# Mathematica 11.3 Integration Test Results

# Test results for the 208 problems in "8.3 Exponential integral functions.m"

### Problem 4: Unable to integrate problem.

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\int \frac{\text{ExpIntegralE}[1, b \, x]}{x} \, \mathrm{d}x Optimal (type 5, 32 leaves, 1 step): b \, x \, \text{HypergeometricPFQ}[\{1, 1, 1\}, \{2, 2, 2\}, -b \, x] - \text{EulerGamma Log}[x] - \frac{1}{2} \, \text{Log}[b \, x]^2 Result (type 8, 11 leaves):
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# $\int \frac{\mathsf{ExpIntegralE}[\mathsf{1,b\,x}]}{\mathsf{x}} \, \mathsf{dx}$

### Problem 5: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[1, b \, x]}{x^2} \, dx$$
Optimal (type 4, 20 leaves, 1 step):
$$-\frac{\text{ExpIntegralE}[1, b \, x]}{x} + \frac{\text{ExpIntegralE}[2, b \, x]}{x}$$
Result (type 8, 11 leaves):
$$\int \frac{\text{ExpIntegralE}[1, b \, x]}{x^2} \, dx$$

### Problem 6: Unable to integrate problem.

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\int \frac{\text{ExpIntegralE}[1, b \, x]}{x^3} \, dx
Optimal (type 4, 25 leaves, 1 step):
-\frac{\text{ExpIntegralE}[1, b \, x]}{2 \, x^2} + \frac{\text{ExpIntegralE}[3, b \, x]}{2 \, x^2}
Result (type 8, 11 leaves):
\int \frac{\text{ExpIntegralE}[1, b \, x]}{2} \, dx
```

### Problem 7: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[1, b x]}{x^4} dx$$
Optimal (type 4, 25 leaves, 1 step):
$$-\frac{\text{ExpIntegralE}[1, b x]}{3 x^3} + \frac{\text{ExpIntegralE}[4, b x]}{3 x^3}$$
Result (type 8, 11 leaves):

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[1, b x]}{x^4} \, dx$$

### Problem 11: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE[2,bx]}}{\mathsf{x}} \, d\mathsf{x}$$

Optimal (type 4, 13 leaves, 1 step):

Result (type 8, 11 leaves):

$$\int \frac{\mathsf{ExpIntegralE[2, bx]}}{\mathsf{x}} \, \mathsf{dx}$$

### Problem 12: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[2, bx]}}{x^2} \, dx$$

Optimal (type 5, 46 leaves, 2 steps):

$$b^2 \times \text{HypergeometricPFQ}[\{1, 1, 1\}, \{2, 2, 2\}, -b \times] + b \text{ EulerGamma Log}[x] + \frac{1}{2} b \text{ Log}[b \times]^2$$

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[2, bx]}{x^2} dx$$

### Problem 13: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[\mathsf{2,\,b\,x}\right]}{\mathsf{x}^{\mathsf{3}}}\,\mathrm{d}\mathsf{x}$$

Optimal (type 4, 20 leaves, 1 step):

$$-\frac{\mathsf{ExpIntegralE}\left[\mathtt{2,bx}\right]}{\mathsf{x}^2} + \frac{\mathsf{ExpIntegralE}\left[\mathtt{3,bx}\right]}{\mathsf{x}^2}$$

$$\int \frac{\text{ExpIntegralE}[2, b x]}{x^3} \, dx$$

### Problem 14: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[2, bx]}{x^4} dx$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\mathsf{ExpIntegralE}[2, bx]}{2x^3} + \frac{\mathsf{ExpIntegralE}[4, bx]}{2x^3}$$

Result (type 8, 11 leaves):

$$\int \frac{\mathsf{ExpIntegralE}[2, b \, x]}{x^4} \, \mathrm{d} x$$

### Problem 15: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[2, bx]}}{x^5} \, dx$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\mathsf{ExpIntegralE[2,bx]}}{3x^4} + \frac{\mathsf{ExpIntegralE[5,bx]}}{3x^4}$$

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[2,b\,x]}{x^5} \, dx$$

### Problem 19: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[3, bx]}}{x} \, dx$$

Optimal (type 4, 19 leaves, 1 step):

$$-\frac{1}{2}$$
 ExpIntegralE[1, bx] +  $\frac{1}{2}$  ExpIntegralE[3, bx]

$$\int \frac{\mathsf{ExpIntegralE}[3, b \, x]}{\mathsf{x}} \, \mathrm{d} \mathsf{x}$$

### Problem 20: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[3, bx]}}{x^2} \, dx$$

Optimal (type 4, 20 leaves, 1 step):

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE[3, bx]}}{x^2} \, dx$$

### Problem 21: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[3, bx]}}{x^3} \, dx$$

Optimal (type 5, 70 leaves, 3 steps):

$$\frac{b \, ExpIntegralE[2, b \, x]}{2 \, x} - \frac{ExpIntegralE[3, b \, x]}{2 \, x^2} +$$

$$\frac{1}{2}\,b^3\,x\,\,\text{HypergeometricPFQ}\,[\,\{\textbf{1, 1, 1}\}\,,\,\,\{\textbf{2, 2, 2}\}\,,\,\,-\,b\,x\,]\,\,-\,\,\frac{1}{2}\,b^2\,\,\text{EulerGamma}\,\,\text{Log}\,[\,x\,]\,\,-\,\,\frac{1}{4}\,b^2\,\,\text{Log}\,[\,b\,\,x\,]^{\,2}$$

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE[3, bx]}}{x^3} \, dx$$

### Problem 22: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[3,bx]}}{x^4} \, dx$$

Optimal (type 4, 20 leaves, 1 step):

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[3, bx]}{v^4} \, dx$$

### Problem 23: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[3, bx]}{x^5} dx$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\text{ExpIntegralE[3, bx]}}{2 x^4} + \frac{\text{ExpIntegralE[5, bx]}}{2 x^4}$$

$$\int \frac{\text{ExpIntegralE}[3, bx]}{x^5} dx$$

### Problem 24: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[3, bx]}{x^6} dx$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\text{ExpIntegralE}[3, bx]}{3x^5} + \frac{\text{ExpIntegralE}[6, bx]}{3x^5}$$

Result (type 8, 11 leaves):

$$\int \frac{\mathsf{ExpIntegralE}[3, b \, x]}{x^6} \, \mathrm{d} x$$

### Problem 29: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[-1, b x]}{x} \, dx$$

Optimal (type 4, 19 leaves, 1 step):

$$-\frac{1}{2}$$
 ExpIntegralE[-1, bx]  $+\frac{1}{2}$  ExpIntegralE[1, bx]

