- 1. $\int (c + dx)^m \operatorname{Hyper}[a + bx]^n \operatorname{Hyper}[a + bx]^p dx$
 - 1. $\int (c + dx)^m \sinh[a + bx]^n \cosh[a + bx]^p dx$
 - 1: $\int (c + dx)^m \sinh[a + bx]^n \cosh[a + bx] dx \text{ when } m \in \mathbb{Z}^+ \bigwedge n \neq -1$
 - **Derivation: Integration by parts**
 - Basis: $Sinh[a+bx]^n Cosh[a+bx] = \partial_x \frac{Sinh[a+bx]^{n+1}}{b(n+1)}$
 - Rule: If $m \in \mathbb{Z}^+ \land n \neq -1$, then

$$\int (c+d\,x)^m\, \text{Sinh}[a+b\,x]^n\, \text{Cosh}[a+b\,x]\,\,dx \,\, \longrightarrow \,\, \frac{\left(c+d\,x\right)^m\, \text{Sinh}[a+b\,x]^{n+1}}{b\,\,(n+1)} \, - \, \frac{d\,m}{b\,\,(n+1)} \,\, \int (c+d\,x)^{m-1}\, \text{Sinh}[a+b\,x]^{n+1}\,\,dx$$

- Program code:

2:
$$\int (c + dx)^m \sinh[a + bx]^n \cosh[a + bx]^p dx \text{ when } n \in \mathbb{Z}^+ \bigwedge p \in \mathbb{Z}^+$$

- **Derivation:** Algebraic expansion
- Rule: If $n \in \mathbb{Z}^+ \land p \in \mathbb{Z}^+$, then

$$\int (c+d\,x)^m\,Sinh[a+b\,x]^n\,Cosh[a+b\,x]^p\,dx\,\,\rightarrow\,\,\int (c+d\,x)^m\,TrigReduce[Sinh[a+b\,x]^n\,Cosh[a+b\,x]^p]\,dx$$

```
Int[(c_.+d_.*x_)^m_.*Sinh[a_.+b_.*x_]^n_.*Cosh[a_.+b_.*x_]^p_.,x_Symbol] :=
   Int[ExpandTrigReduce[(c+d*x)^m,Sinh[a+b*x]^n*Cosh[a+b*x]^p,x],x] /;
FreeQ[{a,b,c,d,m},x] && IGtQ[n,0] && IGtQ[p,0]
```

2: $\int (c + dx)^m \sinh[a + bx]^n \tanh[a + bx]^p dx \text{ when } n \in \mathbb{Z}^+ \land p \in \mathbb{Z}^+$

Derivation: Algebraic expansion

Basis: $Sinh[z]^2 Tanh[z]^2 = Sinh[z]^2 - Tanh[z]^2$

Rule: If $n \in \mathbb{Z}^+ \land p \in \mathbb{Z}^+$, then

$$\int (c + d x)^m \sinh[a + b x]^n \tanh[a + b x]^p dx \rightarrow$$

$$\int (c + d x)^m \sinh[a + b x]^n \tanh[a + b x]^{p-2} dx - \int (c + d x)^m \sinh[a + b x]^{n-2} \tanh[a + b x]^p dx$$

```
Int[(c_.+d_.*x_)^m_.*Sinh[a_.+b_.*x_]^n_.*Tanh[a_.+b_.*x_]^p_.,x_Symbol] :=
   Int[(c+d*x)^m*Sinh[a+b*x]^n*Tanh[a+b*x]^(p-2),x] - Int[(c+d*x)^m*Sinh[a+b*x]^(n-2)*Tanh[a+b*x]^p,x] /;
   FreeQ[{a,b,c,d,m},x] && IGtQ[n,0] && IGtQ[p,0]
```

```
Int[(c_.+d_.*x_)^m_.*Cosh[a_.+b_.*x_]^n_.*Coth[a_.+b_.*x_]^p_.,x_Symbol] :=
   Int[(c+d*x)^m*Cosh[a+b*x]^n*Coth[a+b*x]^(p-2),x] + Int[(c+d*x)^m*Cosh[a+b*x]^(n-2)*Coth[a+b*x]^p,x] /;
   FreeQ[{a,b,c,d,m},x] && IGtQ[n,0] && IGtQ[p,0]
```

3. $\int (c + dx)^m \operatorname{Sech}[a + bx]^n \operatorname{Tanh}[a + bx]^p dx$

1: $\int (c + dx)^m \operatorname{Sech}[a + bx]^n \operatorname{Tanh}[a + bx] dx \text{ when } m > 0$

- Derivation: Integration by parts
- Basis: Sech $[a + b x]^n$ Tanh $[a + b x] = -\partial_x \frac{\operatorname{Sech}[a + b x]^n}{b^n}$

Note: Dummy exponent p === 1 required in program code so InputForm of integrand is recognized.

