#### Rules for integrands involving hyperbolic integral functions

1.  $\int u \, SinhIntegral[a + b \, x] \, dx$ 

**Derivation: Integration by parts** 

Rule:

$$\int SinhIntegral[a+bx] dx \rightarrow \frac{(a+bx) SinhIntegral[a+bx]}{b} - \frac{Cosh[a+bx]}{b}$$

# Program code:

```
Int[SinhIntegral[a_.+b_.*x_],x_Symbol] :=
    (a+b*x)*SinhIntegral[a+b*x]/b - Cosh[a+b*x]/b/;
FreeQ[{a,b},x]

Int[CoshIntegral[a_.+b_.*x_],x_Symbol] :=
    (a+b*x)*CoshIntegral[a+b*x]/b - Sinh[a+b*x]/b /;
FreeQ[{a,b},x]
```

Basis: SinhIntegral[z] = 
$$-\frac{1}{2}$$
 (ExpIntegralE[1, -z] - ExpIntegralE[1, z] + Log[-z] - Log[z])

Basis: CoshIntegral[z] = 
$$-\frac{1}{2}$$
 (ExpIntegralE[1, -z] + ExpIntegralE[1, z] + Log[-z] - Log[z])

Rule:

$$\int \frac{\text{SinhIntegral}[b \times]}{x} \, dx \rightarrow$$

 $\frac{1}{2}$  b x HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, -b x] +  $\frac{1}{2}$  b x HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, b x]

### Program code:

2: 
$$\int (c + dx)^m SinhIntegral[a + bx] dx$$
 when  $m \neq -1$ 

### **Derivation: Integration by parts**

### Rule: If $m \neq -1$ , then

$$\int (c+d\,x)^{\,m}\,SinhIntegral\,[a+b\,x]\,\,\mathrm{d}x\,\,\rightarrow\,\,\frac{(c+d\,x)^{\,m+1}\,SinhIntegral\,[a+b\,x]}{d\,(m+1)}\,-\,\frac{b}{d\,(m+1)}\,\int\frac{(c+d\,x)^{\,m+1}\,Sinh\,[a+b\,x]}{a+b\,x}\,\,\mathrm{d}x$$

```
Int[(c_.+d_.*x_)^m_.*SinhIntegral[a_.+b_.*x_],x_Symbol] :=
    (c+d*x)^(m+1)*SinhIntegral[a+b*x]/(d*(m+1)) -
    b/(d*(m+1))*Int[(c+d*x)^(m+1)*Sinh[a+b*x]/(a+b*x),x] /;
FreeQ[{a,b,c,d,m},x] && NeQ[m,-1]

Int[(c_.+d_.*x_)^m_.*CoshIntegral[a_.+b_.*x_],x_Symbol] :=
    (c+d*x)^(m+1)*CoshIntegral[a+b*x]/(d*(m+1)) -
    b/(d*(m+1))*Int[(c+d*x)^(m+1)*Cosh[a+b*x]/(a+b*x),x] /;
FreeQ[{a,b,c,d,m},x] && NeQ[m,-1]
```

```
    2.  \int u SinhIntegral [a + b x] 2 dx
    1:  \int SinhIntegral [a + b x] 2 dx
```

Rule:

$$\int SinhIntegral \left[ a + b \, x \right]^2 \, dx \, \, \rightarrow \, \, \frac{\left( a + b \, x \right) \, SinhIntegral \left[ a + b \, x \right]^2}{b} \, - \, 2 \, \int Sinh \left[ a + b \, x \right] \, SinhIntegral \left[ a + b \, x \right] \, dx$$

```
Int[SinhIntegral[a_.+b_.*x_]^2,x_Symbol] :=
    (a+b*x)*SinhIntegral[a+b*x]^2/b -
    2*Int[Sinh[a+b*x]*SinhIntegral[a+b*x],x] /;
FreeQ[{a,b},x]

Int[CoshIntegral[a_.+b_.*x_]^2,x_Symbol] :=
    (a+b*x)*CoshIntegral[a+b*x]^2/b -
    2*Int[Cosh[a+b*x]*CoshIntegral[a+b*x],x] /;
FreeQ[{a,b},x]
```

```
2. \int (c + dx)^{m} SinhIntegral[a + bx]^{2} dx
1: \int x^{m} SinhIntegral[bx]^{2} dx \text{ when } m \in \mathbb{Z}^{+}
```