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[-1, b x]}{x} \, dx$$

### Problem 30: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}[-1,\,b\,x]}{x^2}\,\mathrm{d}x$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\mathsf{ExpIntegralE}[-1,\,\mathsf{b}\,\mathsf{x}]}{3\,\mathsf{x}} + \frac{\mathsf{ExpIntegralE}[2,\,\mathsf{b}\,\mathsf{x}]}{3\,\mathsf{x}}$$

$$\int \frac{\mathsf{ExpIntegralE}\left[-1,\,b\,x\right]}{x^2}\,\mathrm{d}x$$

### Problem 31: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[-1, b x]}{x^3} \, dx$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\mathsf{ExpIntegralE}\left[-1,\,b\,x\right]}{4\,x^2}+\frac{\mathsf{ExpIntegralE}\left[3,\,b\,x\right]}{4\,x^2}$$

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[-1, b x]}{x^3} \, dx$$

### Problem 37: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}[-2, b \, x]}{\mathsf{x}} \, \mathrm{d} \mathbf{x}$$

Optimal (type 4, 19 leaves, 1 step):

$$-\frac{1}{3} ExpIntegralE[-2, bx] + \frac{1}{3} ExpIntegralE[1, bx]$$

Result (type 8, 11 leaves):

$$\int \frac{\mathsf{ExpIntegralE}\left[-2,\,b\,x\right]}{x}\,\mathrm{d}x$$

### Problem 38: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[-2,\,b\,x\right]}{x^2}\,\mathrm{d}x$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\mathsf{ExpIntegralE}[-2,\,b\,x]}{4\,x}+\frac{\mathsf{ExpIntegralE}[2,\,b\,x]}{4\,x}$$

Result (type 8, 11 leaves):

$$\int \frac{\mathsf{ExpIntegralE}[-2, b \, x]}{x^2} \, \mathrm{d}x$$

### Problem 39: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}[-2, b \, x]}{x^3} \, \mathrm{d} x$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\mathsf{ExpIntegralE}\left[-2,\,b\,x\right]}{5\,x^2} + \frac{\mathsf{ExpIntegralE}\left[3,\,b\,x\right]}{5\,x^2}$$

$$\int \frac{\mathsf{ExpIntegralE}[-2, b \, x]}{x^3} \, \mathrm{d}x$$

### Problem 40: Result more than twice size of optimal antiderivative.

$$\int x^5 \operatorname{ExpIntegralE}[-3, b x] dx$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{1}{2} x^6 \text{ ExpIntegralE}[-5, bx] + \frac{1}{2} x^6 \text{ ExpIntegralE}[-3, bx]$$

Result (type 4, 60 leaves):

$$-\frac{1}{b^{6}}e^{-bx}\left(60+60\ b\ x+20\ b^{2}\ x^{2}+b^{5}\ e^{bx}\ x^{5}\ \text{ExpIntegralE}\left[-2\text{, }b\ x\right]+5\ b^{4}\ e^{bx}\ x^{4}\ \text{ExpIntegralE}\left[-1\text{, }b\ x\right]\right)$$

### Problem 41: Result more than twice size of optimal antiderivative.

$$\int x^4 \text{ ExpIntegralE}[-3, bx] dx$$

Optimal (type 4, 20 leaves, 1 step):

$$-x^5$$
 ExpIntegralE[-4, bx] +  $x^5$  ExpIntegralE[-3, bx]

Result (type 4, 49 leaves):

$$-\,\frac{1}{b^{5}}\left(b^{4}\,x^{4}\,\text{ExpIntegralE}\,[\,-\,2\,\text{,}\,\,b\,x\,]\,\,+\,4\,\,\mathrm{e}^{-b\,x}\,\left(6\,+\,3\,\,b\,\,x\,+\,b^{3}\,\,\mathrm{e}^{b\,x}\,x^{3}\,\,\text{ExpIntegralE}\,[\,-\,1\,\text{,}\,\,b\,\,x\,]\,\,\right)\,\right)$$

### Problem 43: Result more than twice size of optimal antiderivative.

$$\int x^2 \, ExpIntegralE[-3, bx] \, dx$$

Optimal (type 4, 20 leaves, 1 step):

$$-x^3$$
 ExpIntegralE[-3, bx] +  $x^3$  ExpIntegralE[-2, bx]

Result (type 4, 42 leaves):

$$-\frac{2 e^{-b x} + b^3 x^3 ExpIntegralE[-2, b x] + 2 b^2 x^2 ExpIntegralE[-1, b x]}{b^4 x}$$

### Problem 46: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}[-3, b \, x]}{\mathsf{x}} \, \mathrm{d} \mathsf{x}$$

Optimal (type 4, 19 leaves, 1 step):

$$-\frac{1}{4}$$
ExpIntegralE[-3, bx] +  $\frac{1}{4}$ ExpIntegralE[1, bx]

$$\int \frac{\text{ExpIntegralE}\left[-3,\,b\,x\right]}{x}\,\text{d}x$$

### Problem 47: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[-3, bx]}{x^2} dx$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\mathsf{ExpIntegralE}\left[-3,\,b\,x\right]}{5\,\mathsf{x}}+\frac{\mathsf{ExpIntegralE}\left[2,\,b\,x\right]}{5\,\mathsf{x}}$$

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[-3, b x]}{x^2} \, dx$$

### Problem 48: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[-3, bx]}{x^3} dx$$

Optimal (type 4, 25 leaves, 1 step):

$$-\frac{\text{ExpIntegralE}[-3, bx]}{6x^2} + \frac{\text{ExpIntegralE}[3, bx]}{6x^2}$$

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[-3, b x]}{x^3} \, dx$$

### Problem 53: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[\mathbf{1,\,b\,x}\right]}{\mathsf{x}}\,\mathrm{d}\mathbf{x}$$

Optimal (type 5, 32 leaves, 1 step):

b x HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, -bx] - EulerGamma Log[x] - 
$$\frac{1}{2}$$
 Log[bx]<sup>2</sup>

$$\int \frac{\text{ExpIntegralE}[1, b x]}{x} \, dx$$

### Problem 54: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[2, bx]}}{x^2} \, dx$$

Optimal (type 5, 46 leaves, 2 steps):

$$b^2$$
 x HypergeometricPFQ[{1, 1, 1}, {2, 2, 2}, -bx] + b EulerGamma Log[x] +  $\frac{1}{2}$  b Log[bx]<sup>2</sup>

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[2, b x]}{x^2} \, dx$$

### Problem 55: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[3, bx]}}{x^3} \, dx$$

Optimal (type 5, 70 leaves, 3 steps):

$$\frac{b \, ExpIntegralE[2, b \, x]}{2 \, x} - \frac{ExpIntegralE[3, b \, x]}{2 \, x^2} +$$

$$\frac{1}{2} b^{3} x \text{ HypergeometricPFQ}[\{1, 1, 1\}, \{2, 2, 2\}, -b x] - \frac{1}{2} b^{2} \text{ EulerGamma Log}[x] - \frac{1}{4} b^{2} \text{ Log}[b x]^{2}$$

Result (type 8, 11 leaves):

$$\int \frac{\mathsf{ExpIntegralE[3,bx]}}{\mathsf{x}^3} \, \mathrm{d} \mathsf{x}$$

