 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + a^2 p \right. \right. \\
& \left. \left. \text{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \right) \tan[c + d x]^2 \right) \\
& \left. \left( -b^2 \tan[c + d x]^2 + a^2 (1 + \tan[c + d x]^2) \right) \right) + \frac{1}{(b^2 \tan[c + d x]^2 - a^2 (1 + \tan[c + d x]^2))^2} \\
& 2 a b \left( - \left( \left( 3 a b \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \right) / \right. \right. \\
& \left. \left( -3 a^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \left. \left. \left( 4 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \left. \left. a^2 p \text{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \right) \tan[c + d x]^2 \right) \right) + \left( 2 (-a^2 + b^2) \text{AppellF1} \left[ 1, \frac{1}{2} (-1 + p), 2, 2, \right. \right. \\
& \left. \left. -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \tan[c + d x] \sqrt{1 + \tan[c + d x]^2} \right) / \\
& \left( -4 a^2 \text{AppellF1} \left[ 1, \frac{1}{2} (-1 + p), 2, 2, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \\
& \left. \left( 4 (a^2 - b^2) \text{AppellF1} \left[ 2, \frac{1}{2} (-1 + p), 3, 3, -\tan[c + d x]^2, \right. \right. \\
& \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + a^2 (-1 + p) \text{AppellF1} \left[ 2, \frac{1+p}{2}, 2, 3, \right. \right. \\
& \left. \left. -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \right) \tan[c + d x]^2 \right) \right) / \\
& \left( (-a^2 + b^2) d (a + b \sin[c + d x])^2 \left( -\frac{1}{-a^2 + b^2} a^2 p \sec[c + d x]^2 \tan[c + d x]^2 \right. \right. \\
& \left. \left( 1 + \tan[c + d x]^2 \right)^{-1-\frac{p}{2}} \right. \\
& \left. \left( 3 (a^2 + b^2) \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \right) / \right. \\
& \left. \left( -3 a^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right)
\end{aligned}$$

$$\begin{aligned}
& \left( 2 \left( a^2 - b^2 \right) \text{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \\
& \quad a^2 p \text{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \\
& \quad \left. \tan[c + d x]^2 \right) \left( -b^2 \tan[c + d x]^2 + a^2 (1 + \tan[c + d x]^2) \right) \Big) + \\
& \frac{1}{(b^2 \tan[c + d x]^2 - a^2 (1 + \tan[c + d x]^2))^2} 2 a b \\
& \left( - \left( \left( 3 a b \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \right) \right. \right. \\
& \quad \left( -3 a^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \\
& \quad \left. \left( 4 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \quad a^2 p \text{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \\
& \quad \left. \tan[c + d x]^2 \right) \Big) + \left( 2 (-a^2 + b^2) \text{AppellF1} \left[ 1, \frac{1}{2} (-1 + p), 2, 2, \right. \right. \\
& \quad \left. \left. -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \tan[c + d x] \sqrt{1 + \tan[c + d x]^2} \right) \Big) \\
& \left( -4 a^2 \text{AppellF1} \left[ 1, \frac{1}{2} (-1 + p), 2, 2, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \\
& \quad \left. \left( 4 (a^2 - b^2) \text{AppellF1} \left[ 2, \frac{1}{2} (-1 + p), 3, 3, -\tan[c + d x]^2, \right. \right. \right. \\
& \quad \left. \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + a^2 (-1 + p) \text{AppellF1} \left[ 2, \frac{1+p}{2}, 2, 3, \right. \right. \\
& \quad \left. \left. \left. -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \right) \tan[c + d x]^2 \right) \Big) + \\
& \frac{1}{-a^2 + b^2} a^2 \sec[c + d x]^2 (1 + \tan[c + d x]^2)^{-p/2} \left( \left( 3 (a^2 + b^2) \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1, \frac{3}{2}, -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \right) \right. \\
& \quad \left( \left( -3 a^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \quad \left. \left. \left( 2 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \quad a^2 p \text{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \\
& \quad \left. \tan[c + d x]^2 \right) \left( -b^2 \tan[c + d x]^2 + a^2 (1 + \tan[c + d x]^2) \right) \Big) + 
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{(b^2 \tan[c + d x]^2 - a^2 (1 + \tan[c + d x]^2))^2} 2 a b \\
& \left( - \left( \left( 3 a b \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \right) \right. \right. \\
& \left. \left. \left( -3 a^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \left. \left. \left( 4 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \left. \left. \left. a^2 p \text{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \right) \right. \\
& \left. \left. \left( \tan[c + d x]^2 \right) \right) + \left( 2 (-a^2 + b^2) \text{AppellF1} \left[ 1, \frac{1}{2} (-1 + p), 2, 2, \right. \right. \\
& \left. \left. \left. -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \tan[c + d x] \sqrt{1 + \tan[c + d x]^2} \right) \right. \\
& \left. \left( -4 a^2 \text{AppellF1} \left[ 1, \frac{1}{2} (-1 + p), 2, 2, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \left. \left. \left( 4 (a^2 - b^2) \text{AppellF1} \left[ 2, \frac{1}{2} (-1 + p), 3, 3, -\tan[c + d x]^2, \right. \right. \right. \\
& \left. \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 + a^2 (-1 + p) \text{AppellF1} \left[ 2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \\
& \left. \left. \left. -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \right) \tan[c + d x]^2 \right) \right) + \\
& \frac{1}{-a^2 + b^2} a^2 \tan[c + d x] (1 + \tan[c + d x]^2)^{-p/2} \left( - \left( \left( 3 (a^2 + b^2) \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. 1, \frac{3}{2}, -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \right. \right. \\
& \left. \left. \left( 2 a^2 \text{Sec}[c + d x]^2 \tan[c + d x] - 2 b^2 \text{Sec}[c + d x]^2 \tan[c + d x] \right) \right) \right) \right. \\
& \left. \left( \left( -3 a^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \left. \left. \left( 2 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] + \right. \right. \\
& \left. \left. \left. a^2 p \text{AppellF1} \left[ \frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \right) \right. \\
& \left. \left. \left( \tan[c + d x]^2 \right) \left( -b^2 \tan[c + d x]^2 + a^2 (1 + \tan[c + d x]^2) \right)^2 \right) \right) + \\
& \left( 3 (a^2 + b^2) \left( -\frac{1}{3} p \text{AppellF1} \left[ \frac{3}{2}, 1 + \frac{p}{2}, 1, \frac{5}{2}, -\tan[c + d x]^2, \frac{(-a^2 + b^2) \tan[c + d x]^2}{a^2} \right] \right. \right. \\
& \left. \left. \left. \text{Sec}[c + d x]^2 \tan[c + d x] + \frac{1}{3 a^2} 2 (-a^2 + b^2) \text{AppellF1} \left[ \frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \\
& \left. \left. \left. -\tan[c + d x]^2, \left( -1 + \frac{b^2}{a^2} \right) \tan[c + d x]^2 \right] \right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \left( -\frac{\text{Tan}[c + d x]^2}{a^2} \left[ \frac{(-a^2 + b^2) \text{Tan}[c + d x]^2}{a^2} \right] \text{Sec}[c + d x]^2 \text{Tan}[c + d x] \right) \right) / \\
& \left( \left( -3 a^2 \text{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] + \right. \right. \\
& \left( 2 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] + \right. \\
& a^2 p \text{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] \\
& \left. \left. \text{Tan}[c + d x]^2 \right) \left( -b^2 \text{Tan}[c + d x]^2 + a^2 (1 + \text{Tan}[c + d x]^2) \right) \right) - \\
& \frac{1}{(b^2 \text{Tan}[c + d x]^2 - a^2 (1 + \text{Tan}[c + d x]^2))^3} 4 a b (-2 a^2 \text{Sec}[c + d x]^2 \text{Tan}[c + d x] + \\
& 2 b^2 \text{Sec}[c + d x]^2 \text{Tan}[c + d x]) \\
& \left( - \left( \left( 3 a b \text{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\text{Tan}[c + d x]^2, \frac{(-a^2 + b^2) \text{Tan}[c + d x]^2}{a^2}\right] \right) / \right. \\
& \left( -3 a^2 \text{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] + \right. \\
& \left( 4 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] + \right. \\
& a^2 p \text{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] \\
& \left. \left. \text{Tan}[c + d x]^2 \right) \right) + \left( 2 (-a^2 + b^2) \text{AppellF1}\left[1, \frac{1}{2} (-1 + p), 2, 2, \right. \right. \\
& \left. \left. -\text{Tan}[c + d x]^2, \frac{(-a^2 + b^2) \text{Tan}[c + d x]^2}{a^2}\right] \text{Tan}[c + d x] \sqrt{1 + \text{Tan}[c + d x]^2} \right) / \\
& \left( -4 a^2 \text{AppellF1}\left[1, \frac{1}{2} (-1 + p), 2, 2, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] + \right. \\
& \left( 4 (a^2 - b^2) \text{AppellF1}\left[2, \frac{1}{2} (-1 + p), 3, 3, -\text{Tan}[c + d x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] + a^2 (-1 + p) \text{AppellF1}\left[2, \frac{1+p}{2}, 2, \right. \right. \\
& \left. \left. 3, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] \right) \text{Tan}[c + d x]^2 \right) - \\
& \left( 3 (a^2 + b^2) \text{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\text{Tan}[c + d x]^2, \frac{(-a^2 + b^2) \text{Tan}[c + d x]^2}{a^2}\right] \right. \\
& \left( 2 \left( 2 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] + \right. \right. \\
& a^2 p \text{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\text{Tan}[c + d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + d x]^2\right] \\
& \left. \left. \text{Sec}[c + d x]^2 \text{Tan}[c + d x] - 3 a^2 \left( -\frac{1}{3} p \text{AppellF1}\left[\frac{3}{2}, 1 + \frac{p}{2}, 1, \frac{5}{2}, \right. \right. \right. \\
& \left. \left. \left. -\text{Tan}[c + d x]^2, \frac{(-a^2 + b^2) \text{Tan}[c + d x]^2}{a^2}\right] \right) \right) / 
\end{aligned}$$