Rule: If  $m \in \mathbb{Z}^+$ , then

$$\int x^m \, SinhIntegral[b \, x]^2 \, dlx \, \, \longrightarrow \, \, \frac{x^{m+1} \, SinhIntegral[b \, x]^2}{m+1} \, - \, \frac{2}{m+1} \, \int x^m \, Sinh[b \, x] \, SinhIntegral[b \, x] \, dlx$$

# Program code:

```
Int[x_^m_.*SinhIntegral[b_.*x_]^2,x_Symbol] :=
    x^(m+1)*SinhIntegral[b*x]^2/(m+1) -
    2/(m+1)*Int[x^m*Sinh[b*x]*SinhIntegral[b*x],x] /;
FreeQ[b,x] && IGtQ[m,0]

Int[x_^m_.*CoshIntegral[b_.*x_]^2,x_Symbol] :=
    x^(m+1)*CoshIntegral[b*x]^2/(m+1) -
    2/(m+1)*Int[x^m*Cosh[b*x]*CoshIntegral[b*x],x] /;
FreeQ[b,x] && IGtQ[m,0]
```

2: 
$$\int (c + dx)^{m} SinhIntegral[a + bx]^{2} dx when m \in \mathbb{Z}^{+}$$

### Derivation: Iterated integration by parts

Rule: If  $m \in \mathbb{Z}^+$ , then

$$\frac{\int (c + dx)^{m} \operatorname{SinhIntegral}[a + bx]^{2} dx \longrightarrow}{\frac{(a + bx) (c + dx)^{m} \operatorname{SinhIntegral}[a + bx]^{2}}{b (m + 1)}}$$

$$\frac{2}{m+1}\int (c+d\,x)^{\,m}\,Sinh[a+b\,x]\,\,SinhIntegral[a+b\,x]\,\,dx + \frac{(b\,c-a\,d)\,\,m}{b\,(m+1)}\int (c+d\,x)^{\,m-1}\,SinhIntegral[a+b\,x]^{\,2}\,dx$$

### Program code:

```
Int[(c_.+d_.*x_)^m_.*SinhIntegral[a_+b_.*x_]^2,x_Symbol] :=
    (a+b*x)*(c+d*x)^m*SinhIntegral[a+b*x]^2/(b*(m+1)) -
    2/(m+1)*Int[(c+d*x)^m*Sinh[a+b*x]*SinhIntegral[a+b*x],x] +
    (b*c-a*d)*m/(b*(m+1))*Int[(c+d*x)^(m-1)*SinhIntegral[a+b*x]^2,x] /;
FreeQ[{a,b,c,d},x] && IGtQ[m,0]

Int[(c_.+d_.*x_)^m_.*CoshIntegral[a_+b_.*x_]^2,x_Symbol] :=
    (a+b*x)*(c+d*x)^m*CoshIntegral[a+b*x]^2/(b*(m+1)) -
    2/(m+1)*Int[(c+d*x)^m*Cosh[a+b*x]*CoshIntegral[a+b*x],x] +
    (b*c-a*d)*m/(b*(m+1))*Int[(c+d*x)^(m-1)*CoshIntegral[a+b*x]^2,x] /;
FreeQ[{a,b,c,d},x] && IGtQ[m,0]
```

```
x: \int x^m SinhIntegral[a + b x]^2 dx when m + 2 \in \mathbb{Z}^-
```

#### Derivation: Inverted integration by parts

## Rule: If $m + 2 \in \mathbb{Z}^-$ , then

$$\int x^m \, SinhIntegral[a+b\,x]^2 \, dx \, \rightarrow \, \frac{b\,x^{m+2} \, SinhIntegral[a+b\,x]^2}{a\,(m+1)} + \frac{x^{m+1} \, SinhIntegral[a+b\,x]^2}{m+1} - \frac{2\,b}{a\,(m+1)} \, \int x^{m+1} \, Sinh[a+b\,x] \, SinhIntegral[a+b\,x] \, dx - \frac{b\,(m+2)}{a\,(m+1)} \, \int x^{m+1} \, SinhIntegral[a+b\,x]^2 \, dx$$

```
(* Int[x_^m_.*SinhIntegral[a_+b_.*x_]^2,x_Symbol] :=
b*x^(m+2)*SinhIntegral[a+b*x]^2/(a*(m+1)) +
    x^(m+1)*SinhIntegral[a+b*x]^2/(m+1) -
    2*b/(a*(m+1))*Int[x^(m+1)*Sinh[a+b*x]*SinhIntegral[a+b*x],x] -
    b*(m+2)/(a*(m+1))*Int[x^(m+1)*SinhIntegral[a+b*x]^2,x] /;
FreeQ[{a,b},x] && ILtQ[m,-2] *)
```

```
(* Int[x_^m_.*CoshIntegral[a_+b_.*x_]^2,x_Symbol] :=
b*x^(m+2)*CoshIntegral[a+b*x]^2/(a*(m+1)) +
    x^(m+1)*CoshIntegral[a+b*x]^2/(m+1) -
    2*b/(a*(m+1))*Int[x^(m+1)*Cosh[a+b*x]*CoshIntegral[a+b*x],x] -
    b*(m+2)/(a*(m+1))*Int[x^(m+1)*CoshIntegral[a+b*x]^2,x] /;
FreeQ[{a,b},x] && ILtQ[m,-2] *)
```