### Problem 56: Unable to integrate problem.

$$\int (dx)^{3/2} ExpIntegralE \left[ -\frac{3}{2}, bx \right] dx$$

Optimal (type 5, 62 leaves, 1 step):

$$-\frac{4 \left(\text{d x}\right)^{5/2} \text{ HypergeometricPFQ} \left[\left\{\frac{5}{2}, \frac{5}{2}\right\}, \left\{\frac{7}{2}, \frac{7}{2}\right\}, -\text{b x}\right]}{25 \text{ d}} + \frac{3 \sqrt{\pi} \left(\text{d x}\right)^{3/2} \text{Log} \left[\text{x}\right]}{4 \text{ b} \left(\text{b x}\right)^{3/2}}$$

$$\int (dx)^{3/2} ExpIntegralE \left[ -\frac{3}{2}, bx \right] dx$$

### Problem 57: Unable to integrate problem.

$$\int \sqrt{d\,x} \, \, \mathsf{ExpIntegralE} \, \big[ \, - \, \frac{1}{2} \,, \, \, b \, x \, \big] \, \, \mathrm{d} x$$

Optimal (type 5, 62 leaves, 1 step):

$$-\frac{4\left(\mathsf{d}\,\mathsf{x}\right)^{3/2}\,\mathsf{HypergeometricPFQ}\left[\left\{\frac{3}{2},\,\frac{3}{2}\right\},\,\left\{\frac{5}{2},\,\frac{5}{2}\right\},\,-\mathsf{b}\,\mathsf{x}\right]}{9\,\mathsf{d}}+\frac{\sqrt{\pi}\,\,\sqrt{\mathsf{d}\,\mathsf{x}}\,\,\mathsf{Log}\,[\mathsf{x}]}{2\,\mathsf{b}\,\sqrt{\mathsf{b}\,\mathsf{x}}}$$

Result (type 8, 17 leaves):

$$\int \sqrt{dx} \, ExpIntegralE \left[ -\frac{1}{2}, bx \right] dx$$

### Problem 58: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[\frac{1}{2},\,\mathsf{b}\,\mathsf{x}\right]}{\sqrt{\mathsf{d}\,\mathsf{x}}}\,\mathrm{d}\mathsf{x}$$

Optimal (type 5, 57 leaves, 1 step):

$$-\frac{4\sqrt{\text{d}\,x}\ \text{HypergeometricPFQ}\big[\big\{\frac{1}{2},\,\frac{1}{2}\big\},\,\big\{\frac{3}{2},\,\frac{3}{2}\big\},\,-\text{b}\,x\big]}{\text{d}}+\frac{\sqrt{\pi}\ \sqrt{\text{b}\,x}\ \text{Log}\,[x]}{\text{b}\,\sqrt{\text{d}\,x}}$$

Result (type 8, 17 leaves):

$$\int \frac{\mathsf{ExpIntegralE}\left[\frac{1}{2},\,\mathsf{b}\,\mathsf{x}\right]}{\sqrt{\mathsf{d}\,\mathsf{x}}}\,\mathsf{d}\mathsf{x}$$

### Problem 59: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[\frac{3}{2},\,b\,x\right]}{\left(d\,x\right)^{3/2}}\,\mathrm{d}x$$

Optimal (type 5, 58 leaves, 1 step):

$$-\frac{\text{4 HypergeometricPFQ}\Big[\left\{-\frac{1}{2}\text{, }-\frac{1}{2}\right\}\text{, }\left\{\frac{1}{2}\text{, }\frac{1}{2}\right\}\text{, }-\text{b x}\Big]}{\text{d }\sqrt{\text{d x}}}-\frac{2\,\sqrt{\pi}\,\left(\text{b x}\right)^{3/2}\,\text{Log}\left[\text{x}\right]}{\text{b }\left(\text{d x}\right)^{3/2}}$$

$$\int \frac{\text{ExpIntegralE}\left[\frac{3}{2},\,b\,x\right]}{\left(d\,x\right)^{3/2}}\,\mathrm{d}x$$

### Problem 60: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[\frac{5}{2},\,b\,x\right]}{\left(d\,x\right)^{5/2}}\,\mathrm{d}x$$

Optimal (type 5, 62 leaves, 1 step):

$$-\frac{4 \text{ HypergeometricPFQ} \left[\left\{-\frac{3}{2},-\frac{3}{2}\right\},\left\{-\frac{1}{2},-\frac{1}{2}\right\},-b \times\right]}{9 \text{ d } \left(\text{d } x\right)^{3/2}}+\frac{4 \sqrt{\pi} \left(b \times\right)^{5/2} \text{ Log } [x]}{3 \text{ b } \left(\text{d } x\right)^{5/2}}$$

Result (type 8, 17 leaves):

$$\int \frac{\mathsf{ExpIntegralE}\left[\frac{5}{2},\,b\,x\right]}{\left(d\,x\right)^{5/2}}\,\mathrm{d}x$$

### Problem 61: Unable to integrate problem.

Optimal (type 4, 32 leaves, 1 step):

$$-\frac{x^{1+m} \operatorname{ExpIntegralE}[-m, x]}{m+n} + \frac{x^{1+m} \operatorname{ExpIntegralE}[n, x]}{m+n}$$

Result (type 8, 9 leaves):

$$\int x^m \, \text{ExpIntegralE}[n, x] \, dx$$

### Problem 62: Unable to integrate problem.

Optimal (type 4, 36 leaves, 1 step):

$$-\frac{x^{1+m} \; ExpIntegralE\left[-m,\; b\; x\right]}{m+n} \; + \; \frac{x^{1+m} \; ExpIntegralE\left[n,\; b\; x\right]}{m+n}$$

Result (type 8, 11 leaves):