$$\begin{aligned}
& a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \\
& \sec[c+d x]^2 \tan[c+d x] - 3 a^2 \left(-\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1 + \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \\
& \left. \left. -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \sec[c+d x]^2 \tan[c+d x] + \right. \\
& \left. \frac{4}{3} \left(-1 + \frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan[c+d x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \sec[c+d x]^2 \tan[c+d x]\right) + \tan[c+d x]^2 \\
& \left(4 (a^2 - b^2) \left(-\frac{3}{5} p \operatorname{AppellF1}\left[\frac{5}{2}, 1 + \frac{p}{2}, 3, \frac{7}{2}, -\tan[c+d x]^2, \right. \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \sec[c+d x]^2 \tan[c+d x] + \frac{18}{5} \left(-1 + \frac{b^2}{a^2}\right) \right. \\
& \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{p}{2}, 4, \frac{7}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \right. \\
& \left. \sec[c+d x]^2 \tan[c+d x]\right) + a^2 p \left(\frac{12}{5} \left(-1 + \frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2+p}{2}, \right. \right. \\
& \left. \left. 3, \frac{7}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \sec[c+d x]^2 \right. \\
& \left. \tan[c+d x] - \frac{3}{5} (2+p) \operatorname{AppellF1}\left[\frac{5}{2}, 1 + \frac{2+p}{2}, 2, \frac{7}{2}, -\tan[c+d x]^2, \right. \right. \\
& \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] \sec[c+d x]^2 \tan[c+d x]\right)\right)\Bigg) \\
& \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + \right. \\
& \left. \left(4 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + \right. \right. \\
& \left. \left. a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right]\right) \right. \\
& \left. \tan[c+d x]^2\right)^2 - \left(2 (-a^2 + b^2) \operatorname{AppellF1}\left[1, \frac{1}{2} (-1 + p), 2, 2, \right. \right. \\
& \left. \left. -\tan[c+d x]^2, \frac{(-a^2 + b^2) \tan[c+d x]^2}{a^2}\right] \tan[c+d x] \sqrt{1 + \tan[c+d x]^2} \right. \\
& \left. \left(2 \left(4 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1}{2} (-1 + p), 3, 3, -\tan[c+d x]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right] + a^2 (-1 + p) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \\
& \left. \left. \left. -\tan[c+d x]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right]\right) \sec[c+d x]^2 \tan[c+d x] - \right. \\
& \left. 4 a^2 \left(-\frac{1}{2} (-1 + p) \operatorname{AppellF1}\left[2, 1 + \frac{1}{2} (-1 + p), 2, 3, -\tan[c+d x]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+d x]^2\right]\right)\right)
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + \frac{b^2}{a^2} \right) \tan[(c + dx)^2] \sec[(c + dx)^2] \tan[(c + dx)] + \\
& 2 \left( -1 + \frac{b^2}{a^2} \right) \text{AppellF1} \left[ 2, \frac{1}{2} (-1 + p), 3, 3, -\tan[(c + dx)^2], \right. \\
& \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[(c + dx)^2] \sec[(c + dx)^2] \tan[(c + dx)] \right) + \\
& \tan[(c + dx)^2] \left( 4 (a^2 - b^2) \left( -\frac{2}{3} (-1 + p) \text{AppellF1} \left[ 3, 1 + \frac{1}{2} (-1 + p), \right. \right. \right. \\
& \left. \left. \left. 3, 4, -\tan[(c + dx)^2], \left( -1 + \frac{b^2}{a^2} \right) \tan[(c + dx)^2] \sec[(c + dx)^2] \right. \right. \right. \\
& \left. \left. \left. \tan[(c + dx)] + 4 \left( -1 + \frac{b^2}{a^2} \right) \text{AppellF1} \left[ 3, \frac{1}{2} (-1 + p), 4, 4, \right. \right. \right. \\
& \left. \left. \left. -\tan[(c + dx)^2], \left( -1 + \frac{b^2}{a^2} \right) \tan[(c + dx)^2] \sec[(c + dx)^2] \tan[(c + dx)] \right) + \right. \right. \\
& a^2 (-1 + p) \left( \frac{8}{3} \left( -1 + \frac{b^2}{a^2} \right) \text{AppellF1} \left[ 3, \frac{1+p}{2}, 3, 4, -\tan[(c + dx)^2], \right. \right. \\
& \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[(c + dx)^2] \sec[(c + dx)^2] \tan[(c + dx)] - \right. \right. \\
& \left. \frac{2}{3} (1 + p) \text{AppellF1} \left[ 3, 1 + \frac{1+p}{2}, 2, 4, -\tan[(c + dx)^2], \right. \right. \\
& \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[(c + dx)^2] \sec[(c + dx)^2] \tan[(c + dx)] \right) \right) \right) \Bigg) \\
& \left( -4 a^2 \text{AppellF1} \left[ 1, \frac{1}{2} (-1 + p), 2, 2, -\tan[(c + dx)^2], \left( -1 + \frac{b^2}{a^2} \right) \tan[(c + dx)^2] \right] + \right. \\
& \left. \left( 4 (a^2 - b^2) \text{AppellF1} \left[ 2, \frac{1}{2} (-1 + p), 3, 3, -\tan[(c + dx)^2], \right. \right. \right. \\
& \left. \left. \left. \left( -1 + \frac{b^2}{a^2} \right) \tan[(c + dx)^2] + a^2 (-1 + p) \text{AppellF1} \left[ 2, \frac{1+p}{2}, 2, 3, \right. \right. \right. \\
& \left. \left. \left. -\tan[(c + dx)^2], \left( -1 + \frac{b^2}{a^2} \right) \tan[(c + dx)^2] \right] \tan[(c + dx)^2] \right)^2 \right) \right) \Bigg)
\end{aligned}$$

Problem 621: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^p}{(a + b \sin [c + d x])^3} dx$$

Optimal (type 6, 170 leaves, 1 step):

$$-\left( \left( e \operatorname{AppellF1}\left[3-p, \frac{1-p}{2}, \frac{1-p}{2}, 4-p, \frac{a+b}{a+b \operatorname{Sin}[c+d x]}, \frac{a-b}{a+b \operatorname{Sin}[c+d x]} \right] \left( e \operatorname{Cos}[c+d x] \right)^{-1+p} \right. \right. \\ \left. \left. \left( -\frac{b (1-\operatorname{Sin}[c+d x])}{a+b \operatorname{Sin}[c+d x]} \right)^{\frac{1-p}{2}} \left( \frac{b (1+\operatorname{Sin}[c+d x])}{a+b \operatorname{Sin}[c+d x]} \right)^{\frac{1-p}{2}} \right) \right) \right) \left( b d (3-p) (a+b \operatorname{Sin}[c+d x])^2 \right)$$

Result (type 6, 20626 leaves): Display of huge result suppressed!