- 3.  $\int u \, Sinh[a + b \, x] \, SinhIntegral[c + d \, x] \, dx$ 
  - 1:  $\int Sinh[a + b x] SinhIntegral[c + d x] dx$

Rule:

$$\int Sinh[a+b\,x] \, SinhIntegral[c+d\,x] \, \, dx \, \, \rightarrow \, \, \frac{Cosh[a+b\,x] \, SinhIntegral[c+d\,x]}{b} \, - \, \frac{d}{b} \int \frac{Cosh[a+b\,x] \, Sinh[c+d\,x]}{c+d\,x} \, \, dx$$

```
Int[Sinh[a_.+b_.*x_]*SinhIntegral[c_.+d_.*x_],x_Symbol] :=
    Cosh[a+b*x]*SinhIntegral[c+d*x]/b -
    d/b*Int[Cosh[a+b*x]*Sinh[c+d*x]/(c+d*x),x] /;
FreeQ[{a,b,c,d},x]

Int[Cosh[a_.+b_.*x_]*CoshIntegral[c_.+d_.*x_],x_Symbol] :=
    Sinh[a+b*x]*CoshIntegral[c+d*x]/b -
    d/b*Int[Sinh[a+b*x]*Cosh[c+d*x]/(c+d*x),x] /;
FreeQ[{a,b,c,d},x]
```

```
2. \int (e + fx)^m \sinh[a + bx] \sinh[ntegral[c + dx] dx
1: \int (e + fx)^m \sinh[a + bx] \sinh[ntegral[c + dx] dx \text{ when } m \in \mathbb{Z}^+
```

Rule: If  $m \in \mathbb{Z}^+$ , then

$$\int \left(e+fx\right)^m Sinh[a+b\,x] \, SinhIntegral[c+d\,x] \, dx \, \longrightarrow \\ \frac{\left(e+fx\right)^m Cosh[a+b\,x] \, SinhIntegral[c+d\,x]}{b} \, - \\ \frac{d}{b} \int \frac{\left(e+fx\right)^m Cosh[a+b\,x] \, Sinh[c+d\,x]}{c+d\,x} \, dx \, - \frac{f\,m}{b} \int \left(e+f\,x\right)^{m-1} Cosh[a+b\,x] \, SinhIntegral[c+d\,x] \, dx}{c+d\,x}$$

```
Int[(e_.+f_.*x_)^m_.*Sinh[a_.+b_.*x_]*SinhIntegral[c_.+d_.*x_],x_Symbol] :=
    (e+f*x)^m*Cosh[a+b*x]*SinhIntegral[c+d*x]/b -
    d/b*Int[(e+f*x)^m*Cosh[a+b*x]*Sinh[c+d*x]/(c+d*x),x] -
    f*m/b*Int[(e+f*x)^(m-1)*Cosh[a+b*x]*SinhIntegral[c+d*x],x] /;
FreeQ[{a,b,c,d,e,f},x] && IGtQ[m,0]

Int[(e_.+f_.*x_)^m_.*Cosh[a_.+b_.*x_]*CoshIntegral[c_.+d_.*x_],x_Symbol] :=
    (e+f*x)^m*Sinh[a+b*x]*CoshIntegral[c+d*x]/b -
    d/b*Int[(e+f*x)^m*Sinh[a+b*x]*Cosh[c+d*x]/(c+d*x),x] -
    f*m/b*Int[(e+f*x)^m*Sinh[a+b*x]*CoshIntegral[c+d*x]/;
FreeQ[{a,b,c,d,e,f},x] && IGtQ[m,0]
```

2: 
$$\int (e + f x)^m Sinh[a + b x] SinhIntegral[c + d x] dx when m + 1 \in \mathbb{Z}^-$$