### Problem 63: Unable to integrate problem.

$$\int (dx)^m ExpIntegralE[n, x] dx$$

Optimal (type 4, 42 leaves, 1 step):

$$-\frac{\left(\text{d}\,x\right)^{\text{1+m}}\,\text{ExpIntegralE}\left[-\text{m, x}\right]}{\text{d}\,\left(\text{m}+\text{n}\right)}\,+\,\frac{\left(\text{d}\,x\right)^{\text{1+m}}\,\text{ExpIntegralE}\left[\text{n, x}\right]}{\text{d}\,\left(\text{m}+\text{n}\right)}$$

$$(dx)^m$$
 ExpIntegralE[n, x]  $dx$ 

### Problem 64: Unable to integrate problem.

$$\int (dx)^m ExpIntegralE[n, bx] dx$$

#### Optimal (type 4, 46 leaves, 1 step):

$$-\frac{\left(\text{d}\,x\right)^{\text{1+m}}\,\text{ExpIntegralE}\left[-\text{m, b}\,x\right]}{\text{d}\,\left(\text{m}+\text{n}\right)}+\frac{\left(\text{d}\,x\right)^{\text{1+m}}\,\text{ExpIntegralE}\left[\text{n, b}\,x\right]}{\text{d}\,\left(\text{m}+\text{n}\right)}$$

#### Result (type 8, 13 leaves):

$$\left( (dx)^{m} ExpIntegralE[n, bx] dx \right)$$

### Problem 65: Unable to integrate problem.

$$\int x^{-n} ExpIntegralE[n, x] dx$$

#### Optimal (type 5, 52 leaves, 1 step):

$$-\frac{x^{1-n} \; Hypergeometric PFQ \left[\; \left\{1-n,\; 1-n\right\},\; \left\{2-n,\; 2-n\right\},\; -x \; \right]}{\left(1-n\right)^{\; 2}} \; + \; \mathsf{Gamma} \left[1-n\right] \; \mathsf{Log} \left[x\right]$$

#### Result (type 8, 11 leaves):

$$x^{-n}$$
 ExpIntegralE[n, x] dx

### Problem 66: Unable to integrate problem.

$$\int x^{-n} ExpIntegralE[n, bx] dx$$

#### Optimal (type 5, 66 leaves, 1 step):

$$-\frac{x^{1-n} \; \text{HypergeometricPFQ[} \; \{1-n,\; 1-n\} \;, \; \{2-n,\; 2-n\} \;, \; -b \; x]}{\left(1-n\right)^2} \; + \; \frac{x^{-n} \; \left(b \; x\right)^n \; \text{Gamma} \; [1-n] \; \; \text{Log} \left[x\right]}{b}$$

$$\int x^{-n} \, ExpIntegralE[n, bx] \, dx$$

### Problem 67: Unable to integrate problem.

$$\int (dx)^{-n} ExpIntegralE[n, x] dx$$

Optimal (type 5, 67 leaves, 1 step):

$$-\frac{\left(\text{d x}\right)^{\text{1-n }} \text{ HypergeometricPFQ[}\left\{\text{1-n,1-n}\right\}, \; \left\{\text{2-n,2-n}\right\}, \; -\text{x}\right]}{\text{d } \left(\text{1-n}\right)^{2}} + \text{x}^{n} \; \left(\text{d x}\right)^{-n} \text{ Gamma}\left[\text{1-n}\right] \; \text{Log}\left[\text{x}\right]$$

Result (type 8, 13 leaves):

$$\int (dx)^{-n} ExpIntegralE[n, x] dx$$

### Problem 68: Unable to integrate problem.

$$\int (dx)^{-n} ExpIntegralE[n, bx] dx$$

Optimal (type 5, 73 leaves, 1 step):

$$-\frac{\left(d\,x\right)^{\,1-n}\,HypergeometricPFQ[\,\{1-n,\,1-n\}\,,\,\{2-n,\,2-n\}\,,\,-b\,x\,]}{d\,\left(1-n\right)^{\,2}} + \\ \frac{\left(b\,x\right)^{\,n}\,\left(d\,x\right)^{\,-n}\,Gamma\,[\,1-n\,]\,\,Log\,[\,x\,]}{b}$$

Result (type 8, 15 leaves):

$$\int (dx)^{-n} ExpIntegralE[n, bx] dx$$

### Problem 72: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[n, bx]}}{x} \, dx$$

Optimal (type 4, 28 leaves, 1 step):

$$\frac{\mathsf{ExpIntegralE}[1, b x]}{1-n} - \frac{\mathsf{ExpIntegralE}[n, b x]}{1-n}$$

Result (type 8, 11 leaves):

$$\int \frac{\mathsf{ExpIntegralE}[\mathsf{n,bx}]}{\mathsf{x}} \, d\mathsf{x}$$

### Problem 73: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[n, bx]}}{x^2} \, \text{d}x$$

Optimal (type 4, 34 leaves, 1 step):

$$\frac{\texttt{ExpIntegralE[2,bx]}}{\left(2-n\right)\,x} - \frac{\texttt{ExpIntegralE[n,bx]}}{\left(2-n\right)\,x}$$

$$\int \frac{\text{ExpIntegralE[n,bx]}}{x^2} \, \mathrm{d}x$$

### Problem 74: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[n, b x]}{x^3} \, dx$$

Optimal (type 4, 34 leaves, 1 step):

$$\frac{\texttt{ExpIntegralE[3, bx]}}{(3-n) \ x^2} - \frac{\texttt{ExpIntegralE[n, bx]}}{(3-n) \ x^2}$$

Result (type 8, 11 leaves):

$$\int \frac{\text{ExpIntegralE}[n,b\,x]}{x^3}\,\text{d}x$$

### Problem 80: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}[1, a + b x]}{(c + d x)^2} \, dx$$

Optimal (type 4, 84 leaves, 5 steps):

$$-\frac{\text{ExpIntegralE[1, a+bx]}}{\text{d}\left(\text{c+dx}\right)} - \frac{\text{b}\left(\text{ExpIntegralEi}\left[-\text{a-bx}\right]\right)}{\text{d}\left(\text{bc-ad}\right)} + \frac{\text{b}\left(\text{e}^{-\text{a}+\frac{\text{bc}}{d}}\right)}{\text{ExpIntegralEi}\left[-\frac{\text{b}\left(\text{c+dx}\right)}{d}\right]} + \frac{\text{b}\left(\text{b}\left(\text{c-ad}\right)\right)}{\text{d}\left(\text{bc-ad}\right)} + \frac{\text{b}\left(\text{c-a}+\frac{\text{bc}}{d}\right)}{\text{c}\left(\text{bc-ad}\right)} + \frac{\text{c}\left(\text{c-a}+\frac{\text{bc}}{d}\right)}{\text{c}\left(\text{c-ad}\right)} + \frac{\text{c}\left(\text{c-a}+\frac{\text{bc}}{d}\right)}{\text{c}\left(\text{c-ad}\right)} + \frac{\text{c}\left(\text{c-a}+\frac{\text{bc}}{d}\right)}{\text{c}\left(\text{c-ad}\right)} + \frac{\text{c}\left(\text{c-ad}\right)}{\text{c}\left(\text{c-ad}\right)} + \frac{\text{c}\left(\text{c-ad$$

