

# Mathematica 11.3 Integration Test Results

Test results for the 634 problems in "4.5.3.1 (a+b sec)^m (d sec)^n (A+B sec).m"

Problem 27: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + d x]^m (b \text{Sec}[c + d x])^{4/3} (A + B \text{Sec}[c + d x]) dx$$

Optimal (type 5, 167 leaves, 6 steps):

$$\begin{aligned} & \left( 3 A b \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(-1-3m), \frac{1}{6}(5-3m), \cos[c + d x]^2\right] \right. \\ & \quad \left. \text{Sec}[c + d x]^m (b \text{Sec}[c + d x])^{1/3} \sin[c + d x] \right) / \left( d (1+3m) \sqrt{\sin[c + d x]^2} \right) + \\ & \left( 3 b B \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6}(-4-3m), \frac{1}{6}(2-3m), \cos[c + d x]^2\right] \text{Sec}[c + d x]^{1+m} \right. \\ & \quad \left. (b \text{Sec}[c + d x])^{1/3} \sin[c + d x] \right) / \left( d (4+3m) \sqrt{\sin[c + d x]^2} \right) \end{aligned}$$

Result (type 6, 4860 leaves):

$$\begin{aligned} & - \left( 18 \text{Sec}[c + d x]^{-2+m} (b \text{Sec}[c + d x])^{4/3} (A + B \text{Sec}[c + d x]) \right. \\ & \quad \left( B \text{Sec}[c + d x]^{\frac{1}{3}+m} \cos[2(c + d x)] \left( \frac{1}{2} A \text{Sec}[c + d x]^{\frac{4}{3}+m} - \frac{1}{2} A \text{Sec}[c + d x]^{\frac{7}{3}+m} \sin[c + d x] \right) + \right. \\ & \quad \text{Sec}[c + d x] \left( \frac{1}{2} A \text{Sec}[c + d x]^{\frac{1}{3}+m} + \frac{1}{2} A \text{Sec}[c + d x]^{\frac{1}{3}+m} \sin[2(c + d x)] \right) + \\ & \quad \text{Sec}[c + d x]^2 \left( B \text{Sec}[c + d x]^{\frac{1}{3}+m} \sin[c + d x]^2 + \right. \\ & \quad \left. \sin[c + d x] \left( -\frac{1}{2} A \text{Sec}[c + d x]^{\frac{1}{3}+m} + \frac{1}{2} A \text{Sec}[c + d x]^{\frac{1}{3}+m} \sin[2(c + d x)] \right) \right) \left. \right) \\ & \quad \tan\left[\frac{1}{2}(c + d x)\right] \left( (A - B) \text{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c + d x)\right]^2, \right. \right. \\ & \quad \left. \left. -\tan\left[\frac{1}{2}(c + d x)\right]^2\right] \left( -1 + \tan\left[\frac{1}{2}(c + d x)\right]^2 \right) \right) / \right. \\ & \quad \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c + d x)\right]^2, -\tan\left[\frac{1}{2}(c + d x)\right]^2\right] + \right. \\ & \quad \left. 2 \left( (1+3m) \text{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c + d x)\right]^2, -\tan\left[\frac{1}{2}(c + d x)\right]^2\right] + \right. \right. \end{aligned}$$

$$\begin{aligned}
& (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
& \left(2B \operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
& \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. (7+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{10}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Bigg) / \left( d (B+A \cos[c+dx]) \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 \right. \\
& \quad \left( \frac{1}{\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3} 36 \sec\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]^{\frac{1}{3}+m} \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \right. \right. \\
& \quad \left. \left. -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \right. \\
& \quad \left( 2B \operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \\
& \quad \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. (7+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{10}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) - \\
& \frac{1}{\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2} 9 \sec\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]^{\frac{1}{3}+m} \\
& \quad \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) / \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
\end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{2}(c+dx)\right]^2 + 2\left((1+3m)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \right.\right. \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 + (4+3m)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \right. \\
& \quad \left. -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
& \quad \left(2B\operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)/ \\
& \quad \left(9\operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2\left((1+3m)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad (7+3m)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{10}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) - \\
& \quad \frac{1}{(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2)^2} 18\left(\frac{1}{3}+m\right)\sec[c+dx]^{\frac{4}{3}+m}\sin[c+dx]\tan\left[\frac{1}{2}(c+dx)\right] \\
& \quad \left(\left((A-B)\operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.\right. \\
& \quad \left. \left. (-1+\tan\left[\frac{1}{2}(c+dx)\right]^2)\right)\right)/\left(9\operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((1+3m)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \right.\right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (4+3m)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \right.\right. \\
& \quad \left. \left. -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
& \quad \left(2B\operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)/ \\
& \quad \left(9\operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2\left((1+3m)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad (7+3m)\operatorname{AppellF1}\left[\frac{3}{2}, \frac{10}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) - \\
& \quad \frac{1}{(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2)^2} 18\sec[c+dx]^{\frac{1}{3}+m}\tan\left[\frac{1}{2}(c+dx)\right] \\
& \quad \left(\left((A-B)\operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.\right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\right)\right)/\left(9\operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \right.\right.
\end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left(\left(1+3m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
& \quad \left((A-B)\left(-\frac{1}{3}\left(-\frac{1}{3}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}\left(\frac{4}{3}+m\right) \right. \right. \\
& \quad \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) / \\
& \quad \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2\left(\left(1+3m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
& \quad \left(2B\left(-\frac{1}{3}\left(-\frac{1}{3}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \frac{1}{3}\left(\frac{7}{3}+m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{10}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) / \\
& \quad \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2\left(\left(1+3m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. (7+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{10}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - \\
& \quad \left((A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\left(2\left(\left(1+3m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) + (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \sec\left[\frac{1}{2}(c+dx)\right]^2
\end{aligned}$$

$$\begin{aligned} & \tan\left[\frac{1}{2}(c+dx)\right] + 9\left(-\frac{1}{3}\left(-\frac{1}{3}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\ & \quad \frac{1}{3}\left(\frac{4}{3}+m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\left. \right) + \\ & \quad 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (1+3m) \left(-\frac{3}{5}\left(\frac{2}{3}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\ & \quad \left. \left. \frac{3}{5}\left(\frac{4}{3}+m\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) + \right. \\ & \quad \left. (4+3m) \left(-\frac{3}{5}\left(-\frac{1}{3}-m\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\ & \quad \left. \left. \frac{3}{5}\left(\frac{7}{3}+m\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{10}{3}+m, -\frac{1}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) \right) \Big/ \\ & \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ & \quad 2 \left( (1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \Big) \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\ & \left( 2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{7}{3}+m, -\frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\ & \quad \left. \left( 2 \left( (1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \right. \\ & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + (7+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{10}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\ & \quad \left. (c+dx) \right) + 9 \left( -\frac{1}{3}\left(-\frac{1}{3}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\ & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}\left(\frac{7}{3}+m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{10}{3}+m, -\frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) \end{aligned}$$

$$\begin{aligned}
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left( (1+3m) \left( -\frac{3}{5} \left( \frac{2}{3} - m \right) \text{AppellF1}\left[\frac{5}{2}, \frac{7}{3} + m, \frac{5}{3} - m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{3}{5} \left( \frac{7}{3} + m \right) \text{AppellF1}\left[\frac{5}{2}, \frac{10}{3} + m, \frac{2}{3} - m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + (7+3m) \right. \right. \\
& \quad \left( -\frac{3}{5} \left( -\frac{1}{3} - m \right) \text{AppellF1}\left[\frac{5}{2}, \frac{10}{3} + m, \frac{2}{3} - m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \right. \\
& \quad \left. \left. \left. \frac{3}{5} \left( \frac{10}{3} + m \right) \text{AppellF1}\left[\frac{5}{2}, \frac{13}{3} + m, -\frac{1}{3} - m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Bigg/ \\
& \left( 9 \text{AppellF1}\left[\frac{1}{2}, \frac{7}{3} + m, -\frac{1}{3} - m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (1+3m) \text{AppellF1}\left[\frac{3}{2}, \frac{7}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (7+3m) \text{AppellF1}\left[\frac{3}{2}, \frac{10}{3} + m, -\frac{1}{3} - m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) \Bigg)
\end{aligned}$$

**Problem 28: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sec[c+dx]^m (b \sec[c+dx])^{2/3} (A+B \sec[c+dx]) dx$$

Optimal (type 5, 165 leaves, 6 steps):

$$\begin{aligned}
& - \left( \left( 3 A \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6} (1-3m), \frac{1}{6} (7-3m), \cos[c+dx]^2\right] \right. \right. \\
& \quad \left. \left. \sec[c+dx]^{-1+m} (b \sec[c+dx])^{2/3} \sin[c+dx] \right) \Bigg/ \left( d (1-3m) \sqrt{\sin[c+dx]^2} \right) \right) + \\
& \left( 3 B \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{6} (-2-3m), \frac{1}{6} (4-3m), \cos[c+dx]^2\right] \sec[c+dx]^m \right. \\
& \quad \left. (b \sec[c+dx])^{2/3} \sin[c+dx] \right) \Bigg/ \left( d (2+3m) \sqrt{\sin[c+dx]^2} \right)
\end{aligned}$$

Result (type 6, 5573 leaves):

$$\begin{aligned}
& \left( 2 \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{-\frac{1}{3}+m} (b \sec [c + d x])^{2/3} \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{\frac{2}{3}+m} \right. \\
& (A + B \sec [c + d x]) \left( B \sec [c + d x]^{-\frac{1}{3}+m} + \frac{1}{2} A \sec [c + d x]^{\frac{2}{3}+m} + \right. \\
& \cos [2 (c + d x)] \left( \frac{1}{2} A \sec [c + d x]^{\frac{2}{3}+m} - \frac{1}{2} i A \sec [c + d x]^{\frac{5}{3}+m} \sin [c + d x] \right) + \frac{1}{2} i A \\
& \sec [c + d x]^{\frac{2}{3}+m} \sin [2 (c + d x)] + \sec [c + d x] \left( B \sec [c + d x]^{\frac{2}{3}+m} \sin [c + d x]^2 + \sin [c + d x] \right. \\
& \left. \left. \left( -\frac{1}{2} i A \sec [c + d x]^{\frac{2}{3}+m} + \frac{1}{2} A \sec [c + d x]^{\frac{2}{3}+m} \sin [2 (c + d x)] \right) \right) \right) \tan \left[ \frac{1}{2} (c + d x) \right] \\
& \left( - \left( \left( 9 (A + B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{3} + m, \frac{1}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \right. \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{3} + m, \frac{1}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& 2 \left( (-1 + 3 m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3} + m, \frac{4}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& (5 + 3 m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{8}{3} + m, \frac{1}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \\
& \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left. \right) + \left( 5 (A - B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3} + m, \frac{1}{3} - m, \frac{5}{2}, \right. \right. \\
& \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left. \right) / \\
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3} + m, \frac{1}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& 2 \left( (-1 + 3 m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3} + m, \frac{4}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& (5 + 3 m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{8}{3} + m, \frac{1}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
& \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left. \right) \right) / \\
& \left( d (B + A \cos [c + d x]) \sec [c + d x]^{5/3} \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right. \\
& \left( -\frac{1}{\left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2} \right. \\
& 2 \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{\frac{2}{3}+m} \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{\frac{2}{3}+m} \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \left( - \left( \left( 9 (A + B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{3} + m, \frac{1}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \right. \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{5}{3} + m, \frac{1}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + 2 \right. \\
& \left. \left( (-1 + 3 m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3} + m, \frac{4}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + (5+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \right. \\
& \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
& \left(5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) / \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-1+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}+m, \right. \right. \\
& \left. \left. \frac{1}{3}-m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
& \frac{1}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^{\frac{2}{3}+m} \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{\frac{2}{3}+m} \\
& \left(-\left(\left(9(A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \right. \right. \\
& \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2\left((-1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
& \left(5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) / \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-1+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}+m, \right. \right. \\
& \left. \left. \frac{1}{3}-m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
& \frac{1}{-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} 2\left(-\frac{1}{3}+m\right) \left(\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2\right)^{-\frac{1}{3}+m} \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]^2 \operatorname{Sec}[c+dx]\right)^{\frac{2}{3}+m} \\
& \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left(-\left(\left(9(A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \right. \right. \\
& \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.
\end{aligned}$$



$$\begin{aligned}
& 2 \left( (-1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& \left( 5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-1+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}+m, \right. \right. \\
& \quad \left. \left. \frac{1}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& \frac{1}{-1+\tan\left[\frac{1}{2}(c+dx)\right]^2} 2 \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-\frac{1}{3}+m} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{\frac{2}{3}+m} \\
& \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left( - \left( \left( 9(A+B) \left( -\frac{1}{3} \left( \frac{1}{3}-m \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} \left( \frac{5}{3}+m \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{8}{3}+m, \right. \right. \\
& \quad \left. \left. \frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& \left( 5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \\
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-1+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. (5+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \left( 5(A-B) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -\frac{3}{5} \left( \frac{1}{3} - m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{5}{3} + m, \frac{4}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{3}{5} \left( \frac{5}{3} + m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{8}{3} + m, \frac{1}{3} - m, \frac{7}{2}, \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \Big) / \\
& \left( 15 \text{AppellF1} \left[ \frac{3}{2}, \frac{5}{3} + m, \frac{1}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( (-1 + 3 m) \text{AppellF1} \left[ \frac{5}{2}, \frac{5}{3} + m, \frac{4}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (5 + 3 m) \text{AppellF1} \left[ \frac{5}{2}, \frac{8}{3} + m, \frac{1}{3} - m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Big) + \\
& \left( 9 (A + B) \text{AppellF1} \left[ \frac{1}{2}, \frac{5}{3} + m, \frac{1}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left( 2 \left( (-1 + 3 m) \text{AppellF1} \left[ \frac{3}{2}, \frac{5}{3} + m, \frac{4}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + \right. \right. \right. \\
& \quad \left. \left. d x) \right]^2 \right] + (5 + 3 m) \text{AppellF1} \left[ \frac{3}{2}, \frac{8}{3} + m, \frac{1}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + 9 \left( -\frac{1}{3} \right. \\
& \quad \left( \frac{1}{3} - m \right) \text{AppellF1} \left[ \frac{3}{2}, \frac{5}{3} + m, \frac{4}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{3} \left( \frac{5}{3} + m \right) \text{AppellF1} \left[ \frac{3}{2}, \frac{8}{3} + m, \frac{1}{3} - m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \Big) + \\
& \quad 2 \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left( (-1 + 3 m) \left( -\frac{3}{5} \left( \frac{4}{3} - m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{5}{3} + m, \frac{7}{3} - m, \right. \right. \right. \\
& \quad \left. \left. \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \right. \right. \\
& \quad \left. \left. \frac{1}{2} (c + d x) \right] + \frac{3}{5} \left( \frac{5}{3} + m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{8}{3} + m, \frac{4}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \Big) + \\
& \quad (5 + 3 m) \left( -\frac{3}{5} \left( \frac{1}{3} - m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{8}{3} + m, \frac{4}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \right. \\
& \quad \left. \frac{3}{5} \left( \frac{8}{3} + m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{11}{3} + m, \frac{1}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \Big) \Big) / \\
& \left( 9 \text{AppellF1} \left[ \frac{1}{2}, \frac{5}{3} + m, \frac{1}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right.
\end{aligned}$$

$$\begin{aligned}
& 2 \left( (-1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
& \left( 5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 2 \left( (-1+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad 15 \left( -\frac{3}{5} \left( \frac{1}{3}-m \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{3}{5} \left( \frac{5}{3}+m \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\
& \quad 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (-1+3m) \left( -\frac{5}{7} \left( \frac{4}{3}-m \right) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}+m, \frac{7}{3}-m, \right. \right. \right. \\
& \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
& \quad \left. \left. + \frac{5}{7} \left( \frac{5}{3}+m \right) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}+m, \frac{4}{3}-m, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\
& \quad (5+3m) \left( -\frac{5}{7} \left( \frac{1}{3}-m \right) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}+m, \frac{4}{3}-m, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{5}{7} \left( \frac{8}{3}+m \right) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{11}{3}+m, \frac{1}{3}-m, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Bigg/ \\
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( (-1+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 +
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} 2^{\left(\frac{2}{3}+m\right)} \left(\sec\left[\frac{1}{2}(c+dx)\right]^2\right)^{-\frac{1}{3}+m} \\
& \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{-\frac{1}{3}+m} \\
& \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left(-\left(\left(9(A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right)/\right. \\
& \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2\left(\left(-1+3m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \right. \right. \\
& \left. \left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + \\
& \left(5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) / \\
& \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}+m, \frac{1}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2\left(\left(-1+3m\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}+m, \frac{4}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (5+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}+m, \frac{1}{3}-m, \frac{7}{2}, \right. \right. \\
& \left. \left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \left(-\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \sec[c+dx] \tan[c+dx]\right) \Bigg)
\end{aligned}$$

**Problem 29: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sec[c+dx]^m (b \sec[c+dx])^{1/3} (A+B \sec[c+dx]) dx$$

Optimal (type 5, 165 leaves, 6 steps):

$$\begin{aligned}
& - \left( \left( 3 A \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{6} (2-3m), \frac{1}{6} (8-3m), \cos [c+dx]^2 \right] \right. \right. \\
& \quad \left. \left. \sec [c+dx]^{-1+m} (b \sec [c+dx])^{1/3} \sin [c+dx] \right) / \left( d (2-3m) \sqrt{\sin [c+dx]^2} \right) \right) + \\
& \left( 3 B \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{6} (-1-3m), \frac{1}{6} (5-3m), \cos [c+dx]^2 \right] \sec [c+dx]^m \right. \\
& \quad \left. (b \sec [c+dx])^{1/3} \sin [c+dx] \right) / \left( d (1+3m) \sqrt{\sin [c+dx]^2} \right)
\end{aligned}$$

Result(type 6, 5573 leaves):

$$\begin{aligned}
& \left( 2 \left( \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-\frac{2}{3}+m} (b \sec [c+dx])^{1/3} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{\frac{1}{3}+m} \right. \\
& \quad (A+B \sec [c+dx]) \left( B \sec [c+dx]^{-\frac{2}{3}+m} + \frac{1}{2} A \sec [c+dx]^{\frac{1}{3}+m} + \right. \\
& \quad \cos [2 (c+dx)] \left( \frac{1}{2} A \sec [c+dx]^{\frac{1}{3}+m} - \frac{1}{2} A \sec [c+dx]^{\frac{4}{3}+m} \sin [c+dx] \right) + \frac{1}{2} A \\
& \quad \sec [c+dx]^{\frac{1}{3}+m} \sin [2 (c+dx)] + \sec [c+dx] \left( B \sec [c+dx]^{\frac{1}{3}+m} \sin [c+dx]^2 + \sin [c+dx] \right. \\
& \quad \left. \left( -\frac{1}{2} A \sec [c+dx]^{\frac{1}{3}+m} + \frac{1}{2} A \sec [c+dx]^{\frac{1}{3}+m} \sin [2 (c+dx)] \right) \right) \tan \left[ \frac{1}{2} (c+dx) \right] \\
& \quad \left. \left( - \left( \left( 9 (A+B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \right. \right. \right. \\
& \quad \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( (-2+3m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. \left. (4+3m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \left( 5 (A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \right. \right. \\
& \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) / \\
& \quad \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( (-2+3m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. \left. (4+3m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) \Big) / \\
& \left( d (B+A \cos [c+dx]) \sec [c+dx]^{4/3} \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -\frac{1}{\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2} \right. \\
& 2 \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{\frac{1}{3}+m} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{\frac{1}{3}+m} \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left( -\left( \left( 9(A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right. \\
& \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
& \left( (-2+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& \left( 5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (4+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}+m, \right. \right. \\
& \left. \left. \frac{2}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& \frac{1}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{\frac{1}{3}+m} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{\frac{1}{3}+m} \\
& \left( -\left( \left( 9(A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right. \\
& \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( (-2+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& \left( 5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left( (-2+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (4+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}+m, \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{2}{3} - m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& \frac{1}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} 2 \left(-\frac{2}{3} + m\right) \left(\sec\left[\frac{1}{2}(c+dx)\right]^2\right)^{-\frac{2}{3}+m} \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{\frac{1}{3}+m} \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left(-\left(\left(9(A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \right. \\
& \left.\left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right.\right. \\
& \left.2\left((-2+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right. \\
& \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \right. \\
& \left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& \left.5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left.\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Bigg) \Bigg/ \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
& \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-2+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{7}{2}, \right.\right. \\
& \left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (4+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}+m, \right. \\
& \left.\frac{2}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& \frac{1}{-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} 2 \left(\sec\left[\frac{1}{2}(c+dx)\right]^2\right)^{-\frac{2}{3}+m} \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{\frac{1}{3}+m} \\
& \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left(-\left(\left(9(A+B) \left(-\frac{1}{3}\left(\frac{2}{3}-m\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right.\right.\right.\right.\right. \\
& \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}\left(\frac{4}{3}+m\right) \operatorname{AppellF1}\left[\right. \\
& \left.\frac{3}{2}, \frac{7}{3}+m, \frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left.\tan\left[\frac{1}{2}(c+dx)\right]\right) \Bigg) \Bigg/ \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{4}{3}+m, \frac{2}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right.\right. \\
& \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\left((-2+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}+m, \frac{5}{3}-m, \frac{5}{2}, \right.\right. \\
& \left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (4+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{3}+m, \right. \\
& \left.\frac{2}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) +
\end{aligned}$$

$$\begin{aligned}
& \left( 5 (A - B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) / \\
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( (-2 + 3 m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3} + m, \frac{5}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. (4 + 3 m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3} + m, \frac{2}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left. + \left( 5 (A - B) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right. \right. \\
& \quad \left. \left( -\frac{3}{5} \left( \frac{2}{3} - m \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3} + m, \frac{5}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{3}{5} \left( \frac{4}{3} + m \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3} + m, \frac{2}{3} - m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( (-2 + 3 m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3} + m, \frac{5}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (4 + 3 m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3} + m, \frac{2}{3} - m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left. + \right. \\
& \left( 9 (A + B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{4}{3} + m, \frac{2}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left( 2 \left( (-2 + 3 m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3} + m, \frac{5}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + \right. \right. \right. \\
& \quad \left. \left. \left. d x) \right]^2 \right] + (4 + 3 m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + 9 \left( -\frac{1}{3} \right. \right. \\
& \quad \left. \left( \frac{2}{3} - m \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3} + m, \frac{5}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{3} \left( \frac{4}{3} + m \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{7}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \left. + \right. \\
& \quad 2 \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left( (-2 + 3 m) \left( -\frac{3}{5} \left( \frac{5}{3} - m \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3} + m, \frac{8}{3} - m, \right. \right. \right. \\
& \quad \left. \left. \left. \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \right. \right. \right. \\
& \quad \left. \left. \left. \frac{1}{2} (c + d x) \right] + \frac{3}{5} \left( \frac{4}{3} + m \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3} + m, \frac{5}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right.
\end{aligned}$$



$$\begin{aligned} & -\tan\left[\frac{1}{2}(c+dx)\right]^2\Big]\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\Big)+ \\ & (4+3m)\left(-\frac{3}{5}\left(\frac{2}{3}-m\right)\operatorname{AppellF1}\left[\frac{5}{2},\frac{7}{3}+m,\frac{5}{3}-m,\frac{7}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right. \\ & \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\Big]\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]+\right. \\ & \left.\frac{3}{5}\left(\frac{7}{3}+m\right)\operatorname{AppellF1}\left[\frac{5}{2},\frac{10}{3}+m,\frac{2}{3}-m,\frac{7}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right. \\ & \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\Big]\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\Big)\Big)\Big)\Big)\Big)\Big)/ \\ & \left(9\operatorname{AppellF1}\left[\frac{1}{2},\frac{4}{3}+m,\frac{2}{3}-m,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\ & 2\left((-2+3m)\operatorname{AppellF1}\left[\frac{3}{2},\frac{4}{3}+m,\frac{5}{3}-m,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right. \\ & \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+(4+3m)\operatorname{AppellF1}\left[\frac{3}{2},\frac{7}{3}+m,\frac{2}{3}-m,\frac{5}{2},\right. \\ & \left.\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\tan\left[\frac{1}{2}(c+dx)\right]^2- \\ & \left.5(A-B)\operatorname{AppellF1}\left[\frac{3}{2},\frac{4}{3}+m,\frac{2}{3}-m,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\ & \tan\left[\frac{1}{2}(c+dx)\right]^2\left(2\left((-2+3m)\operatorname{AppellF1}\left[\frac{5}{2},\frac{4}{3}+m,\frac{5}{3}-m,\frac{7}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right.\right. \\ & \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+(4+3m)\operatorname{AppellF1}\left[\frac{5}{2},\frac{7}{3}+m,\frac{2}{3}-m,\frac{7}{2},\right. \\ & \left.\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]+ \\ & 15\left(-\frac{3}{5}\left(\frac{2}{3}-m\right)\operatorname{AppellF1}\left[\frac{5}{2},\frac{4}{3}+m,\frac{5}{3}-m,\frac{7}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right. \\ & \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\Big]\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]+\right. \\ & \left.\frac{3}{5}\left(\frac{4}{3}+m\right)\operatorname{AppellF1}\left[\frac{5}{2},\frac{7}{3}+m,\frac{2}{3}-m,\frac{7}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right. \\ & \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\Big]\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\Big)+ \right. \\ & 2\tan\left[\frac{1}{2}(c+dx)\right]^2\left((-2+3m)\left(-\frac{5}{7}\left(\frac{5}{3}-m\right)\operatorname{AppellF1}\left[\frac{7}{2},\frac{4}{3}+m,\frac{8}{3}-m,\right.\right.\right. \\ & \left.\frac{9}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]+ \right. \\ & \left.\frac{5}{7}\left(\frac{4}{3}+m\right)\operatorname{AppellF1}\left[\frac{7}{2},\frac{7}{3}+m,\frac{5}{3}-m,\frac{9}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right. \\ & \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\Big]\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]\Big)+ \right. \\ & (4+3m)\left(-\frac{5}{7}\left(\frac{2}{3}-m\right)\operatorname{AppellF1}\left[\frac{7}{2},\frac{7}{3}+m,\frac{5}{3}-m,\frac{9}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right. \\ & \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\Big]\sec\left[\frac{1}{2}(c+dx)\right]^2\tan\left[\frac{1}{2}(c+dx)\right]+ \right. \end{aligned}$$

$$\begin{aligned}
& \frac{5}{7} \left( \frac{7}{3} + m \right) \text{AppellF1} \left[ \frac{7}{2}, \frac{10}{3} + m, \frac{2}{3} - m, \frac{9}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
& \quad \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) \Bigg/ \\
& \left( 15 \text{AppellF1} \left[ \frac{3}{2}, \frac{4}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( (-2 + 3 m) \text{AppellF1} \left[ \frac{5}{2}, \frac{4}{3} + m, \frac{5}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (4 + 3 m) \text{AppellF1} \left[ \frac{5}{2}, \frac{7}{3} + m, \frac{2}{3} - m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) + \\
& \frac{1}{-1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2} 2 \left( \frac{1}{3} + m \right) \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{-\frac{2}{3} + m} \\
& \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{-\frac{2}{3} + m} \\
& \tan \left[ \frac{1}{2} (c + d x) \right] \\
& \left( - \left( \left( 9 (A + B) \text{AppellF1} \left[ \frac{1}{2}, \frac{4}{3} + m, \frac{2}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \right) \right. \\
& \quad \left( 9 \text{AppellF1} \left[ \frac{1}{2}, \frac{4}{3} + m, \frac{2}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( (-2 + 3 m) \text{AppellF1} \left[ \frac{3}{2}, \frac{4}{3} + m, \frac{5}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (4 + 3 m) \text{AppellF1} \left[ \frac{3}{2}, \frac{7}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) + \\
& \left( 5 (A - B) \text{AppellF1} \left[ \frac{3}{2}, \frac{4}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \Bigg/ \\
& \left( 15 \text{AppellF1} \left[ \frac{3}{2}, \frac{4}{3} + m, \frac{2}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( (-2 + 3 m) \text{AppellF1} \left[ \frac{5}{2}, \frac{4}{3} + m, \frac{5}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (4 + 3 m) \text{AppellF1} \left[ \frac{5}{2}, \frac{7}{3} + m, \frac{2}{3} - m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) \\
& \left( - \cos \left[ \frac{1}{2} (c + d x) \right] \sec [c + d x] \sin \left[ \frac{1}{2} (c + d x) \right] + \cos \left[ \frac{1}{2} (c + d x) \right]^2 \right)
\end{aligned}$$



$$\begin{aligned}
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& 2 \left( (-7+3m) \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \left. (-1+3m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}+m, \frac{7}{3}-m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
& \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \Bigg) / \left( d (B+A \cos [c+dx]) (b \sec [c+dx])^{4/3} \right. \\
& \left( 2 \left( \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-\frac{4}{3}+m} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{\frac{2}{3}+m} \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
& \left. - \left( \left( 9 (A+B) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) / \right. \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& 2 \left( (-7+3m) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + (-1+3m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \Bigg) + \\
& \left( 5 (A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) / \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( (-7+3m) \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + (-1+3m) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}+m, \right. \right. \\
& \left. \left. \frac{7}{3}-m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \Bigg) + \\
& \left( \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-\frac{4}{3}+m} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{\frac{2}{3}+m} \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \left( - \left( \left( 9 (A+B) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) / \right. \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& 2 \left( (-7+3m) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + (-1+3m) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \Bigg) + \\
& \left( 5 (A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( (-7+3m) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (-1+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}+m, \frac{7}{3}-m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& 2 \left( -\frac{7}{3}+m \right) \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-\frac{7}{3}+m} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{\frac{2}{3}+m} \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \left( - \left( \left( 9(A+B) \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) / \right. \\
& \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( (-7+3m) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (-1+3m) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& \left( 5(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \\
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( (-7+3m) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (-1+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}+m, \frac{7}{3}-m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& 2 \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-\frac{7}{3}+m} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{\frac{2}{3}+m} \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \left( - \left( \left( 9(A+B) \left( -\frac{1}{3} \left( \frac{7}{3}-m \right) \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} \right. \right. \right. \right. \right. \right. \right. \\
\end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{1}{3} + m \right) \text{AppellF1} \left[ \frac{3}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
 & \quad \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \Bigg) / \\
 & \left( 9 \text{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3} + m, \frac{7}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-7 + 3m) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3} + m, \frac{10}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (-1 + 3m) \text{AppellF1} \left[ \frac{3}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \Bigg) + \\
 & \left( 5 (A - B) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3} + m, \frac{7}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
 & \quad \left. \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) / \\
 & \left( 15 \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3} + m, \frac{7}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + 2 \right. \\
 & \quad \left( (-7 + 3m) \text{AppellF1} \left[ \frac{5}{2}, -\frac{1}{3} + m, \frac{10}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
 & \quad \left. (-1 + 3m) \text{AppellF1} \left[ \frac{5}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \\
 & \quad \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) + \left( 5 (A - B) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right. \\
 & \quad \left( -\frac{3}{5} \left( \frac{7}{3} - m \right) \text{AppellF1} \left[ \frac{5}{2}, -\frac{1}{3} + m, \frac{10}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
 & \quad \left. \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{3}{5} \left( -\frac{1}{3} + m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \Bigg) / \\
 & \left( 15 \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3} + m, \frac{7}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
 & \quad 2 \left( (-7 + 3m) \text{AppellF1} \left[ \frac{5}{2}, -\frac{1}{3} + m, \frac{10}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (-1 + 3m) \text{AppellF1} \left[ \frac{5}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) + \\
 & \left( 9 (A + B) \text{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3} + m, \frac{7}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
 & \quad \left( 2 \left( (-7 + 3m) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3} + m, \frac{10}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (-1 + 3m) \text{AppellF1} \left[ \frac{3}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \text{Sec} \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
& 9 \left( -\frac{1}{3} \left( \frac{7}{3} - m \right) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3} + m, \frac{10}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{3} \left( -\frac{1}{3} + m \right) \right. \\
& \quad \left. \text{AppellF1} \left[ \frac{3}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) + 2 \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \quad \left( (-7 + 3m) \left( -\frac{3}{5} \left( \frac{10}{3} - m \right) \text{AppellF1} \left[ \frac{5}{2}, -\frac{1}{3} + m, \frac{13}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \right. \\
& \quad \left. \frac{3}{5} \left( -\frac{1}{3} + m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{2}{3} + m, \frac{10}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) + \\
& \quad (-1 + 3m) \left( -\frac{3}{5} \left( \frac{7}{3} - m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{2}{3} + m, \frac{10}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \right. \\
& \quad \left. \frac{3}{5} \left( \frac{2}{3} + m \right) \text{AppellF1} \left[ \frac{5}{2}, \frac{5}{3} + m, \frac{7}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \Big/ \\
& \quad \left( 9 \text{AppellF1} \left[ \frac{1}{2}, -\frac{1}{3} + m, \frac{7}{3} - m, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( (-7 + 3m) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3} + m, \frac{10}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (-1 + 3m) \text{AppellF1} \left[ \frac{3}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 - \\
& \quad \left( 5 (A - B) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{3} + m, \frac{7}{3} - m, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left( 2 \left( (-7 + 3m) \text{AppellF1} \left[ \frac{5}{2}, -\frac{1}{3} + m, \frac{10}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (-1 + 3m) \text{AppellF1} \left[ \frac{5}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \\
& \quad 15 \left( -\frac{3}{5} \left( \frac{7}{3} - m \right) \text{AppellF1} \left[ \frac{5}{2}, -\frac{1}{3} + m, \frac{10}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. - \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{3}{5} \left( -\frac{1}{3} + m \right) \right. \\
& \quad \left. \text{AppellF1} \left[ \frac{5}{2}, \frac{2}{3} + m, \frac{7}{3} - m, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right)
\end{aligned}$$

$$\begin{aligned}
 & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \left( (-7+3m) \left( -\frac{5}{7} \left( \frac{10}{3} - m \right) \text{AppellF1}\left[\frac{7}{2}, -\frac{1}{3}+m, \frac{13}{3}-m, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{5}{7} \left( -\frac{1}{3}+m \right) \text{AppellF1}\left[\frac{7}{2}, \frac{2}{3}+m, \frac{10}{3}-m, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
 & \quad (-1+3m) \left( -\frac{5}{7} \left( \frac{7}{3} - m \right) \text{AppellF1}\left[\frac{7}{2}, \frac{2}{3}+m, \frac{10}{3}-m, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
 & \quad \left. \frac{5}{7} \left( \frac{2}{3}+m \right) \text{AppellF1}\left[\frac{7}{2}, \frac{5}{3}+m, \frac{7}{3}-m, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Big/ \\
 & \left( 15 \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-7+3m) \text{AppellF1}\left[\frac{5}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (-1+3m) \text{AppellF1}\left[\frac{5}{2}, \frac{2}{3}+m, \frac{7}{3}-m, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
 & 2 \left( \frac{2}{3}+m \right) \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \right)^{-\frac{7}{3}+m} \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{-\frac{1}{3}+m} \\
 & \tan\left[ \frac{1}{2}(c+dx) \right] \\
 & \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
 & \left( - \left( \left( 9(A+B) \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right) \Big/ \\
 & \left( 9 \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
 & \quad 2 \left( (-7+3m) \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (-1+3m) \text{AppellF1}\left[\frac{3}{2}, \frac{2}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) + \\
 & \left( 5(A-B) \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
 \end{aligned}$$



$$\begin{aligned} & \left. \left. \left. \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2\right) / \right. \right. \right. \right. \right. \\ & \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, -\frac{1}{3}+m, \frac{7}{3}-m, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ & 2 \left( (-7+3m) \operatorname{AppellF1}\left[\frac{5}{2}, -\frac{1}{3}+m, \frac{10}{3}-m, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\ & \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (-1+3m) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}+m, \frac{7}{3}-m, \frac{7}{2}, \right. \right. \\ & \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\ & \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\ & \left. \left. \sec[c+dx] \tan[c+dx] \right) \right) \right) \right) \right) \end{aligned}$$

**Problem 39: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sec[c+dx]^{3/2} (b \sec[c+dx])^n (A+B \sec[c+dx]) dx$$

Optimal (type 5, 163 leaves, 6 steps):

$$\begin{aligned} & \left( 2 A \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(-1-2n), \frac{1}{4}(3-2n), \cos[c+dx]^2\right] \right. \\ & \left. \sqrt{\sec[c+dx]} (b \sec[c+dx])^n \sin[c+dx] \right) / \left( d(1+2n) \sqrt{\sin[c+dx]^2} \right) + \\ & \left( 2 B \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1}{4}(-3-2n), \frac{1}{4}(1-2n), \cos[c+dx]^2\right] \sec[c+dx]^{3/2} \right. \\ & \left. (b \sec[c+dx])^n \sin[c+dx] \right) / \left( d(3+2n) \sqrt{\sin[c+dx]^2} \right) \end{aligned}$$

Result (type 6, 4819 leaves):

$$\begin{aligned} & - \left( \left( 6 \sqrt{\sec[c+dx]} (b \sec[c+dx])^n \right. \right. \\ & \left( B \sec[c+dx]^{\frac{1}{2}+n} + \cos[2(c+dx)] \left( \frac{1}{2} A \sec[c+dx]^{\frac{3}{2}+n} - \frac{1}{2} A \sec[c+dx]^{\frac{5}{2}+n} \sin[c+dx] \right) + \right. \\ & \sec[c+dx] \left( \frac{1}{2} A \sec[c+dx]^{\frac{1}{2}+n} + \frac{1}{2} A \sec[c+dx]^{\frac{1}{2}+n} \sin[2(c+dx)] \right) + \\ & \sec[c+dx]^2 \left( B \sec[c+dx]^{\frac{1}{2}+n} \sin[c+dx]^2 + \right. \\ & \left. \left. \sin[c+dx] \left( -\frac{1}{2} A \sec[c+dx]^{\frac{1}{2}+n} + \frac{1}{2} A \sec[c+dx]^{\frac{1}{2}+n} \sin[2(c+dx)] \right) \right) \right) \\ & \tan\left[\frac{1}{2}(c+dx)\right] \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{2}(c+dx)\right]^2\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\Bigg)\Bigg/\Bigg( \\
& \left(3\operatorname{AppellF1}\left[\frac{1}{2},\frac{3}{2}+n,-\frac{1}{2}-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
& \left.\left((1+2n)\operatorname{AppellF1}\left[\frac{3}{2},\frac{3}{2}+n,\frac{1}{2}-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \right. \\
& \left.\left.(3+2n)\operatorname{AppellF1}\left[\frac{3}{2},\frac{5}{2}+n,-\frac{1}{2}-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left.\left.\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\tan\left[\frac{1}{2}(c+dx)\right]^2\right)- \right. \right. \\
& \left.\left.(2B\operatorname{AppellF1}\left[\frac{1}{2},\frac{5}{2}+n,-\frac{1}{2}-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\Bigg)\Bigg/\Bigg( \\
& \left(3\operatorname{AppellF1}\left[\frac{1}{2},\frac{5}{2}+n,-\frac{1}{2}-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
& \left.\left((1+2n)\operatorname{AppellF1}\left[\frac{3}{2},\frac{5}{2}+n,\frac{1}{2}-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \right. \\
& \left.\left.(5+2n)\operatorname{AppellF1}\left[\frac{3}{2},\frac{7}{2}+n,-\frac{1}{2}-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2\Bigg)\Bigg)\Bigg/\left(d\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right. \\
& \left.\left(\frac{1}{\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^3}12\sec\left[\frac{1}{2}(c+dx)\right]^2\sec[c+dx]^{\frac{1}{2}+n}\tan\left[\frac{1}{2}(c+dx)\right]^2\right. \right. \\
& \left.\left.\left(\left((A-B)\operatorname{AppellF1}\left[\frac{1}{2},\frac{3}{2}+n,-\frac{1}{2}-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \right. \\
& \left.\left.\left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\Bigg)\Bigg/\left(3\operatorname{AppellF1}\left[\frac{1}{2},\frac{3}{2}+n,-\frac{1}{2}-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left.\left.\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right)+\left((1+2n)\operatorname{AppellF1}\left[\frac{3}{2},\frac{3}{2}+n,\frac{1}{2}-n,\frac{5}{2}, \right. \right. \right. \right. \\
& \left.\left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right)+(3+2n)\operatorname{AppellF1}\left[\frac{3}{2},\frac{5}{2}+n, \right. \right. \right. \\
& \left.\left.\left.-\frac{1}{2}-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\tan\left[\frac{1}{2}(c+dx)\right]^2\right)- \right. \right. \\
& \left.\left.(2B\operatorname{AppellF1}\left[\frac{1}{2},\frac{5}{2}+n,-\frac{1}{2}-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)\Bigg)\Bigg/\Bigg( \\
& \left(3\operatorname{AppellF1}\left[\frac{1}{2},\frac{5}{2}+n,-\frac{1}{2}-n,\frac{3}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \\
& \left.\left((1+2n)\operatorname{AppellF1}\left[\frac{3}{2},\frac{5}{2}+n,\frac{1}{2}-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2,-\tan\left[\frac{1}{2}(c+dx)\right]^2\right]+ \right. \right. \\
& \left.\left.(5+2n)\operatorname{AppellF1}\left[\frac{3}{2},\frac{7}{2}+n,-\frac{1}{2}-n,\frac{5}{2},\tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left.\left.\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\Bigg)\Bigg)-
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{(-1 + \tan[\frac{1}{2}(c+dx)]^2)^2} 3 \sec[\frac{1}{2}(c+dx)]^2 \sec[c+dx]^{\frac{1}{2}+n} \\
& \left( \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right. \right. \\
& \quad \left. \left. (-1 + \tan[\frac{1}{2}(c+dx)]^2) \right) \right) / \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan[\frac{1}{2}(c+dx)]^2, \right. \right. \\
& \quad \left. \left. -\tan[\frac{1}{2}(c+dx)]^2\right] + \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] + (3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \right. \right. \\
& \quad \left. \left. -\frac{1}{2}-n, \frac{5}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right) \tan[\frac{1}{2}(c+dx)]^2 \right) - \\
& \left( 2 B \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] + \right. \\
& \quad \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] + \right. \\
& \quad \left. (5+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{2}+n, -\frac{1}{2}-n, \frac{5}{2}, \tan[\frac{1}{2}(c+dx)]^2, \right. \right. \\
& \quad \left. \left. -\tan[\frac{1}{2}(c+dx)]^2\right] \right) \tan[\frac{1}{2}(c+dx)]^2 \right) \right) - \\
& \frac{1}{(-1 + \tan[\frac{1}{2}(c+dx)]^2)^2} 6 \left(\frac{1}{2}+n\right) \sec[c+dx]^{\frac{3}{2}+n} \sin[c+dx] \tan[\frac{1}{2}(c+dx)] \\
& \left( \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right. \right. \\
& \quad \left. \left. (-1 + \tan[\frac{1}{2}(c+dx)]^2) \right) \right) / \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan[\frac{1}{2}(c+dx)]^2, \right. \right. \\
& \quad \left. \left. -\tan[\frac{1}{2}(c+dx)]^2\right] + \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] + (3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \right. \right. \\
& \quad \left. \left. -\frac{1}{2}-n, \frac{5}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right) \tan[\frac{1}{2}(c+dx)]^2 \right) - \\
& \left( 2 B \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] + \right. \\
& \quad \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan[\frac{1}{2}(c+dx)]^2, -\tan[\frac{1}{2}(c+dx)]^2\right] + \right. \\
& \quad \left. (5+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{2}+n, -\frac{1}{2}-n, \frac{5}{2}, \tan[\frac{1}{2}(c+dx)]^2, \right. \right. \\
& \quad \left. \left. -\tan[\frac{1}{2}(c+dx)]^2\right] \right) \tan[\frac{1}{2}(c+dx)]^2 \right) \right) -
\end{aligned}$$

$$\begin{aligned}
& \frac{1}{\left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]\right)^2} 6 \operatorname{Sec}[c+dx]^{\frac{1}{2}+n} \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left( \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \right. \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + (3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \right. \right. \\
& \quad \left. \left. -\frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + \\
& \left( (A-B) \left( -\frac{1}{3} \left( -\frac{1}{2}-n \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3} \left( \frac{3}{2}+n \right) \right. \right. \\
& \quad \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. (3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
& \left( 2B \left( -\frac{1}{3} \left( -\frac{1}{2}-n \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \frac{1}{3} \left( \frac{5}{2}+n \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{2}+n, -\frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. (5+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{2}+n, -\frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
& \left( (A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \right. \right. \right. \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right] + (3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \right. \\
& \quad \left. -\frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left( -\frac{1}{3} \left( -\frac{1}{2}-n \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. \frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{1}{3} \left( \frac{3}{2}+n \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (1+2n) \left( -\frac{3}{5} \left( \frac{1}{2}-n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, \frac{3}{2}-n, \frac{7}{2}, \right. \right. \right. \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + \\
& \quad \left. \frac{3}{5} \left( \frac{3}{2}+n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\
& \quad \left. (3+2n) \left( -\frac{3}{5} \left( -\frac{1}{2}-n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \left. \frac{3}{5} \left( \frac{5}{2}+n \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{2}+n, -\frac{1}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Bigg/ \\
& \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \\
& \quad \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + (3+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
& \left( 2 B \operatorname{AppellF1}\left[\frac{1}{2}, \frac{5}{2}+n, -\frac{1}{2}-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
& \quad \left( \left( (1+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \right. \\
& \quad \left. \left. (5+2n) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{7}{2}+n, -\frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right.
\end{aligned}$$



$$\begin{aligned}
& - \left( \left( 2 A \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{4} (1-2n), \frac{1}{4} (5-2n), \cos [c+dx]^2 \right] \right. \right. \\
& \quad \left. \left. (b \sec [c+dx])^n \sin [c+dx] \right) / \left( d (1-2n) \sqrt{\sec [c+dx]} \sqrt{\sin [c+dx]^2} \right) \right) + \\
& \left( 2 B \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{1}{4} (-1-2n), \frac{1}{4} (3-2n), \cos [c+dx]^2 \right] \sqrt{\sec [c+dx]} \right. \\
& \quad \left. (b \sec [c+dx])^n \sin [c+dx] \right) / \left( d (1+2n) \sqrt{\sin [c+dx]^2} \right)
\end{aligned}$$

Result (type 6, 5543 leaves):

$$\begin{aligned}
& \left( 2 \left( \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-\frac{1}{2}+n} \sec [c+dx]^{-n} (b \sec [c+dx])^n \right. \\
& \quad \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{\frac{1}{2}+n} \left( B \sec [c+dx]^{-\frac{1}{2}+n} + \frac{1}{2} A \sec [c+dx]^{\frac{1}{2}+n} + \right. \\
& \quad \cos [2 (c+dx)] \left( \frac{1}{2} A \sec [c+dx]^{\frac{1}{2}+n} - \frac{1}{2} B \sec [c+dx]^{\frac{3}{2}+n} \sin [c+dx] \right) + \frac{1}{2} B A \\
& \quad \sec [c+dx]^{\frac{1}{2}+n} \sin [2 (c+dx)] + \sec [c+dx] \left( B \sec [c+dx]^{\frac{1}{2}+n} \sin [c+dx]^2 + \sin [c+dx] \right. \\
& \quad \left. \left. \left( -\frac{1}{2} B A \sec [c+dx]^{\frac{1}{2}+n} + \frac{1}{2} A \sec [c+dx]^{\frac{1}{2}+n} \sin [2 (c+dx)] \right) \right) \right) \tan \left[ \frac{1}{2} (c+dx) \right] \\
& \quad \left( - \left( \left( 9 (A+B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \right. \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left( (-1+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2}+n, \frac{3}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. (3+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \left( 5 (A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \right. \right. \\
& \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) / \\
& \quad \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left( (-1+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{3}{2}+n, \frac{3}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. (3+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left. \right) / \left( 3 d \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \\
& \quad \left( -\frac{1}{3 \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2} 2 \left( \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{\frac{1}{2}+n} \right.
\end{aligned}$$

$$\begin{aligned}
& \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{\frac{1}{2}+n} \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \left( - \left( \left( 9 (A + B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \Bigg) + \\
& \quad \left( 5 (A - B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (3 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{2} + n, \right. \right. \\
& \quad \left. \left. \frac{1}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) + \\
& \frac{1}{3 \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)} \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{\frac{1}{2}+n} \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{\frac{1}{2}+n} \\
& \left( - \left( \left( 9 (A + B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. (3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) + \left( 5 (A - B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \right. \right. \\
& \quad \left. \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) / \\
& \quad \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (3 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) +
\end{aligned}$$



$$\begin{aligned}
& \frac{1}{3 \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)} 2 \left( -\frac{1}{2} + n \right) \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{-\frac{1}{2}+n} \\
& \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{\frac{1}{2}+n} \\
& \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \left( - \left( \left( 9 (A + B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. (3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) + \left( 5 (A - B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \right. \right. \\
& \quad \left. \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) / \\
& \quad \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (3 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) + \\
& \frac{1}{3 \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)} 2 \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{-\frac{1}{2}+n} \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{\frac{1}{2}+n} \\
& \tan \left[ \frac{1}{2} (c + d x) \right] \\
& \left( - \left( \left( 9 (A + B) \left( -\frac{1}{3} \left( \frac{1}{2} - n \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{3} \left( \frac{3}{2} + n \right) \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{3}{2}, \right. \right. \\
& \quad \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \right. \right. \\
& \quad \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{2} + n, \right. \\
& \quad \left. \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \right) +
\end{aligned}$$

$$\begin{aligned}
& \left( 5 (A - B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) / \\
& \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left. (3 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (c + d x) \right]^2 + \left( 5 (A - B) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right. \\
& \quad \left. - \frac{3}{5} \left( \frac{1}{2} - n \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{3}{5} \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) / \\
& \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + (3 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 + \\
& \left( 9 (A + B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{3}{2} + n, \frac{1}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left( \left( (-1 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. (3 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + 3 \left( -\frac{1}{3} \left( \frac{1}{2} - n \right) \right. \\
& \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{3}{2} + n, \frac{3}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{3} \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{2} + n, \frac{1}{2} - n, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) + \\
& \quad \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left( (-1 + 2n) \left( -\frac{3}{5} \left( \frac{3}{2} - n \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{3}{2} + n, \frac{5}{2} - n, \right. \right. \right. \\
& \quad \left. \left. \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \right. \right. \\
& \quad \left. \left. \frac{1}{2} (c + d x) \right] + \frac{3}{5} \left( \frac{3}{2} + n \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{2} + n, \frac{3}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
& -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
& (3+2n) \left( -\frac{3}{5} \left( \frac{1}{2} - n \right) \text{AppellF1}\left[\frac{5}{2}, \frac{5}{2}+n, \frac{3}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{3}{5} \left( \frac{5}{2} + n \right) \text{AppellF1}\left[\frac{5}{2}, \frac{7}{2}+n, \frac{1}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
& \left( 3 \text{AppellF1}\left[\frac{1}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \\
& \quad \left( (-1+2n) \text{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{3}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \\
& \quad \left. (3+2n) \text{AppellF1}\left[\frac{3}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
& \left( 5(A-B) \text{AppellF1}\left[\frac{3}{2}, \frac{3}{2}+n, \frac{1}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left( \left( (-1+2n) \text{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, \frac{3}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \right. \\
& \quad \left. \left. (3+2n) \text{AppellF1}\left[\frac{5}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 5 \left( -\frac{3}{5} \left( \frac{1}{2} - n \right) \right. \right. \\
& \quad \left. \left. \text{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, \frac{3}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5} \left( \frac{3}{2} + n \right) \text{AppellF1}\left[\frac{5}{2}, \frac{5}{2}+n, \frac{1}{2}-n, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (-1+2n) \left( -\frac{5}{7} \left( \frac{3}{2} - n \right) \text{AppellF1}\left[\frac{7}{2}, \frac{3}{2}+n, \frac{5}{2}-n, \right. \right. \right. \\
& \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right. \right. \\
& \quad \left. \left. \frac{1}{2}(c+dx) \right) + \frac{5}{7} \left( \frac{3}{2} + n \right) \text{AppellF1}\left[\frac{7}{2}, \frac{5}{2}+n, \frac{3}{2}-n, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
& (3+2n) \left( -\frac{5}{7} \left( \frac{1}{2} - n \right) \text{AppellF1}\left[\frac{7}{2}, \frac{5}{2}+n, \frac{3}{2}-n, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right.
\end{aligned}$$





$$\begin{aligned}
& \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left( (-5+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad (-1+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) \Big) / \\
& \left( 3d \left( \frac{2}{3} \left( \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-\frac{3}{2}+n} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{\frac{1}{2}+n} \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
& \quad \left. \left( - \left( \left( 9(A+B) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) / \right. \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left( (-5+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \quad (-1+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) + \left( 5(A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \right. \right. \\
& \quad \quad \left. \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) / \\
& \quad \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left( (-5+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \quad (-1+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) + \\
& \quad \frac{1}{3} \left( \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-\frac{3}{2}+n} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{\frac{1}{2}+n} \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \quad \left( - \left( \left( 9(A+B) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) / \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left( (-5+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \quad (-1+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) + \left( 5(A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \right. \right. \\
& \quad \quad \left. \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) /
\end{aligned}$$

$$\begin{aligned}
& \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, \frac{5}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-5 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2} + n, \frac{7}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad (-1 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2} + n, \frac{5}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) + \\
& \frac{2}{3} \left( -\frac{5}{2} + n \right) \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{-\frac{5}{2} + n} \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{\frac{1}{2} + n} \\
& \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \\
& \left( - \left( \left( 9 (A + B) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} + n, \frac{5}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) / \right. \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} + n, \frac{5}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-5 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, \frac{7}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad (-1 + 2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} + n, \frac{5}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) + \left( 5 (A - B) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, \right. \right. \\
& \quad \left. \frac{5}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) / \\
& \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, \frac{5}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad \left( (-5 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2} + n, \frac{7}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad (-1 + 2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2} + n, \frac{5}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Bigg) + \\
& \frac{2}{3} \left( \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right)^{-\frac{5}{2} + n} \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{\frac{1}{2} + n} \tan \left[ \frac{1}{2} (c + d x) \right] \\
& \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \\
& \left( - \left( \left( 9 (A + B) \left( -\frac{1}{3} \left( \frac{5}{2} - n \right) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, \frac{7}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \right. \right. \right. \right. \right. \right. \\
& \quad \left. \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] + \frac{1}{3} \right. \right. \right. \\
& \quad \left( -\frac{1}{2} + n \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} + n, \frac{5}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \tan \left[ \frac{1}{2} (c + d x) \right] \right) \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left( (-5+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left. (-1+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \\
& \left( 5 (A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) / \\
& \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left( (-5+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left. (-1+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \left( 5 (A-B) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
& \quad \left( -\frac{3}{5} \left( \frac{5}{2}-n \right) \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{3}{5} \left( -\frac{1}{2}+n \right) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{7}{2}, \right. \right. \\
& \quad \quad \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Bigg) / \\
& \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left( (-5+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \quad \left. (-1+2n) \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \\
& \left( 9 (A+B) \operatorname{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left( \left( (-5+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad \quad \left. (-1+2n) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \quad \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 3 \left( -\frac{1}{3} \left( \frac{5}{2}-n \right) \right. \\
& \quad \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{3} \left( -\frac{1}{2}+n \right) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \right. \right.
\end{aligned}$$



$$\begin{aligned}
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Bigg) + \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (-5+2n) \left( -\frac{3}{5} \left( \frac{7}{2} - n \right) \text{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, \frac{9}{2}-n, \right. \right. \right. \\
& \quad \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \left. (c+dx) \right] + \frac{3}{5} \left( -\frac{1}{2}+n \right) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, \frac{7}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\
& \quad \left( -1+2n \right) \left( -\frac{3}{5} \left( \frac{5}{2} - n \right) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, \frac{7}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \left. \frac{3}{5} \left( \frac{1}{2}+n \right) \text{AppellF1}\left[\frac{5}{2}, \frac{3}{2}+n, \frac{5}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg) \Bigg) / \\
& \left( 3 \text{AppellF1}\left[\frac{1}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \\
& \quad \left( (-5+2n) \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \\
& \quad \left. (-1+2n) \text{AppellF1}\left[\frac{3}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) - \\
& \left( 5 (A-B) \text{AppellF1}\left[\frac{3}{2}, -\frac{1}{2}+n, \frac{5}{2}-n, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \quad \left( \left( (-5+2n) \text{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \right. \\
& \quad \left. (-1+2n) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 5 \left( -\frac{3}{5} \left( \frac{5}{2} - n \right) \right. \right. \\
& \quad \left. \left. \text{AppellF1}\left[\frac{5}{2}, -\frac{1}{2}+n, \frac{7}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{3}{5} \left( -\frac{1}{2}+n \right) \text{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( (-5+2n) \left( -\frac{5}{7} \left( \frac{7}{2} - n \right) \text{AppellF1}\left[\frac{7}{2}, -\frac{1}{2}+n, \frac{9}{2}-n, \right. \right. \right. \\
& \quad \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \right.
\end{aligned}$$

$$\begin{aligned}
& (c+dx) + \frac{5}{7} \left( -\frac{1}{2} + n \right) \text{AppellF1} \left[ \frac{7}{2}, \frac{1}{2} + n, \frac{7}{2} - n, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \\
& (-1+2n) \left( -\frac{5}{7} \left( \frac{5}{2} - n \right) \text{AppellF1} \left[ \frac{7}{2}, \frac{1}{2} + n, \frac{7}{2} - n, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
& \left. \frac{5}{7} \left( \frac{1}{2} + n \right) \text{AppellF1} \left[ \frac{7}{2}, \frac{3}{2} + n, \frac{5}{2} - n, \frac{9}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Bigg) \Bigg) / \\
& \left( 5 \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, \frac{5}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \left( (-5+2n) \text{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2} + n, \frac{7}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \left. (-1+2n) \text{AppellF1} \left[ \frac{5}{2}, \frac{1}{2} + n, \frac{5}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) + \\
& \frac{2}{3} \left( \frac{1}{2} + n \right) \left( \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{-\frac{5}{2}+n} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{-\frac{1}{2}+n} \\
& \tan \left[ \frac{1}{2} (c+dx) \right] \\
& \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \left( - \left( \left( 9(A+B) \text{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} + n, \frac{5}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right) / \right. \\
& \left( 3 \text{AppellF1} \left[ \frac{1}{2}, -\frac{1}{2} + n, \frac{5}{2} - n, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \left( (-5+2n) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, \frac{7}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \left. (-1+2n) \text{AppellF1} \left[ \frac{3}{2}, \frac{1}{2} + n, \frac{5}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) \Bigg) + \\
& \left( 5(A-B) \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, \frac{5}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) / \\
& \left( 5 \text{AppellF1} \left[ \frac{3}{2}, -\frac{1}{2} + n, \frac{5}{2} - n, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \left( (-5+2n) \text{AppellF1} \left[ \frac{5}{2}, -\frac{1}{2} + n, \frac{7}{2} - n, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right.
\end{aligned}$$

$$\begin{aligned} & (-1+2n) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{2}+n, \frac{5}{2}-n, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\ & \quad \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\ & \left(-\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\ & \quad \left. \sec[c+dx] \tan[c+dx] \right) \Bigg) \Bigg) \end{aligned}$$

**Problem 44: Result more than twice size of optimal antiderivative.**

$$\int \sec[c+dx]^3 (a+a \sec[c+dx]) (A+B \sec[c+dx]) dx$$

Optimal (type 3, 106 leaves, 6 steps):

$$\begin{aligned} & \frac{a(4A+3B) \operatorname{ArcTanh}[\sin[c+dx]]}{8d} + \frac{a(A+B) \tan[c+dx]}{d} + \\ & \frac{a(4A+3B) \sec[c+dx] \tan[c+dx]}{8d} + \frac{aB \sec[c+dx]^3 \tan[c+dx]}{4d} + \frac{a(A+B) \tan[c+dx]^3}{3d} \end{aligned}$$

Result (type 3, 403 leaves):

$$\begin{aligned} & -\frac{aA \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} - \frac{3aB \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\ & \frac{aA \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{2d} + \frac{3aB \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{8d} + \\ & \frac{aB}{16d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4} + \frac{aA}{4d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \\ & \frac{3aB}{16d \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{aB}{16d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4} - \\ & \frac{aA}{4d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} - \frac{3aB}{16d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \\ & \frac{2aA \tan[c+dx]}{3d} + \frac{2aB \tan[c+dx]}{3d} + \frac{aA \sec[c+dx]^2 \tan[c+dx]}{3d} + \frac{aB \sec[c+dx]^2 \tan[c+dx]}{3d} \end{aligned}$$

**Problem 46: Result more than twice size of optimal antiderivative.**

$$\int \sec[c+dx] (a+a \sec[c+dx]) (A+B \sec[c+dx]) dx$$

Optimal (type 3, 56 leaves, 5 steps):

$$\frac{a(2A+B) \operatorname{ArcTanh}[\sin[c+dx]]}{2d} + \frac{a(A+B) \tan[c+dx]}{d} + \frac{aB \sec[c+dx] \tan[c+dx]}{2d}$$

Result (type 3, 154 leaves):

$$\frac{1}{4d} a \left( -2 (2A+B) \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c+dx) \right] - \sin \left[ \frac{1}{2} (c+dx) \right] \right] + \right. \\ 4A \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c+dx) \right] + \sin \left[ \frac{1}{2} (c+dx) \right] \right] + \\ 2B \operatorname{Log} \left[ \cos \left[ \frac{1}{2} (c+dx) \right] + \sin \left[ \frac{1}{2} (c+dx) \right] \right] + \frac{B}{\left( \cos \left[ \frac{1}{2} (c+dx) \right] - \sin \left[ \frac{1}{2} (c+dx) \right] \right)^2} - \\ \left. \frac{B}{\left( \cos \left[ \frac{1}{2} (c+dx) \right] + \sin \left[ \frac{1}{2} (c+dx) \right] \right)^2} + 4(A+B) \tan [c+dx] \right)$$

Problem 47: Result more than twice size of optimal antiderivative.

$$\int (a + a \sec [c+dx]) (A+B \sec [c+dx]) dx$$

Optimal (type 3, 32 leaves, 4 steps):

$$aAx + \frac{a(A+B) \operatorname{ArcTanh} [\sin [c+dx]]}{d} + \frac{aB \tan [c+dx]}{d}$$

Result (type 3, 159 leaves):

$$aAx - \frac{aA \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} - \frac{aB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \\ \frac{aA \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \frac{aB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \frac{aB \tan [c+dx]}{d}$$

Problem 48: Result more than twice size of optimal antiderivative.

$$\int \cos [c+dx] (a + a \sec [c+dx]) (A+B \sec [c+dx]) dx$$

Optimal (type 3, 32 leaves, 3 steps):

$$a(A+B)x + \frac{aB \operatorname{ArcTanh} [\sin [c+dx]]}{d} + \frac{aA \sin [c+dx]}{d}$$

Result (type 3, 104 leaves):

$$aAx + aBx - \frac{aB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \\ \frac{aB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \frac{aA \cos [dx] \sin [c]}{d} + \frac{aA \cos [c] \sin [dx]}{d}$$

### Problem 55: Result more than twice size of optimal antiderivative.

$$\int \sec[c + d x] (a + a \sec[c + d x])^2 (A + B \sec[c + d x]) dx$$

Optimal (type 3, 103 leaves, 6 steps):

$$\frac{a^2 (3 A + 2 B) \operatorname{ArcTanh}[\sin[c + d x]]}{2 d} + \frac{2 a^2 (3 A + 2 B) \tan[c + d x]}{3 d} +$$

$$\frac{a^2 (3 A + 2 B) \sec[c + d x] \tan[c + d x]}{6 d} + \frac{B (a + a \sec[c + d x])^2 \tan[c + d x]}{3 d}$$

Result (type 3, 993 leaves):

$$\begin{aligned}
 & \left( (-3A - 2B) \cos[c + dx]^3 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \\
 & \quad \left. (a + a \sec[c + dx])^2 (A + B \sec[c + dx]) \right) / (8d (B + A \cos[c + dx])) + \\
 & \left( (3A + 2B) \cos[c + dx]^3 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \right. \\
 & \quad \left. (a + a \sec[c + dx])^2 (A + B \sec[c + dx]) \right) / (8d (B + A \cos[c + dx])) + \\
 & \left( B \cos[c + dx]^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx]) \sin\left[\frac{dx}{2}\right] \right) / \\
 & \left( 24d (B + A \cos[c + dx]) \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^3 \right) + \\
 & \left( \cos[c + dx]^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx]) \right. \\
 & \quad \left. \left( 3A \cos\left[\frac{c}{2}\right] + 7B \cos\left[\frac{c}{2}\right] - 3A \sin\left[\frac{c}{2}\right] - 5B \sin\left[\frac{c}{2}\right] \right) \right) / \\
 & \left( 48d (B + A \cos[c + dx]) \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
 & \left( \cos[c + dx]^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 \right. \\
 & \quad \left. (A + B \sec[c + dx]) \left( 6A \sin\left[\frac{dx}{2}\right] + 5B \sin\left[\frac{dx}{2}\right] \right) \right) / \\
 & \left( 12d (B + A \cos[c + dx]) \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right) + \\
 & \left( B \cos[c + dx]^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx]) \sin\left[\frac{dx}{2}\right] \right) / \\
 & \left( 24d (B + A \cos[c + dx]) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^3 \right) + \\
 & \left( \cos[c + dx]^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 (A + B \sec[c + dx]) \right. \\
 & \quad \left. \left( -3A \cos\left[\frac{c}{2}\right] - 7B \cos\left[\frac{c}{2}\right] - 3A \sin\left[\frac{c}{2}\right] - 5B \sin\left[\frac{c}{2}\right] \right) \right) / \\
 & \left( 48d (B + A \cos[c + dx]) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right)^2 \right) + \\
 & \left( \cos[c + dx]^3 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a + a \sec[c + dx])^2 \right. \\
 & \quad \left. (A + B \sec[c + dx]) \left( 6A \sin\left[\frac{dx}{2}\right] + 5B \sin\left[\frac{dx}{2}\right] \right) \right) / \\
 & \left( 12d (B + A \cos[c + dx]) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right] \right) \right)
 \end{aligned}$$

**Problem 56: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sec[c + dx])^2 (A + B \sec[c + dx]) dx$$

Optimal (type 3, 82 leaves, 5 steps):

$$a^2 A x + \frac{a^2 (4 A + 3 B) \operatorname{ArcTanh}[\sin[c + d x]]}{2 d} +$$

$$\frac{a^2 (2 A + 3 B) \tan[c + d x]}{2 d} + \frac{B (a^2 + a^2 \sec[c + d x]) \tan[c + d x]}{2 d}$$

Result (type 3, 307 leaves):

$$\frac{1}{16 (B + A \cos[c + d x])} a^2 \cos[c + d x]^3 \sec\left[\frac{1}{2} (c + d x)\right]^4 (1 + \sec[c + d x])^2$$

$$(A + B \sec[c + d x]) \left( 4 A x - \frac{2 (4 A + 3 B) \log\left[\cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right]\right]}{d} + \right.$$

$$\frac{2 (4 A + 3 B) \log\left[\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right]}{d} +$$

$$\frac{B}{d \left(\cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right]\right)^2} +$$

$$\frac{4 (A + 2 B) \sin\left[\frac{d x}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right]\right)} -$$

$$\frac{B}{d \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)^2} +$$

$$\left. \frac{4 (A + 2 B) \sin\left[\frac{d x}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right)} \right)$$

Problem 57: Result more than twice size of optimal antiderivative.

$$\int \cos[c + d x] (a + a \sec[c + d x])^2 (A + B \sec[c + d x]) dx$$

Optimal (type 3, 73 leaves, 4 steps):

$$a^2 (2 A + B) x + \frac{a^2 (A + 2 B) \operatorname{ArcTanh}[\sin[c + d x]]}{d} +$$

$$\frac{a^2 (A - B) \sin[c + d x]}{d} + \frac{B (a^2 + a^2 \sec[c + d x]) \sin[c + d x]}{d}$$

Result (type 3, 258 leaves):

$$\left( a^2 \cos[c+dx]^3 \sec\left[\frac{1}{2}(c+dx)\right]^4 (1+\sec[c+dx])^2 \right. \\ \left. (A+B \sec[c+dx]) \left( (2A+B)x - \frac{(A+2B) \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right]}{d} + \right. \right. \\ \left. \frac{(A+2B) \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right]}{d} + \frac{A \cos[dx] \sin[c]}{d} + \right. \\ \left. \frac{A \cos[c] \sin[dx]}{d} + \frac{B \sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)} + \right. \\ \left. \left. \frac{B \sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)} \right) \right) / (4(B+A \cos[c+dx]))$$

**Problem 64: Result more than twice size of optimal antiderivative.**

$$\int \sec[c+dx] (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) dx$$

Optimal (type 3, 125 leaves, 10 steps):

$$\frac{5 a^3 (4 A+3 B) \operatorname{ArcTanh}[\sin[c+dx]]}{8 d} + \\ \frac{a^3 (4 A+3 B) \tan[c+dx]}{d} + \frac{3 a^3 (4 A+3 B) \sec[c+dx] \tan[c+dx]}{8 d} + \\ \frac{B (a+a \sec[c+dx])^3 \tan[c+dx]}{4 d} + \frac{a^3 (4 A+3 B) \tan[c+dx]^3}{12 d}$$

Result (type 3, 273 leaves):

$$-\frac{1}{1536 d} a^3 (1+\cos[c+dx])^3 \sec\left[\frac{1}{2}(c+dx)\right]^6 \sec[c+dx]^4 \left( 120 (4 A+3 B) \cos[c+dx]^4 \right. \\ \left( \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] - \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] \right) - \\ \sec[c] (-24 (11 A+9 B) \sin[c] + (36 A+69 B) \sin[dx] + 36 A \sin[2 c+dx] + \\ 69 B \sin[2 c+dx] + 280 A \sin[c+2 dx] + 264 B \sin[c+2 dx] - 72 A \sin[3 c+2 dx] - \\ 24 B \sin[3 c+2 dx] + 36 A \sin[2 c+3 dx] + 45 B \sin[2 c+3 dx] + 36 A \sin[4 c+3 dx] + \\ 45 B \sin[4 c+3 dx] + 88 A \sin[3 c+4 dx] + 72 B \sin[3 c+4 dx]) \right)$$

**Problem 65: Result more than twice size of optimal antiderivative.**

$$\int (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) dx$$

Optimal (type 3, 111 leaves, 6 steps):



$$\begin{aligned}
 & a^3 A x + \frac{a^3 (7 A + 5 B) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} + \frac{5 a^3 (A + B) \operatorname{Tan}[c + d x]}{2 d} + \\
 & \frac{a B (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{3 d} + \frac{(3 A + 5 B) (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Tan}[c + d x]}{6 d}
 \end{aligned}$$

Result (type 3, 1056 leaves):

$$\begin{aligned}
& \left( A x \cos [c+d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \left( 8 (B+A \cos [c+d x]) \right) + \\
& \left( (-7 A-5 B) \cos [c+d x]^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \right. \\
& \quad \left. (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \left( 16 d (B+A \cos [c+d x]) \right) + \\
& \left( (7 A+5 B) \cos [c+d x]^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \right. \\
& \quad \left. (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \left( 16 d (B+A \cos [c+d x]) \right) + \\
& \left( B \cos [c+d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \sin \left[ \frac{d x}{2} \right] \right) / \\
& \left( 48 d (B+A \cos [c+d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
& \left( \cos [c+d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right. \\
& \quad \left. \left( 3 A \cos \left[ \frac{c}{2} \right] + 10 B \cos \left[ \frac{c}{2} \right] - 3 A \sin \left[ \frac{c}{2} \right] - 8 B \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 96 d (B+A \cos [c+d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
& \left( \cos [c+d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 \right. \\
& \quad \left. (A+B \sec [c+d x]) \left( 9 A \sin \left[ \frac{d x}{2} \right] + 11 B \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
& \left( 24 d (B+A \cos [c+d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right) + \\
& \left( B \cos [c+d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \sin \left[ \frac{d x}{2} \right] \right) / \\
& \left( 48 d (B+A \cos [c+d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
& \left( \cos [c+d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right. \\
& \quad \left. \left( -3 A \cos \left[ \frac{c}{2} \right] - 10 B \cos \left[ \frac{c}{2} \right] - 3 A \sin \left[ \frac{c}{2} \right] - 8 B \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 96 d (B+A \cos [c+d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
& \left( \cos [c+d x]^4 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (a+a \sec [c+d x])^3 \right. \\
& \quad \left. (A+B \sec [c+d x]) \left( 9 A \sin \left[ \frac{d x}{2} \right] + 11 B \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
& \left( 24 d (B+A \cos [c+d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right)
\end{aligned}$$

### Problem 66: Result more than twice size of optimal antiderivative.

$$\int \cos[c + dx] (a + a \sec[c + dx])^3 (A + B \sec[c + dx]) dx$$

Optimal (type 3, 108 leaves, 5 steps):

$$\begin{aligned} & a^3 (3A + B) x + \frac{a^3 (6A + 7B) \operatorname{ArcTanh}[\sin[c + dx]]}{2d} - \frac{5a^3 B \sin[c + dx]}{2d} + \\ & \frac{aB (a + a \sec[c + dx])^2 \sin[c + dx]}{2d} + \frac{(A + 2B) (a^3 + a^3 \sec[c + dx]) \sin[c + dx]}{d} \end{aligned}$$

Result (type 3, 335 leaves):

$$\begin{aligned} & \frac{1}{32 (B + A \cos[c + dx])} a^3 \cos[c + dx]^4 \sec\left[\frac{1}{2}(c + dx)\right]^6 (1 + \sec[c + dx])^3 \\ & (A + B \sec[c + dx]) \left( 4 (3A + B) x - \frac{2 (6A + 7B) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right]}{d} + \right. \\ & \frac{2 (6A + 7B) \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right]}{d} + \frac{4A \cos[dx] \sin[c]}{d} + \\ & \frac{4A \cos[c] \sin[dx]}{d} + \frac{B}{d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} + \\ & \frac{4 (A + 3B) \sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)} - \\ & \frac{B}{d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} + \\ & \left. \frac{4 (A + 3B) \sin\left[\frac{dx}{2}\right]}{d \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)} \right) \end{aligned}$$

### Problem 67: Result more than twice size of optimal antiderivative.

$$\int \cos[c + dx]^2 (a + a \sec[c + dx])^3 (A + B \sec[c + dx]) dx$$

Optimal (type 3, 117 leaves, 5 steps):

$$\begin{aligned} & \frac{1}{2} a^3 (7A + 6B) x + \frac{a^3 (A + 3B) \operatorname{ArcTanh}[\sin[c + dx]]}{d} + \frac{5a^3 A \sin[c + dx]}{2d} + \\ & \frac{aA \cos[c + dx] (a + a \sec[c + dx])^2 \sin[c + dx]}{2d} - \frac{(A - 2B) (a^3 + a^3 \sec[c + dx]) \sin[c + dx]}{2d} \end{aligned}$$

Result (type 3, 802 leaves):

$$\begin{aligned}
& \left( (7A+6B) x \cos[c+dx]^4 \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \right) / \\
& \left( 16 (B+A \cos[c+dx]) \right) + \\
& \left( (-A-3B) \cos[c+dx]^4 \log\left[\cos\left[\frac{c}{2}+\frac{dx}{2}\right] - \sin\left[\frac{c}{2}+\frac{dx}{2}\right]\right] \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^6 \right. \\
& \quad \left. (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \right) / (8d (B+A \cos[c+dx])) + \\
& \left( (A+3B) \cos[c+dx]^4 \log\left[\cos\left[\frac{c}{2}+\frac{dx}{2}\right] + \sin\left[\frac{c}{2}+\frac{dx}{2}\right]\right] \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^6 \right. \\
& \quad \left. (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \right) / (8d (B+A \cos[c+dx])) + \\
& \left( (3A+B) \cos[dx] \cos[c+dx]^4 \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \sin[c] \right) / \\
& \left( 8d (B+A \cos[c+dx]) \right) + \\
& \left( A \cos[2dx] \cos[c+dx]^4 \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \sin[2c] \right) / \\
& \left( 32d (B+A \cos[c+dx]) \right) + \\
& \left( (3A+B) \cos[c] \cos[c+dx]^4 \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \sin[dx] \right) / \\
& \left( 8d (B+A \cos[c+dx]) \right) + \\
& \left( A \cos[2c] \cos[c+dx]^4 \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \sin[2dx] \right) / \\
& \left( 32d (B+A \cos[c+dx]) \right) + \\
& \left( B \cos[c+dx]^4 \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \sin\left[\frac{dx}{2}\right] \right) / \\
& \left( 8d (B+A \cos[c+dx]) \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}+\frac{dx}{2}\right] - \sin\left[\frac{c}{2}+\frac{dx}{2}\right] \right) \right) + \\
& \left( B \cos[c+dx]^4 \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \sin\left[\frac{dx}{2}\right] \right) / \\
& \left( 8d (B+A \cos[c+dx]) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}+\frac{dx}{2}\right] + \sin\left[\frac{c}{2}+\frac{dx}{2}\right] \right) \right)
\end{aligned}$$