## Derivation: Inverted integration by parts

Rule: If  $m + 1 \in \mathbb{Z}^-$ , then

$$\int \left(e + f \, x\right)^m Sinh[a + b \, x] \, SinhIntegral[c + d \, x] \, dx \, \rightarrow \\ \frac{\left(e + f \, x\right)^{m+1} \, Sinh[a + b \, x] \, SinhIntegral[c + d \, x]}{f \, (m+1)} \, - \\ \frac{d}{f \, (m+1)} \int \frac{\left(e + f \, x\right)^{m+1} \, Sinh[a + b \, x] \, Sinh[c + d \, x]}{c + d \, x} \, dx \, - \frac{b}{f \, (m+1)} \int \left(e + f \, x\right)^{m+1} \, Cosh[a + b \, x] \, SinhIntegral[c + d \, x] \, dx$$

```
Int[(e_.+f_.*x__)^m_*Sinh[a_.+b_.*x__]*SinhIntegral[c_.+d_.*x__],x_Symbol] :=
    (e+f*x)^(m+1)*Sinh[a+b*x]*SinhIntegral[c+d*x]/(f*(m+1)) -
    d/(f*(m+1))*Int[(e+f*x)^(m+1)*Sinh[a+b*x]*Sinh[c+d*x]/(c+d*x),x] -
    b/(f*(m+1))*Int[(e+f*x)^(m+1)*Cosh[a+b*x]*SinhIntegral[c+d*x],x] /;
FreeQ[{a,b,c,d,e,f},x] && ILtQ[m,-1]

Int[(e_.+f_.*x__)^m_.*Cosh[a_.+b_.*x__]*CoshIntegral[c_.+d_.*x__],x_Symbol] :=
    (e+f*x)^(m+1)*Cosh[a+b*x]*CoshIntegral[c+d*x]/(f*(m+1)) -
    d/(f*(m+1))*Int[(e+f*x)^(m+1)*Cosh[a+b*x]*Cosh[c+d*x]/(c+d*x),x] -
    b/(f*(m+1))*Int[(e+f*x)^(m+1)*Sinh[a+b*x]*CoshIntegral[c+d*x],x] /;
FreeQ[{a,b,c,d,e,f},x] && ILtQ[m,-1]
```

4.  $\int u \, Cosh[a + b \, x] \, SinhIntegral[c + d \, x] \, dx$ 

1:  $\int Cosh[a+bx] SinhIntegral[c+dx] dx$ 

### Derivation: Integration by parts

Rule:

$$\int\! Cosh[a+b\,x] \, SinhIntegral[c+d\,x] \, \, dx \, \rightarrow \, \frac{Sinh[a+b\,x] \, SinhIntegral[c+d\,x]}{b} - \frac{d}{b} \int\! \frac{Sinh[a+b\,x] \, Sinh[c+d\,x]}{c+d\,x} \, \, dx$$

Program code:

```
Int[Cosh[a_.+b_.*x_]*SinhIntegral[c_.+d_.*x_],x_Symbol] :=
    Sinh[a+b*x]*SinhIntegral[c+d*x]/b -
    d/b*Int[Sinh[a+b*x]*Sinh[c+d*x]/(c+d*x),x] /;
FreeQ[{a,b,c,d},x]

Int[Sinh[a_.+b_.*x_]*CoshIntegral[c_.+d_.*x_],x_Symbol] :=
    Cosh[a+b*x]*CoshIntegral[c+d*x]/b -
    d/b*Int[Cosh[a+b*x]*Cosh[c+d*x]/(c+d*x),x] /;
FreeQ[{a,b,c,d},x]
```

2. ∫(e+fx)<sup>m</sup> Cosh[a+bx] SinhIntegral[c+dx] dx
 1: ∫(e+fx)<sup>m</sup> Cosh[a+bx] SinhIntegral[c+dx] dx when m∈ Z<sup>+</sup>