Result (type 8, 17 leaves):

$$\int \frac{\mathsf{ExpIntegralE}\left[\mathbf{1},\,\mathsf{a}+\mathsf{b}\,\mathsf{x}\right]}{\left(\mathsf{c}+\mathsf{d}\,\mathsf{x}\right)^2}\,\,\mathrm{d}\mathsf{x}$$

### Problem 81: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[1, a+bx]}{(c+dx)^3} dx$$

Optimal (type 4, 174 leaves, 7 steps):

$$-\frac{b \, e^{-a-b \, x}}{2 \, d \, \left(b \, c - a \, d\right) \, \left(c + d \, x\right)} - \frac{\text{ExpIntegralE}\left[1, \, a + b \, x\right]}{2 \, d \, \left(c + d \, x\right)^2} - \frac{b^2 \, \text{ExpIntegralEi}\left[-a - b \, x\right]}{2 \, d \, \left(b \, c - a \, d\right)^2} + \frac{b^2 \, e^{-a + \frac{b \, c}{d}} \, \text{ExpIntegralEi}\left[-\frac{b \, \left(c + d \, x\right)}{d}\right]}{2 \, d \, \left(b \, c - a \, d\right)^2} - \frac{b^2 \, e^{-a + \frac{b \, c}{d}} \, \text{ExpIntegralEi}\left[-\frac{b \, \left(c + d \, x\right)}{d}\right]}{2 \, d^2 \, \left(b \, c - a \, d\right)}$$

$$\int \frac{\text{ExpIntegralE}[1, a + b x]}{(c + d x)^3} dx$$

### Problem 82: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[1, a+bx]}{(c+dx)^4} dx$$

Optimal (type 4, 292 leaves, 10 steps):

$$-\frac{b \, \mathrm{e}^{-a-b \, x}}{6 \, d \, \left( b \, c - a \, d \right) \, \left( c + d \, x \right)^2} - \frac{b^2 \, \mathrm{e}^{-a-b \, x}}{3 \, d \, \left( b \, c - a \, d \right)^2 \, \left( c + d \, x \right)} + \frac{b^2 \, \mathrm{e}^{-a-b \, x}}{6 \, d^2 \, \left( b \, c - a \, d \right) \, \left( c + d \, x \right)} - \frac{3 \, d \, \left( b \, c - a \, d \right)^2 \, \left( c + d \, x \right)}{3 \, d \, \left( b \, c - a \, d \right)^3} + \frac{b^3 \, \mathrm{e}^{-a + \frac{b \, c}{d}} \, \mathrm{ExpIntegralEi} \left[ -\frac{b \, \left( c + d \, x \right)}{d} \right]}{3 \, d \, \left( b \, c - a \, d \right)^3} - \frac{b^3 \, \mathrm{e}^{-a + \frac{b \, c}{d}} \, \mathrm{ExpIntegralEi} \left[ -\frac{b \, \left( c + d \, x \right)}{d} \right]}{3 \, d \, \left( b \, c - a \, d \right)^3} - \frac{b^3 \, \mathrm{e}^{-a + \frac{b \, c}{d}} \, \mathrm{ExpIntegralEi} \left[ -\frac{b \, \left( c + d \, x \right)}{d} \right]}{6 \, d^3 \, \left( b \, c - a \, d \right)}$$

#### Result (type 8, 17 leaves):

$$\int \frac{\mathsf{ExpIntegralE}\left[\mathbf{1,\,a+b\,x}\right]}{\left(c+d\,x\right)^4}\,\mathrm{d}x$$

### Problem 89: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[2, a+bx]}{(c+dx)^3} dx$$

#### Optimal (type 4, 117 leaves, 6 steps):

$$\begin{split} &\frac{b \: \text{ExpIntegralE}\left[1\text{, a} + b \: x\right]}{2 \: d^2 \: \left(\text{c} + d \: x\right)} - \frac{\text{ExpIntegralE}\left[2\text{, a} + b \: x\right]}{2 \: d \: \left(\text{c} + d \: x\right)^2} + \\ &\frac{b^2 \: \text{ExpIntegralEi}\left[-\text{a} - b \: x\right]}{2 \: d^2 \: \left(\text{b} \: \text{c} - \text{a} \: d\right)} - \frac{b^2 \: \text{e}^{-\text{a} + \frac{\text{b} \: c}{d}} \: \text{ExpIntegralEi}\left[-\frac{\text{b} \: (\text{c} + d \: x)}{d}\right]}{2 \: d^2 \: \left(\text{b} \: \text{c} - \text{a} \: d\right)} \end{split}$$

#### Result (type 8, 17 leaves):

$$\int \frac{\text{ExpIntegralE}[2, a+bx]}{(c+dx)^3} dx$$

### Problem 90: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[2, a+bx]}{(c+dx)^4} dx$$

#### Optimal (type 4, 198 leaves, 8 steps):

$$\begin{split} &\frac{b^2 \, \mathrm{e}^{-a-b \, x}}{6 \, d^2 \, \left( b \, c - a \, d \right) \, \left( c + d \, x \right)} \, + \, \frac{b \, ExpIntegralE \left[ 1, \, a + b \, x \right]}{6 \, d^2 \, \left( c + d \, x \right)^2} \, - \\ &\frac{ExpIntegralE \left[ 2, \, a + b \, x \right]}{3 \, d \, \left( c + d \, x \right)^3} \, + \, \frac{b^3 \, ExpIntegralEi \left[ -a - b \, x \right]}{6 \, d^2 \, \left( b \, c - a \, d \right)^2} \, - \\ &\frac{b^3 \, \mathrm{e}^{-a + \frac{b \, c}{d}} \, ExpIntegralEi \left[ -\frac{b \, \left( c + d \, x \right)}{d} \right]}{6 \, d^2 \, \left( b \, c - a \, d \right)^2} \, + \, \frac{b^3 \, \mathrm{e}^{-a + \frac{b \, c}{d}} \, ExpIntegralEi \left[ -\frac{b \, \left( c + d \, x \right)}{d} \right]}{6 \, d^3 \, \left( b \, c - a \, d \right)} \end{split}$$

#### Result (type 8, 17 leaves):

$$\int \frac{\mathsf{ExpIntegralE}\left[\mathsf{2,a+b\,x}\right]}{\left(\mathsf{c}+\mathsf{d\,x}\right)^4}\,\mathrm{d}\mathsf{x}$$

### Problem 98: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE[3, a+bx]}}{(c+dx)^4} dx$$

#### Optimal (type 4, 141 leaves, 7 steps):

$$- \, \frac{ \, b^2 \, \text{ExpIntegralE} \, [\, \textbf{1, a + b x} \,] }{ \, 6 \, \, d^3 \, \, \left( \, c \, + \, d \, \, x \, \right) } \, \, + \, \, \frac{ \, b \, \, \text{ExpIntegralE} \, [\, \textbf{2, a + b x} \,] }{ \, 6 \, \, d^2 \, \, \left( \, c \, + \, d \, \, x \, \right)^{\, 2} } \, \, - \, \,$$