**Problem 74: Result more than twice size of optimal antiderivative.**

$$\int (a+a \sec[c+dx])^4 (A+B \sec[c+dx]) dx$$

Optimal (type 3, 151 leaves, 7 steps):

$$\begin{aligned}
& a^4 A x + \frac{a^4 (48A+35B) \operatorname{ArcTanh}\left[\sin[c+dx]\right]}{8d} + \\
& \frac{5a^4 (8A+7B) \tan[c+dx]}{8d} + \frac{aB (a+a \sec[c+dx])^3 \tan[c+dx]}{4d} + \\
& \frac{(4A+7B) (a^2+a^2 \sec[c+dx])^2 \tan[c+dx]}{12d} + \frac{(32A+35B) (a^4+a^4 \sec[c+dx]) \tan[c+dx]}{24d}
\end{aligned}$$

Result (type 3, 326 leaves):

$$\frac{1}{3072 d} a^4 \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^8 (1+\operatorname{Sec}[c+d x])^4$$

$$\left(-24(48 A+35 B) \cos [c+d x]^4\left(\operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right]-\right.\right.$$

$$\left.\operatorname{Log}\left[\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right]\right)+\operatorname{Sec}[c]$$

$$(72 A d x \cos [c]+48 A d x \cos [c+2 d x]+48 A d x \cos [3 c+2 d x]+12 A d x \cos [3 c+4 d x]+$$

$$12 A d x \cos [5 c+4 d x]-480 A \sin [c]-480 B \sin [c]+48 A \sin [d x]+105 B \sin [d x]+$$

$$48 A \sin [2 c+d x]+105 B \sin [2 c+d x]+496 A \sin [c+2 d x]+544 B \sin [c+2 d x]-$$

$$144 A \sin [3 c+2 d x]-96 B \sin [3 c+2 d x]+48 A \sin [2 c+3 d x]+81 B \sin [2 c+3 d x]+$$

$$48 A \sin [4 c+3 d x]+81 B \sin [4 c+3 d x]+160 A \sin [3 c+4 d x]+160 B \sin [3 c+4 d x])$$

**Problem 75: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x](a+a \operatorname{Sec}[c+d x])^4(A+B \operatorname{Sec}[c+d x]) d x$$

Optimal (type 3, 151 leaves, 6 steps):

$$a^4(4 A+B) x+\frac{a^4(13 A+12 B) \operatorname{ArcTanh}[\sin [c+d x]]}{2 d}-$$

$$\frac{5 a^4(A+2 B) \sin [c+d x]}{2 d}+\frac{a B(a+a \operatorname{Sec}[c+d x])^3 \sin [c+d x]}{3 d}+$$

$$\frac{(A+2 B)\left(a^2+a^2 \operatorname{Sec}[c+d x]\right)^2 \sin [c+d x]}{2 d}+\frac{(9 A+11 B)\left(a^4+a^4 \operatorname{Sec}[c+d x]\right) \sin [c+d x]}{3 d}$$

Result (type 3, 1202 leaves):

$$\left((4 A+B) x \cos [c+d x]^5 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8(a+a \operatorname{Sec}[c+d x])^4(A+B \operatorname{Sec}[c+d x])\right) /$$

$$(16(B+A \cos [c+d x]))+(-13 A-12 B) \cos [c+d x]^5 \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]-\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8$$

$$(a+a \operatorname{Sec}[c+d x])^4(A+B \operatorname{Sec}[c+d x])\right) / (32 d(B+A \cos [c+d x]))+((13 A+12 B) \cos [c+d x]^5 \operatorname{Log}\left[\cos \left[\frac{c}{2}+\frac{d x}{2}\right]+\sin \left[\frac{c}{2}+\frac{d x}{2}\right]\right] \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8$$

$$(a+a \operatorname{Sec}[c+d x])^4(A+B \operatorname{Sec}[c+d x])\right) / (32 d(B+A \cos [c+d x]))+((A \cos [d x] \cos [c+d x]^5 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8(a+a \operatorname{Sec}[c+d x])^4(A+B \operatorname{Sec}[c+d x]) \sin [c]) /$$

$$(16 d(B+A \cos [c+d x]))+(A \cos [c] \cos [c+d x]^5 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8(a+a \operatorname{Sec}[c+d x])^4(A+B \operatorname{Sec}[c+d x]) \sin [d x]) /$$

$$(16 d(B+A \cos [c+d x]))+(B \cos [c+d x]^5 \operatorname{Sec}\left[\frac{c}{2}+\frac{d x}{2}\right]^8(a+a \operatorname{Sec}[c+d x])^4(A+B \operatorname{Sec}[c+d x]) \sin \left[\frac{d x}{2}\right]) /$$

$$\begin{aligned}
& \left( 96 d (B + A \cos [c + d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
& \left( \cos [c + d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x]) \right. \\
& \quad \left. \left( 3 A \cos \left[ \frac{c}{2} \right] + 13 B \cos \left[ \frac{c}{2} \right] - 3 A \sin \left[ \frac{c}{2} \right] - 11 B \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 192 d (B + A \cos [c + d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
& \left( \cos [c + d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 \right. \\
& \quad \left. (A + B \sec [c + d x]) \left( 3 A \sin \left[ \frac{d x}{2} \right] + 5 B \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
& \left( 12 d (B + A \cos [c + d x]) \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] - \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right) + \\
& \left( B \cos [c + d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x]) \sin \left[ \frac{d x}{2} \right] \right) / \\
& \left( 96 d (B + A \cos [c + d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^3 \right) + \\
& \left( \cos [c + d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 (A + B \sec [c + d x]) \right. \\
& \quad \left. \left( -3 A \cos \left[ \frac{c}{2} \right] - 13 B \cos \left[ \frac{c}{2} \right] - 3 A \sin \left[ \frac{c}{2} \right] - 11 B \sin \left[ \frac{c}{2} \right] \right) \right) / \\
& \left( 192 d (B + A \cos [c + d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right)^2 \right) + \\
& \left( \cos [c + d x]^5 \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^8 (a + a \sec [c + d x])^4 \right. \\
& \quad \left. (A + B \sec [c + d x]) \left( 3 A \sin \left[ \frac{d x}{2} \right] + 5 B \sin \left[ \frac{d x}{2} \right] \right) \right) / \\
& \left( 12 d (B + A \cos [c + d x]) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right] + \sin \left[ \frac{c}{2} + \frac{d x}{2} \right] \right) \right)
\end{aligned}$$

**Problem 76: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^2 (a + a \sec [c + d x])^4 (A + B \sec [c + d x]) dx$$

Optimal (type 3, 160 leaves, 6 steps):

$$\begin{aligned}
& \frac{1}{2} a^4 (13 A + 8 B) x + \frac{a^4 (8 A + 13 B) \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \\
& \frac{5 a^4 (A - B) \sin [c + d x]}{2 d} + \frac{a A \cos [c + d x] (a + a \sec [c + d x])^3 \sin [c + d x]}{2 d} - \\
& \frac{(A - B) (a^2 + a^2 \sec [c + d x])^2 \sin [c + d x]}{2 d} + \frac{(A + 6 B) (a^4 + a^4 \sec [c + d x]) \sin [c + d x]}{2 d}
\end{aligned}$$

Result (type 3, 1018 leaves):

$$\begin{aligned}
& \left( (13A + 8B) x \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx]) \right) / \\
& \quad (32 (B + A \cos[c + dx])) + \\
& \left( (-8A - 13B) \cos[c + dx]^5 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \right. \\
& \quad \left. (a + a \sec[c + dx])^4 (A + B \sec[c + dx]) \right) / (32d (B + A \cos[c + dx])) + \\
& \left( (8A + 13B) \cos[c + dx]^5 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \right. \\
& \quad \left. (a + a \sec[c + dx])^4 (A + B \sec[c + dx]) \right) / (32d (B + A \cos[c + dx])) + \\
& \left( (4A + B) \cos[dx] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx]) \sin[c] \right) / \\
& \quad (16d (B + A \cos[c + dx])) + \\
& \left( A \cos[2dx] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx]) \sin[2c] \right) / \\
& \quad (64d (B + A \cos[c + dx])) + \\
& \left( (4A + B) \cos[c] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx]) \sin[dx] \right) / \\
& \quad (16d (B + A \cos[c + dx])) + \\
& \left( A \cos[2c] \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx]) \sin[2dx] \right) / \\
& \quad (64d (B + A \cos[c + dx])) + \\
& \frac{B \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx])}{64d (B + A \cos[c + dx]) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2} + \left(\cos[c + dx]^5 \right. \\
& \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx]) \left(A \sin\left[\frac{dx}{2}\right] + 4B \sin\left[\frac{dx}{2}\right]\right) \right) / \\
& \left( 16d (B + A \cos[c + dx]) \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right) \right) - \\
& \frac{B \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 (A + B \sec[c + dx])}{64d (B + A \cos[c + dx]) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2} + \\
& \left( \cos[c + dx]^5 \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^8 (a + a \sec[c + dx])^4 \right. \\
& \quad \left. (A + B \sec[c + dx]) \left(A \sin\left[\frac{dx}{2}\right] + 4B \sin\left[\frac{dx}{2}\right]\right) \right) / \\
& \left( 16d (B + A \cos[c + dx]) \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right) \right)
\end{aligned}$$

**Problem 77: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx]^3 (a + a \sec[c + dx])^4 (A + B \sec[c + dx]) dx$$

Optimal (type 3, 165 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{2} a^4 (12 A + 13 B) x + \frac{a^4 (A + 4 B) \operatorname{ArcTanh}[\sin[c + d x]]}{d} + \\ & \frac{5 a^4 (2 A + B) \sin[c + d x]}{2 d} + \frac{a A \cos[c + d x]^2 (a + a \sec[c + d x])^3 \sin[c + d x]}{3 d} + \\ & \frac{(2 A + B) \cos[c + d x] (a^2 + a^2 \sec[c + d x])^2 \sin[c + d x]}{2 d} - \\ & \frac{(8 A - 3 B) (a^4 + a^4 \sec[c + d x]) \sin[c + d x]}{6 d} \end{aligned}$$

Result (type 3, 342 leaves):

$$\begin{aligned} & \frac{1}{192 (B + A \cos[c + d x])} a^4 \cos[c + d x]^5 \sec\left[\frac{1}{2} (c + d x)\right]^8 (1 + \sec[c + d x])^4 \\ & (A + B \sec[c + d x]) \left( 72 A x + 78 B x - \frac{12 (A + 4 B) \log\left[\cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right]\right]}{d} + \right. \\ & \frac{12 (A + 4 B) \log\left[\cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right]\right]}{d} + \frac{3 (27 A + 16 B) \cos[d x] \sin[c]}{d} + \\ & \frac{3 (4 A + B) \cos[2 d x] \sin[2 c]}{d} + \frac{A \cos[3 d x] \sin[3 c]}{d} + \\ & \frac{3 (27 A + 16 B) \cos[c] \sin[d x]}{d} + \frac{3 (4 A + B) \cos[2 c] \sin[2 d x]}{d} + \\ & \frac{A \cos[3 c] \sin[3 d x]}{d} + \frac{12 B \sin\left[\frac{d x}{2}\right]}{d \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2} (c + d x)\right] - \sin\left[\frac{1}{2} (c + d x)\right] \right)} + \\ & \left. \frac{12 B \sin\left[\frac{d x}{2}\right]}{d \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{1}{2} (c + d x)\right] + \sin\left[\frac{1}{2} (c + d x)\right] \right)} \right) \end{aligned}$$

**Problem 82: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + d x]^4 (A + B \sec[c + d x])}{a + a \sec[c + d x]} dx$$

Optimal (type 3, 131 leaves, 6 steps):

$$\begin{aligned} & \frac{3 (A - B) \operatorname{ArcTanh}[\sin[c + d x]]}{2 a d} - \frac{(3 A - 4 B) \tan[c + d x]}{a d} + \\ & \frac{3 (A - B) \sec[c + d x] \tan[c + d x]}{2 a d} + \frac{(A - B) \sec[c + d x]^3 \tan[c + d x]}{d (a + a \sec[c + d x])} - \frac{(3 A - 4 B) \tan[c + d x]^3}{3 a d} \end{aligned}$$

Result (type 3, 635 leaves):



$$\begin{aligned}
& \left( 3 (-A+B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A+B \sec[c+dx]) \right) / \\
& \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx]) \right) - \\
& \left( 3 (-A+B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A+B \sec[c+dx]) \right) / \\
& \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx]) \right) + \frac{1}{48 d (B+A \cos[c+dx]) (a+a \sec[c+dx])} \\
& \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] \sec[c+dx]^3 (A+B \sec[c+dx]) \\
& \left( 6 A \sin\left[\frac{dx}{2}\right] + 6 B \sin\left[\frac{dx}{2}\right] - 27 A \sin\left[\frac{3 dx}{2}\right] + 39 B \sin\left[\frac{3 dx}{2}\right] + 12 A \sin\left[c - \frac{dx}{2}\right] - 24 B \right. \\
& \quad \sin\left[c - \frac{dx}{2}\right] + 6 A \sin\left[c + \frac{dx}{2}\right] - 6 B \sin\left[c + \frac{dx}{2}\right] + 24 A \sin\left[2 c + \frac{dx}{2}\right] - 24 B \sin\left[2 c + \frac{dx}{2}\right] - \\
& \quad 9 A \sin\left[c + \frac{3 dx}{2}\right] + 21 B \sin\left[c + \frac{3 dx}{2}\right] - 9 A \sin\left[2 c + \frac{3 dx}{2}\right] + 9 B \sin\left[2 c + \frac{3 dx}{2}\right] + \\
& \quad 9 A \sin\left[3 c + \frac{3 dx}{2}\right] - 9 B \sin\left[3 c + \frac{3 dx}{2}\right] - 3 A \sin\left[c + \frac{5 dx}{2}\right] + 7 B \sin\left[c + \frac{5 dx}{2}\right] + \\
& \quad 3 A \sin\left[2 c + \frac{5 dx}{2}\right] + B \sin\left[2 c + \frac{5 dx}{2}\right] + 3 A \sin\left[3 c + \frac{5 dx}{2}\right] - 3 B \sin\left[3 c + \frac{5 dx}{2}\right] + \\
& \quad 9 A \sin\left[4 c + \frac{5 dx}{2}\right] - 9 B \sin\left[4 c + \frac{5 dx}{2}\right] - 12 A \sin\left[2 c + \frac{7 dx}{2}\right] + 16 B \sin\left[2 c + \frac{7 dx}{2}\right] - \\
& \quad \left. 6 A \sin\left[3 c + \frac{7 dx}{2}\right] + 10 B \sin\left[3 c + \frac{7 dx}{2}\right] - 6 A \sin\left[4 c + \frac{7 dx}{2}\right] + 6 B \sin\left[4 c + \frac{7 dx}{2}\right] \right)
\end{aligned}$$

**Problem 83: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^3 (A+B \sec[c+dx])}{a+a \sec[c+dx]} dx$$

Optimal (type 3, 108 leaves, 6 steps):

$$\begin{aligned}
& - \frac{(2A-3B) \operatorname{ArcTanh}[\sin[c+dx]]}{2ad} + \frac{2(A-B) \tan[c+dx]}{ad} - \\
& \frac{(2A-3B) \sec[c+dx] \tan[c+dx]}{2ad} + \frac{(A-B) \sec[c+dx]^2 \tan[c+dx]}{d(a+a \sec[c+dx])}
\end{aligned}$$

Result (type 3, 671 leaves):

$$\begin{aligned}
& \left( (2A - 3B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A + B \sec[c + dx]) \right) / \\
& \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx]) \right) + \\
& \left( (-2A + 3B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] (A + B \sec[c + dx]) \right) / \\
& \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx]) \right) - \\
& \frac{2 \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx]) \left(-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right]\right)}{d (B + A \cos[c + dx]) (a + a \sec[c + dx])} + \\
& \left( B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + B \sec[c + dx]) \right) / \\
& \left( 2 d (B + A \cos[c + dx]) (a + a \sec[c + dx]) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2 \right) - \\
& \left( 2 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + B \sec[c + dx]) \left(-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right]\right) \right) / \\
& \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx]) \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right) \right) - \\
& \left( B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + B \sec[c + dx]) \right) / \\
& \left( 2 d (B + A \cos[c + dx]) (a + a \sec[c + dx]) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)^2 \right) - \\
& \left( 2 \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 (A + B \sec[c + dx]) \left(-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right]\right) \right) / \\
& \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx]) \left(\cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right]\right) \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right) \right)
\end{aligned}$$

**Problem 84: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^2 (A + B \sec[c + dx])}{a + a \sec[c + dx]} dx$$

Optimal (type 3, 62 leaves, 5 steps):

$$\frac{(A - B) \operatorname{ArcTanh}\left[\sin[c + dx]\right]}{a d} + \frac{B \tan[c + dx]}{a d} - \frac{(A - B) \tan[c + dx]}{d (a + a \sec[c + dx])}$$

Result (type 3, 224 leaves):

$$\begin{aligned}
& \left( 2 \cos\left[\frac{1}{2} (c + dx)\right] (A + B \sec[c + dx]) \left( (-A + B) \sec\left[\frac{c}{2}\right] \sin\left[\frac{dx}{2}\right] + \cos\left[\frac{1}{2} (c + dx)\right] \left( - (A - B) \right. \right. \right. \\
& \left. \left. \left( \log\left[\cos\left[\frac{1}{2} (c + dx)\right] - \sin\left[\frac{1}{2} (c + dx)\right]\right] - \log\left[\cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right]\right] \right) \right) + \right. \\
& \left. (B \sin[dx]) \right) / \left( \left( \cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right] \right) \left( \cos\left[\frac{c}{2}\right] + \sin\left[\frac{c}{2}\right] \right) \right. \\
& \left. \left( \cos\left[\frac{1}{2} (c + dx)\right] - \sin\left[\frac{1}{2} (c + dx)\right] \right) \left( \cos\left[\frac{1}{2} (c + dx)\right] + \sin\left[\frac{1}{2} (c + dx)\right] \right) \right) / \\
& (a d (B + A \cos[c + dx]) (1 + \sec[c + dx]))
\end{aligned}$$

**Problem 85: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx] (A+B \sec[c+dx])}{a+a \sec[c+dx]} dx$$

Optimal (type 3, 43 leaves, 3 steps):

$$\frac{B \operatorname{ArcTanh}[\sin[c+dx]]}{a d} + \frac{(A-B) \tan[c+dx]}{d (a+a \sec[c+dx])}$$

Result (type 3, 109 leaves):

$$\left( 2 \cos\left[\frac{1}{2}(c+dx)\right] \left( B \cos\left[\frac{1}{2}(c+dx)\right] \right. \right. \\ \left. \left. - \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] + \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] \right) \right. \\ \left. + (A-B) \sec\left[\frac{c}{2}\right] \sin\left[\frac{dx}{2}\right] \right) / (a d (1 + \cos[c+dx]))$$

**Problem 86: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx]}{a+a \sec[c+dx]} dx$$

Optimal (type 3, 35 leaves, 2 steps):

$$\frac{A x}{a} - \frac{(A-B) \tan[c+dx]}{d (a+a \sec[c+dx])}$$

Result (type 3, 72 leaves):

$$\left( \cos\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{c}{2}\right] \left( A dx \cos\left[\frac{dx}{2}\right] + A dx \cos\left[c + \frac{dx}{2}\right] + 2(-A+B) \sin\left[\frac{dx}{2}\right] \right) \right. \\ \left. + (a d (1 + \cos[c+dx])) \right)$$

**Problem 88: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^2 (A+B \sec[c+dx])}{a+a \sec[c+dx]} dx$$

Optimal (type 3, 98 leaves, 5 steps):

$$\frac{(3A-2B)x}{2a} - \frac{2(A-B) \sin[c+dx]}{a d} + \\ \frac{(3A-2B) \cos[c+dx] \sin[c+dx]}{2 a d} - \frac{(A-B) \cos[c+dx] \sin[c+dx]}{d (a+a \sec[c+dx])}$$

Result (type 3, 197 leaves):

$$\left( \cos\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{c}{2}\right] \left( 4(3A-2B)dx \cos\left[\frac{dx}{2}\right] + 4(3A-2B)dx \cos\left[c+\frac{dx}{2}\right] - 20A \sin\left[\frac{dx}{2}\right] + 20B \sin\left[\frac{dx}{2}\right] - 4A \sin\left[c+\frac{dx}{2}\right] + 4B \sin\left[c+\frac{dx}{2}\right] - 3A \sin\left[c+\frac{3dx}{2}\right] + 4B \sin\left[c+\frac{3dx}{2}\right] - 3A \sin\left[2c+\frac{3dx}{2}\right] + 4B \sin\left[2c+\frac{3dx}{2}\right] + A \sin\left[2c+\frac{5dx}{2}\right] + A \sin\left[3c+\frac{5dx}{2}\right] \right) \right) / (8ad(1+\cos[c+dx]))$$

**Problem 89: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^3 (A+B \sec[c+dx])}{a+a \sec[c+dx]} dx$$

Optimal (type 3, 122 leaves, 6 steps):

$$-\frac{3(A-B)x}{2a} + \frac{(4A-3B)\sin[c+dx]}{ad} - \frac{3(A-B)\cos[c+dx]\sin[c+dx]}{2ad} - \frac{(A-B)\cos[c+dx]^2\sin[c+dx]}{d(a+a \sec[c+dx])} - \frac{(4A-3B)\sin[c+dx]^3}{3ad}$$

Result (type 3, 249 leaves):

$$\frac{1}{24ad(1+\cos[c+dx])} \cos\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{c}{2}\right] \left( -36(A-B)dx \cos\left[\frac{dx}{2}\right] - 36(A-B)dx \cos\left[c+\frac{dx}{2}\right] + 69A \sin\left[\frac{dx}{2}\right] - 60B \sin\left[\frac{dx}{2}\right] + 21A \sin\left[c+\frac{dx}{2}\right] - 12B \sin\left[c+\frac{dx}{2}\right] + 18A \sin\left[c+\frac{3dx}{2}\right] - 9B \sin\left[c+\frac{3dx}{2}\right] + 18A \sin\left[2c+\frac{3dx}{2}\right] - 9B \sin\left[2c+\frac{3dx}{2}\right] - 2A \sin\left[2c+\frac{5dx}{2}\right] + 3B \sin\left[2c+\frac{5dx}{2}\right] - 2A \sin\left[3c+\frac{5dx}{2}\right] + 3B \sin\left[3c+\frac{5dx}{2}\right] + A \sin\left[3c+\frac{7dx}{2}\right] + A \sin\left[4c+\frac{7dx}{2}\right] \right)$$

**Problem 90: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^5 (A+B \sec[c+dx])}{(a+a \sec[c+dx])^2} dx$$

Optimal (type 3, 179 leaves, 7 steps):

$$\frac{(7A-10B)\operatorname{ArcTanh}[\sin[c+dx]]}{2a^2d} - \frac{4(2A-3B)\tan[c+dx]}{a^2d} + \frac{(7A-10B)\sec[c+dx]\tan[c+dx]}{2a^2d} + \frac{(7A-10B)\sec[c+dx]^3\tan[c+dx]}{3a^2d(1+\sec[c+dx])} + \frac{(A-B)\sec[c+dx]^4\tan[c+dx]}{3d(a+a \sec[c+dx])^2} - \frac{4(2A-3B)\tan[c+dx]^3}{3a^2d}$$

Result (type 3, 764 leaves):

$$\begin{aligned} & \left( 2 \left( -7A + 10B \right) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec [c + dx] (A + B \sec [c + dx]) \right) / \\ & \left( d (B + A \cos [c + dx]) (a + a \sec [c + dx])^2 \right) - \\ & \left( 2 \left( -7A + 10B \right) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec [c + dx] \right. \\ & \left. (A + B \sec [c + dx]) \right) / \left( d (B + A \cos [c + dx]) (a + a \sec [c + dx])^2 \right) + \\ & \frac{1}{96 d (B + A \cos [c + dx]) (a + a \sec [c + dx])^2} \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c] \sec [c + dx]^4 \\ & (A + B \sec [c + dx]) \left( 45 A \sin \left[ \frac{dx}{2} \right] - 6 B \sin \left[ \frac{dx}{2} \right] - 201 A \sin \left[ \frac{3 dx}{2} \right] + 310 B \sin \left[ \frac{3 dx}{2} \right] + \right. \\ & 195 A \sin \left[ c - \frac{dx}{2} \right] - 306 B \sin \left[ c - \frac{dx}{2} \right] - 51 A \sin \left[ c + \frac{dx}{2} \right] + 42 B \sin \left[ c + \frac{dx}{2} \right] + \\ & 189 A \sin \left[ 2c + \frac{dx}{2} \right] - 270 B \sin \left[ 2c + \frac{dx}{2} \right] - A \sin \left[ c + \frac{3 dx}{2} \right] + 50 B \sin \left[ c + \frac{3 dx}{2} \right] - \\ & 81 A \sin \left[ 2c + \frac{3 dx}{2} \right] + 90 B \sin \left[ 2c + \frac{3 dx}{2} \right] + 119 A \sin \left[ 3c + \frac{3 dx}{2} \right] - \\ & 170 B \sin \left[ 3c + \frac{3 dx}{2} \right] - 129 A \sin \left[ c + \frac{5 dx}{2} \right] + 198 B \sin \left[ c + \frac{5 dx}{2} \right] - 9 A \sin \left[ 2c + \frac{5 dx}{2} \right] + \\ & 42 B \sin \left[ 2c + \frac{5 dx}{2} \right] - 57 A \sin \left[ 3c + \frac{5 dx}{2} \right] + 66 B \sin \left[ 3c + \frac{5 dx}{2} \right] + 63 A \sin \left[ 4c + \frac{5 dx}{2} \right] - \\ & 90 B \sin \left[ 4c + \frac{5 dx}{2} \right] - 75 A \sin \left[ 2c + \frac{7 dx}{2} \right] + 114 B \sin \left[ 2c + \frac{7 dx}{2} \right] - \\ & 15 A \sin \left[ 3c + \frac{7 dx}{2} \right] + 36 B \sin \left[ 3c + \frac{7 dx}{2} \right] - 39 A \sin \left[ 4c + \frac{7 dx}{2} \right] + 48 B \sin \left[ 4c + \frac{7 dx}{2} \right] + \\ & 21 A \sin \left[ 5c + \frac{7 dx}{2} \right] - 30 B \sin \left[ 5c + \frac{7 dx}{2} \right] - 32 A \sin \left[ 3c + \frac{9 dx}{2} \right] + 48 B \sin \left[ 3c + \frac{9 dx}{2} \right] - \\ & \left. 12 A \sin \left[ 4c + \frac{9 dx}{2} \right] + 22 B \sin \left[ 4c + \frac{9 dx}{2} \right] - 20 A \sin \left[ 5c + \frac{9 dx}{2} \right] + 26 B \sin \left[ 5c + \frac{9 dx}{2} \right] \right) \end{aligned}$$

Problem 91: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + dx]^4 (A + B \sec [c + dx])}{(a + a \sec [c + dx])^2} dx$$

Optimal (type 3, 156 leaves, 7 steps):

$$\begin{aligned} & - \frac{(4A - 7B) \operatorname{ArcTanh}[\sin [c + dx]]}{2 a^2 d} + \frac{2 (5A - 8B) \tan [c + dx]}{3 a^2 d} - \frac{(4A - 7B) \sec [c + dx] \tan [c + dx]}{2 a^2 d} + \\ & \frac{(5A - 8B) \sec [c + dx]^2 \tan [c + dx]}{3 a^2 d (1 + \sec [c + dx])} + \frac{(A - B) \sec [c + dx]^3 \tan [c + dx]}{3 d (a + a \sec [c + dx])^2} \end{aligned}$$

Result (type 3, 652 leaves):

$$\begin{aligned}
 & - \left( \left( 2 (-4A + 7B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \right. \\
 & \quad \left. \left. \sec[c + dx] (A + B \sec[c + dx]) \right) \right) / \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx])^2 \right) + \\
 & \left( 2 (-4A + 7B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec[c + dx] (A + B \sec[c + dx]) \right) / \\
 & \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx])^2 \right) + \\
 & \frac{1}{48 d (B + A \cos[c + dx]) (a + a \sec[c + dx])^2} \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] \sec[c + dx]^3 (A + B \sec[c + dx]) \\
 & \left( -14A \sin\left[\frac{dx}{2}\right] + 14B \sin\left[\frac{dx}{2}\right] + 64A \sin\left[\frac{3dx}{2}\right] - 97B \sin\left[\frac{3dx}{2}\right] - 84A \sin\left[c - \frac{dx}{2}\right] + 126B \right. \\
 & \quad \left. \sin\left[c - \frac{dx}{2}\right] + 42A \sin\left[c + \frac{dx}{2}\right] - 42B \sin\left[c + \frac{dx}{2}\right] - 56A \sin\left[2c + \frac{dx}{2}\right] + 98B \sin\left[2c + \frac{dx}{2}\right] - \right. \\
 & \quad \left. 6A \sin\left[c + \frac{3dx}{2}\right] + 3B \sin\left[c + \frac{3dx}{2}\right] + 34A \sin\left[2c + \frac{3dx}{2}\right] - 37B \sin\left[2c + \frac{3dx}{2}\right] - \right. \\
 & \quad \left. 36A \sin\left[3c + \frac{3dx}{2}\right] + 63B \sin\left[3c + \frac{3dx}{2}\right] + 48A \sin\left[c + \frac{5dx}{2}\right] - 75B \sin\left[c + \frac{5dx}{2}\right] + \right. \\
 & \quad \left. 6A \sin\left[2c + \frac{5dx}{2}\right] - 15B \sin\left[2c + \frac{5dx}{2}\right] + 30A \sin\left[3c + \frac{5dx}{2}\right] - 39B \sin\left[3c + \frac{5dx}{2}\right] - \right. \\
 & \quad \left. 12A \sin\left[4c + \frac{5dx}{2}\right] + 21B \sin\left[4c + \frac{5dx}{2}\right] + 20A \sin\left[2c + \frac{7dx}{2}\right] - 32B \sin\left[2c + \frac{7dx}{2}\right] + \right. \\
 & \quad \left. 6A \sin\left[3c + \frac{7dx}{2}\right] - 12B \sin\left[3c + \frac{7dx}{2}\right] + 14A \sin\left[4c + \frac{7dx}{2}\right] - 20B \sin\left[4c + \frac{7dx}{2}\right] \right)
 \end{aligned}$$

Problem 92: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec[c + dx]^3 (A + B \sec[c + dx])}{(a + a \sec[c + dx])^2} dx$$

Optimal (type 3, 108 leaves, 6 steps):

$$\begin{aligned}
 & \frac{(A - 2B) \operatorname{ArcTanh}[\sin[c + dx]]}{a^2 d} - \frac{(A - 4B) \tan[c + dx]}{3 a^2 d} - \\
 & \frac{(A - 2B) \tan[c + dx]}{a^2 d (1 + \sec[c + dx])} + \frac{(A - B) \sec[c + dx]^2 \tan[c + dx]}{3 d (a + a \sec[c + dx])^2}
 \end{aligned}$$

Result (type 3, 292 leaves):

$$\frac{1}{3 a^2 d (B + A \cos [c + d x]) (1 + \sec [c + d x])^2} 2 \cos \left[ \frac{1}{2} (c + d x) \right] \sec [c + d x] (A + B \sec [c + d x])$$

$$\left( (-A + B) \sec \left[ \frac{c}{2} \right] \sin \left[ \frac{d x}{2} \right] - 2 (4 A - 7 B) \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec \left[ \frac{c}{2} \right] \sin \left[ \frac{d x}{2} \right] + \right.$$

$$\cos \left[ \frac{1}{2} (c + d x) \right]^3 \left( -6 (A - 2 B) \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right.$$

$$\left. \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) + (6 B \sin [d x]) \right) /$$

$$\left( \left( \cos \left[ \frac{c}{2} \right] - \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right.$$

$$\left. \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) - (A - B) \cos \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{c}{2} \right]$$

**Problem 93: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^2 (A + B \sec [c + d x])}{(a + a \sec [c + d x])^2} dx$$

Optimal (type 3, 79 leaves, 4 steps):

$$\frac{B \operatorname{ArcTanh} [\sin [c + d x]]}{a^2 d} + \frac{(2 A - 5 B) \tan [c + d x]}{3 a^2 d (1 + \sec [c + d x])} - \frac{(A - B) \tan [c + d x]}{3 d (a + a \sec [c + d x])^2}$$

Result (type 3, 169 leaves):

$$- \left( \left( 2 \cos \left[ \frac{1}{2} (c + d x) \right] \left( 6 B \cos \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right. \right.$$

$$\left. \left( \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) + \right.$$

$$\left. (-A + B) \sec \left[ \frac{c}{2} \right] \sin \left[ \frac{d x}{2} \right] - 2 (A - 4 B) \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec \left[ \frac{c}{2} \right] \sin \left[ \frac{d x}{2} \right] - \right.$$

$$\left. (A - B) \cos \left[ \frac{1}{2} (c + d x) \right] \tan \left[ \frac{c}{2} \right] \right) / \left( 3 a^2 d (1 + \cos [c + d x])^2 \right)$$

**Problem 95: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x]}{(a + a \sec [c + d x])^2} dx$$

Optimal (type 3, 70 leaves, 3 steps):

$$\frac{A x}{a^2} - \frac{(4 A - B) \tan [c + d x]}{3 a^2 d (1 + \sec [c + d x])} - \frac{(A - B) \tan [c + d x]}{3 d (a + a \sec [c + d x])^2}$$

Result (type 3, 153 leaves):

$$\begin{aligned} & \frac{1}{24 a^2 d} \sec\left[\frac{c}{2}\right] \sec\left[\frac{1}{2}(c+dx)\right]^3 \\ & \left(9 A dx \cos\left[\frac{dx}{2}\right] + 9 A dx \cos\left[c + \frac{dx}{2}\right] + 3 A dx \cos\left[c + \frac{3 dx}{2}\right] + 3 A dx \cos\left[2c + \frac{3 dx}{2}\right] - \right. \\ & 18 A \sin\left[\frac{dx}{2}\right] + 6 B \sin\left[\frac{dx}{2}\right] + 12 A \sin\left[c + \frac{dx}{2}\right] - \\ & \left. 6 B \sin\left[c + \frac{dx}{2}\right] - 10 A \sin\left[c + \frac{3 dx}{2}\right] + 4 B \sin\left[c + \frac{3 dx}{2}\right]\right) \end{aligned}$$

Problem 96: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx] (A+B \sec[c+dx])}{(a+a \sec[c+dx])^2} dx$$

Optimal (type 3, 98 leaves, 5 steps):

$$-\frac{(2A-B)x}{a^2} + \frac{2(5A-2B)\sin[c+dx]}{3a^2d} - \frac{(2A-B)\sin[c+dx]}{a^2d(1+\sec[c+dx])} - \frac{(A-B)\sin[c+dx]}{3d(a+a \sec[c+dx])^2}$$

Result (type 3, 245 leaves):

$$\begin{aligned} & \frac{1}{12 a^2 d (1+\cos[c+dx])^2} \\ & \cos\left[\frac{1}{2}(c+dx)\right] \sec\left[\frac{c}{2}\right] \left(-18(2A-B) dx \cos\left[\frac{dx}{2}\right] - 18(2A-B) dx \cos\left[c + \frac{dx}{2}\right] - \right. \\ & 12 A dx \cos\left[c + \frac{3 dx}{2}\right] + 6 B dx \cos\left[c + \frac{3 dx}{2}\right] - 12 A dx \cos\left[2c + \frac{3 dx}{2}\right] + 6 B dx \cos\left[2c + \frac{3 dx}{2}\right] + \\ & 66 A \sin\left[\frac{dx}{2}\right] - 36 B \sin\left[\frac{dx}{2}\right] - 30 A \sin\left[c + \frac{dx}{2}\right] + 24 B \sin\left[c + \frac{dx}{2}\right] + 41 A \sin\left[c + \frac{3 dx}{2}\right] - \\ & \left. 20 B \sin\left[c + \frac{3 dx}{2}\right] + 9 A \sin\left[2c + \frac{3 dx}{2}\right] + 3 A \sin\left[2c + \frac{5 dx}{2}\right] + 3 A \sin\left[3c + \frac{5 dx}{2}\right]\right) \end{aligned}$$

Problem 97: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^2 (A+B \sec[c+dx])}{(a+a \sec[c+dx])^2} dx$$

Optimal (type 3, 143 leaves, 6 steps):

$$\begin{aligned} & \frac{(7A-4B)x}{2a^2} - \frac{2(8A-5B)\sin[c+dx]}{3a^2d} + \frac{(7A-4B)\cos[c+dx]\sin[c+dx]}{2a^2d} - \\ & \frac{(8A-5B)\cos[c+dx]\sin[c+dx]}{3a^2d(1+\sec[c+dx])} - \frac{(A-B)\cos[c+dx]\sin[c+dx]}{3d(a+a \sec[c+dx])^2} \end{aligned}$$

Result (type 3, 315 leaves):



$$\begin{aligned}
& \frac{1}{48 a^2 d \left(1 + \cos[c + d x]\right)^2} \\
& \cos\left[\frac{1}{2}(c + d x)\right] \sec\left[\frac{c}{2}\right] \left( 36 (7 A - 4 B) d x \cos\left[\frac{d x}{2}\right] + 36 (7 A - 4 B) d x \cos\left[c + \frac{d x}{2}\right] + \right. \\
& \quad 84 A d x \cos\left[c + \frac{3 d x}{2}\right] - 48 B d x \cos\left[c + \frac{3 d x}{2}\right] + 84 A d x \cos\left[2 c + \frac{3 d x}{2}\right] - \\
& \quad 48 B d x \cos\left[2 c + \frac{3 d x}{2}\right] - 381 A \sin\left[\frac{d x}{2}\right] + 264 B \sin\left[\frac{d x}{2}\right] + 147 A \sin\left[c + \frac{d x}{2}\right] - \\
& \quad 120 B \sin\left[c + \frac{d x}{2}\right] - 239 A \sin\left[c + \frac{3 d x}{2}\right] + 164 B \sin\left[c + \frac{3 d x}{2}\right] - 63 A \sin\left[2 c + \frac{3 d x}{2}\right] + \\
& \quad 36 B \sin\left[2 c + \frac{3 d x}{2}\right] - 15 A \sin\left[2 c + \frac{5 d x}{2}\right] + 12 B \sin\left[2 c + \frac{5 d x}{2}\right] - \\
& \quad \left. 15 A \sin\left[3 c + \frac{5 d x}{2}\right] + 12 B \sin\left[3 c + \frac{5 d x}{2}\right] + 3 A \sin\left[3 c + \frac{7 d x}{2}\right] + 3 A \sin\left[4 c + \frac{7 d x}{2}\right] \right)
\end{aligned}$$

Problem 98: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + d x]^3 (A + B \sec[c + d x])}{(a + a \sec[c + d x])^2} dx$$

Optimal (type 3, 170 leaves, 7 steps):

$$\begin{aligned}
& -\frac{(10 A - 7 B) x}{2 a^2} + \frac{4 (3 A - 2 B) \sin[c + d x]}{a^2 d} - \\
& \frac{(10 A - 7 B) \cos[c + d x] \sin[c + d x]}{2 a^2 d} - \frac{(10 A - 7 B) \cos[c + d x]^2 \sin[c + d x]}{3 a^2 d (1 + \sec[c + d x])} - \\
& \frac{(A - B) \cos[c + d x]^2 \sin[c + d x]}{3 d (a + a \sec[c + d x])^2} - \frac{4 (3 A - 2 B) \sin[c + d x]^3}{3 a^2 d}
\end{aligned}$$

Result (type 3, 369 leaves):

$$\frac{1}{48 a^2 d \left(1 + \cos[c + d x]\right)^2} \cos\left[\frac{1}{2}(c + d x)\right] \sec\left[\frac{c}{2}\right] \left( -36 (10 A - 7 B) d x \cos\left[\frac{d x}{2}\right] - 36 (10 A - 7 B) d x \cos\left[c + \frac{d x}{2}\right] - 120 A d x \cos\left[c + \frac{3 d x}{2}\right] + 84 B d x \cos\left[c + \frac{3 d x}{2}\right] - 120 A d x \cos\left[2 c + \frac{3 d x}{2}\right] + 84 B d x \cos\left[2 c + \frac{3 d x}{2}\right] + 516 A \sin\left[\frac{d x}{2}\right] - 381 B \sin\left[\frac{d x}{2}\right] - 156 A \sin\left[c + \frac{d x}{2}\right] + 147 B \sin\left[c + \frac{d x}{2}\right] + 342 A \sin\left[c + \frac{3 d x}{2}\right] - 239 B \sin\left[c + \frac{3 d x}{2}\right] + 118 A \sin\left[2 c + \frac{3 d x}{2}\right] - 63 B \sin\left[2 c + \frac{3 d x}{2}\right] + 30 A \sin\left[2 c + \frac{5 d x}{2}\right] - 15 B \sin\left[2 c + \frac{5 d x}{2}\right] + 30 A \sin\left[3 c + \frac{5 d x}{2}\right] - 15 B \sin\left[3 c + \frac{5 d x}{2}\right] - 3 A \sin\left[3 c + \frac{7 d x}{2}\right] + 3 B \sin\left[3 c + \frac{7 d x}{2}\right] - 3 A \sin\left[4 c + \frac{7 d x}{2}\right] + 3 B \sin\left[4 c + \frac{7 d x}{2}\right] + A \sin\left[4 c + \frac{9 d x}{2}\right] + A \sin\left[5 c + \frac{9 d x}{2}\right] \right)$$

Problem 99: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec[c + d x]^5 (A + B \sec[c + d x])}{(a + a \sec[c + d x])^3} dx$$

Optimal (type 3, 202 leaves, 8 steps):

$$-\frac{(6 A - 13 B) \operatorname{ArcTanh}[\sin[c + d x]]}{2 a^3 d} + \frac{8 (9 A - 19 B) \tan[c + d x]}{15 a^3 d} - \frac{(6 A - 13 B) \sec[c + d x] \tan[c + d x]}{2 a^3 d} + \frac{(A - B) \sec[c + d x]^4 \tan[c + d x]}{5 d (a + a \sec[c + d x])^3} + \frac{(6 A - 11 B) \sec[c + d x]^3 \tan[c + d x]}{15 a d (a + a \sec[c + d x])^2} + \frac{4 (9 A - 19 B) \sec[c + d x]^2 \tan[c + d x]}{15 d (a^3 + a^3 \sec[c + d x])}$$

Result (type 3, 768 leaves):

$$\begin{aligned}
& - \left( \left( 4 \left( -6A + 13B \right) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \right. \right. \\
& \quad \left. \left. \sec [c + dx]^2 (A + B \sec [c + dx]) \right) \right) / \left( d (B + A \cos [c + dx]) (a + a \sec [c + dx])^3 \right) + \\
& \left( 4 \left( -6A + 13B \right) \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^6 \log \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right] \sec [c + dx]^2 \right. \\
& \quad \left. (A + B \sec [c + dx]) \right) / \left( d (B + A \cos [c + dx]) (a + a \sec [c + dx])^3 \right) + \\
& \frac{1}{480 d (B + A \cos [c + dx]) (a + a \sec [c + dx])^3} \\
& \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c] \sec [c + dx]^4 (A + B \sec [c + dx]) \\
& \left( -870 A \sin \left[ \frac{dx}{2} \right] + 1235 B \sin \left[ \frac{dx}{2} \right] + 1830 A \sin \left[ \frac{3 dx}{2} \right] - 3805 B \sin \left[ \frac{3 dx}{2} \right] - 2094 A \sin \left[ c - \frac{dx}{2} \right] + \right. \\
& \quad 4329 B \sin \left[ c - \frac{dx}{2} \right] + 1314 A \sin \left[ c + \frac{dx}{2} \right] - 1989 B \sin \left[ c + \frac{dx}{2} \right] - 1650 A \sin \left[ 2c + \frac{dx}{2} \right] + \\
& \quad 3575 B \sin \left[ 2c + \frac{dx}{2} \right] - 450 A \sin \left[ c + \frac{3 dx}{2} \right] + 475 B \sin \left[ c + \frac{3 dx}{2} \right] + 1230 A \sin \left[ 2c + \frac{3 dx}{2} \right] - \\
& \quad 2005 B \sin \left[ 2c + \frac{3 dx}{2} \right] - 1050 A \sin \left[ 3c + \frac{3 dx}{2} \right] + 2275 B \sin \left[ 3c + \frac{3 dx}{2} \right] + \\
& \quad 1278 A \sin \left[ c + \frac{5 dx}{2} \right] - 2673 B \sin \left[ c + \frac{5 dx}{2} \right] - 90 A \sin \left[ 2c + \frac{5 dx}{2} \right] - 105 B \sin \left[ 2c + \frac{5 dx}{2} \right] + \\
& \quad 918 A \sin \left[ 3c + \frac{5 dx}{2} \right] - 1593 B \sin \left[ 3c + \frac{5 dx}{2} \right] - 450 A \sin \left[ 4c + \frac{5 dx}{2} \right] + \\
& \quad 975 B \sin \left[ 4c + \frac{5 dx}{2} \right] + 630 A \sin \left[ 2c + \frac{7 dx}{2} \right] - 1325 B \sin \left[ 2c + \frac{7 dx}{2} \right] + \\
& \quad 60 A \sin \left[ 3c + \frac{7 dx}{2} \right] - 255 B \sin \left[ 3c + \frac{7 dx}{2} \right] + 480 A \sin \left[ 4c + \frac{7 dx}{2} \right] - 875 B \sin \left[ 4c + \frac{7 dx}{2} \right] - \\
& \quad 90 A \sin \left[ 5c + \frac{7 dx}{2} \right] + 195 B \sin \left[ 5c + \frac{7 dx}{2} \right] + 144 A \sin \left[ 3c + \frac{9 dx}{2} \right] - 304 B \sin \left[ 3c + \frac{9 dx}{2} \right] + \\
& \quad \left. 30 A \sin \left[ 4c + \frac{9 dx}{2} \right] - 90 B \sin \left[ 4c + \frac{9 dx}{2} \right] + 114 A \sin \left[ 5c + \frac{9 dx}{2} \right] - 214 B \sin \left[ 5c + \frac{9 dx}{2} \right] \right)
\end{aligned}$$

Problem 100: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + dx]^4 (A + B \sec [c + dx])}{(a + a \sec [c + dx])^3} dx$$

Optimal (type 3, 156 leaves, 7 steps):

$$\begin{aligned}
& \frac{(A - 3B) \operatorname{ArcTanh}[\sin [c + dx]]}{a^3 d} - \frac{(7A - 27B) \tan [c + dx]}{15 a^3 d} + \\
& \frac{(A - B) \sec [c + dx]^3 \tan [c + dx]}{5 d (a + a \sec [c + dx])^3} + \frac{(4A - 9B) \sec [c + dx]^2 \tan [c + dx]}{15 a d (a + a \sec [c + dx])^2} - \frac{(A - 3B) \tan [c + dx]}{d (a^3 + a^3 \sec [c + dx])}
\end{aligned}$$

Result (type 3, 642 leaves):

$$\begin{aligned}
& \left( 8 (-A + 3B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec[c + dx]^2 (A + B \sec[c + dx]) \right) / \\
& \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx])^3 \right) - \\
& \left( 8 (-A + 3B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec[c + dx]^2 (A + B \sec[c + dx]) \right) / \\
& \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx])^3 \right) + \frac{1}{120 d (B + A \cos[c + dx]) (a + a \sec[c + dx])^3} \\
& \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] \sec[c + dx]^3 (A + B \sec[c + dx]) \\
& \left( 160 A \sin\left[\frac{dx}{2}\right] - 255 B \sin\left[\frac{dx}{2}\right] - 167 A \sin\left[\frac{3dx}{2}\right] + 567 B \sin\left[\frac{3dx}{2}\right] + 170 A \sin\left[c - \frac{dx}{2}\right] - \right. \\
& 600 B \sin\left[c - \frac{dx}{2}\right] - 170 A \sin\left[c + \frac{dx}{2}\right] + 375 B \sin\left[c + \frac{dx}{2}\right] + 160 A \sin\left[2c + \frac{dx}{2}\right] - \\
& 480 B \sin\left[2c + \frac{dx}{2}\right] + 75 A \sin\left[c + \frac{3dx}{2}\right] - 60 B \sin\left[c + \frac{3dx}{2}\right] - 167 A \sin\left[2c + \frac{3dx}{2}\right] + \\
& 402 B \sin\left[2c + \frac{3dx}{2}\right] + 75 A \sin\left[3c + \frac{3dx}{2}\right] - 225 B \sin\left[3c + \frac{3dx}{2}\right] - 95 A \sin\left[c + \frac{5dx}{2}\right] + \\
& 315 B \sin\left[c + \frac{5dx}{2}\right] + 15 A \sin\left[2c + \frac{5dx}{2}\right] + 30 B \sin\left[2c + \frac{5dx}{2}\right] - 95 A \sin\left[3c + \frac{5dx}{2}\right] + \\
& 240 B \sin\left[3c + \frac{5dx}{2}\right] + 15 A \sin\left[4c + \frac{5dx}{2}\right] - 45 B \sin\left[4c + \frac{5dx}{2}\right] - 22 A \sin\left[2c + \frac{7dx}{2}\right] + \\
& \left. 72 B \sin\left[2c + \frac{7dx}{2}\right] + 15 B \sin\left[3c + \frac{7dx}{2}\right] - 22 A \sin\left[4c + \frac{7dx}{2}\right] + 57 B \sin\left[4c + \frac{7dx}{2}\right] \right)
\end{aligned}$$

### Problem 104: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \sec[c + dx]}{(a + a \sec[c + dx])^3} dx$$

Optimal (type 3, 108 leaves, 4 steps):

$$\frac{Ax}{a^3} - \frac{(A-B) \tan[c + dx]}{5d (a + a \sec[c + dx])^3} - \frac{(7A-2B) \tan[c + dx]}{15ad (a + a \sec[c + dx])^2} - \frac{2(11A-B) \tan[c + dx]}{15d (a^3 + a^3 \sec[c + dx])}$$

Result (type 3, 241 leaves):

$$\begin{aligned}
& \frac{1}{480 a^3 d} \sec\left[\frac{c}{2}\right] \sec\left[\frac{1}{2}(c + dx)\right]^5 \\
& \left( 150 A dx \cos\left[\frac{dx}{2}\right] + 150 A dx \cos\left[c + \frac{dx}{2}\right] + 75 A dx \cos\left[c + \frac{3dx}{2}\right] + 75 A dx \cos\left[2c + \frac{3dx}{2}\right] + \right. \\
& 15 A dx \cos\left[2c + \frac{5dx}{2}\right] + 15 A dx \cos\left[3c + \frac{5dx}{2}\right] - 370 A \sin\left[\frac{dx}{2}\right] + 80 B \sin\left[\frac{dx}{2}\right] + \\
& 270 A \sin\left[c + \frac{dx}{2}\right] - 60 B \sin\left[c + \frac{dx}{2}\right] - 230 A \sin\left[c + \frac{3dx}{2}\right] + 40 B \sin\left[c + \frac{3dx}{2}\right] + \\
& \left. 90 A \sin\left[2c + \frac{3dx}{2}\right] - 30 B \sin\left[2c + \frac{3dx}{2}\right] - 64 A \sin\left[2c + \frac{5dx}{2}\right] + 14 B \sin\left[2c + \frac{5dx}{2}\right] \right)
\end{aligned}$$

### Problem 105: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx] (A + B \sec[c + dx])}{(a + a \sec[c + dx])^3} dx$$

Optimal (type 3, 136 leaves, 6 steps):

$$-\frac{(3A - B)x}{a^3} + \frac{2(36A - 11B)\sin[c + dx]}{15a^3d} - \frac{(A - B)\sin[c + dx]}{5d(a + a \sec[c + dx])^3} - \frac{(9A - 4B)\sin[c + dx]}{15ad(a + a \sec[c + dx])^2} - \frac{(3A - B)\sin[c + dx]}{d(a^3 + a^3 \sec[c + dx])}$$

Result (type 3, 365 leaves):

$$\frac{1}{120a^3d(1 + \cos[c + dx])^3} \cos\left[\frac{1}{2}(c + dx)\right] \sec\left[\frac{c}{2}\right] \left( -300(3A - B)dx \cos\left[\frac{dx}{2}\right] - 300(3A - B)dx \cos\left[c + \frac{dx}{2}\right] - 450Adx \cos\left[c + \frac{3dx}{2}\right] + 150Bdx \cos\left[c + \frac{3dx}{2}\right] - 450Adx \cos\left[2c + \frac{3dx}{2}\right] + 150Bdx \cos\left[2c + \frac{3dx}{2}\right] - 90Adx \cos\left[2c + \frac{5dx}{2}\right] + 30Bdx \cos\left[2c + \frac{5dx}{2}\right] - 90Adx \cos\left[3c + \frac{5dx}{2}\right] + 30Bdx \cos\left[3c + \frac{5dx}{2}\right] + 1755A \sin\left[\frac{dx}{2}\right] - 740B \sin\left[\frac{dx}{2}\right] - 1125A \sin\left[c + \frac{dx}{2}\right] + 540B \sin\left[c + \frac{dx}{2}\right] + 1215A \sin\left[c + \frac{3dx}{2}\right] - 460B \sin\left[c + \frac{3dx}{2}\right] - 225A \sin\left[2c + \frac{3dx}{2}\right] + 180B \sin\left[2c + \frac{3dx}{2}\right] + 363A \sin\left[2c + \frac{5dx}{2}\right] - 128B \sin\left[2c + \frac{5dx}{2}\right] + 75A \sin\left[3c + \frac{5dx}{2}\right] + 15A \sin\left[3c + \frac{7dx}{2}\right] + 15A \sin\left[4c + \frac{7dx}{2}\right] \right)$$

### Problem 106: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx]^2 (A + B \sec[c + dx])}{(a + a \sec[c + dx])^3} dx$$

Optimal (type 3, 187 leaves, 7 steps):

$$\frac{(13A - 6B)x}{2a^3} - \frac{8(19A - 9B)\sin[c + dx]}{15a^3d} + \frac{(13A - 6B)\cos[c + dx]\sin[c + dx]}{2a^3d} - \frac{(A - B)\cos[c + dx]\sin[c + dx]}{5d(a + a \sec[c + dx])^3} - \frac{(11A - 6B)\cos[c + dx]\sin[c + dx]}{15ad(a + a \sec[c + dx])^2} - \frac{4(19A - 9B)\cos[c + dx]\sin[c + dx]}{15d(a^3 + a^3 \sec[c + dx])}$$

Result (type 3, 435 leaves):

$$\frac{1}{480 a^3 d \left(1 + \cos[c + d x]\right)^3} \cos\left[\frac{1}{2}(c + d x)\right] \sec\left[\frac{c}{2}\right] \left(600 (13 A - 6 B) d x \cos\left[\frac{d x}{2}\right] + 600 (13 A - 6 B) d x \cos\left[c + \frac{d x}{2}\right] + 3900 A d x \cos\left[c + \frac{3 d x}{2}\right] - 1800 B d x \cos\left[c + \frac{3 d x}{2}\right] + 3900 A d x \cos\left[2 c + \frac{3 d x}{2}\right] - 1800 B d x \cos\left[2 c + \frac{3 d x}{2}\right] + 780 A d x \cos\left[2 c + \frac{5 d x}{2}\right] - 360 B d x \cos\left[2 c + \frac{5 d x}{2}\right] + 780 A d x \cos\left[3 c + \frac{5 d x}{2}\right] - 360 B d x \cos\left[3 c + \frac{5 d x}{2}\right] - 12760 A \sin\left[\frac{d x}{2}\right] + 7020 B \sin\left[\frac{d x}{2}\right] + 7560 A \sin\left[c + \frac{d x}{2}\right] - 4500 B \sin\left[c + \frac{d x}{2}\right] - 9230 A \sin\left[c + \frac{3 d x}{2}\right] + 4860 B \sin\left[c + \frac{3 d x}{2}\right] + 930 A \sin\left[2 c + \frac{3 d x}{2}\right] - 900 B \sin\left[2 c + \frac{3 d x}{2}\right] - 2782 A \sin\left[2 c + \frac{5 d x}{2}\right] + 1452 B \sin\left[2 c + \frac{5 d x}{2}\right] - 750 A \sin\left[3 c + \frac{5 d x}{2}\right] + 300 B \sin\left[3 c + \frac{5 d x}{2}\right] - 105 A \sin\left[3 c + \frac{7 d x}{2}\right] + 60 B \sin\left[3 c + \frac{7 d x}{2}\right] - 105 A \sin\left[4 c + \frac{7 d x}{2}\right] + 60 B \sin\left[4 c + \frac{7 d x}{2}\right] + 15 A \sin\left[4 c + \frac{9 d x}{2}\right] + 15 A \sin\left[5 c + \frac{9 d x}{2}\right]\right)$$

**Problem 107: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + d x]^3 (A + B \sec[c + d x])}{(a + a \sec[c + d x])^3} dx$$

Optimal (type 3, 218 leaves, 8 steps):

$$\begin{aligned} & -\frac{(23 A - 13 B) x}{2 a^3} + \frac{4 (34 A - 19 B) \sin[c + d x]}{5 a^3 d} - \frac{(23 A - 13 B) \cos[c + d x] \sin[c + d x]}{2 a^3 d} - \\ & \frac{(A - B) \cos[c + d x]^2 \sin[c + d x]}{5 d (a + a \sec[c + d x])^3} - \frac{(13 A - 8 B) \cos[c + d x]^2 \sin[c + d x]}{15 a d (a + a \sec[c + d x])^2} - \\ & \frac{(23 A - 13 B) \cos[c + d x]^2 \sin[c + d x]}{3 d (a^3 + a^3 \sec[c + d x])} - \frac{4 (34 A - 19 B) \sin[c + d x]^3}{15 a^3 d} \end{aligned}$$

Result (type 3, 491 leaves):

$$\begin{aligned}
& \frac{1}{480 a^3 d \left(1 + \cos[c + dx]\right)^3} \\
& \cos\left[\frac{1}{2}(c + dx)\right] \sec\left[\frac{c}{2}\right] \left( -600(23A - 13B) dx \cos\left[\frac{dx}{2}\right] - 600(23A - 13B) dx \cos\left[c + \frac{dx}{2}\right] - \right. \\
& \quad 6900A dx \cos\left[c + \frac{3dx}{2}\right] + 3900B dx \cos\left[c + \frac{3dx}{2}\right] - 6900A dx \cos\left[2c + \frac{3dx}{2}\right] + \\
& \quad 3900B dx \cos\left[2c + \frac{3dx}{2}\right] - 1380A dx \cos\left[2c + \frac{5dx}{2}\right] + 780B dx \cos\left[2c + \frac{5dx}{2}\right] - \\
& \quad 1380A dx \cos\left[3c + \frac{5dx}{2}\right] + 780B dx \cos\left[3c + \frac{5dx}{2}\right] + 20410A \sin\left[\frac{dx}{2}\right] - 12760B \sin\left[\frac{dx}{2}\right] - \\
& \quad 11110A \sin\left[c + \frac{dx}{2}\right] + 7560B \sin\left[c + \frac{dx}{2}\right] + 15380A \sin\left[c + \frac{3dx}{2}\right] - 9230B \sin\left[c + \frac{3dx}{2}\right] - \\
& \quad 380A \sin\left[2c + \frac{3dx}{2}\right] + 930B \sin\left[2c + \frac{3dx}{2}\right] + 4777A \sin\left[2c + \frac{5dx}{2}\right] - 2782B \sin\left[2c + \frac{5dx}{2}\right] + \\
& \quad 1625A \sin\left[3c + \frac{5dx}{2}\right] - 750B \sin\left[3c + \frac{5dx}{2}\right] + 230A \sin\left[3c + \frac{7dx}{2}\right] - 105B \sin\left[3c + \frac{7dx}{2}\right] + \\
& \quad 230A \sin\left[4c + \frac{7dx}{2}\right] - 105B \sin\left[4c + \frac{7dx}{2}\right] - 20A \sin\left[4c + \frac{9dx}{2}\right] + 15B \sin\left[4c + \frac{9dx}{2}\right] - \\
& \quad \left. 20A \sin\left[5c + \frac{9dx}{2}\right] + 15B \sin\left[5c + \frac{9dx}{2}\right] + 5A \sin\left[5c + \frac{11dx}{2}\right] + 5A \sin\left[6c + \frac{11dx}{2}\right] \right)
\end{aligned}$$

**Problem 108: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^6 (A + B \sec[c + dx])}{(a + a \sec[c + dx])^4} dx$$

Optimal (type 3, 238 leaves, 9 steps):

$$\begin{aligned}
& - \frac{(8A - 21B) \operatorname{ArcTanh}[\sin[c + dx]]}{2a^4 d} + \\
& \frac{8(83A - 216B) \tan[c + dx]}{105a^4 d} - \frac{(8A - 21B) \sec[c + dx] \tan[c + dx]}{2a^4 d} + \\
& \frac{(52A - 129B) \sec[c + dx]^3 \tan[c + dx]}{105a^4 d (1 + \sec[c + dx])^2} + \frac{4(83A - 216B) \sec[c + dx]^2 \tan[c + dx]}{105a^4 d (1 + \sec[c + dx])} + \\
& \frac{(A - B) \sec[c + dx]^5 \tan[c + dx]}{7d (a + a \sec[c + dx])^4} + \frac{(A - 2B) \sec[c + dx]^4 \tan[c + dx]}{5a d (a + a \sec[c + dx])^3}
\end{aligned}$$

Result (type 3, 880 leaves):

$$\begin{aligned}
& - \left( \left( 8 (-8A + 21B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \right. \right. \\
& \quad \left. \left. \sec[c + dx]^3 (A + B \sec[c + dx]) \right) \right) / \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx])^4 \right) + \\
& \left( 8 (-8A + 21B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec[c + dx]^3 \right. \\
& \quad \left. (A + B \sec[c + dx]) \right) / \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx])^4 \right) + \\
& \quad 1 \\
& \hline
& 6720 d (B + A \cos[c + dx]) (a + a \sec[c + dx])^4 \\
& \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] \sec[c + dx]^5 (A + B \sec[c + dx]) \\
& \left( -38668 A \sin\left[\frac{dx}{2}\right] + 73206 B \sin\left[\frac{dx}{2}\right] + 64384 A \sin\left[\frac{3dx}{2}\right] - 166668 B \sin\left[\frac{3dx}{2}\right] - \right. \\
& \quad 70896 A \sin\left[c - \frac{dx}{2}\right] + 183162 B \sin\left[c - \frac{dx}{2}\right] + 50316 A \sin\left[c + \frac{dx}{2}\right] - 100842 B \sin\left[c + \frac{dx}{2}\right] - \\
& \quad 59248 A \sin\left[2c + \frac{dx}{2}\right] + 155526 B \sin\left[2c + \frac{dx}{2}\right] - 22820 A \sin\left[c + \frac{3dx}{2}\right] + \\
& \quad 37380 B \sin\left[c + \frac{3dx}{2}\right] + 48004 A \sin\left[2c + \frac{3dx}{2}\right] - 101148 B \sin\left[2c + \frac{3dx}{2}\right] - \\
& \quad 39200 A \sin\left[3c + \frac{3dx}{2}\right] + 102900 B \sin\left[3c + \frac{3dx}{2}\right] + 46032 A \sin\left[c + \frac{5dx}{2}\right] - \\
& \quad 119364 B \sin\left[c + \frac{5dx}{2}\right] - 8750 A \sin\left[2c + \frac{5dx}{2}\right] + 8820 B \sin\left[2c + \frac{5dx}{2}\right] + \\
& \quad 35742 A \sin\left[3c + \frac{5dx}{2}\right] - 78204 B \sin\left[3c + \frac{5dx}{2}\right] - \\
& \quad 19040 A \sin\left[4c + \frac{5dx}{2}\right] + 49980 B \sin\left[4c + \frac{5dx}{2}\right] + 24664 A \sin\left[2c + \frac{7dx}{2}\right] - \\
& \quad 64053 B \sin\left[2c + \frac{7dx}{2}\right] - 1050 A \sin\left[3c + \frac{7dx}{2}\right] - 3885 B \sin\left[3c + \frac{7dx}{2}\right] + \\
& \quad 19834 A \sin\left[4c + \frac{7dx}{2}\right] - 44733 B \sin\left[4c + \frac{7dx}{2}\right] - 5880 A \sin\left[5c + \frac{7dx}{2}\right] + \\
& \quad 15435 B \sin\left[5c + \frac{7dx}{2}\right] + 8456 A \sin\left[3c + \frac{9dx}{2}\right] - 21987 B \sin\left[3c + \frac{9dx}{2}\right] + \\
& \quad 630 A \sin\left[4c + \frac{9dx}{2}\right] - 3675 B \sin\left[4c + \frac{9dx}{2}\right] + 6986 A \sin\left[5c + \frac{9dx}{2}\right] - \\
& \quad 16107 B \sin\left[5c + \frac{9dx}{2}\right] - 840 A \sin\left[6c + \frac{9dx}{2}\right] + 2205 B \sin\left[6c + \frac{9dx}{2}\right] + \\
& \quad 1328 A \sin\left[4c + \frac{11dx}{2}\right] - 3456 B \sin\left[4c + \frac{11dx}{2}\right] + 210 A \sin\left[5c + \frac{11dx}{2}\right] - \\
& \quad \left. 840 B \sin\left[5c + \frac{11dx}{2}\right] + 1118 A \sin\left[6c + \frac{11dx}{2}\right] - 2616 B \sin\left[6c + \frac{11dx}{2}\right] \right)
\end{aligned}$$



### Problem 109: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec[c + dx]^5 (A + B \sec[c + dx])}{(a + a \sec[c + dx])^4} dx$$

Optimal (type 3, 194 leaves, 8 steps):

$$\begin{aligned} & \frac{(A - 4B) \operatorname{ArcTanh}[\sin[c + dx]]}{a^4 d} - \frac{(55A - 244B) \tan[c + dx]}{105 a^4 d} + \\ & \frac{(25A - 88B) \sec[c + dx]^2 \tan[c + dx]}{105 a^4 d (1 + \sec[c + dx])^2} - \frac{(A - 4B) \tan[c + dx]}{a^4 d (1 + \sec[c + dx])} + \\ & \frac{(A - B) \sec[c + dx]^4 \tan[c + dx]}{7 d (a + a \sec[c + dx])^4} + \frac{(5A - 12B) \sec[c + dx]^3 \tan[c + dx]}{35 a d (a + a \sec[c + dx])^3} \end{aligned}$$

Result (type 3, 754 leaves):

$$\begin{aligned} & \left( 16 (-A + 4B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec[c + dx]^3 (A + B \sec[c + dx]) \right) / \\ & \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx])^4 \right) - \\ & \left( 16 (-A + 4B) \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^8 \log\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right] \sec[c + dx]^3 (A + B \sec[c + dx]) \right) / \\ & \left( d (B + A \cos[c + dx]) (a + a \sec[c + dx])^4 \right) + \\ & \frac{1}{1680 d (B + A \cos[c + dx]) (a + a \sec[c + dx])^4} \cos\left[\frac{c}{2} + \frac{dx}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c] \sec[c + dx]^4 \\ & (A + B \sec[c + dx]) \left( 4165 A \sin\left[\frac{dx}{2}\right] - 10780 B \sin\left[\frac{dx}{2}\right] - 4445 A \sin\left[\frac{3 dx}{2}\right] + \right. \\ & 18788 B \sin\left[\frac{3 dx}{2}\right] + 4795 A \sin\left[c - \frac{dx}{2}\right] - 20524 B \sin\left[c - \frac{dx}{2}\right] - 4795 A \sin\left[c + \frac{dx}{2}\right] + \\ & 14644 B \sin\left[c + \frac{dx}{2}\right] + 4165 A \sin\left[2c + \frac{dx}{2}\right] - 16660 B \sin\left[2c + \frac{dx}{2}\right] + 2275 A \sin\left[c + \frac{3 dx}{2}\right] - \\ & 4690 B \sin\left[c + \frac{3 dx}{2}\right] - 4445 A \sin\left[2c + \frac{3 dx}{2}\right] + 14378 B \sin\left[2c + \frac{3 dx}{2}\right] + \\ & 2275 A \sin\left[3c + \frac{3 dx}{2}\right] - 9100 B \sin\left[3c + \frac{3 dx}{2}\right] - 2785 A \sin\left[c + \frac{5 dx}{2}\right] + \\ & 11668 B \sin\left[c + \frac{5 dx}{2}\right] + 735 A \sin\left[2c + \frac{5 dx}{2}\right] - 630 B \sin\left[2c + \frac{5 dx}{2}\right] - \\ & 2785 A \sin\left[3c + \frac{5 dx}{2}\right] + 9358 B \sin\left[3c + \frac{5 dx}{2}\right] + 735 A \sin\left[4c + \frac{5 dx}{2}\right] - \\ & 2940 B \sin\left[4c + \frac{5 dx}{2}\right] - 1015 A \sin\left[2c + \frac{7 dx}{2}\right] + 4228 B \sin\left[2c + \frac{7 dx}{2}\right] + \\ & 105 A \sin\left[3c + \frac{7 dx}{2}\right] + 315 B \sin\left[3c + \frac{7 dx}{2}\right] - 1015 A \sin\left[4c + \frac{7 dx}{2}\right] + \\ & 3493 B \sin\left[4c + \frac{7 dx}{2}\right] + 105 A \sin\left[5c + \frac{7 dx}{2}\right] - 420 B \sin\left[5c + \frac{7 dx}{2}\right] - 160 A \sin\left[3c + \frac{9 dx}{2}\right] + \\ & \left. 664 B \sin\left[3c + \frac{9 dx}{2}\right] + 105 B \sin\left[4c + \frac{9 dx}{2}\right] - 160 A \sin\left[5c + \frac{9 dx}{2}\right] + 559 B \sin\left[5c + \frac{9 dx}{2}\right] \right) \end{aligned}$$

**Problem 114: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x]}{(a + a \sec [c + d x])^4} dx$$

Optimal (type 3, 138 leaves, 5 steps):

$$\frac{A x}{a^4} - \frac{(55 A - 6 B) \tan [c + d x]}{105 a^4 d (1 + \sec [c + d x])^2} - \frac{2 (80 A - 3 B) \tan [c + d x]}{105 a^4 d (1 + \sec [c + d x])} - \frac{(A - B) \tan [c + d x]}{7 d (a + a \sec [c + d x])^4} - \frac{(10 A - 3 B) \tan [c + d x]}{35 a d (a + a \sec [c + d x])^3}$$

Result (type 3, 329 leaves):

$$\frac{1}{13440 a^4 d} \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{1}{2} (c + d x) \right]^7 \left( 3675 A d x \cos \left[ \frac{d x}{2} \right] + 3675 A d x \cos \left[ c + \frac{d x}{2} \right] + 2205 A d x \cos \left[ c + \frac{3 d x}{2} \right] + 2205 A d x \cos \left[ 2 c + \frac{3 d x}{2} \right] + 735 A d x \cos \left[ 2 c + \frac{5 d x}{2} \right] + 735 A d x \cos \left[ 3 c + \frac{5 d x}{2} \right] + 105 A d x \cos \left[ 3 c + \frac{7 d x}{2} \right] + 105 A d x \cos \left[ 4 c + \frac{7 d x}{2} \right] - 9940 A \sin \left[ \frac{d x}{2} \right] + 1260 B \sin \left[ \frac{d x}{2} \right] + 8260 A \sin \left[ c + \frac{d x}{2} \right] - 1260 B \sin \left[ c + \frac{d x}{2} \right] - 7140 A \sin \left[ c + \frac{3 d x}{2} \right] + 882 B \sin \left[ c + \frac{3 d x}{2} \right] + 3780 A \sin \left[ 2 c + \frac{3 d x}{2} \right] - 630 B \sin \left[ 2 c + \frac{3 d x}{2} \right] - 2800 A \sin \left[ 2 c + \frac{5 d x}{2} \right] + 294 B \sin \left[ 2 c + \frac{5 d x}{2} \right] + 840 A \sin \left[ 3 c + \frac{5 d x}{2} \right] - 210 B \sin \left[ 3 c + \frac{5 d x}{2} \right] - 520 A \sin \left[ 3 c + \frac{7 d x}{2} \right] + 72 B \sin \left[ 3 c + \frac{7 d x}{2} \right] \right)$$

**Problem 115: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x] (A + B \sec [c + d x])}{(a + a \sec [c + d x])^4} dx$$

Optimal (type 3, 166 leaves, 7 steps):

$$-\frac{(4 A - B) x}{a^4} + \frac{8 (83 A - 20 B) \sin [c + d x]}{105 a^4 d} - \frac{(88 A - 25 B) \sin [c + d x]}{105 a^4 d (1 + \sec [c + d x])^2} - \frac{(4 A - B) \sin [c + d x]}{a^4 d (1 + \sec [c + d x])} - \frac{(A - B) \sin [c + d x]}{7 d (a + a \sec [c + d x])^4} - \frac{(12 A - 5 B) \sin [c + d x]}{35 a d (a + a \sec [c + d x])^3}$$

Result (type 3, 485 leaves):

$$\begin{aligned}
& \frac{1}{1680 a^4 d \left(1 + \cos[c + d x]\right)^4} \\
& \cos\left[\frac{1}{2}(c + d x)\right] \sec\left[\frac{c}{2}\right] \left( -7350 (4A - B) d x \cos\left[\frac{d x}{2}\right] - 7350 (4A - B) d x \cos\left[c + \frac{d x}{2}\right] - \right. \\
& 17640 A d x \cos\left[c + \frac{3 d x}{2}\right] + 4410 B d x \cos\left[c + \frac{3 d x}{2}\right] - 17640 A d x \cos\left[2c + \frac{3 d x}{2}\right] + \\
& 4410 B d x \cos\left[2c + \frac{3 d x}{2}\right] - 5880 A d x \cos\left[2c + \frac{5 d x}{2}\right] + 1470 B d x \cos\left[2c + \frac{5 d x}{2}\right] - \\
& 5880 A d x \cos\left[3c + \frac{5 d x}{2}\right] + 1470 B d x \cos\left[3c + \frac{5 d x}{2}\right] - 840 A d x \cos\left[3c + \frac{7 d x}{2}\right] + \\
& 210 B d x \cos\left[3c + \frac{7 d x}{2}\right] - 840 A d x \cos\left[4c + \frac{7 d x}{2}\right] + 210 B d x \cos\left[4c + \frac{7 d x}{2}\right] + \\
& 60830 A \sin\left[\frac{d x}{2}\right] - 19880 B \sin\left[\frac{d x}{2}\right] - 46130 A \sin\left[c + \frac{d x}{2}\right] + 16520 B \sin\left[c + \frac{d x}{2}\right] + \\
& 46116 A \sin\left[c + \frac{3 d x}{2}\right] - 14280 B \sin\left[c + \frac{3 d x}{2}\right] - 18060 A \sin\left[2c + \frac{3 d x}{2}\right] + \\
& 7560 B \sin\left[2c + \frac{3 d x}{2}\right] + 19292 A \sin\left[2c + \frac{5 d x}{2}\right] - 5600 B \sin\left[2c + \frac{5 d x}{2}\right] - \\
& 2100 A \sin\left[3c + \frac{5 d x}{2}\right] + 1680 B \sin\left[3c + \frac{5 d x}{2}\right] + 3791 A \sin\left[3c + \frac{7 d x}{2}\right] - \\
& \left. 1040 B \sin\left[3c + \frac{7 d x}{2}\right] + 735 A \sin\left[4c + \frac{7 d x}{2}\right] + 105 A \sin\left[4c + \frac{9 d x}{2}\right] + 105 A \sin\left[5c + \frac{9 d x}{2}\right] \right)
\end{aligned}$$

**Problem 116: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + d x]^2 (A + B \sec[c + d x])}{(a + a \sec[c + d x])^4} dx$$

Optimal (type 3, 223 leaves, 8 steps):

$$\begin{aligned}
& \frac{(21A - 8B)x}{2a^4} - \frac{8(216A - 83B) \sin[c + d x]}{105a^4 d} + \frac{(21A - 8B) \cos[c + d x] \sin[c + d x]}{2a^4 d} - \\
& \frac{(129A - 52B) \cos[c + d x] \sin[c + d x]}{105a^4 d (1 + \sec[c + d x])^2} - \frac{4(216A - 83B) \cos[c + d x] \sin[c + d x]}{105a^4 d (1 + \sec[c + d x])} - \\
& \frac{(A - B) \cos[c + d x] \sin[c + d x]}{7d (a + a \sec[c + d x])^4} - \frac{(2A - B) \cos[c + d x] \sin[c + d x]}{5a d (a + a \sec[c + d x])^3}
\end{aligned}$$