#### Derivation: Integration by parts

Rule: If  $m \in \mathbb{Z}^+$ , then

$$\int (e + f x)^m Cosh[a + b x] SinhIntegral[c + d x] dx \rightarrow$$

$$\frac{\left(e+fx\right)^{m} Sinh[a+b\,x] \, SinhIntegral[c+d\,x]}{b} - \\ \frac{d}{b} \int \frac{\left(e+f\,x\right)^{m} Sinh[a+b\,x] \, Sinh[c+d\,x]}{c+d\,x} \, dx - \frac{f\,m}{b} \int \left(e+f\,x\right)^{m-1} Sinh[a+b\,x] \, SinhIntegral[c+d\,x] \, dx}{c+d\,x}$$

```
Int[(e_.+f_.*x_)^m_.*Cosh[a_.+b_.*x_]*SinhIntegral[c_.+d_.*x_],x_Symbol] :=
    (e+f*x)^m*Sinh[a+b*x]*SinhIntegral[c+d*x]/b -
    d/b*Int[(e+f*x)^m*Sinh[a+b*x]*Sinh[c+d*x]/(c+d*x),x] -
    f*m/b*Int[(e+f*x)^(m-1)*Sinh[a+b*x]*SinhIntegral[c+d*x],x]/;
FreeQ[{a,b,c,d,e,f},x] && IGtQ[m,0]

Int[(e_.+f_.*x_)^m_.*Sinh[a_.+b_.*x_]*CoshIntegral[c_.+d_.*x_],x_Symbol] :=
    (e+f*x)^m*Cosh[a+b*x]*CoshIntegral[c+d*x]/b -
    d/b*Int[(e+f*x)^m*Cosh[a+b*x]*Cosh[c+d*x]/(c+d*x),x] -
    f*m/b*Int[(e+f*x)^m*Cosh[a+b*x]*Cosh[a+b*x]*CoshIntegral[c+d*x],x]/;
FreeQ[{a,b,c,d,e,f},x] && IGtQ[m,0]
```

2: 
$$\int (e + f x)^m \cosh[a + b x] \sinh[ntegral[c + d x] dx$$
 when  $m + 1 \in \mathbb{Z}^-$ 

## Derivation: Inverted integration by parts

Rule: If  $m + 1 \in \mathbb{Z}^-$ , then

$$\int \left(e + f \, x\right)^m \mathsf{Cosh}[a + b \, x] \, \mathsf{SinhIntegral}[c + d \, x] \, dx \, \rightarrow \\ \frac{\left(e + f \, x\right)^{m+1} \, \mathsf{Cosh}[a + b \, x] \, \mathsf{SinhIntegral}[c + d \, x]}{f \, (m+1)} \, - \\ \frac{d}{f \, (m+1)} \int \frac{\left(e + f \, x\right)^{m+1} \, \mathsf{Cosh}[a + b \, x] \, \mathsf{Sinh}[c + d \, x]}{c + d \, x} \, dx \, - \frac{b}{f \, (m+1)} \int \left(e + f \, x\right)^{m+1} \, \mathsf{Sinh}[a + b \, x] \, \mathsf{SinhIntegral}[c + d \, x] \, dx$$

```
Int[(e_.+f_.*x_)^m_.*Cosh[a_.+b_.*x_]*SinhIntegral[c_.+d_.*x_],x_Symbol] :=
    (e+f*x)^(m+1)*Cosh[a+b*x]*SinhIntegral[c+d*x]/(f*(m+1)) -
    d/(f*(m+1))*Int[(e+f*x)^(m+1)*Sinh[a+b*x]*SinhIntegral[c+d*x],x] -
    b/(f*(m+1))*Int[(e+f*x)^(m+1)*Sinh[a+b*x]*SinhIntegral[c+d*x],x] /;
FreeQ[{a,b,c,d,e,f},x] && ILtQ[m,-1]

Int[(e_.+f_.*x_)^m_*Sinh[a_.+b_.*x_]*CoshIntegral[c_.+d_.*x_],x_Symbol] :=
    (e+f*x)^(m+1)*Sinh[a+b*x]*CoshIntegral[c+d*x]/(f*(m+1)) -
    d/(f*(m+1))*Int[(e+f*x)^(m+1)*Sinh[a+b*x]*Cosh[c+d*x]/(c+d*x),x] -
    b/(f*(m+1))*Int[(e+f*x)^(m+1)*Cosh[a+b*x]*CoshIntegral[c+d*x],x] /;
FreeQ[{a,b,c,d,e,f},x] && ILtQ[m,-1]
```

```
5.  \int u \, SinhIntegral [d \, (a+b \, Log[c \, x^n])] \, dx 
1:  \int SinhIntegral [d \, (a+b \, Log[c \, x^n])] \, dx 
Derivation:  Integration \, by \, parts 
 Basis: \partial_x \, SinhIntegral [d \, (a+b \, Log[c \, x^n])] = \frac{b \, d \, n \, Sinh[d \, (a+b \, Log[c \, x^n])]}{x \, (d \, (a+b \, Log[c \, x^n]))} 
 Rule: If \, m \neq -1, \, then 
 \int SinhIntegral [d \, (a+b \, Log[c \, x^n])] \, dx \, \rightarrow \, x \, SinhIntegral [d \, (a+b \, Log[c \, x^n])] - b \, dn \int \frac{Sinh[d \, (a+b \, Log[c \, x^n])]}{d \, (a+b \, Log[c \, x^n])} \, dx
```

```
Int[SinhIntegral[d_.*(a_.+b_.*Log[c_.*x_^n_.])],x_Symbol] :=
    x*SinhIntegral[d*(a+b*Log[c*x^n])] - b*d*n*Int[Sinh[d*(a+b*Log[c*x^n])]/(d*(a+b*Log[c*x^n])),x] /;
FreeQ[{a,b,c,d,n},x]

Int[CoshIntegral[d_.*(a_.+b_.*Log[c_.*x_^n_.])],x_Symbol] :=
    x*CoshIntegral[d*(a+b*Log[c*x^n])] - b*d*n*Int[Cosh[d*(a+b*Log[c*x^n])]/(d*(a+b*Log[c*x^n])),x] /;
FreeQ[{a,b,c,d,n},x]
```