$$\frac{\text{ExpIntegralE[3, a+bx]}}{\text{3 d } \left(\text{c}+\text{d}\,\text{x}\right)^3} - \frac{\text{b}^3\,\text{ExpIntegralEi[-a-b\,x]}}{6\,\text{d}^3\,\left(\text{b c-a d}\right)} + \frac{\text{b}^3\,\,\text{e}^{-\text{a}+\frac{\text{b c}}{\text{d}}}\,\text{ExpIntegralEi}\left[-\frac{\text{b }\left(\text{c}+\text{d}\,\text{x}\right)}{\text{d}}\right]}{6\,\text{d}^3\,\left(\text{b c-a d}\right)}$$

#### Result (type 8, 17 leaves):

$$\int \frac{\text{ExpIntegralE[3, a+bx]}}{(c+dx)^4} dx$$

### Problem 104: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[-1,\,\mathsf{a}+\mathsf{b}\,\mathsf{x}\right]}{\mathsf{c}+\mathsf{d}\,\mathsf{x}}\,\mathrm{d}\mathsf{x}$$

#### Optimal (type 4, 157 leaves, 7 steps):

$$-\frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right) \, \left(c + d \, x\right)} - \frac{e^{-a-b \, x}}{b \, \left(a + b \, x\right) \, \left(c + d \, x\right)} - \frac{d \, ExpIntegralEi \left[-a - b \, x\right]}{\left(b \, c - a \, d\right)^2} + \\ \frac{d \, e^{-a + \frac{b \, c}{d}} \, ExpIntegralEi \left[-\frac{b \, \left(c + d \, x\right)}{d}\right]}{\left(b \, c - a \, d\right)^2} - \frac{e^{-a + \frac{b \, c}{d}} \, ExpIntegralEi \left[-\frac{b \, \left(c + d \, x\right)}{d}\right]}{b \, c - a \, d}$$

$$\int \frac{\mathsf{ExpIntegralE}[-1, a+bx]}{c+dx} \, dx$$

### Problem 105: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[-1,\,\mathsf{a}+\mathsf{b}\,\mathsf{x}\right]}{\left(\mathsf{c}+\mathsf{d}\,\mathsf{x}\right)^2}\,\mathsf{d}\mathsf{x}$$

Optimal (type 4, 258 leaves, 10 steps):

$$-\frac{d\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)\,\left(c+d\,x\right)^{\,2}}-\frac{e^{-a-b\,x}}{b\,\left(a+b\,x\right)\,\left(c+d\,x\right)^{\,2}}-\frac{2\,d\,e^{-a-b\,x}}{\left(b\,c-a\,d\right)^{\,2}\,\left(c+d\,x\right)}+\\ \\ \frac{e^{-a-b\,x}}{\left(b\,c-a\,d\right)\,\left(c+d\,x\right)}-\frac{2\,b\,d\,\text{ExpIntegralEi}\left[-a-b\,x\right]}{\left(b\,c-a\,d\right)^{\,3}}+\frac{2\,b\,d\,e^{-a+\frac{b\,c}{d}}\,\text{ExpIntegralEi}\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{\left(b\,c-a\,d\right)^{\,3}}-\\ \frac{2\,b\,e^{-a+\frac{b\,c}{d}}\,\text{ExpIntegralEi}\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{\left(b\,c-a\,d\right)^{\,2}}+\frac{b\,e^{-a+\frac{b\,c}{d}}\,\text{ExpIntegralEi}\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{d\,\left(b\,c-a\,d\right)}$$

#### Result (type 8, 17 leaves):

$$\int \frac{\mathsf{ExpIntegralE}\left[-1,\,\mathsf{a}+\mathsf{b}\,\mathsf{x}\right]}{\left(\mathsf{c}+\mathsf{d}\,\mathsf{x}\right)^2}\,\mathsf{d}\mathsf{x}$$

### Problem 106: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[-1,\,\mathsf{a}+\mathsf{b}\,\mathsf{x}\right]}{\left(\mathsf{c}+\mathsf{d}\,\mathsf{x}\right)^3}\,\,\mathsf{d}\,\mathsf{x}$$

Optimal (type 4, 416 leaves, 14 steps):

$$\int \frac{\text{ExpIntegralE}[-1, a+bx]}{(c+dx)^3} dx$$

#### Problem 112: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}[-2, a+b x]}{c+d x} \, dx$$

Optimal (type 4, 287 leaves, 11 steps):

$$\frac{d^2 \, \mathrm{e}^{-a-b\,x}}{b^2 \, \left( b \, c - a \, d \right) \, \left( c + d \, x \right)^2} + \frac{d \, \mathrm{e}^{-a-b\,x}}{b^2 \, \left( a + b \, x \right) \, \left( c + d \, x \right)^2} + \frac{2 \, d^2 \, \mathrm{e}^{-a-b\,x}}{b \, \left( b \, c - a \, d \right)^2 \, \left( c + d \, x \right)} - \frac{d \, \mathrm{e}^{-a-b\,x}}{b \, \left( b \, c - a \, d \right) \, \left( c + d \, x \right)} - \frac{d \, \mathrm{e}^{-a-b\,x}}{b \, \left( b \, c - a \, d \right) \, \left( c + d \, x \right)} - \frac{ExpIntegralE \left[ -1, \, a + b \, x \right]}{b \, \left( c + d \, x \right)} + \frac{2 \, d^2 \, ExpIntegralEi \left[ -a - b \, x \right]}{\left( b \, c - a \, d \right)^3} - \frac{2 \, d^2 \, \mathrm{e}^{-a + \frac{b \, c}{d}} \, ExpIntegralEi \left[ -\frac{b \, \left( c + d \, x \right)}{d} \right]}{\left( b \, c - a \, d \right)^3} + \frac{2 \, d \, \mathrm{e}^{-a + \frac{b \, c}{d}} \, ExpIntegralEi \left[ -\frac{b \, \left( c + d \, x \right)}{d} \right]}{\left( b \, c - a \, d \right)^2} - \frac{e^{-a + \frac{b \, c}{d}} \, ExpIntegralEi \left[ -\frac{b \, \left( c + d \, x \right)}{d} \right]}{b \, c - a \, d}$$

Result (type 8, 17 leaves):

$$\int \frac{\text{ExpIntegralE}[-2, a+bx]}{c+dx} dx$$

### Problem 113: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[-2,\,\mathsf{a}+\mathsf{b}\,\mathsf{x}\right]}{\left(\mathsf{c}+\mathsf{d}\,\mathsf{x}\right)^2}\,\mathsf{d}\mathsf{x}$$

Optimal (type 4, 422 leaves, 15 steps):