Result (type 3, 555 leaves):

$$\begin{aligned}
& \frac{1}{6720 a^4 d \left(1 + \cos[c + dx]\right)^4} \\
& \cos\left[\frac{1}{2}(c + dx)\right] \sec\left[\frac{c}{2}\right] \left(14700 (21A - 8B) dx \cos\left[\frac{dx}{2}\right] + 14700 (21A - 8B) dx \cos\left[c + \frac{dx}{2}\right] + \right. \\
& 185220 A dx \cos\left[c + \frac{3dx}{2}\right] - 70560 B dx \cos\left[c + \frac{3dx}{2}\right] + 185220 A dx \cos\left[2c + \frac{3dx}{2}\right] - \\
& 70560 B dx \cos\left[2c + \frac{3dx}{2}\right] + 61740 A dx \cos\left[2c + \frac{5dx}{2}\right] - 23520 B dx \cos\left[2c + \frac{5dx}{2}\right] + \\
& 61740 A dx \cos\left[3c + \frac{5dx}{2}\right] - 23520 B dx \cos\left[3c + \frac{5dx}{2}\right] + 8820 A dx \cos\left[3c + \frac{7dx}{2}\right] - \\
& 3360 B dx \cos\left[3c + \frac{7dx}{2}\right] + 8820 A dx \cos\left[4c + \frac{7dx}{2}\right] - 3360 B dx \cos\left[4c + \frac{7dx}{2}\right] - \\
& 539490 A \sin\left[\frac{dx}{2}\right] + 243320 B \sin\left[\frac{dx}{2}\right] + 386190 A \sin\left[c + \frac{dx}{2}\right] - 184520 B \sin\left[c + \frac{dx}{2}\right] - \\
& 422478 A \sin\left[c + \frac{3dx}{2}\right] + 184464 B \sin\left[c + \frac{3dx}{2}\right] + 132930 A \sin\left[2c + \frac{3dx}{2}\right] - \\
& 72240 B \sin\left[2c + \frac{3dx}{2}\right] - 181461 A \sin\left[2c + \frac{5dx}{2}\right] + 77168 B \sin\left[2c + \frac{5dx}{2}\right] + \\
& 3675 A \sin\left[3c + \frac{5dx}{2}\right] - 8400 B \sin\left[3c + \frac{5dx}{2}\right] - 36003 A \sin\left[3c + \frac{7dx}{2}\right] + \\
& 15164 B \sin\left[3c + \frac{7dx}{2}\right] - 9555 A \sin\left[4c + \frac{7dx}{2}\right] + 2940 B \sin\left[4c + \frac{7dx}{2}\right] - \\
& 945 A \sin\left[4c + \frac{9dx}{2}\right] + 420 B \sin\left[4c + \frac{9dx}{2}\right] - 945 A \sin\left[5c + \frac{9dx}{2}\right] + \\
& \left. 420 B \sin\left[5c + \frac{9dx}{2}\right] + 105 A \sin\left[5c + \frac{11dx}{2}\right] + 105 A \sin\left[6c + \frac{11dx}{2}\right]\right)
\end{aligned}$$

**Problem 117: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + dx]^3 (A + B \sec[c + dx])}{(a + a \sec[c + dx])^4} dx$$

Optimal (type 3, 256 leaves, 9 steps):

$$\begin{aligned}
& -\frac{(44A - 21B)x}{2a^4} + \frac{8(227A - 108B)\sin[c + dx]}{35a^4d} - \\
& \frac{(44A - 21B)\cos[c + dx]\sin[c + dx]}{2a^4d} - \frac{(178A - 87B)\cos[c + dx]^2\sin[c + dx]}{105a^4d(1 + \sec[c + dx])^2} - \\
& \frac{(44A - 21B)\cos[c + dx]^2\sin[c + dx]}{3a^4d(1 + \sec[c + dx])} - \frac{(A - B)\cos[c + dx]^2\sin[c + dx]}{7d(a + a \sec[c + dx])^4} - \\
& \frac{(16A - 9B)\cos[c + dx]^2\sin[c + dx]}{35ad(a + a \sec[c + dx])^3} - \frac{8(227A - 108B)\sin[c + dx]^3}{105a^4d}
\end{aligned}$$

Result (type 3, 611 leaves):

$$\begin{aligned}
& \frac{1}{6720 a^4 d \left(1 + \cos[c + d x]\right)^4} \\
& \cos\left[\frac{1}{2}(c + d x)\right] \sec\left[\frac{c}{2}\right] \left( -14700 (44 A - 21 B) d x \cos\left[\frac{d x}{2}\right] - 14700 (44 A - 21 B) d x \cos\left[c + \frac{d x}{2}\right] - \right. \\
& \quad 388080 A d x \cos\left[c + \frac{3 d x}{2}\right] + 185220 B d x \cos\left[c + \frac{3 d x}{2}\right] - 388080 A d x \cos\left[2 c + \frac{3 d x}{2}\right] + \\
& \quad 185220 B d x \cos\left[2 c + \frac{3 d x}{2}\right] - 129360 A d x \cos\left[2 c + \frac{5 d x}{2}\right] + 61740 B d x \cos\left[2 c + \frac{5 d x}{2}\right] - \\
& \quad 129360 A d x \cos\left[3 c + \frac{5 d x}{2}\right] + 61740 B d x \cos\left[3 c + \frac{5 d x}{2}\right] - 18480 A d x \cos\left[3 c + \frac{7 d x}{2}\right] + \\
& \quad 8820 B d x \cos\left[3 c + \frac{7 d x}{2}\right] - 18480 A d x \cos\left[4 c + \frac{7 d x}{2}\right] + 8820 B d x \cos\left[4 c + \frac{7 d x}{2}\right] + \\
& \quad 1010660 A \sin\left[\frac{d x}{2}\right] - 539490 B \sin\left[\frac{d x}{2}\right] - 687260 A \sin\left[c + \frac{d x}{2}\right] + 386190 B \sin\left[c + \frac{d x}{2}\right] + \\
& \quad 814107 A \sin\left[c + \frac{3 d x}{2}\right] - 422478 B \sin\left[c + \frac{3 d x}{2}\right] - 204645 A \sin\left[2 c + \frac{3 d x}{2}\right] + \\
& \quad 132930 B \sin\left[2 c + \frac{3 d x}{2}\right] + 357609 A \sin\left[2 c + \frac{5 d x}{2}\right] - 181461 B \sin\left[2 c + \frac{5 d x}{2}\right] + \\
& \quad 18025 A \sin\left[3 c + \frac{5 d x}{2}\right] + 3675 B \sin\left[3 c + \frac{5 d x}{2}\right] + 72522 A \sin\left[3 c + \frac{7 d x}{2}\right] - \\
& \quad 36003 B \sin\left[3 c + \frac{7 d x}{2}\right] + 24010 A \sin\left[4 c + \frac{7 d x}{2}\right] - 9555 B \sin\left[4 c + \frac{7 d x}{2}\right] + \\
& \quad 2310 A \sin\left[4 c + \frac{9 d x}{2}\right] - 945 B \sin\left[4 c + \frac{9 d x}{2}\right] + 2310 A \sin\left[5 c + \frac{9 d x}{2}\right] - \\
& \quad 945 B \sin\left[5 c + \frac{9 d x}{2}\right] - 175 A \sin\left[5 c + \frac{11 d x}{2}\right] + 105 B \sin\left[5 c + \frac{11 d x}{2}\right] - \\
& \quad \left. 175 A \sin\left[6 c + \frac{11 d x}{2}\right] + 105 B \sin\left[6 c + \frac{11 d x}{2}\right] + 35 A \sin\left[6 c + \frac{13 d x}{2}\right] + 35 A \sin\left[7 c + \frac{13 d x}{2}\right] \right)
\end{aligned}$$

Problem 122: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{a + a \sec[c + d x]} (A + B \sec[c + d x]) dx$$

Optimal (type 3, 66 leaves, 4 steps):

$$\frac{2 \sqrt{a} A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c + d x]}{\sqrt{a + a \sec[c + d x]}}\right]}{d} + \frac{2 a B \tan[c + d x]}{d \sqrt{a + a \sec[c + d x]}}$$

Result (type 4, 407 leaves):

$$\begin{aligned}
& -\frac{1}{d (B + A \cos [c + d x])} 8 (-3 - 2 \sqrt{2}) A \cos \left[ \frac{1}{4} (c + d x) \right]^4 \\
& \sqrt{\frac{7 - 5 \sqrt{2} + (10 - 7 \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right]}{1 + \cos \left[ \frac{1}{2} (c + d x) \right]}} \\
& \left( 1 - \sqrt{2} + (-2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \left( \text{EllipticF} \left[ \text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] + \right. \\
& \left. 2 \text{EllipticPi} \left[ -3 + 2 \sqrt{2}, -\text{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right) \\
& \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \cos \left[ \frac{1}{2} (c + d x) \right] \right) \sec \left[ \frac{1}{4} (c + d x) \right]^2 \sec \left[ \frac{1}{2} (c + d x) \right]} \\
& \sqrt{a (1 + \sec [c + d x])} (A + B \sec [c + d x]) \sqrt{3 - 2 \sqrt{2} - \tan \left[ \frac{1}{4} (c + d x) \right]^2} + \\
& \left( 2 B \cos [c + d x] \sqrt{a (1 + \sec [c + d x])} (A + B \sec [c + d x]) \tan \left[ \frac{1}{2} (c + d x) \right] \right) / \\
& (d (B + A \cos [c + d x]))
\end{aligned}$$

**Problem 123: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] \sqrt{a + a \sec [c + d x]} (A + B \sec [c + d x]) dx$$

Optimal (type 3, 68 leaves, 3 steps):

$$\frac{\sqrt{a} (A + 2 B) \text{ArcTan} \left[ \frac{\sqrt{a} \tan [c + d x]}{\sqrt{a + a \sec [c + d x]}} \right]}{d} + \frac{a A \sin [c + d x]}{d \sqrt{a + a \sec [c + d x]}}$$

Result (type 4, 396 leaves):

$$\begin{aligned}
& \frac{1}{d} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \left(-\frac{1}{2} A \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2} A \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]\right) - \\
& \frac{1}{d} 4(-3-2\sqrt{2})(A+2B) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\
& \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \left(1-\sqrt{2}+(-2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \\
& \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
& \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]\right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]} \\
& \operatorname{Sec}[c+dx] \sqrt{a(1+\operatorname{Sec}[c+dx])} \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 124: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Cos}[c+dx]^2 \sqrt{a+a \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 117 leaves, 4 steps):

$$\frac{\sqrt{a} (3A+4B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4d} + \frac{a (3A+4B) \operatorname{Sin}[c+dx]}{4d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a A \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{2d \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 4, 418 leaves):

$$\begin{aligned}
& \frac{1}{d} \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\sec[c+dx])} \\
& \left(-\frac{1}{8}(A+4B) \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{4}(A+2B) \sin\left[\frac{3}{2}(c+dx)\right] + \frac{1}{8}A \sin\left[\frac{5}{2}(c+dx)\right]\right) + \\
& \frac{1}{d} \left(2 + \frac{3}{\sqrt{2}}\right) (3A+4B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2} + (10-7\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \left(1-\sqrt{2} + (-2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \left(\text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \left. 2 \text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
& \sqrt{\left(-1+\sqrt{2} - (-2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left(-1-\sqrt{2} + (2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]} \\
& \sec[c+dx] \sqrt{a(1+\sec[c+dx])} \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 125: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 \sqrt{a+a \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 160 leaves, 5 steps):

$$\begin{aligned}
& \frac{\sqrt{a} (5A+6B) \text{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{8d} + \frac{a (5A+6B) \sin[c+dx]}{8d \sqrt{a+a \sec[c+dx]}} + \\
& \frac{a (5A+6B) \cos[c+dx] \sin[c+dx]}{12d \sqrt{a+a \sec[c+dx]}} + \frac{a A \cos[c+dx]^2 \sin[c+dx]}{3d \sqrt{a+a \sec[c+dx]}}
\end{aligned}$$

Result (type 4, 443 leaves):



$$\begin{aligned}
& \frac{1}{d} \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\sec[c+dx])} \left( -\frac{1}{48} (11A+6B) \sin\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{1}{12} (4A+3B) \sin\left[\frac{3}{2}(c+dx)\right] + \frac{1}{16} (A+2B) \sin\left[\frac{5}{2}(c+dx)\right] + \frac{1}{24} A \sin\left[\frac{7}{2}(c+dx)\right] \right) + \\
& \frac{1}{d} \left( 1 + \frac{3}{2\sqrt{2}} \right) (5A+6B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \left( 1 - \sqrt{2} + (-2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right] \right) \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \quad \left. 2 \text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
& \sqrt{\left( -1 + \sqrt{2} - (-2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right] \right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left( -1 - \sqrt{2} + (2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right] \right) \sec\left[\frac{1}{4}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]} \\
& \sec[c+dx] \sqrt{a(1+\sec[c+dx])} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 126: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^4 \sqrt{a+a \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 203 leaves, 6 steps):

$$\begin{aligned}
& \frac{5\sqrt{a}(7A+8B) \text{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{64d} + \\
& \frac{5a(7A+8B) \sin[c+dx]}{64d\sqrt{a+a \sec[c+dx]}} + \frac{5a(7A+8B) \cos[c+dx] \sin[c+dx]}{96d\sqrt{a+a \sec[c+dx]}} + \\
& \frac{a(7A+8B) \cos[c+dx]^2 \sin[c+dx]}{24d\sqrt{a+a \sec[c+dx]}} + \frac{aA \cos[c+dx]^3 \sin[c+dx]}{4d\sqrt{a+a \sec[c+dx]}}
\end{aligned}$$

Result (type 4, 465 leaves):

$$\begin{aligned}
& \frac{1}{d} \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\sec[c+dx])} \\
& \left( -\frac{1}{384} (41A+88B) \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{48} (11A+16B) \sin\left[\frac{3}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{1}{128} (15A+8B) \sin\left[\frac{5}{2}(c+dx)\right] + \frac{1}{48} (A+2B) \sin\left[\frac{7}{2}(c+dx)\right] + \frac{1}{64} A \sin\left[\frac{9}{2}(c+dx)\right] \right) + \\
& \frac{1}{(-64+48\sqrt{2})d} 5(7A+8B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \left( (1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]) \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \right. \\
& \quad \left. \left. 2\text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \right) \\
& \sqrt{\left( -1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right] \right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left( -1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right] \right) \sec\left[\frac{1}{4}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]} \\
& \sec[c+dx] \sqrt{a(1+\sec[c+dx])} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 130: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (a+a \sec[c+dx])^{3/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 105 leaves, 5 steps):

$$\frac{2a^{3/2}A \text{ArcTan}\left[\frac{\sqrt{a}\tan[c+dx]}{\sqrt{a+a\sec[c+dx]}}\right]}{d} + \frac{2a^2(3A+4B)\tan[c+dx]}{3d\sqrt{a+a\sec[c+dx]}} + \frac{2aB\sqrt{a+a\sec[c+dx]}\tan[c+dx]}{3d}$$

Result (type 4, 460 leaves):

$$\begin{aligned}
& \left( \cos[c+dx]^2 \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2} (A+B \sec[c+dx]) \right. \\
& \quad \left. \left( \frac{1}{3}(3A+5B) \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{3}B \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / (d(B+A \cos[c+dx])) - \\
& \frac{1}{d(B+A \cos[c+dx])} 4(-3-2\sqrt{2}) A \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \left(1-\sqrt{2}+(-2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \\
& \cos[c+dx] \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \quad \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
& \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^3} \\
& (a(1+\sec[c+dx]))^{3/2} (A+B \sec[c+dx]) \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 131: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx] (a+a \sec[c+dx])^{3/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 103 leaves, 4 steps):

$$\begin{aligned}
& \frac{a^{3/2} (3A+2B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{d} + \\
& \frac{a^2 (A-2B) \sin[c+dx]}{d \sqrt{a+a \sec[c+dx]}} + \frac{2aB \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{d}
\end{aligned}$$

Result (type 4, 408 leaves):

$$\begin{aligned}
& \frac{1}{d} \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2} \\
& \left( \frac{1}{4}(-A+4B) \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{4}A \sin\left[\frac{3}{2}(c+dx)\right] \right) - \\
& \frac{1}{d} 2(-3-2\sqrt{2}) (3A+2B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \\
& \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
& \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^3} \\
& \left(a(1+\sec[c+dx])\right)^{3/2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 132: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^2 (a+a \sec[c+dx])^{3/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 119 leaves, 4 steps):

$$\begin{aligned}
& \frac{a^{3/2} (7A+12B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{4d} + \\
& \frac{a^2 (5A+4B) \sin[c+dx]}{4d \sqrt{a+a \sec[c+dx]}} + \frac{aA \cos[c+dx] \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{2d}
\end{aligned}$$

Result (type 4, 428 leaves):

$$\begin{aligned}
& \frac{1}{d} \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2} \\
& \left(-\frac{1}{16}(5A+4B)\sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{8}(3A+2B)\sin\left[\frac{3}{2}(c+dx)\right] + \frac{1}{16}A\sin\left[\frac{5}{2}(c+dx)\right]\right) + \\
& \frac{1}{d} \left(1 + \frac{3}{2\sqrt{2}}\right) (7A+12B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2} + (10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \left(1-\sqrt{2} + (-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \left. 2\operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
& \sqrt{\left(-1+\sqrt{2} - (-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left(-1-\sqrt{2} + (2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2} \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 133: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 (a+a\sec[c+dx])^{3/2} (A+B\sec[c+dx]) dx$$

Optimal (type 3, 164 leaves, 5 steps):

$$\begin{aligned}
& \frac{a^{3/2} (11A+14B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a\sec[c+dx]}}\right]}{8d} + \frac{a^2 (11A+14B) \sin[c+dx]}{8d \sqrt{a+a\sec[c+dx]}} + \\
& \frac{a^2 (7A+6B) \cos[c+dx] \sin[c+dx]}{12d \sqrt{a+a\sec[c+dx]}} + \frac{aA \cos[c+dx]^2 \sqrt{a+a\sec[c+dx]} \sin[c+dx]}{3d}
\end{aligned}$$

Result (type 4, 450 leaves):

$$\begin{aligned}
& \frac{1}{d} \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2} \\
& \left(-\frac{1}{96}(17A+30B)\sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{24}(7A+9B)\sin\left[\frac{3}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{1}{32}(3A+2B)\sin\left[\frac{5}{2}(c+dx)\right] + \frac{1}{48}A\sin\left[\frac{7}{2}(c+dx)\right]\right) + \\
& \frac{1}{8d} (4+3\sqrt{2}) (11A+14B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2} + (10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \left(1-\sqrt{2} + (-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \quad \left. 2\operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
& \sqrt{\left(-1+\sqrt{2} - (-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left(-1-\sqrt{2} + (2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2} \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 134: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^4 (a+a\sec[c+dx])^{3/2} (A+B\sec[c+dx]) dx$$

Optimal (type 3, 209 leaves, 6 steps):

$$\begin{aligned}
& \frac{a^{3/2} (75A+88B) \operatorname{ArcTan}\left[\frac{\sqrt{a}\tan[c+dx]}{\sqrt{a+a\sec[c+dx]}}\right]}{64d} + \\
& \frac{a^2 (75A+88B) \sin[c+dx]}{64d\sqrt{a+a\sec[c+dx]}} + \frac{a^2 (75A+88B) \cos[c+dx] \sin[c+dx]}{96d\sqrt{a+a\sec[c+dx]}} + \\
& \frac{a^2 (9A+8B) \cos[c+dx]^2 \sin[c+dx]}{24d\sqrt{a+a\sec[c+dx]}} + \frac{aA \cos[c+dx]^3 \sqrt{a+a\sec[c+dx]} \sin[c+dx]}{4d}
\end{aligned}$$

Result (type 4, 471 leaves):

$$\begin{aligned}
& \frac{1}{d} \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2} \\
& \left( -\frac{1}{768} (129A+136B) \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{96} (27A+28B) \sin\left[\frac{3}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{1}{256} (23A+24B) \sin\left[\frac{5}{2}(c+dx)\right] + \frac{1}{96} (3A+2B) \sin\left[\frac{7}{2}(c+dx)\right] + \frac{1}{128} A \sin\left[\frac{9}{2}(c+dx)\right] \right) + \\
& \frac{1}{64d} (4+3\sqrt{2}) (75A+88B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \left( (1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]) \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \right. \\
& \quad \left. \left. 2\text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \right) \\
& \sqrt{\left( -1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right] \right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left( -1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right] \right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 138: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int (a+a \sec[c+dx])^{5/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 142 leaves, 6 steps):

$$\begin{aligned}
& \frac{2a^{5/2}A \text{ArcTan}\left[\frac{\sqrt{a}\tan[c+dx]}{\sqrt{a+a\sec[c+dx]}}\right]}{d} + \frac{2a^3(35A+32B)\tan[c+dx]}{15d\sqrt{a+a\sec[c+dx]}} + \\
& \frac{2a^2(5A+8B)\sqrt{a+a\sec[c+dx]}\tan[c+dx]}{15d} + \frac{2aB(a+a\sec[c+dx])^{3/2}\tan[c+dx]}{5d}
\end{aligned}$$

Result (type 4, 501 leaves):

$$\begin{aligned}
 & \left( \cos [c+d x]^3 \sec \left[ \frac{1}{2} (c+d x) \right]^5 (a (1+\sec [c+d x]))^{5/2} (A+B \sec [c+d x]) \right. \\
 & \quad \left( \frac{1}{30} (40 A+43 B) \sin \left[ \frac{1}{2} (c+d x) \right] + \frac{1}{10} B \sec [c+d x]^2 \sin \left[ \frac{1}{2} (c+d x) \right] + \right. \\
 & \quad \left. \left. \frac{1}{30} \sec [c+d x] \left( 5 A \sin \left[ \frac{1}{2} (c+d x) \right] + 14 B \sin \left[ \frac{1}{2} (c+d x) \right] \right) \right) \right) / (d (B+A \cos [c+d x])) - \\
 & \frac{1}{d (B+A \cos [c+d x])^2 (-3-2 \sqrt{2}) A \cos \left[ \frac{1}{4} (c+d x) \right]^4} \sqrt{\frac{7-5 \sqrt{2}+(10-7 \sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right]}{1+\cos \left[ \frac{1}{2} (c+d x) \right]}} \\
 & \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right]}{1+\cos \left[ \frac{1}{2} (c+d x) \right]}} \left( 1-\sqrt{2}+(-2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \\
 & \cos [c+d x]^2 \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] + \right. \\
 & \quad \left. 2 \operatorname{EllipticPi} \left[ -3+2 \sqrt{2}, -\operatorname{ArcSin} \left[ \frac{\tan \left[ \frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] \right) \\
 & \sqrt{\left( -1-\sqrt{2}+(2+\sqrt{2}) \cos \left[ \frac{1}{2} (c+d x) \right] \right) \sec \left[ \frac{1}{4} (c+d x) \right]^2 \sec \left[ \frac{1}{2} (c+d x) \right]^5} \\
 & (a (1+\sec [c+d x]))^{5/2} (A+B \sec [c+d x]) \sqrt{3-2 \sqrt{2}-\tan \left[ \frac{1}{4} (c+d x) \right]^2}
 \end{aligned}$$

**Problem 139: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x] (a+a \sec [c+d x])^{5/2} (A+B \sec [c+d x]) dx$$

Optimal (type 3, 143 leaves, 5 steps):

$$\begin{aligned}
 & \frac{a^{5/2} (5 A+2 B) \operatorname{ArcTan} \left[ \frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}} \right]}{d} - \frac{a^3 (3 A+14 B) \sin [c+d x]}{3 d \sqrt{a+a \sec [c+d x]}} + \\
 & \frac{2 a^2 (A+2 B) \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{d} + \frac{2 a B (a+a \sec [c+d x])^{3/2} \sin [c+d x]}{3 d}
 \end{aligned}$$

Result (type 4, 434 leaves):



$$\begin{aligned}
& \frac{1}{d} \cos[c+dx]^2 \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \\
& \left( \frac{1}{24} (9A+32B) \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{6} B \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{8} A \sin\left[\frac{3}{2}(c+dx)\right] \right) + \\
& \frac{1}{d} \left(2 + \frac{3}{\sqrt{2}}\right) (5A+2B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2} + (10-7\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \left(1 - \sqrt{2} + (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \cos[c+dx] \\
& \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \quad \left. 2 \text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
& \sqrt{\left(-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left(-1 - \sqrt{2} + (2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 140: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^2 (a+a \sec[c+dx])^{5/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 154 leaves, 5 steps):

$$\begin{aligned}
& \frac{a^{5/2} (19A+20B) \text{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{4d} + \frac{a^3 (9A-4B) \sin[c+dx]}{4d \sqrt{a+a \sec[c+dx]}} - \\
& \frac{a^2 (A-4B) \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{2d} + \frac{a A \cos[c+dx] (a+a \sec[c+dx])^{3/2} \sin[c+dx]}{2d}
\end{aligned}$$

Result (type 4, 437 leaves):

$$\begin{aligned}
& \frac{1}{d} \cos[c+dx]^2 \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \\
& \left( \frac{3}{32} (-3A+4B) \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{16} (5A+2B) \sin\left[\frac{3}{2}(c+dx)\right] + \frac{1}{32} A \sin\left[\frac{5}{2}(c+dx)\right] \right) + \\
& \frac{1}{8d} (4+3\sqrt{2}) (19A+20B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \left(1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \cos[c+dx] \\
& \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \quad \left. 2 \text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
& \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 141: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 (a+a \sec[c+dx])^{5/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 164 leaves, 5 steps):

$$\begin{aligned}
& \frac{a^{5/2} (25A+38B) \text{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{8d} + \frac{a^3 (49A+54B) \sin[c+dx]}{24d \sqrt{a+a \sec[c+dx]}} + \\
& \frac{a^2 (3A+2B) \cos[c+dx] \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{4d} + \\
& \frac{a A \cos[c+dx]^2 (a+a \sec[c+dx])^{3/2} \sin[c+dx]}{3d}
\end{aligned}$$

Result (type 4, 458 leaves):

$$\begin{aligned}
& \frac{1}{d} \cos[c+dx]^2 \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \\
& \left( -\frac{1}{192} (47A+54B) \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{48} (16A+15B) \sin\left[\frac{3}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{1}{64} (5A+2B) \sin\left[\frac{5}{2}(c+dx)\right] + \frac{1}{96} A \sin\left[\frac{7}{2}(c+dx)\right] \right) + \\
& \frac{1}{8d} \left( 2 + \frac{3}{\sqrt{2}} \right) (25A+38B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\
& \left( 1 - \sqrt{2} + (-2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right] \right) \cos[c+dx] \\
& \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\
& \quad \left. 2 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\
& \sqrt{\left( -1 + \sqrt{2} - (-2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right] \right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left( -1 - \sqrt{2} + (2+\sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right] \right) \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

**Problem 142: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^4 \left(a+a \sec[c+dx]\right)^{5/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 209 leaves, 6 steps):

$$\begin{aligned}
& \frac{a^{5/2} (163A+200B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{64d} + \\
& \frac{a^3 (163A+200B) \sin[c+dx]}{64d \sqrt{a+a \sec[c+dx]}} + \frac{a^3 (95A+104B) \cos[c+dx] \sin[c+dx]}{96d \sqrt{a+a \sec[c+dx]}} + \\
& \frac{a^2 (11A+8B) \cos[c+dx]^2 \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{24d} + \\
& \frac{a A \cos[c+dx]^3 (a+a \sec[c+dx])^{3/2} \sin[c+dx]}{4d}
\end{aligned}$$

Result (type 4, 479 leaves):

$$\begin{aligned} & \frac{1}{d} \cos[c+dx]^2 \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \\ & \left( -\frac{(265A+376B)\sin\left[\frac{1}{2}(c+dx)\right]}{1536} + \frac{1}{192}(55A+64B)\sin\left[\frac{3}{2}(c+dx)\right] + \right. \\ & \quad \left. \frac{1}{512}(47A+40B)\sin\left[\frac{5}{2}(c+dx)\right] + \frac{1}{192}(5A+2B)\sin\left[\frac{7}{2}(c+dx)\right] + \frac{1}{256}A\sin\left[\frac{9}{2}(c+dx)\right] \right) + \\ & \frac{1}{64d} \left( 2 + \frac{3}{\sqrt{2}} \right) (163A+200B) \cos\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7-5\sqrt{2}+(10-7\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \\ & \left( 1-\sqrt{2}+(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right] \right) \cos[c+dx] \\ & \left( \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] + \right. \\ & \quad \left. 2\text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right) \\ & \sqrt{\left(-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right)\sec\left[\frac{1}{4}(c+dx)\right]^2} \\ & \sqrt{\left(-1-\sqrt{2}+(2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]\right)\sec\left[\frac{1}{4}(c+dx)\right]^2} \\ & \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \end{aligned}$$

**Problem 143: Result unnecessarily involves higher level functions.**

$$\int \cos[c+dx]^5 \left(a+a\sec[c+dx]\right)^{5/2} (A+B\sec[c+dx]) dx$$

Optimal (type 3, 254 leaves, 7 steps):

$$\begin{aligned}
& \frac{a^{5/2} (283 A + 326 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{128 d} + \frac{a^3 (283 A + 326 B) \operatorname{Sin}[c+dx]}{128 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
& \frac{a^3 (283 A + 326 B) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{192 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a^3 (157 A + 170 B) \operatorname{Cos}[c+dx]^2 \operatorname{Sin}[c+dx]}{240 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
& \frac{a^2 (13 A + 10 B) \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{40 d} + \\
& \frac{a A \operatorname{Cos}[c+dx]^4 (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{5 d}
\end{aligned}$$

Result(type 4, 500 leaves):

$$\begin{aligned}
& \frac{1}{d} \operatorname{Cos}[c+dx]^2 \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \\
& \left( -\frac{(2309 A + 2650 B) \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]}{15360} + \frac{(509 A + 550 B) \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{1920} + \right. \\
& \quad \frac{(95 A + 94 B) \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{1024} + \frac{1}{960} (32 A + 25 B) \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right] + \\
& \quad \left. \frac{1}{512} (5 A + 2 B) \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right] + \frac{1}{640} A \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right] \right) + \\
& \frac{1}{256 d} (4 + 3\sqrt{2}) (283 A + 326 B) \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{\frac{7 - 5\sqrt{2} + (10 - 7\sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]}} \\
& \left( (1 - \sqrt{2} + (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]) \operatorname{Cos}[c+dx] \right. \\
& \quad \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] + \right. \\
& \quad \left. \left. 2 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right) \right) \\
& \sqrt{\left( -1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
& \sqrt{\left( -1 - \sqrt{2} + (2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \right) \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
& \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
\end{aligned}$$

### Problem 162: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x]^2 (A+B \sec [c+d x])}{(a+a \sec [c+d x])^{5/2}} dx$$

Optimal (type 3, 126 leaves, 4 steps):

$$\frac{(5 A+19 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right]}{16 \sqrt{2} a^{5/2} d}-\frac{(A-B) \tan [c+d x]}{4 d(a+a \sec [c+d x])^{5/2}}+\frac{(5 A-13 B) \tan [c+d x]}{16 a d(a+a \sec [c+d x])^{3/2}}$$

Result (type 3, 256 leaves):

$$\left( (5 A+19 B) \operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right] \cos \left[\frac{1}{2}(c+d x)\right]^4 \sqrt{\frac{\cos [c+d x]}{1+\cos [c+d x]}} \sec [c+d x]^{5/2} \right. \\ \left. \sqrt{1+\sec [c+d x]}\right) / \left( 4 d \sqrt{\sec \left[\frac{1}{2}(c+d x)\right]^2(a(1+\sec [c+d x]))^{5/2}} \right) + \\ \left( \cos \left[\frac{1}{2}(c+d x)\right]^5 \sec [c+d x]^3 \left(-\frac{1}{2}(-A+9 B) \sin \left[\frac{1}{2}(c+d x)\right] + \right. \right. \\ \left. \frac{1}{2} \sec \left[\frac{1}{2}(c+d x)\right]^4 \left(-A \sin \left[\frac{1}{2}(c+d x)\right] + B \sin \left[\frac{1}{2}(c+d x)\right]\right) + \frac{1}{4} \sec \left[\frac{1}{2}(c+d x)\right]^2 \right. \\ \left. \left. \left(3 A \sin \left[\frac{1}{2}(c+d x)\right] + 5 B \sin \left[\frac{1}{2}(c+d x)\right]\right)\right) \right) / \left( d(a(1+\sec [c+d x]))^{5/2} \right)$$

### Problem 163: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x](A+B \sec [c+d x])}{(a+a \sec [c+d x])^{5/2}} dx$$

Optimal (type 3, 126 leaves, 4 steps):

$$\frac{(3 A+5 B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right]}{16 \sqrt{2} a^{5/2} d}+\frac{(A-B) \tan [c+d x]}{4 d(a+a \sec [c+d x])^{5/2}}+\frac{(3 A+5 B) \tan [c+d x]}{16 a d(a+a \sec [c+d x])^{3/2}}$$

Result (type 3, 298 leaves):

$$\begin{aligned}
& \left( (3A + 5B) \operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c + dx)\right]\right] \cos\left[\frac{1}{2}(c + dx)\right]^4 \right. \\
& \quad \left. \sqrt{\frac{\cos[c + dx]}{1 + \cos[c + dx]}} \sec[c + dx]^{3/2} \sqrt{1 + \sec[c + dx]} (A + B \sec[c + dx]) \right) / \\
& \left( 4d (B + A \cos[c + dx]) \sqrt{\sec\left[\frac{1}{2}(c + dx)\right]^2 (a (1 + \sec[c + dx]))^{5/2}} + \right. \\
& \quad \left( \cos\left[\frac{1}{2}(c + dx)\right]^5 \sec[c + dx]^2 (A + B \sec[c + dx]) \right. \\
& \quad \left( \frac{1}{2} (7A + B) \sin\left[\frac{1}{2}(c + dx)\right] + \frac{1}{2} \sec\left[\frac{1}{2}(c + dx)\right]^4 \left( A \sin\left[\frac{1}{2}(c + dx)\right] - B \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) + \\
& \quad \left. \frac{1}{4} \sec\left[\frac{1}{2}(c + dx)\right]^2 \left( -11A \sin\left[\frac{1}{2}(c + dx)\right] + 3B \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) / \\
& \quad \left( d (B + A \cos[c + dx]) (a (1 + \sec[c + dx]))^{5/2} \right)
\end{aligned}$$

**Problem 164: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + dx]}{(a + a \sec[c + dx])^{5/2}} dx$$

Optimal (type 3, 164 leaves, 7 steps):

$$\begin{aligned}
& \frac{2A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c + dx]}{\sqrt{a + a \sec[c + dx]}}\right]}{a^{5/2} d} - \frac{(43A - 3B) \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c + dx]}{\sqrt{2} \sqrt{a + a \sec[c + dx]}}\right]}{16\sqrt{2} a^{5/2} d} - \\
& \frac{(A - B) \tan[c + dx]}{4d (a + a \sec[c + dx])^{5/2}} - \frac{(11A - 3B) \tan[c + dx]}{16ad (a + a \sec[c + dx])^{3/2}}
\end{aligned}$$

Result (type 3, 343 leaves):

$$\left( \left( (-43 A + 3 B) \operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right] + 32 \sqrt{2} A \operatorname{ArcTan}\left[\frac{\tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{\frac{\cos[c+dx]}{1+\cos[c+dx]}}}\right] \right) \cos\left[\frac{1}{2}(c+dx)\right]^4 \right. \\ \left. \sqrt{\frac{\cos[c+dx]}{1+\cos[c+dx]}} \operatorname{Sec}[c+dx]^{3/2} \sqrt{1+\operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx]) \right) / \\ \left( 4 d (B+A \cos[c+dx]) \sqrt{\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a(1+\operatorname{Sec}[c+dx]))^{5/2}} \right) + \\ \left( \cos\left[\frac{1}{2}(c+dx)\right]^5 \operatorname{Sec}[c+dx]^2 (A+B \operatorname{Sec}[c+dx]) \left( \frac{1}{2} (-15 A + 7 B) \sin\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\ \left. \frac{1}{4} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left( 19 A \sin\left[\frac{1}{2}(c+dx)\right] - 11 B \sin\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\ \left. \left. \frac{1}{2} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \left( -A \sin\left[\frac{1}{2}(c+dx)\right] + B \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\ \left( d (B+A \cos[c+dx]) (a(1+\operatorname{Sec}[c+dx]))^{5/2} \right)$$

**Problem 167: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{A + A \operatorname{Sec}[c+dx]}{\sqrt{a - a \operatorname{Sec}[c+dx]}} dx$$

Optimal (type 3, 89 leaves, 5 steps):

$$\frac{2 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a - a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a} d} - \frac{2 \sqrt{2} A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{2} \sqrt{a - a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a} d}$$

Result (type 3, 176 leaves):

$$- \left( \left( A (-1 + e^{i(c+dx)}) \left( \sqrt{2} dx + i \sqrt{2} \operatorname{ArcSinh}\left[e^{i(c+dx)}\right] + 4 i \operatorname{Log}\left[1 - e^{i(c+dx)}\right] + \right. \right. \right. \\ \left. i \sqrt{2} \operatorname{Log}\left[1 + \sqrt{1 + e^{2i(c+dx)}}\right] - 4 i \operatorname{Log}\left[1 + e^{i(c+dx)} + \sqrt{2} \sqrt{1 + e^{2i(c+dx)}}\right] \right) \right) / \\ \left( \sqrt{2} d \sqrt{1 + e^{2i(c+dx)}} \sqrt{a - a \operatorname{Sec}[c+dx]} \right)$$

**Problem 168: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx] (A + A \operatorname{Sec}[c+dx])}{\sqrt{a - a \operatorname{Sec}[c+dx]}} dx$$



Optimal (type 3, 115 leaves, 6 steps):

$$\frac{3 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a-a \sec [c+d x]}}\right]}{\sqrt{a} d}-\frac{2 \sqrt{2} A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{2} \sqrt{a-a \sec [c+d x]}}\right]}{\sqrt{a} d}+\frac{A \sin [c+d x]}{d \sqrt{a-a \sec [c+d x]}}$$

Result (type 3, 382 leaves):

$$A \left( \left( e^{\frac{-1}{2} i (c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \sqrt{1+e^{2 i (c+d x)}} (1+\cos [c+d x]) \right. \right. \\ \left. \left. \left( -3 i d x+3 \operatorname{ArcSinh}\left[e^{i (c+d x)}\right]+4 \sqrt{2} \log \left[1-e^{i (c+d x)}\right]+3 \log \left[1+\sqrt{1+e^{2 i (c+d x)}}\right]- \right. \right. \\ \left. \left. 4 \sqrt{2} \log \left[1+e^{i (c+d x)}+\sqrt{2} \sqrt{1+e^{2 i (c+d x)}}\right]\right) \sec \left[\frac{c}{2}+\frac{d x}{2}\right] \sqrt{\sec [c+d x]} \tan \left[\frac{c}{2}+\frac{d x}{2}\right] \right) / \\ \left( 2 \sqrt{2} d \sqrt{a-a \sec [c+d x]} \right)+\left( (1+\cos [c+d x]) \sec \left[\frac{c}{2}+\frac{d x}{2}\right] \sec [c+d x] \right. \\ \left. \left( \frac{\cos \left[\frac{c}{2}\right] \cos \left[\frac{d x}{2}\right]}{2 d}+\frac{\cos \left[\frac{3 c}{2}\right] \cos \left[\frac{3 d x}{2}\right]}{2 d}-\frac{\sin \left[\frac{c}{2}\right] \sin \left[\frac{d x}{2}\right]}{2 d}-\frac{\sin \left[\frac{3 c}{2}\right] \sin \left[\frac{3 d x}{2}\right]}{2 d} \right) \right. \\ \left. \tan \left[\frac{c}{2}+\frac{d x}{2}\right] \right) / \left( \sqrt{a-a \sec [c+d x]} \right) \right)$$

**Problem 169: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c+d x]^2 (A+A \sec [c+d x])}{\sqrt{a-a \sec [c+d x]}} d x$$

Optimal (type 3, 155 leaves, 7 steps):

$$\frac{11 A \operatorname{ArcTan}\left[\frac{-\sqrt{a} \tan [c+d x]}{\sqrt{a-a \sec [c+d x]}}\right]}{4 \sqrt{a} d}-\frac{2 \sqrt{2} A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{2} \sqrt{a-a \sec [c+d x]}}\right]}{\sqrt{a} d}+ \\ \frac{5 A \sin [c+d x]}{4 d \sqrt{a-a \sec [c+d x]}}+\frac{A \cos [c+d x] \sin [c+d x]}{2 d \sqrt{a-a \sec [c+d x]}}$$

Result (type 3, 332 leaves):

$$\frac{1}{8 d \sqrt{a - a \operatorname{Sec}[c + d x]}}$$

$$A e^{-i(c+dx)} \left( 7 + 6 e^{-i(c+dx)} + 7 e^{i(c+dx)} + e^{-2i(c+dx)} + 6 e^{2i(c+dx)} + e^{3i(c+dx)} - 11 i d \sqrt{1 + e^{2i(c+dx)}} x + \right.$$

$$11 \sqrt{1 + e^{2i(c+dx)}} \operatorname{ArcSinh}\left[e^{i(c+dx)}\right] + 16 \sqrt{2} \sqrt{1 + e^{2i(c+dx)}} \operatorname{Log}\left[1 - e^{i(c+dx)}\right] +$$

$$11 \sqrt{1 + e^{2i(c+dx)}} \operatorname{Log}\left[1 + \sqrt{1 + e^{2i(c+dx)}}\right] -$$

$$16 \sqrt{2} \sqrt{1 + e^{2i(c+dx)}} \operatorname{Log}\left[1 + e^{i(c+dx)} + \sqrt{2} \sqrt{1 + e^{2i(c+dx)}}\right] \Big)$$

$$\operatorname{Sec}[c + d x] \left( \cos\left[\frac{1}{2}(c + d x)\right] + i \sin\left[\frac{1}{2}(c + d x)\right] \right) \sin\left[\frac{1}{2}(c + d x)\right]$$

**Problem 170: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cos[c + d x]^3 (A + A \operatorname{Sec}[c + d x])}{\sqrt{a - a \operatorname{Sec}[c + d x]}} dx$$

Optimal (type 3, 192 leaves, 8 steps):

$$\frac{23 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a-a \operatorname{Sec}[c+dx]}}\right]}{8 \sqrt{a} d} - \frac{2 \sqrt{2} A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a-a \operatorname{Sec}[c+dx]}}\right]}{\sqrt{a} d} +$$

$$\frac{9 A \sin[c + d x]}{8 d \sqrt{a - a \operatorname{Sec}[c + d x]}} + \frac{7 A \cos[c + d x] \sin[c + d x]}{12 d \sqrt{a - a \operatorname{Sec}[c + d x]}} + \frac{A \cos[c + d x]^2 \sin[c + d x]}{3 d \sqrt{a - a \operatorname{Sec}[c + d x]}}$$

Result (type 3, 362 leaves):

$$\frac{1}{48 d \sqrt{a - a \operatorname{Sec}[c + d x]}}$$

$$A e^{-i(c+dx)} \left( 47 + 40 e^{-i(c+dx)} + 47 e^{i(c+dx)} + 9 e^{-2i(c+dx)} + 40 e^{2i(c+dx)} + 2 e^{-3i(c+dx)} + \right.$$

$$9 e^{3i(c+dx)} + 2 e^{4i(c+dx)} - 69 i d \sqrt{1 + e^{2i(c+dx)}} x + 69 \sqrt{1 + e^{2i(c+dx)}} \operatorname{ArcSinh}\left[e^{i(c+dx)}\right] +$$

$$96 \sqrt{2} \sqrt{1 + e^{2i(c+dx)}} \operatorname{Log}\left[1 - e^{i(c+dx)}\right] + 69 \sqrt{1 + e^{2i(c+dx)}} \operatorname{Log}\left[1 + \sqrt{1 + e^{2i(c+dx)}}\right] -$$

$$96 \sqrt{2} \sqrt{1 + e^{2i(c+dx)}} \operatorname{Log}\left[1 + e^{i(c+dx)} + \sqrt{2} \sqrt{1 + e^{2i(c+dx)}}\right] \Big)$$

$$\operatorname{Sec}[c + d x] \left( \cos\left[\frac{1}{2}(c + d x)\right] + i \sin\left[\frac{1}{2}(c + d x)\right] \right) \sin\left[\frac{1}{2}(c + d x)\right]$$

**Problem 171: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A + A \operatorname{Sec}[c + d x]}{(a - a \operatorname{Sec}[c + d x])^{3/2}} dx$$

Optimal (type 3, 116 leaves, 6 steps):

$$\frac{2 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a-a \operatorname{Sec}[c+d x]}}\right]}{a^{3/2} d} - \frac{3 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{2} \sqrt{a-a \operatorname{Sec}[c+d x]}}\right]}{\sqrt{2} a^{3/2} d} - \frac{A \operatorname{Tan}[c+d x]}{d (a-a \operatorname{Sec}[c+d x])^{3/2}}$$

Result (type 3, 265 leaves):

$$\frac{1}{d (a-a \operatorname{Sec}[c+d x])^{3/2}} A \left( \sqrt{2} e^{-\frac{1}{2} i (c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \sqrt{1+e^{2 i (c+d x)}} \left( 2 i d x - 2 \operatorname{ArcSinh}\left[e^{i (c+d x)}\right] - 3 \sqrt{2} \operatorname{Log}\left[1 - e^{i (c+d x)}\right] - 2 \operatorname{Log}\left[1 + \sqrt{1+e^{2 i (c+d x)}}\right] + 3 \sqrt{2} \operatorname{Log}\left[1 + e^{i (c+d x)} + \sqrt{2} \sqrt{1+e^{2 i (c+d x)}}\right] \right) - \left( \cos\left[\frac{1}{2} (c+d x)\right] + \cos\left[\frac{3}{2} (c+d x)\right] \right) \operatorname{Csc}\left[\frac{1}{2} (c+d x)\right]^2 \sqrt{\operatorname{Sec}[c+d x]} \right) \operatorname{Sec}[c+d x]^{3/2} \sin\left[\frac{1}{2} (c+d x)\right]^3$$

**Problem 172: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cos[c+d x] (A+A \operatorname{Sec}[c+d x])}{(a-a \operatorname{Sec}[c+d x])^{3/2}} dx$$

Optimal (type 3, 146 leaves, 7 steps):

$$\frac{5 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a-a \operatorname{Sec}[c+d x]}}\right]}{a^{3/2} d} - \frac{7 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{2} \sqrt{a-a \operatorname{Sec}[c+d x]}}\right]}{\sqrt{2} a^{3/2} d} - \frac{A \sin[c+d x]}{d (a-a \operatorname{Sec}[c+d x])^{3/2}} + \frac{2 A \sin[c+d x]}{a d \sqrt{a-a \operatorname{Sec}[c+d x]}}$$

Result (type 3, 281 leaves):

$$\frac{1}{d (a-a \operatorname{Sec}[c+d x])^{3/2}} A \left( \sqrt{2} e^{-\frac{1}{2} i (c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \sqrt{1+e^{2 i (c+d x)}} \left( 5 i d x - 5 \operatorname{ArcSinh}\left[e^{i (c+d x)}\right] - 7 \sqrt{2} \operatorname{Log}\left[1 - e^{i (c+d x)}\right] - 5 \operatorname{Log}\left[1 + \sqrt{1+e^{2 i (c+d x)}}\right] + 7 \sqrt{2} \operatorname{Log}\left[1 + e^{i (c+d x)} + \sqrt{2} \sqrt{1+e^{2 i (c+d x)}}\right] \right) + \frac{1}{2} \left( -2 \cos\left[\frac{1}{2} (c+d x)\right] - 3 \cos\left[\frac{3}{2} (c+d x)\right] + \cos\left[\frac{5}{2} (c+d x)\right] \right) \operatorname{Csc}\left[\frac{1}{2} (c+d x)\right]^2 \sqrt{\operatorname{Sec}[c+d x]} \right) \operatorname{Sec}[c+d x]^{3/2} \sin\left[\frac{1}{2} (c+d x)\right]^3$$

**Problem 173: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cos [c+d x]^2 (A+A \sec [c+d x])}{(a-a \sec [c+d x])^{3/2}} dx$$

Optimal (type 3, 194 leaves, 8 steps):

$$\frac{31 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a-a \sec [c+d x]}}\right]}{4 a^{3/2} d} - \frac{11 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{2} \sqrt{a-a \sec [c+d x]}}\right]}{\sqrt{2} a^{3/2} d} - \frac{A \cos [c+d x] \sin [c+d x]}{d (a-a \sec [c+d x])^{3/2}} + \frac{13 A \sin [c+d x]}{4 a d \sqrt{a-a \sec [c+d x]}} + \frac{3 A \cos [c+d x] \sin [c+d x]}{2 a d \sqrt{a-a \sec [c+d x]}}$$

Result (type 3, 296 leaves):

$$\frac{1}{4 d (a-a \sec [c+d x])^{3/2}} A \left( \sqrt{2} e^{-\frac{1}{2} i (c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \right. \\ \left. \sqrt{1+e^{2 i (c+d x)}} \left( 31 i d x - 31 \operatorname{ArcSinh}\left[e^{i (c+d x)}\right] - 44 \sqrt{2} \operatorname{Log}\left[1-e^{i (c+d x)}\right] - \right. \right. \\ \left. \left. 31 \operatorname{Log}\left[1+\sqrt{1+e^{2 i (c+d x)}}\right] + 44 \sqrt{2} \operatorname{Log}\left[1+e^{i (c+d x)}+\sqrt{2} \sqrt{1+e^{2 i (c+d x)}}\right] \right) + \right. \\ \left. \frac{1}{2} \left( -9 \cos \left[\frac{1}{2} (c+d x)\right] - 16 \cos \left[\frac{3}{2} (c+d x)\right] + 8 \cos \left[\frac{5}{2} (c+d x)\right] + \cos \left[\frac{7}{2} (c+d x)\right] \right) \right. \\ \left. \csc \left[\frac{1}{2} (c+d x)\right]^2 \sqrt{\sec [c+d x]} \right) \sec [c+d x]^{3/2} \sin \left[\frac{1}{2} (c+d x)\right]^3$$

**Problem 174: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cos [c+d x]^3 (A+A \sec [c+d x])}{(a-a \sec [c+d x])^{3/2}} dx$$

Optimal (type 3, 236 leaves, 9 steps):

$$\frac{85 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a-a \sec [c+d x]}}\right]}{8 a^{3/2} d} - \frac{15 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{2} \sqrt{a-a \sec [c+d x]}}\right]}{\sqrt{2} a^{3/2} d} - \frac{A \cos [c+d x]^2 \sin [c+d x]}{d (a-a \sec [c+d x])^{3/2}} + \frac{35 A \sin [c+d x]}{8 a d \sqrt{a-a \sec [c+d x]}} + \frac{25 A \cos [c+d x] \sin [c+d x]}{12 a d \sqrt{a-a \sec [c+d x]}} + \frac{4 A \cos [c+d x]^2 \sin [c+d x]}{3 a d \sqrt{a-a \sec [c+d x]}}$$

Result (type 3, 314 leaves):

$$\begin{aligned}
& \left( A \left( -\frac{1}{d} 5 \sqrt{2} e^{\frac{1}{2} i (c+dx)} \sqrt{\frac{e^{i (c+dx)}}{1 + e^{2 i (c+dx)}}} \right. \right. \\
& \quad \sqrt{1 + e^{2 i (c+dx)}} \left( -17 i dx + 17 \operatorname{ArcSinh}[e^{i (c+dx)}] + 24 \sqrt{2} \operatorname{Log}[1 - e^{i (c+dx)}] + \right. \\
& \quad \left. 17 \operatorname{Log}[1 + \sqrt{1 + e^{2 i (c+dx)}}] - 24 \sqrt{2} \operatorname{Log}[1 + e^{i (c+dx)} + \sqrt{2} \sqrt{1 + e^{2 i (c+dx)}}] \right) + \\
& \quad \frac{1}{6d} \left( -61 \operatorname{Cos}\left[\frac{1}{2} (c+dx)\right] - 120 \operatorname{Cos}\left[\frac{3}{2} (c+dx)\right] + 72 \operatorname{Cos}\left[\frac{5}{2} (c+dx)\right] + \right. \\
& \quad \left. 11 \operatorname{Cos}\left[\frac{7}{2} (c+dx)\right] + 2 \operatorname{Cos}\left[\frac{9}{2} (c+dx)\right] \right) \operatorname{Csc}\left[\frac{1}{2} (c+dx)\right]^2 \sqrt{\operatorname{Sec}[c+dx]} \left. \right) \\
& \quad \left. \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}\left[\frac{1}{2} (c+dx)\right]^3 \right) / \left( 8 (a - a \operatorname{Sec}[c+dx])^{3/2} \right)
\end{aligned}$$

Problem 175: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{A + A \operatorname{Sec}[c+dx]}{(a - a \operatorname{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 3, 152 leaves, 7 steps):

$$\begin{aligned}
& \frac{2 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a - a \operatorname{Sec}[c+dx]}}\right]}{a^{5/2} d} - \frac{23 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{2} \sqrt{a - a \operatorname{Sec}[c+dx]}}\right]}{8 \sqrt{2} a^{5/2} d} - \\
& \frac{A \operatorname{Tan}[c+dx]}{2 d (a - a \operatorname{Sec}[c+dx])^{5/2}} - \frac{7 A \operatorname{Tan}[c+dx]}{8 a d (a - a \operatorname{Sec}[c+dx])^{3/2}}
\end{aligned}$$

Result (type 3, 421 leaves):

$$\begin{aligned}
& A \left( \left( e^{-\frac{1}{2} i (c+dx)} \sqrt{\frac{e^{i (c+dx)}}{1+e^{2 i (c+dx)}}} \sqrt{1+e^{2 i (c+dx)}} \right. \right. \\
& \quad \left( -16 i dx + 16 \operatorname{ArcSinh}[e^{i (c+dx)}] + 23 \sqrt{2} \operatorname{Log}[1 - e^{i (c+dx)}] + \right. \\
& \quad \left. 16 \operatorname{Log}[1 + \sqrt{1+e^{2 i (c+dx)}}] - 23 \sqrt{2} \operatorname{Log}[1 + e^{i (c+dx)} + \sqrt{2} \sqrt{1+e^{2 i (c+dx)}}] \right) \\
& \quad \left. \sec[c+dx]^{5/2} \sin\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \right) / \left( 2 \sqrt{2} d (a - a \sec[c+dx])^{5/2} \right) + \\
& \quad \left( \sec[c+dx]^3 \left( -\frac{11 \cos\left[\frac{c}{2}\right] \cos\left[\frac{dx}{2}\right]}{d} + \frac{15 \cot\left[\frac{c}{2}\right] \csc\left[\frac{c}{2} + \frac{dx}{2}\right]}{2d} - \frac{\cot\left[\frac{c}{2}\right] \csc\left[\frac{c}{2} + \frac{dx}{2}\right]^3}{d} - \right. \right. \\
& \quad \left. \frac{15 \csc\left[\frac{c}{2}\right] \csc\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sin\left[\frac{dx}{2}\right]}{2d} + \frac{\csc\left[\frac{c}{2}\right] \csc\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sin\left[\frac{dx}{2}\right]}{d} + \frac{11 \sin\left[\frac{c}{2}\right] \sin\left[\frac{dx}{2}\right]}{d} \right) \\
& \quad \left. \sin\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \right) / (a - a \sec[c+dx])^{5/2} \Bigg)
\end{aligned}$$

**Problem 176: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\cos[c+dx] (A + A \sec[c+dx])}{(a - a \sec[c+dx])^{5/2}} dx$$

Optimal (type 3, 184 leaves, 8 steps):

$$\begin{aligned}
& \frac{7 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a-a \sec[c+dx]}}\right]}{a^{5/2} d} - \frac{79 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{2} \sqrt{a-a \sec[c+dx]}}\right]}{8 \sqrt{2} a^{5/2} d} - \\
& \frac{A \sin[c+dx]}{2 d (a - a \sec[c+dx])^{5/2}} - \frac{11 A \sin[c+dx]}{8 a d (a - a \sec[c+dx])^{3/2}} + \frac{23 A \sin[c+dx]}{8 a^2 d \sqrt{a - a \sec[c+dx]}}
\end{aligned}$$

Result (type 3, 298 leaves):

$$\frac{1}{4 d (a - a \operatorname{Sec}[c + d x])^{5/2}} A \left( \sqrt{2} e^{-\frac{1}{2} i (c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \right. \\ \left. \sqrt{1 + e^{2 i (c + d x)}} \left( -56 i d x + 56 \operatorname{ArcSinh}[e^{i (c + d x)}] + 79 \sqrt{2} \operatorname{Log}[1 - e^{i (c + d x)}] + \right. \right. \\ \left. \left. 56 \operatorname{Log}[1 + \sqrt{1 + e^{2 i (c + d x)}}] - 79 \sqrt{2} \operatorname{Log}[1 + e^{i (c + d x)} + \sqrt{2} \sqrt{1 + e^{2 i (c + d x)}}] \right) + \right. \\ \left. \frac{1}{4} \left( -12 \operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + 23 \operatorname{Cos}\left[\frac{3}{2} (c + d x)\right] - 31 \operatorname{Cos}\left[\frac{5}{2} (c + d x)\right] + 4 \operatorname{Cos}\left[\frac{7}{2} (c + d x)\right] \right) \right. \\ \left. \operatorname{Csc}\left[\frac{1}{2} (c + d x)\right]^4 \sqrt{\operatorname{Sec}[c + d x]} \right) \operatorname{Sec}[c + d x]^{5/2} \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]^5$$

Problem 177: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Cos}[c + d x]^2 (A + A \operatorname{Sec}[c + d x])}{(a - a \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 236 leaves, 9 steps):

$$\frac{59 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{a - a \operatorname{Sec}[c + d x]}}\right]}{4 a^{5/2} d} - \frac{167 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c + d x]}{\sqrt{2} \sqrt{a - a \operatorname{Sec}[c + d x]}}\right]}{8 \sqrt{2} a^{5/2} d} - \frac{A \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]}{2 d (a - a \operatorname{Sec}[c + d x])^{5/2}} - \\ \frac{15 A \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]}{8 a d (a - a \operatorname{Sec}[c + d x])^{3/2}} + \frac{49 A \operatorname{Sin}[c + d x]}{8 a^2 d \sqrt{a - a \operatorname{Sec}[c + d x]}} + \frac{23 A \operatorname{Cos}[c + d x] \operatorname{Sin}[c + d x]}{8 a^2 d \sqrt{a - a \operatorname{Sec}[c + d x]}}$$

Result (type 3, 308 leaves):

$$\frac{1}{4 d (a - a \operatorname{Sec}[c + d x])^{5/2}} A \left( \sqrt{2} e^{-\frac{1}{2} i (c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \right. \\ \left. \sqrt{1 + e^{2 i (c + d x)}} \left( -118 i d x + 118 \operatorname{ArcSinh}[e^{i (c + d x)}] + 167 \sqrt{2} \operatorname{Log}[1 - e^{i (c + d x)}] + \right. \right. \\ \left. \left. 118 \operatorname{Log}[1 + \sqrt{1 + e^{2 i (c + d x)}}] - 167 \sqrt{2} \operatorname{Log}[1 + e^{i (c + d x)} + \sqrt{2} \sqrt{1 + e^{2 i (c + d x)}}] \right) + \right. \\ \left. \frac{1}{4} \left( -19 \operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + 54 \operatorname{Cos}\left[\frac{3}{2} (c + d x)\right] - 62 \operatorname{Cos}\left[\frac{5}{2} (c + d x)\right] + 10 \operatorname{Cos}\left[\frac{7}{2} (c + d x)\right] + \right. \right. \\ \left. \left. \operatorname{Cos}\left[\frac{9}{2} (c + d x)\right] \right) \operatorname{Csc}\left[\frac{1}{2} (c + d x)\right]^4 \sqrt{\operatorname{Sec}[c + d x]} \right) \operatorname{Sec}[c + d x]^{5/2} \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]^5$$

Problem 178: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Cos}[c + d x]^3 (A + A \operatorname{Sec}[c + d x])}{(a - a \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 280 leaves, 10 steps):

$$\frac{203 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a-a \operatorname{Sec}[c+d x]}}\right]}{8 a^{5/2} d} - \frac{287 A \operatorname{ArcTan}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{2} \sqrt{a-a \operatorname{Sec}[c+d x]}}\right]}{8 \sqrt{2} a^{5/2} d} -$$

$$\frac{A \cos [c+d x]^2 \sin [c+d x]}{2 d (a-a \operatorname{Sec}[c+d x])^{5/2}} - \frac{19 A \cos [c+d x]^2 \sin [c+d x]}{8 a d (a-a \operatorname{Sec}[c+d x])^{3/2}} + \frac{21 A \sin [c+d x]}{2 a^2 d \sqrt{a-a \operatorname{Sec}[c+d x]}} +$$

$$\frac{119 A \cos [c+d x] \sin [c+d x]}{24 a^2 d \sqrt{a-a \operatorname{Sec}[c+d x]}} + \frac{77 A \cos [c+d x]^2 \sin [c+d x]}{24 a^2 d \sqrt{a-a \operatorname{Sec}[c+d x]}}$$

Result (type 3, 323 leaves):

$$\frac{1}{12 d (a-a \operatorname{Sec}[c+d x])^{5/2}} A \left( 21 \sqrt{2} e^{-\frac{1}{2} i (c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \right.$$

$$\sqrt{1+e^{2 i (c+d x)}} \left( -29 i d x + 29 \operatorname{ArcSinh}\left[e^{i (c+d x)}\right] + 41 \sqrt{2} \operatorname{Log}\left[1-e^{i (c+d x)}\right] + \right.$$

$$\left. 29 \operatorname{Log}\left[1+\sqrt{1+e^{2 i (c+d x)}}\right] - 41 \sqrt{2} \operatorname{Log}\left[1+e^{i (c+d x)}+\sqrt{2} \sqrt{1+e^{2 i (c+d x)}}\right] \right) +$$

$$\frac{1}{8} \left( -173 \cos \left[\frac{1}{2} (c+d x)\right] + 575 \cos \left[\frac{3}{2} (c+d x)\right] - 625 \cos \left[\frac{5}{2} (c+d x)\right] + \right.$$

$$\left. 112 \cos \left[\frac{7}{2} (c+d x)\right] + 13 \cos \left[\frac{9}{2} (c+d x)\right] + 2 \cos \left[\frac{11}{2} (c+d x)\right] \right)$$

$$\left. \operatorname{Csc}\left[\frac{1}{2} (c+d x)\right]^4 \sqrt{\operatorname{Sec}[c+d x]}\right) \operatorname{Sec}[c+d x]^{5/2} \sin \left[\frac{1}{2} (c+d x)\right]^5$$

**Problem 186: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+d x]^{3/2} (a+a \operatorname{Sec}[c+d x])^2 (A+B \operatorname{Sec}[c+d x]) dx$$

Optimal (type 4, 234 leaves, 9 steps):

$$-\frac{1}{5 d} 4 a^2 (4 A+3 B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right] \sqrt{\operatorname{Sec}[c+d x]} +$$

$$\frac{1}{21 d} 4 a^2 (7 A+6 B) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right] \sqrt{\operatorname{Sec}[c+d x]} +$$

$$\frac{4 a^2 (4 A+3 B) \sqrt{\operatorname{Sec}[c+d x]} \sin [c+d x]}{5 d} + \frac{4 a^2 (7 A+6 B) \operatorname{Sec}[c+d x]^{3/2} \sin [c+d x]}{21 d} +$$

$$\frac{2 a^2 (7 A+9 B) \operatorname{Sec}[c+d x]^{5/2} \sin [c+d x]}{35 d} + \frac{2 B \operatorname{Sec}[c+d x]^{5/2} (a^2+a^2 \operatorname{Sec}[c+d x]) \sin [c+d x]}{7 d}$$

Result (type 5, 731 leaves):



$$\begin{aligned}
& - \left( \left( 2 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \csc[c] \right. \right. \\
& \quad \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) \right) / (5d(B+A \cos[c+dx])) - \\
& \left( 3B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \csc[c] \right. \\
& \quad \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) \right) / (5\sqrt{2}d(B+A \cos[c+dx])) + \\
& \left( A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 \right. \\
& \quad \left. (A+B \sec[c+dx]) \right) / (3d(B+A \cos[c+dx]) \sec[c+dx]^{5/2}) + \\
& \left( 2B \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 \right. \\
& \quad \left. (A+B \sec[c+dx]) \right) / (7d(B+A \cos[c+dx]) \sec[c+dx]^{5/2}) + \\
& \left( \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) \right. \\
& \quad \left( \frac{(4A+3B) \cos[dx] \csc[c]}{5d} + \frac{B \sec[c] \sec[c+dx]^3 \sin[dx]}{14d} + \right. \\
& \quad \left. \frac{\sec[c] \sec[c+dx]^2 (5B \sin[c] + 7A \sin[dx] + 14B \sin[dx])}{70d} + \frac{1}{210d} \right. \\
& \quad \left. \sec[c] \sec[c+dx] (21A \sin[c] + 42B \sin[c] + 70A \sin[dx] + 60B \sin[dx]) + \right. \\
& \quad \left. \left. \frac{(7A+6B) \tan[c]}{21d} \right) \right) / ((B+A \cos[c+dx]) \sec[c+dx]^{5/2})
\end{aligned}$$

**Problem 187: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec[c+dx]} (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) dx$$

Optimal (type 4, 199 leaves, 8 steps):

$$\begin{aligned}
& -\frac{1}{5d} 4a^2 (5A+4B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
& \frac{4a^2 (2A+B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3d} + \\
& \frac{4a^2 (5A+4B) \sqrt{\sec[c+dx]} \sin[c+dx]}{5d} + \frac{2a^2 (5A+7B) \sec[c+dx]^{3/2} \sin[c+dx]}{15d} + \\
& \frac{2B \sec[c+dx]^{3/2} (a^2 + a^2 \sec[c+dx]) \sin[c+dx]}{5d}
\end{aligned}$$

Result (type 5, 685 leaves):

$$\begin{aligned}
& -\left( \left( A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \csc[c] \right. \right. \\
& \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) \right) \Bigg/ \left( \sqrt{2} d (B+A \cos[c+dx]) \right) \Bigg) - \\
& \left( 2\sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^3 \csc[c] \right. \\
& \quad \left. \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) \right) \Bigg/ \left( 5d (B+A \cos[c+dx]) \right) \Bigg) + \\
& \left( 2A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 \right. \\
& \quad \left. (A+B \sec[c+dx]) \right) \Bigg/ \left( 3d (B+A \cos[c+dx]) \sec[c+dx]^{5/2} \right) + \\
& \left( B \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 \right. \\
& \quad \left. (A+B \sec[c+dx]) \right) \Bigg/ \left( 3d (B+A \cos[c+dx]) \sec[c+dx]^{5/2} \right) + \\
& \left( \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) \right. \\
& \quad \left( \frac{(5A+4B) \cos[dx] \csc[c]}{5d} + \frac{B \sec[c] \sec[c+dx]^2 \sin[dx]}{10d} + \right. \\
& \quad \left. \frac{\sec[c] \sec[c+dx] (3B \sin[c] + 5A \sin[dx] + 10B \sin[dx])}{30d} + \frac{(A+2B) \tan[c]}{6d} \right) \Bigg) \Bigg/ \\
& \left( (B+A \cos[c+dx]) \sec[c+dx]^{5/2} \right)
\end{aligned}$$

### Problem 188: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x])}{\sqrt{\operatorname{Sec}[c + d x]}} dx$$

Optimal (type 4, 160 leaves, 7 steps):

$$\begin{aligned} & -\frac{4 a^2 B \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{d} + \frac{1}{3 d} \\ & 4 a^2 (3 A + 2 B) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{2 a^2 (3 A + 5 B) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 d} + \frac{2 B \sqrt{\operatorname{Sec}[c + d x]} (a^2 + a^2 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{3 d} \end{aligned}$$

Result (type 5, 313 leaves):

$$\begin{aligned} & \frac{1}{12 d (B + A \operatorname{Cos}[c + d x])} a^2 \operatorname{Sec}\left[\frac{1}{2}(c + d x)\right]^4 (1 + \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x]) \\ & \left( -\frac{1}{-1 + e^{2 i c}} 4^{\frac{1}{2}} \sqrt{2} e^{-i(c + d x)} \sqrt{\frac{e^{i(c + d x)}}{1 + e^{2 i(c + d x)}}} \operatorname{Cos}[c + d x]^3 \left( 3 B (1 + e^{2 i(c + d x)}) + 3 B (-1 + e^{2 i c}) \right. \right. \\ & \quad \sqrt{1 + e^{2 i(c + d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i(c + d x)}\right] + (3 A + 2 B) e^{i(c + d x)} \\ & \quad \left. (-1 + e^{2 i c}) \sqrt{1 + e^{2 i(c + d x)}} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i(c + d x)}\right] \right) + \frac{1}{\operatorname{Sec}[c + d x]^{5/2}} \\ & \quad \left. (-3 (-A - 4 B + A \operatorname{Cos}[2 c]) \operatorname{Cos}[d x] \operatorname{Csc}[c] + 6 A \operatorname{Cos}[c] \operatorname{Sin}[d x] + 2 B \operatorname{Tan}[c + d x]) \right) \end{aligned}$$

### Problem 189: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x])}{\operatorname{Sec}[c + d x]^{3/2}} dx$$

Optimal (type 4, 158 leaves, 7 steps):

$$\begin{aligned} & \frac{4 a^2 A \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{d} + \frac{1}{3 d} \\ & 4 a^2 (2 A + 3 B) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} - \\ & \frac{2 a^2 (A - 3 B) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 d} + \frac{2 A (a^2 + a^2 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{3 d \sqrt{\operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 5, 183 leaves):

$$\left( a^2 \left( \cos \left[ \frac{c}{2} \right] - i \sin \left[ \frac{c}{2} \right] \right) \left( -i \cos \left[ \frac{c}{2} \right] + \sin \left[ \frac{c}{2} \right] \right) \right. \\ \left( 12 A - \frac{24 A \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)} \right]}{\sqrt{1 + e^{2 i (c+d x)}}} + \right. \\ \left. \frac{8 (2 A + 3 B) e^{i (c+d x)} \operatorname{Hypergeometric2F1} \left[ \frac{1}{4}, \frac{1}{2}, \frac{5}{4}, -e^{2 i (c+d x)} \right]}{\sqrt{1 + e^{2 i (c+d x)}}} + \right. \\ \left. \left. 2 i A \sin [c + d x] + 6 i B \tan [c + d x] \right) \right) / \left( 3 d \sqrt{\sec [c + d x]} \right)$$

**Problem 190: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec [c + d x])^2 (A + B \sec [c + d x])}{\sec [c + d x]^{5/2}} dx$$

Optimal (type 4, 166 leaves, 7 steps):

$$\frac{1}{5 d} 4 a^2 (4 A + 5 B) \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} + \\ \frac{4 a^2 (A + 2 B) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{3 d} + \\ \frac{2 a^2 (7 A + 5 B) \sin [c + d x]}{15 d \sqrt{\sec [c + d x]}} + \frac{2 A (a^2 + a^2 \sec [c + d x]) \sin [c + d x]}{5 d \sec [c + d x]^{3/2}}$$

Result (type 5, 155 leaves):

$$\frac{1}{30 d} a^2 \sqrt{\sec [c + d x]} \left( 40 (A + 2 B) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] + \right. \\ \left. 24 i (4 A + 5 B) e^{-i (c+d x)} \sqrt{1 + e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)} \right] + \right. \\ \left. 2 \cos [c + d x] (-12 i (4 A + 5 B) + 10 (2 A + B) \sin [c + d x] + 3 A \sin [2 (c + d x)]) \right)$$

**Problem 191: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec [c + d x])^2 (A + B \sec [c + d x])}{\sec [c + d x]^{7/2}} dx$$

Optimal (type 4, 201 leaves, 8 steps):

$$\frac{1}{5 d} 4 a^2 (3 A + 4 B) \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} + \\ \frac{1}{21 d} 4 a^2 (6 A + 7 B) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} + \\ \frac{2 a^2 (9 A + 7 B) \sin [c + d x]}{35 d \sec [c + d x]^{3/2}} + \frac{4 a^2 (6 A + 7 B) \sin [c + d x]}{21 d \sqrt{\sec [c + d x]}} + \frac{2 A (a^2 + a^2 \sec [c + d x]) \sin [c + d x]}{7 d \sec [c + d x]^{5/2}}$$

Result (type 5, 207 leaves):

$$\begin{aligned} & \frac{1}{420 d} a^2 e^{-i(2c+dx)} \sqrt{\sec[c+dx]} \left( 80(6A+7B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \right. \\ & \quad 336i(3A+4B) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & \quad 2\cos[c+dx](-504iA-672iB+5(51A+56B)\sin[c+dx] + \\ & \quad \left. 42(2A+B)\sin[2(c+dx)] + 15A\sin[3(c+dx)]\right) \left( \cos[2c+dx] + i\sin[2c+dx] \right) \end{aligned}$$

Problem 192: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \sec[c+dx])^2 (A + B \sec[c+dx])}{\sec[c+dx]^{9/2}} dx$$

Optimal (type 4, 234 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{15 d} 4 a^2 (8 A + 9 B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21 d} 4 a^2 (5 A + 6 B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{2 a^2 (11 A + 9 B) \sin[c+dx]}{63 d \sec[c+dx]^{5/2}} + \frac{4 a^2 (8 A + 9 B) \sin[c+dx]}{45 d \sec[c+dx]^{3/2}} + \\ & \frac{4 a^2 (5 A + 6 B) \sin[c+dx]}{21 d \sqrt{\sec[c+dx]}} + \frac{2 A (a^2 + a^2 \sec[c+dx]) \sin[c+dx]}{9 d \sec[c+dx]^{7/2}} \end{aligned}$$

Result (type 5, 231 leaves):

$$\begin{aligned} & \frac{1}{2520 d} a^2 e^{-i(2c+dx)} \sqrt{\sec[c+dx]} \left( 480(5A+6B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \right. \\ & \quad 672i(8A+9B) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & \quad 2\cos[c+dx](-2688iA-3024iB+30(46A+51B)\sin[c+dx] + \\ & \quad 14(37A+36B)\sin[2(c+dx)] + 180A\sin[3(c+dx)] + \\ & \quad \left. 90B\sin[3(c+dx)] + 35A\sin[4(c+dx)]\right) \left( \cos[2c+dx] + i\sin[2c+dx] \right) \end{aligned}$$

Problem 193: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sec[c+dx]^{3/2} (a + a \sec[c+dx])^3 (A + B \sec[c+dx]) dx$$

Optimal (type 4, 277 leaves, 10 steps):

$$\begin{aligned}
 & -\frac{1}{15d} 4a^3 (21A + 17B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{1}{21d} 4a^3 (13A + 11B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{4a^3 (21A + 17B) \sqrt{\sec[c+dx]} \sin[c+dx]}{15d} + \\
 & \frac{4a^3 (13A + 11B) \sec[c+dx]^{3/2} \sin[c+dx]}{21d} + \frac{4a^3 (24A + 23B) \sec[c+dx]^{5/2} \sin[c+dx]}{105d} + \\
 & \frac{2aB \sec[c+dx]^{5/2} (a + a \sec[c+dx])^2 \sin[c+dx]}{9d} + \\
 & \frac{2(9A + 13B) \sec[c+dx]^{5/2} (a^3 + a^3 \sec[c+dx]) \sin[c+dx]}{63d}
 \end{aligned}$$

Result(type 5, 773 leaves):

$$\begin{aligned}
& - \left( \left( 7 A e^{-i (2 c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \cos [c+d x]^4 \csc [c] \right. \right. \\
& \quad \left( 1+e^{2 i (c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \\
& \quad \left. \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \left( 10 \sqrt{2} d (B+A \cos [c+d x]) \right) - \\
& \left( 17 B e^{-i (2 c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \cos [c+d x]^4 \csc [c] \right. \\
& \quad \left( 1+e^{2 i (c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \\
& \quad \left. \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \left( 30 \sqrt{2} d (B+A \cos [c+d x]) \right) + \\
& \left( 13 A \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \right. \\
& \quad \left. (A+B \sec [c+d x]) \right) / \left( 42 d (B+A \cos [c+d x]) \sec [c+d x]^{7/2} \right) + \\
& \left( 11 B \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \right. \\
& \quad \left. (A+B \sec [c+d x]) \right) / \left( 42 d (B+A \cos [c+d x]) \sec [c+d x]^{7/2} \right) + \\
& \left( \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right. \\
& \quad \left( \frac{(21 A+17 B) \cos [d x] \csc [c]}{30 d} + \frac{B \sec [c] \sec [c+d x]^4 \sin [d x]}{36 d} + \right. \\
& \quad \frac{\sec [c] \sec [c+d x]^3 (7 B \sin [c] + 9 A \sin [d x] + 27 B \sin [d x])}{252 d} + \frac{1}{1260 d} \\
& \quad \sec [c] \sec [c+d x]^2 (45 A \sin [c] + 135 B \sin [c] + 189 A \sin [d x] + 238 B \sin [d x]) + \\
& \quad \frac{1}{1260 d} \sec [c] \sec [c+d x] (189 A \sin [c] + 238 B \sin [c] + 390 A \sin [d x] + 330 B \sin [d x]) + \\
& \quad \left. \left. \frac{(13 A+11 B) \tan [c]}{42 d} \right) \right) / \left( (B+A \cos [c+d x]) \sec [c+d x]^{7/2} \right)
\end{aligned}$$