Rule: If m > 0, then

$$\int (c+d\,x)^m\, \mathrm{Sech}[a+b\,x]^n\, \mathrm{Tanh}[a+b\,x]\,\,\mathrm{d}x \,\,\rightarrow\,\, -\frac{(c+d\,x)^m\, \mathrm{Sech}[a+b\,x]^n}{b\,n} \,+\, \frac{d\,m}{b\,n}\, \int (c+d\,x)^{m-1}\, \mathrm{Sech}[a+b\,x]^n\,\,\mathrm{d}x$$

```
Int[(c_.+d_.*x_)^m_.*Sech[a_.+b_.*x_]^n_.*Tanh[a_.+b_.*x_]^p_.,x_Symbol] :=
    -(c+d*x)^m*Sech[a+b*x]^n/(b*n) +
    d*m/(b*n)*Int[(c+d*x)^(m-1)*Sech[a+b*x]^n,x] /;
FreeQ[{a,b,c,d,n},x] && EqQ[p,1] && GtQ[m,0]

Int[(c_.+d_.*x_)^m_.*Csch[a_.+b_.*x_]^n_.*Coth[a_.+b_.*x_]^p_.,x_Symbol] :=
    -(c+d*x)^m*Csch[a+b*x]^n/(b*n) +
    d*m/(b*n)*Int[(c+d*x)^(m-1)*Csch[a+b*x]^n,x] /;
FreeQ[{a,b,c,d,n},x] && EqQ[p,1] && GtQ[m,0]
```

2: $\int (c + dx)^m \operatorname{Sech}[a + bx]^2 \operatorname{Tanh}[a + bx]^n dx \text{ when } m \in \mathbb{Z}^+ \bigwedge n \neq -1$

Derivation: Integration by parts

Basis: Sech $[a + b x]^2$ Tanh $[a + b x]^n = \partial_x \frac{\text{Tanh} [a+b x]^{n+1}}{b (n+1)}$

Rule: If $m \in \mathbb{Z}^+ \land n \neq -1$, then

$$\int (c + dx)^m \operatorname{Sech}[a + bx]^2 \operatorname{Tanh}[a + bx]^n dx \rightarrow \frac{(c + dx)^m \operatorname{Tanh}[a + bx]^{n+1}}{b(n+1)} - \frac{dm}{b(n+1)} \int (c + dx)^{m-1} \operatorname{Tanh}[a + bx]^{n+1} dx$$

Program code:

```
Int[(c_.+d_.*x_)^m_.*Sech[a_.+b_.*x_]^2*Tanh[a_.+b_.*x_]^n_.,x_Symbol] :=
   (c+d*x)^m*Tanh[a+b*x]^(n+1)/(b*(n+1)) -
   d*m/(b*(n+1))*Int[(c+d*x)^(m-1)*Tanh[a+b*x]^(n+1),x] /;
FreeQ[{a,b,c,d,n},x] && IGtQ[m,0] && NeQ[n,-1]
```

```
Int[(c_.+d_.*x_)^m_.*Csch[a_.+b_.*x_]^2*Coth[a_.+b_.*x_]^n_.,x_Symbol] :=
    -(c+d*x)^m*Coth[a+b*x]^(n+1)/(b*(n+1)) +
    d*m/(b*(n+1))*Int[(c+d*x)^(m-1)*Coth[a+b*x]^(n+1),x] /;
FreeQ[{a,b,c,d,n},x] && IGtQ[m,0] && NeQ[n,-1]
```

3:
$$\int (c + dx)^m \operatorname{Sech}[a + bx]^n \operatorname{Tanh}[a + bx]^p dx \text{ when } \frac{p}{2} \in \mathbb{Z}^+$$