$$\frac{2\,d^{2}\,e^{-a-b\,x}}{b^{2}\,\left(b\,c-a\,d\right)\,\left(c+d\,x\right)^{3}} + \frac{2\,d\,e^{-a-b\,x}}{b^{2}\,\left(a+b\,x\right)\,\left(c+d\,x\right)^{3}} + \frac{3\,d^{2}\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)^{2}\,\left(c+d\,x\right)^{2}} - \frac{d\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)\,\left(c+d\,x\right)^{2}} + \frac{6\,d^{2}\,e^{-a-b\,x}}{\left(b\,c-a\,d\right)^{3}\,\left(c+d\,x\right)} - \frac{3\,d\,e^{-a-b\,x}}{\left(b\,c-a\,d\right)^{2}\,\left(c+d\,x\right)} + \frac{6\,b\,d^{2}\,e^{-a-b\,x}}{\left(b\,c-a\,d\right)^{3}\,\left(c+d\,x\right)} - \frac{ExpIntegralE\left[-1,\,a+b\,x\right]}{b\,\left(c+d\,x\right)^{2}} + \frac{6\,b\,d^{2}\,ExpIntegralEi\left[-a-b\,x\right]}{\left(b\,c-a\,d\right)^{4}} - \frac{6\,b\,d^{2}\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,(c+d\,x)}{d}\right]}{\left(b\,c-a\,d\right)^{4}} + \frac{6\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,(c+d\,x)}{d}\right]}{\left(b\,c-a\,d\right)^{3}} - \frac{3\,b\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,(c+d\,x)}{d}\right]}{\left(b\,c-a\,d\right)^{2}} + \frac{b\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,(c+d\,x)}{d}\right]}{d\,\left(b\,c-a\,d\right)} - \frac{1}{2} + \frac{1}{$$

$$\int \frac{\text{ExpIntegralE}[-2, a+bx]}{(c+dx)^2} dx$$

### Problem 114: Unable to integrate problem.

$$\int \frac{\mathsf{ExpIntegralE}\left[-2,\,\mathsf{a}+\mathsf{b}\,\mathsf{x}\right]}{\left(\mathsf{c}+\mathsf{d}\,\mathsf{x}\right)^3}\,\mathsf{d}\mathsf{x}$$

Optimal (type 4, 609 leaves, 20 steps):

$$\frac{3\,d^{2}\,e^{-a-b\,x}}{b^{2}\,\left(b\,c-a\,d\right)\,\left(c+d\,x\right)^{4}} + \frac{3\,d\,e^{-a-b\,x}}{b^{2}\,\left(a+b\,x\right)\,\left(c+d\,x\right)^{4}} + \frac{4\,d^{2}\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)^{2}\,\left(c+d\,x\right)^{3}} - \frac{d\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)\,\left(c+d\,x\right)^{3}} + \frac{6\,d^{2}\,e^{-a-b\,x}}{\left(b\,c-a\,d\right)^{3}\,\left(c+d\,x\right)^{2}} - \frac{2\,d\,e^{-a-b\,x}}{\left(b\,c-a\,d\right)^{2}\,\left(c+d\,x\right)^{2}} + \frac{e^{-a-b\,x}}{2\,\left(b\,c-a\,d\right)\,\left(c+d\,x\right)^{2}} + \frac{12\,b\,d^{2}\,e^{-a-b\,x}}{\left(b\,c-a\,d\right)^{4}\,\left(c+d\,x\right)} - \frac{6\,b\,d\,e^{-a-b\,x}}{\left(b\,c-a\,d\right)^{3}\,\left(c+d\,x\right)} + \frac{2\,b\,e^{-a-b\,x}}{\left(b\,c-a\,d\right)^{2}\,\left(c+d\,x\right)} - \frac{b\,e^{-a-b\,x}}{2\,d\,\left(b\,c-a\,d\right)\,\left(c+d\,x\right)} - \frac{ExpIntegralE\,[-1,\,a+b\,x]}{b\,\left(c+d\,x\right)^{3}} + \frac{12\,b^{2}\,d^{2}\,e^{-a-b\,x}}{b\,\left(c+d\,x\right)^{3}} + \frac{12\,b^{2}\,d^{2}\,e^{-a-b\,x}}{b\,\left(c+d\,x\right)^{3}} + \frac{12\,b^{2}\,d^{2}\,e^{-a-b\,x}}{b\,\left(c+d\,x\right)^{3}} + \frac{12\,b^{2}\,d^{2}\,e^{-a-b\,x}}{b\,\left(c+d\,x\right)^{3}} + \frac{12\,b^{2}\,d^{2}\,e^{-a-b\,x}}{b\,\left(c-a\,d\right)^{5}} + \frac{12\,b^{2}\,d^{2}\,e^{-a-b\,x}}{b\,\left(c-a\,d\right)^{5}} + \frac{12\,b^{2}\,d^{2}\,e^{-a-b\,x}}{b\,\left(c+d\,x\right)^{3}} + \frac{12\,b^{2}\,d^{2}\,e^{-a-b\,x}}{b\,\left(c-a\,d\right)^{5}} +$$

#### Result (type 8, 17 leaves):

$$\int \frac{\text{ExpIntegralE}[-2, a+bx]}{(c+dx)^3} dx$$

### Problem 120: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[-3, a+bx]}{c+dx} dx$$

Optimal (type 4, 453 leaves, 16 steps):

$$\frac{2 \, d^{3} \, e^{-a-b \, x}}{b^{3} \, \left(b \, c - a \, d\right) \, \left(c + d \, x\right)^{3}} = \frac{2 \, d^{2} \, e^{-a-b \, x}}{b^{3} \, \left(a + b \, x\right) \, \left(c + d \, x\right)^{3}} = \frac{3 \, d^{3} \, e^{-a-b \, x}}{b^{2} \, \left(b \, c - a \, d\right)^{2} \, \left(c + d \, x\right)^{2}} + \frac{d \, e^{-a-b \, x}}{b^{3} \, \left(a + b \, x\right) \, \left(c + d \, x\right)^{3}} = \frac{6 \, d^{3} \, e^{-a-b \, x}}{b^{2} \, \left(b \, c - a \, d\right)^{2} \, \left(c + d \, x\right)^{2}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{3} \, \left(c + d \, x\right)} + \frac{3 \, d^{2} \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{2} \, \left(c + d \, x\right)} = \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{2} \, \left(c + d \, x\right)} - \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{2} \, \left(c + d \, x\right)} + \frac{d \, e^{-a-b \, x}}{b \, \left(c + d \, x\right)^{2}} + \frac{d \, e^{-a-b \, x}}{b \, \left(c + d \, x\right)^{2}} - \frac{d \, e^{-a-b \, x}}{b^{2} \, \left(c + d \, x\right)} - \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b^{2} \, \left(c + d \, x\right)^{2}} - \frac{d \, e^{-a+\frac{b \, c}{d}} \, e^{-a+\frac{b \, c}{d}} \, e^{-a+\frac{b \, c}{d}} \, e^{-a+\frac{b \, c}{d}} \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{4}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{3}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{3}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{3}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{3}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{3}} + \frac{d \, e^{-a-b \, x}}{b \, \left(b \, c - a \, d\right)^{3}} + \frac{d$$

$$\int \frac{\text{ExpIntegralE}[-3, a+bx]}{c+dx} dx$$