2: 
$$\int \frac{SinhIntegral[d(a+bLog[cx^n])]}{x} dx$$

Derivation: Integration by substitution

Basis: 
$$\frac{F[Log[c x^n]]}{x} = \frac{1}{n} Subst[F[x], x, Log[c x^n]] \partial_x Log[c x^n]$$

Rule:

$$\int \frac{SinhIntegral\big[d\left(a+b\,Log\big[c\,x^n\big]\right)\big]}{x}\,dx\,\rightarrow\,\frac{1}{n}\,Subst\big[SinhIntegral\big[d\left(a+b\,x\right)\big],\,x,\,Log\big[c\,x^n\big]\big]$$

```
Int[F_[d_.*(a_.+b_.*Log[c_.*x_^n_.])]/x_,x_Symbol] :=
    1/n*Subst[F[d*(a+b*x)],x,Log[c*x^n]] /;
FreeQ[{a,b,c,d,n},x] && MemberQ[{SinhIntegral,CoshIntegral},x]
```

```
3: \int (e x)^m SinhIntegral[d (a + b Log[c x^n])] dx when m \neq -1
```

```
Basis: \partial_x SinhIntegral[d(a+bLog[cx^n])] = \frac{bdnSinh[d(a+bLog[cx^n])]}{x(d(a+bLog[cx^n]))}
```

Rule: If  $m \neq -1$ , then

```
\int \left(e\,x\right)^{\,m} \, SinhIntegral\left[d\,\left(a+b\,Log\left[c\,x^{n}\right]\right)\right] \, dx \,\, \rightarrow \,\, \frac{\left(e\,x\right)^{\,m+1} \, SinhIntegral\left[d\,\left(a+b\,Log\left[c\,x^{n}\right]\right)\right]}{e\,\left(m+1\right)} \, - \, \frac{b\,d\,n}{m+1} \int \frac{\left(e\,x\right)^{\,m} \, Sinh\left[d\,\left(a+b\,Log\left[c\,x^{n}\right]\right)\right]}{d\,\left(a+b\,Log\left[c\,x^{n}\right]\right)} \, dx
```

```
Int[(e_.*x_)^m_.*SinhIntegral[d_.*(a_.+b_.*Log[c_.*x_^n_.])],x_Symbol] :=
    (e*x)^(m+1)*SinhIntegral[d*(a+b*Log[c*x^n])]/(e*(m+1)) -
    b*d*n/(m+1)*Int[(e*x)^m*Sinh[d*(a+b*Log[c*x^n])]/(d*(a+b*Log[c*x^n])),x] /;
FreeQ[{a,b,c,d,e,m,n},x] && NeQ[m,-1]

Int[(e_.*x_)^m_.*CoshIntegral[d_.*(a_.+b_.*Log[c_.*x_^n_.])],x_Symbol] :=
    (e*x)^(m+1)*CoshIntegral[d*(a+b*Log[c*x^n])]/(e*(m+1)) -
    b*d*n/(m+1)*Int[(e*x)^m*Cosh[d*(a+b*Log[c*x^n])]/(d*(a+b*Log[c*x^n])),x] /;
FreeQ[{a,b,c,d,e,m,n},x] && NeQ[m,-1]
```