**Problem 194:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{\sec [c+d x]} (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) dx$$

Optimal (type 4, 244 leaves, 9 steps):

$$\begin{aligned}
 & -\frac{1}{5d} 4a^3 (9A+7B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{1}{21d} 4a^3 (21A+13B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
 & \frac{4a^3 (9A+7B) \sqrt{\sec[c+dx]} \sin[c+dx]}{5d} + \frac{4a^3 (42A+41B) \sec[c+dx]^{3/2} \sin[c+dx]}{105d} + \\
 & \frac{2aB \sec[c+dx]^{3/2} (a+a \sec[c+dx])^2 \sin[c+dx]}{7d} + \\
 & \frac{2(7A+11B) \sec[c+dx]^{3/2} (a^3+a^3 \sec[c+dx]) \sin[c+dx]}{35d}
 \end{aligned}$$

Result (type 5, 731 leaves):



$$\begin{aligned}
& - \left( \left( 9 A e^{-i (2 c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \cos [c+d x]^4 \csc [c] \right. \right. \\
& \quad \left( 1+e^{2 i (c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \\
& \quad \left. \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \left( 10 \sqrt{2} d (B+A \cos [c+d x]) \right) \Bigg) - \\
& \left( 7 B e^{-i (2 c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \cos [c+d x]^4 \csc [c] \right. \\
& \quad \left( 1+e^{2 i (c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \\
& \quad \left. \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \left( 10 \sqrt{2} d (B+A \cos [c+d x]) \right) \Bigg) + \\
& \left( A \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \right. \\
& \quad \left. (A+B \sec [c+d x]) \right) / \left( 2 d (B+A \cos [c+d x]) \sec [c+d x]^{7/2} \right) + \\
& \left( 13 B \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 \right. \\
& \quad \left. (A+B \sec [c+d x]) \right) / \left( 42 d (B+A \cos [c+d x]) \sec [c+d x]^{7/2} \right) + \\
& \left( \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^6 (a+a \sec [c+d x])^3 (A+B \sec [c+d x]) \right. \\
& \quad \left( \frac{(9 A+7 B) \cos [d x] \csc [c]}{10 d} + \frac{B \sec [c] \sec [c+d x]^3 \sin [d x]}{28 d} + \right. \\
& \quad \frac{\sec [c] \sec [c+d x]^2 (5 B \sin [c] + 7 A \sin [d x] + 21 B \sin [d x])}{140 d} + \frac{1}{420 d} \\
& \quad \left. \sec [c] \sec [c+d x] (21 A \sin [c] + 63 B \sin [c] + 105 A \sin [d x] + 130 B \sin [d x]) + \right. \\
& \quad \left. \frac{(21 A+26 B) \tan [c]}{84 d} \right) \Bigg) / \left( (B+A \cos [c+d x]) \sec [c+d x]^{7/2} \right)
\end{aligned}$$

**Problem 195: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec [c+d x])^3 (A+B \sec [c+d x])}{\sqrt{\sec [c+d x]}} dx$$

Optimal (type 4, 211 leaves, 8 steps):

$$\begin{aligned}
& -\frac{1}{5d} 4a^3 (5A+9B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
& \frac{1}{3d} 4a^3 (5A+3B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
& \frac{4a^3 (20A+21B) \sqrt{\sec[c+dx]} \sin[c+dx]}{15d} + \\
& \frac{2aB \sqrt{\sec[c+dx]} (a+a \sec[c+dx])^2 \sin[c+dx]}{5d} + \\
& \frac{2(5A+9B) \sqrt{\sec[c+dx]} (a^3+a^3 \sec[c+dx]) \sin[c+dx]}{15d}
\end{aligned}$$

Result (type 5, 257 leaves):

$$\begin{aligned}
& \frac{1}{30d} a^3 e^{-i(2c+dx)} \sec[c+dx]^{5/2} \left( 90i A \cos[c+dx] + 162i B \cos[c+dx] + 30i A \cos[3(c+dx)] + \right. \\
& 54i B \cos[3(c+dx)] + 40(5A+3B) \cos[c+dx]^{5/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] - \\
& 6i(5A+9B) e^{-3i(c+dx)} (1+e^{2i(c+dx)})^{5/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\
& 45A \sin[c+dx] + 66B \sin[c+dx] + 10A \sin[2(c+dx)] + 30B \sin[2(c+dx)] + \\
& \left. 45A \sin[3(c+dx)] + 54B \sin[3(c+dx)] \right) (\cos[2c+dx] + i \sin[2c+dx])
\end{aligned}$$

**Problem 196: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec[c+dx])^3 (A+B \sec[c+dx])}{\sec[c+dx]^{3/2}} dx$$

Optimal (type 4, 199 leaves, 8 steps):

$$\begin{aligned}
& \frac{4a^3 (A-B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{d} + \\
& \frac{20a^3 (A+B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3d} + \\
& \frac{4a^3 (A+4B) \sqrt{\sec[c+dx]} \sin[c+dx]}{3d} + \frac{2aA (a+a \sec[c+dx])^2 \sin[c+dx]}{3d \sqrt{\sec[c+dx]}} - \\
& \frac{2(A-B) \sqrt{\sec[c+dx]} (a^3+a^3 \sec[c+dx]) \sin[c+dx]}{3d}
\end{aligned}$$

Result (type 5, 226 leaves):

$$\begin{aligned} & \frac{1}{6d} a^3 e^{-i(2c+dx)} \operatorname{Sec}[c+dx]^{3/2} \left( -12iA + 12iB - 12iA \cos[2(c+dx)] + \right. \\ & 12iB \cos[2(c+dx)] + 40(A+B) \cos[c+dx]^{3/2} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \\ & 12i(A-B) e^{-2i(c+dx)} \left(1 + e^{2i(c+dx)}\right)^{3/2} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & A \sin[c+dx] + 4B \sin[c+dx] + 6A \sin[2(c+dx)] + \\ & \left. 18B \sin[2(c+dx)] + A \sin[3(c+dx)] \right) (\cos[2c+dx] + i \sin[2c+dx]) \end{aligned}$$

**Problem 197: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c+dx])^3 (A + B \operatorname{Sec}[c+dx])}{\operatorname{Sec}[c+dx]^{5/2}} dx$$

Optimal (type 4, 211 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{5d} 4a^3 (9A + 5B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} + \\ & \frac{1}{3d} 4a^3 (3A + 5B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\operatorname{Sec}[c+dx]} - \\ & \frac{4a^3 (6A - 5B) \sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{15d} + \frac{2aA (a + a \operatorname{Sec}[c+dx])^2 \sin[c+dx]}{5d \operatorname{Sec}[c+dx]^{3/2}} + \\ & \frac{2(9A + 5B) (a^3 + a^3 \operatorname{Sec}[c+dx]) \sin[c+dx]}{15d \sqrt{\operatorname{Sec}[c+dx]}} \end{aligned}$$

Result (type 5, 220 leaves):

$$\begin{aligned} & \frac{1}{30d} a^3 e^{-i(2c+dx)} \sqrt{\operatorname{Sec}[c+dx]} \left( -216iA \cos[c+dx] - \right. \\ & 120iB \cos[c+dx] + 40(3A + 5B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \\ & 24i(9A + 5B) e^{-i(c+dx)} \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & 3A \sin[c+dx] + 60B \sin[c+dx] + 30A \sin[2(c+dx)] + \\ & \left. 10B \sin[2(c+dx)] + 3A \sin[3(c+dx)] \right) (\cos[2c+dx] + i \sin[2c+dx]) \end{aligned}$$

**Problem 198: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \operatorname{Sec}[c+dx])^3 (A + B \operatorname{Sec}[c+dx])}{\operatorname{Sec}[c+dx]^{7/2}} dx$$

Optimal (type 4, 211 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{5d} 4a^3 (7A+9B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21d} 4a^3 (13A+21B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{4a^3 (41A+42B) \sin[c+dx]}{105d \sqrt{\sec[c+dx]}} + \frac{2aA (a+a \sec[c+dx])^2 \sin[c+dx]}{7d \sec[c+dx]^{5/2}} + \\ & \frac{2(11A+7B) (a^3+a^3 \sec[c+dx]) \sin[c+dx]}{35d \sec[c+dx]^{3/2}} \end{aligned}$$

Result (type 5, 208 leaves):

$$\begin{aligned} & \frac{1}{420d} a^3 e^{-i(2c+dx)} \sqrt{\sec[c+dx]} \left( 80(13A+21B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + \right. \\ & 336i(7A+9B) e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + \\ & 2\cos[c+dx] (-168i(7A+9B) + 5(107A+84B) \sin[c+dx] + \\ & \left. 42(3A+B) \sin[2(c+dx)] + 15A \sin[3(c+dx)] \right) \left( \cos[2c+dx] + i \sin[2c+dx] \right) \end{aligned}$$

**Problem 199: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec[c+dx])^3 (A+B \sec[c+dx])}{\sec[c+dx]^{9/2}} dx$$

Optimal (type 4, 244 leaves, 9 steps):

$$\begin{aligned} & \frac{1}{15d} 4a^3 (17A+21B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{1}{21d} 4a^3 (11A+13B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \frac{4a^3 (23A+24B) \sin[c+dx]}{105d \sec[c+dx]^{3/2}} + \frac{4a^3 (11A+13B) \sin[c+dx]}{21d \sqrt{\sec[c+dx]}} + \\ & \frac{2aA (a+a \sec[c+dx])^2 \sin[c+dx]}{9d \sec[c+dx]^{7/2}} + \frac{2(13A+9B) (a^3+a^3 \sec[c+dx]) \sin[c+dx]}{63d \sec[c+dx]^{5/2}} \end{aligned}$$

Result (type 5, 197 leaves):

$$\begin{aligned} & \frac{1}{2520d} a^3 \sqrt{\sec[c+dx]} \left( 480(11A+13B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] + 672i(17A+21B) \right. \\ & e^{-i(c+dx)} \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] + 2\cos[c+dx] \\ & (-5712iA - 7056iB + 30(97A+107B) \sin[c+dx] + 14(73A+54B) \sin[2(c+dx)] + \\ & \left. 270A \sin[3(c+dx)] + 90B \sin[3(c+dx)] + 35A \sin[4(c+dx)] \right) \end{aligned}$$

**Problem 200: Result unnecessarily involves higher level functions and more**

than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sec}[c + d x])^3 (A + B \operatorname{Sec}[c + d x])}{\operatorname{Sec}[c + d x]^{11/2}} dx$$

Optimal (type 4, 277 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{15 d} 4 a^3 (15 A + 17 B) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{1}{231 d} 4 a^3 (105 A + 121 B) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]} + \\ & \frac{20 a^3 (21 A + 22 B) \operatorname{Sin}[c + d x]}{693 d \operatorname{Sec}[c + d x]^{5/2}} + \frac{4 a^3 (15 A + 17 B) \operatorname{Sin}[c + d x]}{45 d \operatorname{Sec}[c + d x]^{3/2}} + \frac{4 a^3 (105 A + 121 B) \operatorname{Sin}[c + d x]}{231 d \sqrt{\operatorname{Sec}[c + d x]}} + \\ & \frac{2 a A (a + a \operatorname{Sec}[c + d x])^2 \operatorname{Sin}[c + d x]}{11 d \operatorname{Sec}[c + d x]^{9/2}} + \frac{2 (15 A + 11 B) (a^3 + a^3 \operatorname{Sec}[c + d x]) \operatorname{Sin}[c + d x]}{99 d \operatorname{Sec}[c + d x]^{7/2}} \end{aligned}$$

Result (type 5, 864 leaves):

$$\begin{aligned}
& \left( A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \csc[c] \right. \\
& \quad \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \right) / (2\sqrt{2} d (B+A \cos[c+dx])) + \\
& \left( 17 B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos[c+dx]^4 \csc[c] \right. \\
& \quad \left( 1+e^{2i(c+dx)} + (-1+e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \right) / (30\sqrt{2} d (B+A \cos[c+dx])) + \\
& \left( 5 A \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 \right. \\
& \quad \left. (A+B \sec[c+dx]) \right) / (22 d (B+A \cos[c+dx]) \sec[c+dx]^{7/2}) + \\
& \left( 11 B \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 \right. \\
& \quad \left. (A+B \sec[c+dx]) \right) / (42 d (B+A \cos[c+dx]) \sec[c+dx]^{7/2}) + \\
& \frac{1}{(B+A \cos[c+dx]) \sec[c+dx]^{7/2}} \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^6 (a+a \sec[c+dx])^3 (A+B \sec[c+dx]) \\
& \left( -\frac{1}{2880 d} (645 A + 743 B + 795 A \cos[2c] + 889 B \cos[2c]) \cos[dx] \csc[c] + \right. \\
& \quad \frac{(4473 A + 4664 B) \cos[2dx] \sin[2c]}{29568 d} + \frac{(165 A + 151 B) \cos[3dx] \sin[3c]}{2880 d} + \\
& \quad \frac{(49 A + 33 B) \cos[4dx] \sin[4c]}{2464 d} + \frac{(3 A + B) \cos[5dx] \sin[5c]}{576 d} + \\
& \quad \frac{A \cos[6dx] \sin[6c]}{1408 d} + \frac{(795 A + 889 B) \cos[c] \sin[dx]}{1440 d} + \\
& \quad \frac{(4473 A + 4664 B) \cos[2c] \sin[2dx]}{29568 d} + \frac{(165 A + 151 B) \cos[3c] \sin[3dx]}{2880 d} + \\
& \quad \left. \frac{(49 A + 33 B) \cos[4c] \sin[4dx]}{2464 d} + \frac{(3 A + B) \cos[5c] \sin[5dx]}{576 d} + \frac{A \cos[6c] \sin[6dx]}{1408 d} \right)
\end{aligned}$$

Problem 201: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sec[c+dx]^{7/2} (A+B \sec[c+dx])}{a+a \sec[c+dx]} dx$$

Optimal (type 4, 229 leaves, 9 steps):

$$\begin{aligned} & \frac{3(5A-7B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{5ad} + \\ & \frac{5(A-B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3ad} - \\ & \frac{3(5A-7B) \sqrt{\sec[c+dx]} \sin[c+dx]}{5ad} + \frac{5(A-B) \sec[c+dx]^{3/2} \sin[c+dx]}{3ad} - \\ & \frac{(5A-7B) \sec[c+dx]^{5/2} \sin[c+dx]}{5ad} + \frac{(A-B) \sec[c+dx]^{7/2} \sin[c+dx]}{d(a+a \sec[c+dx])} \end{aligned}$$

Result (type 5, 794 leaves):

$$\begin{aligned}
& \left( 3 A e^{-i (2 c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \cos\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1+e^{2 i (c+d x)}+(-1+e^{2 i c}) \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] (A+B \sec [c+d x]) \right) / \left( \sqrt{2} d (B+A \cos [c+d x]) (a+a \sec [c+d x]) \right) - \\
& \left( 21 B e^{-i (2 c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \cos\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1+e^{2 i (c+d x)}+(-1+e^{2 i c}) \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] (A+B \sec [c+d x]) \right) / \left( 5 \sqrt{2} d (B+A \cos [c+d x]) (a+a \sec [c+d x]) \right) + \\
& \left( 5 A \cos\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \sqrt{\cos [c+d x]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sec\left[\frac{c}{2}\right] \sqrt{\sec [c+d x]} \right. \\
& \quad \left. (A+B \sec [c+d x]) \sin [c] \right) / \left( 3 d (B+A \cos [c+d x]) (a+a \sec [c+d x]) \right) - \\
& \left( 5 B \cos\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \sqrt{\cos [c+d x]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sec\left[\frac{c}{2}\right] \sqrt{\sec [c+d x]} \right. \\
& \quad \left. (A+B \sec [c+d x]) \sin [c] \right) / \left( 3 d (B+A \cos [c+d x]) (a+a \sec [c+d x]) \right) + \\
& \left( \cos\left[\frac{c}{2}+\frac{d x}{2}\right]^2 \sqrt{\sec [c+d x]} (A+B \sec [c+d x]) \right. \\
& \quad \left( \frac{3(-5 A+7 B) \cos [d x] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{5 d} - \frac{(-A+B) \sec\left[\frac{c}{2}\right] \sec [c] \left(-\sin\left[\frac{c}{2}\right]+5 \sin\left[\frac{3 c}{2}\right]\right)}{3 d} - \right. \\
& \quad \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}+\frac{d x}{2}\right] \left(-A \sin\left[\frac{d x}{2}\right]+B \sin\left[\frac{d x}{2}\right]\right)}{d} + \frac{4 B \sec [c] \sec [c+d x]^2 \sin [d x]}{5 d} + \\
& \quad \left. \frac{4 \sec [c] \sec [c+d x] \left(3 B \sin [c]+5 A \sin [d x]-5 B \sin [d x]\right)}{15 d} \right) / \\
& \quad \left( (B+A \cos [c+d x]) (a+a \sec [c+d x]) \right)
\end{aligned}$$

**Problem 202: Result unnecessarily involves higher level functions.**

$$\int \frac{\sec [c+d x]^{5 / 2} (A+B \sec [c+d x])}{a+a \sec [c+d x]} d x$$

Optimal (type 4, 192 leaves, 8 steps):



$$\begin{aligned}
& - \frac{3 (A - B) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{a d} \\
& + \frac{(3A - 5B) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{3 a d} \\
& - \frac{3 (A - B) \sqrt{\sec[c + dx]} \sin[c + dx]}{a d} \\
& + \frac{(3A - 5B) \sec[c + dx]^{3/2} \sin[c + dx]}{3 a d} + \frac{(A - B) \sec[c + dx]^{5/2} \sin[c + dx]}{d (a + a \sec[c + dx])}
\end{aligned}$$

Result (type 5, 371 leaves):

$$\begin{aligned}
& - \frac{1}{3 a d (1 + e^{2i(c+dx)}) (B + A \cos[c + dx]) (1 + \sec[c + dx])} \\
& e^{-\frac{3}{2}i(c+dx)} \cos\left[\frac{1}{2}(c + dx)\right] \left( (3A - 5B) e^{i(c+dx)} (1 + e^{i(c+dx)} + e^{2i(c+dx)} + e^{3i(c+dx)}) \right. \\
& \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] - i \left( 9A - 9B + 6A e^{i(c+dx)} - 4B e^{i(c+dx)} + \right. \\
& 12A e^{2i(c+dx)} - 10B e^{2i(c+dx)} + 6A e^{3i(c+dx)} - 8B e^{3i(c+dx)} + 3A e^{4i(c+dx)} - \\
& 5B e^{4i(c+dx)} - 9(A - B) \sqrt{1 + e^{2i(c+dx)}} (1 + e^{i(c+dx)} + e^{2i(c+dx)} + e^{3i(c+dx)}) \\
& \left. \left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right]\right) \right) \sqrt{\sec[c + dx]} (A + B \sec[c + dx])
\end{aligned}$$

**Problem 203: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^{3/2} (A + B \sec[c + dx])}{a + a \sec[c + dx]} dx$$

Optimal (type 4, 153 leaves, 7 steps):

$$\begin{aligned}
& \frac{(A - 3B) \sqrt{\cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{a d} + \\
& \frac{(A - B) \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right] \sqrt{\sec[c + dx]}}{a d} - \\
& \frac{(A - 3B) \sqrt{\sec[c + dx]} \sin[c + dx]}{a d} + \frac{(A - B) \sec[c + dx]^{3/2} \sin[c + dx]}{d (a + a \sec[c + dx])}
\end{aligned}$$

Result (type 5, 705 leaves):

$$\begin{aligned}
& \left( A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] (A+B \sec[c+dx]) \right) / \left( \sqrt{2} d (B+A \cos[c+dx]) (a+a \sec[c+dx]) \right) - \\
& \left( 3 B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] (A+B \sec[c+dx]) \right) / \left( \sqrt{2} d (B+A \cos[c+dx]) (a+a \sec[c+dx]) \right) + \\
& \left( A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sqrt{\sec[c+dx]} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx]) \right) - \\
& \left( B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sqrt{\sec[c+dx]} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx]) \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sqrt{\sec[c+dx]} (A+B \sec[c+dx]) \right) \left( \frac{(-A+3B) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{d} - \right. \\
& \quad \left. \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] \left(-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right]\right)}{d} - \frac{2(-A+B) \tan\left[\frac{c}{2}\right]}{d} \right) / \\
& \quad \left( (B+A \cos[c+dx]) (a+a \sec[c+dx]) \right)
\end{aligned}$$

**Problem 204: Result unnecessarily involves higher level functions.**

$$\int \frac{\sqrt{\sec[c+dx]} (A+B \sec[c+dx])}{a+a \sec[c+dx]} dx$$

Optimal (type 4, 123 leaves, 6 steps):

$$\begin{aligned}
& - \frac{(A-B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} + \\
& \frac{(A+B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} + \\
& \frac{(A-B) \sqrt{\sec[c+dx]} \sin[c+dx]}{d(a+a \sec[c+dx])}
\end{aligned}$$

Result (type 5, 207 leaves):

$$\begin{aligned}
& \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{4(A+B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{d} + \right. \right. \\
& \frac{1}{d(1+e^{i(c+dx)})} 4i(A-B) e^{-i(c+dx)} \\
& \left. \left( 1+e^{2i(c+dx)} - (1+e^{i(c+dx)}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \left. \left. \sqrt{\sec[c+dx]} \right) (A+B \sec[c+dx]) \right) / (2a(B+A \cos[c+dx])(1+\sec[c+dx]))
\end{aligned}$$

**Problem 205: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx]}{\sqrt{\sec[c+dx]} (a+a \sec[c+dx])} dx$$

Optimal (type 4, 128 leaves, 6 steps):

$$\begin{aligned}
& \frac{(3A-B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} - \\
& \frac{(A-B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{ad} - \\
& \frac{(A-B) \sqrt{\sec[c+dx]} \sin[c+dx]}{d(a+a \sec[c+dx])}
\end{aligned}$$

Result (type 5, 425 leaves):

$$\begin{aligned}
& \frac{1}{2 a d (B + A \cos [c + d x]) (1 + \sec [c + d x])} \\
& \cos \left[ \frac{1}{2} (c + d x) \right]^2 \left( 6 \sqrt{2} A e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \csc [c] \right. \\
& \quad \left. \left( 1 + e^{2 i (c + d x)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)} \right] \right) - \right. \\
& \quad 2 \sqrt{2} B e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \csc [c] \\
& \quad \left. \left( 1 + e^{2 i (c + d x)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)} \right] \right) \right) - \\
& \frac{1}{\sqrt{\sec [c + d x]}} 2 \left( (2 A - B) \cos \left[ \frac{1}{2} (c - d x) \right] + A \cos \left[ \frac{1}{2} (3 c + d x) \right] \right) \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \\
& \sec \left[ \frac{1}{2} (c + d x) \right] - 4 A \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} + \\
& 4 B \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} \right) (A + B \sec [c + d x])
\end{aligned}$$

**Problem 206: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x]}{\sec [c + d x]^{3/2} (a + a \sec [c + d x])} dx$$

Optimal (type 4, 164 leaves, 7 steps):

$$\begin{aligned}
& - \frac{3 (A - B) \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{a d} + \\
& \frac{(5 A - 3 B) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{3 a d} + \\
& \frac{(5 A - 3 B) \sin [c + d x]}{3 a d \sqrt{\sec [c + d x]}} - \frac{(A - B) \sin [c + d x]}{d \sqrt{\sec [c + d x]} (a + a \sec [c + d x])}
\end{aligned}$$

Result (type 5, 479 leaves):

$$\begin{aligned}
& \frac{1}{6 a d (B + A \cos [c + d x]) (1 + \sec [c + d x])} \\
& \cos \left[ \frac{1}{2} (c + d x) \right]^2 (A + B \sec [c + d x]) \left( -18 \sqrt{2} A e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \csc [c] \right. \\
& \quad \left. \left( 1 + e^{2 i (c + d x)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)} \right] \right) + \right. \\
& \quad 18 \sqrt{2} B e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \csc [c] \\
& \quad \left. \left( 1 + e^{2 i (c + d x)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)} \right] \right) + \right. \\
& \quad 20 A \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} - \\
& \quad 12 B \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} + \\
& \quad 2 \sqrt{\sec [c + d x]} \left( 3 (A - B) (2 + \cos [2 c]) \cos [d x] \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] + \right. \\
& \quad 2 A \cos [2 d x] \sin [2 c] - 6 (A - B) \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{1}{2} (c + d x) \right] \sin \left[ \frac{d x}{2} \right] - \\
& \quad \left. \left. 12 (A - B) \cos [c] \sin [d x] + 2 A \cos [2 c] \sin [2 d x] - 6 (A - B) \tan \left[ \frac{c}{2} \right] \right) \right)
\end{aligned}$$

**Problem 207: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x]}{\sec [c + d x]^{5/2} (a + a \sec [c + d x])} dx$$

Optimal (type 4, 197 leaves, 8 steps):

$$\begin{aligned}
& \frac{3 (7 A - 5 B) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{5 a d} - \\
& \frac{5 (A - B) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{3 a d} + \\
& \frac{(7 A - 5 B) \sin [c + d x]}{5 a d \sec [c + d x]^{3/2}} - \frac{5 (A - B) \sin [c + d x]}{3 a d \sqrt{\sec [c + d x]}} - \frac{(A - B) \sin [c + d x]}{d \sec [c + d x]^{3/2} (a + a \sec [c + d x])}
\end{aligned}$$

Result (type 5, 520 leaves):

$$\begin{aligned}
& \frac{1}{60 a d (B + A \cos [c + d x]) (1 + \sec [c + d x])} \\
& \cos \left[ \frac{1}{2} (c + d x) \right]^2 (A + B \sec [c + d x]) \left( 252 \sqrt{2} A e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \csc [c] \right. \\
& \quad \left( 1 + e^{2 i (c + d x)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)} \right] \right) - \\
& \quad 180 \sqrt{2} B e^{-i (2 c + d x)} \sqrt{\frac{e^{i (c + d x)}}{1 + e^{2 i (c + d x)}}} \csc [c] \\
& \quad \left( 1 + e^{2 i (c + d x)} + (-1 + e^{2 i c}) \sqrt{1 + e^{2 i (c + d x)}} \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c + d x)} \right] \right) - \\
& \quad 200 A \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} + \\
& \quad 200 B \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]} + \\
& \quad \sqrt{\sec [c + d x]} \left( -3 (51 A - 40 B + (33 A - 20 B) \cos [2 c]) \cos [d x] \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] - \right. \\
& \quad 40 (A - B) \cos [2 d x] \sin [2 c] + 12 A \cos [3 d x] \sin [3 c] + \\
& \quad 120 (A - B) \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{1}{2} (c + d x) \right] \sin \left[ \frac{d x}{2} \right] + 12 (33 A - 20 B) \cos [c] \sin [d x] - \\
& \quad \left. 40 (A - B) \cos [2 c] \sin [2 d x] + 12 A \cos [3 c] \sin [3 d x] + 120 (A - B) \tan \left[ \frac{c}{2} \right] \right) \Bigg)
\end{aligned}$$

**Problem 208: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x]}{\sec [c + d x]^{7/2} (a + a \sec [c + d x])} dx$$

Optimal (type 4, 230 leaves, 9 steps):

$$\begin{aligned}
& - \frac{21 (A - B) \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{5 a d} + \\
& \frac{5 (9 A - 7 B) \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right] \sqrt{\sec [c + d x]}}{21 a d} + \frac{(9 A - 7 B) \sin [c + d x]}{7 a d \sec [c + d x]^{5/2}} - \\
& \frac{7 (A - B) \sin [c + d x]}{5 a d \sec [c + d x]^{3/2}} + \frac{5 (9 A - 7 B) \sin [c + d x]}{21 a d \sqrt{\sec [c + d x]}} - \frac{(A - B) \sin [c + d x]}{d \sec [c + d x]^{5/2} (a + a \sec [c + d x])}
\end{aligned}$$

Result (type 5, 864 leaves):

$$\begin{aligned}
& - \left( \left( 21 A e^{-i (2 c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \csc\left[\frac{c}{2}\right] \right. \right. \\
& \quad \left. \left( 1+e^{2 i (c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] (A+B \sec[c+d x]) \right) / \left( 5 \sqrt{2} d (B+A \cos[c+d x]) (a+a \sec[c+d x]) \right) \Bigg) + \\
& \left( 21 B e^{-i (2 c+d x)} \sqrt{\frac{e^{i (c+d x)}}{1+e^{2 i (c+d x)}}} \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1+e^{2 i (c+d x)} + (-1+e^{2 i c}) \sqrt{1+e^{2 i (c+d x)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i (c+d x)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] (A+B \sec[c+d x]) \right) / \left( 5 \sqrt{2} d (B+A \cos[c+d x]) (a+a \sec[c+d x]) \right) \Bigg) + \\
& \left( 15 A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sqrt{\cos[c+d x]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sec\left[\frac{c}{2}\right] \sqrt{\sec[c+d x]} \right. \\
& \quad \left. (A+B \sec[c+d x]) \sin[c] \right) / \left( 7 d (B+A \cos[c+d x]) (a+a \sec[c+d x]) \right) - \\
& \left( 5 B \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sqrt{\cos[c+d x]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sec\left[\frac{c}{2}\right] \sqrt{\sec[c+d x]} \right. \\
& \quad \left. (A+B \sec[c+d x]) \sin[c] \right) / \left( 3 d (B+A \cos[c+d x]) (a+a \sec[c+d x]) \right) + \\
& \frac{1}{(B+A \cos[c+d x]) (a+a \sec[c+d x])} \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sqrt{\sec[c+d x]} \\
& (A+B \sec[c+d x]) \left( -\frac{3(-A+B)(17+11 \cos[2 c]) \cos[d x] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{20 d} - \right. \\
& \quad \frac{(-27 A+14 B) \cos[2 d x] \sin[2 c]}{21 d} + \frac{(-A+B) \cos[3 d x] \sin[3 c]}{5 d} + \\
& \quad \frac{A \cos[4 d x] \sin[4 c]}{14 d} + \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right] \left(-A \sin\left[\frac{d x}{2}\right] + B \sin\left[\frac{d x}{2}\right]\right)}{d} + \\
& \quad \frac{33(-A+B) \cos[c] \sin[d x]}{5 d} - \frac{(-27 A+14 B) \cos[2 c] \sin[2 d x]}{21 d} + \\
& \quad \left. \frac{(-A+B) \cos[3 c] \sin[3 d x]}{5 d} + \frac{A \cos[4 c] \sin[4 d x]}{14 d} + \frac{2(-A+B) \tan\left[\frac{c}{2}\right]}{d} \right) \Bigg)
\end{aligned}$$

Problem 209: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x]^{7 / 2} (A+B \sec [c+d x])}{(a+a \sec [c+d x])^2} d x$$

Optimal (type 4, 237 leaves, 9 steps):

$$\begin{aligned} & - \frac{(4 A-7 B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{a^2 d} - \\ & \frac{5(A-2 B) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 a^2 d} + \\ & \frac{(4 A-7 B) \sqrt{\sec [c+d x]} \sin [c+d x]}{a^2 d} - \frac{5(A-2 B) \sec [c+d x]^{3 / 2} \sin [c+d x]}{3 a^2 d} + \\ & \frac{(4 A-7 B) \sec [c+d x]^{5 / 2} \sin [c+d x]}{3 a^2 d(1+\sec [c+d x])} + \frac{(A-B) \sec [c+d x]^{7 / 2} \sin [c+d x]}{3 d(a+a \sec [c+d x])^2} \end{aligned}$$

Result (type 5, 841 leaves):



$$\begin{aligned}
& - \left( \left( 4 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( 7 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \\
& \quad \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) - \\
& \left( 10 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \sin[c] \right) / \\
& \quad \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( 20 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \right. \\
& \quad \left( -\frac{2(-4A+7B) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{d} + \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3d} \right. \\
& \quad \left. \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-5A \sin\left[\frac{dx}{2}\right] + 8B \sin\left[\frac{dx}{2}\right])}{3d} + \frac{8B \sec[c] \sec[c+dx] \sin[dx]}{3d} \right. \\
& \quad \left. \left. \frac{4(2B-5A \cos[c] + 10B \cos[c]) \sec[c] \tan\left[\frac{c}{2}\right]}{3d} + \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right) \right) / \\
& \quad \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right)
\end{aligned}$$

Problem 210: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x]^{5 / 2} (A+B \sec [c+d x])}{(a+a \sec [c+d x])^2} d x$$

Optimal (type 4, 204 leaves, 8 steps):

$$\begin{aligned} & \frac{(A-4 B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{a^2 d} + \\ & \frac{(2 A-5 B) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{3 a^2 d} - \\ & \frac{(A-4 B) \sqrt{\sec [c+d x]} \sin [c+d x]}{a^2 d} + \\ & \frac{(2 A-5 B) \sec [c+d x]^{3 / 2} \sin [c+d x]}{3 a^2 d (1+\sec [c+d x])} + \frac{(A-B) \sec [c+d x]^{5 / 2} \sin [c+d x]}{3 d (a+a \sec [c+d x])^2} \end{aligned}$$

Result (type 5, 811 leaves):

$$\begin{aligned}
& \left( \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) - \\
& \left( 4 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( 4 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) - \\
& \left( 10 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \right) \\
& \left( \frac{2(-A+4B) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{d} - \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3d} - \right. \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-2A \sin\left[\frac{dx}{2}\right] + 5B \sin\left[\frac{dx}{2}\right])}{3d} - \frac{4(-2A+5B) \tan\left[\frac{c}{2}\right]}{3d} - \\
& \quad \left. \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right) / \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right)
\end{aligned}$$

**Problem 211:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sec[c+dx]^{3/2} (A+B \sec[c+dx])}{(a+a \sec[c+dx])^2} dx$$

Optimal (type 4, 161 leaves, 7 steps):

$$\frac{B \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{a^2 d} +$$

$$\frac{(A+2B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3 a^2 d} -$$

$$\frac{B \sqrt{\sec[c+dx]} \sin[c+dx]}{a^2 d (1+\sec[c+dx])} + \frac{(A-B) \sec[c+dx]^{3/2} \sin[c+dx]}{3 d (a+a \sec[c+dx])^2}$$

Result(type 5, 617 leaves):

$$\left( \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right.$$

$$\left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right.$$

$$\left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) +$$

$$\left( 2 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right.$$

$$\left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) +$$

$$\left( 4 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right.$$

$$\left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) +$$

$$\left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \right.$$

$$\left( -\frac{2 B \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{d} + \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3 d} + \right.$$

$$\frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + 2 B \sin\left[\frac{dx}{2}\right])}{3 d} + \frac{4 (A+2B) \tan\left[\frac{c}{2}\right]}{3 d} +$$

$$\left. \frac{2 (-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3 d} \right) / \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right)$$

**Problem 212: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec[c+dx]} (A+B \sec[c+dx])}{(a+a \sec[c+dx])^2} dx$$

Optimal (type 4, 168 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{A \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{a^2 d} + \\
 & \frac{(2A+B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{3 a^2 d} + \\
 & \frac{(2A+B) \sqrt{\sec[c+dx]} \sin[c+dx]}{3 a^2 d (1+\sec[c+dx])} + \frac{(A-B) \sqrt{\sec[c+dx]} \sin[c+dx]}{3 d (a+a \sec[c+dx])^2}
 \end{aligned}$$

Result (type 5, 618 leaves):

$$\begin{aligned}
 & - \left( \left( \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \right. \\
 & \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
 & \quad \left. \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
 & \left( 4 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \right. \\
 & \quad \left. \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \sin[c] \right) / \\
 & \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
 & \left( 2 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right. \\
 & \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
 & \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \right. \\
 & \quad \left( \frac{2 A \cos[dx] \operatorname{Csc}\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{d} + \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-4 A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3 d} - \right. \\
 & \quad \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3 d} + \frac{4 (-4 A + B) \tan\left[\frac{c}{2}\right]}{3 d} - \\
 & \quad \left. \left. \frac{2 (-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3 d} \right) \right) / \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right)
 \end{aligned}$$

Problem 213: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 177 leaves, 7 steps):

$$\frac{(4A - B) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{a^2 d} - \frac{(5A - 2B) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{3 a^2 d} - \frac{(5A - 2B) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 a^2 d (1 + \operatorname{Sec}[c + d x])} - \frac{(A - B) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{3 d (a + a \operatorname{Sec}[c + d x])^2}$$

Result (type 5, 830 leaves):

$$\begin{aligned}
& \left( 4 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) - \\
& \left( \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) - \\
& \left( 10 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( 4 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \sin[c] \right) / \\
& \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sec[c+dx]^{3/2} \right. \\
& \quad (A+B \sec[c+dx]) \left( -\frac{2(3A-B+A \cos[2c]) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{d} + \right. \\
& \quad \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3 d} - \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-7 A \sin\left[\frac{dx}{2}\right] + 4 B \sin\left[\frac{dx}{2}\right])}{3 d} + \frac{8 A \cos[c] \sin[dx]}{d} - \\
& \quad \left. \frac{4(-7A+4B) \tan\left[\frac{c}{2}\right]}{3 d} + \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3 d} \right) / \\
& \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right)
\end{aligned}$$

Problem 214: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \sec[c + d x]}{\sec[c + d x]^{3/2} (a + a \sec[c + d x])^2} dx$$

Optimal (type 4, 211 leaves, 8 steps):

$$\begin{aligned} & - \frac{(7A - 4B) \sqrt{\cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]}}{a^2 d} + \\ & \frac{5(2A - B) \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]}}{3a^2 d} + \frac{5(2A - B) \sin[c + d x]}{3a^2 d \sqrt{\sec[c + d x]}} - \\ & \frac{(7A - 4B) \sin[c + d x]}{3a^2 d \sqrt{\sec[c + d x]} (1 + \sec[c + d x])} - \frac{(A - B) \sin[c + d x]}{3d \sqrt{\sec[c + d x]} (a + a \sec[c + d x])^2} \end{aligned}$$

Result (type 5, 875 leaves):



$$\begin{aligned}
& - \left( \left( 7 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( 4 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \\
& \quad \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( 20 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \sin[c] \right) / \\
& \quad \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) - \\
& \left( 10 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3 d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \right. \\
& \quad \left( -\frac{1}{d} 2 (-5A+3B-2A \cos[2c]+B \cos[2c]) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] + \right. \\
& \quad \frac{4A \cos[2dx] \sin[2c]}{3d} - \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3d} + \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-10A \sin\left[\frac{dx}{2}\right] + 7B \sin\left[\frac{dx}{2}\right])}{3d} + \frac{8(-2A+B) \cos[c] \sin[dx]}{d} + \\
& \quad \left. \frac{4A \cos[2c] \sin[2dx]}{3d} + \frac{4(-10A+7B) \tan\left[\frac{c}{2}\right]}{3d} - \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right) / \\
& \quad \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right)
\end{aligned}$$

Problem 215: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\operatorname{Sec}[c + d x]^{5/2} (a + a \operatorname{Sec}[c + d x])^2} dx$$

Optimal (type 4, 244 leaves, 9 steps):

$$\begin{aligned} & \frac{7 (8 A - 5 B) \sqrt{\cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{5 a^2 d} - \\ & \frac{5 (3 A - 2 B) \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\operatorname{Sec}[c + d x]}}{3 a^2 d} + \\ & \frac{7 (8 A - 5 B) \sin[c + d x]}{15 a^2 d \operatorname{Sec}[c + d x]^{3/2}} - \frac{5 (3 A - 2 B) \sin[c + d x]}{3 a^2 d \sqrt{\operatorname{Sec}[c + d x]}} - \\ & \frac{(3 A - 2 B) \sin[c + d x]}{a^2 d \operatorname{Sec}[c + d x]^{3/2} (1 + \operatorname{Sec}[c + d x])} - \frac{(A - B) \sin[c + d x]}{3 d \operatorname{Sec}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^2} \end{aligned}$$

Result (type 5, 924 leaves):

$$\begin{aligned}
& \left( 56 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) - \\
& \left( 7 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) - \\
& \left( 10 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \left( 20 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{3/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3d (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right) + \\
& \frac{1}{(B+A \cos[c+dx]) (a+a \sec[c+dx])^2} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \sec[c+dx]^{3/2} (A+B \sec[c+dx]) \\
& \left( \frac{1}{10d} (-151A + 100B - 73A \cos[2c] + 40B \cos[2c]) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] + \right. \\
& \quad \frac{4(-2A+B) \cos[2dx] \sin[2c]}{3d} + \frac{2A \cos[3dx] \sin[3c]}{5d} + \\
& \quad \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3d} - \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-13A \sin\left[\frac{dx}{2}\right] + 10B \sin\left[\frac{dx}{2}\right])}{3d} - \\
& \quad \frac{2(-73A + 40B) \cos[c] \sin[dx]}{5d} + \frac{4(-2A+B) \cos[2c] \sin[2dx]}{3d} + \\
& \quad \left. \frac{2A \cos[3c] \sin[3dx]}{5d} - \frac{4(-13A + 10B) \tan\left[\frac{c}{2}\right]}{3d} + \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right)
\end{aligned}$$

Problem 216: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{\text{Sec}[c + d x]^{9/2} (A + B \text{Sec}[c + d x])}{(a + a \text{Sec}[c + d x])^3} dx$$

Optimal (type 4, 292 leaves, 10 steps):

$$\begin{aligned} & -\frac{1}{10 a^3 d} 7 (7 A - 17 B) \sqrt{\text{Cos}[c + d x]} \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\text{Sec}[c + d x]} - \\ & \frac{(13 A - 33 B) \sqrt{\text{Cos}[c + d x]} \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\text{Sec}[c + d x]}}{6 a^3 d} + \\ & \frac{7 (7 A - 17 B) \sqrt{\text{Sec}[c + d x]} \text{Sin}[c + d x]}{10 a^3 d} - \\ & \frac{(13 A - 33 B) \text{Sec}[c + d x]^{3/2} \text{Sin}[c + d x]}{6 a^3 d} + \frac{(A - B) \text{Sec}[c + d x]^{9/2} \text{Sin}[c + d x]}{5 d (a + a \text{Sec}[c + d x])^3} + \\ & \frac{(A - 2 B) \text{Sec}[c + d x]^{7/2} \text{Sin}[c + d x]}{3 a d (a + a \text{Sec}[c + d x])^2} + \frac{7 (7 A - 17 B) \text{Sec}[c + d x]^{5/2} \text{Sin}[c + d x]}{30 d (a^3 + a^3 \text{Sec}[c + d x])} \end{aligned}$$

Result (type 5, 933 leaves):

$$\begin{aligned}
& - \left( \left( 49 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2i c}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 119 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2i c}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \\
& \quad \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) - \\
& \left( 26 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 22 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \frac{1}{(B+A \cos[c+dx]) (a+a \sec[c+dx])^3} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c+dx]^{5/2} (A+B \sec[c+dx]) \\
& \left( -\frac{14(-7A+17B) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{5d} + \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{5d} \right. \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-8A \sin\left[\frac{dx}{2}\right] + 13B \sin\left[\frac{dx}{2}\right])}{15d} + \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-13A \sin\left[\frac{dx}{2}\right] + 29B \sin\left[\frac{dx}{2}\right])}{3d} + \\
& \quad \frac{16B \sec[c] \sec[c+dx] \sin[dx]}{3d} + \frac{4(4B-13A \cos[c] + 33B \cos[c]) \sec[c] \tan\left[\frac{c}{2}\right]}{3d} + \\
& \quad \left. \frac{4(-8A+13B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} + \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right)
\end{aligned}$$

Problem 217: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{\sec[c+dx]^{7/2} (A+B \sec[c+dx])}{(a+a \sec[c+dx])^3} dx$$

Optimal (type 4, 261 leaves, 9 steps):

$$\begin{aligned} & \frac{(9A-49B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{10a^3d} + \\ & \frac{(3A-13B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{6a^3d} - \\ & \frac{(9A-49B) \sqrt{\sec[c+dx]} \sin[c+dx]}{10a^3d} + \frac{(A-B) \sec[c+dx]^{7/2} \sin[c+dx]}{5d(a+a \sec[c+dx])^3} + \\ & \frac{(3A-8B) \sec[c+dx]^{5/2} \sin[c+dx]}{15ad(a+a \sec[c+dx])^2} + \frac{(3A-13B) \sec[c+dx]^{3/2} \sin[c+dx]}{6d(a^3+a^3 \sec[c+dx])} \end{aligned}$$

Result (type 5, 904 leaves):

$$\begin{aligned}
& \left( 9 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) - \\
& \left( 49 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 2A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) - \\
& \left( 26B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c+dx]^{5/2} (A+B \sec[c+dx]) \right) \\
& \left( \frac{2(-9A+49B) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{5d} - \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{5d} - \right. \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-3A \sin\left[\frac{dx}{2}\right] + 8B \sin\left[\frac{dx}{2}\right])}{15d} - \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-3A \sin\left[\frac{dx}{2}\right] + 13B \sin\left[\frac{dx}{2}\right])}{3d} - \frac{4(-3A+13B) \tan\left[\frac{c}{2}\right]}{3d} - \\
& \quad \left. \frac{4(-3A+8B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} - \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) / \\
& \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right)
\end{aligned}$$

**Problem 218:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x]^{5 / 2} (A+B \sec [c+d x])}{(a+a \sec [c+d x])^3} d x$$

Optimal (type 4, 220 leaves, 8 steps):

$$\begin{aligned} & \frac{(A+9 B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{10 a^3 d} + \\ & \frac{(A+3 B) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{6 a^3 d} + \\ & \frac{(A-B) \sec [c+d x]^{5 / 2} \sin [c+d x]}{5 d (a+a \sec [c+d x])^3} + \\ & \frac{(A-6 B) \sec [c+d x]^{3 / 2} \sin [c+d x]}{15 a d (a+a \sec [c+d x])^2} - \frac{(A+9 B) \sqrt{\sec [c+d x]} \sin [c+d x]}{10 d (a^3+a^3 \sec [c+d x])} \end{aligned}$$

Result (type 5, 899 leaves):



$$\begin{aligned}
& \left( \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 9 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1+e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 2A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 2B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c+dx]^{5/2} (A+B \sec[c+dx]) \right. \\
& \quad \left( -\frac{2(A+9B) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{5d} + \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{5d} + \right. \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + 3B \sin\left[\frac{dx}{2}\right])}{3d} + \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (2A \sin\left[\frac{dx}{2}\right] + 3B \sin\left[\frac{dx}{2}\right])}{15d} + \frac{4(A+3B) \tan\left[\frac{c}{2}\right]}{3d} + \\
& \quad \left. \frac{4(2A+3B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} + \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) / \\
& \quad \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right)
\end{aligned}$$

Problem 219: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x]^{3 / 2} (A+B \sec [c+d x])}{(a+a \sec [c+d x])^3} d x$$

Optimal (type 4, 216 leaves, 8 steps):

$$\begin{aligned} & -\frac{(A-B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{10 a^3 d} + \\ & \frac{(A+B) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]}}{6 a^3 d} + \\ & \frac{(A-B) \sec [c+d x]^{3 / 2} \sin [c+d x]}{5 d (a+a \sec [c+d x])^3} - \\ & \frac{(A+4 B) \sqrt{\sec [c+d x]} \sin [c+d x]}{15 a d (a+a \sec [c+d x])^2} + \frac{(A+B) \sqrt{\sec [c+d x]} \sin [c+d x]}{6 d (a^3+a^3 \sec [c+d x])} \end{aligned}$$

Result (type 5, 898 leaves):

$$\begin{aligned}
& - \left( \left( \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \\
& \quad \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 2A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 2B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c+dx]^{5/2} (A+B \sec[c+dx]) \right. \\
& \quad \left( -\frac{2(-A+B) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{5d} - \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{5d} + \right. \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3d} + \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-7A \sin\left[\frac{dx}{2}\right] + 2B \sin\left[\frac{dx}{2}\right])}{15d} + \frac{4(A+B) \tan\left[\frac{c}{2}\right]}{3d} + \\
& \quad \left. \left. \frac{4(-7A+2B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} - \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) \right) / \\
& \quad \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right)
\end{aligned}$$

Problem 220: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\sec[c+dx]} (A+B \sec[c+dx])}{(a+a \sec[c+dx])^3} dx$$

Optimal (type 4, 222 leaves, 8 steps):

$$\begin{aligned} & - \frac{(9A+B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{10a^3d} + \\ & \frac{(3A+B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{6a^3d} + \\ & \frac{(A-B) \sqrt{\sec[c+dx]} \sin[c+dx]}{5d(a+a \sec[c+dx])^3} + \\ & \frac{(3A+2B) \sqrt{\sec[c+dx]} \sin[c+dx]}{15ad(a+a \sec[c+dx])^2} + \frac{(3A+B) \sqrt{\sec[c+dx]} \sin[c+dx]}{6d(a^3+a^3 \sec[c+dx])} \end{aligned}$$

Result (type 5, 899 leaves):

$$\begin{aligned}
& - \left( \left( 9 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) - \\
& \left( \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \\
& \quad \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 2A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 2B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c+dx]^{5/2} (A+B \sec[c+dx]) \right. \\
& \quad \left( \frac{2(9A+B) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{5d} + \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-9A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3d} + \right. \\
& \quad \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{5d} - \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-12A \sin\left[\frac{dx}{2}\right] + 7B \sin\left[\frac{dx}{2}\right])}{15d} + \frac{4(-9A+B) \tan\left[\frac{c}{2}\right]}{3d} - \\
& \quad \left. \frac{4(-12A+7B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} + \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right) / \\
& \quad \left( (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right)
\end{aligned}$$

**Problem 221:** Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{A + B \sec[c + d x]}{\sqrt{\sec[c + d x]} (a + a \sec[c + d x])^3} dx$$

Optimal (type 4, 228 leaves, 8 steps):

$$\begin{aligned} & \frac{(49A - 9B) \sqrt{\cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]}}{10 a^3 d} - \\ & \frac{(13A - 3B) \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]}}{6 a^3 d} - \\ & \frac{(A - B) \sqrt{\sec[c + d x]} \sin[c + d x]}{5 d (a + a \sec[c + d x])^3} - \frac{(8A - 3B) \sqrt{\sec[c + d x]} \sin[c + d x]}{15 a d (a + a \sec[c + d x])^2} - \\ & \frac{(13A - 3B) \sqrt{\sec[c + d x]} \sin[c + d x]}{6 d (a^3 + a^3 \sec[c + d x])} \end{aligned}$$

Result (type 5, 923 leaves):

$$\begin{aligned}
& \left( 49 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) - \\
& \left( 9 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) - \\
& \left( 26 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 2 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \frac{1}{(B+A \cos[c+dx]) (a+a \sec[c+dx])^3} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c+dx]^{5/2} \\
& (A+B \sec[c+dx]) \left( -\frac{2(39A-9B+10A \cos[2c]) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]}{5d} - \right. \\
& \quad \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 \left( -A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right] \right)}{5d} - \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] \left( -23A \sin\left[\frac{dx}{2}\right] + 9B \sin\left[\frac{dx}{2}\right] \right)}{3d} + \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \left( -17A \sin\left[\frac{dx}{2}\right] + 12B \sin\left[\frac{dx}{2}\right] \right)}{15d} + \\
& \quad \frac{16A \cos[c] \sin[dx]}{d} - \frac{4(-23A+9B) \tan\left[\frac{c}{2}\right]}{3d} + \\
& \quad \left. \frac{4(-17A+12B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} - \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right)
\end{aligned}$$

Problem 222: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \sec[c + d x]}{\sec[c + d x]^{3/2} (a + a \sec[c + d x])^3} dx$$

Optimal (type 4, 261 leaves, 9 steps):

$$\begin{aligned} & -\frac{1}{10 a^3 d} 7 (17 A - 7 B) \sqrt{\cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]} + \\ & \frac{(33 A - 13 B) \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]}}{6 a^3 d} + \\ & \frac{(33 A - 13 B) \sin[c + d x]}{6 a^3 d \sqrt{\sec[c + d x]}} - \frac{(A - B) \sin[c + d x]}{5 d \sqrt{\sec[c + d x]} (a + a \sec[c + d x])^3} - \\ & \frac{(2 A - B) \sin[c + d x]}{3 a d \sqrt{\sec[c + d x]} (a + a \sec[c + d x])^2} - \frac{7 (17 A - 7 B) \sin[c + d x]}{30 d \sqrt{\sec[c + d x]} (a^3 + a^3 \sec[c + d x])} \end{aligned}$$

Result (type 5, 968 leaves):



$$\begin{aligned}
& - \left( \left( 119 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 49 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \right. \\
& \quad \left. \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \right) / \\
& \quad \left( 5d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \left( 22 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) - \\
& \left( 26 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c+dx]} \csc\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sec\left[\frac{c}{2}\right] \sec[c+dx]^{5/2} \right. \\
& \quad \left. (A+B \sec[c+dx]) \sin[c] \right) / \left( 3d (B+A \cos[c+dx]) (a+a \sec[c+dx])^3 \right) + \\
& \frac{1}{(B+A \cos[c+dx]) (a+a \sec[c+dx])^3} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sec[c+dx]^{5/2} (A+B \sec[c+dx]) \\
& \left( -\frac{1}{5d} 2 (-89A + 39B - 30A \cos[2c] + 10B \cos[2c]) \cos[dx] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] + \right. \\
& \quad \frac{8A \cos[2dx] \sin[2c]}{3d} + \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^5 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{5d} - \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-22A \sin\left[\frac{dx}{2}\right] + 17B \sin\left[\frac{dx}{2}\right])}{15d} + \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-43A \sin\left[\frac{dx}{2}\right] + 23B \sin\left[\frac{dx}{2}\right])}{3d} + \\
& \quad \frac{16(-3A+B) \cos[c] \sin[dx]}{d} + \frac{8A \cos[2c] \sin[2dx]}{3d} + \frac{4(-43A+23B) \tan\left[\frac{c}{2}\right]}{3d} - \\
& \quad \left. \frac{4(-22A+17B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15d} + \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5d} \right)
\end{aligned}$$

**Problem 223: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + d x]}{\sec[c + d x]^{5/2} (a + a \sec[c + d x])^3} dx$$

Optimal (type 4, 294 leaves, 10 steps):

$$\begin{aligned} & \frac{7 (33 A - 17 B) \sqrt{\cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]}}{10 a^3 d} - \\ & \frac{(21 A - 11 B) \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]}}{2 a^3 d} + \\ & \frac{7 (33 A - 17 B) \sin[c + d x]}{30 a^3 d \sec[c + d x]^{3/2}} - \frac{(21 A - 11 B) \sin[c + d x]}{2 a^3 d \sqrt{\sec[c + d x]}} - \frac{(A - B) \sin[c + d x]}{5 d \sec[c + d x]^{3/2} (a + a \sec[c + d x])^3} - \\ & \frac{(12 A - 7 B) \sin[c + d x]}{15 a d \sec[c + d x]^{3/2} (a + a \sec[c + d x])^2} - \frac{3 (21 A - 11 B) \sin[c + d x]}{10 d \sec[c + d x]^{3/2} (a^3 + a^3 \sec[c + d x])} \end{aligned}$$

Result (type 5, 1012 leaves):

$$\begin{aligned} & \left( 231 \sqrt{2} A e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ & \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\ & \quad \left. \sec\left[\frac{c}{2}\right] \sec[c + d x]^2 (A + B \sec[c + d x]) \right) / \left( 5 d (B + A \cos[c + d x]) (a + a \sec[c + d x])^3 \right) - \\ & \left( 119 \sqrt{2} B e^{-i(2c+dx)} \sqrt{\frac{e^{i(c+dx)}}{1+e^{2i(c+dx)}}} \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \right. \\ & \quad \left( 1 + e^{2i(c+dx)} + (-1 + e^{2ic}) \sqrt{1 + e^{2i(c+dx)}} \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c+dx)}\right] \right) \\ & \quad \left. \sec\left[\frac{c}{2}\right] \sec[c + d x]^2 (A + B \sec[c + d x]) \right) / \left( 5 d (B + A \cos[c + d x]) (a + a \sec[c + d x])^3 \right) - \\ & \left( 42 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c + d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sec\left[\frac{c}{2}\right] \sec[c + d x]^{5/2} \right. \\ & \quad \left. (A + B \sec[c + d x]) \sin[c] \right) / \left( d (B + A \cos[c + d x]) (a + a \sec[c + d x])^3 \right) + \\ & \left( 22 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \sqrt{\cos[c + d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sec\left[\frac{c}{2}\right] \sec[c + d x]^{5/2} \right. \\ & \quad \left. (A + B \sec[c + d x]) \sin[c] \right) / \left( d (B + A \cos[c + d x]) (a + a \sec[c + d x])^3 \right) + \end{aligned}$$

$$\frac{1}{(B + A \cos[c + d x]) (a + a \sec[c + d x])^3} \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \sec[c + d x]^{5/2} (A + B \sec[c + d x])$$

$$\left( \frac{1}{5 d} (-329 A + 178 B - 133 A \cos[2 c] + 60 B \cos[2 c]) \cos[d x] \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] + \right.$$

$$\frac{8 (-3 A + B) \cos[2 d x] \sin[2 c]}{3 d} + \frac{4 A \cos[3 d x] \sin[3 c]}{5 d} -$$

$$\frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^5 (-A \sin\left[\frac{d x}{2}\right] + B \sin\left[\frac{d x}{2}\right])}{5 d} +$$

$$\frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^3 (-27 A \sin\left[\frac{d x}{2}\right] + 22 B \sin\left[\frac{d x}{2}\right])}{15 d} -$$

$$\frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right] (-69 A \sin\left[\frac{d x}{2}\right] + 43 B \sin\left[\frac{d x}{2}\right])}{3 d} - \frac{4 (-133 A + 60 B) \cos[c] \sin[d x]}{5 d} +$$

$$\frac{8 (-3 A + B) \cos[2 c] \sin[2 d x]}{3 d} + \frac{4 A \cos[3 c] \sin[3 d x]}{5 d} - \frac{4 (-69 A + 43 B) \tan\left[\frac{c}{2}\right]}{3 d} +$$

$$\left. \frac{4 (-27 A + 22 B) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15 d} - \frac{2 (-A + B) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5 d} \right)$$

**Problem 224: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec[c + d x]^{5/2} \sqrt{a + a \sec[c + d x]} (A + B \sec[c + d x]) dx$$

Optimal (type 3, 176 leaves, 5 steps):

$$\frac{\sqrt{a} (6 A + 5 B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c + d x]}{\sqrt{a + a \sec[c + d x]}}\right]}{8 d} + \frac{a (6 A + 5 B) \sec[c + d x]^{3/2} \sin[c + d x]}{8 d \sqrt{a + a \sec[c + d x]}} +$$

$$\frac{a (6 A + 5 B) \sec[c + d x]^{5/2} \sin[c + d x]}{12 d \sqrt{a + a \sec[c + d x]}} + \frac{a B \sec[c + d x]^{7/2} \sin[c + d x]}{3 d \sqrt{a + a \sec[c + d x]}}$$

Result (type 3, 1184 leaves):

$$-\left( \left( \left( \frac{1}{64} + \frac{i}{64} \right) ((-1 + i) + \sqrt{2}) \left( (18 + 6 i) A + 6 \sqrt{2} A + (15 + 5 i) B + 5 \sqrt{2} B \right) \right. \right.$$

$$\operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c + d x)\right] - \sin\left[\frac{1}{4}(c + d x)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c + d x)\right]}{-\cos\left[\frac{1}{4}(c + d x)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c + d x)\right] - \sin\left[\frac{1}{4}(c + d x)\right]} \right]$$

$$\left. \sec\left[\frac{1}{2}(c + d x)\right] \sqrt{a (1 + \sec[c + d x])} \right) / \left( \sqrt{2} (i + \sqrt{2}) d \sqrt{\sec[c + d x]} \right) -$$

$$\begin{aligned}
& \left( \left( \frac{1}{64} - \frac{i}{64} \right) \left( (1+i) + \sqrt{2} \right) \left( (-18+6i) A + 6\sqrt{2} A - (15-5i) B + 5\sqrt{2} B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+dx) \right]}{\cos \left[ \frac{1}{4} (c+dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right]} \right] \\
& \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right] \sqrt{a(1+\sec[c+dx])} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sqrt{\sec[c+dx]} \right) + \\
& \left( (12A+6i\sqrt{2}A+10B+5i\sqrt{2}B) \log[\sqrt{2}+2\sin[\frac{1}{2}(c+dx)]] \sec[\frac{1}{2}(c+dx)] \right. \\
& \quad \left. \sqrt{a(1+\sec[c+dx])} \right) / \left( 32(i+\sqrt{2}) d \sqrt{\sec[c+dx]} \right) - \\
& \left( \left( \frac{1}{128} - \frac{i}{128} \right) \left( (-1+i) + \sqrt{2} \right) \left( (18+6i) A + 6\sqrt{2} A + (15+5i) B + 5\sqrt{2} B \right) \right. \\
& \quad \log[2-\sqrt{2}\cos[\frac{1}{2}(c+dx)]-\sqrt{2}\sin[\frac{1}{2}(c+dx)]] \sec[\frac{1}{2}(c+dx)] \\
& \quad \left. \sqrt{a(1+\sec[c+dx])} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sqrt{\sec[c+dx]} \right) + \\
& \left( \left( \frac{1}{128} + \frac{i}{128} \right) \left( (1+i) + \sqrt{2} \right) \left( (-18+6i) A + 6\sqrt{2} A - (15-5i) B + 5\sqrt{2} B \right) \right. \\
& \quad \log[2+\sqrt{2}\cos[\frac{1}{2}(c+dx)]-\sqrt{2}\sin[\frac{1}{2}(c+dx)]] \sec[\frac{1}{2}(c+dx)] \sqrt{a(1+\sec[c+dx])} \left. \right) / \\
& \left( \sqrt{2} (i+\sqrt{2}) d \sqrt{\sec[c+dx]} \right) + \frac{B \sec[\frac{1}{2}(c+dx)] \sqrt{a(1+\sec[c+dx])}}{12 d \sqrt{\sec[c+dx]} \left( \cos[\frac{1}{2}(c+dx)] - \sin[\frac{1}{2}(c+dx)] \right)^3} + \\
& \frac{(6A+5B) \sec[\frac{1}{2}(c+dx)] \sqrt{a(1+\sec[c+dx])}}{16 d \sqrt{\sec[c+dx]} \left( \cos[\frac{1}{2}(c+dx)] - \sin[\frac{1}{2}(c+dx)] \right)} - \\
& \frac{B \sec[\frac{1}{2}(c+dx)] \sqrt{a(1+\sec[c+dx])}}{12 d \sqrt{\sec[c+dx]} \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^3} + \\
& \frac{(-6A-5B) \sec[\frac{1}{2}(c+dx)] \sqrt{a(1+\sec[c+dx])}}{16 d \sqrt{\sec[c+dx]} \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)} + \\
& \left( \sec[\frac{1}{2}(c+dx)] \sqrt{a(1+\sec[c+dx])} \left( 2A \sin[\frac{1}{2}(c+dx)] + B \sin[\frac{1}{2}(c+dx)] \right) \right) / \\
& \left( 8 d \sqrt{\sec[c+dx]} \left( \cos[\frac{1}{2}(c+dx)] - \sin[\frac{1}{2}(c+dx)] \right)^2 \right) + \\
& \left( \sec[\frac{1}{2}(c+dx)] \sqrt{a(1+\sec[c+dx])} \left( 2A \sin[\frac{1}{2}(c+dx)] + B \sin[\frac{1}{2}(c+dx)] \right) \right) / \\
& \left( 8 d \sqrt{\sec[c+dx]} \left( \cos[\frac{1}{2}(c+dx)] + \sin[\frac{1}{2}(c+dx)] \right)^2 \right)
\end{aligned}$$

Problem 225: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 131 leaves, 4 steps):

$$\frac{\sqrt{a} (4A+3B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{4d} + \frac{a (4A+3B) \sec[c+dx]^{3/2} \sin[c+dx]}{4d \sqrt{a+a \sec[c+dx]}} + \frac{aB \sec[c+dx]^{5/2} \sin[c+dx]}{2d \sqrt{a+a \sec[c+dx]}}$$

Result (type 3, 1002 leaves):

$$\begin{aligned}
& - \left( \left( \frac{1}{32} + \frac{i}{32} \right) \left( (-1+i) + \sqrt{2} \right) \left( (12+4i) A + 4\sqrt{2} A + (9+3i) B + 3\sqrt{2} B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+dx) \right]}{-\cos \left[ \frac{1}{4} (c+dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right]} \right] \\
& \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right] \sqrt{a(1+\sec[c+dx])} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sqrt{\sec[c+dx]} \right) - \\
& \left( \left( \frac{1}{32} - \frac{i}{32} \right) \left( (1+i) + \sqrt{2} \right) \left( (-12+4i) A + 4\sqrt{2} A - (9-3i) B + 3\sqrt{2} B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+dx) \right]}{\cos \left[ \frac{1}{4} (c+dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right]} \right] \\
& \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right] \sqrt{a(1+\sec[c+dx])} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sqrt{\sec[c+dx]} \right) + \\
& \left( (8A+4i\sqrt{2}A+6B+3i\sqrt{2}B) \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+dx) \right] \right] \sec \left[ \frac{1}{2} (c+dx) \right] \right. \\
& \quad \left. \sqrt{a(1+\sec[c+dx])} \right) / \left( 16 (i+\sqrt{2}) d \sqrt{\sec[c+dx]} \right) - \\
& \left( \left( \frac{1}{64} - \frac{i}{64} \right) \left( (-1+i) + \sqrt{2} \right) \left( (12+4i) A + 4\sqrt{2} A + (9+3i) B + 3\sqrt{2} B \right) \right. \\
& \quad \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \sec \left[ \frac{1}{2} (c+dx) \right] \\
& \quad \left. \sqrt{a(1+\sec[c+dx])} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sqrt{\sec[c+dx]} \right) + \\
& \left( \left( \frac{1}{64} + \frac{i}{64} \right) \left( (1+i) + \sqrt{2} \right) \left( (-12+4i) A + 4\sqrt{2} A - (9-3i) B + 3\sqrt{2} B \right) \right. \\
& \quad \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \sec \left[ \frac{1}{2} (c+dx) \right] \sqrt{a(1+\sec[c+dx])} \right) / \\
& \left( \sqrt{2} (i+\sqrt{2}) d \sqrt{\sec[c+dx]} \right) + \frac{(4A+3B) \sec \left[ \frac{1}{2} (c+dx) \right] \sqrt{a(1+\sec[c+dx])}}{8d \sqrt{\sec[c+dx]} \left( \cos \left[ \frac{1}{2} (c+dx) \right] - \sin \left[ \frac{1}{2} (c+dx) \right] \right)} + \\
& \frac{(-4A-3B) \sec \left[ \frac{1}{2} (c+dx) \right] \sqrt{a(1+\sec[c+dx])}}{8d \sqrt{\sec[c+dx]} \left( \cos \left[ \frac{1}{2} (c+dx) \right] + \sin \left[ \frac{1}{2} (c+dx) \right] \right)} + \\
& \frac{B \sqrt{a(1+\sec[c+dx])} \tan \left[ \frac{1}{2} (c+dx) \right]}{4d \sqrt{\sec[c+dx]} \left( \cos \left[ \frac{1}{2} (c+dx) \right] - \sin \left[ \frac{1}{2} (c+dx) \right] \right)^2} + \\
& \frac{B \sqrt{a(1+\sec[c+dx])} \tan \left[ \frac{1}{2} (c+dx) \right]}{4d \sqrt{\sec[c+dx]} \left( \cos \left[ \frac{1}{2} (c+dx) \right] + \sin \left[ \frac{1}{2} (c+dx) \right] \right)^2}
\end{aligned}$$

Problem 226: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{\sec[c+dx]} \sqrt{a+a \sec[c+dx]} (A+B \sec[c+dx])}{dx}$$

Optimal (type 3, 78 leaves, 3 steps):

$$\frac{\sqrt{a} (2A+B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{d} + \frac{a B \sec[c+dx]^{3/2} \sin[c+dx]}{d \sqrt{a+a \sec[c+dx]}}$$

Result (type 3, 522 leaves):

$$\begin{aligned} & \frac{1}{d \sqrt{\sec[c+dx]}} \left( \frac{1}{32} + \frac{i}{32} \right) \sec\left[\frac{1}{2}(c+dx)\right] \\ & \sqrt{a(1+\sec[c+dx])} \left( \frac{1}{i+\sqrt{2}} 2i\sqrt{2} \left( (-3+i) + \sqrt{2} \right) \left( (1+i) + \sqrt{2} \right) (2A+B) \right. \\ & \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] - \frac{1}{i+\sqrt{2}} 2\sqrt{2} \left( (-1+i) + \sqrt{2} \right) \\ & \quad \left. \left( (3+i) + \sqrt{2} \right) (2A+B) \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] + \right. \\ & \quad \left. \frac{(4+4i) (-2i+\sqrt{2}) (2A+B) \operatorname{Log}\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c+dx)\right]\right]}{i+\sqrt{2}} + \right. \\ & \quad \left. \frac{1}{i+\sqrt{2}} i\sqrt{2} \left( (-1+i) + \sqrt{2} \right) \left( (3+i) + \sqrt{2} \right) (2A+B) \right. \\ & \quad \left. \operatorname{Log}\left[ 2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right] \right] + \frac{1}{i+\sqrt{2}} \sqrt{2} \left( (-3+i) + \sqrt{2} \right) \right. \\ & \quad \left. \left( (1+i) + \sqrt{2} \right) (2A+B) \operatorname{Log}\left[ 2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right] \right] + \right. \\ & \quad \left. \frac{(8-8i) B}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} - \frac{(8-8i) B}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} \right) \end{aligned}$$

Problem 227: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{a+a \sec[c+dx]} (A+B \sec[c+dx])}{\sqrt{\sec[c+dx]}} dx$$

Optimal (type 3, 76 leaves, 3 steps):

$$\frac{2 \sqrt{a} B \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{d} + \frac{2 a A \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{d \sqrt{a+a \operatorname{Sec}[c+dx]}}$$

Result (type 3, 321 leaves):

$$\begin{aligned} & \frac{1}{4 d \sqrt{\operatorname{Sec}[c+dx]}} \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\operatorname{Sec}[c+dx])} \\ & \left( -2 i \sqrt{2} B \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right] - \right. \\ & \quad 2 i \sqrt{2} B \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right] + 2 \sqrt{2} B \\ & \quad \operatorname{Log}\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c+dx)\right]\right] - \sqrt{2} B \operatorname{Log}\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] - \\ & \quad \left. \sqrt{2} B \operatorname{Log}\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] + 8 A \sin\left[\frac{1}{2}(c+dx)\right] \right) \end{aligned}$$

**Problem 231: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^{5/2} (a+a \operatorname{Sec}[c+dx])^{3/2} (A+B \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 227 leaves, 6 steps):

$$\begin{aligned} & \frac{a^{3/2} (88 A + 75 B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{64 d} + \\ & \frac{a^2 (88 A + 75 B) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{64 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a^2 (88 A + 75 B) \operatorname{Sec}[c+dx]^{5/2} \operatorname{Sin}[c+dx]}{96 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\ & \frac{a^2 (8 A + 9 B) \operatorname{Sec}[c+dx]^{7/2} \operatorname{Sin}[c+dx]}{24 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a B \operatorname{Sec}[c+dx]^{7/2} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4 d} \end{aligned}$$

Result (type 3, 1376 leaves):

$$\begin{aligned} & - \left( \left( \frac{1}{1024} + \frac{i}{1024} \right) \left( (-1+i) + \sqrt{2} \right) \left( (264+88i) A + 88 \sqrt{2} A + (225+75i) B + 75 \sqrt{2} B \right) \right. \\ & \quad \operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right] \\ & \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \operatorname{Sec}[c+dx]^{3/2} \right) - \end{aligned}$$



$$\begin{aligned}
& \left( \left( \frac{1}{1024} - \frac{i}{1024} \right) \left( (1+i) + \sqrt{2} \right) \left( (-264+88i) A + 88\sqrt{2} A - (225-75i) B + 75\sqrt{2} B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sec[c+dx]^{3/2} \right) + \\
& \left( (176A + 88i\sqrt{2}A + 150B + 75i\sqrt{2}B) \log\left[\sqrt{2} + 2\sin\left[\frac{1}{2}(c+dx)\right]\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2} \right) / \left( 512 (i+\sqrt{2}) d \sec[c+dx]^{3/2} \right) - \\
& \left( \left( \frac{1}{2048} - \frac{i}{2048} \right) \left( (-1+i) + \sqrt{2} \right) \left( (264+88i) A + 88\sqrt{2} A + (225+75i) B + 75\sqrt{2} B \right) \right. \\
& \quad \log\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \sec\left[\frac{1}{2}(c+dx)\right]^3 \\
& \quad \left. (a(1+\sec[c+dx]))^{3/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sec[c+dx]^{3/2} \right) + \\
& \left( \left( \frac{1}{2048} + \frac{i}{2048} \right) \left( (1+i) + \sqrt{2} \right) \left( (-264+88i) A + 88\sqrt{2} A - (225-75i) B + 75\sqrt{2} B \right) \right. \\
& \quad \log\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \sec\left[\frac{1}{2}(c+dx)\right]^3 \\
& \quad \left. (a(1+\sec[c+dx]))^{3/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sec[c+dx]^{3/2} \right) + \\
& \frac{(8A + 15B) \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2}}{192 d \sec[c+dx]^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \\
& \frac{(88A + 75B) \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2}}{256 d \sec[c+dx]^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)} + \\
& \frac{(-8A - 15B) \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2}}{192 d \sec[c+dx]^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \\
& \frac{(-88A - 75B) \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2}}{256 d \sec[c+dx]^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} + \\
& \left( \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2} \left( 24A \sin\left[\frac{1}{2}(c+dx)\right] + 19B \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
& \left( 128 d \sec[c+dx]^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) + \\
& \left( \sec\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\sec[c+dx]))^{3/2} \left( 24A \sin\left[\frac{1}{2}(c+dx)\right] + 19B \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
& \left( 128 d \sec[c+dx]^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) +
\end{aligned}$$

$$\frac{B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a(1+\operatorname{Sec}[c+dx]))^{3/2} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{32 d \operatorname{Sec}[c+dx]^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4} +$$

$$\frac{B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a(1+\operatorname{Sec}[c+dx]))^{3/2} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{32 d \operatorname{Sec}[c+dx]^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}$$

**Problem 232: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx]^{3/2} (a+a \operatorname{Sec}[c+dx])^{3/2} (A+B \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 180 leaves, 5 steps):

$$\frac{a^{3/2} (14A+11B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{8d} + \frac{a^2 (14A+11B) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{8d \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a^2 (6A+7B) \operatorname{Sec}[c+dx]^{5/2} \operatorname{Sin}[c+dx]}{12d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{aB \operatorname{Sec}[c+dx]^{5/2} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{3d}$$

Result (type 3, 1208 leaves):

$$-\left(\left(\left(\frac{1}{128} + \frac{i}{128}\right) \left((-1+i) + \sqrt{2}\right) \left((42+14i)A + 14\sqrt{2}A + (33+11i)B + 11\sqrt{2}B\right)\right.\right.$$

$$\left.\operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right]\right.$$

$$\left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2}\right) / \left(\sqrt{2}(i+\sqrt{2}) d \operatorname{Sec}[c+dx]^{3/2}\right) -$$

$$\left(\left(\frac{1}{128} - \frac{i}{128}\right) \left((1+i) + \sqrt{2}\right) \left((-42+14i)A + 14\sqrt{2}A - (33-11i)B + 11\sqrt{2}B\right)\right.$$

$$\left.\operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right]\right.$$

$$\left.\operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\operatorname{Sec}[c+dx]))^{3/2}\right) / \left(\sqrt{2}(i+\sqrt{2}) d \operatorname{Sec}[c+dx]^{3/2}\right) +$$

$$\left(\left(28A + 14i\sqrt{2}A + 22B + 11i\sqrt{2}B\right) \operatorname{Log}\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^3\right.$$

$$\left.\left(a(1+\operatorname{Sec}[c+dx])\right)^{3/2}\right) / \left(64(i+\sqrt{2}) d \operatorname{Sec}[c+dx]^{3/2}\right) -$$

$$\left(\left(\frac{1}{256} - \frac{i}{256}\right) \left((-1+i) + \sqrt{2}\right) \left((42+14i)A + 14\sqrt{2}A + (33+11i)B + 11\sqrt{2}B\right)\right.$$

$$\begin{aligned}
& \text{Log}\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \sec\left[\frac{1}{2}(c+dx)\right]^3 \\
& \left(a(1+\sec[c+dx])\right)^{3/2} \Big/ \left(\sqrt{2}(\sqrt{2}+1) d \sec[c+dx]^{3/2}\right) + \\
& \left(\left(\frac{1}{256} + \frac{i}{256}\right) \left((1+i) + \sqrt{2}\right) \left((-42+14i)A + 14\sqrt{2}A - (33-11i)B + 11\sqrt{2}B\right)\right. \\
& \left.\text{Log}\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \sec\left[\frac{1}{2}(c+dx)\right]^3\right. \\
& \left.\left(a(1+\sec[c+dx])\right)^{3/2} \Big/ \left(\sqrt{2}(\sqrt{2}+1) d \sec[c+dx]^{3/2}\right) +\right. \\
& \left.\frac{B \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2}}{24 d \sec[c+dx]^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} +\right. \\
& \left.\frac{(14A+11B) \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2}}{32 d \sec[c+dx]^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)} -\right. \\
& \left.\frac{B \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2}}{24 d \sec[c+dx]^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} +\right. \\
& \left.\frac{(-14A-11B) \sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2}}{32 d \sec[c+dx]^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)} +\right. \\
& \left.\left(\sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2} \left(2A \sin\left[\frac{1}{2}(c+dx)\right] + 3B \sin\left[\frac{1}{2}(c+dx)\right]\right)\right) \Big/ \right. \\
& \left.\left(16 d \sec[c+dx]^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2\right) +\right. \\
& \left.\left(\sec\left[\frac{1}{2}(c+dx)\right]^3 \left(a(1+\sec[c+dx])\right)^{3/2} \left(2A \sin\left[\frac{1}{2}(c+dx)\right] + 3B \sin\left[\frac{1}{2}(c+dx)\right]\right)\right) \Big/ \right. \\
& \left.\left(16 d \sec[c+dx]^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2\right)\right)
\end{aligned}$$