Derivation: Algebraic expansion

Basis: $Tanh[z]^2 = 1 - Sech[z]^2$

Rule: If $\frac{p}{2} \in \mathbb{Z}^+$, then

$$\int (c+d\,x)^m\, \mathrm{Sech}[a+b\,x]^n\, \mathrm{Tanh}[a+b\,x]^p\, \mathrm{d}x \,\, \longrightarrow \\ \int (c+d\,x)^m\, \mathrm{Sech}[a+b\,x]^n\, \mathrm{Tanh}[a+b\,x]^{p-2}\, \mathrm{d}x - \int (c+d\,x)^m\, \mathrm{Sech}[a+b\,x]^{n+2}\, \mathrm{Tanh}[a+b\,x]^{p-2}\, \mathrm{d}x$$

```
Int[(c_.+d_.*x_)^m_.*Sech[a_.+b_.*x_]*Tanh[a_.+b_.*x_]^p_,x_Symbol] :=
   Int[(c+d*x)^m*Sech[a+b*x]*Tanh[a+b*x]^(p-2),x] - Int[(c+d*x)^m*Sech[a+b*x]^3*Tanh[a+b*x]^(p-2),x] /;
   FreeQ[{a,b,c,d,m},x] && IGtQ[p/2,0]
```

```
Int[(c_.+d_.*x_)^m_.*Sech[a_.+b_.*x_]^n_.*Tanh[a_.+b_.*x_]^p_,x_Symbol] :=
    Int[(c+d*x)^m*Sech[a+b*x]^n*Tanh[a+b*x]^(p-2),x] - Int[(c+d*x)^m*Sech[a+b*x]^(n+2)*Tanh[a+b*x]^(p-2),x] /;
FreeQ[{a,b,c,d,m,n},x] && IGtQ[p/2,0]

Int[(c_.+d_.*x_)^m_.*Csch[a_.+b_.*x_]*Coth[a_.+b_.*x_]^p_,x_Symbol] :=
    Int[(c+d*x)^m*Csch[a+b*x]*Coth[a+b*x]^(p-2),x] + Int[(c+d*x)^m*Csch[a+b*x]^3*Coth[a+b*x]^(p-2),x] /;
FreeQ[{a,b,c,d,m},x] && IGtQ[p/2,0]

Int[(c_.+d_.*x_)^m_.*Csch[a_.+b_.*x_]^n_.*Coth[a_.+b_.*x_]^p_,x_Symbol] :=
    Int[(c+d*x)^m*Csch[a+b*x]^n*Coth[a+b*x]^(p-2),x] + Int[(c+d*x)^m*Csch[a+b*x]^(n+2)*Coth[a+b*x]^(p-2),x] /;
FreeQ[{a,b,c,d,m,n},x] && IGtQ[p/2,0]
```

4:
$$\int (c + dx)^m \operatorname{Sech}[a + bx]^n \operatorname{Tanh}[a + bx]^p dx \text{ when } m \in \mathbb{Z}^+ \bigwedge \left(\frac{n}{2} \in \mathbb{Z} \setminus \frac{p+1}{2} \in \mathbb{Z}\right)$$

Derivation: Integration by parts

Rule: If $m \in \mathbb{Z}^+ \bigwedge \left(\frac{n}{2} \in \mathbb{Z} \bigvee \frac{p+1}{2} \in \mathbb{Z}\right)$, let $u = \int Sech[a+bx]^n Tanh[a+bx]^p dx$, then $\int (c+dx)^m Sech[a+bx]^n Tanh[a+bx]^p dx \rightarrow u (c+dx)^m - dm \int u (c+dx)^{m-1} dx$

```
Int[(c_.+d_.*x_)^m_.*Sech[a_.+b_.*x_]^n_.*Tanh[a_.+b_.*x_]^p_.,x_Symbol] :=
With[{u=IntHide[Sech[a+b*x]^n*Tanh[a+b*x]^p,x]},
Dist[(c+d*x)^m,u,x] - d*m*Int[(c+d*x)^(m-1)*u,x]] /;
FreeQ[{a,b,c,d,n,p},x] && IGtQ[m,0] && (IntegerQ[n/2] || IntegerQ[(p-1)/2])

Int[(c_.+d_.*x_)^m_.*Csch[a_.+b_.*x_]^n_.*Coth[a_.+b_.*x_]^p_.,x_Symbol] :=
With[{u=IntHide[Csch[a+b*x]^n*Coth[a+b*x]^p,x]},
Dist[(c+d*x)^m,u,x] - d*m*Int[(c+d*x)^(m-1)*u,x]] /;
FreeQ[{a,b,c,d,n,p},x] && IGtQ[m,0] && (IntegerQ[n/2] || IntegerQ[(p-1)/2])
```

