## Rubi 4.16.1.4 Integration Test Results

## on the problems in the test-suite directory "6 Hyperbolic functions"

Test results for the 502 problems in "6.1.1 (c+d x)^m (a+b sinh)^n.m"

Test results for the 102 problems in "6.1.3 (e x) $^m$  (a+b sinh(c+d x $^n$ )) $^p$ .m"

Test results for the 33 problems in "6.1.4 (d+e x) $^n$ m sinh(a+b x+c x $^2$ ) $^n$ n.m"

Test results for the 369 problems in "6.1.5 Hyperbolic sine functions.m"

Test results for the 525 problems in "6.1.7 hyper^m (a+b sinh^n)^p.m"

Test results for the 183 problems in "6.2.1 (c+d x)^m (a+b cosh)^n.m"

Test results for the 111 problems in "6.2.2 (e x)^m (a+b x^n)^p cosh.m"

Test results for the 68 problems in "6.2.3 (e x) $^m$  (a+b cosh(c+d x $^n$ )) $^p$ .m"

Test results for the 33 problems in "6.2.4 (d+e x) $^m$  cosh(a+b x+c x $^2$ ) $^n$ .m"

Test results for the 336 problems in "6.2.5 Hyperbolic cosine functions.m"

Test results for the 85 problems in "6.2.7 hyper^m (a+b) cosh^n)^p.m"

Test results for the 77 problems in "6.3.1 (c+d x)^m (a+b tanh)^n.m"

Test results for the 247 problems in "6.3.2 Hyperbolic tangent functions.m"

Test results for the 263 problems in "6.3.7 (d hyper)^m (a+b (c tanh)^n)^p.m"

Test results for the 61 problems in "6.4.1 (c+d x)^m (a+b coth)^n.m"

Test results for the 224 problems in "6.4.2 Hyperbolic cotangent functions.m"

Test results for the 53 problems in "6.4.7 (d hyper)^m (a+b (c coth)^n)^p.m"

Test results for the 16 problems in "6.5.1 (c+d x)^m (a+b sech)^n.m"

Test results for the 84 problems in "6.5.2 (e x)<sup>m</sup> (a+b sech(c+d x^n))^p.m"

Test results for the 201 problems in "6.5.3 Hyperbolic secant functions.m"

Problem 186: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \left( \, \left( 1 - b^2 \, n^2 \right) \, \mathsf{Sech} \left[ \, a + b \, \mathsf{Log} \left[ \, c \, \, x^n \, \right] \, \right] \, + 2 \, b^2 \, n^2 \, \mathsf{Sech} \left[ \, a + b \, \mathsf{Log} \left[ \, c \, \, x^n \, \right] \, \right]^3 \right) \, \mathrm{d} x$$

Optimal (type 3, 40 leaves, ? steps):

$$x\,\mathsf{Sech}\left[\,\mathsf{a}\,+\,\mathsf{b}\,\mathsf{Log}\left[\,\mathsf{c}\,\,\mathsf{x}^n\,\right]\,\right]\,+\,\mathsf{b}\,\,\mathsf{n}\,\,\mathsf{x}\,\,\mathsf{Sech}\left[\,\mathsf{a}\,+\,\mathsf{b}\,\mathsf{Log}\left[\,\mathsf{c}\,\,\mathsf{x}^n\,\right]\,\right]\,\,\mathsf{Tanh}\left[\,\mathsf{a}\,+\,\mathsf{b}\,\mathsf{Log}\left[\,\mathsf{c}\,\,\mathsf{x}^n\,\right]\,\right]$$

Result (type 5, 139 leaves, 9 steps):

$$2\,e^{a}\,\left(1-b\,n\right)\,x\,\left(c\,x^{n}\right)^{b}\,\text{Hypergeometric2F1}\!\left[1,\,\frac{b+\frac{1}{n}}{2\,b},\,\frac{1}{2}\left(3+\frac{1}{b\,n}\right),\,-\,e^{2\,a}\,\left(c\,x^{n}\right)^{2\,b}\right]\,+\,\frac{1}{1+3\,b\,n}$$
 
$$16\,b^{2}\,e^{3\,a}\,n^{2}\,x\,\left(c\,x^{n}\right)^{3\,b}\,\text{Hypergeometric2F1}\!\left[3,\,\frac{3\,b+\frac{1}{n}}{2\,b},\,\frac{1}{2}\left(5+\frac{1}{b\,n}\right),\,-\,e^{2\,a}\,\left(c\,x^{n}\right)^{2\,b}\right]$$

Test results for the 220 problems in "6.5.7 (d hyper)^m (a+b (c sech)^n)^p.m"

Test results for the 29 problems in "6.6.1 (c+d x)^m (a+b csch)^n.m"

Test results for the 83 problems in "6.6.2 (e x)^m (a+b csch(c+d x^n))^p.m"

Test results for the 175 problems in "6.6.3 Hyperbolic cosecant functions.m"

Problem 160: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \left( -\left(1-b^2 \ n^2\right) \ \mathsf{Csch}\left[\, a+b \ \mathsf{Log}\left[\, c \ x^n\,\right]\,\right] \ + \ 2 \ b^2 \ n^2 \ \mathsf{Csch}\left[\, a+b \ \mathsf{Log}\left[\, c \ x^n\,\right]\,\right]^{\,3}\right) \ \mathbb{d} x$$

Optimal (type 3, 42 leaves, ? steps):

$$-x\, Csch \left[\, a+b\, Log \left[\, c\, \, x^n\, \right]\, \right]\, -b\, n\, x\, Coth \left[\, a+b\, Log \left[\, c\, \, x^n\, \right]\, \right]\, Csch \left[\, a+b\, Log \left[\, c\, \, x^n\, \right]\, \right]$$

Result (type 5, 137 leaves, 9 steps):

$$2 \, e^{a} \, \left(1 - b \, n\right) \, x \, \left(c \, x^{n}\right)^{b} \, \text{Hypergeometric2F1} \left[1, \, \frac{b + \frac{1}{n}}{2 \, b}, \, \frac{1}{2} \left(3 + \frac{1}{b \, n}\right), \, e^{2 \, a} \, \left(c \, x^{n}\right)^{2 \, b}\right] - \\ \frac{1}{1 + 3 \, b \, n} 16 \, b^{2} \, e^{3 \, a} \, n^{2} \, x \, \left(c \, x^{n}\right)^{3 \, b} \, \text{Hypergeometric2F1} \left[3, \, \frac{3 \, b + \frac{1}{n}}{2 \, b}, \, \frac{1}{2} \left(5 + \frac{1}{b \, n}\right), \, e^{2 \, a} \, \left(c \, x^{n}\right)^{2 \, b}\right]$$

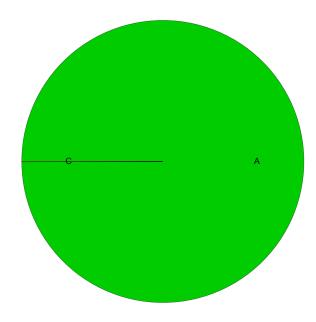
Test results for the 27 problems in "6.6.7 (d hyper)^m (a+b (c

csch)^n)^p.m"

Test results for the 1059 problems in "6.7.1 Hyperbolic functions.m"

## **Summary of Integration Test Results**

## 5166 integration problems



- A 5164 optimal antiderivatives
- B 0 valid but suboptimal antiderivatives
- C 2 unnecessarily complex antiderivatives
- D 0 unable to integrate problems
- E 0 integration timeouts
- F 0 invalid antiderivatives