**Problem 233: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\sec[c+dx]} (a+a \sec[c+dx])^{3/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 133 leaves, 4 steps):

$$\begin{aligned}
& \frac{a^{3/2} (12A+7B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{4d} + \\
& \frac{a^2 (4A+5B) \sec[c+dx]^{3/2} \sin[c+dx]}{4d \sqrt{a+a \sec[c+dx]}} + \frac{aB \sec[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{2d}
\end{aligned}$$

Result (type 3, 1040 leaves):

$$\begin{aligned}
& - \left( \left( \frac{1}{64} + \frac{i}{64} \right) \left( (-1+i) + \sqrt{2} \right) \left( (36+12i) A + 12\sqrt{2} A + (21+7i) B + 7\sqrt{2} B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^3 (a(1+\text{Sec}[c+dx]))^{3/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \text{Sec}[c+dx]^{3/2} \right) \Bigg) - \\
& \left( \left( \frac{1}{64} - \frac{i}{64} \right) \left( (1+i) + \sqrt{2} \right) \left( (-36+12i) A + 12\sqrt{2} A - (21-7i) B + 7\sqrt{2} B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \text{Sec} \left[ \frac{1}{2}(c+dx) \right]^3 (a(1+\text{Sec}[c+dx]))^{3/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \text{Sec}[c+dx]^{3/2} \right) + \\
& \left( (24A + 12i\sqrt{2}A + 14B + 7i\sqrt{2}B) \log\left[\sqrt{2} + 2\sin\left[\frac{1}{2}(c+dx)\right]\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^3 \right. \\
& \quad \left. (a(1+\text{Sec}[c+dx]))^{3/2} \right) / \left( 32(i+\sqrt{2}) d \text{Sec}[c+dx]^{3/2} \right) - \\
& \left( \left( \frac{1}{128} - \frac{i}{128} \right) \left( (-1+i) + \sqrt{2} \right) \left( (36+12i) A + 12\sqrt{2} A + (21+7i) B + 7\sqrt{2} B \right) \right. \\
& \quad \log\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^3 \\
& \quad \left. (a(1+\text{Sec}[c+dx]))^{3/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \text{Sec}[c+dx]^{3/2} \right) + \\
& \left( \left( \frac{1}{128} + \frac{i}{128} \right) \left( (1+i) + \sqrt{2} \right) \left( (-36+12i) A + 12\sqrt{2} A - (21-7i) B + 7\sqrt{2} B \right) \right. \\
& \quad \log\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \text{Sec}\left[\frac{1}{2}(c+dx)\right]^3 \\
& \quad \left. (a(1+\text{Sec}[c+dx]))^{3/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \text{Sec}[c+dx]^{3/2} \right) + \\
& \frac{(4A+7B) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\text{Sec}[c+dx]))^{3/2}}{16 d \text{Sec}[c+dx]^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)} + \\
& \frac{(-4A-7B) \text{Sec}\left[\frac{1}{2}(c+dx)\right]^3 (a(1+\text{Sec}[c+dx]))^{3/2}}{16 d \text{Sec}[c+dx]^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} + \\
& \frac{B \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 (a(1+\text{Sec}[c+dx]))^{3/2} \tan\left[\frac{1}{2}(c+dx)\right]}{8 d \text{Sec}[c+dx]^{3/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^2} +
\end{aligned}$$

$$\frac{B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \left(a \left(1 + \operatorname{Sec}[c+dx]\right)\right)^{3/2} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{8 d \operatorname{Sec}[c+dx]^{3/2} \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2}$$

**Problem 234: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\left(a + a \operatorname{Sec}[c+dx]\right)^{3/2} \left(A + B \operatorname{Sec}[c+dx]\right)}{\sqrt{\operatorname{Sec}[c+dx]}} dx$$

Optimal (type 3, 124 leaves, 4 steps):

$$\frac{a^{3/2} (2A + 3B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{d} + \frac{a^2 (2A - B) \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{a B \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{d}$$

Result (type 3, 603 leaves):

$$\begin{aligned}
& \frac{1}{d \operatorname{Sec}[c+dx]^{3/2}} \left( \frac{1}{64} + \frac{i}{64} \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left( a \left( 1 + \operatorname{Sec}[c+dx] \right) \right)^{3/2} \left( \frac{1}{i+\sqrt{2}} 2i\sqrt{2} \left( (-3+i) + \sqrt{2} \right) \left( (1+i) + \sqrt{2} \right) (2A+3B) \right. \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] - \\
& \quad \frac{1}{i+\sqrt{2}} 2\sqrt{2} \left( (-1+i) + \sqrt{2} \right) \left( (3+i) + \sqrt{2} \right) (2A+3B) \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{i+\sqrt{2}} \\
& \quad (4+4i) \left( -2i + \sqrt{2} \right) (2A+3B) \operatorname{Log}\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] + \\
& \quad \frac{1}{i+\sqrt{2}} i\sqrt{2} \left( (-1+i) + \sqrt{2} \right) \left( (3+i) + \sqrt{2} \right) (2A+3B) \\
& \quad \operatorname{Log}\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] + \\
& \quad \frac{1}{i+\sqrt{2}} \sqrt{2} \left( (-3+i) + \sqrt{2} \right) \left( (1+i) + \sqrt{2} \right) (2A+3B) \\
& \quad \operatorname{Log}\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] - \\
& \quad \left. \frac{(8-8i) B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{-1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} + (32-32i) A \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right] - \frac{(8-8i) B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]} \right)
\end{aligned}$$

**Problem 235: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c+dx])^{3/2} (A + B \operatorname{Sec}[c+dx])}{\operatorname{Sec}[c+dx]^{3/2}} dx$$

Optimal (type 3, 125 leaves, 4 steps):

$$\begin{aligned}
& \frac{2 a^{3/2} B \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{d} + \\
& \frac{2 a^2 (4 A + 3 B) \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{3 d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \frac{2 a A \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{3 d \sqrt{\operatorname{Sec}[c+dx]}}
\end{aligned}$$

Result (type 3, 348 leaves):

$$\frac{1}{12 d \sqrt{\sec [c+d x]}} a \sec \left[ \frac{1}{2} (c+d x) \right] \sqrt{a (1+\sec [c+d x])} \left( -6 i \sqrt{2} B \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (-1+\sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(1+\sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] - 6 i \sqrt{2} B \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (1+\sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(-1+\sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] + 6 \sqrt{2} B \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right] \right] - 3 \sqrt{2} B \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] - 3 \sqrt{2} B \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] + 36 A \sin \left[ \frac{1}{2} (c+d x) \right] + 24 B \sin \left[ \frac{1}{2} (c+d x) \right] + 4 A \sin \left[ \frac{3}{2} (c+d x) \right] \right)$$

**Problem 239: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec [c+d x]^{5/2} (a+a \sec [c+d x])^{5/2} (A+B \sec [c+d x]) d x$$

Optimal (type 3, 274 leaves, 7 steps):

$$\frac{a^{5/2} (326 A + 283 B) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}} \right]}{128 d} + \frac{a^3 (326 A + 283 B) \sec [c+d x]^{3/2} \sin [c+d x]}{128 d \sqrt{a+a \sec [c+d x]}} + \frac{a^3 (326 A + 283 B) \sec [c+d x]^{5/2} \sin [c+d x]}{192 d \sqrt{a+a \sec [c+d x]}} + \frac{a^3 (170 A + 157 B) \sec [c+d x]^{7/2} \sin [c+d x]}{240 d \sqrt{a+a \sec [c+d x]}} + \frac{a^2 (10 A + 13 B) \sec [c+d x]^{7/2} \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{40 d} + \frac{a B \sec [c+d x]^{7/2} (a+a \sec [c+d x])^{3/2} \sin [c+d x]}{5 d}$$

Result (type 3, 1544 leaves):

$$- \left( \left( \left( \frac{1}{4096} + \frac{i}{4096} \right) \left( (-1+i) + \sqrt{2} \right) \left( (978+326 i) A + 326 \sqrt{2} A + (849+283 i) B + 283 \sqrt{2} B \right) \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+d x) \right]}{-\cos \left[ \frac{1}{4} (c+d x) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] \sec \left[ \frac{1}{2} (c+d x) \right]^5 (a (1+\sec [c+d x]))^{5/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sec [c+d x]^{5/2} \right) \right) -$$

$$\begin{aligned}
& \left( \left( \frac{1}{4096} - \frac{i}{4096} \right) \left( (1+i) + \sqrt{2} \right) \left( (-978+326i)A + 326\sqrt{2}A - (849-283i)B + 283\sqrt{2}B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2} \right) / \left( \sqrt{2}(i+\sqrt{2}) d \sec[c+dx]^{5/2} \right) + \\
& \left( (652A + 326i\sqrt{2}A + 566B + 283i\sqrt{2}B) \log\left[\sqrt{2} + 2\sin\left[\frac{1}{2}(c+dx)\right]\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2} \right) / \left( 2048(i+\sqrt{2}) d \sec[c+dx]^{5/2} \right) - \\
& \left( \left( \frac{1}{8192} - \frac{i}{8192} \right) \left( (-1+i) + \sqrt{2} \right) \left( (978+326i)A + 326\sqrt{2}A + (849+283i)B + 283\sqrt{2}B \right) \right. \\
& \quad \log\left[2 - \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] \sec\left[\frac{1}{2}(c+dx)\right]^5 \\
& \quad \left. (a(1+\sec[c+dx]))^{5/2} \right) / \left( \sqrt{2}(i+\sqrt{2}) d \sec[c+dx]^{5/2} \right) + \\
& \left( \left( \frac{1}{8192} + \frac{i}{8192} \right) \left( (1+i) + \sqrt{2} \right) \left( (-978+326i)A + 326\sqrt{2}A - (849-283i)B + 283\sqrt{2}B \right) \right. \\
& \quad \log\left[2 + \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] \sec\left[\frac{1}{2}(c+dx)\right]^5 \\
& \quad \left. (a(1+\sec[c+dx]))^{5/2} \right) / \left( \sqrt{2}(i+\sqrt{2}) d \sec[c+dx]^{5/2} \right) + \\
& \quad \frac{B \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{160 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^5} + \\
& \quad \frac{(46A + 59B) \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{768 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \\
& \quad \frac{(326A + 283B) \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{1024 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)} - \\
& \quad \frac{B \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{160 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5} + \\
& \quad \frac{(-46A - 59B) \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{768 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \\
& \quad \frac{(-326A - 283B) \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{1024 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} +
\end{aligned}$$



$$\begin{aligned}
& \left( \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \left(2A \sin\left[\frac{1}{2}(c+dx)\right] + 5B \sin\left[\frac{1}{2}(c+dx)\right]\right) \right) / \\
& \left( 128d \sec[c+dx]^{5/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4 \right) + \\
& \left( \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \left(2A \sin\left[\frac{1}{2}(c+dx)\right] + 5B \sin\left[\frac{1}{2}(c+dx)\right]\right) \right) / \\
& \left( 128d \sec[c+dx]^{5/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4 \right) + \\
& \left( \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \left(86A \sin\left[\frac{1}{2}(c+dx)\right] + 75B \sin\left[\frac{1}{2}(c+dx)\right]\right) \right) / \\
& \left( 512d \sec[c+dx]^{5/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2 \right) + \\
& \left( \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \left(86A \sin\left[\frac{1}{2}(c+dx)\right] + 75B \sin\left[\frac{1}{2}(c+dx)\right]\right) \right) / \\
& \left( 512d \sec[c+dx]^{5/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2 \right)
\end{aligned}$$

**Problem 240: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sec[c+dx]^{3/2} (a+a \sec[c+dx])^{5/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 227 leaves, 6 steps):

$$\begin{aligned}
& \frac{a^{5/2} (200A + 163B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{64d} + \\
& \frac{a^3 (200A + 163B) \sec[c+dx]^{3/2} \sin[c+dx]}{64d \sqrt{a+a \sec[c+dx]}} + \frac{a^3 (104A + 95B) \sec[c+dx]^{5/2} \sin[c+dx]}{96d \sqrt{a+a \sec[c+dx]}} + \\
& \frac{a^2 (8A + 11B) \sec[c+dx]^{5/2} \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{24d} + \\
& \frac{aB \sec[c+dx]^{5/2} (a+a \sec[c+dx])^{3/2} \sin[c+dx]}{4d}
\end{aligned}$$

Result (type 3, 1376 leaves):

$$\begin{aligned}
& - \left( \left( \frac{1}{2048} + \frac{i}{2048} \right) \left( (-1+i) + \sqrt{2} \right) \left( (600+200i)A + 200\sqrt{2}A + (489+163i)B + 163\sqrt{2}B \right) \right. \\
& \quad \left. \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^5 \left(a(1+\sec[c+dx])\right)^{5/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sec[c+dx]^{5/2} \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( \left( \frac{1}{2048} - \frac{i}{2048} \right) \left( (1+i) + \sqrt{2} \right) \left( (-600+200i) A + 200\sqrt{2} A - (489-163i) B + 163\sqrt{2} B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sec[c+dx]^{5/2} \right) + \\
& \left( (400A + 200i\sqrt{2}A + 326B + 163i\sqrt{2}B) \log\left[\sqrt{2} + 2\sin\left[\frac{1}{2}(c+dx)\right]\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2} \right) / \left( 1024 (i+\sqrt{2}) d \sec[c+dx]^{5/2} \right) - \\
& \left( \left( \frac{1}{4096} - \frac{i}{4096} \right) \left( (-1+i) + \sqrt{2} \right) \left( (600+200i) A + 200\sqrt{2} A + (489+163i) B + 163\sqrt{2} B \right) \right. \\
& \quad \log\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \sec\left[\frac{1}{2}(c+dx)\right]^5 \\
& \quad \left. (a(1+\sec[c+dx]))^{5/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sec[c+dx]^{5/2} \right) + \\
& \left( \left( \frac{1}{4096} + \frac{i}{4096} \right) \left( (1+i) + \sqrt{2} \right) \left( (-600+200i) A + 200\sqrt{2} A - (489-163i) B + 163\sqrt{2} B \right) \right. \\
& \quad \log\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \sec\left[\frac{1}{2}(c+dx)\right]^5 \\
& \quad \left. (a(1+\sec[c+dx]))^{5/2} \right) / \left( \sqrt{2} (i+\sqrt{2}) d \sec[c+dx]^{5/2} \right) + \\
& \frac{(8A + 23B) \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{384 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \\
& \frac{(200A + 163B) \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{512 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)} + \\
& \frac{(-8A - 23B) \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{384 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \\
& \frac{(-200A - 163B) \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2}}{512 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} + \\
& \left( \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2} \left( 40A \sin\left[\frac{1}{2}(c+dx)\right] + 43B \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
& \left( 256 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) + \\
& \left( \sec\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\sec[c+dx]))^{5/2} \left( 40A \sin\left[\frac{1}{2}(c+dx)\right] + 43B \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \\
& \left( 256 d \sec[c+dx]^{5/2} \left( \cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) +
\end{aligned}$$

$$\frac{B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{64 d \operatorname{Sec}[c+dx]^{5/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4} +$$

$$\frac{B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{64 d \operatorname{Sec}[c+dx]^{5/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4}$$

**Problem 241: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \sqrt{\operatorname{Sec}[c+dx]} (a+a \operatorname{Sec}[c+dx])^{5/2} (A+B \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 180 leaves, 5 steps):

$$\frac{a^{5/2} (38A+25B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{8d} + \frac{a^3 (54A+49B) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{24d \sqrt{a+a \operatorname{Sec}[c+dx]}} +$$

$$\frac{a^2 (2A+3B) \operatorname{Sec}[c+dx]^{3/2} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4d} +$$

$$\frac{aB \operatorname{Sec}[c+dx]^{3/2} (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{3d}$$

Result (type 3, 1208 leaves):

$$-\left(\left(\frac{1}{256} + \frac{i}{256}\right) \left((-1+i) + \sqrt{2}\right) \left((114+38i)A + 38\sqrt{2}A + (75+25i)B + 25\sqrt{2}B\right) \right.$$

$$\operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right]$$

$$\left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2}\right) / \left(\sqrt{2}(i+\sqrt{2})d \operatorname{Sec}[c+dx]^{5/2}\right) -$$

$$\left(\left(\frac{1}{256} - \frac{i}{256}\right) \left((1+i) + \sqrt{2}\right) \left((-114+38i)A + 38\sqrt{2}A - (75-25i)B + 25\sqrt{2}B\right) \right.$$

$$\operatorname{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right]$$

$$\left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2}\right) / \left(\sqrt{2}(i+\sqrt{2})d \operatorname{Sec}[c+dx]^{5/2}\right) +$$

$$\left((76A+38i\sqrt{2}A+50B+25i\sqrt{2}B) \operatorname{Log}\left[\sqrt{2}+2 \sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5\right)$$

$$\begin{aligned}
& \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \Bigg/ \left( 128 \left( i + \sqrt{2} \right) d \sec [c + d x]^{5/2} \right) - \\
& \left( \left( \frac{1}{512} - \frac{i}{512} \right) \left( (-1 + i) + \sqrt{2} \right) \left( (114 + 38 i) A + 38 \sqrt{2} A + (75 + 25 i) B + 25 \sqrt{2} B \right) \right. \\
& \quad \left. \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right]^5 \right. \\
& \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \right) \Bigg/ \left( \sqrt{2} \left( i + \sqrt{2} \right) d \sec [c + d x]^{5/2} \right) + \\
& \left( \left( \frac{1}{512} + \frac{i}{512} \right) \left( (1 + i) + \sqrt{2} \right) \left( (-114 + 38 i) A + 38 \sqrt{2} A - (75 - 25 i) B + 25 \sqrt{2} B \right) \right. \\
& \quad \left. \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] \sec \left[ \frac{1}{2} (c + d x) \right]^5 \right. \\
& \quad \left. \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \right) \Bigg/ \left( \sqrt{2} \left( i + \sqrt{2} \right) d \sec [c + d x]^{5/2} \right) + \\
& \frac{B \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2}}{48 d \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \\
& \frac{\left( 22 A + 25 B \right) \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2}}{64 d \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)} - \\
& \frac{B \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2}}{48 d \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3} + \\
& \frac{\left( -22 A - 25 B \right) \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2}}{64 d \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)} + \\
& \left( \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( 2 A \sin \left[ \frac{1}{2} (c + d x) \right] + 5 B \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) \Bigg/ \\
& \left( 32 d \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( \sec \left[ \frac{1}{2} (c + d x) \right]^5 \left( a \left( 1 + \sec [c + d x] \right) \right)^{5/2} \left( 2 A \sin \left[ \frac{1}{2} (c + d x) \right] + 5 B \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) \Bigg/ \\
& \left( 32 d \sec [c + d x]^{5/2} \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right)
\end{aligned}$$

**Problem 242: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\left( a + a \sec [c + d x] \right)^{5/2} \left( A + B \sec [c + d x] \right)}{\sqrt{\sec [c + d x]}} dx$$

Optimal (type 3, 180 leaves, 5 steps):

$$\begin{aligned}
& \frac{a^{5/2} (20A + 19B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{4d} + \frac{a^3 (4A - 9B) \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
& \frac{a^2 (4A + 7B) \sqrt{\operatorname{Sec}[c+dx]} \sqrt{a+a \operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{4d} + \\
& \frac{aB \sqrt{\operatorname{Sec}[c+dx]} (a+a \operatorname{Sec}[c+dx])^{3/2} \operatorname{Sin}[c+dx]}{2d}
\end{aligned}$$

Result (type 3, 1094 leaves):

$$\begin{aligned}
& - \left( \left( \frac{1}{128} + \frac{i}{128} \right) \left( (-1+i) + \sqrt{2} \right) \left( (60+20i)A + 20\sqrt{2}A + (57+19i)B + 19\sqrt{2}B \right) \right. \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \right] / \left( \sqrt{2}(i+\sqrt{2})d \operatorname{Sec}[c+dx]^{5/2} \right) \Bigg) - \\
& \left( \left( \frac{1}{128} - \frac{i}{128} \right) \left( (1+i) + \sqrt{2} \right) \left( (-60+20i)A + 20\sqrt{2}A - (57-19i)B + 19\sqrt{2}B \right) \right. \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 (a(1+\operatorname{Sec}[c+dx]))^{5/2} \right] / \left( \sqrt{2}(i+\sqrt{2})d \operatorname{Sec}[c+dx]^{5/2} \right) + \\
& \left( (40A + 20i\sqrt{2}A + 38B + 19i\sqrt{2}B) \operatorname{Log}\left[\sqrt{2} + 2\sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \right. \\
& \quad \left. (a(1+\operatorname{Sec}[c+dx]))^{5/2} \right) / \left( 64(i+\sqrt{2})d \operatorname{Sec}[c+dx]^{5/2} \right) - \\
& \left( \left( \frac{1}{256} - \frac{i}{256} \right) \left( (-1+i) + \sqrt{2} \right) \left( (60+20i)A + 20\sqrt{2}A + (57+19i)B + 19\sqrt{2}B \right) \right. \\
& \quad \operatorname{Log}\left[2 - \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \\
& \quad \left. (a(1+\operatorname{Sec}[c+dx]))^{5/2} \right] / \left( \sqrt{2}(i+\sqrt{2})d \operatorname{Sec}[c+dx]^{5/2} \right) + \\
& \left( \left( \frac{1}{256} + \frac{i}{256} \right) \left( (1+i) + \sqrt{2} \right) \left( (-60+20i)A + 20\sqrt{2}A - (57-19i)B + 19\sqrt{2}B \right) \right. \\
& \quad \operatorname{Log}\left[2 + \sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^5 \\
& \quad \left. (a(1+\operatorname{Sec}[c+dx]))^{5/2} \right] / \left( \sqrt{2}(i+\sqrt{2})d \operatorname{Sec}[c+dx]^{5/2} \right) +
\end{aligned}$$

$$\begin{aligned}
& \frac{(4A + 11B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^5 (a(1 + \operatorname{Sec}[c + dx]))^{5/2}}{32d \operatorname{Sec}[c + dx]^{5/2} \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)} + \\
& \frac{(-4A - 11B) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^5 (a(1 + \operatorname{Sec}[c + dx]))^{5/2}}{32d \operatorname{Sec}[c + dx]^{5/2} \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)} + \\
& \frac{A \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4 (a(1 + \operatorname{Sec}[c + dx]))^{5/2} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{2d \operatorname{Sec}[c + dx]^{5/2}} + \\
& \frac{B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4 (a(1 + \operatorname{Sec}[c + dx]))^{5/2} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{16d \operatorname{Sec}[c + dx]^{5/2} \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} + \\
& \frac{B \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^4 (a(1 + \operatorname{Sec}[c + dx]))^{5/2} \operatorname{Tan}\left[\frac{1}{2}(c + dx)\right]}{16d \operatorname{Sec}[c + dx]^{5/2} \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^2}
\end{aligned}$$

**Problem 243: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \operatorname{Sec}[c + dx])^{5/2} (A + B \operatorname{Sec}[c + dx])}{\operatorname{Sec}[c + dx]^{3/2}} dx$$

Optimal (type 3, 177 leaves, 5 steps):

$$\begin{aligned}
& \frac{a^{5/2} (2A + 5B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c + dx]}{\sqrt{a + a \operatorname{Sec}[c + dx]}}\right]}{d} + \frac{a^3 (14A + 3B) \sqrt{\operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{3d \sqrt{a + a \operatorname{Sec}[c + dx]}} - \\
& \frac{a^2 (2A - 3B) \sqrt{\operatorname{Sec}[c + dx]} \sqrt{a + a \operatorname{Sec}[c + dx]} \operatorname{Sin}[c + dx]}{3d} + \\
& \frac{2aA (a + a \operatorname{Sec}[c + dx])^{3/2} \operatorname{Sin}[c + dx]}{3d \sqrt{\operatorname{Sec}[c + dx]}}
\end{aligned}$$

Result (type 3, 635 leaves):

$$\begin{aligned}
& \frac{1}{d \operatorname{Sec}[c+dx]^{5/2}} \left( \frac{1}{384} + \frac{i}{384} \right) \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^4 \\
& (a(1+\operatorname{Sec}[c+dx]))^{5/2} \left( \frac{1}{i+\sqrt{2}} 6i\sqrt{2} \left( (-3+i)+\sqrt{2} \right) \left( (1+i)+\sqrt{2} \right) (2A+5B) \right. \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2})\sin\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2})\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] - \\
& \quad \frac{1}{i+\sqrt{2}} 6\sqrt{2} \left( (-1+i)+\sqrt{2} \right) \left( (3+i)+\sqrt{2} \right) (2A+5B) \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2})\sin\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2})\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] + \frac{1}{i+\sqrt{2}} \\
& \quad (12+12i) \left( -2i+\sqrt{2} \right) (2A+5B) \operatorname{Log}\left[\sqrt{2}+2\sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] + \\
& \quad \frac{1}{i+\sqrt{2}} 3i\sqrt{2} \left( (-1+i)+\sqrt{2} \right) \left( (3+i)+\sqrt{2} \right) (2A+5B) \\
& \quad \operatorname{Log}\left[2-\sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] + \\
& \quad \frac{1}{i+\sqrt{2}} 3\sqrt{2} \left( (-3+i)+\sqrt{2} \right) \left( (1+i)+\sqrt{2} \right) (2A+5B) \\
& \quad \operatorname{Log}\left[2+\sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] + \\
& \quad (16-16i) A \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right] \sin\left[\frac{3}{2}(c+dx)\right] - \frac{(24-24i) B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{-1+\tan\left[\frac{1}{2}(c+dx)\right]} + \\
& \quad \left. (48-48i) (5A+2B) \tan\left[\frac{1}{2}(c+dx)\right] - \frac{(24-24i) B \operatorname{Sec}\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]} \right)
\end{aligned}$$

**Problem 244: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a+a \operatorname{Sec}[c+dx])^{5/2} (A+B \operatorname{Sec}[c+dx])}{\operatorname{Sec}[c+dx]^{5/2}} dx$$

Optimal (type 3, 172 leaves, 5 steps):

$$\begin{aligned}
& \frac{2a^{5/2} B \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{d} + \frac{2a^3 (32A+35B) \sqrt{\operatorname{Sec}[c+dx]} \sin[c+dx]}{15d \sqrt{a+a \operatorname{Sec}[c+dx]}} + \\
& \frac{2a^2 (8A+5B) \sqrt{a+a \operatorname{Sec}[c+dx]} \sin[c+dx]}{15d \sqrt{\operatorname{Sec}[c+dx]}} + \frac{2aA (a+a \operatorname{Sec}[c+dx])^{3/2} \sin[c+dx]}{5d \operatorname{Sec}[c+dx]^{3/2}}
\end{aligned}$$

Result (type 3, 376 leaves):

$$\begin{aligned} & \frac{1}{60 d \sqrt{\sec [c+d x]}} a^2 \sec \left[ \frac{1}{2} (c+d x) \right] \sqrt{a (1+\sec [c+d x])} \\ & \left( -30 i \sqrt{2} B \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (-1+\sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(1+\sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] - \right. \\ & 30 i \sqrt{2} B \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (1+\sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(-1+\sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] + \\ & 30 \sqrt{2} B \operatorname{Log} \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \\ & 15 \sqrt{2} B \operatorname{Log} \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \\ & 15 \sqrt{2} B \operatorname{Log} \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] + 300 A \sin \left[ \frac{1}{2} (c+d x) \right] + \\ & \left. 300 B \sin \left[ \frac{1}{2} (c+d x) \right] + 50 A \sin \left[ \frac{3}{2} (c+d x) \right] + 20 B \sin \left[ \frac{3}{2} (c+d x) \right] + 6 A \sin \left[ \frac{5}{2} (c+d x) \right] \right) \end{aligned}$$

**Problem 248: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^{5/2} (A+B \sec [c+d x])}{\sqrt{a+a \sec [c+d x]}} dx$$

Optimal (type 3, 190 leaves, 7 steps):

$$\begin{aligned} & -\frac{(4 A-7 B) \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}} \right]}{4 \sqrt{a} d} + \frac{\sqrt{2} (A-B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}} \right]}{\sqrt{a} d} \\ & + \frac{(4 A-B) \sec [c+d x]^{3/2} \sin [c+d x]}{4 d \sqrt{a+a \sec [c+d x]}} + \frac{B \sec [c+d x]^{5/2} \sin [c+d x]}{2 d \sqrt{a+a \sec [c+d x]}} \end{aligned}$$

Result (type 3, 684 leaves):



$$\begin{aligned}
& \frac{1}{d \sqrt{a (1 + \sec [c + d x])}} \left( \frac{1}{64} + \frac{i}{64} \right) \cos \left[ \frac{1}{2} (c + d x) \right] \\
& \sqrt{\sec [c + d x]} \left( \frac{1}{-1 + i \sqrt{2}} 2 \sqrt{2} \left( (-3 + i) + \sqrt{2} \right) \left( (1 + i) + \sqrt{2} \right) (4A - 7B) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (-1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] + \frac{1}{i + \sqrt{2}} 2 \sqrt{2} \left( (-1 + i) + \sqrt{2} \right) \\
& \quad \left. \left( (3 + i) + \sqrt{2} \right) (4A - 7B) \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c + d x) \right] - (1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c + d x) \right]}{(-1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right]} \right] - \right. \\
& \quad (64 - 64i) (A - B) \log \left[ \cos \left[ \frac{1}{4} (c + d x) \right] - \sin \left[ \frac{1}{4} (c + d x) \right] \right] + \\
& \quad (64 - 64i) (A - B) \log \left[ \cos \left[ \frac{1}{4} (c + d x) \right] + \sin \left[ \frac{1}{4} (c + d x) \right] \right] - \\
& \quad \left. \frac{(4 + 4i) (-2i + \sqrt{2}) (4A - 7B) \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c + d x) \right] \right]}{i + \sqrt{2}} + \right. \\
& \quad \frac{1}{-1 + i \sqrt{2}} \sqrt{2} \left( (-1 + i) + \sqrt{2} \right) \left( (3 + i) + \sqrt{2} \right) (4A - 7B) \\
& \quad \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \frac{1}{i + \sqrt{2}} \sqrt{2} \left( (-3 + i) + \sqrt{2} \right) \\
& \quad \left. \left( (1 + i) + \sqrt{2} \right) (4A - 7B) \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c + d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \right. \\
& \quad \frac{(8 - 8i) (4A - B)}{\cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right]} + \frac{(16 - 16i) B \sin \left[ \frac{1}{2} (c + d x) \right]}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \\
& \quad \left. \frac{(16 - 16i) B \sin \left[ \frac{1}{2} (c + d x) \right]}{\left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2} + \frac{(8 - 8i) (-4A + B)}{\cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right]} \right)
\end{aligned}$$

**Problem 249: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^{3/2} (A + B \sec [c + d x])}{\sqrt{a + a \sec [c + d x]}} dx$$

Optimal (type 3, 141 leaves, 6 steps):

$$\frac{(2A-B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{\sqrt{a} d} -$$

$$\frac{\sqrt{2} (A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec[c+dx]} \sin[c+dx]}{\sqrt{2} \sqrt{a+a \sec[c+dx]}}\right]}{\sqrt{a} d} + \frac{B \sec[c+dx]^{3/2} \sin[c+dx]}{d \sqrt{a+a \sec[c+dx]}}$$

Result(type 3, 596 leaves):

$$\frac{1}{d \sqrt{a(1+\sec[c+dx])}} \left( \frac{1}{16} + \frac{i}{16} \right) \cos\left[\frac{1}{2}(c+dx)\right]$$

$$\sqrt{\sec[c+dx]} \left( \frac{1}{i+\sqrt{2}} 2i\sqrt{2} \left( (-3+i) + \sqrt{2} \right) \left( (1+i) + \sqrt{2} \right) (2A-B) \right.$$

$$\operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (-1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] - \frac{1}{i+\sqrt{2}} 2\sqrt{2} \left( (-1+i) + \sqrt{2} \right)$$

$$\left( (3+i) + \sqrt{2} \right) (2A-B) \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - (1+\sqrt{2}) \sin\left[\frac{1}{4}(c+dx)\right]}{(-1+\sqrt{2}) \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] +$$

$$(16-16i) (A-B) \log\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] -$$

$$(16-16i) (A-B) \log\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] +$$

$$\frac{(4+4i) \left( -2i + \sqrt{2} \right) (2A-B) \log\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c+dx)\right]\right]}{i+\sqrt{2}} +$$

$$\frac{1}{i+\sqrt{2}} i\sqrt{2} \left( (-1+i) + \sqrt{2} \right) \left( (3+i) + \sqrt{2} \right) (2A-B)$$

$$\log\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] + \frac{1}{i+\sqrt{2}} \sqrt{2} \left( (-3+i) + \sqrt{2} \right)$$

$$\left( (1+i) + \sqrt{2} \right) (2A-B) \log\left[2 + \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] +$$

$$\left. \frac{(8-8i) B}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} - \frac{(8-8i) B}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} \right)$$

**Problem 250: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec[c+dx]} (A+B \sec[c+dx])}{\sqrt{a+a \sec[c+dx]}} dx$$

Optimal (type 3, 100 leaves, 5 steps):

$$\frac{2 B \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right]}{\sqrt{a} d} + \frac{\sqrt{2} (A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right]}{\sqrt{a} d}$$

Result (type 3, 412 leaves):

$$\begin{aligned} & \frac{1}{2 d \sqrt{a (1+\sec [c+d x])}} \\ & \cos \left[ \frac{1}{2} (c+d x) \right] \left( -2 i \sqrt{2} B \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (-1+\sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(1+\sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] - \right. \\ & \quad 2 i \sqrt{2} B \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (1+\sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(-1+\sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] - \\ & \quad 4 A \log \left[ \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right] \right] + \\ & \quad 4 B \log \left[ \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right] \right] + 4 A \log \left[ \cos \left[ \frac{1}{4} (c+d x) \right] + \sin \left[ \frac{1}{4} (c+d x) \right] \right] - \\ & \quad 4 B \log \left[ \cos \left[ \frac{1}{4} (c+d x) \right] + \sin \left[ \frac{1}{4} (c+d x) \right] \right] + 2 \sqrt{2} B \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \\ & \quad \sqrt{2} B \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] - \\ & \quad \left. \sqrt{2} B \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right) \sqrt{\sec [c+d x]} \end{aligned}$$

**Problem 255: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^{7/2} (A+B \sec [c+d x])}{(a+a \sec [c+d x])^{3/2}} dx$$

Optimal (type 3, 247 leaves, 8 steps):

$$\begin{aligned} & -\frac{(12 A-19 B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right]}{4 a^{3/2} d} + \\ & \frac{(9 A-13 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right]}{2 \sqrt{2} a^{3/2} d} + \frac{(A-B) \sec [c+d x]^{7/2} \sin [c+d x]}{2 d (a+a \sec [c+d x])^{3/2}} + \\ & \frac{(6 A-7 B) \sec [c+d x]^{3/2} \sin [c+d x]}{4 a d \sqrt{a+a \sec [c+d x]}} - \frac{(A-2 B) \sec [c+d x]^{5/2} \sin [c+d x]}{2 a d \sqrt{a+a \sec [c+d x]}} \end{aligned}$$

Result (type 3, 1318 leaves):

$$\begin{aligned}
& - \left( \left( \frac{1}{8} + \frac{i}{8} \right) \left( (-1+i) + \sqrt{2} \right) \left( (-36-12i) A - 12\sqrt{2} A + (57+19i) B + 19\sqrt{2} B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+dx) \right]}{-\cos \left[ \frac{1}{4} (c+dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right]} \right] \\
& \quad \left. \cos \left[ \frac{1}{2} (c+dx) \right]^3 \sec [c+dx]^{3/2} \right) / \left( \sqrt{2} (i + \sqrt{2}) d (a (1 + \sec [c+dx]))^{3/2} \right) - \\
& \left( \left( \frac{1}{8} - \frac{i}{8} \right) \left( (1+i) + \sqrt{2} \right) \left( (36-12i) A - 12\sqrt{2} A - (57-19i) B + 19\sqrt{2} B \right) \right. \\
& \quad \text{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{4} (c+dx) \right]}{\cos \left[ \frac{1}{4} (c+dx) \right] + \sqrt{2} \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right]} \right] \\
& \quad \left. \cos \left[ \frac{1}{2} (c+dx) \right]^3 \sec [c+dx]^{3/2} \right) / \left( \sqrt{2} (i + \sqrt{2}) d (a (1 + \sec [c+dx]))^{3/2} \right) + \\
& \left( (-9A + 13B) \cos \left[ \frac{1}{2} (c+dx) \right]^3 \log \left[ \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] \right] \sec [c+dx]^{3/2} \right) / \\
& \left( d (a (1 + \sec [c+dx]))^{3/2} \right) + \\
& \left( (9A - 13B) \cos \left[ \frac{1}{2} (c+dx) \right]^3 \log \left[ \cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] \right] \sec [c+dx]^{3/2} \right) / \\
& \left( d (a (1 + \sec [c+dx]))^{3/2} \right) + \\
& \left( (-24A - 12i\sqrt{2}A + 38B + 19i\sqrt{2}B) \cos \left[ \frac{1}{2} (c+dx) \right]^3 \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+dx) \right] \right] \right. \\
& \quad \left. \sec [c+dx]^{3/2} \right) / \left( 4 (i + \sqrt{2}) d (a (1 + \sec [c+dx]))^{3/2} \right) - \\
& \left( \left( \frac{1}{16} - \frac{i}{16} \right) \left( (-1+i) + \sqrt{2} \right) \left( (-36-12i) A - 12\sqrt{2} A + (57+19i) B + 19\sqrt{2} B \right) \right. \\
& \quad \left. \cos \left[ \frac{1}{2} (c+dx) \right]^3 \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \sec [c+dx]^{3/2} \right) / \\
& \left( \sqrt{2} (i + \sqrt{2}) d (a (1 + \sec [c+dx]))^{3/2} \right) + \\
& \left( \left( \frac{1}{16} + \frac{i}{16} \right) \left( (1+i) + \sqrt{2} \right) \left( (36-12i) A - 12\sqrt{2} A - (57-19i) B + 19\sqrt{2} B \right) \right. \\
& \quad \left. \cos \left[ \frac{1}{2} (c+dx) \right]^3 \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \sec [c+dx]^{3/2} \right) / \\
& \left( \sqrt{2} (i + \sqrt{2}) d (a (1 + \sec [c+dx]))^{3/2} \right) + \\
& \frac{(A-B) \cos \left[ \frac{1}{2} (c+dx) \right]^3 \sec [c+dx]^{3/2}}{2 d (a (1 + \sec [c+dx]))^{3/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] \right)^2} + \\
& \frac{(-A+B) \cos \left[ \frac{1}{2} (c+dx) \right]^3 \sec [c+dx]^{3/2}}{2 d (a (1 + \sec [c+dx]))^{3/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] \right)^2} +
\end{aligned}$$

$$\begin{aligned}
& \frac{(4A - 5B) \cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2}}{2d \left(a \left(1 + \sec[c+dx]\right)\right)^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)} + \\
& \frac{B \cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2} \sin\left[\frac{1}{2}(c+dx)\right]}{d \left(a \left(1 + \sec[c+dx]\right)\right)^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \\
& \frac{B \cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2} \sin\left[\frac{1}{2}(c+dx)\right]}{d \left(a \left(1 + \sec[c+dx]\right)\right)^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \\
& \frac{(-4A + 5B) \cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2}}{2d \left(a \left(1 + \sec[c+dx]\right)\right)^{3/2} \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)}
\end{aligned}$$

**Problem 256: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^{5/2} (A + B \sec[c+dx])}{(a + a \sec[c+dx])^{3/2}} dx$$

Optimal (type 3, 197 leaves, 7 steps):

$$\begin{aligned}
& \frac{(2A - 3B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right]}{a^{3/2} d} - \frac{(5A - 9B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec[c+dx]} \sin[c+dx]}{\sqrt{2} \sqrt{a+a \sec[c+dx]}}\right]}{2\sqrt{2} a^{3/2} d} + \\
& \frac{(A - B) \sec[c+dx]^{5/2} \sin[c+dx]}{2d (a + a \sec[c+dx])^{3/2}} - \frac{(A - 3B) \sec[c+dx]^{3/2} \sin[c+dx]}{2ad \sqrt{a+a \sec[c+dx]}}
\end{aligned}$$

Result (type 3, 1157 leaves):

$$\begin{aligned}
& - \left( \left( \frac{1}{2} - \frac{i}{2} \right) \left( (1+i) - i\sqrt{2} \right) \left( (-6-2i)A - 2\sqrt{2}A + (9+3i)B + 3\sqrt{2}B \right) \right. \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2} \right) / \left( \sqrt{2} (i + \sqrt{2}) d (a (1 + \sec[c+dx]))^{3/2} \right) + \\
& \left( \left( \frac{1}{2} - \frac{i}{2} \right) \left( (1+i) + \sqrt{2} \right) \left( (6-2i)A - 2\sqrt{2}A - (9-3i)B + 3\sqrt{2}B \right) \right. \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right]
\end{aligned}$$

$$\begin{aligned}
& \cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2} \Bigg/ \left(\sqrt{2}(\mathbf{i}+\sqrt{2})d(a(1+\sec[c+dx]))^{3/2}\right) + \\
& \left((5A-9B)\cos\left[\frac{1}{2}(c+dx)\right]^3 \log\left[\cos\left[\frac{1}{4}(c+dx)\right]-\sin\left[\frac{1}{4}(c+dx)\right]\right]\sec[c+dx]^{3/2}\right) \Bigg/ \\
& \left(d(a(1+\sec[c+dx]))^{3/2}\right) + \\
& \left((-5A+9B)\cos\left[\frac{1}{2}(c+dx)\right]^3 \log\left[\cos\left[\frac{1}{4}(c+dx)\right]+\sin\left[\frac{1}{4}(c+dx)\right]\right]\sec[c+dx]^{3/2}\right) \Bigg/ \\
& \left(d(a(1+\sec[c+dx]))^{3/2}\right) + \\
& \left((4A+2\mathbf{i}\sqrt{2}A-6B-3\mathbf{i}\sqrt{2}B)\cos\left[\frac{1}{2}(c+dx)\right]^3 \log\left[\sqrt{2}+2\sin\left[\frac{1}{2}(c+dx)\right]\right]\sec[c+dx]^{3/2}\right) \Bigg/ \\
& \left((\mathbf{i}+\sqrt{2})d(a(1+\sec[c+dx]))^{3/2}\right) + \\
& \left(\left(\frac{1}{4}+\frac{\mathbf{i}}{4}\right)\left((1+\mathbf{i})-\mathbf{i}\sqrt{2}\right)\left((-6-2\mathbf{i})A-2\sqrt{2}A+(9+3\mathbf{i})B+3\sqrt{2}B\right)\cos\left[\frac{1}{2}(c+dx)\right]^3 \right. \\
& \quad \left. \log\left[2-\sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right]-\sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right]\sec[c+dx]^{3/2}\right) \Bigg/ \\
& \left(\sqrt{2}(\mathbf{i}+\sqrt{2})d(a(1+\sec[c+dx]))^{3/2}\right) - \\
& \left(\left(\frac{1}{4}+\frac{\mathbf{i}}{4}\right)\left((1+\mathbf{i})+\sqrt{2}\right)\left((6-2\mathbf{i})A-2\sqrt{2}A-(9-3\mathbf{i})B+3\sqrt{2}B\right)\cos\left[\frac{1}{2}(c+dx)\right]^3 \right. \\
& \quad \left. \log\left[2+\sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right]-\sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right]\sec[c+dx]^{3/2}\right) \Bigg/ \\
& \left(\sqrt{2}(\mathbf{i}+\sqrt{2})d(a(1+\sec[c+dx]))^{3/2}\right) + \\
& \frac{(-A+B)\cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2}}{2d(a(1+\sec[c+dx]))^{3/2}\left(\cos\left[\frac{1}{4}(c+dx)\right]-\sin\left[\frac{1}{4}(c+dx)\right]\right)^2} + \\
& \frac{(A-B)\cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2}}{2d(a(1+\sec[c+dx]))^{3/2}\left(\cos\left[\frac{1}{4}(c+dx)\right]+\sin\left[\frac{1}{4}(c+dx)\right]\right)^2} + \\
& \frac{2B\cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2}}{d(a(1+\sec[c+dx]))^{3/2}\left(\cos\left[\frac{1}{2}(c+dx)\right]-\sin\left[\frac{1}{2}(c+dx)\right]\right)} - \\
& \frac{2B\cos\left[\frac{1}{2}(c+dx)\right]^3 \sec[c+dx]^{3/2}}{d(a(1+\sec[c+dx]))^{3/2}\left(\cos\left[\frac{1}{2}(c+dx)\right]+\sin\left[\frac{1}{2}(c+dx)\right]\right)}
\end{aligned}$$

**Problem 257: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^{3/2}(A+B\sec[c+dx])}{(a+a\sec[c+dx])^{3/2}} dx$$

Optimal (type 3, 145 leaves, 6 steps):

$$\frac{2 B \operatorname{ArcSinh}\left[\frac{-\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \sec [c+d x]}}\right]}{a^{3/2} d} +$$

$$\frac{(A-5 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec [c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right]}{2 \sqrt{2} a^{3/2} d} + \frac{(A-B) \sec [c+d x]^{3/2} \operatorname{Sin}[c+d x]}{2 d (a+a \sec [c+d x])^{3/2}}$$

Result (type 3, 430 leaves):

$$\frac{1}{2 d (a (1 + \sec [c+d x]))^{3/2}} \cos \left[ \frac{1}{2} (c+d x) \right]^3 \sec [c+d x]^{3/2}$$

$$\left( -4 i \sqrt{2} B \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (-1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] - \right.$$

$$4 i \sqrt{2} B \operatorname{ArcTan} \left[ \frac{\cos \left[ \frac{1}{4} (c+d x) \right] - (1 + \sqrt{2}) \sin \left[ \frac{1}{4} (c+d x) \right]}{(-1 + \sqrt{2}) \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right]} \right] -$$

$$2 (A-5 B) \log \left[ \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right] \right] +$$

$$2 (A-5 B) \log \left[ \cos \left[ \frac{1}{4} (c+d x) \right] + \sin \left[ \frac{1}{4} (c+d x) \right] \right] + 4 \sqrt{2} B \log \left[ \sqrt{2} + 2 \sin \left[ \frac{1}{2} (c+d x) \right] \right] -$$

$$2 \sqrt{2} B \log \left[ 2 - \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] -$$

$$2 \sqrt{2} B \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+d x) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+d x) \right] \right] +$$

$$\left. \frac{A-B}{\left( \cos \left[ \frac{1}{4} (c+d x) \right] - \sin \left[ \frac{1}{4} (c+d x) \right] \right)^2} + \frac{-A+B}{\left( \cos \left[ \frac{1}{4} (c+d x) \right] + \sin \left[ \frac{1}{4} (c+d x) \right] \right)^2} \right)$$

**Problem 262: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^{7/2} (A+B \sec [c+d x])}{(a+a \sec [c+d x])^{5/2}} dx$$

Optimal (type 3, 246 leaves, 8 steps):

$$\begin{aligned}
& \frac{(2A - 5B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+dx]}{\sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{a^{5/2} d} - \\
& \frac{(43A - 115B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+dx]} \operatorname{Sin}[c+dx]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+dx]}}\right]}{16 \sqrt{2} a^{5/2} d} + \frac{(A - B) \operatorname{Sec}[c+dx]^{7/2} \operatorname{Sin}[c+dx]}{4 d (a + a \operatorname{Sec}[c+dx])^{5/2}} + \\
& \frac{(7A - 15B) \operatorname{Sec}[c+dx]^{5/2} \operatorname{Sin}[c+dx]}{16 a d (a + a \operatorname{Sec}[c+dx])^{3/2}} - \frac{(11A - 35B) \operatorname{Sec}[c+dx]^{3/2} \operatorname{Sin}[c+dx]}{16 a^2 d \sqrt{a + a \operatorname{Sec}[c+dx]}}
\end{aligned}$$

Result(type 3, 1304 leaves):

$$\begin{aligned}
& - \left( \left( (1 - i) \left( (1 + i) - i \sqrt{2} \right) \left( (-6 - 2i) A - 2 \sqrt{2} A + (15 + 5i) B + 5 \sqrt{2} B \right) \right. \right. \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \cos\left[\frac{1}{2}(c+dx)\right]^5 \operatorname{Sec}[c+dx]^{5/2} \right) / \left( \sqrt{2} (i + \sqrt{2}) d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) + \\
& \left( (1 - i) \left( (1 + i) + \sqrt{2} \right) \left( (6 - 2i) A - 2 \sqrt{2} A - (15 - 5i) B + 5 \sqrt{2} B \right) \right. \\
& \quad \operatorname{ArcTan}\left[ \frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]} \right] \\
& \quad \left. \cos\left[\frac{1}{2}(c+dx)\right]^5 \operatorname{Sec}[c+dx]^{5/2} \right) / \left( \sqrt{2} (i + \sqrt{2}) d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) + \\
& \left( (43A - 115B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \operatorname{Log}\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] \operatorname{Sec}[c+dx]^{5/2} \right) / \\
& \left( 4 d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) + \\
& \left( (-43A + 115B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \operatorname{Log}\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] \operatorname{Sec}[c+dx]^{5/2} \right) / \\
& \left( 4 d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) + \\
& \left( 2 (4A + 2i \sqrt{2} A - 10B - 5i \sqrt{2} B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \operatorname{Log}\left[\sqrt{2} + 2 \sin\left[\frac{1}{2}(c+dx)\right]\right] \right. \\
& \quad \left. \operatorname{Sec}[c+dx]^{5/2} \right) / \left( (i + \sqrt{2}) d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) + \\
& \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( (1 + i) - i \sqrt{2} \right) \left( (-6 - 2i) A - 2 \sqrt{2} A + (15 + 5i) B + 5 \sqrt{2} B \right) \cos\left[\frac{1}{2}(c+dx)\right]^5 \right. \\
& \quad \left. \operatorname{Log}\left[2 - \sqrt{2} \cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2} \sin\left[\frac{1}{2}(c+dx)\right]\right] \operatorname{Sec}[c+dx]^{5/2} \right) / \\
& \left( \sqrt{2} (i + \sqrt{2}) d (a (1 + \operatorname{Sec}[c+dx]))^{5/2} \right) -
\end{aligned}$$



$$\begin{aligned}
& \left( \left( \frac{1}{2} + \frac{i}{2} \right) \left( (1+i) + \sqrt{2} \right) \left( (6-2i) A - 2\sqrt{2} A - (15-5i) B + 5\sqrt{2} B \right) \cos \left[ \frac{1}{2} (c+dx) \right]^5 \right. \\
& \quad \left. \log \left[ 2 + \sqrt{2} \cos \left[ \frac{1}{2} (c+dx) \right] - \sqrt{2} \sin \left[ \frac{1}{2} (c+dx) \right] \right] \sec [c+dx]^{5/2} \right) / \\
& \quad \left( \sqrt{2} (i + \sqrt{2}) d (a (1 + \sec [c+dx]))^{5/2} \right) + \\
& \quad \frac{(-A+B) \cos \left[ \frac{1}{2} (c+dx) \right]^5 \sec [c+dx]^{5/2}}{8 d (a (1 + \sec [c+dx]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] \right)^4} + \\
& \quad \frac{(-11A+19B) \cos \left[ \frac{1}{2} (c+dx) \right]^5 \sec [c+dx]^{5/2}}{8 d (a (1 + \sec [c+dx]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] - \sin \left[ \frac{1}{4} (c+dx) \right] \right)^2} + \\
& \quad \frac{(A-B) \cos \left[ \frac{1}{2} (c+dx) \right]^5 \sec [c+dx]^{5/2}}{8 d (a (1 + \sec [c+dx]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] \right)^4} + \\
& \quad \frac{(11A-19B) \cos \left[ \frac{1}{2} (c+dx) \right]^5 \sec [c+dx]^{5/2}}{8 d (a (1 + \sec [c+dx]))^{5/2} \left( \cos \left[ \frac{1}{4} (c+dx) \right] + \sin \left[ \frac{1}{4} (c+dx) \right] \right)^2} + \\
& \quad \frac{4B \cos \left[ \frac{1}{2} (c+dx) \right]^5 \sec [c+dx]^{5/2}}{d (a (1 + \sec [c+dx]))^{5/2} \left( \cos \left[ \frac{1}{2} (c+dx) \right] - \sin \left[ \frac{1}{2} (c+dx) \right] \right)} - \\
& \quad \frac{4B \cos \left[ \frac{1}{2} (c+dx) \right]^5 \sec [c+dx]^{5/2}}{d (a (1 + \sec [c+dx]))^{5/2} \left( \cos \left[ \frac{1}{2} (c+dx) \right] + \sin \left[ \frac{1}{2} (c+dx) \right] \right)}
\end{aligned}$$

**Problem 263: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+dx]^{5/2} (A+B \sec [c+dx])}{(a+a \sec [c+dx])^{5/2}} dx$$

Optimal (type 3, 194 leaves, 7 steps):

$$\begin{aligned}
& \frac{2B \operatorname{ArcSinh} \left[ \frac{\sqrt{a} \tan [c+dx]}{\sqrt{a+a \sec [c+dx]}} \right]}{a^{5/2} d} + \frac{(3A-43B) \operatorname{ArcTanh} \left[ \frac{\sqrt{a} \sqrt{\sec [c+dx]} \sin [c+dx]}{\sqrt{2} \sqrt{a+a \sec [c+dx]}} \right]}{16 \sqrt{2} a^{5/2} d} + \\
& \frac{(A-B) \sec [c+dx]^{5/2} \sin [c+dx]}{4 d (a+a \sec [c+dx])^{5/2}} + \frac{(3A-11B) \sec [c+dx]^{3/2} \sin [c+dx]}{16 a d (a+a \sec [c+dx])^{3/2}}
\end{aligned}$$

Result (type 3, 988 leaves):

$$- \left( \left( 2 \left( (-1+i) + \sqrt{2} \right) \left( (1+i) + \sqrt{2} \right) B \right. \right.$$

$$\begin{aligned}
& \text{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{4}(c+dx)\right]}{-\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right] \cos\left[\frac{1}{2}(c+dx)\right]^5 \\
& \sec[c+dx]^{5/2} \Bigg/ \left(d(a(1+\sec[c+dx]))^{5/2}\right) - \left(2((-1+i) + \sqrt{2})\right. \\
& \left.((1+i) + \sqrt{2}) B \text{ArcTan}\left[\frac{\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{4}(c+dx)\right]}{\cos\left[\frac{1}{4}(c+dx)\right] + \sqrt{2}\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]}\right]\right. \\
& \left.\cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}\right) \Bigg/ \left(d(a(1+\sec[c+dx]))^{5/2}\right) + \\
& \left((-3A+43B)\cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] \sec[c+dx]^{5/2}\right) \Bigg/ \\
& \left(4d(a(1+\sec[c+dx]))^{5/2}\right) + \\
& \left((3A-43B)\cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] \sec[c+dx]^{5/2}\right) \Bigg/ \\
& \left(4d(a(1+\sec[c+dx]))^{5/2}\right) + \\
& \left(4\sqrt{2}B\cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\sqrt{2}+2\sin\left[\frac{1}{2}(c+dx)\right]\right] \sec[c+dx]^{5/2}\right) \Bigg/ \\
& \left(d(a(1+\sec[c+dx]))^{5/2}\right) + \\
& \left(i((-1+i) + \sqrt{2})((1+i) + \sqrt{2})B\cos\left[\frac{1}{2}(c+dx)\right]^5\right. \\
& \left.\log\left[2-\sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] \sec[c+dx]^{5/2}\right) \Bigg/ \\
& \left(d(a(1+\sec[c+dx]))^{5/2}\right) + \left(i((-1+i) + \sqrt{2})((1+i) + \sqrt{2})B\cos\left[\frac{1}{2}(c+dx)\right]^5\right. \\
& \left.\log\left[2+\sqrt{2}\cos\left[\frac{1}{2}(c+dx)\right] - \sqrt{2}\sin\left[\frac{1}{2}(c+dx)\right]\right] \sec[c+dx]^{5/2}\right) \Bigg/ \\
& \left(d(a(1+\sec[c+dx]))^{5/2}\right) + \frac{(A-B)\cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8d(a(1+\sec[c+dx]))^{5/2}\left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^4} + \\
& \frac{(3A-11B)\cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8d(a(1+\sec[c+dx]))^{5/2}\left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^2} + \\
& \frac{(-A+B)\cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8d(a(1+\sec[c+dx]))^{5/2}\left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^4} + \\
& \frac{(-3A+11B)\cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8d(a(1+\sec[c+dx]))^{5/2}\left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^2}
\end{aligned}$$

Problem 266: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\sqrt{\operatorname{Sec}[c + d x]} (a + a \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 203 leaves, 5 steps):

$$\begin{aligned} & - \frac{(75A - 19B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{\sqrt{2} \sqrt{a + a \operatorname{Sec}[c + d x]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A - B) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{4 d (a + a \operatorname{Sec}[c + d x])^{5/2}} - \\ & \frac{(13A - 5B) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{16 a d (a + a \operatorname{Sec}[c + d x])^{3/2}} + \frac{(49A - 9B) \sqrt{\operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{16 a^2 d \sqrt{a + a \operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 3, 491 leaves):

$$\begin{aligned} & \left( (75A - 19B) \cos\left[\frac{1}{2}(c + dx)\right]^5 \operatorname{Log}\left[\cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]\right] \operatorname{Sec}[c + dx]^{5/2} \right) / \\ & \left( 4 d (a (1 + \operatorname{Sec}[c + dx]))^{5/2} \right) + \\ & \left( (-75A + 19B) \cos\left[\frac{1}{2}(c + dx)\right]^5 \operatorname{Log}\left[\cos\left[\frac{1}{4}(c + dx)\right] + \sin\left[\frac{1}{4}(c + dx)\right]\right] \operatorname{Sec}[c + dx]^{5/2} \right) / \\ & \left( 4 d (a (1 + \operatorname{Sec}[c + dx]))^{5/2} \right) + \\ & \frac{(-A + B) \cos\left[\frac{1}{2}(c + dx)\right]^5 \operatorname{Sec}[c + dx]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c + dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]\right)^4} + \\ & \frac{(21A - 13B) \cos\left[\frac{1}{2}(c + dx)\right]^5 \operatorname{Sec}[c + dx]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c + dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c + dx)\right] - \sin\left[\frac{1}{4}(c + dx)\right]\right)^2} + \\ & \frac{(A - B) \cos\left[\frac{1}{2}(c + dx)\right]^5 \operatorname{Sec}[c + dx]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c + dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c + dx)\right] + \sin\left[\frac{1}{4}(c + dx)\right]\right)^4} + \\ & \frac{(-21A + 13B) \cos\left[\frac{1}{2}(c + dx)\right]^5 \operatorname{Sec}[c + dx]^{5/2}}{8 d (a (1 + \operatorname{Sec}[c + dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c + dx)\right] + \sin\left[\frac{1}{4}(c + dx)\right]\right)^2} + \\ & \frac{16 A \cos\left[\frac{1}{2}(c + dx)\right]^5 \operatorname{Sec}[c + dx]^{5/2} \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]}{d (a (1 + \operatorname{Sec}[c + dx]))^{5/2}} \end{aligned}$$

**Problem 267: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\operatorname{Sec}[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 3, 250 leaves, 6 steps):

$$\begin{aligned}
& \frac{(163A - 75B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec[c+dx]} \sin[c+dx]}{\sqrt{2} \sqrt{a+a \sec[c+dx]}}\right]}{16 \sqrt{2} a^{5/2} d} - \\
& \frac{(A-B) \sin[c+dx]}{4 d \sqrt{\sec[c+dx]} (a+a \sec[c+dx])^{5/2}} - \frac{(17A-9B) \sin[c+dx]}{16 a d \sqrt{\sec[c+dx]} (a+a \sec[c+dx])^{3/2}} + \\
& \frac{(95A-39B) \sin[c+dx]}{48 a^2 d \sqrt{\sec[c+dx]} \sqrt{a+a \sec[c+dx]}} - \frac{(299A-147B) \sqrt{\sec[c+dx]} \sin[c+dx]}{48 a^2 d \sqrt{a+a \sec[c+dx]}}
\end{aligned}$$

Result (type 3, 551 leaves):

$$\begin{aligned}
& \left( (-163A + 75B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] \sec[c+dx]^{5/2} \right) / \\
& \left( 4 d (a (1 + \sec[c+dx]))^{5/2} \right) + \\
& \left( (163A - 75B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] \sec[c+dx]^{5/2} \right) / \\
& \left( 4 d (a (1 + \sec[c+dx]))^{5/2} \right) + \\
& \frac{(A-B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8 d (a (1 + \sec[c+dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^4} + \\
& \frac{(-29A + 21B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8 d (a (1 + \sec[c+dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^2} + \\
& \frac{(-A+B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8 d (a (1 + \sec[c+dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^4} + \\
& \frac{(29A - 21B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8 d (a (1 + \sec[c+dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^2} + \\
& \frac{8 (-5A + 2B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2} \sin\left[\frac{1}{2}(c+dx)\right]}{d (a (1 + \sec[c+dx]))^{5/2}} + \\
& \frac{8 A \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2} \sin\left[\frac{3}{2}(c+dx)\right]}{3 d (a (1 + \sec[c+dx]))^{5/2}}
\end{aligned}$$

**Problem 268: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c+dx]}{\sec[c+dx]^{5/2} (a + a \sec[c+dx])^{5/2}} dx$$

Optimal (type 3, 297 leaves, 7 steps):

$$\begin{aligned}
& - \frac{(283 A - 163 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec[c+dx]} \sin[c+dx]}{\sqrt{2} \sqrt{a+a \sec[c+dx]}}\right]}{16 \sqrt{2} a^{5/2} d} - \frac{(A-B) \sin[c+dx]}{4 d \sec[c+dx]^{3/2} (a+a \sec[c+dx])^{5/2}} - \\
& \frac{(21 A - 13 B) \sin[c+dx]}{16 a d \sec[c+dx]^{3/2} (a+a \sec[c+dx])^{3/2}} + \frac{(157 A - 85 B) \sin[c+dx]}{80 a^2 d \sec[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}} - \\
& \frac{(787 A - 475 B) \sin[c+dx]}{240 a^2 d \sqrt{\sec[c+dx]} \sqrt{a+a \sec[c+dx]}} + \frac{(2671 A - 1495 B) \sqrt{\sec[c+dx]} \sin[c+dx]}{240 a^2 d \sqrt{a+a \sec[c+dx]}}
\end{aligned}$$

Result (type 3, 609 leaves):

$$\begin{aligned}
& \left( (283 A - 163 B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right] \sec[c+dx]^{5/2} \right) / \\
& \left( 4 d (a (1 + \sec[c+dx]))^{5/2} \right) + \\
& \left( (-283 A + 163 B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \log\left[\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right] \sec[c+dx]^{5/2} \right) / \\
& \left( 4 d (a (1 + \sec[c+dx]))^{5/2} \right) + \\
& \frac{(-A+B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8 d (a (1 + \sec[c+dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^4} + \\
& \frac{(37 A - 29 B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8 d (a (1 + \sec[c+dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c+dx)\right] - \sin\left[\frac{1}{4}(c+dx)\right]\right)^2} + \\
& \frac{(A-B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8 d (a (1 + \sec[c+dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^4} + \\
& \frac{(-37 A + 29 B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2}}{8 d (a (1 + \sec[c+dx]))^{5/2} \left(\cos\left[\frac{1}{4}(c+dx)\right] + \sin\left[\frac{1}{4}(c+dx)\right]\right)^2} - \\
& \frac{40 (-2 A + B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2} \sin\left[\frac{1}{2}(c+dx)\right]}{d (a (1 + \sec[c+dx]))^{5/2}} + \\
& \frac{4 (-5 A + 2 B) \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2} \sin\left[\frac{3}{2}(c+dx)\right]}{3 d (a (1 + \sec[c+dx]))^{5/2}} + \\
& \frac{4 A \cos\left[\frac{1}{2}(c+dx)\right]^5 \sec[c+dx]^{5/2} \sin\left[\frac{5}{2}(c+dx)\right]}{5 d (a (1 + \sec[c+dx]))^{5/2}}
\end{aligned}$$

**Problem 269: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sec[c+dx])^{2/3} (A + B \sec[c+dx]) dx$$

Optimal (type 6, 406 leaves, 9 steps):

$$\begin{aligned}
& \left( 3 \sqrt{2} \operatorname{AppellF1} \left[ \frac{7}{6}, \frac{1}{2}, 1, \frac{13}{6}, \frac{1}{2} (1 + \sec[c + dx]), 1 + \sec[c + dx] \right] (a + a \sec[c + dx])^{2/3} \right. \\
& \quad \left. \tan[c + dx] \right) / \left( 7 d \sqrt{1 - \sec[c + dx]} \right) + \frac{3 B (a + a \sec[c + dx])^{2/3} \tan[c + dx]}{2 d (1 + \sec[c + dx])} - \\
& \left( 3^{3/4} \operatorname{EllipticF} \left[ \operatorname{ArcCos} \left[ \frac{2^{1/3} - (1 - \sqrt{3}) (1 + \sec[c + dx])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right. \\
& \quad \left. (a + a \sec[c + dx])^{2/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3}) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \sec[c + dx])^{1/3} + (1 + \sec[c + dx])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3})^2}} \tan[c + dx] \right) / \left( 2 \times 2^{1/3} d \right. \\
& \quad \left. (1 - \sec[c + dx]) (1 + \sec[c + dx]) \sqrt{-\frac{(1 + \sec[c + dx])^{1/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3})^2}} \right)
\end{aligned}$$

Result (type 6, 7123 leaves):

$$\begin{aligned}
& \left( 3 B \cos[c + dx] ((1 + \cos[c + dx]) \sec[c + dx])^{2/3} (a (1 + \sec[c + dx]))^{2/3} \right. \\
& \quad \left. (A + B \sec[c + dx]) \tan\left[\frac{1}{2} (c + dx)\right] \right) / \left( 2 d (B + A \cos[c + dx]) (1 + \sec[c + dx])^{2/3} \right) + \\
& \left( \cos[c + dx] (a (1 + \sec[c + dx]))^{2/3} (A + B \sec[c + dx]) \right. \\
& \quad \left( \frac{1}{2} A \cos[c + dx] \sec\left[\frac{1}{2} (c + dx)\right]^2 (1 + \sec[c + dx])^{2/3} + \right. \\
& \quad \left. \sec\left[\frac{1}{2} (c + dx)\right]^2 \left( \frac{1}{2} A (1 + \sec[c + dx])^{2/3} + \frac{1}{4} B (1 + \sec[c + dx])^{2/3} \right) \right) \tan\left[\frac{1}{2} (c + dx)\right] \\
& \quad \left( \frac{1}{1 - \tan\left[\frac{1}{2} (c + dx)\right]^2} \right)^{2/3} \left( 10 B \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2} (c + dx)\right]^2, -\tan\left[\frac{1}{2} (c + dx)\right]^2 \right] \right. \\
& \quad \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2} (c + dx)\right]^2, -\tan\left[\frac{1}{2} (c + dx)\right]^2 \right] + \right. \\
& \quad \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2} (c + dx)\right]^2, -\tan\left[\frac{1}{2} (c + dx)\right]^2 \right] \right) \tan\left[\frac{1}{2} (c + dx)\right]^4 + \\
& \quad 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2} (c + dx)\right]^2, -\tan\left[\frac{1}{2} (c + dx)\right]^2 \right] \\
& \quad \left( -2 (4 A + B) \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2} (c + dx)\right]^2, -\tan\left[\frac{1}{2} (c + dx)\right]^2 \right] - \right. \right. \\
& \quad \left. \left. 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2} (c + dx)\right]^2, -\tan\left[\frac{1}{2} (c + dx)\right]^2 \right] \right) \tan\left[\frac{1}{2} (c + dx)\right]^2 + \right. \\
& \quad \left. 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2} (c + dx)\right]^2, -\tan\left[\frac{1}{2} (c + dx)\right]^2 \right] \right)
\end{aligned}$$

[illegible]

$$\begin{aligned} & \left( 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right.\right.\right. \\ & \quad \left.\left.\frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \right. \\ & \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \left( 10 B \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \right.\right.\right. \\ & \quad \left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\ & \quad \left. \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right.\right.\right. \\ & \quad \left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^4 + \right. \\ & \quad \left. 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\ & \quad \left. \left(-2(4A+B) \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right.\right.\right. \\ & \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\ & \quad \left. \left. + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\ & \quad \left. \left. \left( 12 A + B \left( 3 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \Bigg) / \left( 2 \times 2^{1/3} \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\ & \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ & \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right.\right. \\ & \quad \left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\ & \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ & \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right.\right. \\ & \quad \left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \right. \\ & \left( 2^{2/3} \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{5/3} \right. \\ & \quad \left( 10 B \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\ & \quad \left. \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right.\right. \right. \\ & \quad \left.\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^4 + \right. \\ & \quad \left. \left. \left( 12 A + B \left( 3 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \end{aligned}$$



$$\begin{aligned}
& 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \left(-2(4A+B)\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right.\right. \\
& \quad \left.2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \quad \left.\left.\left(12A+B\left(3+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right)\right)\right) \Bigg/ \left(3\left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \\
& \left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \quad \left.-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left.2\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \Bigg) - \\
& \left(\tan\left[\frac{1}{2}(c+dx)\right] \left(\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}\right)^{2/3} \left(2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right.\right. \\
& \quad \left.9\left(-\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left.3\left(-\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right) - \\
& \quad \left.2\left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \frac{1}{2} (c+dx)^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \\
& \left( 10 B \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 + \\
& \quad 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \quad \left( -2 (4A+B) \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. \left( 12A+B \left( 3 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \right) / \left( 2^{1/3} \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \\
& \quad \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \\
& \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \\
& \quad \left( \tan\left[\frac{1}{2}(c+dx)\right] \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \left( 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \right. \\
& \quad \left. \left. 15 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \right. \\
& \quad \left. \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \left( 3 \left( -\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) - \\
& 2 \left( -\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right] \right) \Big) \\
& \left( 10 B \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 + \\
& 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \quad \left( -2(4A+B) \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 12A+B \left( 3 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \right) \Big) / \\
& \left( 2^{1/3} \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) \\
& \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) \Big) + \\
& \left( \tan\left[\frac{1}{2}(c+dx)\right] \left( \frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{2/3} \left( 20 B \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2] + 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + \\
& 10 B \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \tan\left[\frac{1}{2}(c+dx)\right]^4 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \right. \right. \\
& \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \\
& 10 B \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^4 \\
& \left( -3 \left( -\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + \right. \\
& \left. 2 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
& 9 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \\
& \left( -2 (4 A + B) \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( 12 A + B \left( 3 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) + \\
& 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \left( 5 B \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.
\end{aligned}$$

$$\begin{aligned}
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 2(4A+B) \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \right. \right. \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2] \Big) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \\
& 2(4A+B) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( 3 \left( -\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - 2 \left( -\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\
& \quad \left. \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 5 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \right. \right. \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
& \quad \left. \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \left( 12A+B \left( 3 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg) \Bigg/ \\
& \left( 2^{1/3} \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) \Bigg)
\end{aligned}$$

Problem 270: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \sec [c + d x]}{(a + a \sec [c + d x])^{1/3}} dx$$

Optimal (type 6, 354 leaves, 8 steps):

$$\begin{aligned} & \left( 3 \sqrt{2} A \operatorname{AppellF1} \left[ \frac{1}{6}, \frac{1}{2}, 1, \frac{7}{6}, \frac{1}{2} (1 + \sec [c + d x]), 1 + \sec [c + d x] \right] \tan [c + d x] \right) / \\ & \left( d \sqrt{1 - \sec [c + d x]} (a + a \sec [c + d x])^{1/3} \right) - \\ & \left( 3^{3/4} B \operatorname{EllipticF} \left[ \operatorname{ArcCos} \left[ \frac{2^{1/3} - (1 - \sqrt{3}) (1 + \sec [c + d x])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \sec [c + d x])^{1/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right. \\ & \left. (2^{1/3} - (1 + \sec [c + d x])^{1/3}) \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \sec [c + d x])^{1/3} + (1 + \sec [c + d x])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \sec [c + d x])^{1/3})^2}} \right. \\ & \left. \tan [c + d x] \right) / \left( 2^{1/3} d (1 - \sec [c + d x]) (a + a \sec [c + d x])^{1/3} \right. \\ & \left. \sqrt{-\frac{(1 + \sec [c + d x])^{1/3} (2^{1/3} - (1 + \sec [c + d x])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \sec [c + d x])^{1/3})^2}} \right) \end{aligned}$$

Result (type 6, 7136 leaves):

$$\begin{aligned} & \left( 2^{2/3} \cos [c + d x]^2 \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{5/3} \right. \\ & (1 + \sec [c + d x])^{1/3} (A + B \sec [c + d x]) \left( \frac{1}{2} B \sec \left[ \frac{1}{2} (c + d x) \right]^2 (1 + \sec [c + d x])^{2/3} + \right. \\ & \left. \frac{1}{2} A \cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^2 (1 + \sec [c + d x])^{2/3} \right) \tan \left[ \frac{1}{2} (c + d x) \right] \\ & \left( 10 (A - B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\ & \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \\ & \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^4 - \\ & 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \\ & \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\ & (A + 2 B + (2 A + B) \cos [c + d x]) \sec \left[ \frac{1}{2} (c + d x) \right]^2 + \\ & 2 (A + B) \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\ & \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left. \right) \left. \right) / \end{aligned}$$

$$\begin{aligned}
& \left( d (B + A \cos[c + dx]) (a (1 + \sec[c + dx]))^{1/3} \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \Big) \\
& \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \Big) \\
& \left( \cos[c + dx] \sec\left[\frac{1}{2}(c + dx)\right]^2 \left( \cos\left[\frac{1}{2}(c + dx)\right]^2 \sec[c + dx] \right)^{5/3} \right. \\
& \quad \left( 10 (A - B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \\
& \quad \tan\left[\frac{1}{2}(c + dx)\right]^4 - 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \\
& \quad \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \\
& \quad \left. (A + 2B + (2A + B) \cos[c + dx]) \sec\left[\frac{1}{2}(c + dx)\right]^2 + 2(A + B) \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \Big) \Big) \Big) / \\
& \left( 2^{1/3} \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \Big) \\
& \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \Big) \Big) - \\
& \left( 2^{2/3} \left( \cos\left[\frac{1}{2}(c + dx)\right]^2 \sec[c + dx] \right)^{5/3} \sin[c + dx] \tan\left[\frac{1}{2}(c + dx)\right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left( 10 (A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^4 - 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \quad \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. (A+2B+(2A+B)\cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(A+B) \right. \\
& \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) \right) \Bigg/ \\
& \left( \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \frac{5}{3}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) - \\
& \left( 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( 10 (A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^4 - 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \quad \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. (A+2B+(2A+B)\cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(A+B) \right. \\
& \quad \left. \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \frac{5}{3}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left. \right) \right) \Bigg)
\end{aligned}$$



$$\begin{aligned}
& \left( 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \\
& \quad 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \\
& \quad \tan \left[ \frac{1}{2} (c+dx) \right] - 9 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + \\
& \quad 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+ \right. \right. \right. \\
& \quad \left. \left. \left. dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) - \\
& \quad 2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) \Bigg/ \\
& \left( \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right)^2 \\
& \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \Bigg) - \\
& \left( 2^{2/3} \cos [c+dx] \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{5/3} \tan \left[ \frac{1}{2} (c+dx) \right] \right. \\
& \quad \left( 10 (A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
& \quad \tan \left[ \frac{1}{2} (c+dx) \right]^4 - 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \\
& \quad \left. \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right.
\end{aligned}$$

$$\begin{aligned}
& (A + 2B + (2A + B) \cos[c + dx]) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 + 2(A + B) \\
& \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \Bigg) \\
& \left(2 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - \right. \right. \\
& \quad \left. \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right]\right) \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] - \right. \\
& \quad 15 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \\
& \quad \left. \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right]\right) + 2 \tan\left[\frac{1}{2}(c + dx)\right]^2 \\
& \quad \left(3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right]\right) \right) - \\
& \quad \left. 2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \right. \\
& \quad \left. \left. \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c + \right. \right. \right. \\
& \quad \left. \left. \left. dx\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right]\right)\right) \Bigg) \Bigg) / \\
& \left( \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. 2 \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right. \\
& \quad \left. \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. 2 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c + dx)\right]^2 \right) \right) + \\
& \quad \left( 2^{2/3} \cos[c + dx] \left( \cos\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Sec}[c + dx] \right)^{5/3} \tan\left[\frac{1}{2}(c + dx)\right] \right. \\
& \quad \left. \left( 20(A - B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \\
& \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^3 + 10 (A-B) \\
& \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^4 \\
& \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \Big) - \\
& 9 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \Big) \\
& \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. (A+2B+(2A+B) \cos [c+dx]) \sec \left[ \frac{1}{2} (c+dx) \right]^2 + 2 (A+B) \right. \\
& \quad \left. \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big) + \\
& 10 (A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \\
& \tan \left[ \frac{1}{2} (c+dx) \right]^4 \\
& \left( 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{2}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \Big) - \\
& 2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \Big) -
\end{aligned}$$

$$9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]$$
$$\left(5(2A+B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right.$$
$$\sec\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] +$$
$$2(A+B) \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] -\right.$$
$$\left.2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right)$$
$$\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2,\right.$$
$$\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right](A+2B+(2A+B)\cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2$$
$$\tan\left[\frac{1}{2}(c+dx)\right] - 5(A+2B+(2A+B)\cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2$$
$$\left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right.$$
$$\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2},\right.$$
$$\left.\tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\Bigg) +$$
$$2(A+B) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(3\left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2,\right.\right.\right.$$
$$\left.\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] +\right.$$
$$\left.\frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right.$$
$$\left.\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) - 2\left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2,\right.\right.$$
$$\left.\frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2$$
$$\tan\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2,\right.$$
$$\left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\Bigg)\Bigg)/$$
$$\left(\left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] +\right.\right.$$
$$\left.2\left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\right.\right.$$
$$\left.\left.\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right)$$
$$\left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] +\right.$$
$$\left.2\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2},\right.\right.\right.$$

$$\begin{aligned}
& \left( \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& \left( 5 \times 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( 10(A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^4 - 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \\
& \quad \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \\
& \quad \left. (A+2B + (2A+B) \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(A+B) \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \quad \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \sec[c+dx] \tan[c+dx] \right) \Bigg) / \\
& \left( 3 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \Bigg)
\end{aligned}$$