4. $\int (c + dx)^m \operatorname{Sech}[a + bx]^p \operatorname{Csch}[a + bx]^n dx$

1: $\int (c + dx)^m \operatorname{Csch}[a + bx]^n \operatorname{Sech}[a + bx]^n dx \text{ when } n \in \mathbb{Z}$

Derivation: Algebraic simplification

Basis: Csch[z] Sech[z] = 2 Csch[2z]

Rule: If $n \in \mathbb{Z}$, then

$$\int \left(c+d\,x\right)^m \texttt{Csch}[\,a+b\,x\,]^n\,\texttt{Sech}[\,a+b\,x\,]^n\,\text{d}x \ \longrightarrow \ 2^n\,\int \,\left(c+d\,x\right)^m \texttt{Csch}[\,2\,a+2\,b\,x\,]^n\,\text{d}x$$

Program code:

```
Int[(c_.+d_.*x_)^m_.*Csch[a_.+b_.*x_]^n_.*Sech[a_.+b_.*x_]^n_., x_Symbol] :=
    2^n*Int[(c+d*x)^m*Csch[2*a+2*b*x]^n,x] /;
FreeQ[{a,b,c,d},x] && RationalQ[m] && IntegerQ[n]
```

Derivation: Integration by parts

Rule: If $(n \mid p) \in \mathbb{Z} \land m > 0 \land n \neq p$, let $u = \int Csch[a+bx]^n Sech[a+bx]^p dx$, then $\int (c+dx)^m Csch[a+bx]^n Sech[a+bx]^p dx \rightarrow (c+dx)^m u - dm \int (c+dx)^{m-1} u dx$

```
Int[(c_.+d_.*x_)^m_.*Csch[a_.+b_.*x_]^n_.*Sech[a_.+b_.*x_]^p_., x_Symbol] :=
With[{u=IntHide[Csch[a+b*x]^n*Sech[a+b*x]^p,x]},
Dist[(c+d*x)^m,u,x] - d*m*Int[(c+d*x)^(m-1)*u,x]] /;
FreeQ[{a,b,c,d},x] && IntegersQ[n,p] && GtQ[m,0] && NeQ[n,p]
```

5: $\int u^m \, \text{Hyper[v]}^n \, \text{Hyper[w]}^p \, dx \text{ when } u =: c + d \, x \, \bigwedge \, v =: w =: a + b \, x$

Derivation: Algebraic normalization

Rule: If $u = c + dx \wedge v = w = a + bx$, then

$$\int \! u^m \, \text{Hyper[v]}^n \, \text{Hyper[w]}^p \, \text{d} x \,\, \rightarrow \,\, \int (c + d \, x)^m \, \text{Hyper[a + b } x]^n \, \text{Hyper[a + b } x]^p \, \text{d} x$$

Program code:

```
Int[u_^m_.*F_[v_]^n_.*G_[w_]^p_.,x_Symbol] :=
   Int[ExpandToSum[u,x]^m*F[ExpandToSum[v,x]]^n*G[ExpandToSum[v,x]]^p,x] /;
FreeQ[{m,n,p},x] && HyperbolicQ[F] && HyperbolicQ[G] && EqQ[v,w] && LinearQ[{u,v,w},x] && Not[LinearMatchQ[{u,v,w},x]]
```

2: $(e+fx)^m Cosh[c+dx] (a+b Sinh[c+dx])^n dx$ when $m \in \mathbb{Z}^+ \bigwedge n \neq -1$

Derivation: Integration by parts

Basis: Cosh[c+dx] (a+b Sinh[c+dx])ⁿ = $\partial_x \frac{(a+b Sinh[c+dx])^{n+1}}{bd (n+1)}$