Problem 622: Unable to integrate problem.

$$\int \frac{(e \cos[c + d x])^p}{(a + b \sin[c + d x])^8} dx$$

Optimal (type 6, 170 leaves, 1 step):

$$-\left( \left( e \text{AppellF1}\left[8-p, \frac{1-p}{2}, \frac{1-p}{2}, 9-p, \frac{a+b}{a+b \sin[c+d x]}, \frac{a-b}{a+b \sin[c+d x]} \right] (e \cos[c+d x])^{-1+p} \right. \right. \\ \left. \left. - \frac{b (1-\sin[c+d x])}{a+b \sin[c+d x]} \right)^{\frac{1-p}{2}} \left( \frac{b (1+\sin[c+d x])}{a+b \sin[c+d x]} \right)^{\frac{1-p}{2}} \right) / \left( b d (8-p) (a+b \sin[c+d x])^7 \right)$$

Result (type 8, 25 leaves):

$$\int \frac{(e \cos[c + d x])^p}{(a + b \sin[c + d x])^8} dx$$

Problem 623: Result more than twice size of optimal antiderivative.

$$\int (e \cos[c + d x])^p (a + b \sin[c + d x])^{5/2} dx$$

Optimal (type 6, 156 leaves, 2 steps):

$$\frac{1}{7 b d} 2 e \text{AppellF1}\left[\frac{7}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{9}{2}, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] \\ (e \cos[c+d x])^{-1+p} (a+b \sin[c+d x])^{7/2} \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{\frac{1-p}{2}} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{\frac{1-p}{2}}$$

Result (type 6, 2612 leaves):

$$\frac{1}{2 d} \cos[c + d x]^{-p} (e \cos[c + d x])^p \\ - \left( \left( 10 (a^2 - b^2)^2 (2 a^2 + b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a - \sqrt{b^2}}\right], \right. \right. \\ \left. \left. \frac{a+b \sin[c+d x]}{a + \sqrt{b^2}} \right) \cos[c+d x]^{1+p} (a+b \sin[c+d x])^{3/2} \right. \\ \left( -\sqrt{b^2} + b \sin[c+d x] \right) \left( \sqrt{b^2} + b \sin[c+d x] \right) \left( 1 - \sin[c+d x]^2 \right)^{-\frac{1}{2} - \frac{p}{2}} \\ \left. \left( -\frac{a^2 - b^2 - 2 a (a+b \sin[c+d x]) + (a+b \sin[c+d x])^2}{b^2} \right)^{\frac{1}{2} (-3+p)} \right) / \\ \left( 3 b^3 \left( a - \sqrt{b^2} \right) \left( a + \sqrt{b^2} \right) \left( 5 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a - \sqrt{b^2}}\right], \right. \right. \\ \left. \left. \frac{a+b \sin[c+d x]}{a + \sqrt{b^2}} \right) \cos[c+d x]^{1+p} (a+b \sin[c+d x])^{3/2} \right. \\ \left( -\sqrt{b^2} + b \sin[c+d x] \right) \left( \sqrt{b^2} + b \sin[c+d x] \right) \left( 1 - \sin[c+d x]^2 \right)^{-\frac{1}{2} - \frac{p}{2}} \\ \left. \left( -\frac{a^2 - b^2 - 2 a (a+b \sin[c+d x]) + (a+b \sin[c+d x])^2}{b^2} \right)^{\frac{1}{2} (-3+p)} \right) /$$

$$\begin{aligned}
& \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}}] + (-1+p) \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{2} - \frac{p}{2}, \frac{3}{2} - \frac{p}{2}, \frac{7}{2}, \right. \right. \\
& \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}}] - \left( a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} - \frac{p}{2}, \right. \\
& \left. \frac{1}{2} - \frac{p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \left. \left( a+b \sin[c+d x] \right) \right) \Bigg) - \\
& \frac{1}{15 b^3} 8 a (a^2 - b^2) \cos[c+d x]^{1+p} (a+b \sin[c+d x])^{3/2} \left( -\sqrt{b^2} + b \sin[c+d x] \right) \\
& \left( \sqrt{b^2} + b \sin[c+d x] \right) (1 - \sin[c+d x]^2)^{-\frac{1}{2} - \frac{p}{2}} \\
& \left( - \frac{a^2 - b^2 - 2 a (a+b \sin[c+d x]) + (a+b \sin[c+d x])^2}{b^2} \right)^{\frac{1}{2} (-3+p)} \\
& \left( - \left( \left( 25 a \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right) / \right. \right. \\
& \left. \left( 5 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] + \right. \\
& (-1+p) \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{2} - \frac{p}{2}, \frac{3}{2} - \frac{p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \right. \right. \\
& \left. \left. \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \left( a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{7}{2}, \right. \right. \\
& \left. \left. \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \left. \left( a+b \sin[c+d x] \right) \right) \right) + \\
& \left( 21 \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right. \\
& \left. \left( a+b \sin[c+d x] \right) \right) / \\
& \left( 7 (a^2 - b^2) \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] + \right. \\
& (-1+p) \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{7}{2}, \frac{1}{2} - \frac{p}{2}, \frac{3}{2} - \frac{p}{2}, \frac{9}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \right. \right. \\
& \left. \left. \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \left( a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{7}{2}, \frac{3}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{9}{2}, \right. \right. \\
& \left. \left. \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \left. \left( a+b \sin[c+d x] \right) \right) \right) + \\
& \left( 1 / \left( 105 b \left( -2 a^2 + b^2 + 4 a (a+b \sin[c+d x]) - 2 (a+b \sin[c+d x])^2 \right) \right) \right) \\
& 2 \\
& (a^2 - b^2) \\
& \cos[c+d x]^{1+p} \\
& \cos[2 (c+d x)] \\
& (a+b \sin[c+d x])^{3/2}
\end{aligned}$$