**Problem 271: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx]}{(a+a \sec[c+dx])^{4/3}} dx$$

Optimal (type 6, 415 leaves, 9 steps):

$$\begin{aligned}
& \frac{3 B \tan [c+d x]}{5 a d (1+\sec [c+d x]) (a+a \sec [c+d x])^{1/3}} - \\
& \left( 3 \sqrt{2} \operatorname{AppellF1}\left[-\frac{5}{6}, \frac{1}{2}, 1, \frac{1}{6}, \frac{1}{2} (1+\sec [c+d x]), 1+\sec [c+d x]\right] \tan [c+d x] \right) / \\
& \left( 5 a d \sqrt{1-\sec [c+d x]} (1+\sec [c+d x]) (a+a \sec [c+d x])^{1/3} \right) - \\
& \left( 3^{3/4} B \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3}-\left(1-\sqrt{3}\right)(1+\sec [c+d x])^{1/3}}{2^{1/3}-\left(1+\sqrt{3}\right)(1+\sec [c+d x])^{1/3}}\right], \frac{1}{4}(2+\sqrt{3})\right] \right. \\
& \left. \left( 2^{1/3}-\left(1+\sec [c+d x]\right)^{1/3} \right) \sqrt{\frac{2^{2/3}+2^{1/3}(1+\sec [c+d x])^{1/3}+(1+\sec [c+d x])^{2/3}}{\left(2^{1/3}-\left(1+\sqrt{3}\right)(1+\sec [c+d x])^{1/3}\right)^2}} \right. \right. \\
& \left. \left. \tan [c+d x] \right) \right) / \left( 5 \times 2^{1/3} a d (1-\sec [c+d x]) (a+a \sec [c+d x])^{1/3} \right. \\
& \left. \sqrt{-\frac{(1+\sec [c+d x])^{1/3}\left(2^{1/3}-\left(1+\sec [c+d x]\right)^{1/3}\right)}{\left(2^{1/3}-\left(1+\sqrt{3}\right)(1+\sec [c+d x])^{1/3}\right)^2}} \right)
\end{aligned}$$

Result (type 6, 7385 leaves):

$$\begin{aligned}
& \left( \cos [c+d x] \left( (1+\cos [c+d x]) \sec [c+d x] \right)^{2/3} (1+\sec [c+d x])^{4/3} \right. \\
& \left( A+B \sec [c+d x] \right) \left( \frac{3}{5} \sec \left[ \frac{1}{2} (c+d x) \right] \left( -A \sin \left[ \frac{1}{2} (c+d x) \right] + B \sin \left[ \frac{1}{2} (c+d x) \right] \right) - \right. \\
& \left. \frac{3}{10} \sec \left[ \frac{1}{2} (c+d x) \right]^3 \left( -A \sin \left[ \frac{1}{2} (c+d x) \right] + B \sin \left[ \frac{1}{2} (c+d x) \right] \right) \right) / \\
& \left( d (B+A \cos [c+d x]) (a(1+\sec [c+d x]))^{4/3} \right) + \\
& \left( 2^{2/3} \cos [c+d x]^2 \left( \cos \left[ \frac{1}{2} (c+d x) \right]^2 \sec [c+d x] \right)^{5/3} (1+\sec [c+d x])^{4/3} \right. \\
& \left( A+B \sec [c+d x] \right) \left( \frac{1}{2} A \cos [c+d x] \sec \left[ \frac{1}{2} (c+d x) \right]^2 (1+\sec [c+d x])^{2/3} + \right. \\
& \left. \sec \left[ \frac{1}{2} (c+d x) \right]^2 \left( -\frac{1}{10} A (1+\sec [c+d x])^{2/3} + \frac{1}{10} B (1+\sec [c+d x])^{2/3} \right) \right) \tan \left[ \frac{1}{2} (c+d x) \right] \\
& \left( 10 (6 A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \right. \\
& \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] - \right. \\
& \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \right) \tan \left[ \frac{1}{2} (c+d x) \right]^4 - \\
& 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \\
& \left. \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( 3 A + 2 B + (9 A + B) \cos [c + d x] \right) \sec \left[ \frac{1}{2} (c + d x) \right]^2 + 2 (4 A + B) \\
& \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Big) \Big) / \\
& \left( 5 d (B + A \cos [c + d x]) (a (1 + \sec [c + d x]))^{4/3} \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Big) \\
& \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Big) \\
& \left( \left( \cos [c + d x] \sec \left[ \frac{1}{2} (c + d x) \right]^2 \left( \cos \left[ \frac{1}{2} (c + d x) \right]^2 \sec [c + d x] \right)^{5/3} \right. \right. \\
& \quad \left( 10 (6 A - B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^4 - \\
& \quad 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \\
& \quad \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right. \\
& \quad \left. \left( 3 A + 2 B + (9 A + B) \cos [c + d x] \right) \sec \left[ \frac{1}{2} (c + d x) \right]^2 + 2 (4 A + B) \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
& \quad \quad \left. \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \right. \\
& \quad \quad \left. 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Big) \Big) / \\
& \left( 5 \times 2^{1/3} \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \Big) \\
& \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right.
\end{aligned}$$

$$\begin{aligned}
& 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) - \\
& \left( 2^{2/3} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{5/3} \sin [c+dx] \tan \left[ \frac{1}{2} (c+dx) \right] \right. \\
& \quad \left( 10 (6A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^4 - \\
& \quad 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \\
& \quad \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. (3A+2B+(9A+B) \cos [c+dx]) \sec \left[ \frac{1}{2} (c+dx) \right]^2 + 2(4A+B) \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{5}{3}, \right. \right. \\
& \quad \left. \left. 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) \Bigg) / \\
& \left( 5 \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) \\
& \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Bigg) - \\
& \left( 2^{2/3} \cos [c+dx] \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{5/3} \tan \left[ \frac{1}{2} (c+dx) \right] \right. \\
& \quad \left( 10 (6A-B) \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - 2 \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^4 - \\
& \quad 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \\
& \quad \left. \left( -5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right)
\end{aligned}$$



$$\begin{aligned}
& (3A + 2B + (9A + B) \cos[c + dx]) \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 + 2(4A + B) \\
& \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \tan\left[\frac{1}{2}(c + dx)\right]^2\right) \right. \\
& \left. \left(2 \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] \right. \right. \right. \\
& \left. \left. \frac{1}{2}(c + dx)\right] - 9 \left(-\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right]\right) + 2 \tan\left[\frac{1}{2}(c + dx)\right]^2 \right. \right. \\
& \left. \left(3 \left(-\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \right. \right. \right. \\
& \left. \left. \left. \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right]\right) \right) - \right. \\
& \left. 2 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, \right. \right. \right. \right. \\
& \left. \left. \left. -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(c + dx)\right]^2 \tan\left[\frac{1}{2}(c + dx)\right]\right)\right) \right) \Bigg/ \\
& \left(5 \left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \right. \\
& \left. 2 \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \tan\left[\frac{1}{2}(c + dx)\right]^2\right) \right. \\
& \left. \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] + \right. \right. \\
& \left. 2 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \tan\left[\frac{1}{2}(c + dx)\right]^2\right) \right) - \right. \\
& \left. \left(2^{2/3} \cos[c + dx] \left(\cos\left[\frac{1}{2}(c + dx)\right]^2 \operatorname{Sec}[c + dx]\right)^{5/3} \tan\left[\frac{1}{2}(c + dx)\right] \right. \right. \\
& \left. \left(10(6A - B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \right. \right. \\
& \left. \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c + dx)\right]^2, -\tan\left[\frac{1}{2}(c + dx)\right]^2\right] \tan\left[\frac{1}{2}(c + dx)\right]^2\right) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \\
& 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \left(-5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left.(3A+2B+(9A+B)\cos[c+dx])\sec\left[\frac{1}{2}(c+dx)\right]^2+2(4A+B) \right. \\
& \quad \left.(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \left(2 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \quad \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 15 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \right. \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
& \quad \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \quad \left(3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \right. \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\
& 2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \Bigg/ \\
& \left(5 \left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad 2 \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \quad \left(-15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. 2 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 + \\
& \left( 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{5/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( 20(6A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + 10(6A-B) \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \quad \left. 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \\
& \quad \tan\left[\frac{1}{2}(c+dx)\right]^4 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \right. \right. \\
& \quad \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\
& 9 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \\
& \quad \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. (3A+2B+(9A+B) \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(4A+B) \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) + 10(6A-B) \\
& \quad \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^4 \\
& \quad \left( 3 \left( -\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 3, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) - \\
& 2 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right.
\end{aligned}$$

$$\begin{aligned}
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{8}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) - \\
& 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \left(5(9A+B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] + \right. \\
& 2(4A+B) \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\
& \left. 2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \\
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& - \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(3A+2B+(9A+B) \cos[c+dx]\right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \\
& - 5(3A+2B+(9A+B) \cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
& \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{2}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{5}{3}, 1, \frac{7}{2}, \right. \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) + \\
& 2(4A+B) \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{2}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \left. \frac{10}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) - 2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{5}{3}, 2, \right. \right. \\
& \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \\
& \tan\left[\frac{1}{2}(c+dx)\right] + \frac{25}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{8}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Big) \Big) \Big) / \\
& \left(5 \left(-9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& 2 \left(3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big)
\end{aligned}$$

$$\begin{aligned}
& \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& \quad \left( 2^{2/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3} \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( 10(6A-B) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^4 - \\
& \quad 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \quad \left( -5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \quad \left. (3A+2B+(9A+B)\cos[c+dx]) \sec\left[\frac{1}{2}(c+dx)\right]^2 + 2(4A+B) \right. \\
& \quad \quad \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \quad \quad \left. \left. \frac{5}{3}, \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \\
& \quad \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \quad \left. \sec[c+dx] \tan[c+dx] \right) \Bigg) / \\
& \quad \left( 3 \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{2}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, \frac{5}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\
& \quad \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - 2 \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \frac{5}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \Bigg)
\end{aligned}$$

**Problem 272: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sec[c+dx])^{4/3} (A + B \sec[c+dx]) dx$$

Optimal (type 6, 787 leaves, 11 steps):

$$\begin{aligned}
& \frac{3 a B \left( a + a \operatorname{Sec}[c + d x] \right)^{1/3} \operatorname{Tan}[c + d x]}{4 d} + \\
& \left( 3 \sqrt{2} a \operatorname{AppellF1} \left[ \frac{11}{6}, \frac{1}{2}, 1, \frac{17}{6}, \frac{1}{2} \left( 1 + \operatorname{Sec}[c + d x] \right), 1 + \operatorname{Sec}[c + d x] \right] \right. \\
& \quad \left. \left( 1 + \operatorname{Sec}[c + d x] \right) \left( a + a \operatorname{Sec}[c + d x] \right)^{1/3} \operatorname{Tan}[c + d x] \right) / \left( 11 d \sqrt{1 - \operatorname{Sec}[c + d x]} \right) - \\
& \frac{15 \left( 1 + \sqrt{3} \right) a B \left( a + a \operatorname{Sec}[c + d x] \right)^{1/3} \operatorname{Tan}[c + d x]}{4 d \left( 1 + \operatorname{Sec}[c + d x] \right)^{2/3} \left( 2^{1/3} - \left( 1 + \sqrt{3} \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right)} + \\
& \left( 15 \times 3^{1/4} a B \operatorname{EllipticE} \left[ \operatorname{ArcCos} \left[ \frac{2^{1/3} - \left( 1 - \sqrt{3} \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3}}{2^{1/3} - \left( 1 + \sqrt{3} \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3}} \right], \frac{1}{4} \left( 2 + \sqrt{3} \right) \right] \right. \\
& \quad \left. \left( a + a \operatorname{Sec}[c + d x] \right)^{1/3} \left( 2^{1/3} - \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} + \left( 1 + \operatorname{Sec}[c + d x] \right)^{2/3}}{\left( 2^{1/3} - \left( 1 + \sqrt{3} \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right)^2}} \operatorname{Tan}[c + d x]} \right) / \left( 2 \times 2^{2/3} d \right. \\
& \quad \left. \left( 1 - \operatorname{Sec}[c + d x] \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{2/3} \sqrt{-\frac{\left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \left( 2^{1/3} - \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right)}{\left( 2^{1/3} - \left( 1 + \sqrt{3} \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right)^2}} \right) + \\
& \left( 5 \times 3^{3/4} \left( 1 - \sqrt{3} \right) a B \operatorname{EllipticF} \left[ \operatorname{ArcCos} \left[ \frac{2^{1/3} - \left( 1 - \sqrt{3} \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3}}{2^{1/3} - \left( 1 + \sqrt{3} \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3}} \right], \frac{1}{4} \left( 2 + \sqrt{3} \right) \right] \right. \\
& \quad \left. \left( a + a \operatorname{Sec}[c + d x] \right)^{1/3} \left( 2^{1/3} - \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} + \left( 1 + \operatorname{Sec}[c + d x] \right)^{2/3}}{\left( 2^{1/3} - \left( 1 + \sqrt{3} \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right)^2}} \operatorname{Tan}[c + d x]} \right) / \left( 4 \times 2^{2/3} d \right. \\
& \quad \left. \left( 1 - \operatorname{Sec}[c + d x] \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{2/3} \sqrt{-\frac{\left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \left( 2^{1/3} - \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right)}{\left( 2^{1/3} - \left( 1 + \sqrt{3} \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right)^2}} \right)
\end{aligned}$$

Result(type 6, 5276 leaves):

$$\begin{aligned}
& \left( \operatorname{Cos}[c + d x] \left( \left( 1 + \operatorname{Cos}[c + d x] \right) \operatorname{Sec}[c + d x] \right)^{1/3} \left( a \left( 1 + \operatorname{Sec}[c + d x] \right) \right)^{4/3} \right. \\
& \quad \left. \left( A + B \operatorname{Sec}[c + d x] \right) \left( \frac{3}{4} (4 A + 5 B) \operatorname{Sin}[c + d x] + \frac{3}{4} B \operatorname{Tan}[c + d x] \right) \right) / \\
& \left( d \left( B + A \operatorname{Cos}[c + d x] \right) \left( 1 + \operatorname{Sec}[c + d x] \right)^{4/3} \right) - \left( \operatorname{Cos}[c + d x] \left( a \left( 1 + \operatorname{Sec}[c + d x] \right) \right)^{4/3} \right. \\
& \quad \left( A + B \operatorname{Sec}[c + d x] \right) \left( 2 A \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} + \frac{5}{4} B \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} + \right. \\
& \quad \left. \left. \operatorname{Cos}[c + d x] \left( -3 A \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} - \frac{15}{4} B \left( 1 + \operatorname{Sec}[c + d x] \right)^{1/3} \right) \right) \operatorname{Tan} \left[ \frac{1}{2} (c + d x) \right] \right)
\end{aligned}$$

$$\begin{aligned}
& \left( \left( 9 (4A - 5B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) / \right. \\
& \quad \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\
& \quad \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\
& \quad \quad \quad \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) + \\
& \quad \left( (4A + 5B) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] - \right. \right. \right. \\
& \quad \quad \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \right. \\
& \quad \quad \left. \cos [c + dx] \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
& \quad \quad \quad \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \Big) / \\
& \quad \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\
& \quad \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \\
& \quad \quad \quad \left. \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \Big) \Big) / \\
& \quad \left( 2 \times 2^{2/3} d (B + A \cos [c + dx]) \left( \cos \left[ \frac{1}{2} (c + dx) \right]^2 \sec [c + dx] \right)^{2/3} \right. \\
& \quad \quad \left( 1 + \sec [c + dx] \right)^{4/3} \\
& \quad \quad \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^4 \right) \\
& \quad \quad \left( \left( 1 / \left( 2^{2/3} \left( \cos \left[ \frac{1}{2} (c + dx) \right]^2 \sec [c + dx] \right) \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^4 \right)^2 \right) \right) \\
& \quad \quad \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right]^4 \\
& \quad \quad \left( \left( 9 (4A - 5B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) / \right. \\
& \quad \quad \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \\
& \quad \quad \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \quad \quad \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + dx) \right]^2 \Big) + \\
& \quad \quad \left( (4A + 5B) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] - \right. \right. \right. \\
& \quad \quad \quad \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) \right. \\
& \quad \quad \quad \left. \cos [c + dx] \sec \left[ \frac{1}{2} (c + dx) \right]^2 \tan \left[ \frac{1}{2} (c + dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
& \quad \quad \quad \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right) \Big) \Big) /
\end{aligned}$$

$$\begin{aligned}
 & \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) - \\
 & \left( 1 / \left( 4 \times 2^{2/3} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^4 \right) \right) \right) \\
 & \sec \left[ \frac{1}{2} (c+dx) \right]^2 \\
 & \left( \left( 9 (4A-5B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \right. \\
 & \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) + \\
 & \left( (4A+5B) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
 & \quad \left. \cos [c+dx] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) / \\
 & \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) - \\
 & \left( 1 / \left( 2 \times 2^{2/3} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^4 \right) \right) \right) \\
 & \tan \left[ \frac{1}{2} (c+dx) \right] \\
 & \left( \left( 9 (4A-5B) \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \right. \\
 & \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \right. \\
 & \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) / \\
 & \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
 & 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
 & \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) - \\
 & \left( 1 / \left( 2 \times 2^{2/3} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^4 \right) \right) \right) \\
 & \tan \left[ \frac{1}{2} (c+dx) \right]
 \end{aligned}$$



$$\begin{aligned}
& \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 - \\
& \left( 9(4A-5B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left( 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \\
& \quad \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 9 \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \right. \\
& \quad \left. \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \quad \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left( -\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{4}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{7}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 3 \left( -\frac{6}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 3, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Bigg/ \\
& \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
& \quad \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 - \\
& \left( (4A+5B) \left( 6 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
& \quad \left. \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \left( -9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right. \\
& \quad \left( 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right)
\end{aligned}$$

$$\begin{aligned} & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 15\left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right.\right. \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\ & \quad \left.\frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right. \\ & \quad \left.\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right) + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \right.\right. \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right] + \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\ & \quad \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 3\left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, \right.\right. \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\ & \quad \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right)\right) / \\ & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2\right. \\ & \quad \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right.\right. \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \tan\left[\frac{1}{2}(c+dx)\right]^2)^2 + \\ & \left((4A+5B)\left(40 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right.\right. \\ & \quad \left.\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 6\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right.\right. \right. \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^4 \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right] - 6\left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\ & \quad \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\ & \quad \left.-\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sec\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right]^2 + 6 \\ & \quad \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \\ & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \cos[c+dx] \\ & \quad \left.\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + 5\left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right.\right.\right. \end{aligned}$$



$$\begin{aligned}
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \right. \\
& 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c + d x) \right]^2, -\tan \left[ \frac{1}{2} (c + d x) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c + d x) \right]^2 \left. \right) \\
& \left( -\cos \left[ \frac{1}{2} (c + d x) \right] \sec [c + d x] \sin \left[ \frac{1}{2} (c + d x) \right] + \cos \left[ \frac{1}{2} (c + d x) \right]^2 \right. \\
& \quad \left. \sec [c + d x] \tan [c + d x] \right) \left. \right) \left. \right)
\end{aligned}$$

**Problem 273: Result more than twice size of optimal antiderivative.**

$$\int (a + a \sec [c + d x])^{1/3} (A + B \sec [c + d x]) \, dx$$

Optimal (type 6, 739 leaves, 10 steps):

$$\begin{aligned}
& \left( 3 \sqrt{2} \operatorname{AppellF1} \left[ \frac{5}{6}, \frac{1}{2}, 1, \frac{11}{6}, \frac{1}{2} (1 + \sec[c + dx]), 1 + \sec[c + dx] \right] \right. \\
& \quad \left. (a + a \sec[c + dx])^{1/3} \tan[c + dx] \right) / \left( 5 d \sqrt{1 - \sec[c + dx]} \right) - \\
& \quad \frac{3 (1 + \sqrt{3}) B (a + a \sec[c + dx])^{1/3} \tan[c + dx]}{d (1 + \sec[c + dx])^{2/3} (2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3})} + \\
& \quad \left( 3 \times 2^{1/3} \times 3^{1/4} B \operatorname{EllipticE} \left[ \operatorname{ArcCos} \left[ \frac{2^{1/3} - (1 - \sqrt{3}) (1 + \sec[c + dx])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right. \\
& \quad \left. (a + a \sec[c + dx])^{1/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3}) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \sec[c + dx])^{1/3} + (1 + \sec[c + dx])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3})^2}} \tan[c + dx] \right) / \\
& \quad \left( d (1 - \sec[c + dx]) (1 + \sec[c + dx])^{2/3} \sqrt{-\frac{(1 + \sec[c + dx])^{1/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3})^2}} \right) + \\
& \quad \left( 3^{3/4} (1 - \sqrt{3}) B \operatorname{EllipticF} \left[ \operatorname{ArcCos} \left[ \frac{2^{1/3} - (1 - \sqrt{3}) (1 + \sec[c + dx])^{1/3}}{2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3}} \right], \frac{1}{4} (2 + \sqrt{3}) \right] \right. \\
& \quad \left. (a + a \sec[c + dx])^{1/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3}) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1 + \sec[c + dx])^{1/3} + (1 + \sec[c + dx])^{2/3}}{(2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3})^2}} \tan[c + dx] \right) / \left( 2^{2/3} d \right. \\
& \quad \left. (1 - \sec[c + dx]) (1 + \sec[c + dx])^{2/3} \sqrt{-\frac{(1 + \sec[c + dx])^{1/3} (2^{1/3} - (1 + \sec[c + dx])^{1/3})}{(2^{1/3} - (1 + \sqrt{3}) (1 + \sec[c + dx])^{1/3})^2}} \right)
\end{aligned}$$

Result(type 6, 4726 leaves):

$$\begin{aligned}
& \left( 3 B \cos[c + dx] \left( (1 + \cos[c + dx]) \sec[c + dx] \right)^{1/3} (a (1 + \sec[c + dx]))^{1/3} \right. \\
& \quad \left. (A + B \sec[c + dx]) \sin[c + dx] \right) / \left( d (B + A \cos[c + dx]) (1 + \sec[c + dx])^{1/3} \right) + \\
& \quad \left( 2^{1/3} \cos[c + dx]^2 \left( \cos \left[ \frac{1}{2} (c + dx) \right]^2 \sec[c + dx] \right)^{1/3} (a (1 + \sec[c + dx]))^{1/3} (A + B \sec[c + dx]) \right. \\
& \quad \left( A (1 + \sec[c + dx])^{1/3} + B (1 + \sec[c + dx])^{1/3} - 3 B \cos[c + dx] (1 + \sec[c + dx])^{1/3} \right) \tan \left[ \right. \\
& \quad \left. \frac{1}{2} (c + dx) \right] \left( \left( 9 (2 A - B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] \right) / \right. \\
& \quad \left( \left( -1 + \tan \left[ \frac{1}{2} (c + dx) \right]^2 \right) \right. \\
& \quad \left. \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c + dx) \right]^2, -\tan \left[ \frac{1}{2} (c + dx) \right]^2 \right] + \right. \right.
\end{aligned}$$

$$\begin{aligned}
& 2 \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \\
& \quad \left. \left. \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) + \\
& B \left( -3 - \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) / \left( \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \right. \\
& \quad \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad \left. 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \operatorname{AppellF1} \left[ \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) / \\
& \left( d (B + A \cos [c+dx]) (1 + \sec [c+dx])^{1/3} \left( \frac{1}{2^{2/3}} \cos [c+dx] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right. \right. \\
& \quad \left. \left. \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{1/3} \right. \right. \\
& \quad \left( \left( 9 (2A - B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \right. \\
& \quad \left( \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right. \\
& \quad \left( -9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \right. \\
& \quad \left( 3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \operatorname{AppellF1} \left[ \frac{3}{2}, \right. \right. \\
& \quad \left. \left. \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) + \\
& B \left( -3 - \left( 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) / \left( \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left( -15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right) - \\
& 2^{1/3} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{1/3} \sin [c+dx] \tan \left[ \frac{1}{2} (c+dx) \right] \\
& \left( \left( 9 (2A - B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \right. \\
& \quad \left( \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \left. \left. \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& B \left( -3 - \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \right. \right. \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \Bigg) \Bigg) \Bigg) + \\
& 2^{1/3} \cos[c+dx] \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{1/3} \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left( - \left( \left( 9(2A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \right. \\
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Bigg) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \left( -9 \right. \right. \right. \\
& \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \right. \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \Bigg) \Bigg) \Bigg) + \\
& \left( 9(2A-B) \left( -\frac{1}{3} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \right. \\
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{9} \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \Bigg) \Bigg) / \\
& \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + \\
& 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \Bigg) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \Bigg) - \\
& \left( 9(2A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \left( 2 \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right.
\end{aligned}$$





$$\begin{aligned}
& \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2] - \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \right. \\
& \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \Big) - \\
& \left(5 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{3}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \text{AppellF1}\left[\frac{5}{2}, \right. \right. \right. \\
& \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]\right] \right) \Big) / \left( \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(-15 \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \right. \\
& \left. \left. \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \left(3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, \right. \right. \right. \right. \\
& \left. \left. 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \right. \right. \right. \\
& \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) + \\
& \left(5 \text{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \left(2 \left(3 \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \right. \\
& \left. \left. \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 15 \left(-\frac{3}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \right. \right. \right. \right. \\
& \left. \left. \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{1}{5} \text{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) + \\
& 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{5}{7} \text{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
& \left. \frac{20}{21} \text{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{10}{7} \text{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \right. \right. \right. \\
& \left. \left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \text{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big) /
\end{aligned}$$

$$\begin{aligned}
& \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \right. \\
& \quad \left. \left. - \tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \Bigg) + \\
& \frac{1}{3 \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3}} 2^{1/3} \cos[c+dx] \tan\left[\frac{1}{2}(c+dx)\right] \\
& \left( \left( 9(2A-B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) / \right. \\
& \quad \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right. \\
& \quad \left( -9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \right. \\
& \quad \left( 3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - \operatorname{AppellF1}\left[\frac{3}{2}, \right. \right. \\
& \quad \left. \left. \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) + \\
& B \left( -3 - \left( 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right. \right. \\
& \quad \left. \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) / \left( \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \left( -15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] + 2 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] - \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \Bigg) \Bigg) \\
& \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \quad \left. \sec[c+dx] \tan[c+dx] \right) \Bigg) \Bigg)
\end{aligned}$$

**Problem 274: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c+dx]}{(a + a \sec[c+dx])^{2/3}} dx$$

Optimal (type 6, 764 leaves, 11 steps):

$$\begin{aligned}
& \frac{3 B \tan [c+d x]}{d (a+a \sec [c+d x])^{2/3}} - \\
& \left( 3 \sqrt{2} \operatorname{AppellF1}\left[-\frac{1}{6}, \frac{1}{2}, 1, \frac{5}{6}, \frac{1}{2} (1+\sec [c+d x]), 1+\sec [c+d x]\right] \tan [c+d x] \right) / \\
& \left( d \sqrt{1-\sec [c+d x]} (a+a \sec [c+d x])^{2/3} \right) + \\
& \frac{3 (1+\sqrt{3}) B (1+\sec [c+d x])^{1/3} \tan [c+d x]}{d (a+a \sec [c+d x])^{2/3} \left( 2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3} \right)} - \\
& \left( 3 \times 2^{1/3} \times 3^{1/4} B \operatorname{EllipticE}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1-\sqrt{3}) (1+\sec [c+d x])^{1/3}}{2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3}}\right], \frac{1}{4} (2+\sqrt{3})\right] \right. \\
& \quad \left. (1+\sec [c+d x])^{1/3} \left( 2^{1/3} - (1+\sec [c+d x])^{1/3} \right) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1+\sec [c+d x])^{1/3} + (1+\sec [c+d x])^{2/3}}{(2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3})^2}} \tan [c+d x] \right) / \left( d (1-\sec [c+d x]) \right. \\
& \quad \left. (a+a \sec [c+d x])^{2/3} \sqrt{-\frac{(1+\sec [c+d x])^{1/3} \left( 2^{1/3} - (1+\sec [c+d x])^{1/3} \right)}{(2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3})^2}} \right) - \\
& \left( 3^{3/4} (1-\sqrt{3}) B \operatorname{EllipticF}\left[\operatorname{ArcCos}\left[\frac{2^{1/3} - (1-\sqrt{3}) (1+\sec [c+d x])^{1/3}}{2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3}}\right], \frac{1}{4} (2+\sqrt{3})\right] \right. \\
& \quad \left. (1+\sec [c+d x])^{1/3} \left( 2^{1/3} - (1+\sec [c+d x])^{1/3} \right) \right. \\
& \quad \left. \sqrt{\frac{2^{2/3} + 2^{1/3} (1+\sec [c+d x])^{1/3} + (1+\sec [c+d x])^{2/3}}{(2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3})^2}} \tan [c+d x] \right) / \left( 2^{2/3} d \right. \\
& \quad \left. (1-\sec [c+d x]) (a+a \sec [c+d x])^{2/3} \sqrt{-\frac{(1+\sec [c+d x])^{1/3} \left( 2^{1/3} - (1+\sec [c+d x])^{1/3} \right)}{(2^{1/3} - (1+\sqrt{3}) (1+\sec [c+d x])^{1/3})^2}} \right)
\end{aligned}$$

Result (type 6, 5254 leaves):

$$\begin{aligned}
& \left( \cos [c+d x] \left( (1+\cos [c+d x]) \sec [c+d x] \right)^{1/3} (1+\sec [c+d x])^{2/3} (A+B \sec [c+d x]) \right. \\
& \quad \left( 3 \sec \left[ \frac{1}{2} (c+d x) \right] \left( -A \sin \left[ \frac{1}{2} (c+d x) \right] + B \sin \left[ \frac{1}{2} (c+d x) \right] \right) - 3 (-A+B) \sin [c+d x] \right) / \\
& \quad \left( d (B+A \cos [c+d x]) (a (1+\sec [c+d x]))^{2/3} \right) - \\
& \left( 2^{1/3} \cos [c+d x] (1+\sec [c+d x])^{2/3} (A+B \sec [c+d x]) \left( 2 A (1+\sec [c+d x])^{1/3} - \right. \right. \\
& \quad \left. \left. B (1+\sec [c+d x])^{1/3} + \cos [c+d x] \left( -3 A (1+\sec [c+d x])^{1/3} + 3 B (1+\sec [c+d x])^{1/3} \right) \right) \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+d x) \right] \left( \left( 9 (A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+d x) \right]^2, -\tan \left[ \frac{1}{2} (c+d x) \right]^2\right] \right) \right) / \right.
\end{aligned}$$

$$\begin{aligned}
& \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad \left. \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& \left( (A-B) \left( 6 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
& \quad \left. \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( -9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg) / \\
& \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \right. \right. \\
& \quad \left. \left. \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) \Bigg) / \\
& \left( d (B + A \cos[c+dx]) \left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3} (a (1 + \sec[c+dx]))^{2/3} \right. \\
& \quad \left. (-1 + \tan\left[\frac{1}{2}(c+dx)\right]^4) \right) \\
& \left( \frac{1}{\left( \cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx] \right)^{2/3} (-1 + \tan\left[\frac{1}{2}(c+dx)\right]^4)^2} \right. \\
& \quad 2 \times 2^{1/3} \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^4 \\
& \quad \left( \left( 9 (A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) / \right. \\
& \quad \left( 9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\
& \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \Bigg) + \\
& \quad \left( (A-B) \left( 6 \left( 3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right. \right. \\
& \quad \left. \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \left( -9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \Bigg) /
\end{aligned}$$

$$\begin{aligned}
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) - \\
& \left( 1 / \left( 2^{2/3} \left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^4 \right) \right) \right) \\
& \sec \left[ \frac{1}{2} (c+dx) \right]^2 \\
& \left( \left( 9 (A+B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) / \right. \\
& \quad \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) + \\
& \quad (A-B) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \\
& \quad \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
& \quad \cos [c+dx] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \right. \\
& \quad \quad \left. \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \left. \right) \left. \right) / \\
& \left( 15 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) - \\
& \frac{1}{\left( \cos \left[ \frac{1}{2} (c+dx) \right]^2 \sec [c+dx] \right)^{2/3} \left( -1 + \tan \left[ \frac{1}{2} (c+dx) \right]^4 \right)} 2^{1/3} \tan \left[ \frac{1}{2} (c+dx) \right] \\
& \left( \left( 9 (A+B) \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \right. \right. \\
& \quad \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \right. \\
& \quad \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \left. \right) \left. \right) / \\
& \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \\
& \quad 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left. \right) -
\end{aligned}$$

$$\begin{aligned}
& \left( 9 (A+B) \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left( 2 \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 9 \left( -\frac{1}{3} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + \right. \\
& \quad \left. \frac{1}{9} \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) + 2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{4}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{7}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] - 3 \left( -\frac{6}{5} \operatorname{AppellF1} \left[ \right. \right. \right. \\
& \quad \left. \left. \frac{5}{2}, \frac{1}{3}, 3, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \right. \\
& \quad \left. \tan \left[ \frac{1}{2} (c+dx) \right] + \frac{1}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, \right. \right. \\
& \quad \left. \left. -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] \right) \right) \Big/ \\
& \quad \left( 9 \operatorname{AppellF1} \left[ \frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + 2 \right. \\
& \quad \left( -3 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \operatorname{AppellF1} \left[ \right. \right. \\
& \quad \left. \left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (c+dx) \right]^2 \Big)^2 - \\
& \quad \left( (A-B) \left( 6 \left( 3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] - \right. \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
& \quad \left. \cos [c+dx] \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right]^2 + 5 \operatorname{AppellF1} \left[ \frac{3}{2}, \frac{1}{3}, \right. \right. \\
& \quad \left. \left. 1, \frac{5}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \left( -9 + 8 \tan \left[ \frac{1}{2} (c+dx) \right]^2 \right) \right) \right. \\
& \quad \left( 2 \left( -3 \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] + \right. \right. \\
& \quad \left. \left. \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan \left[ \frac{1}{2} (c+dx) \right]^2, -\tan \left[ \frac{1}{2} (c+dx) \right]^2 \right] \right) \right. \\
& \quad \left. \sec \left[ \frac{1}{2} (c+dx) \right]^2 \tan \left[ \frac{1}{2} (c+dx) \right] + 15 \left( -\frac{3}{5} \operatorname{AppellF1} \left[ \frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\
& \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(-\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \tan\left[\frac{1}{2}(c+dx)\right] + \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\
& \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - 3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) \Bigg/ \\
& \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + 2 \right. \\
& \left. \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2 + \\
& (A-B) \left(40 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right. \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 6 \right. \\
& \left. \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
& \left. \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^4 \tan\left[\frac{1}{2}(c+dx)\right] - 6 \right. \\
& \left. \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \right. \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \sin[c+dx] \tan\left[\frac{1}{2}(c+dx)\right]^2 + 6 \right. \\
& \left. \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \cos[c+dx] \right. \\
& \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + 5 \left(-\frac{3}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \right. \right. \right.
\end{aligned}$$

$$\frac{\begin{aligned} & \tan\left[\frac{1}{2}(c+dx)\right]^2 - \tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + \\ & \frac{1}{5} \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\ & \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(-9 + 8 \tan\left[\frac{1}{2}(c+dx)\right]^2\right) + 6 \\ & \cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 \left(\frac{5}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \right. \right. \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] - \\ & \quad \frac{20}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{7}{3}, 1, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \\ & \quad \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + 3 \left(-\frac{10}{7} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1}{3}, 3, \right. \right. \\ & \quad \left.\left. \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \\ & \quad \tan\left[\frac{1}{2}(c+dx)\right] + \frac{5}{21} \operatorname{AppellF1}\left[\frac{7}{2}, \frac{4}{3}, 2, \frac{9}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, \right. \\ & \quad \left.\left. -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]\right)\right) \Bigg] \Bigg/ \\ & \left(15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ & \quad 2 \left(-3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\right. \right. \\ & \quad \left.\left. \frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \Bigg] + \\ & \quad 1 \end{aligned}}{3 \left(\cos\left[\frac{1}{2}(c+dx)\right]^2 \sec[c+dx]\right)^{5/3} \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^4\right)} \cdot \frac{2^{\times} 2^{1/3} \tan\left[\frac{1}{2}(c+dx)\right]}{\left(\left(9(A+B) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right]\right) \Bigg/ \right. \\ \left(9 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{1}{3}, 1, \frac{3}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ \left. 2 \left(-3 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 2, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\right. \right. \right. \\ \left.\left.\left. \frac{3}{2}, \frac{4}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) + \right. \\ \left.(A-B) \left(6 \left(3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] - \right. \right. \right. \\ \left.\left.\left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \right) \right. \\ \left.\cos[c+dx] \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^2 + 5 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1,$$



$$\begin{aligned} & \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2 \right] \left(-9+8 \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \right) \right) / \\ & \left( 15 \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1}{3}, 1, \frac{5}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \right. \\ & \quad 2 \left( -3 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1}{3}, 2, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] + \operatorname{AppellF1}\left[\frac{5}{2}, \frac{4}{3}, 1, \frac{7}{2}, \tan\left[\frac{1}{2}(c+dx)\right]^2, -\tan\left[\frac{1}{2}(c+dx)\right]^2\right] \right) \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \\ & \left. \left. \left. \left( -\cos\left[\frac{1}{2}(c+dx)\right] \sec[c+dx] \sin\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{1}{2}(c+dx)\right]^2 \right. \right. \right. \right. \\ & \quad \left. \left. \left. \sec[c+dx] \tan[c+dx] \right) \right) \right) \right) \end{aligned}$$

### Problem 275: Result more than twice size of optimal antiderivative.

$$\int (c \sec[e+fx])^n (a+a \sec[e+fx])^m (A+B \sec[e+fx]) dx$$

Optimal (type 6, 197 leaves, 7 steps):

$$\begin{aligned} & - \left( \left( B \operatorname{AppellF1}\left[n, \frac{1}{2}, -\frac{1}{2}-m, 1+n, \sec[e+fx], -\sec[e+fx]\right] (c \sec[e+fx])^n \right. \right. \\ & \quad \left. \left. (1+\sec[e+fx])^{-\frac{1}{2}-m} (a+a \sec[e+fx])^m \tan[e+fx] \right) / (fn \sqrt{1-\sec[e+fx]}) \right) - \\ & \left( (A-B) \operatorname{AppellF1}\left[n, \frac{1}{2}, \frac{1}{2}-m, 1+n, \sec[e+fx], -\sec[e+fx]\right] (c \sec[e+fx])^n \right. \\ & \quad \left. (1+\sec[e+fx])^{-\frac{1}{2}-m} (a+a \sec[e+fx])^m \tan[e+fx] \right) / (fn \sqrt{1-\sec[e+fx]}) \end{aligned}$$

Result (type 6, 4897 leaves):

$$\begin{aligned} & \left( 2^{1+m} \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^n \sec[e+fx]^{-1-n} (c \sec[e+fx])^n \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{m+n} \right. \\ & \quad \left. (1+\sec[e+fx])^{-m} (a(1+\sec[e+fx]))^m (A+B \sec[e+fx]) \right. \\ & \quad \left. (A \sec[e+fx]^n (1+\sec[e+fx])^m + B \sec[e+fx]^{1+n} (1+\sec[e+fx])^m) \tan\left[\frac{1}{2}(e+fx)\right] \right. \\ & \quad \left. \left( - \left( \left( 3 A \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right) / \right. \right. \right. \right. \\ & \quad \left( 3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\ & \quad \left. 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \right. \\ & \quad \left. \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \\ & \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right) \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) - \right. \\ & \quad \left. \left( B \operatorname{AppellF1}\left[\frac{1}{2}, 1+m+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) / \right. \end{aligned}$$

$$\begin{aligned}
& \left( \text{AppellF1}\left[\frac{1}{2}, 1+m+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \frac{2}{3} \left( n \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \quad \quad \left. (1+m+n) \text{AppellF1}\left[\frac{3}{2}, 2+m+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \right) \\
& \quad \left. \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) / \left( f (B + A \cos[e+fx]) \left( -1 + \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right. \\
& \quad \left( -\frac{1}{(-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2)^2} 2^{1+m} \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{m+n} \right. \\
& \quad \tan\left[\frac{1}{2}(e+fx)\right]^2 \left( -\left( \left( 3A \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \right. \right. \right. \\
& \quad \quad \left. \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \cos[e+fx] \right) / \left( 3 \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \right. \right. \right. \right. \\
& \quad \quad \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \right. \right. \\
& \quad \quad \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + (m+n) \text{AppellF1}\left[\frac{3}{2}, 1+m+n, \right. \\
& \quad \quad \left. 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) - \\
& \quad \left( B \text{AppellF1}\left[\frac{1}{2}, 1+m+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \right) / \\
& \quad \left( \text{AppellF1}\left[\frac{1}{2}, 1+m+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
& \quad \frac{2}{3} \left( n \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
& \quad \quad \left. (1+m+n) \text{AppellF1}\left[\frac{3}{2}, 2+m+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) + \\
& \quad \frac{1}{-1 + \tan\left[\frac{1}{2}(e+fx)\right]^2} 2^m \left( \sec\left[\frac{1}{2}(e+fx)\right]^2 \right)^{1+n} \left( \cos\left[\frac{1}{2}(e+fx)\right]^2 \sec[e+fx] \right)^{m+n} \\
& \quad \left( -\left( \left( 3A \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \cos[e+ \right. \right. \right. \\
& \quad \quad \left. \left. \left. fx \right] \right) / \left( 3 \text{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \right. \right. \\
& \quad \quad 2 \left( (-1+n) \text{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] + \right. \\
& \quad \quad \left. (m+n) \text{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{2}(e+fx)\right]^2 \right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) \right) -
\end{aligned}$$



$$\begin{aligned}
& (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \\
& \tan\left[\frac{1}{2}(e+fx)\right]^2 - \left(3A \cos[e+fx] \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right.\right. \\
& \left.\frac{1}{3}(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) \Bigg) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& 2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right.\right. \\
& \left.\tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 - \\
& \left. \left(B \left(\frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m+n, -n, \frac{5}{2}, \right.\right.\right.\right. \\
& \left.\tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) \Bigg) / \\
& \left( \operatorname{AppellF1}\left[\frac{1}{2}, 1+m+n, -n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \frac{2}{3} \left( n \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right. \\
& \left. (1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m+n, -n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \tan\left[\frac{1}{2}(e+fx)\right]^2 \right) + \\
& \left. \left(3A \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \cos[e+fx] \right.\right. \\
& \left. \left(2 \left( (-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] + \right.\right.\right. \\
& \left. (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \right. \\
& \left. \left. 3 \left(-\frac{1}{3}(1-n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right] + \frac{1}{3}(m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \right.\right.\right.\right. \\
& \left.\tan\left[\frac{1}{2}(e+fx)\right]^2, -\tan\left[\frac{1}{2}(e+fx)\right]^2\right] \sec\left[\frac{1}{2}(e+fx)\right]^2 \tan\left[\frac{1}{2}(e+fx)\right]\right) \Bigg) +
\end{aligned}$$

$$\begin{aligned} & 2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\left((-1+n)\left(-\frac{3}{5}(2-n) \operatorname{AppellF1}\left[\frac{5}{2}, m+n, 3-n, \frac{7}{2},\right.\right.\right. \\ & \quad \left.\left.\left.\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+\right.\right.\right. \\ & \quad \left.\left.f x)\right]+\frac{3}{5}(m+n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,\right.\right. \\ & \quad \left.-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\Bigg)+ \\ & (m+n)\left(-\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,\right.\right. \\ & \quad \left.-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+ \\ & \quad \frac{3}{5}(1+m+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,\right. \\ & \quad \left.-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\Bigg)\Bigg)/ \\ & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, m+n, 1-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \\ & \quad 2\left((-1+n) \operatorname{AppellF1}\left[\frac{3}{2}, m+n, 2-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right. \\ & \quad (m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,\right. \\ & \quad \left.-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]) \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2)^2+ \\ & \left.(B \operatorname{AppellF1}\left[\frac{1}{2}, 1+m+n,-n, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \\ & \quad \left.\left(\frac{1}{3} n \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \right. \right. \\ & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+\frac{1}{3}(1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m+n,-n, \frac{5}{2},\right.\right.\right. \\ & \quad \left.\left.\left.\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+ \right.\right. \\ & \quad \left.\frac{2}{3}\left(n \operatorname{AppellF1}\left[\frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]+ \right.\right. \\ & \quad \left.\left.(1+m+n) \operatorname{AppellF1}\left[\frac{3}{2}, 2+m+n,-n, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,\right.\right.\right. \\ & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right]) \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+ \right. \\ & \quad \left.\frac{2}{3} \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\left(n\left(-\frac{3}{5}(1-n) \operatorname{AppellF1}\left[\frac{5}{2}, 1+m+n, 2-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+\right.\right.\right.\right. \right. \\ & \quad \left.\left.\left.f x)\right]^2,-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]+ \right. \\ & \quad \left.\frac{3}{5}(1+m+n) \operatorname{AppellF1}\left[\frac{5}{2}, 2+m+n, 1-n, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2,\right.\right. \\ & \quad \left.-\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\Bigg)+ \end{aligned}$$

$$\begin{aligned}
 & (1+m+n) \left( \frac{3}{5} n \operatorname{AppellF1} \left[ \frac{5}{2}, 2+m+n, 1-n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] + \right. \\
 & \quad \left. \frac{3}{5} (2+m+n) \operatorname{AppellF1} \left[ \frac{5}{2}, 3+m+n, -n, \frac{7}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \tan \left[ \frac{1}{2} (e+fx) \right] \right) \right) \Bigg/ \\
 & \left( \operatorname{AppellF1} \left[ \frac{1}{2}, 1+m+n, -n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \frac{2}{3} \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \left. (1+m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m+n, -n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) + \\
 & \frac{1}{-1 + \tan \left[ \frac{1}{2} (e+fx) \right]^2} 2^{1+m} (m+n) \left( \operatorname{Sec} \left[ \frac{1}{2} (e+fx) \right]^2 \right)^n \\
 & \left( \cos \left[ \frac{1}{2} (e+fx) \right]^2 \operatorname{Sec} [e+fx] \right)^{-1+m+n} \\
 & \tan \left[ \frac{1}{2} (e+fx) \right] \\
 & \left( - \left( \left( 3 A \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \cos [e+ \right. \right. \right. \\
 & \quad \left. \left. \left. fx \right] \right) \Bigg/ \left( 3 \operatorname{AppellF1} \left[ \frac{1}{2}, m+n, 1-n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left( (-1+n) \operatorname{AppellF1} \left[ \frac{3}{2}, m+n, 2-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \right. \\
 & \quad \left. (m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) - \\
 & \left( B \operatorname{AppellF1} \left[ \frac{1}{2}, 1+m+n, -n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \Bigg/ \\
 & \left( \operatorname{AppellF1} \left[ \frac{1}{2}, 1+m+n, -n, \frac{3}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \frac{2}{3} \left( n \operatorname{AppellF1} \left[ \frac{3}{2}, 1+m+n, 1-n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] + \right. \\
 & \quad \left. (1+m+n) \operatorname{AppellF1} \left[ \frac{3}{2}, 2+m+n, -n, \frac{5}{2}, \tan \left[ \frac{1}{2} (e+fx) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[ \frac{1}{2} (e+fx) \right]^2 \right] \right) \tan \left[ \frac{1}{2} (e+fx) \right]^2 \right) \\
 & \left( -\cos \left[ \frac{1}{2} (e+fx) \right] \operatorname{Sec} [e+fx] \sin \left[ \frac{1}{2} (e+fx) \right] + \cos \left[ \frac{1}{2} (e+fx) \right]^2 \right)
 \end{aligned}$$



$$\frac{1}{4d} \left( -2(2aA + bB) \operatorname{Log} \left[ \cos \left[ \frac{1}{2}(c + dx) \right] - \sin \left[ \frac{1}{2}(c + dx) \right] \right] + \right. \\
4aA \operatorname{Log} \left[ \cos \left[ \frac{1}{2}(c + dx) \right] + \sin \left[ \frac{1}{2}(c + dx) \right] \right] + \\
2bB \operatorname{Log} \left[ \cos \left[ \frac{1}{2}(c + dx) \right] + \sin \left[ \frac{1}{2}(c + dx) \right] \right] + \frac{bB}{\left( \cos \left[ \frac{1}{2}(c + dx) \right] - \sin \left[ \frac{1}{2}(c + dx) \right] \right)^2} - \\
\left. \frac{bB}{\left( \cos \left[ \frac{1}{2}(c + dx) \right] + \sin \left[ \frac{1}{2}(c + dx) \right] \right)^2} + 4(Ab + aB) \tan[c + dx] \right)$$

**Problem 280: Result more than twice size of optimal antiderivative.**

$$\int (a + b \sec[c + dx]) (A + B \sec[c + dx]) dx$$

Optimal (type 3, 35 leaves, 4 steps):

$$aAx + \frac{(Ab + aB) \operatorname{ArcTanh}[\sin[c + dx]]}{d} + \frac{bB \tan[c + dx]}{d}$$

Result (type 3, 159 leaves):

$$aAx - \frac{Ab \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} - \frac{aB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \\
\frac{Ab \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \frac{aB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \frac{bB \tan[c + dx]}{d}$$

**Problem 281: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + dx] (a + b \sec[c + dx]) (A + B \sec[c + dx]) dx$$

Optimal (type 3, 35 leaves, 3 steps):

$$(Ab + aB)x + \frac{bB \operatorname{ArcTanh}[\sin[c + dx]]}{d} + \frac{aA \sin[c + dx]}{d}$$

Result (type 3, 104 leaves):

$$Abx + aBx - \frac{bB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] - \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \\
\frac{bB \operatorname{Log} \left[ \cos \left[ \frac{c}{2} + \frac{dx}{2} \right] + \sin \left[ \frac{c}{2} + \frac{dx}{2} \right] \right]}{d} + \frac{aA \cos[dx] \sin[c]}{d} + \frac{aA \cos[c] \sin[dx]}{d}$$

**Problem 286: Result more than twice size of optimal antiderivative.**

$$\int \sec[c + dx]^2 (a + b \sec[c + dx])^2 (A + B \sec[c + dx]) dx$$



Optimal (type 3, 179 leaves, 7 steps):

$$\frac{(8 a A b + 4 a^2 B + 3 b^2 B) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \frac{(4 a^2 A b + 4 A b^3 - a^3 B + 8 a b^2 B) \operatorname{Tan}[c + d x]}{6 b d} + \frac{(8 a A b - 2 a^2 B + 9 b^2 B) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{24 d} + \frac{(4 A b - a B) (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{12 b d} + \frac{B (a + b \operatorname{Sec}[c + d x])^3 \operatorname{Tan}[c + d x]}{4 b d}$$

Result (type 3, 457 leaves):

$$\frac{1}{48 d} \left( -6 (8 a A b + 4 a^2 B + 3 b^2 B) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] + 6 (8 a A b + 4 a^2 B + 3 b^2 B) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right] + \frac{3 b^2 B}{\left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^4} + \frac{12 a^2 B + 8 a b (3 A + B) + b^2 (4 A + 9 B)}{\left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^2} + \frac{8 b (A b + 2 a B) \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]}{\left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^3} + \frac{16 (3 a^2 A + 2 A b^2 + 4 a b B) \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]}{\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]} - \frac{3 b^2 B}{\left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^4} + \frac{8 b (A b + 2 a B) \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]}{\left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^3} - \frac{12 a^2 B + 8 a b (3 A + B) + b^2 (4 A + 9 B)}{\left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]\right)^2} + \frac{16 (3 a^2 A + 2 A b^2 + 4 a b B) \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]}{\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right]} \right)$$

**Problem 287: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c + d x] (a + b \operatorname{Sec}[c + d x])^2 (A + B \operatorname{Sec}[c + d x]) dx$$

Optimal (type 3, 116 leaves, 6 steps):

$$\frac{(2 a^2 A + A b^2 + 2 a b B) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{2 d} + \frac{2 (3 a A b + a^2 B + b^2 B) \operatorname{Tan}[c + d x]}{3 d} + \frac{b (3 A b + 2 a B) \operatorname{Sec}[c + d x] \operatorname{Tan}[c + d x]}{6 d} + \frac{B (a + b \operatorname{Sec}[c + d x])^2 \operatorname{Tan}[c + d x]}{3 d}$$

Result (type 3, 239 leaves):

$$\begin{aligned} & \frac{1}{6d} \operatorname{Sec}[c+dx]^3 \left( -\frac{9}{4} (2a^2A + Ab^2 + 2abB) \operatorname{Cos}[c+dx] \right. \\ & \quad \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) - \\ & \quad \frac{3}{4} (2a^2A + Ab^2 + 2abB) \operatorname{Cos}[3(c+dx)] \\ & \quad \left( \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \\ & \quad (6aAb + 3a^2B + 4b^2B + 3b(Ab + 2aB) \operatorname{Cos}[c+dx] + (6aAb + 3a^2B + 2b^2B) \operatorname{Cos}[2(c+dx)]) \\ & \quad \left. \operatorname{Sin}[c+dx] \right) \end{aligned}$$

**Problem 288: Result more than twice size of optimal antiderivative.**

$$\int (a + b \operatorname{Sec}[c+dx])^2 (A + B \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 86 leaves, 5 steps):

$$\begin{aligned} & a^2Ax + \frac{(4aAb + 2a^2B + b^2B) \operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2d} + \\ & \frac{b(2Ab + 3aB) \operatorname{Tan}[c+dx]}{2d} + \frac{bB(a + b \operatorname{Sec}[c+dx]) \operatorname{Tan}[c+dx]}{2d} \end{aligned}$$

Result (type 3, 345 leaves):

$$\begin{aligned} & \frac{1}{4d} \operatorname{Sec}[c+dx]^2 \left( 2a^2Ac + 2a^2Adx - 4aAb \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - \right. \\ & \quad 2a^2B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] - b^2B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & \quad 4aAb \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & \quad 2a^2B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \\ & \quad b^2B \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \operatorname{Cos}[2(c+dx)] \\ & \quad \left( 2a^2A(c+dx) - (4aAb + 2a^2B + b^2B) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] + \right. \\ & \quad \left. (4aAb + 2a^2B + b^2B) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] \right) + \\ & \quad \left. 2b^2B \operatorname{Sin}[c+dx] + 2Ab^2 \operatorname{Sin}[2(c+dx)] + 4abB \operatorname{Sin}[2(c+dx)] \right) \end{aligned}$$

**Problem 295: Result more than twice size of optimal antiderivative.**

$$\int \operatorname{Sec}[c+dx] (a + b \operatorname{Sec}[c+dx])^3 (A + B \operatorname{Sec}[c+dx]) dx$$

Optimal (type 3, 180 leaves, 7 steps):

$$\begin{aligned}
& \frac{(8 a^3 A + 12 a A b^2 + 12 a^2 b B + 3 b^3 B) \operatorname{ArcTanh}[\sin[c + d x]]}{8 d} + \\
& \frac{(16 a^2 A b + 4 A b^3 + 3 a^3 B + 12 a b^2 B) \tan[c + d x]}{6 d} + \\
& \frac{b (20 a A b + 6 a^2 B + 9 b^2 B) \sec[c + d x] \tan[c + d x]}{24 d} + \\
& \frac{(4 A b + 3 a B) (a + b \sec[c + d x])^2 \tan[c + d x]}{12 d} + \frac{B (a + b \sec[c + d x])^3 \tan[c + d x]}{4 d}
\end{aligned}$$

Result(type 3, 1179 leaves):

$$\begin{aligned}
& \left( (-8 a^3 A - 12 a A b^2 - 12 a^2 b B - 3 b^3 B) \cos[c + d x]^4 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right] \right. \\
& \quad \left. (a + b \sec[c + d x])^3 (A + B \sec[c + d x]) \right) / \left( 8 d (b + a \cos[c + d x])^3 (B + A \cos[c + d x]) \right) + \\
& \left( (8 a^3 A + 12 a A b^2 + 12 a^2 b B + 3 b^3 B) \cos[c + d x]^4 \log\left[\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right] \right. \\
& \quad \left. (a + b \sec[c + d x])^3 (A + B \sec[c + d x]) \right) / \left( 8 d (b + a \cos[c + d x])^3 (B + A \cos[c + d x]) \right) + \\
& \left( b^3 B \cos[c + d x]^4 (a + b \sec[c + d x])^3 (A + B \sec[c + d x]) \right) / \\
& \left( 16 d (b + a \cos[c + d x])^3 (B + A \cos[c + d x]) \left( \cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 \right) + \\
& \left( (36 a A b^2 + 4 A b^3 + 36 a^2 b B + 12 a b^2 B + 9 b^3 B) \cos[c + d x]^4 \right. \\
& \quad \left. (a + b \sec[c + d x])^3 (A + B \sec[c + d x]) \right) / \\
& \left( 48 d (b + a \cos[c + d x])^3 (B + A \cos[c + d x]) \left( \cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) - \\
& \left( b^3 B \cos[c + d x]^4 (a + b \sec[c + d x])^3 (A + B \sec[c + d x]) \right) / \\
& \left( 16 d (b + a \cos[c + d x])^3 (B + A \cos[c + d x]) \left( \cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 \right) + \\
& \left( (-36 a A b^2 - 4 A b^3 - 36 a^2 b B - 12 a b^2 B - 9 b^3 B) \right. \\
& \quad \left. \cos[c + d x]^4 (a + b \sec[c + d x])^3 (A + B \sec[c + d x]) \right) / \\
& \left( 48 d (b + a \cos[c + d x])^3 (B + A \cos[c + d x]) \left( \cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^2 \right) + \\
& \left( \cos[c + d x]^4 (a + b \sec[c + d x])^3 (A + B \sec[c + d x]) \right. \\
& \quad \left. \left( A b^3 \sin\left[\frac{1}{2}(c + d x)\right] + 3 a b^2 B \sin\left[\frac{1}{2}(c + d x)\right] \right) \right) / \\
& \left( 6 d (b + a \cos[c + d x])^3 (B + A \cos[c + d x]) \left( \cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right] \right)^3 \right) + \\
& \left( \cos[c + d x]^4 (a + b \sec[c + d x])^3 (A + B \sec[c + d x]) \right. \\
& \quad \left. \left( A b^3 \sin\left[\frac{1}{2}(c + d x)\right] + 3 a b^2 B \sin\left[\frac{1}{2}(c + d x)\right] \right) \right) /
\end{aligned}$$

$$\begin{aligned}
& \left( 6 d (b + a \cos [c + d x])^3 (B + A \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
& \left( \cos [c + d x]^4 (a + b \sec [c + d x])^3 (A + B \sec [c + d x]) \left( 9 a^2 A b \sin \left[ \frac{1}{2} (c + d x) \right] + \right. \right. \\
& \quad \left. \left. 2 A b^3 \sin \left[ \frac{1}{2} (c + d x) \right] + 3 a^3 B \sin \left[ \frac{1}{2} (c + d x) \right] + 6 a b^2 B \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 3 d (b + a \cos [c + d x])^3 (B + A \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( \cos [c + d x]^4 (a + b \sec [c + d x])^3 (A + B \sec [c + d x]) \left( 9 a^2 A b \sin \left[ \frac{1}{2} (c + d x) \right] + \right. \right. \\
& \quad \left. \left. 2 A b^3 \sin \left[ \frac{1}{2} (c + d x) \right] + 3 a^3 B \sin \left[ \frac{1}{2} (c + d x) \right] + 6 a b^2 B \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 3 d (b + a \cos [c + d x])^3 (B + A \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right)
\end{aligned}$$

**Problem 296: Result more than twice size of optimal antiderivative.**

$$\int (a + b \sec [c + d x])^3 (A + B \sec [c + d x]) dx$$

Optimal (type 3, 137 leaves, 6 steps):

$$\begin{aligned}
& a^3 A x + \frac{(6 a^2 A b + A b^3 + 2 a^3 B + 3 a b^2 B) \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} + \\
& \frac{b (9 a A b + 8 a^2 B + 2 b^2 B) \tan [c + d x]}{3 d} + \\
& \frac{b^2 (3 A b + 5 a B) \sec [c + d x] \tan [c + d x]}{6 d} + \frac{b B (a + b \sec [c + d x])^2 \tan [c + d x]}{3 d}
\end{aligned}$$

Result (type 3, 968 leaves):

$$\begin{aligned}
& \frac{a^3 A (c+d x) \cos [c+d x]^4 (a+b \sec [c+d x])^3 (A+B \sec [c+d x])}{d (b+a \cos [c+d x])^3 (B+A \cos [c+d x])} + \\
& \left( (-6 a^2 A b - A b^3 - 2 a^3 B - 3 a b^2 B) \cos [c+d x]^4 \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right. \\
& \quad \left. (a+b \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \left( 2 d (b+a \cos [c+d x])^3 (B+A \cos [c+d x]) \right) + \\
& \left( (6 a^2 A b + A b^3 + 2 a^3 B + 3 a b^2 B) \cos [c+d x]^4 \log \left[ \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right] \right. \\
& \quad \left. (a+b \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \left( 2 d (b+a \cos [c+d x])^3 (B+A \cos [c+d x]) \right) + \\
& \left( (3 A b^3 + 9 a b^2 B + b^3 B) \cos [c+d x]^4 (a+b \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \\
& \left( 12 d (b+a \cos [c+d x])^3 (B+A \cos [c+d x]) \left( \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right) + \\
& \left( b^3 B \cos [c+d x]^4 (a+b \sec [c+d x])^3 (A+B \sec [c+d x]) \sin \left[ \frac{1}{2} (c+d x) \right] \right) / \\
& \left( 6 d (b+a \cos [c+d x])^3 (B+A \cos [c+d x]) \left( \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right)^3 \right) + \\
& \left( b^3 B \cos [c+d x]^4 (a+b \sec [c+d x])^3 (A+B \sec [c+d x]) \sin \left[ \frac{1}{2} (c+d x) \right] \right) / \\
& \left( 6 d (b+a \cos [c+d x])^3 (B+A \cos [c+d x]) \left( \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right)^3 \right) + \\
& \left( (-3 A b^3 - 9 a b^2 B - b^3 B) \cos [c+d x]^4 (a+b \sec [c+d x])^3 (A+B \sec [c+d x]) \right) / \\
& \left( 12 d (b+a \cos [c+d x])^3 (B+A \cos [c+d x]) \left( \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right)^2 \right) + \\
& \cos [c+d x]^4 (a+b \sec [c+d x])^3 (A+B \sec [c+d x]) \\
& \quad \left( 9 a A b^2 \sin \left[ \frac{1}{2} (c+d x) \right] + 9 a^2 b B \sin \left[ \frac{1}{2} (c+d x) \right] + 2 b^3 B \sin \left[ \frac{1}{2} (c+d x) \right] \right) / \\
& \left( 3 d (b+a \cos [c+d x])^3 (B+A \cos [c+d x]) \left( \cos \left[ \frac{1}{2} (c+d x) \right] - \sin \left[ \frac{1}{2} (c+d x) \right] \right) \right) + \\
& \cos [c+d x]^4 (a+b \sec [c+d x])^3 (A+B \sec [c+d x]) \\
& \quad \left( 9 a A b^2 \sin \left[ \frac{1}{2} (c+d x) \right] + 9 a^2 b B \sin \left[ \frac{1}{2} (c+d x) \right] + 2 b^3 B \sin \left[ \frac{1}{2} (c+d x) \right] \right) / \\
& \left( 3 d (b+a \cos [c+d x])^3 (B+A \cos [c+d x]) \left( \cos \left[ \frac{1}{2} (c+d x) \right] + \sin \left[ \frac{1}{2} (c+d x) \right] \right) \right)
\end{aligned}$$

**Problem 297: Result more than twice size of optimal antiderivative.**

$$\int \cos [c+d x] (a+b \sec [c+d x])^3 (A+B \sec [c+d x]) dx$$

Optimal (type 3, 119 leaves, 6 steps):

$$a^2 (3 A b + a B) x + \frac{b (6 a A b + 6 a^2 B + b^2 B) \operatorname{ArcTanh}[\sin [c + d x]]}{2 d} +$$

$$\frac{a^2 (2 a A - b B) \sin [c + d x]}{2 d} + \frac{b B (a + b \sec [c + d x])^2 \sin [c + d x]}{2 d} + \frac{b^2 (A b + 2 a B) \tan [c + d x]}{d}$$

Result (type 3, 399 leaves):

$$\frac{1}{4 d} \sec [c + d x]^2$$

$$\left( 6 a^2 A b c + 2 a^3 B c + 6 a^2 A b d x + 2 a^3 B d x - 6 a A b^2 \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] - \right.$$

$$6 a^2 b B \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] -$$

$$b^3 B \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 6 a A b^2$$

$$\log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 6 a^2 b B \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] +$$

$$b^3 B \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + \cos [2 (c + d x)]$$

$$\left( 2 a^2 (3 A b + a B) (c + d x) - b (6 a A b + 6 a^2 B + b^2 B) \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right) +$$

$$b (6 a A b + 6 a^2 B + b^2 B) \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + (a^3 A + 2 b^3 B)$$

$$\sin [c + d x] + 2 A b^3 \sin [2 (c + d x)] + 6 a b^2 B \sin [2 (c + d x)] + a^3 A \sin [3 (c + d x)] \Big)$$

**Problem 304: Result more than twice size of optimal antiderivative.**

$$\int (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) dx$$

Optimal (type 3, 200 leaves, 7 steps):

$$a^4 A x + \frac{1}{8 d} (32 a^3 A b + 16 a A b^3 + 8 a^4 B + 24 a^2 b^2 B + 3 b^4 B) \operatorname{ArcTanh}[\sin [c + d x]] +$$

$$\frac{b (34 a^2 A b + 4 A b^3 + 19 a^3 B + 16 a b^2 B) \tan [c + d x]}{6 d} +$$

$$\frac{b^2 (32 a A b + 26 a^2 B + 9 b^2 B) \sec [c + d x] \tan [c + d x]}{24 d} +$$

$$\frac{b (4 A b + 7 a B) (a + b \sec [c + d x])^2 \tan [c + d x]}{12 d} + \frac{b B (a + b \sec [c + d x])^3 \tan [c + d x]}{4 d}$$

Result (type 3, 455 leaves):

$$\frac{1}{96 d (b + a \cos [c + d x])^4 (B + A \cos [c + d x])} \cos [c + d x] (a + b \sec [c + d x])^4$$

$$(A + B \sec [c + d x]) \left( 36 a^4 A (c + d x) + 48 a^4 A (c + d x) \cos [2 (c + d x)] + \right.$$

$$12 a^4 A (c + d x) \cos [4 (c + d x)] - 12 (32 a^3 A b + 16 a A b^3 + 8 a^4 B + 24 a^2 b^2 B + 3 b^4 B)$$

$$\cos [c + d x]^4 \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] +$$

$$12 (32 a^3 A b + 16 a A b^3 + 8 a^4 B + 24 a^2 b^2 B + 3 b^4 B) \cos [c + d x]^4$$

$$\log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] + 48 a A b^3 \sin [c + d x] + 72 a^2 b^2 B \sin [c + d x] +$$

$$33 b^4 B \sin [c + d x] + 144 a^2 A b^2 \sin [2 (c + d x)] + 32 A b^4 \sin [2 (c + d x)] +$$

$$96 a^3 b B \sin [2 (c + d x)] + 128 a b^3 B \sin [2 (c + d x)] + 48 a A b^3 \sin [3 (c + d x)] +$$

$$72 a^2 b^2 B \sin [3 (c + d x)] + 9 b^4 B \sin [3 (c + d x)] + 72 a^2 A b^2 \sin [4 (c + d x)] +$$

$$8 A b^4 \sin [4 (c + d x)] + 48 a^3 b B \sin [4 (c + d x)] + 32 a b^3 B \sin [4 (c + d x)] \Big)$$

**Problem 305: Result more than twice size of optimal antiderivative.**

$$\int \cos [c + d x] (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) dx$$

Optimal (type 3, 195 leaves, 7 steps):

$$a^3 (4 A b + a B) x + \frac{b (12 a^2 A b + A b^3 + 8 a^3 B + 4 a b^2 B) \operatorname{ArcTanh} [\sin [c + d x]]}{2 d} +$$

$$\frac{a A (a + b \sec [c + d x])^3 \sin [c + d x]}{d} - \frac{b (6 a^3 A - 12 a A b^2 - 17 a^2 b B - 2 b^3 B) \tan [c + d x]}{3 d} -$$

$$\frac{b^2 (6 a^2 A - 3 A b^2 - 8 a b B) \sec [c + d x] \tan [c + d x]}{6 d} - \frac{b (3 a A - b B) (a + b \sec [c + d x])^2 \tan [c + d x]}{3 d}$$

Result (type 3, 1051 leaves):

$$\begin{aligned}
& \left( a^3 (4 A b + a B) (c + d x) \cos [c + d x]^5 (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \right) / \\
& \left( d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \right) + \\
& \left( (-12 a^2 A b^2 - A b^4 - 8 a^3 b B - 4 a b^3 B) \cos [c + d x]^5 \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right. \\
& \quad \left. (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \right) / \left( 2 d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \right) + \\
& \left( (12 a^2 A b^2 + A b^4 + 8 a^3 b B + 4 a b^3 B) \cos [c + d x]^5 \log \left[ \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right] \right. \\
& \quad \left. (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \right) / \left( 2 d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \right) + \\
& \left( (3 A b^4 + 12 a b^3 B + b^4 B) \cos [c + d x]^5 (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \right) / \\
& \left( 12 d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( b^4 B \cos [c + d x]^5 (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \sin \left[ \frac{1}{2} (c + d x) \right] \right) / \\
& \left( 6 d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
& \left( b^4 B \cos [c + d x]^5 (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \sin \left[ \frac{1}{2} (c + d x) \right] \right) / \\
& \left( 6 d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^3 \right) + \\
& \left( (-3 A b^4 - 12 a b^3 B - b^4 B) \cos [c + d x]^5 (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \right) / \\
& \left( 12 d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right)^2 \right) + \\
& \left( 2 \cos [c + d x]^5 (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \right. \\
& \quad \left. \left( 6 a A b^3 \sin \left[ \frac{1}{2} (c + d x) \right] + 9 a^2 b^2 B \sin \left[ \frac{1}{2} (c + d x) \right] + b^4 B \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 3 d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] - \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( 2 \cos [c + d x]^5 (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \right. \\
& \quad \left. \left( 6 a A b^3 \sin \left[ \frac{1}{2} (c + d x) \right] + 9 a^2 b^2 B \sin \left[ \frac{1}{2} (c + d x) \right] + b^4 B \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) / \\
& \left( 3 d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \left( \cos \left[ \frac{1}{2} (c + d x) \right] + \sin \left[ \frac{1}{2} (c + d x) \right] \right) \right) + \\
& \left( a^4 A \cos [c + d x]^5 (a + b \sec [c + d x])^4 (A + B \sec [c + d x]) \sin [c + d x] \right) / \\
& \left( d (b + a \cos [c + d x])^4 (B + A \cos [c + d x]) \right)
\end{aligned}$$

**Problem 311: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c + d x]^4 (A + B \sec [c + d x])}{a + b \sec [c + d x]} dx$$



Optimal (type 3, 187 leaves, 8 steps):

$$\begin{aligned} & \frac{(2a^2 + b^2)(Ab - aB) \operatorname{ArcTanh}[\sin[c + dx]]}{2b^4 d} - \\ & \frac{2a^3(Ab - aB) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{\sqrt{a-b} b^4 \sqrt{a+b} d} - \frac{(3aAb - 3a^2B - 2b^2B) \tan[c + dx]}{3b^3 d} + \\ & \frac{(Ab - aB) \sec[c + dx] \tan[c + dx]}{2b^2 d} + \frac{B \sec[c + dx]^2 \tan[c + dx]}{3bd} \end{aligned}$$

Result (type 3, 422 leaves):

$$\begin{aligned} & \frac{1}{12b^4 d} \left( \frac{24a^3(Ab - aB) \operatorname{ArcTanh}\left[\frac{(-a+b) \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}} + \right. \\ & 6(2a^2 + b^2)(-Ab + aB) \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] - \\ & 6(2a^2 + b^2)(-Ab + aB) \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] + \\ & \frac{b^2(3Ab + (-3a+b)B)}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{2b^3B \sin\left[\frac{1}{2}(c+dx)\right]}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\ & \frac{4b(-3aAb + 3a^2B + 2b^2B) \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} + \frac{2b^3B \sin\left[\frac{1}{2}(c+dx)\right]}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \\ & \left. \frac{b^2(3Ab + (-3a+b)B)}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{4b(-3aAb + 3a^2B + 2b^2B) \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} \right) \end{aligned}$$

**Problem 312: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c + dx]^3 (A + B \sec[c + dx])}{a + b \sec[c + dx]} dx$$

Optimal (type 3, 143 leaves, 7 steps):

$$\begin{aligned} & - \frac{(2aAb - 2a^2B - b^2B) \operatorname{ArcTanh}[\sin[c + dx]]}{2b^3 d} + \\ & \frac{2a^2(Ab - aB) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right]}{\sqrt{a-b} b^3 \sqrt{a+b} d} + \frac{(Ab - aB) \tan[c + dx]}{b^2 d} + \frac{B \sec[c + dx] \tan[c + dx]}{2bd} \end{aligned}$$

Result (type 3, 300 leaves):

$$\frac{1}{4 b^3 d} \left( \frac{8 a^2 (-A b + a B) \operatorname{ArcTanh}\left[\frac{(-a+b) \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a^2-b^2}}\right]}{\sqrt{a^2-b^2}} - \right.$$

$$2 \left( -2 a A b + 2 a^2 B + b^2 B \right) \log\left[\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right] +$$

$$2 \left( -2 a A b + 2 a^2 B + b^2 B \right) \log\left[\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right] +$$

$$\frac{b^2 B}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{4 b (A b - a B) \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} -$$

$$\frac{b^2 B}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \frac{4 b (A b - a B) \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} \left. \right)$$

**Problem 341: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + dx]}{(a + b \sec[c + dx])^4} dx$$

Optimal (type 3, 292 leaves, 7 steps):

$$\frac{A x}{a^4} - \left( (8 a^6 A b - 8 a^4 A b^3 + 7 a^2 A b^5 - 2 A b^7 - 2 a^7 B - 3 a^5 b^2 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \tan\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right] \right) /$$

$$\left( a^4 (a-b)^{7/2} (a+b)^{7/2} d \right) +$$

$$\frac{b (A b - a B) \tan[c + dx]}{3 a (a^2 - b^2) d (a + b \sec[c + dx])^3} + \frac{b (8 a^2 A b - 3 A b^3 - 5 a^3 B) \tan[c + dx]}{6 a^2 (a^2 - b^2)^2 d (a + b \sec[c + dx])^2} +$$

$$\frac{b (26 a^4 A b - 17 a^2 A b^3 + 6 A b^5 - 11 a^5 B - 4 a^3 b^2 B) \tan[c + dx]}{6 a^3 (a^2 - b^2)^3 d (a + b \sec[c + dx])}$$