Rule: If $m \in \mathbb{Z}^+ \land n \neq -1$, then

$$\int \left(e+f\,x\right)^m \operatorname{Cosh}[c+d\,x] \, \left(a+b\,\operatorname{Sinh}[c+d\,x]\right)^n \, dx \, \rightarrow \, \frac{\left(e+f\,x\right)^m \, \left(a+b\,\operatorname{Sinh}[c+d\,x]\right)^{n+1}}{b\,d \, \left(n+1\right)} - \frac{f\,m}{b\,d \, \left(n+1\right)} \int \left(e+f\,x\right)^{m-1} \, \left(a+b\,\operatorname{Sinh}[c+d\,x]\right)^{n+1} \, dx$$

```
Int[(e_.+f_.*x_)^m_.*Cosh[c_.+d_.*x_]*(a_+b_.*Sinh[c_.+d_.*x_])^n_.,x_Symbol] :=
    (e+f*x)^m*(a+b*Sinh[c+d*x])^(n+1)/(b*d*(n+1)) -
    f*m/(b*d*(n+1))*Int[(e+f*x)^(m-1)*(a+b*Sinh[c+d*x])^(n+1),x] /;
FreeQ[{a,b,c,d,e,f,n},x] && IGtQ[m,0] && NeQ[n,-1]
```

```
Int[(e_.+f_.*x_)^m_.*Sinh[c_.+d_.*x_]*(a_+b_.*Cosh[c_.+d_.*x_])^n_.,x_Symbol] :=
    (e+f*x)^m*(a+b*Cosh[c+d*x])^(n+1)/(b*d*(n+1)) -
    f*m/(b*d*(n+1))*Int[(e+f*x)^(m-1)*(a+b*Cosh[c+d*x])^(n+1),x] /;
FreeQ[{a,b,c,d,e,f,n},x] && IGtQ[m,0] && NeQ[n,-1]
```

3: $\int (e + f x)^m \operatorname{Sech}[c + d x]^2 (a + b \operatorname{Tanh}[c + d x])^n dx \text{ when } m \in \mathbb{Z}^+ \bigwedge n \neq -1$

Derivation: Integration by parts

Basis: Sech $[c + dx]^2$ $(a + b Tanh [c + dx])^n = \partial_x \frac{(a+b Tanh [c+dx])^{n+1}}{bd (n+1)}$

Rule: If $m \in \mathbb{Z}^+ \land n \neq -1$, then

$$\int \left(e+f\,x\right)^m \, Sech[\,c+d\,x]^{\,2} \, \left(a+b\,Tanh[\,c+d\,x]\,\right)^n \, dx \, \rightarrow \, \frac{\left(e+f\,x\right)^m \, \left(a+b\,Tanh[\,c+d\,x]\,\right)^{n+1}}{b\,d \, \left(n+1\right)} - \frac{f\,m}{b\,d \, \left(n+1\right)} \, \int \left(e+f\,x\right)^{m-1} \, \left(a+b\,Tanh[\,c+d\,x]\,\right)^{n+1} \, dx$$

```
Int[(e_.+f_.*x_)^m_.*Sech[c_.+d_.*x_]^2*(a_+b_.*Tanh[c_.+d_.*x_])^n_.,x_Symbol] :=
    (e+f*x)^m*(a+b*Tanh[c+d*x])^(n+1)/(b*d*(n+1)) -
    f*m/(b*d*(n+1))*Int[(e+f*x)^(m-1)*(a+b*Tanh[c+d*x])^(n+1),x] /;
FreeQ[{a,b,c,d,e,f,n},x] && IGtQ[m,0] && NeQ[n,-1]
```

```
Int[(e_.+f_.*x_)^m_.*Csch[c_.+d_.*x_]^2*(a_+b_.*Coth[c_.+d_.*x_])^n_.,x_Symbol] :=
    -(e+f*x)^m*(a+b*Coth[c+d*x])^(n+1)/(b*d*(n+1)) +
    f*m/(b*d*(n+1))*Int[(e+f*x)^(m-1)*(a+b*Coth[c+d*x])^(n+1),x] /;
FreeQ[{a,b,c,d,e,f,n},x] && IGtQ[m,0] && NeQ[n,-1]
```

4: $\int (e + f x)^m \operatorname{Sech}[c + d x] \operatorname{Tanh}[c + d x] (a + b \operatorname{Sech}[c + d x])^n dx \text{ when } m \in \mathbb{Z}^+ \bigwedge n \neq -1$

Derivation: Integration by parts

Basis: Sech[c+dx] Tanh[c+dx] (a+b Sech[c+dx])ⁿ == $-\partial_x \frac{(a+b \operatorname{Sech}[c+dx])^{n+1}}{bd(n+1)}$