$$\begin{aligned}
& \left( -\sqrt{b^2} + b \sin[c + dx] \right) \\
& \left( \sqrt{b^2} + b \sin[c + dx] \right) \\
& (1 - \sin[c + dx]^2)^{-\frac{1}{2} - \frac{p}{2}} \\
& \left( -\frac{a^2 - b^2 - 2a(a + b \sin[c + dx]) + (a + b \sin[c + dx])^2}{b^2} \right)^{\frac{1}{2}(-3+p)} \\
& \left( -\left( \left( 175(2a^2 - b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right) \right. \right. \\
& \left. \left. \left( 5(a^2 - b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] + \right. \right. \\
& \left. \left. (-1+p) \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2} - \frac{p}{2}, \frac{3}{2} - \frac{p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}} \right], \right. \right. \\
& \left. \left. \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \left( a + \sqrt{b^2} \right) \text{AppellF1}\left[\frac{5}{2}, \frac{3}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{7}{2}, \right. \right. \\
& \left. \left. \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right) (a + b \sin[c + d x]) \right) + \\
& \left( 588a \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right. \\
& \left. (a + b \sin[c + d x]) \right) \Big/ \\
& \left( 7(a^2 - b^2) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] + \right. \\
& \left. (-1+p) \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1}\left[\frac{7}{2}, \frac{1}{2} - \frac{p}{2}, \frac{3}{2} - \frac{p}{2}, \frac{9}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}} \right], \right. \right. \\
& \left. \left. \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \left( a + \sqrt{b^2} \right) \text{AppellF1}\left[\frac{7}{2}, \frac{3}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{9}{2}, \right. \right. \\
& \left. \left. \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right) (a + b \sin[c + d x]) \right) - \\
& \left( 270 \text{AppellF1}\left[\frac{7}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{9}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right. \\
& \left. (a + b \sin[c + d x])^2 \right) \Big/ \\
& \left( 9(a^2 - b^2) \text{AppellF1}\left[\frac{7}{2}, \frac{1}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{9}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] + \right. \\
& \left. (-1+p) \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1}\left[\frac{9}{2}, \frac{1}{2} - \frac{p}{2}, \frac{3}{2} - \frac{p}{2}, \frac{11}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \right. \right. \right. \\
& \left. \left. \left. \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \left( a + \sqrt{b^2} \right) \text{AppellF1}\left[\frac{9}{2}, \frac{3}{2} - \frac{p}{2}, \frac{1}{2} - \frac{p}{2}, \frac{11}{2}, \right. \right. \right. \\
& \left. \left. \left. \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right) (a + b \sin[c + d x]) \right)
\end{aligned}$$

$$\frac{a + b \sin(c + dx)}{a - \sqrt{b^2}}, \quad \frac{a + b \sin(c + dx)}{a + \sqrt{b^2}} \Bigg) \Bigg) \Bigg) \Bigg) \Bigg)$$

Problem 624: Result more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + b \sin [c + d x])^{3/2} dx$$

Optimal (type 6, 156 leaves, 2 steps):

$$\frac{1}{5 b d} 2 e \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] \\ (e \cos[c+d x])^{-1+p} (a+b \sin[c+d x])^{5/2} \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{\frac{1-p}{2}} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{\frac{1-p}{2}}$$

### Result (type 6, 447 leaves):

$$\begin{aligned}
& - \left( \left( 14 (a^2 - b^2)^2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] \right. \right. \\
& \left. \left. (e \cos[c+dx])^p \sec[c+dx]^3 (a+b \sin[c+dx])^{5/2} \left( -\sqrt{b^2} + b \sin[c+dx] \right) \right) \right. \\
& \left. \left( \sqrt{b^2} + b \sin[c+dx] \right) \right) \Big/ \left( 5 b^3 \left( a - \sqrt{b^2} \right) \left( a + \sqrt{b^2} \right) d \right. \\
& \left. \left( 7 (a^2 - b^2) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] + (-1+p) \right. \right. \\
& \left. \left( \left( -a + \sqrt{b^2} \right) \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{9}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] - \right. \right. \\
& \left. \left. \left( a + \sqrt{b^2} \right) \operatorname{AppellF1} \left[ \frac{7}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{9}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] \right) (a + \right. \\
& \left. \left. b \sin[c+dx] \right) \right) \right)
\end{aligned}$$

Problem 625: Result more than twice size of optimal antiderivative.

$$\int (e \cos(c + dx))^p \sqrt{a + b \sin(c + dx)} \, dx$$

Optimal (type 6, 156 leaves, 2 steps):

$$\frac{1}{3 b d} 2 e \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] \\ (e \cos[c+d x])^{-1+p} (a+b \sin[c+d x])^{3/2} \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{\frac{1-p}{2}} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{\frac{1-p}{2}}$$

Result (type 6, 447 leaves):

$$\begin{aligned}
& - \left( \left( 10 (a^2 - b^2)^2 \text{AppellF1} \left[ \frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right. \right. \\
& \left. \left. \left( e \cos[c+d x] \right)^p \sec[c+d x]^3 (a+b \sin[c+d x])^{3/2} \left( -\sqrt{b^2} + b \sin[c+d x] \right) \right. \right. \\
& \left. \left. \left( \sqrt{b^2} + b \sin[c+d x] \right) \right) \right) \Big/ \left( 3 b^3 \left( a - \sqrt{b^2} \right) \left( a + \sqrt{b^2} \right) d \right. \\
& \left. \left. \left( 5 (a^2 - b^2) \text{AppellF1} \left[ \frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] + (-1+p) \right. \right. \right. \\
& \left. \left. \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \right. \right. \right. \\
& \left. \left. \left( a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right) (a + \right. \\
& \left. \left. \left. b \sin[c+d x] \right) \right) \right) \right)
\end{aligned}$$

**Problem 626: Result more than twice size of optimal antiderivative.**

$$\int \frac{(e \cos[c+d x])^p}{\sqrt{a+b \sin[c+d x]}} dx$$

Optimal (type 6, 154 leaves, 2 steps):

$$\begin{aligned}
& \frac{1}{b d} 2 e \text{AppellF1} \left[ \frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{3}{2}, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b} \right] \\
& (e \cos[c+d x])^{-1+p} \sqrt{a+b \sin[c+d x]} \left( 1 - \frac{a+b \sin[c+d x]}{a-b} \right)^{\frac{1-p}{2}} \left( 1 - \frac{a+b \sin[c+d x]}{a+b} \right)^{\frac{1-p}{2}}
\end{aligned}$$

Result (type 6, 445 leaves):

$$\begin{aligned}
& - \left( \left( 6 (a^2 - b^2)^2 \text{AppellF1} \left[ \frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{3}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right. \right. \\
& \left. \left. \left( e \cos[c+d x] \right)^p \sec[c+d x]^3 \sqrt{a+b \sin[c+d x]} \left( -\sqrt{b^2} + b \sin[c+d x] \right) \right. \right. \\
& \left. \left. \left( \sqrt{b^2} + b \sin[c+d x] \right) \right) \right) \Big/ \left( b^3 \left( a - \sqrt{b^2} \right) \left( a + \sqrt{b^2} \right) d \right. \\
& \left. \left. \left( 3 (a^2 - b^2) \text{AppellF1} \left[ \frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{3}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] + (-1+p) \right. \right. \right. \\
& \left. \left. \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{3}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \right. \right. \right. \\
& \left. \left. \left( a + \sqrt{b^2} \right) \text{AppellF1} \left[ \frac{3}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right) (a + \right. \\
& \left. \left. \left. b \sin[c+d x] \right) \right) \right) \right)
\end{aligned}$$

### Problem 627: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^p}{(a + b \sin[c + d x])^{3/2}} dx$$

Optimal (type 6, 154 leaves, 2 steps):

$$-\left( \left( 2 e \text{AppellF1}\left[-\frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{1}{2}, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b} \right] (e \cos[c+d x])^{-1+p} \left( 1 - \frac{a+b \sin[c+d x]}{a-b} \right)^{\frac{1-p}{2}} \left( 1 - \frac{a+b \sin[c+d x]}{a+b} \right)^{\frac{1-p}{2}} \right) \right) / \left( b d \sqrt{a+b \sin[c+d x]} \right)$$

Result (type 6, 444 leaves):

$$\begin{aligned} & \left( 2 (a^2 - b^2)^2 \text{AppellF1}\left[-\frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{1}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right. \\ & \quad \left. (e \cos[c+d x])^p \sec[c+d x]^3 \left( \sqrt{b^2} - b \sin[c+d x] \right) \left( \sqrt{b^2} + b \sin[c+d x] \right) \right) / \\ & \left( b^3 \left( a - \sqrt{b^2} \right) \left( a + \sqrt{b^2} \right) d \sqrt{a+b \sin[c+d x]} \right. \\ & \quad \left( (-a^2 + b^2) \text{AppellF1}\left[-\frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{1}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \right. \\ & \quad \left. (-1+p) \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1}\left[\frac{1}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{3}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \right. \right. \\ & \quad \left. \left. \left( a + \sqrt{b^2} \right) \text{AppellF1}\left[\frac{1}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{3}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right) (a + \right. \\ & \quad \left. b \sin[c+d x]) \right) \right) \end{aligned}$$

