X: 
$$\int Tan \left[ a + b x + c x^2 \right]^n dx$$

Rule:

$$\int\! Tan \big[ \, a + b \, x + c \, x^2 \big]^n \, \mathrm{d}x \, \, \longrightarrow \, \, \int\! Tan \big[ \, a + b \, x + c \, x^2 \big]^n \, \mathrm{d}x$$

```
Int[Tan[a_.+b_.*x_+c_.*x_^2]^n_.,x_Symbol] :=
   Unintegrable[Tan[a+b*x+c*x^2]^n,x] /;
FreeQ[{a,b,c,n},x]

Int[Cot[a_.+b_.*x_+c_.*x_^2]^n_.,x_Symbol] :=
   Unintegrable[Cot[a+b*x+c*x^2]^n,x] /;
FreeQ[{a,b,c,n},x]
```

Rules for integrands of the form  $(d + e x)^m Tan [a + b x + c x^2]^n$ 

1. 
$$\int (d + e x) Tan[a + b x + c x^2] dx$$
  
1:  $\int (d + e x) Tan[a + b x + c x^2] dx$  when  $2 c d - b e == 0$ 

Rule: If 2 c d - b e = 0, then

$$\int (d+e\,x)\,\, \mathsf{Tan} \left[ a+b\,x+c\,\,x^2 \right] \,\mathrm{d}x \,\, \longrightarrow \,\, -\frac{e\,\mathsf{Log} \left[ \mathsf{Cos} \left[ a+b\,x+c\,\,x^2 \right] \right]}{2\,c}$$

```
Int[(d_+e_.*x_)*Tan[a_.+b_.*x_+c_.*x_^2],x_Symbol] :=
    -e*Log[Cos[a+b*x+c*x^2]]/(2*c) /;
FreeQ[{a,b,c,d,e},x] && EqQ[2*c*d-b*e,0]

Int[(d_+e_.*x_)*Cot[a_.+b_.*x_+c_.*x_^2],x_Symbol] :=
    e*Log[Sin[a+b*x+c*x^2]]/(2*c) /;
FreeQ[{a,b,c,d,e},x] && EqQ[2*c*d-b*e,0]
```

2: 
$$\int (d + e x) Tan[a + b x + c x^2] dx$$
 when  $2 c d - b e \neq 0$ 

Rule: If  $2 c d - b e \neq 0$ , then

$$\int (d+e\,x)\,\,\mathsf{Tan}\big[a+b\,x+c\,x^2\big]\,\,\mathrm{d}x\,\,\rightarrow\,\,-\frac{e\,\mathsf{Log}\big[\mathsf{Cos}\big[a+b\,x+c\,x^2\big]\big]}{2\,c}\,+\,\frac{2\,c\,d-b\,e}{2\,c}\,\int\!\mathsf{Tan}\big[a+b\,x+c\,x^2\big]\,\,\mathrm{d}x$$

```
Int[(d_.+e_.*x_)*Tan[a_.+b_.*x_+c_.*x_^2],x_Symbol] :=
    -e*Log[Cos[a+b*x+c*x^2]]/(2*c) +
    (2*c*d-b*e)/(2*c)*Int[Tan[a+b*x+c*x^2],x] /;
FreeQ[{a,b,c,d,e},x] && NeQ[2*c*d-b*e,0]

Int[(d_.+e_.*x_)*Cot[a_.+b_.*x_+c_.*x_^2],x_Symbol] :=
    e*Log[Sin[a+b*x+c*x^2]]/(2*c) +
    (2*c*d-b*e)/(2*c)*Int[Cot[a+b*x+c*x^2],x] /;
FreeQ[{a,b,c,d,e},x] && NeQ[2*c*d-b*e,0]
```

**X:** 
$$\int (d + e x)^m Tan[a + b x + c x^2] dx$$
 when m > 1

Note: This rule is valid, but to be useful need a rule for reducing integrands of the form  $x^m Log [Cos [a + b x + c x^2]]$ .

Rule: If m > 1, then

$$\int x^m \, Tan \left[ a + b \, x + c \, x^2 \right] \, dx \, \rightarrow \\ - \frac{x^{m-1} \, Log \left[ Cos \left[ a + b \, x + c \, x^2 \right] \right]}{2 \, c} \, - \frac{b}{2 \, c} \, \int x^{m-1} \, Tan \left[ a + b \, x + c \, x^2 \right] \, dx + \frac{m-1}{2 \, c} \, \int x^{m-2} \, Log \left[ Cos \left[ a + b \, x + c \, x^2 \right] \right] \, dx$$

```
(* Int[x_^m_*Tan[a_.+b_.*x_+c_.*x_^2],x_Symbol] :=
    -x^(m-1)*Log[Cos[a+b*x+c*x^2]]/(2*c) -
    b/(2*c)*Int[x^(m-1)*Tan[a+b*x+c*x^2],x] +
    (m-1)/(2*c)*Int[x^(m-2)*Log[Cos[a+b*x+c*x^2]],x] /;
FreeQ[{a,b,c},x] && GtQ[m,1] *)

(* Int[x_^m_*Cot[a_.+b_.*x_+c_.*x_^2],x_Symbol] :=
    x^(m-1)*Log[Sin[a+b*x+c*x^2]]/(2*c) -
    b/(2*c)*Int[x^(m-1)*Cot[a+b*x+c*x^2],x] -
    (m-1)/(2*c)*Int[x^(m-2)*Log[Sin[a+b*x+c*x^2]],x] /;
FreeQ[{a,b,c},x] && GtQ[m,1]*)
```

X: 
$$\int (d + e x)^m Tan[a + b x + c x^2]^n dx$$

Rule:

$$\int (d+ex)^m \operatorname{Tan} \left[a+bx+cx^2\right]^n dx \ \longrightarrow \ \int (d+ex)^m \operatorname{Tan} \left[a+bx+cx^2\right]^n dx$$

```
Int[(d_.+e_.*x_)^m_.*Tan[a_.+b_.*x_+c_.*x_^2]^n_.,x_Symbol] :=
   Unintegrable[(d+e*x)^m*Tan[a+b*x+c*x^2]^n,x] /;
FreeQ[{a,b,c,d,e,m,n},x]

Int[(d_.+e_.*x_)^m_.*Cot[a_.+b_.*x_+c_.*x_^2]^n_.,x_Symbol] :=
   Unintegrable[(d+e*x)^m*Cot[a+b*x+c*x^2]^n,x] /;
FreeQ[{a,b,c,d,e,m,n},x]
```