Rule: If $m \in \mathbb{Z}^+ \land n \neq -1$, then

$$\int \left(e + f \, x\right)^m \, \text{Sech}[c + d \, x] \, \left[a + b \, \text{Sech}[c + d \, x]\right)^n \, dx \, \rightarrow \, - \, \frac{\left(e + f \, x\right)^m \, \left(a + b \, \text{Sech}[c + d \, x]\right)^{n+1}}{b \, d \, \left(n + 1\right)} + \\ \frac{f \, m}{b \, d \, \left(n + 1\right)} \, \int \left(e + f \, x\right)^{m-1} \, \left(a + b \, \text{Sech}[c + d \, x]\right)^{n+1} \, dx$$

Program code:

5: $\int (e + f x)^m \sinh[a + b x]^p \sinh[c + d x]^q dx$ when $p \in \mathbb{Z}^+ \land q \in \mathbb{Z}^+ \land m \in \mathbb{Z}$

Derivation: Algebraic expansion

Rule: If $p \in \mathbb{Z}^+ \land q \in \mathbb{Z}^+ \land m \in \mathbb{Z}$, then

$$\int (e+f\,x)^m\, Sinh[a+b\,x]^p\, Cosh[c+d\,x]^q\, dx \,\, \rightarrow \,\, \int (e+f\,x)^m\, TrigReduce[Sinh[a+b\,x]^p\, Cosh[c+d\,x]^q]\, dx$$

```
Int[(e_.+f_.*x_)^m_.*Sinh[a_.+b_.*x_]^p_.*Sinh[c_.+d_.*x_]^q_.,x_Symbol] :=
   Int[ExpandTrigReduce[(e+f*x)^m,Sinh[a+b*x]^p*Sinh[c+d*x]^q,x],x] /;
FreeQ[{a,b,c,d,e,f},x] && IGtQ[p,0] && IntegerQ[m]
```

Int[(e_.+f_.*x_)^m_.*Cosh[a_.+b_.*x_]^p_.*Cosh[c_.+d_.*x_]^q_.,x_Symbol] :=
 Int[ExpandTrigReduce[(e+f*x)^m,Cosh[a+b*x]^p*Cosh[c+d*x]^q,x],x] /;
FreeQ[{a,b,c,d,e,f},x] && IGtQ[p,0] && IGtQ[q,0] && IntegerQ[m]

- 6: $\left[(e + f x)^m \operatorname{Sinh}[a + b x]^p \operatorname{Cosh}[c + d x]^q dx \text{ when } p \in \mathbb{Z}^+ \bigwedge q \in \mathbb{Z}^+ \right]$
 - Derivation: Algebraic expansion
 - Rule: If $p \in \mathbb{Z}^+ \land q \in \mathbb{Z}^+$, then

$$\int (e + f x)^m \sinh[a + b x]^p \cosh[c + d x]^q dx \rightarrow \int (e + f x)^m TrigReduce[Sinh[a + b x]^p Cosh[c + d x]^q] dx$$

```
Int[(e_.+f_.*x_)^m_.*Sinh[a_.+b_.*x_]^p_.*Cosh[c_.+d_.*x_]^q_.,x_Symbol] :=
   Int[ExpandTrigReduce[(e+f*x)^m,Sinh[a+b*x]^p*Cosh[c+d*x]^q,x],x] /;
FreeQ[{a,b,c,d,e,f,m},x] && IGtQ[p,0] && IGtQ[q,0]
```

- - **Derivation: Algebraic expansion**
 - Rule: If $p \in \mathbb{Z}^+ \bigwedge q \in \mathbb{Z}^+ \bigwedge bc ad = 0 \bigwedge \frac{b}{d} 1 \in \mathbb{Z}^+$, then $\int (e + fx)^m \sinh[a + bx]^p \operatorname{Sech}[c + dx]^q dx \rightarrow \int (e + fx)^m \operatorname{TrigExpand}[\sinh[a + bx]^p \operatorname{Cosh}[c + dx]^q] dx$
 - Program code:

```
Int[(e_.+f_.*x_)^m_.*F_[a_.+b_.*x_]^p_.*G_[c_.+d_.*x_]^q_.,x_Symbol] :=
Int[ExpandTrigExpand[(e+f*x)^m*G[c+d*x]^q,F,c+d*x,p,b/d,x],x] /;
FreeQ[{a,b,c,d,e,f,m},x] && MemberQ[{Sinh,Cosh},F] && MemberQ[{Sech,Csch},G] && IGtQ[p,0] && IGtQ[q,0] && EqQ[b*c-a*d,0] && IGtQ
```