### Problem 628: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + d x])^p}{(a + b \sin[c + d x])^{5/2}} dx$$

Optimal (type 6, 156 leaves, 2 steps):

$$-\left( \left( 2 e \text{AppellF1}\left[-\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, -\frac{1}{2}, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b} \right] (e \cos[c+d x])^{-1+p} \left( 1 - \frac{a+b \sin[c+d x]}{a-b} \right)^{\frac{1-p}{2}} \left( 1 - \frac{a+b \sin[c+d x]}{a+b} \right)^{\frac{1-p}{2}} \right) \right) / \left( 3 b d (a+b \sin[c+d x])^{3/2} \right)$$

Result (type 6, 446 leaves):

$$\begin{aligned}
& - \left( \left( 2 (a^2 - b^2)^2 \text{AppellF1} \left[ -\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, -\frac{1}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right. \right. \\
& \quad \left. \left. \left( e \cos[c+d x] \right)^p \sec[c+d x]^3 \left( \sqrt{b^2} - b \sin[c+d x] \right) \left( \sqrt{b^2} + b \sin[c+d x] \right) \right) \right) / \\
& \quad \left( 3 b^3 \left( a - \sqrt{b^2} \right) \left( a + \sqrt{b^2} \right) d \left( a + b \sin[c+d x] \right)^{3/2} \right. \\
& \quad \left( (a^2 - b^2) \text{AppellF1} \left[ -\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, -\frac{1}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - (-1+p) \right. \\
& \quad \left( \left( -a + \sqrt{b^2} \right) \text{AppellF1} \left[ -\frac{1}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{1}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] - \right. \\
& \quad \left. \left. \left( a + \sqrt{b^2} \right) \text{AppellF1} \left[ -\frac{1}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{1}{2}, \frac{a+b \sin[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+d x]}{a+\sqrt{b^2}} \right] \right) \left( a + \right. \right. \\
& \quad \left. \left. b \sin[c+d x] \right) \right) \right)
\end{aligned}$$

Problem 629: Unable to integrate problem.

$$\int (e \cos[c+d x])^p (a + b \sin[c+d x])^m dx$$

Optimal (type 6, 158 leaves, 2 steps):

$$\begin{aligned}
& \frac{1}{b d (1+m)} e \text{AppellF1} \left[ 1+m, \frac{1-p}{2}, \frac{1-p}{2}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b} \right] \\
& (e \cos[c+d x])^{-1+p} (a + b \sin[c+d x])^{1+m} \left( 1 - \frac{a+b \sin[c+d x]}{a-b} \right)^{\frac{1-p}{2}} \left( 1 - \frac{a+b \sin[c+d x]}{a+b} \right)^{\frac{1-p}{2}}
\end{aligned}$$

Result (type 8, 25 leaves):

$$\int (e \cos[c+d x])^p (a + b \sin[c+d x])^m dx$$

Problem 630: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos[c+d x]^7 (a + b \sin[c+d x])^m dx$$

Optimal (type 3, 254 leaves, 3 steps):

$$\begin{aligned}
& - \frac{(a^2 - b^2)^3 (a + b \sin[c+d x])^{1+m}}{b^7 d (1+m)} + \frac{6 a (a^2 - b^2)^2 (a + b \sin[c+d x])^{2+m}}{b^7 d (2+m)} - \\
& \frac{3 (5 a^4 - 6 a^2 b^2 + b^4) (a + b \sin[c+d x])^{3+m}}{b^7 d (3+m)} + \frac{4 a (5 a^2 - 3 b^2) (a + b \sin[c+d x])^{4+m}}{b^7 d (4+m)} - \\
& \frac{3 (5 a^2 - b^2) (a + b \sin[c+d x])^{5+m}}{b^7 d (5+m)} + \frac{6 a (a + b \sin[c+d x])^{6+m}}{b^7 d (6+m)} - \frac{(a + b \sin[c+d x])^{7+m}}{b^7 d (7+m)}
\end{aligned}$$

Result (type 3, 1639 leaves):

$$\begin{aligned}
 & \frac{1}{d} (a + b \sin[c + d x])^m \\
 & \left( - \left( \left( a (11520 a^6 - 48384 a^4 b^2 + 80640 a^2 b^4 - 80640 b^6 - 12096 a^4 b^2 m + 50232 a^2 b^4 m - \right. \right. \right. \\
 & \quad 112224 b^6 m + 1728 a^4 b^2 m^2 + 3324 a^2 b^4 m^2 - 54542 b^6 m^2 - 840 a^2 b^4 m^3 - \\
 & \quad 13125 b^6 m^3 - 12 a^2 b^4 m^4 - 1829 b^6 m^4 - 147 b^6 m^5 - 5 b^6 m^6 \left. ) \right) / \\
 & \quad \left( 16 b^7 (1+m) (2+m) (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \\
 & \quad \left( (176400 b^6 + 46080 a^6 m - 182016 a^4 b^2 m + 279936 a^2 b^4 m + 194868 b^6 m - 42624 a^4 b^2 m^2 + \right. \\
 & \quad 169440 a^2 b^4 m^2 + 78968 b^6 m^2 + 1152 a^4 b^2 m^3 + 29328 a^2 b^4 m^3 + 16299 b^6 m^3 + 1632 a^2 b^4 m^4 + \\
 & \quad 2027 b^6 m^4 + 48 a^2 b^4 m^5 + 153 b^6 m^5 + 5 b^6 m^6 \left( \frac{\frac{1}{i} \cos[c + d x]}{128 b^6} + \frac{\sin[c + d x]}{128 b^6} \right) \right) / \\
 & \quad \left( (1+m) (2+m) (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \\
 & \quad \left( (176400 b^6 + 46080 a^6 m - 182016 a^4 b^2 m + 279936 a^2 b^4 m + 194868 b^6 m - 42624 a^4 b^2 m^2 + \right. \\
 & \quad 169440 a^2 b^4 m^2 + 78968 b^6 m^2 + 1152 a^4 b^2 m^3 + 29328 a^2 b^4 m^3 + 16299 b^6 m^3 + 1632 a^2 b^4 m^4 + \\
 & \quad 2027 b^6 m^4 + 48 a^2 b^4 m^5 + 153 b^6 m^5 + 5 b^6 m^6 \left( \frac{\frac{1}{i} \cos[c + d x]}{128 b^6} + \frac{\sin[c + d x]}{128 b^6} \right) \right) / \\
 & \quad \left( (1+m) (2+m) (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \\
 & \quad \left( (1920 a^4 m - 7104 a^2 b^2 m + 10008 b^4 m - 1696 a^2 b^2 m^2 + 6370 b^4 m^2 - 32 a^2 b^2 m^3 + \right. \\
 & \quad 1411 b^4 m^3 + 134 b^4 m^4 + 5 b^4 m^5 \left( \frac{3 a \cos[2(c + d x)]}{64 b^5} - \frac{3 i a \sin[2(c + d x)]}{64 b^5} \right) \right) / \\
 & \quad \left( (2+m) (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \\
 & \quad \left( (1920 a^4 m - 7104 a^2 b^2 m + 10008 b^4 m - 1696 a^2 b^2 m^2 + 6370 b^4 m^2 - 32 a^2 b^2 m^3 + \right. \\
 & \quad 1411 b^4 m^3 + 134 b^4 m^4 + 5 b^4 m^5 \left( \frac{3 a \cos[2(c + d x)]}{64 b^5} + \frac{3 i a \sin[2(c + d x)]}{64 b^5} \right) \right) / \\
 & \quad \left( (2+m) (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \\
 & \quad \left( (5880 b^4 - 640 a^4 m + 2208 a^2 b^2 m + 3602 b^4 m + 552 a^2 b^2 m^2 + 797 b^4 m^2 + 24 a^2 b^2 m^3 + \right. \\
 & \quad 78 b^4 m^3 + 3 b^4 m^4 \left( -\frac{3 i \cos[3(c + d x)]}{128 b^4} + \frac{3 \sin[3(c + d x)]}{128 b^4} \right) \right) / \\
 & \quad \left( (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \left( (5880 b^4 - 640 a^4 m + 2208 a^2 b^2 m + \right. \\
 & \quad 3602 b^4 m + 552 a^2 b^2 m^2 + 797 b^4 m^2 + 24 a^2 b^2 m^3 + 78 b^4 m^3 + 3 b^4 m^4 \left( \frac{3 i \cos[3(c + d x)]}{128 b^4} + \frac{3 \sin[3(c + d x)]}{128 b^4} \right) \right) / \\
 & \quad \left( (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \\
 & \quad \left( (20 a^2 m - 64 b^2 m - 17 b^2 m^2 - b^2 m^3) \left( -\frac{3 a \cos[4(c + d x)]}{32 b^3} - \frac{3 i a \sin[4(c + d x)]}{32 b^3} \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
& \left( (4+m) (5+m) (6+m) (7+m) \right) + \\
& \left( (20 a^2 m - 64 b^2 m - 17 b^2 m^2 - b^2 m^3) \left( -\frac{3 a \cos[4(c+d x)]}{32 b^3} + \frac{3 i a \sin[4(c+d x)]}{32 b^3} \right) \right) / \\
& \left( (4+m) (5+m) (6+m) (7+m) \right) + \\
& \frac{\left( 294 b^2 + 24 a^2 m + 79 b^2 m + 5 b^2 m^2 \right) \left( -\frac{i \cos[5(c+d x)]}{128 b^2} + \frac{\sin[5(c+d x)]}{128 b^2} \right)}{(5+m) (6+m) (7+m)} + \\
& \frac{\left( 294 b^2 + 24 a^2 m + 79 b^2 m + 5 b^2 m^2 \right) \left( \frac{i \cos[5(c+d x)]}{128 b^2} + \frac{\sin[5(c+d x)]}{128 b^2} \right)}{(5+m) (6+m) (7+m)} + \\
& \frac{a m \cos[6(c+d x)] - i a m \sin[6(c+d x)]}{64 b} + \\
& \frac{(6+m) (7+m)}{64 b} + \\
& \frac{a m \cos[6(c+d x)] + i a m \sin[6(c+d x)]}{64 b} + \\
& \frac{(6+m) (7+m)}{64 b} - \\
& \frac{\frac{1}{128} i \cos[7(c+d x)] + \frac{1}{128} \sin[7(c+d x)]}{7+m} + \\
& \frac{\frac{1}{128} i \cos[7(c+d x)] + \frac{1}{128} \sin[7(c+d x)]}{7+m}
\end{aligned}$$