### Problem 121: Unable to integrate problem.

$$\int \frac{\text{ExpIntegralE}[-3, a+bx]}{(c+dx)^2} dx$$

#### Optimal (type 4, 621 leaves, 21 steps):

$$\frac{6\,d^3\,e^{-a-b\,x}}{b^3\,\left(b\,c-a\,d\right)\,\left(c+d\,x\right)^4} = \frac{6\,d^2\,e^{-a-b\,x}}{b^3\,\left(a+b\,x\right)\,\left(c+d\,x\right)^4} = \frac{8\,d^3\,e^{-a-b\,x}}{b^2\,\left(b\,c-a\,d\right)^2\,\left(c+d\,x\right)^3} + \frac{2\,d^2\,e^{-a-b\,x}}{b^2\,\left(b\,c-a\,d\right)\,\left(c+d\,x\right)^3} = \frac{12\,d^3\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)^3\,\left(c+d\,x\right)^2} + \frac{4\,d^2\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)^2\,\left(c+d\,x\right)^2} = \frac{24\,d^3\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)^3\,\left(c+d\,x\right)^2} + \frac{12\,d^2\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)^2\,\left(c+d\,x\right)^2} = \frac{4\,d\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)^3\,\left(c+d\,x\right)} + \frac{12\,d^2\,e^{-a-b\,x}}{b\,\left(b\,c-a\,d\right)^3\,\left(c+d\,x\right)} = \frac{4\,d\,e^{-a-b\,x}}{b\,\left(c-a\,d\right)^2\,\left(c+d\,x\right)} + \frac{2\,d\,ExpIntegralE\left[-1,\,a+b\,x\right]}{b^2\,\left(c+d\,x\right)^3} = \frac{24\,b\,d^3\,ExpIntegralEi\left[-a-b\,x\right]}{b\,\left(c+d\,x\right)^2} + \frac{24\,b\,d^3\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b^2\,\left(c-a\,d\right)^3} = \frac{24\,b\,d^3\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\right)^5} = \frac{24\,b\,d^3\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\right)^5} + \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\right)^3} = \frac{4\,b\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\right)^3} + \frac{b\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\right)^3} = \frac{4\,b\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\right)^3} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,c-a\,d\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,d\,d\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,d\,d\,d\,d\,d} = \frac{12\,b\,d\,e^{-a+\frac{b\,c}{d}}\,ExpIntegralEi\left[-\frac{b\,\left(c+d\,x\right)}{d}\right]}{b\,d\,d\,d\,d\,d\,d\,d\,d\,d\,d$$

$$\int \frac{\mathsf{ExpIntegralE}\left[-3,\, \mathsf{a} + \mathsf{b}\, \mathsf{x}\right]}{\left(\mathsf{c} + \mathsf{d}\, \mathsf{x}\right)^2} \, \mathsf{d} \mathsf{x}$$

### Problem 182: Unable to integrate problem.

$$\int \frac{\mathrm{e}^{b\,x}\,\mathsf{ExpIntegralEi}\,[\,b\,x\,]}{x^3}\,\mathrm{d}x$$

#### Optimal (type 4, 82 leaves, 10 steps):

$$-\frac{e^{2\,b\,x}}{4\,x^2} - \frac{b\,e^{2\,b\,x}}{x} - \frac{e^{b\,x}\,\text{ExpIntegralEi}\,[\,b\,x\,]}{2\,x^2} - \frac{b\,e^{b\,x}\,\text{ExpIntegralEi}\,[\,b\,x\,]}{2\,x} + \frac{1}{4}\,b^2\,\text{ExpIntegralEi}\,[\,b\,x\,]^2 + 2\,b^2\,\text{ExpIntegralEi}\,[\,2\,b\,x\,]$$

#### Result (type 8, 15 leaves):

$$\int \frac{e^{b \, x} \, \mathsf{ExpIntegralEi} [\, b \, x\,]}{x^3} \, \mathrm{d} x$$

### Problem 183: Unable to integrate problem.

$$\int \frac{e^{b \, x} \, \mathsf{ExpIntegralEi} \, [b \, x]}{x^2} \, \mathrm{d} x$$

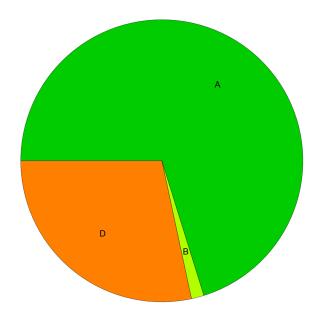
#### Optimal (type 4, 45 leaves, 5 steps):

$$-\frac{\mathrm{e}^{2\,b\,x}}{x}-\frac{\mathrm{e}^{b\,x}\,\mathsf{ExpIntegralEi}\,[\,b\,x\,]}{x}+\frac{1}{2}\,b\,\,\mathsf{ExpIntegralEi}\,[\,b\,x\,]^{\,2}+2\,b\,\,\mathsf{ExpIntegralEi}\,[\,2\,b\,x\,]$$

$$\int \frac{\mathrm{e}^{b\,x}\,\mathsf{ExpIntegralEi}\,[\,b\,x\,]}{x^2}\,\mathrm{d}x$$

## **Summary of Integration Test Results**

### 208 integration problems



- A 146 optimal antiderivatives
- B 3 more than twice size of optimal antiderivatives
- C 0 unnecessarily complex antiderivatives
- D 59 unable to integrate problems
- E 0 integration timeouts