Result (type 3, 769 leaves):

$$\begin{aligned}
& \frac{1}{24 a^4 d (B + A \cos [c + d x]) (a + b \sec [c + d x])^4} (b + a \cos [c + d x])^3 \sec [c + d x]^3 \\
& (A + B \sec [c + d x]) \left( -\frac{1}{(a^2 - b^2)^{7/2}} 24 (-8 a^6 A b + 8 a^4 A b^3 - 7 a^2 A b^5 + 2 A b^7 + 2 a^7 B + 3 a^5 b^2 B) \right. \\
& \quad \text{ArcTanh} \left[ \frac{(-a + b) \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a^2 - b^2}} \right] (b + a \cos [c + d x])^3 + \frac{1}{(a^2 - b^2)^3} \\
& \quad \left( 36 a^8 A b c - 84 a^6 A b^3 c + 36 a^4 A b^5 c + 36 a^2 A b^7 c - 24 A b^9 c + 36 a^8 A b d x - 84 a^6 A b^3 d x + \right. \\
& \quad 36 a^4 A b^5 d x + 36 a^2 A b^7 d x - 24 A b^9 d x + 18 a A (a^2 - b^2)^3 (a^2 + 4 b^2) (c + d x) \cos [c + d x] + \\
& \quad 36 a^2 A b (a^2 - b^2)^3 (c + d x) \cos [2 (c + d x)] + 6 a^9 A c \cos [3 (c + d x)] - \\
& \quad 18 a^7 A b^2 c \cos [3 (c + d x)] + 18 a^5 A b^4 c \cos [3 (c + d x)] - 6 a^3 A b^6 c \cos [3 (c + d x)] + \\
& \quad 6 a^9 A d x \cos [3 (c + d x)] - 18 a^7 A b^2 d x \cos [3 (c + d x)] + 18 a^5 A b^4 d x \cos [3 (c + d x)] - \\
& \quad 6 a^3 A b^6 d x \cos [3 (c + d x)] + 36 a^7 A b^2 \sin [c + d x] + 72 a^5 A b^4 \sin [c + d x] - \\
& \quad 57 a^3 A b^6 \sin [c + d x] + 24 a A b^8 \sin [c + d x] - 18 a^8 b B \sin [c + d x] - 39 a^6 b^3 B \sin [c + d x] - \\
& \quad 18 a^4 b^5 B \sin [c + d x] + 120 a^6 A b^3 \sin [2 (c + d x)] - 90 a^4 A b^5 \sin [2 (c + d x)] + \\
& \quad 30 a^2 A b^7 \sin [2 (c + d x)] - 54 a^7 b^2 B \sin [2 (c + d x)] - 6 a^5 b^4 B \sin [2 (c + d x)] + \\
& \quad 36 a^7 A b^2 \sin [3 (c + d x)] - 32 a^5 A b^4 \sin [3 (c + d x)] + 11 a^3 A b^6 \sin [3 (c + d x)] - \\
& \quad \left. 18 a^8 b B \sin [3 (c + d x)] + 5 a^6 b^3 B \sin [3 (c + d x)] - 2 a^4 b^5 B \sin [3 (c + d x)] \right) \Bigg)
\end{aligned}$$

**Problem 342: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x] (A + B \sec [c + d x])}{(a + b \sec [c + d x])^4} dx$$

Optimal (type 3, 411 leaves, 8 steps):

$$\begin{aligned}
& -\frac{(4 A b - a B) x}{a^5} + \left( b (20 a^6 A b - 35 a^4 A b^3 + 28 a^2 A b^5 - 8 A b^7 - 8 a^7 B + 8 a^5 b^2 B - 7 a^3 b^4 B + 2 a b^6 B) \right. \\
& \quad \left. \text{ArcTanh} \left[ \frac{\sqrt{a - b} \tan \left[ \frac{1}{2} (c + d x) \right]}{\sqrt{a + b}} \right] \right) / \left( a^5 (a - b)^{7/2} (a + b)^{7/2} d \right) + \frac{1}{6 a^4 (a^2 - b^2)^3 d} \\
& \quad (6 a^6 A - 65 a^4 A b^2 + 68 a^2 A b^4 - 24 A b^6 + 26 a^5 b B - 17 a^3 b^3 B + 6 a b^5 B) \sin [c + d x] + \\
& \quad \frac{b (A b - a B) \sin [c + d x]}{3 a (a^2 - b^2) d (a + b \sec [c + d x])^3} + \frac{b (9 a^2 A b - 4 A b^3 - 6 a^3 B + a b^2 B) \sin [c + d x]}{6 a^2 (a^2 - b^2)^2 d (a + b \sec [c + d x])^2} + \\
& \quad \frac{b (12 a^4 A b - 11 a^2 A b^3 + 4 A b^5 - 6 a^5 B + 2 a^3 b^2 B - a b^4 B) \sin [c + d x]}{2 a^3 (a^2 - b^2)^3 d (a + b \sec [c + d x])}
\end{aligned}$$

Result (type 3, 1372 leaves):

$$\begin{aligned}
& - \left( \left( b \left( -20 a^6 A b + 35 a^4 A b^3 - 28 a^2 A b^5 + 8 A b^7 + 8 a^7 B - 8 a^5 b^2 B + 7 a^3 b^4 B - 2 a b^6 B \right) \right. \right. \\
& \quad \left. \left. \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2-b^2}} \right] (b+a \cos [c+dx])^4 \operatorname{Sec} [c+dx]^3 (A+B \operatorname{Sec} [c+dx]) \right) \right) / \\
& \quad \left( a^5 \sqrt{a^2-b^2} (-a^2+b^2)^3 d (B+A \cos [c+dx]) (a+b \operatorname{Sec} [c+dx])^4 \right) + \\
& \quad \frac{1}{24 a^5 (a^2-b^2)^3 d (B+A \cos [c+dx]) (a+b \operatorname{Sec} [c+dx])^4} \\
& \quad (b+a \cos [c+dx]) \operatorname{Sec} [c+dx]^3 (A+B \operatorname{Sec} [c+dx]) \\
& \quad (-144 a^8 A b^2 (c+dx) + 336 a^6 A b^4 (c+dx) - 144 a^4 A b^6 (c+dx) - 144 a^2 A b^8 (c+dx) + \\
& \quad 96 A b^{10} (c+dx) + 36 a^9 b B (c+dx) - 84 a^7 b^3 B (c+dx) + 36 a^5 b^5 B (c+dx) + \\
& \quad 36 a^3 b^7 B (c+dx) - 24 a b^9 B (c+dx) - 72 a^9 A b (c+dx) \cos [c+dx] - 72 a^7 A b^3 (c+dx) \\
& \quad \cos [c+dx] + 648 a^5 A b^5 (c+dx) \cos [c+dx] - 792 a^3 A b^7 (c+dx) \cos [c+dx] + \\
& \quad 288 a A b^9 (c+dx) \cos [c+dx] + 18 a^{10} B (c+dx) \cos [c+dx] + 18 a^8 b^2 B (c+dx) \cos [c+dx] - \\
& \quad 162 a^6 b^4 B (c+dx) \cos [c+dx] + 198 a^4 b^6 B (c+dx) \cos [c+dx] - \\
& \quad 72 a^2 b^8 B (c+dx) \cos [c+dx] - 144 a^8 A b^2 (c+dx) \cos [2 (c+dx)] + \\
& \quad 432 a^6 A b^4 (c+dx) \cos [2 (c+dx)] - 432 a^4 A b^6 (c+dx) \cos [2 (c+dx)] + \\
& \quad 144 a^2 A b^8 (c+dx) \cos [2 (c+dx)] + 36 a^9 b B (c+dx) \cos [2 (c+dx)] - \\
& \quad 108 a^7 b^3 B (c+dx) \cos [2 (c+dx)] + 108 a^5 b^5 B (c+dx) \cos [2 (c+dx)] - \\
& \quad 36 a^3 b^7 B (c+dx) \cos [2 (c+dx)] - 24 a^9 A b (c+dx) \cos [3 (c+dx)] + \\
& \quad 72 a^7 A b^3 (c+dx) \cos [3 (c+dx)] - 72 a^5 A b^5 (c+dx) \cos [3 (c+dx)] + \\
& \quad 24 a^3 A b^7 (c+dx) \cos [3 (c+dx)] + 6 a^{10} B (c+dx) \cos [3 (c+dx)] - \\
& \quad 18 a^8 b^2 B (c+dx) \cos [3 (c+dx)] + 18 a^6 b^4 B (c+dx) \cos [3 (c+dx)] - \\
& \quad 6 a^4 b^6 B (c+dx) \cos [3 (c+dx)] + 18 a^9 A b \sin [c+dx] - 90 a^7 A b^3 \sin [c+dx] - \\
& \quad 135 a^5 A b^5 \sin [c+dx] + 228 a^3 A b^7 \sin [c+dx] - 96 a A b^9 \sin [c+dx] + 36 a^8 b^2 B \sin [c+dx] + \\
& \quad 72 a^6 b^4 B \sin [c+dx] - 57 a^4 b^6 B \sin [c+dx] + 24 a^2 b^8 B \sin [c+dx] + 6 a^{10} A \sin [2 (c+dx)] + \\
& \quad 18 a^8 A b^2 \sin [2 (c+dx)] - 300 a^6 A b^4 \sin [2 (c+dx)] + 336 a^4 A b^6 \sin [2 (c+dx)] - \\
& \quad 120 a^2 A b^8 \sin [2 (c+dx)] + 120 a^7 b^3 B \sin [2 (c+dx)] - 90 a^5 b^5 B \sin [2 (c+dx)] + \\
& \quad 30 a^3 b^7 B \sin [2 (c+dx)] + 18 a^9 A b \sin [3 (c+dx)] - 114 a^7 A b^3 \sin [3 (c+dx)] + \\
& \quad 125 a^5 A b^5 \sin [3 (c+dx)] - 44 a^3 A b^7 \sin [3 (c+dx)] + 36 a^8 b^2 B \sin [3 (c+dx)] - \\
& \quad 32 a^6 b^4 B \sin [3 (c+dx)] + 11 a^4 b^6 B \sin [3 (c+dx)] + 3 a^{10} A \sin [4 (c+dx)] - \\
& \quad 9 a^8 A b^2 \sin [4 (c+dx)] + 9 a^6 A b^4 \sin [4 (c+dx)] - 3 a^4 A b^6 \sin [4 (c+dx)] )
\end{aligned}$$

### Problem 343: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+dx]^2 (A+B \operatorname{Sec} [c+dx])}{(a+b \operatorname{Sec} [c+dx])^4} dx$$

Optimal (type 3, 538 leaves, 9 steps):

$$\begin{aligned}
& \frac{(a^2 A + 20 A b^2 - 8 a b B) x}{2 a^6} - \\
& \left( b^2 (40 a^6 A b - 84 a^4 A b^3 + 69 a^2 A b^5 - 20 A b^7 - 20 a^7 B + 35 a^5 b^2 B - 28 a^3 b^4 B + 8 a b^6 B) \right. \\
& \quad \left. \operatorname{ArcTanh}\left[\frac{\sqrt{a-b} \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]}{\sqrt{a+b}}\right] \right) / \left( a^6 (a-b)^{7/2} (a+b)^{7/2} d \right) - \frac{1}{6 a^5 (a^2-b^2)^3 d} \\
& (24 a^6 A b - 146 a^4 A b^3 + 167 a^2 A b^5 - 60 A b^7 - 6 a^7 B + 65 a^5 b^2 B - 68 a^3 b^4 B + 24 a b^6 B) \operatorname{Sin}[c+dx] + \\
& \frac{1}{2 a^4 (a^2-b^2)^3 d} (a^6 A - 23 a^4 A b^2 + 27 a^2 A b^4 - 10 A b^6 + 12 a^5 b B - 11 a^3 b^3 B + 4 a b^5 B) \\
& \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx] + \frac{b (A b - a B) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{3 a (a^2-b^2) d (a+b \operatorname{Sec}[c+dx])^3} + \\
& \frac{b (10 a^2 A b - 5 A b^3 - 7 a^3 B + 2 a b^2 B) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]}{6 a^2 (a^2-b^2)^2 d (a+b \operatorname{Sec}[c+dx])^2} + \\
& (b (48 a^4 A b - 53 a^2 A b^3 + 20 A b^5 - 27 a^5 B + 20 a^3 b^2 B - 8 a b^4 B) \operatorname{Cos}[c+dx] \operatorname{Sin}[c+dx]) / \\
& (6 a^3 (a^2-b^2)^3 d (a+b \operatorname{Sec}[c+dx]))
\end{aligned}$$

Result (type 3, 1578 leaves):

$$\begin{aligned}
& \left( b^2 \left( -40 a^6 A b + 84 a^4 A b^3 - 69 a^2 A b^5 + 20 A b^7 + 20 a^7 B - 35 a^5 b^2 B + 28 a^3 b^4 B - 8 a b^6 B \right) \right. \\
& \quad \left. \operatorname{ArcTanh} \left[ \frac{(-a+b) \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]}{\sqrt{a^2-b^2}} \right] \right) / \left( a^6 \sqrt{a^2-b^2} (-a^2+b^2)^3 d \right) + \\
& \quad \frac{1}{96 a^6 (a^2-b^2)^3 d (b+a \operatorname{Cos}[c+dx])^3} \left( 72 a^{10} A b (c+dx) + 1272 a^8 A b^3 (c+dx) - \right. \\
& \quad 3288 a^6 A b^5 (c+dx) + 1512 a^4 A b^7 (c+dx) + 1392 a^2 A b^9 (c+dx) - 960 A b^{11} (c+dx) - \\
& \quad 576 a^9 b^2 B (c+dx) + 1344 a^7 b^4 B (c+dx) - 576 a^5 b^6 B (c+dx) - 576 a^3 b^8 B (c+dx) + \\
& \quad 384 a b^{10} B (c+dx) + 36 a^{11} A (c+dx) \operatorname{Cos}[c+dx] + 756 a^9 A b^2 (c+dx) \operatorname{Cos}[c+dx] + \\
& \quad 396 a^7 A b^4 (c+dx) \operatorname{Cos}[c+dx] - 6084 a^5 A b^6 (c+dx) \operatorname{Cos}[c+dx] + \\
& \quad 7776 a^3 A b^8 (c+dx) \operatorname{Cos}[c+dx] - 2880 a A b^{10} (c+dx) \operatorname{Cos}[c+dx] - \\
& \quad 288 a^{10} b B (c+dx) \operatorname{Cos}[c+dx] - 288 a^8 b^3 B (c+dx) \operatorname{Cos}[c+dx] + \\
& \quad 2592 a^6 b^5 B (c+dx) \operatorname{Cos}[c+dx] - 3168 a^4 b^7 B (c+dx) \operatorname{Cos}[c+dx] + \\
& \quad 1152 a^2 b^9 B (c+dx) \operatorname{Cos}[c+dx] + 72 a^{10} A b (c+dx) \operatorname{Cos}[2(c+dx)] + \\
& \quad 1224 a^8 A b^3 (c+dx) \operatorname{Cos}[2(c+dx)] - 4104 a^6 A b^5 (c+dx) \operatorname{Cos}[2(c+dx)] + \\
& \quad 4248 a^4 A b^7 (c+dx) \operatorname{Cos}[2(c+dx)] - 1440 a^2 A b^9 (c+dx) \operatorname{Cos}[2(c+dx)] - \\
& \quad 576 a^9 b^2 B (c+dx) \operatorname{Cos}[2(c+dx)] + 1728 a^7 b^4 B (c+dx) \operatorname{Cos}[2(c+dx)] - \\
& \quad 1728 a^5 b^6 B (c+dx) \operatorname{Cos}[2(c+dx)] + 576 a^3 b^8 B (c+dx) \operatorname{Cos}[2(c+dx)] + \\
& \quad 12 a^{11} A (c+dx) \operatorname{Cos}[3(c+dx)] + 204 a^9 A b^2 (c+dx) \operatorname{Cos}[3(c+dx)] - \\
& \quad 684 a^7 A b^4 (c+dx) \operatorname{Cos}[3(c+dx)] + 708 a^5 A b^6 (c+dx) \operatorname{Cos}[3(c+dx)] - \\
& \quad 240 a^3 A b^8 (c+dx) \operatorname{Cos}[3(c+dx)] - 96 a^{10} b B (c+dx) \operatorname{Cos}[3(c+dx)] + \\
& \quad 288 a^8 b^3 B (c+dx) \operatorname{Cos}[3(c+dx)] - 288 a^6 b^5 B (c+dx) \operatorname{Cos}[3(c+dx)] + \\
& \quad 96 a^4 b^7 B (c+dx) \operatorname{Cos}[3(c+dx)] + 6 a^{11} A \operatorname{Sin}[c+dx] - 270 a^9 A b^2 \operatorname{Sin}[c+dx] + \\
& \quad 750 a^7 A b^4 \operatorname{Sin}[c+dx] + 1086 a^5 A b^6 \operatorname{Sin}[c+dx] - 2232 a^3 A b^8 \operatorname{Sin}[c+dx] + \\
& \quad 960 a A b^{10} \operatorname{Sin}[c+dx] + 72 a^{10} b B \operatorname{Sin}[c+dx] - 360 a^8 b^3 B \operatorname{Sin}[c+dx] - 540 a^6 b^5 B \operatorname{Sin}[c+dx] + \\
& \quad 912 a^4 b^7 B \operatorname{Sin}[c+dx] - 384 a^2 b^9 B \operatorname{Sin}[c+dx] - 60 a^{10} A b \operatorname{Sin}[2(c+dx)] - \\
& \quad 372 a^8 A b^3 \operatorname{Sin}[2(c+dx)] + 2772 a^6 A b^5 \operatorname{Sin}[2(c+dx)] - 3300 a^4 A b^7 \operatorname{Sin}[2(c+dx)] + \\
& \quad 1200 a^2 A b^9 \operatorname{Sin}[2(c+dx)] + 24 a^{11} B \operatorname{Sin}[2(c+dx)] + 72 a^9 b^2 B \operatorname{Sin}[2(c+dx)] - \\
& \quad 1200 a^7 b^4 B \operatorname{Sin}[2(c+dx)] + 1344 a^5 b^6 B \operatorname{Sin}[2(c+dx)] - 480 a^3 b^8 B \operatorname{Sin}[2(c+dx)] + \\
& \quad 9 a^{11} A \operatorname{Sin}[3(c+dx)] - 279 a^9 A b^2 \operatorname{Sin}[3(c+dx)] + 1143 a^7 A b^4 \operatorname{Sin}[3(c+dx)] - \\
& \quad 1253 a^5 A b^6 \operatorname{Sin}[3(c+dx)] + 440 a^3 A b^8 \operatorname{Sin}[3(c+dx)] + 72 a^{10} b B \operatorname{Sin}[3(c+dx)] - \\
& \quad 456 a^8 b^3 B \operatorname{Sin}[3(c+dx)] + 500 a^6 b^5 B \operatorname{Sin}[3(c+dx)] - 176 a^4 b^7 B \operatorname{Sin}[3(c+dx)] - \\
& \quad 30 a^{10} A b \operatorname{Sin}[4(c+dx)] + 90 a^8 A b^3 \operatorname{Sin}[4(c+dx)] - 90 a^6 A b^5 \operatorname{Sin}[4(c+dx)] + \\
& \quad 30 a^4 A b^7 \operatorname{Sin}[4(c+dx)] + 12 a^{11} B \operatorname{Sin}[4(c+dx)] - 36 a^9 b^2 B \operatorname{Sin}[4(c+dx)] + \\
& \quad 36 a^7 b^4 B \operatorname{Sin}[4(c+dx)] - 12 a^5 b^6 B \operatorname{Sin}[4(c+dx)] + 3 a^{11} A \operatorname{Sin}[5(c+dx)] - \\
& \quad 9 a^9 A b^2 \operatorname{Sin}[5(c+dx)] + 9 a^7 A b^4 \operatorname{Sin}[5(c+dx)] - 3 a^5 A b^6 \operatorname{Sin}[5(c+dx)] \Big)
\end{aligned}$$

**Problem 348: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+dx]^4 \sqrt{a+b \operatorname{Sec}[c+dx]} (A+B \operatorname{Sec}[c+dx]) dx$$

Optimal (type 4, 485 leaves, 7 steps):

$$\begin{aligned}
& -\frac{1}{315 b^5 d} 2 (a-b) \sqrt{a+b} (24 a^3 A b + 57 a A b^3 - 16 a^4 B - 24 a^2 b^2 B + 147 b^4 B) \\
& \quad \text{Cot}[c+dx] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \quad \sqrt{\frac{b(1-\text{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+dx])}{a-b}} - \frac{1}{315 b^4 d} \\
& \quad 2(a-b) \sqrt{a+b} (3 b^3 (25 A - 49 B) + 18 a b^2 (A - 2 B) + 12 a^2 b (2 A - B) - 16 a^3 B) \text{Cot}[c+dx] \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \text{Sec}[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\text{Sec}[c+dx])}{a+b}} \sqrt{-\frac{b(1+\text{Sec}[c+dx])}{a-b}} - \\
& \quad \frac{1}{315 b^3 d} 2 (12 a^2 A b - 75 A b^3 - 8 a^3 B - 13 a b^2 B) \sqrt{a+b \text{Sec}[c+dx]} \text{Tan}[c+dx] + \\
& \quad \frac{1}{315 b^2 d} 2 (9 a A b - 6 a^2 B + 49 b^2 B) \text{Sec}[c+dx] \sqrt{a+b \text{Sec}[c+dx]} \text{Tan}[c+dx] + \\
& \quad \frac{2 (9 A b + a B) \text{Sec}[c+dx]^2 \sqrt{a+b \text{Sec}[c+dx]} \text{Tan}[c+dx]}{63 b d} + \\
& \quad \frac{2 B \text{Sec}[c+dx]^3 \sqrt{a+b \text{Sec}[c+dx]} \text{Tan}[c+dx]}{9 d}
\end{aligned}$$

Result(type 1, 1 leaves):

???

**Problem 349: Attempted integration timed out after 120 seconds.**

$$\int \text{Sec}[c+dx]^3 \sqrt{a+b \text{Sec}[c+dx]} (A+B \text{Sec}[c+dx]) dx$$

Optimal (type 4, 397 leaves, 6 steps):

$$\begin{aligned}
& \frac{1}{105 b^4 d} 2 (a-b) \sqrt{a+b} (14 a^2 A b - 63 A b^3 - 8 a^3 B - 19 a b^2 B) \cot [c+d x] \\
& \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\
& \frac{1}{105 b^3 d} 2 (a-b) \sqrt{a+b} (b^2 (63 A - 25 B) + 2 a b (7 A - 3 B) - 8 a^2 B) \cot [c+d x] \\
& \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\
& \frac{2 (7 a A b - 4 a^2 B + 25 b^2 B) \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{105 b^2 d} + \\
& \frac{2 (7 A b + a B) \sec [c+d x] \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{35 b d} + \\
& \frac{2 B \sec [c+d x]^2 \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{7 d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 350: Unable to integrate problem.

$$\int \sec [c+d x]^2 \sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]) dx$$

Optimal (type 4, 314 leaves, 5 steps):

$$\begin{aligned}
& -\frac{1}{15 b^3 d} 2 (a-b) \sqrt{a+b} (5 a A b - 2 a^2 B + 9 b^2 B) \\
& \cot [c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{15 b^2 d} \\
& 2 (a-b) \sqrt{a+b} (5 A b - 2 a B - 9 b B) \cot [c+d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\
& \frac{2 (5 A b - 2 a B) \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{15 b d} + \frac{2 B (a+b \sec [c+d x])^{3/2} \tan [c+d x]}{5 b d}
\end{aligned}$$

Result (type 8, 35 leaves):



$$\int \sec[c+dx]^2 \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Problem 351: Attempted integration timed out after 120 seconds.

$$\int \sec[c+dx] \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 256 leaves, 4 steps):

$$\begin{aligned} & -\frac{1}{3b^2d} 2(a-b) \sqrt{a+b} (3Ab+aB) \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{1}{3bd} \\ & 2(a-b) \sqrt{a+b} (3A-B) \cot[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{2B \sqrt{a+b \sec[c+dx]} \tan[c+dx]}{3d} \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 352: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 320 leaves, 5 steps):

$$\begin{aligned}
& -\frac{1}{bd} 2(a-b) \sqrt{a+b} B \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{1}{bd} \\
& 2\sqrt{a+b} (Ab + (a-b)B) \cot[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} - \frac{1}{d} \\
& 2A\sqrt{a+b} \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}}
\end{aligned}$$

Result (type 4, 913 leaves):

$$\begin{aligned}
& \frac{2B \cos[c+dx] \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) \sin[c+dx]}{d(B+A \cos[c+dx])} + \\
& \left( 2\sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) \right. \\
& \left( a \sqrt{\frac{-a+b}{a+b}} B \tan\left[\frac{1}{2}(c+dx)\right] + b \sqrt{\frac{-a+b}{a+b}} B \tan\left[\frac{1}{2}(c+dx)\right] - 2a \sqrt{\frac{-a+b}{a+b}} B \right. \\
& \left. \tan\left[\frac{1}{2}(c+dx)\right]^3 + a \sqrt{\frac{-a+b}{a+b}} B \tan\left[\frac{1}{2}(c+dx)\right]^5 - b \sqrt{\frac{-a+b}{a+b}} B \tan\left[\frac{1}{2}(c+dx)\right]^5 + \right. \\
& \left. 2ia \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \right. \\
& \left. \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \right. \\
& \left. 2ia \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \right. \\
& \left. \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \right.
\end{aligned}$$

$$\begin{aligned}
& i (a-b) B \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2} \\
& \left( 1 + \tan^2 \left[ \frac{1}{2} (c+dx) \right] \right) \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right] + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - i (a-b) \\
& (A-B) \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2} \\
& \left( 1 + \tan^2 \left[ \frac{1}{2} (c+dx) \right] \right) \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right] + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} \right) \Bigg) / \\
& \left( \sqrt{\frac{-a+b}{a+b}} d \sqrt{b+a \cos [c+dx]} (B+A \cos [c+dx]) \sec [c+dx]^{3/2} \right. \\
& \left. \sqrt{\frac{1}{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}} \left( -1 + \tan^2 \left[ \frac{1}{2} (c+dx) \right] \right) \left( 1 + \tan^2 \left[ \frac{1}{2} (c+dx) \right] \right)^{3/2} \right. \\
& \left. \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right] + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}} \right)
\end{aligned}$$

**Problem 353: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \cos [c+dx] \sqrt{a+b \sec [c+dx]} (A+B \sec [c+dx]) dx$$

Optimal (type 4, 344 leaves, 6 steps):

$$\begin{aligned}
& \frac{1}{b d} A (a-b) \sqrt{a+b} \cot[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{d} \sqrt{a+b} (A+2 B) \cot[c+d x] \\
& \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\
& \frac{1}{a d} \sqrt{a+b} (A b+2 a B) \cot[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{A \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{d}
\end{aligned}$$

Result (type 4, 1107 leaves):

$$\begin{aligned}
& \left( \sqrt{a+b \sec [c+d x]} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
& \left( a A \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right] + A b \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right] - 2 a A \sqrt{\frac{-a+b}{a+b}} \right. \\
& \tan \left[\frac{1}{2}(c+d x)\right]^3 + a A \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]^5 - A b \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]^5 - \\
& 2 i A b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 4 i a B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 2 i A b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right]
\end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 4 \, i \, a \, B \, \text{EllipticPi}\left[-\frac{a+b}{a-b}, \, i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \, \frac{a+b}{a-b}\right] \\
 & \tan\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & i \, A \, (a-b) \, \text{EllipticE}\left[i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \, \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2 \, i \, (a-b) \\
 & B \, \text{EllipticF}\left[i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \, \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) / \\
 & \left( \sqrt{\frac{-a+b}{a+b}} \, d \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
 & \left. \left( b - b \tan\left[\frac{1}{2}(c+dx)\right]^4 + a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right)
 \end{aligned}$$

**Problem 354: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^2 \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) \, dx$$

Optimal (type 4, 429 leaves, 7 steps):

$$\begin{aligned}
& \frac{1}{4 a b d} (a-b) \sqrt{a+b} (A b+4 a B) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{4 a d} \\
& \sqrt{a+b} (A b+2 a(A+2 B)) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{4 a^2 d} \\
& \sqrt{a+b} (4 a^2 A-A b^2+4 a b B) \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\
& \frac{(A b+4 a B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 a d} + \frac{A \cos [c+d x] \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 d}
\end{aligned}$$

Result (type 4, 1161 leaves):

$$\begin{aligned}
& \frac{A \sqrt{a+b \sec [c+d x]} \sin [2(c+d x)]}{4 d} + \\
& \left( \sqrt{a+b \sec [c+d x]} \sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}} \left( a A b \tan \left[\frac{1}{2}(c+d x)\right] + A b^2 \tan \left[\frac{1}{2}(c+d x)\right] + \right. \right. \\
& 4 a^2 B \tan \left[\frac{1}{2}(c+d x)\right] + 4 a b B \tan \left[\frac{1}{2}(c+d x)\right] - 2 a A b \tan \left[\frac{1}{2}(c+d x)\right]^3 - 8 a^2 B \\
& \tan \left[\frac{1}{2}(c+d x)\right]^3 + a A b \tan \left[\frac{1}{2}(c+d x)\right]^5 - A b^2 \tan \left[\frac{1}{2}(c+d x)\right]^5 + 4 a^2 B \tan \left[\frac{1}{2}(c+d x)\right]^5 - \\
& 4 a b B \tan \left[\frac{1}{2}(c+d x)\right]^5 - 8 a^2 A \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 2 A b^2 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\tan \left[\frac{1}{2}(c+d x)\right]^2} \\
& \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 8 a b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right]
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 8a^2 A \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 2Ab^2 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 8abB \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& (a+b)(Ab+4aB) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 2a(2aA - Ab + 4bB) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg) / \\
& \left( 4ad \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
& \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
\end{aligned}$$

Problem 355: Result more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^3 \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 509 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{24 a^2 b d} (a-b) \sqrt{a+b} (16 a^2 A - 3 A b^2 + 6 a b B) \cot[c+dx] \\ & \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \\ & \frac{1}{24 a^2 d} \sqrt{a+b} (2a+b) (8 a A - 3 A b + 6 a B) \cot[c+dx] \\ & \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} - \\ & \frac{1}{8 a^3 d} \sqrt{a+b} (4 a^2 A b + A b^3 + 8 a^3 B - 2 a b^2 B) \cot[c+dx] \\ & \text{EllipticPi}\left[\frac{a+b}{a}, \text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \\ & \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{(16 a^2 A - 3 A b^2 + 6 a b B) \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{24 a^2 d} + \\ & \frac{(A b + 6 a B) \cos[c+dx] \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{12 a d} + \\ & \frac{A \cos[c+dx]^2 \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{3 d} \end{aligned}$$

Result (type 4, 1565 leaves):

$$\begin{aligned} & \frac{1}{d} \sqrt{a+b \sec[c+dx]} \left( \frac{1}{12} A \sin[c+dx] + \frac{(A b + 6 a B) \sin[2(c+dx)]}{24 a} + \frac{1}{12} A \sin[3(c+dx)] \right) + \\ & \left( \sqrt{a+b \sec[c+dx]} \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\ & \left( -16 a^3 A \tan\left[\frac{1}{2}(c+dx)\right] - 16 a^2 A b \tan\left[\frac{1}{2}(c+dx)\right] + 3 a A b^2 \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\ & 3 A b^3 \tan\left[\frac{1}{2}(c+dx)\right] - 6 a^2 b B \tan\left[\frac{1}{2}(c+dx)\right] - 6 a b^2 B \tan\left[\frac{1}{2}(c+dx)\right] + \\ & 32 a^3 A \tan\left[\frac{1}{2}(c+dx)\right]^3 - 6 a A b^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + 12 a^2 b B \tan\left[\frac{1}{2}(c+dx)\right]^3 - \\ & \left. 16 a^3 A \tan\left[\frac{1}{2}(c+dx)\right]^5 + 16 a^2 A b \tan\left[\frac{1}{2}(c+dx)\right]^5 + 3 a A b^2 \tan\left[\frac{1}{2}(c+dx)\right]^5 - \right. \end{aligned}$$



$$\begin{aligned}
& 3 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 6 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 6 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \\
& 24 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 48 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 12 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 24 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 48 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 12 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& (a+b) \left(16a^2A - 3Ab^2 + 6abB\right) \text{EllipticE}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2a \left(-Ab^2 + 2ab(7A - 3B) + 12a^2B\right) \\
& \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg/ \\
& \left(24a^2d \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right. \\
& \left. \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right)
\end{aligned}$$

**Problem 356: Attempted integration timed out after 120 seconds.**

$$\int \sec[c+dx]^3 (a+b \sec[c+dx])^{3/2} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 475 leaves, 7 steps):

$$\begin{aligned}
& \frac{1}{315 b^4 d} 2 (a-b) \sqrt{a+b} (18 a^3 A b - 246 a A b^3 - 8 a^4 B - 33 a^2 b^2 B - 147 b^4 B) \\
& \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{315 b^3 d} \\
& 2 (a-b) \sqrt{a+b} (3 b^3 (25 A - 49 B) - 3 a b^2 (57 A - 13 B) - 6 a^2 b (3 A - B) + 8 a^3 B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \\
& \frac{1}{315 b^2 d} 2 (18 a^2 A b - 75 A b^3 - 8 a^3 B - 39 a b^2 B) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Tan}[c+d x] - \\
& \frac{2 (18 a A b - 8 a^2 B - 49 b^2 B) (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Tan}[c+d x]}{315 b^2 d} + \\
& \frac{2 (9 A b - 4 a B) (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{63 b^2 d} + \\
& \frac{2 B \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{5/2} \operatorname{Tan}[c+d x]}{9 b d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 357: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+d x]^2 (a+b \operatorname{Sec}[c+d x])^{3/2} (A+B \operatorname{Sec}[c+d x]) dx$$

Optimal (type 4, 388 leaves, 6 steps):

$$\begin{aligned}
& -\frac{1}{105 b^3 d} 2 (a-b) \sqrt{a+b} (21 a^2 A b + 63 A b^3 - 6 a^3 B + 82 a b^2 B) \\
& \quad \text{Cot}[c+dx] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \quad \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{1}{105 b^2 d} \\
& 2 (a-b) \sqrt{a+b} (b^2 (63 A - 25 B) + 6 a^2 B - a (21 A b - 57 b B)) \text{Cot}[c+dx] \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \\
& \quad \frac{2 (21 a A b - 6 a^2 B + 25 b^2 B) \sqrt{a+b \sec[c+dx]} \tan[c+dx]}{105 b d} + \\
& \quad \frac{2 (7 A b - 2 a B) (a+b \sec[c+dx])^{3/2} \tan[c+dx]}{35 b d} + \frac{2 B (a+b \sec[c+dx])^{5/2} \tan[c+dx]}{7 b d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 358: Attempted integration timed out after 120 seconds.**

$$\int \sec[c+dx] (a+b \sec[c+dx])^{3/2} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 312 leaves, 5 steps):

$$\begin{aligned}
& -\frac{1}{15 b^2 d} 2 (a-b) \sqrt{a+b} (20 a A b + 3 a^2 B + 9 b^2 B) \text{Cot}[c+dx] \text{EllipticE}\left[ \right. \\
& \quad \text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\left. \right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \\
& \quad \frac{1}{15 b d} 2 (a-b) \sqrt{a+b} (15 a A - 5 A b - 3 a B + 9 b B) \text{Cot}[c+dx] \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \\
& \quad \frac{2 (5 A b + 3 a B) \sqrt{a+b \sec[c+dx]} \tan[c+dx]}{15 d} + \frac{2 B (a+b \sec[c+dx])^{3/2} \tan[c+dx]}{5 d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 359: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int (a+b \sec [c+d x])^{3/2} (A+B \sec [c+d x]) dx$$

Optimal (type 4, 381 leaves, 6 steps):

$$\begin{aligned} & -\frac{1}{3bd} 2(a-b) \sqrt{a+b} (3Ab+4aB) \cot [c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec [c+dx])}{a-b}} - \\ & \frac{1}{3bd} 2\sqrt{a+b} (b^2(3A-B) - 3a^2B - a(6Ab-4bB)) \cot [c+dx] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec [c+dx])}{a-b}} - \\ & \frac{1}{d} 2aA\sqrt{a+b} \cot [c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec [c+dx])}{a-b}} + \frac{2bB\sqrt{a+b \sec [c+dx]} \tan [c+dx]}{3d} \end{aligned}$$

Result (type 4, 1145 leaves):

$$\begin{aligned} & \left( 2(a+b \sec [c+dx])^{3/2} (A+B \sec [c+dx]) \right. \\ & \left( 3aAb \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+dx) \right] + 3Ab^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+dx) \right] + \right. \\ & 4a^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2}(c+dx) \right] + 4ab \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2}(c+dx) \right] - \\ & 6aAb \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+dx) \right]^3 - 8a^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2}(c+dx) \right]^3 + \\ & 3aAb \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+dx) \right]^5 - 3Ab^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2}(c+dx) \right]^5 + \\ & \left. \left. 4a^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2}(c+dx) \right]^5 - 4ab \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2}(c+dx) \right]^5 + \right. \right. \end{aligned}$$

$$\begin{aligned}
& 6 \, i \, a^2 A \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \\
& \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + \\
& 6 \, i \, a^2 A \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
& \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
& i (a-b) (3Ab + 4aB) \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \\
& \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - i (a-b) (3a(A-B) + b(-3A+B)) \\
& \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \sqrt{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \\
& \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} \right) \Bigg/ \\
& \left( 3 \sqrt{\frac{-a+b}{a+b}} d (b+a \operatorname{Cos} [c+dx])^{3/2} (B+A \operatorname{Cos} [c+dx]) \operatorname{Sec} [c+dx]^{5/2} \right. \\
& \sqrt{\frac{1}{1 - \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \left( -1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \left( 1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{3/2} \\
& \left. \sqrt{\frac{a+b - a \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \operatorname{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \right) + \\
& \left( \operatorname{Cos} [c+dx]^2 (a+b \operatorname{Sec} [c+dx])^{3/2} (A+B \operatorname{Sec} [c+dx]) \right)
\end{aligned}$$

$$\left( \frac{2}{3} (3 A b + 4 a B) \sin[c + d x] + \frac{2}{3} b B \tan[c + d x] \right) / \left( d (b + a \cos[c + d x]) (B + A \cos[c + d x]) \right)$$

**Problem 360: Result more than twice size of optimal antiderivative.**

$$\int \cos[c + d x] (a + b \sec[c + d x])^{3/2} (A + B \sec[c + d x]) dx$$

Optimal (type 4, 361 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{b d} (a - b) \sqrt{a + b} (a A - 2 b B) \cot[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \sec[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\ & \sqrt{\frac{b(1 - \sec[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \sec[c + d x])}{a - b}} + \frac{1}{d} \sqrt{a + b} (2 b (A - B) + a (A + 4 B)) \cot[c + d x] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \sec[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \sec[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \sec[c + d x])}{a - b}} - \\ & \frac{1}{d} \sqrt{a + b} (3 A b + 2 a B) \cot[c + d x] \operatorname{EllipticPi}\left[\frac{a + b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a + b \sec[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\ & \sqrt{\frac{b(1 - \sec[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \sec[c + d x])}{a - b}} + \frac{a A \sqrt{a + b \sec[c + d x]} \sin[c + d x]}{d} \end{aligned}$$

Result (type 4, 979 leaves):

$$\begin{aligned} & \frac{2 b B \cos[c + d x] (a + b \sec[c + d x])^{3/2} \sin[c + d x]}{d (b + a \cos[c + d x])} + \\ & \left( (a + b \sec[c + d x])^{3/2} \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c + d x)\right]^2}} \right. \\ & \left( a^2 A \tan\left[\frac{1}{2}(c + d x)\right] + a A b \tan\left[\frac{1}{2}(c + d x)\right] - 2 a b B \tan\left[\frac{1}{2}(c + d x)\right] - \right. \\ & 2 b^2 B \tan\left[\frac{1}{2}(c + d x)\right] - 2 a^2 A \tan\left[\frac{1}{2}(c + d x)\right]^3 + 4 a b B \tan\left[\frac{1}{2}(c + d x)\right]^3 + \\ & a^2 A \tan\left[\frac{1}{2}(c + d x)\right]^5 - a A b \tan\left[\frac{1}{2}(c + d x)\right]^5 - 2 a b B \tan\left[\frac{1}{2}(c + d x)\right]^5 + \\ & 2 b^2 B \tan\left[\frac{1}{2}(c + d x)\right]^5 - 6 a A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c + d x)\right]\right], \frac{a - b}{a + b}\right] \\ & \left. \sqrt{1 - \tan\left[\frac{1}{2}(c + d x)\right]^2} \sqrt{\frac{a + b - a \tan\left[\frac{1}{2}(c + d x)\right]^2 + b \tan\left[\frac{1}{2}(c + d x)\right]^2}{a + b}} - \right. \end{aligned}$$

$$\begin{aligned}
& 4 a^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 6 a A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 4 a^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& (a+b)(aA-2bB) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 2(2ab(A-B)+a^2B-b^2(A+B)) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
& \left( d(b+a \cos[c+dx])^{3/2} \sec[c+dx]^{3/2} \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
& \left. \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right)
\end{aligned}$$

**Problem 361:** Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.



$$\int \cos [c+d x]^2 (a+b \sec [c+d x])^{3/2} (A+B \sec [c+d x]) dx$$

Optimal (type 4, 428 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{4 b d} (a-b) \sqrt{a+b} (5 A b+4 a B) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{4 d} \\ & \sqrt{a+b} (2 a A+5 A b+4 a B+8 b B) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{4 a d} \sqrt{a+b} (4 a^2 A+3 A b^2+12 a b B) \\ & \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\ & \frac{(5 A b+4 a B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 d} + \frac{a A \cos [c+d x] \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 d} \end{aligned}$$

Result (type 4, 1598 leaves):

$$\begin{aligned} & \frac{a A \cos [c+d x] (a+b \sec [c+d x])^{3/2} \sin [2(c+d x)]}{4 d (b+a \cos [c+d x])} - \\ & \left( (a+b \sec [c+d x])^{3/2} \left( 5 a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] + 5 A b^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right] + \right. \right. \\ & 4 a^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2} (c+d x) \right] + 4 a b \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2} (c+d x) \right] - \\ & 10 a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right]^3 - 8 a^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2} (c+d x) \right]^3 + \\ & 5 a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right]^5 - 5 A b^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+d x) \right]^5 + \\ & \left. 4 a^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2} (c+d x) \right]^5 - 4 a b \sqrt{\frac{-a+b}{a+b}} B \tan \left[ \frac{1}{2} (c+d x) \right]^5 \right) \end{aligned}$$

$$\begin{aligned}
& 8 \, i \, a^2 A \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \\
& \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right] + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
& 6 \, i \, A b^2 \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \\
& \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right] + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
& 24 \, i \, a b B \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \\
& \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right] + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
& 8 \, i \, a^2 A \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \tan^2 \left[ \frac{1}{2} (c+dx) \right] \\
& \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right] + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
& 6 \, i \, A b^2 \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \tan^2 \left[ \frac{1}{2} (c+dx) \right] \\
& \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right] + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - 24 \, i \, a b B \\
& \operatorname{EllipticPi} \left[ -\frac{a+b}{a-b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right] \tan^2 \left[ \frac{1}{2} (c+dx) \right] \\
& \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c+dx) \right]} \sqrt{\frac{a+b - a \tan^2 \left[ \frac{1}{2} (c+dx) \right] + b \tan^2 \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
& i (a-b) (5 A b + 4 a B) \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \tan \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a+b}{a-b} \right]
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + 2i(a-b)(2aA + b(A+4B)) \\
& \text{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
& \left(4 \sqrt{\frac{-a+b}{a+b}} d (b+a \cos[c+dx])^{3/2} \sec[c+dx]^{3/2} \sqrt{\frac{1}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
& \left. \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
& \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
\end{aligned}$$

**Problem 362: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 (a+b \sec[c+dx])^{3/2} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 520 leaves, 8 steps):

$$\begin{aligned}
& \frac{1}{24 a b d} (a-b) \sqrt{a+b} (16 a^2 A + 3 A b^2 + 30 a b B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\
& \frac{1}{24 a d} \sqrt{a+b} (16 a^2 A + 14 a A b + 3 A b^2 + 12 a^2 B + 30 a b B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\
& \frac{1}{8 a^2 d} \sqrt{a+b} (12 a^2 A b - A b^3 + 8 a^3 B + 6 a b^2 B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \\
& \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{(16 a^2 A + 3 A b^2 + 30 a b B) \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{24 a d} + \\
& \frac{(7 A b + 6 a B) \operatorname{Cos}[c+d x] \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{12 d} + \\
& \frac{a A \operatorname{Cos}[c+d x]^2 \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{3 d}
\end{aligned}$$

Result (type 4, 1551 leaves):

$$\begin{aligned}
& \left( \operatorname{Cos}[c+d x] (a+b \sec [c+d x])^{3/2} \right. \\
& \left. \left( \frac{1}{12} a A \operatorname{Sin}[c+d x] + \frac{1}{24} (7 A b + 6 a B) \operatorname{Sin}[2(c+d x)] + \frac{1}{12} a A \operatorname{Sin}[3(c+d x)] \right) \right) / \\
& \left( d (b+a \operatorname{Cos}[c+d x]) \right) + \left( (a+b \sec [c+d x])^{3/2} \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
& \left. \left( 16 a^3 A \tan\left[\frac{1}{2}(c+d x)\right] + 16 a^2 A b \tan\left[\frac{1}{2}(c+d x)\right] + 3 a A b^2 \tan\left[\frac{1}{2}(c+d x)\right] + \right. \right. \\
& \left. 3 A b^3 \tan\left[\frac{1}{2}(c+d x)\right] + 30 a^2 b B \tan\left[\frac{1}{2}(c+d x)\right] + 30 a b^2 B \tan\left[\frac{1}{2}(c+d x)\right] - \right. \\
& \left. 32 a^3 A \tan\left[\frac{1}{2}(c+d x)\right]^3 - 6 a A b^2 \tan\left[\frac{1}{2}(c+d x)\right]^3 - 60 a^2 b B \tan\left[\frac{1}{2}(c+d x)\right]^3 + \right. \\
& \left. 16 a^3 A \tan\left[\frac{1}{2}(c+d x)\right]^5 - 16 a^2 A b \tan\left[\frac{1}{2}(c+d x)\right]^5 + 3 a A b^2 \tan\left[\frac{1}{2}(c+d x)\right]^5 - \right. \\
& \left. 3 A b^3 \tan\left[\frac{1}{2}(c+d x)\right]^5 + 30 a^2 b B \tan\left[\frac{1}{2}(c+d x)\right]^5 - 30 a b^2 B \tan\left[\frac{1}{2}(c+d x)\right]^5 - \right.
\end{aligned}$$

$$\begin{aligned}
& 72 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 48 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 36 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 72 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 48 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 36 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} +
\end{aligned}$$

$$\begin{aligned}
& (a+b) \left( 16 a^2 A + 3 A b^2 + 30 a b B \right) \text{EllipticE} \left[ \text{ArcSin} \left[ \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a-b}{a+b} \right] \\
& \sqrt{1 - \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \sqrt{\frac{a+b - a \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
& 2 a \left( 12 a^2 B + b^2 (-7 A + 24 B) + a (26 A b - 6 b B) \right) \text{EllipticF} \left[ \text{ArcSin} \left[ \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \frac{a-b}{a+b} \right] \\
& \sqrt{1 - \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \sqrt{\frac{a+b - a \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} \right) \Bigg) / \\
& \left( 24 a d (b + a \cos [c+dx])^{3/2} \sec [c+dx]^{3/2} \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right)^{3/2} \right. \\
& \left. \sqrt{\frac{a+b - a \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}} \right)
\end{aligned}$$

**Problem 363: Attempted integration timed out after 120 seconds.**

$$\int \sec [c+dx]^3 (a+b \sec [c+dx])^{5/2} (A+B \sec [c+dx]) dx$$

Optimal (type 4, 566 leaves, 8 steps):

$$\begin{aligned}
& \frac{1}{3465 b^4 d} 2 (a-b) \sqrt{a+b} \left( 110 a^4 A b - 3069 a^2 A b^3 - 1617 A b^5 - 40 a^5 B - 255 a^3 b^2 B - 3705 a b^4 B \right) \\
& \cot [c+d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \\
& \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{3465 b^3 d} 2 (a-b) \sqrt{a+b} \\
& \left( 6 a b^3 (209 A - 505 B) - 3 b^4 (539 A - 225 B) - 15 a^2 b^2 (121 A - 19 B) + 40 a^4 B - a^3 (110 A b - 30 b B) \right) \\
& \cot [c+d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \\
& \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} - \frac{1}{3465 b^2 d} \\
& 2 \left( 110 a^3 A b - 1254 a A b^3 - 40 a^4 B - 285 a^2 b^2 B - 675 b^4 B \right) \sqrt{a+b \operatorname{Sec}[c+d x]} \tan [c+d x] - \\
& \frac{1}{3465 b^2 d} 2 \left( 110 a^2 A b - 539 A b^3 - 40 a^3 B - 335 a b^2 B \right) (a+b \operatorname{Sec}[c+d x])^{3/2} \tan [c+d x] - \\
& \frac{2 \left( 22 a A b - 8 a^2 B - 81 b^2 B \right) (a+b \operatorname{Sec}[c+d x])^{5/2} \tan [c+d x]}{693 b^2 d} + \\
& \frac{2 \left( 11 A b - 4 a B \right) (a+b \operatorname{Sec}[c+d x])^{7/2} \tan [c+d x]}{99 b^2 d} + \\
& \frac{2 B \operatorname{Sec}[c+d x] (a+b \operatorname{Sec}[c+d x])^{7/2} \tan [c+d x]}{11 b d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 364: Attempted integration timed out after 120 seconds.**

$$\int \operatorname{Sec}[c+d x]^2 (a+b \operatorname{Sec}[c+d x])^{5/2} (A+B \operatorname{Sec}[c+d x]) dx$$

Optimal (type 4, 469 leaves, 7 steps):

$$\begin{aligned}
& -\frac{1}{315 b^3 d} 2 (a-b) \sqrt{a+b} (45 a^3 A b + 435 a A b^3 - 10 a^4 B + 279 a^2 b^2 B + 147 b^4 B) \\
& \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \quad \sqrt{\frac{b(1-\sec[c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec[c+d x])}{a-b}} - \frac{1}{315 b^2 d} \\
& 2 (a-b) \sqrt{a+b} (3 b^3 (25 A - 49 B) - 6 a b^2 (60 A - 19 B) + 15 a^2 b (3 A - 11 B) - 10 a^3 B) \text{Cot}[c+d x] \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec[c+d x])}{a-b}} + \\
& \quad \frac{1}{315 b d} 2 (45 a^2 A b + 75 A b^3 - 10 a^3 B + 114 a b^2 B) \sqrt{a+b \sec[c+d x]} \tan[c+d x] + \\
& \quad \frac{2 (45 a A b - 10 a^2 B + 49 b^2 B) (a+b \sec[c+d x])^{3/2} \tan[c+d x]}{315 b d} + \\
& \quad \frac{2 (9 A b - 2 a B) (a+b \sec[c+d x])^{5/2} \tan[c+d x]}{63 b d} + \frac{2 B (a+b \sec[c+d x])^{7/2} \tan[c+d x]}{9 b d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 365: Attempted integration timed out after 120 seconds.**

$$\int \sec[c+d x] (a+b \sec[c+d x])^{5/2} (A+B \sec[c+d x]) dx$$

Optimal (type 4, 384 leaves, 6 steps):

$$\begin{aligned}
& -\frac{1}{105 b^2 d} 2 (a-b) \sqrt{a+b} (161 a^2 A b + 63 A b^3 + 15 a^3 B + 145 a b^2 B) \\
& \quad \text{Cot}[c+d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \quad \sqrt{\frac{b(1-\sec[c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec[c+d x])}{a-b}} + \frac{1}{105 b d} \\
& 2 (a-b) \sqrt{a+b} (b^2 (63 A - 25 B) - 8 a b (7 A - 15 B) + 15 a^2 (7 A - B)) \text{Cot}[c+d x] \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec[c+d x])}{a-b}} + \\
& \quad \frac{2 (56 a A b + 15 a^2 B + 25 b^2 B) \sqrt{a+b \sec[c+d x]} \tan[c+d x]}{105 d} + \\
& \quad \frac{2 (7 A b + 5 a B) (a+b \sec[c+d x])^{3/2} \tan[c+d x]}{35 d} + \frac{2 B (a+b \sec[c+d x])^{5/2} \tan[c+d x]}{7 d}
\end{aligned}$$

Result (type 1, 1 leaves):



???

## Problem 367: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x] (a+b \sec [c+d x])^{5/2} (A+B \sec [c+d x]) d x$$

Optimal (type 4, 433 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{3 b d} (a-b) \sqrt{a+b} (3 a^2 A-6 A b^2-14 a b B) \cot [c+d x] \\ & \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\ & \frac{1}{3 d} \sqrt{a+b} (2 a b (9 A-7 B)-2 b^2 (3 A-B)+3 a^2 (A+6 B)) \cot [c+d x] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\ & \frac{1}{d} a \sqrt{a+b} (5 A b+2 a B) \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\ & \frac{a A(a+b \sec [c+d x])^{3/2} \sin [c+d x]}{d} - \frac{b(3 a A-2 b B) \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{3 d} \end{aligned}$$

Result (type 4, 1146 leaves):

$$\begin{aligned} & \left( (a+b \sec [c+d x])^{5/2} \sqrt{\frac{1}{1-\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right. \\ & \left( 3 a^3 A \tan \left[\frac{1}{2}(c+d x)\right] + 3 a^2 A b \tan \left[\frac{1}{2}(c+d x)\right] - 6 a A b^2 \tan \left[\frac{1}{2}(c+d x)\right] - \right. \\ & 6 A b^3 \tan \left[\frac{1}{2}(c+d x)\right] - 14 a^2 b B \tan \left[\frac{1}{2}(c+d x)\right] - 14 a b^2 B \tan \left[\frac{1}{2}(c+d x)\right] - \\ & 6 a^3 A \tan \left[\frac{1}{2}(c+d x)\right]^3 + 12 a A b^2 \tan \left[\frac{1}{2}(c+d x)\right]^3 + 28 a^2 b B \tan \left[\frac{1}{2}(c+d x)\right]^3 + \\ & 3 a^3 A \tan \left[\frac{1}{2}(c+d x)\right]^5 - 3 a^2 A b \tan \left[\frac{1}{2}(c+d x)\right]^5 - 6 a A b^2 \tan \left[\frac{1}{2}(c+d x)\right]^5 + \\ & 6 A b^3 \tan \left[\frac{1}{2}(c+d x)\right]^5 - 14 a^2 b B \tan \left[\frac{1}{2}(c+d x)\right]^5 + 14 a b^2 B \tan \left[\frac{1}{2}(c+d x)\right]^5 - \\ & \left. \left. 30 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 12 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 30 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 12 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) (3 a^2 A - 6 A b^2 - 14 a b B) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2 (9 a^2 b (A-B) + 3 a^3 B - b^3 (3 A+B) - a b^2 (9 A+7 B)) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg/ \\
 & \left(3 d (b + a \cos[c+dx])^{5/2} \sec[c+dx]^{5/2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) +
 \end{aligned}$$

$$\left( \cos[c+dx]^2 (a+b \sec[c+dx])^{5/2} \left( \frac{2}{3} b (3Ab+7aB) \sin[c+dx] + \frac{2}{3} b^2 B \tan[c+dx] \right) \right) / \left( d (b+a \cos[c+dx])^2 \right)$$

**Problem 368: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^2 (a+b \sec[c+dx])^{5/2} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 450 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{4bd} (a-b) \sqrt{a+b} (9aAb+4a^2B-8b^2B) \cot[c+dx] \\ & \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \\ & \frac{1}{4d} \sqrt{a+b} (8b^2(A-B)+2a^2(A+2B)+3ab(3A+8B)) \cot[c+dx] \\ & \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} - \\ & \frac{1}{4d} \sqrt{a+b} (4a^2A+15Ab^2+20abB) \cot[c+dx] \\ & \text{EllipticPi}\left[\frac{a+b}{a}, \text{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \\ & \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{a(7Ab+4aB) \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{4d} + \\ & \frac{aA \cos[c+dx] (a+b \sec[c+dx])^{3/2} \sin[c+dx]}{2d} \end{aligned}$$

Result (type 4, 1338 leaves):

$$\begin{aligned} & \left( \cos[c+dx]^2 (a+b \sec[c+dx])^{5/2} \left( 2b^2 B \sin[c+dx] + \frac{1}{4} a^2 A \sin[2(c+dx)] \right) \right) / \\ & \left( d (b+a \cos[c+dx])^2 \right) + \left( (a+b \sec[c+dx])^{5/2} \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\ & \left( 9a^2Ab \tan\left[\frac{1}{2}(c+dx)\right] + 9aAb^2 \tan\left[\frac{1}{2}(c+dx)\right] + 4a^3B \tan\left[\frac{1}{2}(c+dx)\right] + \right. \\ & \left. \left. 4a^2bB \tan\left[\frac{1}{2}(c+dx)\right] - 8ab^2B \tan\left[\frac{1}{2}(c+dx)\right] - 8b^3B \tan\left[\frac{1}{2}(c+dx)\right] \right) \right) \end{aligned}$$

$$\begin{aligned}
& 18 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 8 a^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 16 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + \\
& 9 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 9 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 4 a^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
& 4 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 8 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 8 b^3 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
& 8 a^3 A \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 30 a A b^2 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 40 a^2 b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 8 a^3 A \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 30 a A b^2 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 40 a^2 b B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& (a+b)\left(9 a A b+4 a^2 B-8 b^2 B\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2\right)
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
 & 2\left(2a^3A-a^2b(A-12B)+12ab^2(A-B)-4b^3(A+B)\right) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \\
 & \left(4d(b+a \cos[c+dx])^{5/2} \sec[c+dx]^{5/2} \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
 & \left. \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}}\right)
 \end{aligned}$$

**Problem 369: Result more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^3 (a+b \sec[c+dx])^{5/2} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 518 leaves, 8 steps):

$$\begin{aligned}
& \frac{1}{24 b d} (a-b) \sqrt{a+b} (16 a^2 A + 33 A b^2 + 54 a b B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\
& \frac{1}{24 d} \sqrt{a+b} (16 a^2 A + 26 a A b + 33 A b^2 + 12 a^2 B + 54 a b B + 48 b^2 B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\
& \frac{1}{8 a d} \sqrt{a+b} (20 a^2 A b + 5 A b^3 + 8 a^3 B + 30 a b^2 B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \\
& \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{(16 a^2 A + 33 A b^2 + 54 a b B) \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{24 d} + \\
& \frac{a(3 A b + 2 a B) \operatorname{Cos}[c+d x] \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{4 d} + \\
& \frac{a A \operatorname{Cos}[c+d x]^2 (a+b \sec [c+d x])^{3/2} \operatorname{Sin}[c+d x]}{3 d}
\end{aligned}$$

Result (type 4, 1567 leaves):

$$\begin{aligned}
& \left( \operatorname{Cos}[c+d x]^2 (a+b \sec [c+d x])^{5/2} \right. \\
& \left. \left( \frac{1}{12} a^2 A \operatorname{Sin}[c+d x] + \frac{1}{24} a (13 A b + 6 a B) \operatorname{Sin}[2(c+d x)] + \frac{1}{12} a^2 A \operatorname{Sin}[3(c+d x)] \right) \right) / \\
& \left( d (b+a \operatorname{Cos}[c+d x])^2 \right) + \left( (a+b \sec [c+d x])^{5/2} \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
& \left. \left( 16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 33 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \right. \\
& 33 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 54 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 54 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - \\
& 32 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 66 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 108 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + \\
& 16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 33 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
& \left. \left. 33 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 54 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 54 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \right) \right)
\end{aligned}$$

$$\begin{aligned}
& 120 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 30 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 48 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 180 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 120 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 30 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 48 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 180 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& (a+b) \left(16 a^2 A + 33 A b^2 + 54 a b B\right) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right]
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + dx) \right]} \left( 1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right] \right) \\
& \sqrt{\frac{a + b - a \tan^2 \left[ \frac{1}{2} (c + dx) \right] + b \tan^2 \left[ \frac{1}{2} (c + dx) \right]}{a + b}} - \\
& 2 \left( 24 b^3 (A - B) + 12 a^3 B + a b^2 (-13 A + 72 B) + a^2 (38 A b - 6 b B) \right) \\
& \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + dx) \right] \right], \frac{a - b}{a + b} \right] \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + dx) \right]} \\
& \left( 1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right] \right) \sqrt{\frac{a + b - a \tan^2 \left[ \frac{1}{2} (c + dx) \right] + b \tan^2 \left[ \frac{1}{2} (c + dx) \right]}{a + b}} \Bigg) / \\
& \left( 24 d (b + a \cos [c + dx])^{5/2} \sec [c + dx]^{5/2} \left( 1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right] \right)^{3/2} \right. \\
& \left. \sqrt{\frac{a + b - a \tan^2 \left[ \frac{1}{2} (c + dx) \right] + b \tan^2 \left[ \frac{1}{2} (c + dx) \right]}{1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right]}} \right)
\end{aligned}$$

### Problem 371: Unable to integrate problem.

$$\int \frac{\sec [c + dx]^3 (A + B \sec [c + dx])}{\sqrt{a + b \sec [c + dx]}} dx$$

Optimal (type 4, 329 leaves, 5 steps):

$$\begin{aligned}
& \frac{1}{15 b^4 d} 2 (a - b) \sqrt{a + b} (10 a A b - 8 a^2 B - 9 b^2 B) \cot [c + dx] \\
& \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + dx]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \sec [c + dx])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + dx])}{a - b}} + \\
& \frac{1}{15 b^3 d} 2 \sqrt{a + b} (b^2 (5 A - 9 B) - 8 a^2 B + 2 a b (5 A + B)) \cot [c + dx] \\
& \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a + b \sec [c + dx]}}{\sqrt{a + b}} \right], \frac{a + b}{a - b} \right] \sqrt{\frac{b (1 - \sec [c + dx])}{a + b}} \sqrt{-\frac{b (1 + \sec [c + dx])}{a - b}} + \\
& \frac{2 (5 A b - 4 a B) \sqrt{a + b \sec [c + dx]} \tan [c + dx]}{15 b^2 d} + \frac{2 B \sec [c + dx] \sqrt{a + b \sec [c + dx]} \tan [c + dx]}{5 b d}
\end{aligned}$$

Result (type 8, 35 leaves):



$$\int \frac{\sec [c+d x]^3 (A+B \sec [c+d x])}{\sqrt{a+b \sec [c+d x]}} dx$$

Problem 372: Attempted integration timed out after 120 seconds.

$$\int \frac{\sec [c+d x]^2 (A+B \sec [c+d x])}{\sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 261 leaves, 4 steps):

$$\begin{aligned} & -\frac{1}{3 b^3 d} 2 (a-b) \sqrt{a+b} (3 A b-2 a B) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{3 b^2 d} \\ & 2 \sqrt{a+b} (3 A b-(2 a+b) B) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{2 B \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{3 b d} \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 373: Unable to integrate problem.

$$\int \frac{\sec [c+d x] (A+B \sec [c+d x])}{\sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 210 leaves, 3 steps):

$$\begin{aligned} & -\frac{1}{b^2 d} 2 (a-b) \sqrt{a+b} B \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{b d} \\ & 2 \sqrt{a+b} (A-B) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} \end{aligned}$$

Result (type 8, 33 leaves):

$$\int \frac{\sec[c+dx] (A+B \sec[c+dx])}{\sqrt{a+b \sec[c+dx]}} dx$$

**Problem 375: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx] (A+B \sec[c+dx])}{\sqrt{a+b \sec[c+dx]}} dx$$

Optimal (type 4, 348 leaves, 6 steps):

$$\begin{aligned} & \frac{1}{a b d} A (a-b) \sqrt{a+b} \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{1}{a d} A \sqrt{a+b} \cot[c+dx] \\ & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \\ & \frac{1}{a^2 d} \sqrt{a+b} (A b - 2 a B) \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \frac{A \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{a d} \end{aligned}$$

Result (type 4, 1027 leaves):

$$\begin{aligned} & \left( \sqrt{b+a \cos[c+dx]} \sqrt{\sec[c+dx]} \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\ & \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \left( a A \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + \right. \\ & A b \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right] \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} - a A \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]^3 \\ & \left. \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + A b \sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]^3 \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + \right. \\ & \left. 2 i A b \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \right) \end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 4 \, i \, a \, B \, \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 2 \, i \, A \, b \, \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 4 \, i \, a \, B \, \text{EllipticPi}\left[-\frac{a+b}{a-b}, i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \tan\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& i \, A \, (a-b) \, \text{EllipticE}\left[i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 2 \, i \, (A \, b-a \, B) \, \text{EllipticF}\left[i \, \text{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
& \left(a \sqrt{\frac{-a+b}{a+b}} d \sqrt{a+b \sec[c+dx]} \left(1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^{3/2} \right. \\
& \left. \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right)
\end{aligned}$$

**Problem 376: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c+d x]^2 (A+B \sec [c+d x])}{\sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 435 leaves, 7 steps):

$$\begin{aligned} & -\frac{1}{4 a^2 b d} (a-b) \sqrt{a+b} (3 A b-4 a B) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} -\frac{1}{4 a^2 d} \\ & \sqrt{a+b} (3 A b-2 a(A+2 B)) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} -\frac{1}{4 a^3 d} \sqrt{a+b} (4 a^2 A+3 A b^2-4 a b B) \\ & \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\ & \frac{(3 A b-4 a B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 a^2 d} +\frac{A \cos [c+d x] \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 a d} \end{aligned}$$

Result (type 4, 1639 leaves):

$$\begin{aligned} & \frac{A(b+a \cos [c+d x]) \sec [c+d x] \sin [2(c+d x)]}{4 a d \sqrt{a+b \sec [c+d x]}} + \\ & \left( \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]} \sqrt{\frac{a+b-a \tan \left[\frac{1}{2}(c+d x)\right]^2+b \tan \left[\frac{1}{2}(c+d x)\right]^2}{1+\tan \left[\frac{1}{2}(c+d x)\right]^2}} \right. \\ & \left( -3 a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right] -3 A b^2 \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right] + \right. \\ & 4 a^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[\frac{1}{2}(c+d x)\right] +4 a b \sqrt{\frac{-a+b}{a+b}} B \tan \left[\frac{1}{2}(c+d x)\right] + \\ & \left. 6 a A b \sqrt{\frac{-a+b}{a+b}} \tan \left[\frac{1}{2}(c+d x)\right]^3 -8 a^2 \sqrt{\frac{-a+b}{a+b}} B \tan \left[\frac{1}{2}(c+d x)\right]^3 - \right. \end{aligned}$$

$$\begin{aligned}
& 3 a A b \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + 3 A b^2 \sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 + \\
& 4 a^2 \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - 4 a b \sqrt{\frac{-a+b}{a+b}} B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^5 - \\
& 8 i a^2 A \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 6 i A b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 8 i a b B \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 8 i a^2 A \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 6 i A b^2 \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + 8 i a b B \\
& \operatorname{EllipticPi}\left[-\frac{a+b}{a-b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a+b}{a-b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + dx) \right]} \sqrt{\frac{a + b - a \tan^2 \left[ \frac{1}{2} (c + dx) \right] + b \tan^2 \left[ \frac{1}{2} (c + dx) \right]}{a + b}} - \\
& i (a - b) (-3Ab + 4aB) \operatorname{EllipticE} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + dx) \right] \right], \frac{a + b}{a - b} \right] \\
& \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + dx) \right]} \left( 1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right] \right) \\
& \sqrt{\frac{a + b - a \tan^2 \left[ \frac{1}{2} (c + dx) \right] + b \tan^2 \left[ \frac{1}{2} (c + dx) \right]}{a + b}} + 2 i (2a^2 A + 3Ab^2 - ab(A + 4B)) \\
& \operatorname{EllipticF} \left[ i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + dx) \right] \right], \frac{a + b}{a - b} \right] \sqrt{1 - \tan^2 \left[ \frac{1}{2} (c + dx) \right]}^2 \\
& \left( 1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right] \right) \sqrt{\frac{a + b - a \tan^2 \left[ \frac{1}{2} (c + dx) \right] + b \tan^2 \left[ \frac{1}{2} (c + dx) \right]}{a + b}} \Bigg) \Bigg/ \\
& \left( 4a^2 \sqrt{\frac{-a + b}{a + b}} d \sqrt{a + b \sec[c + dx]} \left( -1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right] \right) \sqrt{\frac{1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right]}{1 - \tan^2 \left[ \frac{1}{2} (c + dx) \right]}} \right. \\
& \left. \left( a \left( -1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right] \right) - b \left( 1 + \tan^2 \left[ \frac{1}{2} (c + dx) \right] \right) \right) \right)
\end{aligned}$$

**Problem 377: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + dx]^3 (A + B \sec[c + dx])}{\sqrt{a + b \sec[c + dx]}} dx$$

Optimal (type 4, 525 leaves, 8 steps):

$$\begin{aligned}
& \frac{1}{24 a^3 b d} (a-b) \sqrt{a+b} (16 a^2 A + 15 A b^2 - 18 a b B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\
& \frac{1}{24 a^3 d} \sqrt{a+b} (16 a^2 A - 10 a A b + 15 A b^2 + 12 a^2 B - 18 a b B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \\
& \frac{1}{8 a^4 d} \sqrt{a+b} (4 a^2 A b + 5 A b^3 - 8 a^3 B - 6 a b^2 B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \\
& \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{(16 a^2 A + 15 A b^2 - 18 a b B) \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{24 a^3 d} - \\
& \frac{(5 A b - 6 A B) \operatorname{Cos}[c+d x] \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{12 a^2 d} + \\
& \frac{A \operatorname{Cos}[c+d x]^2 \sqrt{a+b \sec [c+d x]} \operatorname{Sin}[c+d x]}{3 a d}
\end{aligned}$$

Result (type 4, 1585 leaves):

$$\begin{aligned}
& \left( (b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}[c+d x] \right. \\
& \left. \left( \frac{A \operatorname{Sin}[c+d x]}{12 a} + \frac{(-5 A b + 6 a B) \operatorname{Sin}[2(c+d x)]}{24 a^2} + \frac{A \operatorname{Sin}[3(c+d x)]}{12 a} \right) \right) / \\
& \left( d \sqrt{a+b \sec [c+d x]} \right) - \left( \sqrt{b+a \operatorname{Cos}[c+d x]} \sqrt{\sec [c+d x]} \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
& \left. \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
& \left( 16 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 16 a^2 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 15 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \\
& 15 A b^3 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 18 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - 18 a b^2 B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] - \\
& \left. 32 a^3 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 - 30 a A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + 36 a^2 b B \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^3 + \right.
\end{aligned}$$

$$\begin{aligned}
& 16 a^3 A \tan\left[\frac{1}{2}(c+dx)\right]^5 - 16 a^2 A b \tan\left[\frac{1}{2}(c+dx)\right]^5 + 15 a A b^2 \tan\left[\frac{1}{2}(c+dx)\right]^5 - \\
& 15 A b^3 \tan\left[\frac{1}{2}(c+dx)\right]^5 - 18 a^2 b B \tan\left[\frac{1}{2}(c+dx)\right]^5 + 18 a b^2 B \tan\left[\frac{1}{2}(c+dx)\right]^5 + \\
& 24 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 30 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 48 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 36 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 24 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 30 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 48 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 36 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2
\end{aligned}$$



$$\begin{aligned}
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
 & (a+b) (16 a^2 A + 15 A b^2 - 18 a b B) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
 & \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
 & \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - 2 a (5 A b^2 + 2 a b (A - 3 B) + 12 a^2 B) \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
 & \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) \Bigg/ \\
 & \left(24 a^3 d \sqrt{a+b \sec[c+dx]} \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right. \\
 & \left. \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right)
 \end{aligned}$$

**Problem 378: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sec[c+dx]^3 (A+B \sec[c+dx])}{(a+b \sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 329 leaves, 5 steps):

$$\begin{aligned}
& -\frac{1}{3 b^4 \sqrt{a+b} d} \\
& 2 \left( 6 a^2 A b - 3 A b^3 - 8 a^3 B + 5 a b^2 B \right) \cot [c+d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \\
& \sqrt{\frac{b (1 - \sec [c+d x])}{a+b}} \sqrt{-\frac{b (1 + \sec [c+d x])}{a-b}} - \frac{1}{3 b^3 \sqrt{a+b} d} \\
& 2 (2 a+b) (3 A b - (4 a+b) B) \cot [c+d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \\
& \sqrt{\frac{b (1 - \sec [c+d x])}{a+b}} \sqrt{-\frac{b (1 + \sec [c+d x])}{a-b}} - \\
& \frac{2 a^2 (A b - a B) \tan [c+d x]}{b^2 (a^2 - b^2) d \sqrt{a+b \sec [c+d x]}} + \frac{2 B \sqrt{a+b \sec [c+d x]} \tan [c+d x]}{3 b^2 d}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 379: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sec [c+d x]^2 (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{3/2}} dx$$

Optimal (type 4, 275 leaves, 4 steps):

$$\begin{aligned}
& \frac{1}{b^3 \sqrt{a+b} d} 2 (a A b - 2 a^2 B + b^2 B) \cot [c+d x] \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \\
& \sqrt{\frac{b (1 - \sec [c+d x])}{a+b}} \sqrt{-\frac{b (1 + \sec [c+d x])}{a-b}} + \frac{1}{b^2 \sqrt{a+b} d} \\
& 2 (A b - (2 a+b) B) \cot [c+d x] \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}} \right], \frac{a+b}{a-b} \right] \\
& \sqrt{\frac{b (1 - \sec [c+d x])}{a+b}} \sqrt{-\frac{b (1 + \sec [c+d x])}{a-b}} + \frac{2 a (A b - a B) \tan [c+d x]}{b (a^2 - b^2) d \sqrt{a+b \sec [c+d x]}}
\end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 380: Attempted integration timed out after 120 seconds.**

$$\int \frac{\sec [c+d x] (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{3/2}} dx$$

Optimal (type 4, 254 leaves, 4 steps):

$$\begin{aligned}
 & -\frac{1}{b^2 \sqrt{a+b} d} 2 (A b - a B) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{1}{b \sqrt{a+b} d} \\
 & 2 (A+B) \cot [c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{2 (A b - a B) \tan [c+d x]}{(a^2 - b^2) d \sqrt{a+b \sec [c+d x]}}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

**Problem 381: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec [c+d x]}{(a+b \sec [c+d x])^{3/2}} dx$$

Optimal (type 4, 376 leaves, 6 steps):

$$\begin{aligned}
 & \frac{1}{a b \sqrt{a+b} d} 2 (A b - a B) \cot [c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{1}{a b \sqrt{a+b} d} 2 (A b - a B) \cot [c+d x] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\
 & \frac{1}{a^2 d} 2 A \sqrt{a+b} \cot [c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
 & \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} + \frac{2 b (A b - a B) \tan [c+d x]}{a (a^2 - b^2) d \sqrt{a+b \sec [c+d x]}}
 \end{aligned}$$

Result (type 4, 1491 leaves):

$$\begin{aligned}
 & \left( (b+a \cos [c+d x])^2 \sec [c+d x] (A+B \sec [c+d x]) \right. \\
 & \left. \left( \frac{2 (-A b+a B) \sin [c+d x]}{a (a^2-b^2)} - \frac{2 (-A b^2 \sin [c+d x]+a b B \sin [c+d x])}{a (a^2-b^2) (b+a \cos [c+d x])} \right) \right) / \\
 & (d (B+A \cos [c+d x]) (a+b \sec [c+d x])^{3/2}) +
 \end{aligned}$$

$$\begin{aligned}
& \left( 2 (b + a \cos [c + d x])^{3/2} \sqrt{\sec [c + d x]} (A + B \sec [c + d x]) \right. \\
& \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \left( a A b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] + \right. \\
& A b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] - a^2 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right] - \\
& a b \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right] - 2 a A b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^3 + 2 a^2 \sqrt{\frac{-a + b}{a + b}} B \\
& \tan \left[ \frac{1}{2} (c + d x) \right]^3 + a A b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 - A b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& a^2 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^5 + a b \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& 2 i a^2 \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \\
& \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + \\
& 2 i A b^2 \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \\
& \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} - \\
& 2 i a^2 \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \tan \left[ \frac{1}{2} (c + d x) \right]^2 \\
& \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + \\
& 2 i A b^2 \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \tan \left[ \frac{1}{2} (c + d x) \right]^2
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& i (a-b) (-Ab + aB) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \\
& \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + i (a-b) (2Ab + a(A-B)) \\
& \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{-a+b}{a+b}} \tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a+b}{a-b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
& \left(a \sqrt{\frac{-a+b}{a+b}} (a^2 - b^2) d (B + A \cos[c+dx]) (a+b \sec[c+dx])^{3/2} \right. \\
& \left. \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2}{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
& \left. \left(a \left(-1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \right)
\end{aligned}$$

**Problem 382: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx] (A+B \sec[c+dx])}{(a+b \sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 427 leaves, 7 steps):

$$\begin{aligned}
& \frac{1}{a^2 b \sqrt{a+b} d} (a^2 A - 3 A b^2 + 2 a b B) \cot[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec[c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec[c+d x])}{a-b}} + \frac{1}{a^2 \sqrt{a+b} d} \\
& (3 A b + a(A-2 B)) \cot[c+d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec[c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec[c+d x])}{a-b}} + \frac{1}{a^3 d} \\
& \sqrt{a+b} (3 A b - 2 a B) \cot[c+d x] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec[c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec[c+d x])}{a-b}} + \\
& \frac{A \sin[c+d x]}{a d \sqrt{a+b \sec[c+d x]}} + \frac{b(a^2 A - 3 A b^2 + 2 a b B) \tan[c+d x]}{a^2 (a^2 - b^2) d \sqrt{a+b \sec[c+d x]}}
\end{aligned}$$

Result(type 4, 1613 leaves):

$$\begin{aligned}
& \left( (b+a \cos[c+d x])^2 \sec[c+d x]^2 \right. \\
& \left. \left( -\frac{2 b(A b-a B) \sin[c+d x]}{a^2(-a^2+b^2)} + \frac{2(-A b^3 \sin[c+d x]+a b^2 B \sin[c+d x])}{a^2(a^2-b^2)(b+a \cos[c+d x])} \right) \right) / \\
& (d(a+b \sec[c+d x])^{3/2}) - \left( (b+a \cos[c+d x])^{3/2} \sec[c+d x]^{3/2} \right. \\
& \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+d x)\right]^2}} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+d x)\right]^2+b \tan\left[\frac{1}{2}(c+d x)\right]^2}{1+\tan\left[\frac{1}{2}(c+d x)\right]^2}} \\
& \left( a^3 A \tan\left[\frac{1}{2}(c+d x)\right] + a^2 A b \tan\left[\frac{1}{2}(c+d x)\right] - 3 a A b^2 \tan\left[\frac{1}{2}(c+d x)\right] - \right. \\
& 3 A b^3 \tan\left[\frac{1}{2}(c+d x)\right] + 2 a^2 b B \tan\left[\frac{1}{2}(c+d x)\right] + 2 a b^2 B \tan\left[\frac{1}{2}(c+d x)\right] - \\
& 2 a^3 A \tan\left[\frac{1}{2}(c+d x)\right]^3 + 6 a A b^2 \tan\left[\frac{1}{2}(c+d x)\right]^3 - 4 a^2 b B \tan\left[\frac{1}{2}(c+d x)\right]^3 + \\
& a^3 A \tan\left[\frac{1}{2}(c+d x)\right]^5 - a^2 A b \tan\left[\frac{1}{2}(c+d x)\right]^5 - 3 a A b^2 \tan\left[\frac{1}{2}(c+d x)\right]^5 + \\
& \left. 3 A b^3 \tan\left[\frac{1}{2}(c+d x)\right]^5 + 2 a^2 b B \tan\left[\frac{1}{2}(c+d x)\right]^5 - 2 a b^2 B \tan\left[\frac{1}{2}(c+d x)\right]^5 + \right.
\end{aligned}$$

$$\begin{aligned}
& 6 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 4 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \\
& \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 4 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 6 a^2 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 6 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} - \\
& 4 a^3 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + \\
& 4 a b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]\right], \frac{a-b}{a+b}\right] \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2 \\
& \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2} \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{a+b}} + (a+b)
\end{aligned}$$

$$\begin{aligned}
& (a^2 A - 3 A b^2 + 2 a b B) \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 2 a(a+b)(-A b+a B) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1-\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) \Bigg/ \\
& \left(a^2(a^2-b^2) d(a+b \sec[c+dx])^{3/2} \sqrt{1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right. \\
& \left. \left(a\left(-1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)-b\left(1+\operatorname{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right)
\end{aligned}$$

**Problem 383: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^2 (A+B \sec[c+dx])}{(a+b \sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 531 leaves, 8 steps):



$$\begin{aligned}
& -\frac{1}{4 a^3 b \sqrt{a+b} d} \\
& (7 a^2 A b - 15 A b^3 - 4 a^3 B + 12 a b^2 B) \operatorname{Cot}[c+d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\
& \frac{1}{4 a^3 \sqrt{a+b} d} (15 A b^2 + a b (5 A - 12 B) - 2 a^2 (A + 2 B)) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \\
& \frac{1}{4 a^4 d} \sqrt{a+b} (4 a^2 A + 15 A b^2 - 12 a b B) \operatorname{Cot}[c+d x] \\
& \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec [c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\
& \sqrt{\frac{b(1-\sec [c+d x])}{a+b}} \sqrt{-\frac{b(1+\sec [c+d x])}{a-b}} - \frac{(5 A b - 4 a B) \sin [c+d x]}{4 a^2 d \sqrt{a+b \sec [c+d x]}} + \\
& \frac{A \cos [c+d x] \sin [c+d x]}{2 a d \sqrt{a+b \sec [c+d x]}} - \frac{b(7 a^2 A b - 15 A b^3 - 4 a^3 B + 12 a b^2 B) \tan [c+d x]}{4 a^3 (a^2 - b^2) d \sqrt{a+b \sec [c+d x]}}
\end{aligned}$$

Result (type 4, 47 132 leaves): Display of huge result suppressed!