Problem 634: Unable to integrate problem.

$$\int \sec[c+d x] (a+b \sin[c+d x])^m \, dx$$

Optimal (type 5, 115 leaves, 5 steps):

$$\begin{aligned}
& - \left( \left( \text{Hypergeometric2F1}[1, 1+m, 2+m, \frac{a+b \sin[c+d x]}{a-b}] (a+b \sin[c+d x])^{1+m} \right) / \right. \\
& \left. (2(a-b) d (1+m)) \right) + \\
& \left( \text{Hypergeometric2F1}[1, 1+m, 2+m, \frac{a+b \sin[c+d x]}{a+b}] (a+b \sin[c+d x])^{1+m} \right) / \\
& (2(a+b) d (1+m))
\end{aligned}$$

Result (type 8, 21 leaves):

$$\int \sec[c+d x] (a+b \sin[c+d x])^m \, dx$$

Problem 635: Unable to integrate problem.

$$\int \sec[c+d x]^3 (a+b \sin[c+d x])^m \, dx$$

Optimal (type 5, 183 leaves, 6 steps):

$$\begin{aligned}
& - \left( \left( (a-b)(1-m) \right) \text{Hypergeometric2F1}[1, 1+m, 2+m, \frac{a+b \sin[c+d x]}{a-b}] (a+b \sin[c+d x])^{1+m} \right) / \\
& \quad \left( 4(a-b)^2 d (1+m) \right) + \\
& \left( (a+b-b m) \text{Hypergeometric2F1}[1, 1+m, 2+m, \frac{a+b \sin[c+d x]}{a+b}] (a+b \sin[c+d x])^{1+m} \right) / \\
& \quad \left( 4(a+b)^2 d (1+m) \right) - \frac{\sec[c+d x]^2 (b-a \sin[c+d x]) (a+b \sin[c+d x])^{1+m}}{2(a^2-b^2) d}
\end{aligned}$$

Result (type 8, 23 leaves):

$$\int \sec[c+d x]^3 (a+b \sin[c+d x])^m \, dx$$

Problem 636: Unable to integrate problem.

$$\int \sec[c+d x]^5 (a+b \sin[c+d x])^m \, dx$$

Optimal (type 5, 305 leaves, 7 steps):

$$\begin{aligned}
& - \left( \left( (3 a^2 - 3 a b (2 - m) + b^2 (3 - 4 m + m^2)) \text{Hypergeometric2F1}[1, 1+m, 2+m, \frac{a+b \sin[c+d x]}{a-b}] \right. \right. \\
& \quad \left. \left. (a+b \sin[c+d x])^{1+m} \right) / \left( 16 (a-b)^3 d (1+m) \right) \right) + \\
& \left( (3 a^2 + 3 a b (2 - m) + b^2 (3 - 4 m + m^2)) \text{Hypergeometric2F1}[1, 1+m, 2+m, \frac{a+b \sin[c+d x]}{a+b}] \right. \\
& \quad \left. (a+b \sin[c+d x])^{1+m} \right) / \left( 16 (a+b)^3 d (1+m) \right) - \\
& \frac{\sec[c+d x]^4 (b-a \sin[c+d x]) (a+b \sin[c+d x])^{1+m}}{4(a^2-b^2) d} + \\
& \frac{1}{8(a^2-b^2)^2 d} \\
& \sec[c+d x]^2 (a+b \sin[c+d x])^{1+m} \\
& (b(b^2(3-m)-a^2(1+m))+a(3a^2-b^2(5-2m)) \sin[c+d x])
\end{aligned}$$

Result (type 8, 23 leaves):

$$\int \sec[c+d x]^5 (a+b \sin[c+d x])^m \, dx$$

Problem 637: Unable to integrate problem.

$$\int \cos[c+d x]^4 (a+b \sin[c+d x])^m \, dx$$

Optimal (type 6, 129 leaves, 2 steps):

$$\left( \text{AppellF1} \left[ 1+m, -\frac{3}{2}, -\frac{3}{2}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b} \right] \cos[c+d x]^3 \right. \\ \left. (a+b \sin[c+d x])^{1+m} \right) \bigg/ \left( b d (1+m) \left( 1 - \frac{a+b \sin[c+d x]}{a-b} \right)^{3/2} \left( 1 - \frac{a+b \sin[c+d x]}{a+b} \right)^{3/2} \right)$$

Result (type 8, 23 leaves):

$$\int \cos[c+d x]^4 (a+b \sin[c+d x])^m \, dx$$

Problem 638: Unable to integrate problem.

$$\int \cos[c+d x]^2 (a+b \sin[c+d x])^m \, dx$$

Optimal (type 6, 127 leaves, 2 steps):

$$\left( \text{AppellF1} \left[ 1+m, -\frac{1}{2}, -\frac{1}{2}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b} \right] \cos[c+d x] \right. \\ \left. (a+b \sin[c+d x])^{1+m} \right) \bigg/ \left( b d (1+m) \sqrt{1 - \frac{a+b \sin[c+d x]}{a-b}} \sqrt{1 - \frac{a+b \sin[c+d x]}{a+b}} \right)$$

Result (type 8, 23 leaves):

$$\int \cos[c+d x]^2 (a+b \sin[c+d x])^m \, dx$$

Problem 639: Unable to integrate problem.

$$\int \sec[c+d x]^2 (a+b \sin[c+d x])^m \, dx$$

Optimal (type 6, 129 leaves, 2 steps):

$$\frac{1}{b d (1+m)} \text{AppellF1} \left[ 1+m, \frac{3}{2}, \frac{3}{2}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b} \right] \\ \sec[c+d x]^3 (a+b \sin[c+d x])^{1+m} \left( 1 - \frac{a+b \sin[c+d x]}{a-b} \right)^{3/2} \left( 1 - \frac{a+b \sin[c+d x]}{a+b} \right)^{3/2}$$

Result (type 8, 23 leaves):

$$\int \sec[c+d x]^2 (a+b \sin[c+d x])^m \, dx$$

Problem 640: Unable to integrate problem.

$$\int \sec[c+d x]^4 (a+b \sin[c+d x])^m \, dx$$

Optimal (type 6, 129 leaves, 2 steps):

$$\frac{1}{b d (1+m)} \text{AppellF1}\left[1+m, \frac{5}{2}, \frac{5}{2}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] \\ \sec[c+d x]^5 (a+b \sin[c+d x])^{1+m} \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{5/2} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{5/2}$$

Result (type 8, 23 leaves):

$$\int \sec[c+d x]^4 (a+b \sin[c+d x])^m dx$$

Problem 641: Unable to integrate problem.

$$\int (\cos[c+d x])^{5/2} (a+b \sin[c+d x])^m dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left( e \text{AppellF1}\left[1+m, -\frac{3}{4}, -\frac{3}{4}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] (\cos[c+d x])^{3/2} \right. \\ \left. (a+b \sin[c+d x])^{1+m} \right) / \left( b d (1+m) \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{3/4} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{3/4} \right)$$

Result (type 8, 27 leaves):

$$\int (\cos[c+d x])^{5/2} (a+b \sin[c+d x])^m dx$$

Problem 642: Unable to integrate problem.

$$\int (\cos[c+d x])^{3/2} (a+b \sin[c+d x])^m dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left( e \text{AppellF1}\left[1+m, -\frac{1}{4}, -\frac{1}{4}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] \sqrt{\cos[c+d x]} \right. \\ \left. (a+b \sin[c+d x])^{1+m} \right) / \left( b d (1+m) \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{1/4} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{1/4} \right)$$

Result (type 8, 27 leaves):

$$\int (\cos[c+d x])^{3/2} (a+b \sin[c+d x])^m dx$$

Problem 643: Unable to integrate problem.

$$\int \sqrt{\cos[c+d x]} (a+b \sin[c+d x])^m dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left( e \text{AppellF1}\left[1+m, \frac{1}{4}, \frac{1}{4}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] (a+b \sin[c+d x])^{1+m} \right. \\ \left. \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{1/4} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{1/4}\right) / \left(b d (1+m) \sqrt{e \cos[c+d x]}\right)$$

Result (type 8, 27 leaves):

$$\int \sqrt{e \cos[c+d x]} (a+b \sin[c+d x])^m dx$$

Problem 644: Unable to integrate problem.

$$\int \frac{(a+b \sin[c+d x])^m}{\sqrt{e \cos[c+d x]}} dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left( e \text{AppellF1}\left[1+m, \frac{3}{4}, \frac{3}{4}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] (a+b \sin[c+d x])^{1+m} \right. \\ \left. \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{3/4} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{3/4}\right) / \left(b d (1+m) (e \cos[c+d x])^{3/2}\right)$$

Result (type 8, 27 leaves):

$$\int \frac{(a+b \sin[c+d x])^m}{\sqrt{e \cos[c+d x]}} dx$$

Problem 645: Unable to integrate problem.

$$\int \frac{(a+b \sin[c+d x])^m}{(e \cos[c+d x])^{3/2}} dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left( e \text{AppellF1}\left[1+m, \frac{5}{4}, \frac{5}{4}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] (a+b \sin[c+d x])^{1+m} \right. \\ \left. \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{5/4} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{5/4}\right) / \left(b d (1+m) (e \cos[c+d x])^{5/2}\right)$$

Result (type 8, 27 leaves):

$$\int \frac{(a+b \sin[c+d x])^m}{(e \cos[c+d x])^{5/2}} dx$$

Problem 646: Unable to integrate problem.

$$\int \frac{(a+b \sin[c+d x])^m}{(e \cos[c+d x])^{5/2}} dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left( e \text{AppellF1}\left[1+m, \frac{7}{4}, \frac{7}{4}, 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] (a+b \sin[c+d x])^{1+m} \right. \\ \left. \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{7/4} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{7/4}\right) / \left(b d (1+m) (e \cos[c+d x])^{7/2}\right)$$

Result (type 8, 27 leaves):

$$\int \frac{(a+b \sin[c+d x])^m}{(e \cos[c+d x])^{5/2}} dx$$

Problem 647: Unable to integrate problem.

$$\int (e \cos[c+d x])^{-4-m} (a+b \sin[c+d x])^m dx$$

Optimal (type 5, 598 leaves, 9 steps):

$$- \frac{(e \cos[c+d x])^{-3-m} (a+b \sin[c+d x])^{1+m}}{(a-b) d e (3+m)} + \frac{2 b (e \cos[c+d x])^{-1-m} (a+b \sin[c+d x])^{1+m}}{(a-b)^2 d e^3 (1+m) (3+m)} + \\ \frac{a (e \cos[c+d x])^{-3-m} (1+\sin[c+d x]) (a+b \sin[c+d x])^{1+m}}{(a^2-b^2) d e (3+m)} + \\ \left( a (3 b + a (2+m)) (e \cos[c+d x])^{-3-m} (1-\sin[c+d x]) (1+\sin[c+d x]) (a+b \sin[c+d x])^{1+m} \right) / \\ \left( (a-b) (a+b)^2 d e (1+m) (3+m) \right) - \\ \left( 2^{\frac{3-m}{2}} a b (e \cos[c+d x])^{-1-m} \text{Hypergeometric2F1}\left[\frac{1}{2} (-1-m), \frac{1+m}{2}, \frac{1-m}{2}, \right. \right. \\ \left. \left. \frac{(a-b) (1-\sin[c+d x])}{2 (a+b \sin[c+d x])} \right] \left( \frac{(a+b) (1+\sin[c+d x])}{a+b \sin[c+d x]} \right)^{\frac{1+m}{2}} (a+b \sin[c+d x])^{1+m} \right) / \\ \left( (a-b)^2 (a+b) d e^3 (1+m) (3+m) \right) - \left( 2^{-\frac{1-m}{2}} a (2 a b - b^2 + a^2 (2+m)) (e \cos[c+d x])^{-3-m} \right. \\ \left. \text{Hypergeometric2F1}\left[\frac{1-m}{2}, \frac{3+m}{2}, \frac{3-m}{2}, \frac{(a-b) (1-\sin[c+d x])}{2 (a+b \sin[c+d x])} \right] (1-\sin[c+d x])^2 \right. \\ \left. \left( \frac{(a+b) (1+\sin[c+d x])}{a+b \sin[c+d x]} \right)^{\frac{3+m}{2}} (a+b \sin[c+d x])^{1+m} \right) / \left( (a-b) (a+b)^3 d e (1-m) (3+m) \right)$$

Result (type 8, 29 leaves):

$$\int (e \cos[c+d x])^{-4-m} (a+b \sin[c+d x])^m dx$$

Problem 648: Unable to integrate problem.

$$\int (e \cos[c+d x])^{-3-m} (a+b \sin[c+d x])^m dx$$

Optimal (type 5, 311 leaves, ? steps):

$$\begin{aligned} & \left( (\cos[c+dx])^{-m} \sec[c+dx]^4 (-1 + \sin[c+dx]) (1 + \sin[c+dx]) (a + b \sin[c+dx])^{1+m} \right) / \\ & \quad \left( (a-b) d e^3 (2+m) \right) + \left( (-2b+a(2+m)) (\cos[c+dx])^{-m} \sec[c+dx]^4 \right. \\ & \quad \left. (-1 + \sin[c+dx]) (1 + \sin[c+dx])^2 (a + b \sin[c+dx])^{1+m} \right) / \left( (a-b)^2 d e^3 m (2+m) \right) - \\ & \left( (-b^2 + a^2 (1+m)) (\cos[c+dx])^{-m} \text{Hypergeometric2F1} \left[ \frac{m}{2}, 1+m, 2+m, \right. \right. \\ & \quad \left. \left. - \frac{2 (a + b \sin[c+dx])}{(a-b) (-1 + \sin[c+dx])} \right] \sec[c+dx]^4 (1 + \sin[c+dx])^3 \right. \\ & \quad \left. \left( \frac{(a+b) (1 + \sin[c+dx])}{(a-b) (-1 + \sin[c+dx])} \right)^{\frac{1}{2} (-2+m)} (a + b \sin[c+dx])^{1+m} \right) / \left( (a-b)^3 d e^3 m (1+m) \right) \end{aligned}$$

Result (type 8, 29 leaves):

$$\int (\cos[c+dx])^{-3-m} (a + b \sin[c+dx])^m \, dx$$

Problem 649: Unable to integrate problem.

$$\int (\cos[c+dx])^{-2-m} (a + b \sin[c+dx])^m \, dx$$

Optimal (type 5, 201 leaves, 3 steps):

$$\begin{aligned} & - \frac{(\cos[c+dx])^{-1-m} (a + b \sin[c+dx])^{1+m}}{(a-b) d e (1+m)} + \left( 2^{\frac{1-m}{2}} a (\cos[c+dx])^{-1-m} \right. \\ & \quad \left. \text{Hypergeometric2F1} \left[ \frac{1}{2} (-1-m), \frac{1+m}{2}, \frac{1-m}{2}, \frac{(a-b) (1 - \sin[c+dx])}{2 (a + b \sin[c+dx])} \right] \right. \\ & \quad \left. \left( \frac{(a+b) (1 + \sin[c+dx])}{a + b \sin[c+dx]} \right)^{\frac{1+m}{2}} (a + b \sin[c+dx])^{1+m} \right) / ((a^2 - b^2) d e (1+m)) \end{aligned}$$

Result (type 8, 29 leaves):

$$\int (\cos[c+dx])^{-2-m} (a + b \sin[c+dx])^m \, dx$$

Problem 650: Unable to integrate problem.

$$\int (\cos[c+dx])^{-1-m} (a + b \sin[c+dx])^m \, dx$$

Optimal (type 5, 132 leaves, 1 step):

$$\frac{1}{(a+b) d (1+m)} e (\cos(c+dx))^{-2-m} \text{Hypergeometric2F1}\left[1+m, \frac{2+m}{2}, 2+m, \frac{2(a+b \sin(c+dx))}{(a+b)(1+\sin(c+dx))}\right] (1-\sin(c+dx)) \left(-\frac{(a-b)(1-\sin(c+dx))}{(a+b)(1+\sin(c+dx))}\right)^{m/2} (a+b \sin(c+dx))^{1+m}$$

Result (type 8, 29 leaves):

$$\int (\cos(c+dx))^{-1-m} (a+b \sin(c+dx))^m dx$$

Problem 651: Unable to integrate problem.

$$\int (\cos(c+dx))^{-m} (a+b \sin(c+dx))^m dx$$

Optimal (type 6, 152 leaves, 2 steps):

$$\frac{1}{b d (1+m)} e \text{AppellF1}\left[1+m, \frac{1+m}{2}, \frac{1+m}{2}, 2+m, \frac{a+b \sin(c+dx)}{a-b}, \frac{a+b \sin(c+dx)}{a+b}\right] (\cos(c+dx))^{-1-m} (a+b \sin(c+dx))^{1+m} \left(1 - \frac{a+b \sin(c+dx)}{a-b}\right)^{\frac{1+m}{2}} \left(1 - \frac{a+b \sin(c+dx)}{a+b}\right)^{\frac{1+m}{2}}$$

Result (type 8, 27 leaves):

$$\int (\cos(c+dx))^{-m} (a+b \sin(c+dx))^m dx$$

Problem 652: Unable to integrate problem.

$$\int (\cos(c+dx))^{1-m} (a+b \sin(c+dx))^m dx$$

Optimal (type 6, 142 leaves, 2 steps):

$$\frac{1}{b d (1+m)} e \text{AppellF1}\left[1+m, \frac{m}{2}, \frac{m}{2}, 2+m, \frac{a+b \sin(c+dx)}{a-b}, \frac{a+b \sin(c+dx)}{a+b}\right] (\cos(c+dx))^{-m} (a+b \sin(c+dx))^{1+m} \left(1 - \frac{a+b \sin(c+dx)}{a-b}\right)^{m/2} \left(1 - \frac{a+b \sin(c+dx)}{a+b}\right)^{m/2}$$

Result (type 8, 29 leaves):

$$\int (\cos(c+dx))^{1-m} (a+b \sin(c+dx))^m dx$$

Problem 653: Unable to integrate problem.

$$\int (\cos(c+dx))^{2-m} (a+b \sin(c+dx))^m dx$$

Optimal (type 6, 152 leaves, 2 steps):

$$\frac{1}{b d (1+m)} e \text{AppellF1}\left[1+m, \frac{1}{2} (-1+m), \frac{1}{2} (-1+m), 2+m, \frac{a+b \sin[c+d x]}{a-b}, \frac{a+b \sin[c+d x]}{a+b}\right] \\ (e \cos[c+d x])^{1-m} (a+b \sin[c+d x])^{1+m} \\ \left(1 - \frac{a+b \sin[c+d x]}{a-b}\right)^{\frac{1}{2} (-1+m)} \left(1 - \frac{a+b \sin[c+d x]}{a+b}\right)^{\frac{1}{2} (-1+m)}$$

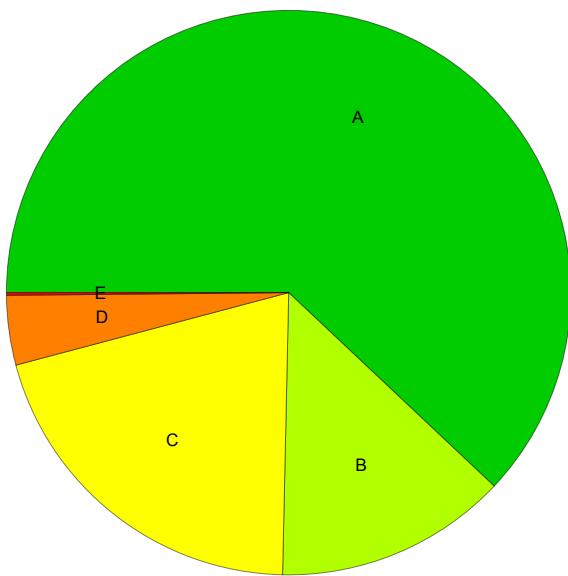
Result (type 8, 29 leaves):

$$\int (e \cos[c+d x])^{2-m} (a+b \sin[c+d x])^m dx$$

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## Summary of Integration Test Results

653 integration problems



A - 405 optimal antiderivatives

B - 87 more than twice size of optimal antiderivatives

C - 134 unnecessarily complex antiderivatives

D - 26 unable to integrate problems

E - 1 integration timeouts