### Problem 384: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^3 (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{3/2}} dx$$

Optimal (type 4, 630 leaves, 9 steps):

$$\begin{aligned}
 & \frac{1}{24 a^4 b \sqrt{a+b} d} \left( 16 a^4 A + 41 a^2 A b^2 - 105 A b^4 - 42 a^3 b B + 90 a b^3 B \right) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{1}{24 a^4 \sqrt{a+b} d} \left( 105 A b^3 + 5 a b^2 (7 A - 18 B) + 4 a^3 (4 A + 3 B) - 6 a^2 b (A + 5 B) \right) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \\
 & \frac{1}{8 a^5 d} \sqrt{a+b} \left( 12 a^2 A b + 35 A b^3 - 8 a^3 B - 30 a b^2 B \right) \operatorname{Cot}[c+d x] \\
 & \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \operatorname{Sec}[c+d x]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \sqrt{\frac{b(1-\operatorname{Sec}[c+d x])}{a+b}} \\
 & \sqrt{-\frac{b(1+\operatorname{Sec}[c+d x])}{a-b}} + \frac{(16 a^2 A + 35 A b^2 - 30 a b B) \operatorname{Sin}[c+d x]}{24 a^3 d \sqrt{a+b \operatorname{Sec}[c+d x]}} - \\
 & \frac{(7 A b - 6 a B) \operatorname{Cos}[c+d x] \operatorname{Sin}[c+d x]}{12 a^2 d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \frac{A \operatorname{Cos}[c+d x]^2 \operatorname{Sin}[c+d x]}{3 a d \sqrt{a+b \operatorname{Sec}[c+d x]}} + \\
 & \frac{b(16 a^4 A + 41 a^2 A b^2 - 105 A b^4 - 42 a^3 b B + 90 a b^3 B) \operatorname{Tan}[c+d x]}{24 a^4 (a^2 - b^2) d \sqrt{a+b \operatorname{Sec}[c+d x]}}
 \end{aligned}$$

Result (type 4, 2343 leaves):

$$\begin{aligned}
 & \left( (b+a \operatorname{Cos}[c+d x])^2 \operatorname{Sec}[c+d x]^2 \right. \\
 & \left( -\frac{(a^4 A - a^2 A b^2 + 24 A b^4 - 24 a b^3 B) \operatorname{Sin}[c+d x]}{12 a^4 (-a^2 + b^2)} - \frac{2 (A b^5 \operatorname{Sin}[c+d x] - a b^4 B \operatorname{Sin}[c+d x])}{a^4 (a^2 - b^2) (b+a \operatorname{Cos}[c+d x])} + \right. \\
 & \left. \left. \frac{(-11 A b + 6 a B) \operatorname{Sin}[2(c+d x)]}{24 a^3} + \frac{A \operatorname{Sin}[3(c+d x)]}{12 a^2} \right) \right) / (d (a+b \operatorname{Sec}[c+d x])^{3/2}) - \\
 & \left( (b+a \operatorname{Cos}[c+d x])^{3/2} \operatorname{Sec}[c+d x]^{3/2} \sqrt{\frac{1}{1-\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
 & \left. \sqrt{\frac{a+b-a \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2+b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}{1+\operatorname{Tan}\left[\frac{1}{2}(c+d x)\right]^2}} \right. \\
 & \left. \left( 16 a^5 A \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 16 a^4 A b \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + 41 a^3 A b^2 \operatorname{Tan}\left[\frac{1}{2}(c+d x)\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& 41 a^2 A b^3 \tan\left[\frac{1}{2}(c+dx)\right] - 105 a A b^4 \tan\left[\frac{1}{2}(c+dx)\right] - 105 A b^5 \tan\left[\frac{1}{2}(c+dx)\right] - \\
& 42 a^4 b B \tan\left[\frac{1}{2}(c+dx)\right] - 42 a^3 b^2 B \tan\left[\frac{1}{2}(c+dx)\right] + 90 a^2 b^3 B \tan\left[\frac{1}{2}(c+dx)\right] + \\
& 90 a b^4 B \tan\left[\frac{1}{2}(c+dx)\right] - 32 a^5 A \tan\left[\frac{1}{2}(c+dx)\right]^3 - 82 a^3 A b^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + \\
& 210 a A b^4 \tan\left[\frac{1}{2}(c+dx)\right]^3 + 84 a^4 b B \tan\left[\frac{1}{2}(c+dx)\right]^3 - 180 a^2 b^3 B \tan\left[\frac{1}{2}(c+dx)\right]^3 + \\
& 16 a^5 A \tan\left[\frac{1}{2}(c+dx)\right]^5 - 16 a^4 A b \tan\left[\frac{1}{2}(c+dx)\right]^5 + 41 a^3 A b^2 \tan\left[\frac{1}{2}(c+dx)\right]^5 - \\
& 41 a^2 A b^3 \tan\left[\frac{1}{2}(c+dx)\right]^5 - 105 a A b^4 \tan\left[\frac{1}{2}(c+dx)\right]^5 + 105 A b^5 \tan\left[\frac{1}{2}(c+dx)\right]^5 - \\
& 42 a^4 b B \tan\left[\frac{1}{2}(c+dx)\right]^5 + 42 a^3 b^2 B \tan\left[\frac{1}{2}(c+dx)\right]^5 + 90 a^2 b^3 B \tan\left[\frac{1}{2}(c+dx)\right]^5 - \\
& 90 a b^4 B \tan\left[\frac{1}{2}(c+dx)\right]^5 + 72 a^4 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right] + b \tan^2\left[\frac{1}{2}(c+dx)\right]}{a+b}} + \\
& 138 a^2 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right] + b \tan^2\left[\frac{1}{2}(c+dx)\right]}{a+b}} - \\
& 210 A b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right] + b \tan^2\left[\frac{1}{2}(c+dx)\right]}{a+b}} - \\
& 48 a^5 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right] + b \tan^2\left[\frac{1}{2}(c+dx)\right]}{a+b}} - \\
& 132 a^3 b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan^2\left[\frac{1}{2}(c+dx)\right]} \sqrt{\frac{a+b - a \tan^2\left[\frac{1}{2}(c+dx)\right] + b \tan^2\left[\frac{1}{2}(c+dx)\right]}{a+b}} + \\
& 180 a b^4 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right]
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 72 a^4 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 138 a^2 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 210 A b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 48 a^5 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 132 a^3 b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 180 a b^4 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& (a+b) (16 a^4 A + 41 a^2 A b^2 - 105 A b^4 - 42 a^3 b B + 90 a b^3 B) \\
& \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1 + \tan\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 2 a (a+b) (-35 A b^3 + 12 a^3 B - 2 a^2 b (5 A + 9 B) + 3 a b^2 (7 A + 10 B))
\end{aligned}$$

$$\begin{aligned}
& \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \\
& \left(1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) \sqrt{\frac{a+b - a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \Bigg) / \\
& \left(24 a^4 (a^2 - b^2) d (a + b \text{Sec}[c+dx])^{3/2} \sqrt{1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2} \right. \\
& \left. \left(a \left(-1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right) - b \left(1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)\right)\right)
\end{aligned}$$

Problem 385: Attempted integration timed out after 120 seconds.

$$\int \frac{\text{Sec}[c+dx]^4 (A+B \text{Sec}[c+dx])}{(a+b \text{Sec}[c+dx])^{5/2}} dx$$

Optimal (type 4, 510 leaves, 6 steps):

$$\begin{aligned}
 & - \left( 2 \left( 8 a^4 A b - 15 a^2 A b^3 + 3 A b^5 - 16 a^5 B + 28 a^3 b^2 B - 8 a b^4 B \right) \right. \\
 & \quad \left. \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\
 & \quad \left. \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / \left( 3 (a - b) b^5 (a + b)^{3/2} d \right) + \\
 & \left( 2 \left( 9 a b^3 (A - B) + b^4 (3 A - B) + 16 a^4 B - 2 a^2 b^2 (3 A + 8 B) - a^3 (8 A b - 12 b B) \right) \right. \\
 & \quad \left. \text{Cot}[c + d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\
 & \quad \left. \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / \\
 & \quad \left( 3 b^4 \sqrt{a + b} (a^2 - b^2) d \right) + \frac{2 a (A b - a B) \text{Sec}[c + d x]^2 \text{Tan}[c + d x]}{3 b (a^2 - b^2) d (a + b \text{Sec}[c + d x])^{3/2}} - \\
 & \quad \frac{2 a^2 (3 a^2 A b - 7 A b^3 - 6 a^3 B + 10 a b^2 B) \text{Tan}[c + d x]}{3 b^3 (a^2 - b^2)^2 d \sqrt{a + b \text{Sec}[c + d x]}} - \\
 & \quad \frac{2 (a A b - 2 a^2 B + b^2 B) \sqrt{a + b \text{Sec}[c + d x]} \text{Tan}[c + d x]}{3 b^3 (a^2 - b^2) d}
 \end{aligned}$$

Result(type 1, 1 leaves):

???

**Problem 386: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Sec}[c + d x]^3 (A + B \text{Sec}[c + d x])}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 417 leaves, 5 steps):

$$\begin{aligned}
& \left( 2 \left( 2 a^3 A b - 6 a A b^3 - 8 a^4 B + 15 a^2 b^2 B - 3 b^4 B \right) \right. \\
& \quad \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
& \quad \left. \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / \left( 3 (a - b) b^4 (a + b)^{3/2} d \right) + \\
& \left( 2 \left( 2 a^2 b (A - 3 B) - 3 b^3 (A - B) - 8 a^3 B + 3 a b^2 (A + 3 B) \right) \text{Cot}[c + d x] \text{EllipticF}\left[ \right. \right. \\
& \quad \left. \left. \text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b (1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b (1 + \text{Sec}[c + d x])}{a - b}} \right) / \\
& \quad \left( 3 b^3 \sqrt{a + b} (a^2 - b^2) d \right) - \frac{2 a^2 (A b - a B) \text{Tan}[c + d x]}{3 b^2 (a^2 - b^2) d (a + b \text{Sec}[c + d x])^{3/2}} + \\
& \quad \frac{2 a (2 a^2 A b - 6 A b^3 - 5 a^3 B + 9 a b^2 B) \text{Tan}[c + d x]}{3 b^2 (a^2 - b^2)^2 d \sqrt{a + b \text{Sec}[c + d x]}}
\end{aligned}$$

Result(type 1, 1 leaves):

???

**Problem 387: Attempted integration timed out after 120 seconds.**

$$\int \frac{\text{Sec}[c + d x]^2 (A + B \text{Sec}[c + d x])}{(a + b \text{Sec}[c + d x])^{5/2}} dx$$

Optimal(type 4, 387 leaves, 5 steps):

$$\begin{aligned}
& \left( 2 (a^2 A b + 3 A b^3 + 2 a^3 B - 6 a b^2 B) \cot[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\
& \quad \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3(a - b)b^3(a + b)^{3/2}d) + \\
& \left( 2 (2 a^2 B - 3 b^2 (A + B) + a b (A + 3 B)) \cot[c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\
& \quad \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3 b^2 \sqrt{a + b} (a^2 - b^2) d) + \\
& \quad \frac{2 a (A b - a B) \tan[c + d x]}{3 b (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \frac{2 (a^2 A b + 3 A b^3 + 2 a^3 B - 6 a b^2 B) \tan[c + d x]}{3 b (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}
\end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 388: Unable to integrate problem.

$$\int \frac{\operatorname{Sec}[c + d x] (A + B \operatorname{Sec}[c + d x])}{(a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 353 leaves, 5 steps):

$$\begin{aligned}
& - \left( 2 (4 a A b - a^2 B - 3 b^2 B) \cot[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\
& \quad \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3(a - b)b^2(a + b)^{3/2}d) + \\
& \left( 2 (3 a A - A b + a B - 3 b B) \cot[c + d x] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \right. \\
& \quad \left. \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \right) / (3(a - b)b(a + b)^{3/2}d) - \\
& \quad \frac{2 (A b - a B) \tan[c + d x]}{3 (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} - \frac{2 (4 a A b - a^2 B - 3 b^2 B) \tan[c + d x]}{3 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}
\end{aligned}$$

Result (type 8, 33 leaves):



$$\int \frac{\sec[c+dx] (A+B \sec[c+dx])}{(a+b \sec[c+dx])^{5/2}} dx$$

**Problem 389: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx]}{(a+b \sec[c+dx])^{5/2}} dx$$

Optimal (type 4, 495 leaves, 7 steps):

$$\begin{aligned} & \left( 2 (7 a^2 A b - 3 A b^3 - 4 a^3 B) \cot[c+dx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \right. \\ & \quad \left. \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} \right) / (3 a^2 (a-b) b (a+b)^{3/2} d) - \\ & \left( 2 (6 a^2 A b - a A b^2 - 3 A b^3 - 3 a^3 B + a^2 b B) \cot[c+dx] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \right. \right. \\ & \quad \left. \left. \frac{a+b}{a-b} \right] \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} \right) / (3 a^2 (a-b) b (a+b)^{3/2} d) - \\ & \frac{1}{a^3 d} 2 A \sqrt{a+b} \cot[c+dx] \operatorname{EllipticPi}\left[\frac{a+b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[c+dx]}}{\sqrt{a+b}}\right], \frac{a+b}{a-b}\right] \\ & \quad \sqrt{\frac{b(1-\sec[c+dx])}{a+b}} \sqrt{-\frac{b(1+\sec[c+dx])}{a-b}} + \\ & \frac{2 b (A b - a B) \tan[c+dx]}{3 a (a^2 - b^2) d (a+b \sec[c+dx])^{3/2}} + \frac{2 b (7 a^2 A b - 3 A b^3 - 4 a^3 B) \tan[c+dx]}{3 a^2 (a^2 - b^2)^2 d \sqrt{a+b \sec[c+dx]}} \end{aligned}$$

Result (type 4, 2083 leaves):

$$\begin{aligned} & \left( (b+a \cos[c+dx])^3 \sec[c+dx]^2 (A+B \sec[c+dx]) \right. \\ & \quad \left( \frac{2 (-7 a^2 A b + 3 A b^3 + 4 a^3 B) \sin[c+dx]}{3 a^2 (a^2 - b^2)^2} - \frac{2 (A b^3 \sin[c+dx] - a b^2 B \sin[c+dx])}{3 a^2 (a^2 - b^2) (b+a \cos[c+dx])^2} \right. \\ & \quad \left. \left. (2 (-8 a^2 A b^2 \sin[c+dx] + 4 A b^4 \sin[c+dx] + 5 a^3 b B \sin[c+dx] - a b^3 B \sin[c+dx])) \right) \right) / \\ & \quad \left( 3 a^2 (a^2 - b^2)^2 (b+a \cos[c+dx]) \right) \Bigg) / (d (B+A \cos[c+dx]) (a+b \sec[c+dx])^{5/2}) + \end{aligned}$$

$$\begin{aligned}
& \left( 2 \left( b + a \cos [c + d x] \right)^{5/2} \sec [c + d x]^{3/2} (A + B \sec [c + d x]) \right. \\
& \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \\
& \left( 7 a^3 A b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] + 7 a^2 A b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] - 3 a A b^3 \sqrt{\frac{-a + b}{a + b}} \right. \\
& \tan \left[ \frac{1}{2} (c + d x) \right] - 3 A b^4 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] - 4 a^4 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right] - \\
& 4 a^3 b \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right] - 14 a^3 A b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^3 + \\
& 6 a A b^3 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^3 + 8 a^4 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^3 + \\
& 7 a^3 A b \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 - 7 a^2 A b^2 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& 3 a A b^3 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 3 A b^4 \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& 4 a^4 \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^5 + 4 a^3 b \sqrt{\frac{-a + b}{a + b}} B \tan \left[ \frac{1}{2} (c + d x) \right]^5 - \\
& 6 i a^4 A \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \\
& \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} + \\
& 12 i a^2 A b^2 \operatorname{EllipticPi} \left[ -\frac{a + b}{a - b}, i \operatorname{ArcSinh} \left[ \sqrt{\frac{-a + b}{a + b}} \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a + b}{a - b} \right] \\
& \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} -
\end{aligned}$$

$$\begin{aligned}
& 6 \, i \, A \, b^4 \, \text{EllipticPi} \left[ -\frac{a+b}{a-b}, \, i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \\
& \sqrt{1 - \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
& 6 \, i \, a^4 \, A \, \text{EllipticPi} \left[ -\frac{a+b}{a-b}, \, i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
& \sqrt{1 - \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + 12 \, i \, a^2 \, A \, b^2 \\
& \text{EllipticPi} \left[ -\frac{a+b}{a-b}, \, i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
& \sqrt{1 - \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} - \\
& 6 \, i \, A \, b^4 \, \text{EllipticPi} \left[ -\frac{a+b}{a-b}, \, i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \\
& \sqrt{1 - \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \sqrt{\frac{a+b - a \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + \\
& i \, (a-b) \, (-7 \, a^2 \, A \, b + 3 \, A \, b^3 + 4 \, a^3 \, B) \, \text{EllipticE} \left[ i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \\
& \sqrt{1 - \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \\
& \sqrt{\frac{a+b - a \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} + \\
& i \, (a-b) \, (-4 \, a \, A \, b^2 - 6 \, A \, b^3 + 3 \, a^3 \, (A-B) + a^2 \, b \, (9 \, A+B)) \\
& \text{EllipticF} \left[ i \, \text{ArcSinh} \left[ \sqrt{\frac{-a+b}{a+b}} \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right] \right], \, \frac{a+b}{a-b} \right] \sqrt{1 - \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2} \\
& \left( 1 + \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 \right) \sqrt{\frac{a+b - a \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2 + b \, \text{Tan} \left[ \frac{1}{2} (c+dx) \right]^2}{a+b}} \right) \Bigg) \Bigg) /
\end{aligned}$$

$$\left( 3 a^2 \sqrt{\frac{-a+b}{a+b}} (a^2-b^2)^2 d (B+A \cos [c+d x]) (a+b \sec [c+d x])^{5/2} \right. \\ \left. \left( -1+\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) \sqrt{\frac{1+\tan \left[ \frac{1}{2} (c+d x) \right]^2}{1-\tan \left[ \frac{1}{2} (c+d x) \right]^2}} \right. \right. \\ \left. \left. \left( a \left( -1+\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) - b \left( 1+\tan \left[ \frac{1}{2} (c+d x) \right]^2 \right) \right) \right) \right)$$

**Problem 390: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c+d x] (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{5/2}} dx$$

Optimal (type 4, 582 leaves, 8 steps):

$$\begin{aligned}
& \left( 3 a^4 A - 26 a^2 A b^2 + 15 A b^4 + 14 a^3 b B - 6 a b^3 B \right) \\
& \operatorname{Cot}[c + d x] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
& \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \Bigg/ \left( 3 a^3 (a - b) b (a + b)^{3/2} d \right) - \\
& \left( 15 A b^3 + a b^2 (5 A - 6 B) - 3 a^3 (A - 4 B) - a^2 b (21 A + 2 B) \right) \operatorname{Cot}[c + d x] \\
& \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \\
& \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} \Bigg/ \left( 3 a^3 \sqrt{a + b} (a^2 - b^2) d \right) + \frac{1}{a^4 d} \\
& \sqrt{a + b} (5 A b - 2 a B) \operatorname{Cot}[c + d x] \operatorname{EllipticPi}\left[\frac{a + b}{a}, \operatorname{ArcSin}\left[\frac{\sqrt{a + b \operatorname{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
& \sqrt{\frac{b(1 - \operatorname{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \operatorname{Sec}[c + d x])}{a - b}} + \\
& \frac{A \operatorname{Sin}[c + d x]}{a d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \frac{b (3 a^2 A - 5 A b^2 + 2 a b B) \operatorname{Tan}[c + d x]}{3 a^2 (a^2 - b^2) d (a + b \operatorname{Sec}[c + d x])^{3/2}} + \\
& \frac{b (3 a^4 A - 26 a^2 A b^2 + 15 A b^4 + 14 a^3 b B - 6 a b^3 B) \operatorname{Tan}[c + d x]}{3 a^3 (a^2 - b^2)^2 d \sqrt{a + b \operatorname{Sec}[c + d x]}}
\end{aligned}$$

Result(type 4, 2390 leaves):

$$\begin{aligned}
& \left( (b + a \operatorname{Cos}[c + d x])^3 \operatorname{Sec}[c + d x]^3 \left( -\frac{2 b (-10 a^2 A b + 6 A b^3 + 7 a^3 B - 3 a b^2 B) \operatorname{Sin}[c + d x]}{3 a^3 (-a^2 + b^2)^2} + \right. \right. \\
& \frac{2 (A b^4 \operatorname{Sin}[c + d x] - a b^3 B \operatorname{Sin}[c + d x])}{3 a^3 (a^2 - b^2) (b + a \operatorname{Cos}[c + d x])^2} + (2 (-11 a^2 A b^3 \operatorname{Sin}[c + d x] + 7 A b^5 \operatorname{Sin}[c + d x] + \\
& 8 a^3 b^2 B \operatorname{Sin}[c + d x] - 4 a b^4 B \operatorname{Sin}[c + d x])) \Bigg/ (3 a^3 (a^2 - b^2)^2 (b + a \operatorname{Cos}[c + d x])) \Bigg) \Bigg/ \\
& \left( d (a + b \operatorname{Sec}[c + d x])^{5/2} \right) - \left( (b + a \operatorname{Cos}[c + d x])^{5/2} \operatorname{Sec}[c + d x]^{5/2} \sqrt{\frac{1}{1 - \operatorname{Tan}\left[\frac{1}{2} (c + d x)\right]^2}} \right)
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
& \left( 3 a^5 A \tan\left[\frac{1}{2}(c+dx)\right] + 3 a^4 A b \tan\left[\frac{1}{2}(c+dx)\right] - 26 a^3 A b^2 \tan\left[\frac{1}{2}(c+dx)\right] - \right. \\
& 26 a^2 A b^3 \tan\left[\frac{1}{2}(c+dx)\right] + 15 a A b^4 \tan\left[\frac{1}{2}(c+dx)\right] + 15 A b^5 \tan\left[\frac{1}{2}(c+dx)\right] + \\
& 14 a^4 b B \tan\left[\frac{1}{2}(c+dx)\right] + 14 a^3 b^2 B \tan\left[\frac{1}{2}(c+dx)\right] - 6 a^2 b^3 B \tan\left[\frac{1}{2}(c+dx)\right] - \\
& 6 a b^4 B \tan\left[\frac{1}{2}(c+dx)\right] - 6 a^5 A \tan\left[\frac{1}{2}(c+dx)\right]^3 + 52 a^3 A b^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 - \\
& 30 a A b^4 \tan\left[\frac{1}{2}(c+dx)\right]^3 - 28 a^4 b B \tan\left[\frac{1}{2}(c+dx)\right]^3 + 12 a^2 b^3 B \tan\left[\frac{1}{2}(c+dx)\right]^3 + \\
& 3 a^5 A \tan\left[\frac{1}{2}(c+dx)\right]^5 - 3 a^4 A b \tan\left[\frac{1}{2}(c+dx)\right]^5 - 26 a^3 A b^2 \tan\left[\frac{1}{2}(c+dx)\right]^5 + \\
& 26 a^2 A b^3 \tan\left[\frac{1}{2}(c+dx)\right]^5 + 15 a A b^4 \tan\left[\frac{1}{2}(c+dx)\right]^5 - 15 A b^5 \tan\left[\frac{1}{2}(c+dx)\right]^5 + \\
& 14 a^4 b B \tan\left[\frac{1}{2}(c+dx)\right]^5 - 14 a^3 b^2 B \tan\left[\frac{1}{2}(c+dx)\right]^5 - 6 a^2 b^3 B \tan\left[\frac{1}{2}(c+dx)\right]^5 + \\
& \left. 6 a b^4 B \tan\left[\frac{1}{2}(c+dx)\right]^5 + 30 a^4 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right. \\
& \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 60 a^2 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 30 A b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 12 a^5 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 24 a^3 b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right]
\end{aligned}$$

$$\begin{aligned}
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 12 a b^4 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 30 a^4 A b \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 60 a^2 A b^3 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 30 A b^5 \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 12 a^5 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& 24 a^3 b^2 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\
& 12 a b^4 B \operatorname{EllipticPi}\left[-1, -\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \tan\left[\frac{1}{2}(c+dx)\right]^2 \\
& \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} + \\
& (a+b) (3 a^4 A - 26 a^2 A b^2 + 15 A b^4 + 14 a^3 b B - 6 a b^3 B) \\
& \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2}
\end{aligned}$$

$$\begin{aligned} & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} - \\ & 2a(a+b) \left( 5Ab^3 + 3a^3B + 3a^2b(-2A+B) - ab^2(3A+2B) \right) \\ & \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \sqrt{1 - \tan\left[\frac{1}{2}(c+dx)\right]^2} \\ & \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \sqrt{\frac{a+b - a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right) / \\ & \left( 3a(a^3 - ab^2)^2 d (a+b \sec[c+dx])^{5/2} \sqrt{1 + \tan\left[\frac{1}{2}(c+dx)\right]^2} \right. \\ & \left. \left( a \left( -1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - b \left( 1 + \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) \end{aligned}$$

**Problem 391: Result more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c+dx]^2 (A+B \sec[c+dx])}{(a+b \sec[c+dx])^{5/2}} dx$$

Optimal (type 4, 686 leaves, 9 steps):



$$\begin{aligned}
& - \left( (33 a^4 A b - 170 a^2 A b^3 + 105 A b^5 - 12 a^5 B + 104 a^3 b^2 B - 60 a b^4 B) \right. \\
& \quad \text{Cot}[c + d x] \text{EllipticE}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
& \quad \left. \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} \right) / (12 a^4 (a - b) b (a + b)^{3/2} d) + \\
& \left( (105 A b^4 + 5 a b^3 (7 A - 12 B) + 6 a^4 (A + 2 B) - 5 a^2 b^2 (27 A + 4 B) - a^3 (27 A b - 84 b B)) \right. \\
& \quad \text{Cot}[c + d x] \text{EllipticF}\left[\text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
& \quad \left. \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} \right) / (12 a^4 \sqrt{a + b} (a^2 - b^2) d) - \\
& \frac{1}{4 a^5 d} \sqrt{a + b} (4 a^2 A + 35 A b^2 - 20 a b B) \text{Cot}[c + d x] \\
& \quad \text{EllipticPi}\left[\frac{a + b}{a}, \text{ArcSin}\left[\frac{\sqrt{a + b \text{Sec}[c + d x]}}{\sqrt{a + b}}\right], \frac{a + b}{a - b}\right] \\
& \quad \sqrt{\frac{b(1 - \text{Sec}[c + d x])}{a + b}} \sqrt{-\frac{b(1 + \text{Sec}[c + d x])}{a - b}} - \\
& \quad \frac{(7 A b - 4 a B) \text{Sin}[c + d x]}{4 a^2 d (a + b \text{Sec}[c + d x])^{3/2}} + \frac{A \text{Cos}[c + d x] \text{Sin}[c + d x]}{2 a d (a + b \text{Sec}[c + d x])^{3/2}} - \\
& \quad \frac{b(27 a^2 A b - 35 A b^3 - 12 a^3 B + 20 a b^2 B) \text{Tan}[c + d x]}{12 a^3 (a^2 - b^2) d (a + b \text{Sec}[c + d x])^{3/2}} - \\
& \quad \frac{(b(33 a^4 A b - 170 a^2 A b^3 + 105 A b^5 - 12 a^5 B + 104 a^3 b^2 B - 60 a b^4 B) \text{Tan}[c + d x])}{(12 a^4 (a^2 - b^2)^2 d \sqrt{a + b \text{Sec}[c + d x]})}
\end{aligned}$$

Result (type 4, 5217 leaves):

$$\begin{aligned}
& \left( (b + a \text{Cos}[c + d x])^3 \text{Sec}[c + d x]^3 \left( \frac{2 b^2 (-13 a^2 A b + 9 A b^3 + 10 a^3 B - 6 a b^2 B) \text{Sin}[c + d x]}{3 a^4 (-a^2 + b^2)^2} - \right. \right. \\
& \quad \frac{2 (A b^5 \text{Sin}[c + d x] - a b^4 B \text{Sin}[c + d x])}{3 a^4 (a^2 - b^2) (b + a \text{Cos}[c + d x])^2} - (2 (-14 a^2 A b^4 \text{Sin}[c + d x] + \\
& \quad 10 A b^6 \text{Sin}[c + d x] + 11 a^3 b^3 B \text{Sin}[c + d x] - 7 a b^5 B \text{Sin}[c + d x])) / \\
& \quad \left. \left. \left( 3 a^4 (a^2 - b^2)^2 (b + a \text{Cos}[c + d x]) \right) + \frac{A \text{Sin}[2 (c + d x)]}{4 a^3} \right) \right) / (d (a + b \text{Sec}[c + d x])^{5/2}) +
\end{aligned}$$

$$\begin{aligned}
& \left( (b + a \cos [c + d x])^{5/2} \left( \frac{a^2 A}{2 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} + \right. \right. \\
& \quad \frac{2 A b^2}{(a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} - \\
& \quad \frac{7 A b^4}{6 a^2 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} - \\
& \quad \frac{2 a b B}{(a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} + \\
& \quad \frac{2 b^3 B}{3 a (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]} \sqrt{\sec [c + d x]}} - \\
& \quad \frac{9 a A b \sqrt{\sec [c + d x]}}{8 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \frac{31 A b^3 \sqrt{\sec [c + d x]}}{12 a (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \\
& \quad \frac{35 A b^5 \sqrt{\sec [c + d x]}}{24 a^3 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \frac{a^2 B \sqrt{\sec [c + d x]}}{2 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \\
& \quad \frac{4 b^2 B \sqrt{\sec [c + d x]}}{3 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \frac{5 b^4 B \sqrt{\sec [c + d x]}}{6 a^2 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \\
& \quad \frac{11 a A b \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{8 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \frac{85 A b^3 \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{12 a (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \\
& \quad \frac{35 A b^5 \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{8 a^3 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \frac{a^2 B \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{2 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} - \\
& \quad \left. \frac{13 b^2 B \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{3 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} + \frac{5 b^4 B \cos [2 (c + d x)] \sqrt{\sec [c + d x]}}{2 a^2 (a^2 - b^2)^2 \sqrt{b + a \cos [c + d x]}} \right) \\
& \sec [c + d x]^{5/2} \left( \left( -33 a^4 A b + 170 a^2 A b^3 - 105 A b^5 + 12 a^5 B - 104 a^3 b^2 B + 60 a b^4 B \right) \right. \\
& \quad \tan \left[ \frac{1}{2} (c + d x) \right] \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \Big/ \\
& \quad \left( 12 a^4 (a^2 - b^2)^2 \sqrt{\frac{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right) - \left( (a + b) \left( (33 a^4 A b - 170 a^2 A b^3 + 105 A b^5 - \right. \right. \\
& \quad \left. \left. 12 a^5 B + 104 a^3 b^2 B - 60 a b^4 B) \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \tan \left[ \frac{1}{2} (c + d x) \right] \right], \frac{a - b}{a + b} \right] + \right. \right. \\
& \quad \left. \left. 2 a (6 a^4 A - 35 A b^4 + 3 a^2 b^2 (11 A - 4 B) - 3 a^3 b (3 A + 8 B) + a b^3 (21 A + 20 B) \right) \right)
\end{aligned}$$

$$\begin{aligned}
& \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + 6(a-b)^2(a+b) \\
& (4a^2A + 35Ab^2 - 20abB) \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
& \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \Bigg) / \\
& \left(12a^4(a^2-b^2)^2 \sqrt{\frac{1}{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right. \\
& \left. \left(b-b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^4+a\left(-1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right) \Bigg) / \\
& \left(d(a+b\sec[c+dx])^{5/2} \left( \left( -33a^4Ab + 170a^2Ab^3 - 105Ab^5 + 12a^5B - 104a^3b^2B + 60ab^4B \right) \right. \right. \\
& \left. \left. \sec\left[\frac{1}{2}(c+dx)\right]^2 \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right) \right) / \\
& \left(24a^4(a^2-b^2)^2 \sqrt{\frac{1+\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1-\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \right) + \\
& \left( (a+b) \left( (33a^4Ab - 170a^2Ab^3 + 105Ab^5 - 12a^5B + 104a^3b^2B - 60ab^4B) \right. \right. \\
& \left. \left. \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + \right. \right. \\
& \left. \left. 2a(6a^4A - 35Ab^4 + 3a^2b^2(11A - 4B) - 3a^3b(3A + 8B) + ab^3(21A + 20B)) \right. \right. \\
& \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + 6(a-b)^2(a+b) \right. \right. \\
& \left. \left. (4a^2A + 35Ab^2 - 20abB) \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right. \right. \\
& \left. \left. \sqrt{\frac{a+b-a\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2+b\text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right. \right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \\
& \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \left(-2b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 + \right. \\
& \left. 2a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)\right) \Bigg/ \left(12a^4(a^2-b^2)^2\right. \\
& \left. \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \left(b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)^2\right) + \\
& \left( (a+b) \left( (33a^4Ab-170a^2Ab^3+105Ab^5-12a^5B+104a^3b^2B-60ab^4B) \right. \right. \\
& \quad \text{EllipticE}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + \\
& \quad 2a(6a^4A-35Ab^4+3a^2b^2(11A-4B)-3a^3b(3A+8B)+ab^3(21A+20B)) \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + 6(a-b)^2(a+b) \\
& \quad \left. (4a^2A+35Ab^2-20abB) \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right) \\
& \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]^3 \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
& \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \Bigg/ \\
& \left(12a^4(a^2-b^2)^2 \sqrt{\frac{1}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \right. \\
& \left. \left(b-b \tan\left[\frac{1}{2}(c+dx)\right]^4+a \left(-1+\tan\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right) - \\
& \left( (33a^4Ab-170a^2Ab^3+105Ab^5-12a^5B+104a^3b^2B-60ab^4B) \right.
\end{aligned}$$

$$\begin{aligned}
& \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + \\
& 2a(6a^4A - 35Ab^4 + 3a^2b^2(11A - 4B) - 3a^3b(3A + 8B) + ab^3(21A + 20B)) \\
& \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + 6(a-b)^2(a+b) \\
& (4a^2A + 35Ab^2 - 20abB) \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \left(-a \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] + b \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right]\right) \\
& \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \Bigg/ \\
& \left(24a^4(a^2 - b^2)^2 \sqrt{\frac{1}{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \right. \\
& \left. \left(b - b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + a \left(-1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right) + \\
& \left((a+b) \left((33a^4Ab - 170a^2Ab^3 + 105Ab^5 - 12a^5B + 104a^3b^2B - 60ab^4B)\right.\right. \\
& \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + \\
& 2a(6a^4A - 35Ab^4 + 3a^2b^2(11A - 4B) - 3a^3b(3A + 8B) + ab^3(21A + 20B)) \\
& \text{EllipticF}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + 6(a-b)^2(a+b) \\
& (4a^2A + 35Ab^2 - 20abB) \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \\
& \text{Sec}\left[\frac{1}{2}(c+dx)\right]^2 \text{Tan}\left[\frac{1}{2}(c+dx)\right] \sqrt{\frac{1}{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \\
& \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \\
& \sqrt{\frac{a+b-a \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2 + b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}{1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{1 - \text{Tan}\left[\frac{1}{2}(c+dx)\right]^4} \Bigg/ \\
& \left. \left(24a^4(a^2 - b^2)^2 \left(b - b \text{Tan}\left[\frac{1}{2}(c+dx)\right]^4 + a \left(-1 + \text{Tan}\left[\frac{1}{2}(c+dx)\right]^2\right)^2\right)\right) - \right.
\end{aligned}$$

$$\begin{aligned}
& \left( (-33 a^4 A b + 170 a^2 A b^3 - 105 A b^5 + 12 a^5 B - 104 a^3 b^2 B + 60 a b^4 B) \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \left( \frac{\sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right]}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} + \right. \\
& \quad \left. \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) \right) / \\
& \quad \left. \left( 1-\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \left( 24 a^4 (a^2-b^2)^2 \left( \frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2} \right)^{3/2} \right) + \\
& \left( (-33 a^4 A b + 170 a^2 A b^3 - 105 A b^5 + 12 a^5 B - 104 a^3 b^2 B + 60 a b^4 B) \tan\left[\frac{1}{2}(c+dx)\right] \right. \\
& \quad \left( \left( -a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
& \quad \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \left( a+b - \right. \right. \\
& \quad \left. \left. a \tan\left[\frac{1}{2}(c+dx)\right]^2 + b \tan\left[\frac{1}{2}(c+dx)\right]^2 \right) \right) / \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right)^2 \right) \right) / \left( 24 a^4 \right. \\
& \quad \left. (a^2-b^2)^2 \sqrt{\frac{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}{1-\tan\left[\frac{1}{2}(c+dx)\right]^2}} \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{1+\tan\left[\frac{1}{2}(c+dx)\right]^2}} \right) - \\
& \left( (a+b) \left( (33 a^4 A b - 170 a^2 A b^3 + 105 A b^5 - 12 a^5 B + 104 a^3 b^2 B - 60 a b^4 B) \right. \right. \\
& \quad \text{EllipticE}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + \\
& \quad 2 a (6 a^4 A - 35 A b^4 + 3 a^2 b^2 (11 A - 4 B) - 3 a^3 b (3 A + 8 B) + a b^3 (21 A + 20 B)) \\
& \quad \text{EllipticF}\left[\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] + 6 (a-b)^2 (a+b) \\
& \quad \left. (4 a^2 A + 35 A b^2 - 20 a b B) \text{EllipticPi}\left[-1, -\text{ArcSin}\left[\tan\left[\frac{1}{2}(c+dx)\right]\right], \frac{a-b}{a+b}\right] \right) \\
& \quad \sqrt{\frac{a+b-a \tan\left[\frac{1}{2}(c+dx)\right]^2+b \tan\left[\frac{1}{2}(c+dx)\right]^2}{a+b}} \sqrt{1-\tan\left[\frac{1}{2}(c+dx)\right]^4} \\
& \quad \left( \left( -a \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] + b \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) / \right. \\
& \quad \left. \left( 1+\tan\left[\frac{1}{2}(c+dx)\right]^2 \right) - \left( \sec\left[\frac{1}{2}(c+dx)\right]^2 \tan\left[\frac{1}{2}(c+dx)\right] \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \Bigg/ \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \Bigg) \Bigg/ \\
 & \left( 24 a^4 (a^2 - b^2)^2 \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \right. \\
 & \left. \left( b - b \tan \left[ \frac{1}{2} (c + d x) \right]^4 + a \left( -1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right)^2 \right) \right) - \\
 & \left( (a + b) \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right. \\
 & \left. \sqrt{\frac{a + b - a \tan \left[ \frac{1}{2} (c + d x) \right]^2 + b \tan \left[ \frac{1}{2} (c + d x) \right]^2}{1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^4} \right. \\
 & \left. \left( a (6 a^4 A - 35 A b^4 + 3 a^2 b^2 (11 A - 4 B) - 3 a^3 b (3 A + 8 B) + a b^3 (21 A + 20 B)) \right. \right. \\
 & \left. \left. \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) \Bigg/ \left( \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \sqrt{1 - \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right) - \right. \\
 & \left( 3 (a - b)^2 (a + b) (4 a^2 A + 35 A b^2 - 20 a b B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right) \Bigg/ \\
 & \left( \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \left( 1 + \tan \left[ \frac{1}{2} (c + d x) \right]^2 \right) \sqrt{1 - \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right) + \\
 & \left( (33 a^4 A b - 170 a^2 A b^3 + 105 A b^5 - 12 a^5 B + 104 a^3 b^2 B - 60 a b^4 B) \sec \left[ \frac{1}{2} (c + d x) \right]^2 \right. \\
 & \left. \sqrt{1 - \frac{(a - b) \tan \left[ \frac{1}{2} (c + d x) \right]^2}{a + b}} \right) \Bigg/ \left( 2 \sqrt{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2} \right) \Bigg) \Bigg/ \\
 & \left( 12 a^4 (a^2 - b^2)^2 \sqrt{\frac{1}{1 - \tan \left[ \frac{1}{2} (c + d x) \right]^2}} \left( b - b \tan \left[ \frac{1}{2} (c + d x) \right]^4 + \right. \right.
 \end{aligned}$$





### Problem 393: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec[e+fx] (A - A \sec[e+fx])}{\sqrt{a+b \sec[e+fx]}} dx$$

Optimal (type 4, 107 leaves, 1 step):

$$\frac{1}{b^2 f} 2 A \sqrt{a-b} (a+b) \cot[e+fx] \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\frac{\sqrt{a+b \sec[e+fx]}}{\sqrt{a-b}}\right], \frac{a-b}{a+b}\right] \\ \sqrt{\frac{b(1-\sec[e+fx])}{a+b}} \sqrt{-\frac{b(1+\sec[e+fx])}{a-b}}$$

Result (type 4, 2069 leaves):

$$\frac{(b+a \cos[e+fx]) \operatorname{Csc}\left[\frac{e}{2} + \frac{fx}{2}\right]^2 (A - A \sec[e+fx]) \sin[e+fx]}{b f \sqrt{a+b \sec[e+fx]}} - \\ \left( (b+a \cos[e+fx]) \operatorname{Csc}\left[\frac{e}{2} + \frac{fx}{2}\right]^2 \sec\left[\frac{1}{2}(e+fx)\right]^4 \right. \\ \left. \left( -\frac{1}{2 \sqrt{b+a \cos[e+fx]} \sqrt{\sec[e+fx]}} - \frac{\sqrt{\sec[e+fx]}}{2 \sqrt{b+a \cos[e+fx]}} - \right. \right. \\ \left. \left. \frac{a \sqrt{\sec[e+fx]}}{2 b \sqrt{b+a \cos[e+fx]}} - \frac{a \cos[2(e+fx)] \sqrt{\sec[e+fx]}}{2 b \sqrt{b+a \cos[e+fx]}} \right) \sqrt{1+\sec[e+fx]} \right. \\ \left. (A - A \sec[e+fx]) \left( 2 \sqrt{\frac{\cos[e+fx]}{1+\cos[e+fx]}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan\left[\frac{1}{2}(e+fx)\right]\right], \frac{a-b}{a+b}\right] + \right. \right. \\ \left. \left. \sqrt{\frac{b+a \cos[e+fx]}{(a+b)(1+\cos[e+fx])}} \sec\left[\frac{1}{2}(e+fx)\right] \left( -\sin\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{3}{2}(e+fx)\right] \right) \right) \right) \right) / \\ \left( 8 b f \left( \frac{1}{1+\cos[e+fx]} \right)^{3/2} \sqrt{\frac{b+a \cos[e+fx]}{(a+b)(1+\cos[e+fx])}} \sqrt{\sec[e+fx]} \sqrt{a+b \sec[e+fx]} \right. \\ \left. \left( a \sec\left[\frac{1}{2}(e+fx)\right]^4 \sqrt{1+\sec[e+fx]} \sin[e+fx] \left( 2 \sqrt{\frac{\cos[e+fx]}{1+\cos[e+fx]}} \right. \right. \right.$$

$$\begin{aligned}
& \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right], \frac{a-b}{a+b}\right] + \sqrt{\frac{b+a \cos[e+fx]}{(a+b)(1+\cos[e+fx])}} \\
& \sec\left[\frac{1}{2}(e+fx)\right] \left(-\sin\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{3}{2}(e+fx)\right]\right) \Bigg) \Bigg) / \\
& \left(16b \left(\frac{1}{1+\cos[e+fx]}\right)^{3/2} \sqrt{b+a \cos[e+fx]} \sqrt{\frac{b+a \cos[e+fx]}{(a+b)(1+\cos[e+fx])}}\right) + \\
& \left(3 \sqrt{b+a \cos[e+fx]} \sec\left[\frac{1}{2}(e+fx)\right]^4 \sqrt{1+\sec[e+fx]} \sin[e+fx] \left(2 \sqrt{\frac{\cos[e+fx]}{1+\cos[e+fx]}}\right.\right. \\
& \left.\left.\text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right], \frac{a-b}{a+b}\right] + \sqrt{\frac{b+a \cos[e+fx]}{(a+b)(1+\cos[e+fx])}}\right.\right. \\
& \left.\left.\sec\left[\frac{1}{2}(e+fx)\right] \left(-\sin\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{3}{2}(e+fx)\right]\right)\right) \Bigg) \Bigg) / \\
& \left(16b \sqrt{\frac{1}{1+\cos[e+fx]}} \sqrt{\frac{b+a \cos[e+fx]}{(a+b)(1+\cos[e+fx])}}\right) + \\
& \left(\sqrt{b+a \cos[e+fx]} \sec\left[\frac{1}{2}(e+fx)\right]^4 \sqrt{1+\sec[e+fx]}\right. \\
& \left.\left(-\frac{a \sin[e+fx]}{(a+b)(1+\cos[e+fx])} + \frac{(b+a \cos[e+fx]) \sin[e+fx]}{(a+b)(1+\cos[e+fx])^2}\right) \left(2 \sqrt{\frac{\cos[e+fx]}{1+\cos[e+fx]}}\right.\right. \\
& \left.\left.\text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right], \frac{a-b}{a+b}\right] + \sqrt{\frac{b+a \cos[e+fx]}{(a+b)(1+\cos[e+fx])}}\right.\right. \\
& \left.\left.\sec\left[\frac{1}{2}(e+fx)\right] \left(-\sin\left[\frac{1}{2}(e+fx)\right] + \sin\left[\frac{3}{2}(e+fx)\right]\right)\right) \Bigg) \Bigg) / \\
& \left(16b \left(\frac{1}{1+\cos[e+fx]}\right)^{3/2} \left(\frac{b+a \cos[e+fx]}{(a+b)(1+\cos[e+fx])}\right)^{3/2}\right) - \\
& \left(\sqrt{b+a \cos[e+fx]} \sec\left[\frac{1}{2}(e+fx)\right]^4 \sqrt{1+\sec[e+fx]}\right. \\
& \left.\left(2 \sqrt{\frac{\cos[e+fx]}{1+\cos[e+fx]}} \text{EllipticE}\left[\text{ArcSin}\left[\text{Tan}\left[\frac{1}{2}(e+fx)\right]\right], \frac{a-b}{a+b}\right] + \right.\right.
\end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{b+a \cos [e+f x]}{(a+b)(1+\cos [e+f x])}} \sec \left[\frac{1}{2}(e+f x)\right] \left(-\sin \left[\frac{1}{2}(e+f x)\right]+\sin \left[\frac{3}{2}(e+f x)\right]\right) \\
& \tan \left[\frac{1}{2}(e+f x)\right] \left/ \left(4 b \left(\frac{1}{1+\cos [e+f x]}\right)^{3/2} \sqrt{\frac{b+a \cos [e+f x]}{(a+b)(1+\cos [e+f x])}}\right)-\right. \\
& \frac{1}{8 b \left(\frac{1}{1+\cos [e+f x]}\right)^{3/2} \sqrt{\frac{b+a \cos [e+f x]}{(a+b)(1+\cos [e+f x])}}} \sqrt{b+a \cos [e+f x]} \\
& \sec \left[\frac{1}{2}(e+f x)\right]^4 \sqrt{1+\sec [e+f x]} \\
& \left(\sqrt{\frac{b+a \cos [e+f x]}{(a+b)(1+\cos [e+f x])}} \left(-\frac{1}{2} \cos \left[\frac{1}{2}(e+f x)\right]+\frac{3}{2} \cos \left[\frac{3}{2}(e+f x)\right]\right)\right. \\
& \sec \left[\frac{1}{2}(e+f x)\right]+\frac{1}{\sqrt{\frac{\cos [e+f x]}{1+\cos [e+f x]}}} \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(e+f x)\right]\right], \frac{a-b}{a+b}\right] \\
& \left(\frac{\cos [e+f x] \sin [e+f x]}{(1+\cos [e+f x])^2}-\frac{\sin [e+f x]}{1+\cos [e+f x]}\right)+ \\
& \left(\sec \left[\frac{1}{2}(e+f x)\right] \left(-\frac{a \sin [e+f x]}{(a+b)(1+\cos [e+f x])}+\frac{(b+a \cos [e+f x]) \sin [e+f x]}{(a+b)(1+\cos [e+f x])^2}\right)\right. \\
& \left.\left(-\sin \left[\frac{1}{2}(e+f x)\right]+\sin \left[\frac{3}{2}(e+f x)\right]\right)\right) \left/ \left(2 \sqrt{\frac{b+a \cos [e+f x]}{(a+b)(1+\cos [e+f x])}}\right)+\right. \\
& \frac{1}{2} \sqrt{\frac{b+a \cos [e+f x]}{(a+b)(1+\cos [e+f x])}} \sec \left[\frac{1}{2}(e+f x)\right] \left(-\sin \left[\frac{1}{2}(e+f x)\right]+\sin \left[\frac{3}{2}(e+f x)\right]\right) \\
& \tan \left[\frac{1}{2}(e+f x)\right]+\frac{\sqrt{\frac{\cos [e+f x]}{1+\cos [e+f x]}} \sec \left[\frac{1}{2}(e+f x)\right]^2 \sqrt{1-\frac{(a-b) \tan \left[\frac{1}{2}(e+f x)\right]^2}{a+b}}}{\sqrt{1-\tan \left[\frac{1}{2}(e+f x)\right]^2}} \left. \right) - \\
& \left(\sqrt{b+a \cos [e+f x]} \sec \left[\frac{1}{2}(e+f x)\right]^4 \sec [e+f x] \left(2 \sqrt{\frac{\cos [e+f x]}{1+\cos [e+f x]}}\right.\right. \\
& \left.\left.\operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\tan \left[\frac{1}{2}(e+f x)\right]\right], \frac{a-b}{a+b}\right]+\sqrt{\frac{b+a \cos [e+f x]}{(a+b)(1+\cos [e+f x])}}\right)\right)
\end{aligned}$$



$$\begin{aligned}
& -\frac{1}{30 b^3 d} \left( - \left( \left( 2 \left( -40 a A b^2 + 40 a^2 b B + 18 b^3 B \right) \cos [c + d x]^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} \left[ \sqrt{\sec [c + d x]} \right] \right], \right. \right. \right. \\
& \quad \left. \left. -1 \right) \left( a + b \sec [c + d x] \right) \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / \\
& \quad \left( a \left( b + a \cos [c + d x] \right) \left( 1 - \cos [c + d x]^2 \right) \right) + \\
& \quad \left( 2 \left( -45 a^2 A b - 10 A b^3 + 45 a^3 B + 19 a b^2 B \right) \cos [c + d x]^2 \left( \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\sec [c + d x]} \right] \right], \right. \right. \\
& \quad \left. \left. -1 \right] + \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} \left[ \sqrt{\sec [c + d x]} \right] \right], -1 \right) \left( a + b \sec [c + d x] \right) \\
& \quad \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) / \left( b \left( b + a \cos [c + d x] \right) \left( 1 - \cos [c + d x]^2 \right) \right) - \\
& \quad \left( 2 \left( -15 a^2 A b + 15 a^3 B + 9 a b^2 B \right) \cos [2 (c + d x)] \left( a + b \sec [c + d x] \right) \right. \\
& \quad \left( 2 a b - 2 a b \sec [c + d x]^2 + 2 a b \operatorname{EllipticE} \left[ \operatorname{ArcSin} \left[ \sqrt{\sec [c + d x]} \right] \right], -1 \right) \sqrt{\sec [c + d x]} \\
& \quad \sqrt{1 - \sec [c + d x]^2} + a \left( a - 2 b \right) \operatorname{EllipticF} \left[ \operatorname{ArcSin} \left[ \sqrt{\sec [c + d x]} \right] \right], -1 \right) \sqrt{\sec [c + d x]} \\
& \quad \sqrt{1 - \sec [c + d x]^2} + a^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} \left[ \sqrt{\sec [c + d x]} \right] \right], -1 \right) \sqrt{\sec [c + d x]} \\
& \quad \sqrt{1 - \sec [c + d x]^2} - 2 b^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} \left[ \sqrt{\sec [c + d x]} \right] \right], -1 \right) \\
& \quad \left. \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} \right) \sin [c + d x] \right) / \\
& \quad \left( a^2 b \left( b + a \cos [c + d x] \right) \left( 1 - \cos [c + d x]^2 \right) \sqrt{\sec [c + d x]} \left( 2 - \sec [c + d x]^2 \right) \right) + \\
& \quad \frac{1}{d} \sqrt{\sec [c + d x]} \left( \frac{2 \left( -5 a A b + 5 a^2 B + 3 b^2 B \right) \sin [c + d x]}{5 b^3} + \right. \\
& \quad \frac{2 \sec [c + d x] \left( A b \sin [c + d x] - a B \sin [c + d x] \right)}{3 b^2} + \\
& \quad \left. \frac{2 B \sec [c + d x] \tan [c + d x]}{5 b} \right)
\end{aligned}$$

**Problem 420: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x]}{\sec [c + d x]^{3/2} (a + b \sec [c + d x])} dx$$

Optimal (type 4, 196 leaves, 9 steps):

$$\begin{aligned}
& -\frac{1}{a^2 d} 2 (A b - a B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \frac{1}{3 a^3 d} \\
& 2 (a^2 A + 3 A b^2 - 3 a b B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} - \\
& \frac{1}{a^3 (a+b) d} 2 b^2 (A b - a B) \sqrt{\cos[c+dx]} \operatorname{EllipticPi}\left[\frac{2a}{a+b}, \frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\
& \frac{2 A \sin[c+dx]}{3 a d \sqrt{\sec[c+dx]}}
\end{aligned}$$

Result (type 4, 545 leaves):

$$\begin{aligned}
& -\frac{1}{6 a d} \left( \left( 4 A \cos[c+dx]^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec[c+dx]}\right], -1\right] (a+b \sec[c+dx]) \right. \right. \\
& \quad \left. \left. \sqrt{1-\sec[c+dx]^2} \sin[c+dx] \right) \right) / \left( (b+a \cos[c+dx]) (1-\cos[c+dx]^2) \right) + \\
& \left( 2 (A b - 3 a B) \cos[c+dx]^2 \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec[c+dx]}\right], -1\right] + \right. \right. \\
& \quad \left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec[c+dx]}\right], -1\right] \right) (a+b \sec[c+dx]) \right. \\
& \quad \left. \sqrt{1-\sec[c+dx]^2} \sin[c+dx] \right) / \left( (b(b+a \cos[c+dx]) (1-\cos[c+dx]^2)) \right) - \\
& \left( 2 (3 A b - 3 a B) \cos[2(c+dx)] (a+b \sec[c+dx]) \left( 2 a b - 2 a b \sec[c+dx]^2 + \right. \right. \\
& \quad 2 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\sec[c+dx]}\right], -1\right] \sqrt{\sec[c+dx]} \sqrt{1-\sec[c+dx]^2} + \\
& \quad a (a-2 b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec[c+dx]}\right], -1\right] \sqrt{\sec[c+dx]} \sqrt{1-\sec[c+dx]^2} + \\
& \quad a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec[c+dx]}\right], -1\right] \sqrt{\sec[c+dx]} \sqrt{1-\sec[c+dx]^2} - \\
& \quad \left. \left. 2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec[c+dx]}\right], -1\right] \sqrt{\sec[c+dx]} \sqrt{1-\sec[c+dx]^2} \right) \right. \\
& \quad \left. \sin[c+dx] \right) / \left( a^2 b (b+a \cos[c+dx]) (1-\cos[c+dx]^2) \sqrt{\sec[c+dx]} \right. \\
& \quad \left. (2-\sec[c+dx]^2) \right) + \frac{A \sqrt{\sec[c+dx]} \sin[2(c+dx)]}{3 a d}
\end{aligned}$$

**Problem 421: Result more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c+dx]}{\sec[c+dx]^{5/2} (a+b \sec[c+dx])} dx$$

Optimal (type 4, 242 leaves, 10 steps):

$$\begin{aligned} & \frac{1}{5 a^3 d} 2 (3 a^2 A + 5 A b^2 - 5 a b B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} - \\ & \frac{1}{3 a^4 d} 2 (a^2 + 3 b^2) (A b - a B) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\ & \frac{1}{a^4 (a+b) d} 2 b^3 (A b - a B) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right] \sqrt{\sec [c+d x]} + \\ & \frac{2 A \sin [c+d x]}{5 a d \sec [c+d x]^{3/2}} - \frac{2 (A b - a B) \sin [c+d x]}{3 a^2 d \sqrt{\sec [c+d x]}} \end{aligned}$$

Result(type 4, 617 leaves):

$$\begin{aligned} & \frac{1}{30 a^2 d} \left( - \left( \left( 2 (8 a A b + 10 a^2 B) \cos [c+d x]^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \right. \right. \right. \\ & \quad \left. \left. \left( a + b \sec [c+d x] \right) \sqrt{1 - \sec [c+d x]^2} \sin [c+d x] \right) \right) / \\ & \quad \left( a (b + a \cos [c+d x]) (1 - \cos [c+d x]^2) \right) \right) + \\ & \quad \left( 2 (9 a^2 A + 5 A b^2 - 5 a b B) \cos [c+d x]^2 \left( \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] + \right. \right. \\ & \quad \left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \right) (a + b \sec [c+d x]) \right. \\ & \quad \left. \sqrt{1 - \sec [c+d x]^2} \sin [c+d x] \right) / \left( b (b + a \cos [c+d x]) (1 - \cos [c+d x]^2) \right) - \\ & \quad \left( 2 (9 a^2 A + 15 A b^2 - 15 a b B) \cos [2(c+d x)] (a + b \sec [c+d x]) \left( 2 a b - 2 a b \sec [c+d x]^2 + \right. \right. \\ & \quad \left. \left. 2 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \sqrt{\sec [c+d x]} \sqrt{1 - \sec [c+d x]^2} + \right. \right. \\ & \quad \left. \left. a (a - 2 b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \sqrt{\sec [c+d x]} \sqrt{1 - \sec [c+d x]^2} + \right. \right. \\ & \quad \left. \left. a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \sqrt{\sec [c+d x]} \sqrt{1 - \sec [c+d x]^2} - \right. \right. \\ & \quad \left. \left. 2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}\left[\sqrt{\sec [c+d x]}\right], -1\right] \sqrt{\sec [c+d x]} \sqrt{1 - \sec [c+d x]^2} \right) \right. \\ & \quad \left. \sin [c+d x] \right) / \left( a^2 b (b + a \cos [c+d x]) (1 - \cos [c+d x]^2) \right. \\ & \quad \left. \sqrt{\sec [c+d x]} (2 - \sec [c+d x]^2) \right) \right) + \\ & \quad \frac{\sqrt{\sec [c+d x]} \left( \frac{A \sin [c+d x]}{10 a} + \frac{(-A b + a B) \sin [2(c+d x)]}{3 a^2} + \frac{A \sin [3(c+d x)]}{10 a} \right)}{d} \end{aligned}$$

**Problem 423: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sec [c+d x]^{5/2} (A + B \sec [c+d x])}{(a + b \sec [c+d x])^2} dx$$

Optimal (type 4, 315 leaves, 10 steps):

$$\frac{1}{b^2 (a^2 - b^2) d} (a A b - 3 a^2 B + 2 b^2 B) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\sec [c + d x]} +$$

$$\frac{(A b - a B) \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\sec [c + d x]}}{b (a^2 - b^2) d} +$$

$$\left( (a^2 A b - 3 A b^3 - 3 a^3 B + 5 a b^2 B) \sqrt{\cos [c + d x]} \right.$$

$$\left. \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2} (c + d x), 2\right] \sqrt{\sec [c + d x]} \right) / \left( (a - b) b^2 (a + b)^2 d \right) -$$

$$\frac{(a A b - 3 a^2 B + 2 b^2 B) \sqrt{\sec [c + d x]} \sin [c + d x]}{b^2 (a^2 - b^2) d} + \frac{a (A b - a B) \sec [c + d x]^{3/2} \sin [c + d x]}{b (a^2 - b^2) d (a + b \sec [c + d x])}$$

Result (type 4, 685 leaves):

$$-\frac{1}{4 (a - b) b^2 (a + b) d}$$

$$\left( - \left( \left( 2 (-4 a A b^2 + 8 a^2 b B - 4 b^3 B) \cos [c + d x]^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec [c + d x]}], -1\right] \right. \right. \right.$$

$$\left. \left. (a + b \sec [c + d x]) \sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \right) \right) /$$

$$\left( a (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \right) +$$

$$\left( 2 (-3 a^2 A b + 4 A b^3 + 9 a^3 B - 10 a b^2 B) \cos [c + d x]^2 \left( \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\sec [c + d x]}], \right. \right.$$

$$\left. -1\right] + \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec [c + d x]}], -1\right] \right) (a + b \sec [c + d x])$$

$$\sqrt{1 - \sec [c + d x]^2} \sin [c + d x] \Big) / \left( b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \right) -$$

$$\left( 2 (-a^2 A b + 3 a^3 B - 2 a b^2 B) \cos [2 (c + d x)] (a + b \sec [c + d x]) \left( 2 a b - 2 a b \sec [c + d x]^2 + \right. \right.$$

$$2 a b \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} +$$

$$a (a - 2 b) \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\sec [c + d x]}], -1] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} +$$

$$a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec [c + d x]}], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} -$$

$$2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec [c + d x]}], -1\right] \sqrt{\sec [c + d x]} \sqrt{1 - \sec [c + d x]^2} \Big)$$

$$\sin [c + d x] \Big) / \left( a^2 b (b + a \cos [c + d x]) (1 - \cos [c + d x]^2) \right.$$

$$\left. \sqrt{\sec [c + d x]} (2 - \sec [c + d x]^2) \right) +$$

$$\frac{\sqrt{\sec [c + d x]} \left( \frac{(a A b - 3 a^2 B + 2 b^2 B) \sin [c + d x]}{b^2 (-a^2 + b^2)} + \frac{-a A b \sin [c + d x] + a^2 B \sin [c + d x]}{b (-a^2 + b^2) (b + a \cos [c + d x])} \right)}{d}$$



### Problem 424: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec[c+dx]^{3/2} (A+B \sec[c+dx])}{(a+b \sec[c+dx])^2} dx$$

Optimal (type 4, 257 leaves, 9 steps):

$$\begin{aligned} & - \frac{(Ab - aB) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{b(a^2 - b^2)d} - \\ & \frac{(Ab - aB) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]}}{a(a^2 - b^2)d} + \\ & \left( (a^2 Ab + Ab^3 + a^3 B - 3ab^2 B) \sqrt{\cos[c+dx]} \operatorname{EllipticPi}\left[\frac{2a}{a+b}, \frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} \right) / \\ & (a(a-b)b(a+b)^2 d) + \frac{a(Ab - aB) \sqrt{\sec[c+dx]} \sin[c+dx]}{b(a^2 - b^2)d(a+b \sec[c+dx])} \end{aligned}$$

Result (type 4, 643 leaves):

$$\begin{aligned}
& \frac{1}{4 b (-a+b) (a+b) d} \\
& \left( - \left( \left( 2 (4 A b^2 - 4 a b B) \cos [c+d x]^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right] \right. \right. \\
& \quad \left. \left. (a+b \sec [c+d x]) \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) \right) / \\
& \quad \left( a (b+a \cos [c+d x]) (1-\cos [c+d x]^2) \right) + \\
& \quad \left( 2 (-a A b - 3 a^2 B + 4 b^2 B) \cos [c+d x]^2 \left( \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) + \right. \\
& \quad \left. \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) (a+b \sec [c+d x]) \\
& \quad \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) / (b (b+a \cos [c+d x]) (1-\cos [c+d x]^2)) - \\
& \quad \left( 2 (a A b - a^2 B) \cos [2 (c+d x)] (a+b \sec [c+d x]) \left( 2 a b - 2 a b \sec [c+d x]^2 + \right. \right. \\
& \quad \left. \left. 2 a b \operatorname{EllipticE} [\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \\
& \quad a (a-2 b) \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \\
& \quad a^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} - \\
& \quad \left. 2 b^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} \right) \\
& \quad \sin [c+d x] \Big) / \left( a^2 b (b+a \cos [c+d x]) (1-\cos [c+d x]^2) \right. \\
& \quad \left. \sqrt{\sec [c+d x]} (2-\sec [c+d x]^2) \right) + \\
& \quad \frac{\sqrt{\sec [c+d x]} \left( -\frac{(A b-a B) \sin [c+d x]}{b (-a^2+b^2)} + \frac{A b \sin [c+d x]-a B \sin [c+d x]}{(-a^2+b^2) (b+a \cos [c+d x])} \right)}{d}
\end{aligned}$$

**Problem 425: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec [c+d x]} (A+B \sec [c+d x])}{(a+b \sec [c+d x])^2} dx$$

Optimal (type 4, 263 leaves, 9 steps):

$$\begin{aligned}
& \frac{(A b - a B) \sqrt{\cos [c+d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c+d x), 2 \right] \sqrt{\sec [c+d x]}}{a (a^2 - b^2) d} + \frac{1}{a^2 (a^2 - b^2) d} \\
& (2 a^2 A - A b^2 - a b B) \sqrt{\cos [c+d x]} \operatorname{EllipticF} \left[ \frac{1}{2} (c+d x), 2 \right] \sqrt{\sec [c+d x]} - \\
& \left( (3 a^2 A b - A b^3 - a^3 B - a b^2 B) \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[ \frac{2 a}{a+b}, \frac{1}{2} (c+d x), 2 \right] \sqrt{\sec [c+d x]} \right) / \\
& \left( a^2 (a-b) (a+b)^2 d \right) - \frac{(A b - a B) \sqrt{\sec [c+d x]} \sin [c+d x]}{(a^2 - b^2) d (a+b \sec [c+d x])}
\end{aligned}$$

Result (type 4, 727 leaves):

$$\begin{aligned}
 & \frac{1}{4 (a-b) (a+b) d (B+A \cos [c+d x]) (a+b \sec [c+d x])^2} \\
 & \left( (b+a \cos [c+d x])^2 \sec [c+d x] (A+B \sec [c+d x]) \right. \\
 & \left( - \left( \left( 2 (4 a A - 4 b B) \cos [c+d x]^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right] \right. \right. \\
 & \left. \left. (a+b \sec [c+d x]) \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) \right) / \\
 & \left( a (b+a \cos [c+d x]) (1-\cos [c+d x]^2) \right) + \\
 & \left( 2 (-A b + a B) \cos [c+d x]^2 \left( \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c+d x]}], -1 \right] + \right. \\
 & \left. \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) (a+b \sec [c+d x]) \\
 & \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) / (b (b+a \cos [c+d x]) (1-\cos [c+d x]^2)) - \\
 & \left( 2 (A b - a B) \cos [2 (c+d x)] (a+b \sec [c+d x]) \left( 2 a b - 2 a b \sec [c+d x]^2 + \right. \right. \\
 & 2 a b \operatorname{EllipticE} [\operatorname{ArcSin} [\sqrt{\sec [c+d x]}], -1] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \\
 & a (a-2 b) \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c+d x]}], -1] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} + \\
 & a^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} - \\
 & \left. 2 b^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1] \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} \right) \\
 & \left. \sin [c+d x] \right) / (a^2 b (b+a \cos [c+d x]) (1-\cos [c+d x]^2)) \\
 & \left. \sqrt{\sec [c+d x]} (2-\sec [c+d x]^2) \right) + \\
 & \left( (b+a \cos [c+d x])^2 \sec [c+d x]^{3/2} (A+B \sec [c+d x]) \right. \\
 & \left. \left( \frac{(-A b + a B) \sin [c+d x]}{a (a^2 - b^2)} + \frac{A b^2 \sin [c+d x] - a b B \sin [c+d x]}{a (a^2 - b^2) (b+a \cos [c+d x])} \right) \right) / \\
 & (d (B+A \cos [c+d x]) (a+b \sec [c+d x])^2)
 \end{aligned}$$

**Problem 426: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec [c+d x]}{\sqrt{\sec [c+d x]} (a+b \sec [c+d x])^2} dx$$

Optimal (type 4, 283 leaves, 9 steps):

$$\frac{1}{a^2 (a^2 - b^2) d} \left( (2 a^2 A - 3 A b^2 + a b B) \sqrt{\cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\sec[c + d x]} - \frac{1}{a^3 (a^2 - b^2) d} \right. \\ \left. (4 a^2 A b - 3 A b^3 - 2 a^3 B + a b^2 B) \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \sqrt{\sec[c + d x]} + \right. \\ \left. \left( b (5 a^2 A b - 3 A b^3 - 3 a^3 B + a b^2 B) \sqrt{\cos[c + d x]} \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2} (c + d x), 2\right] \right. \right. \\ \left. \left. \sqrt{\sec[c + d x]} \right) \right) / \left( a^3 (a - b) (a + b)^2 d \right) + \frac{b (A b - a B) \sqrt{\sec[c + d x]} \sin[c + d x]}{a (a^2 - b^2) d (a + b \sec[c + d x])}$$

Result (type 4, 657 leaves):

$$\frac{1}{4 a (-a + b) (a + b) d} \left( - \left( \left( 2 (4 a A b - 4 a^2 B) \cos[c + d x]^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c + d x]}], -1\right] \right. \right. \right. \\ \left. \left. \left( a + b \sec[c + d x] \right) \sqrt{1 - \sec[c + d x]^2} \sin[c + d x] \right) \right) / \left( a (b + a \cos[c + d x]) (1 - \cos[c + d x]^2) \right) + \\ \left( 2 (-2 a^2 A + A b^2 + a b B) \cos[c + d x]^2 \left( \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\sec[c + d x]}], -1] + \right. \right. \\ \left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c + d x]}], -1\right] \right) (a + b \sec[c + d x]) \right. \\ \left. \sqrt{1 - \sec[c + d x]^2} \sin[c + d x] \right) / \left( b (b + a \cos[c + d x]) (1 - \cos[c + d x]^2) \right) - \\ \left( 2 (-2 a^2 A + 3 A b^2 - a b B) \cos[2 (c + d x)] (a + b \sec[c + d x]) \left( 2 a b - 2 a b \sec[c + d x]^2 + \right. \right. \\ \left. \left. 2 a b \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{\sec[c + d x]}], -1] \sqrt{\sec[c + d x]} \sqrt{1 - \sec[c + d x]^2} + \right. \right. \\ \left. \left. a (a - 2 b) \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\sec[c + d x]}], -1] \sqrt{\sec[c + d x]} \sqrt{1 - \sec[c + d x]^2} + \right. \right. \\ \left. \left. a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c + d x]}], -1\right] \sqrt{\sec[c + d x]} \sqrt{1 - \sec[c + d x]^2} - \right. \right. \\ \left. \left. 2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c + d x]}], -1\right] \sqrt{\sec[c + d x]} \sqrt{1 - \sec[c + d x]^2} \right) \right. \\ \left. \sin[c + d x] \right) / \left( a^2 b (b + a \cos[c + d x]) (1 - \cos[c + d x]^2) \right. \\ \left. \sqrt{\sec[c + d x]} (2 - \sec[c + d x]^2) \right) + \\ \frac{\sqrt{\sec[c + d x]} \left( -\frac{b (A b - a B) \sin[c + d x]}{a^2 (-a^2 + b^2)} + \frac{-A b^3 \sin[c + d x] + a b^2 B \sin[c + d x]}{a^2 (a^2 - b^2) (b + a \cos[c + d x])} \right)}{d}$$

### Problem 431: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec[c+dx]^{3/2} (A+B \sec[c+dx])}{(a+b \sec[c+dx])^3} dx$$

Optimal (type 4, 402 leaves, 10 steps):

$$\begin{aligned} & -\frac{1}{4ab(a^2-b^2)^2d} (5a^2Ab + Ab^3 - a^3B - 5ab^2B) \\ & \quad \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} - \frac{1}{4a^2(a^2-b^2)^2d} \\ & \quad (7a^2Ab - Ab^3 - 3a^3B - 3ab^2B) \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} + \\ & \quad \left( (3a^4Ab + 10a^2Ab^3 - Ab^5 + a^5B - 10a^3b^2B - 3ab^4B) \right. \\ & \quad \left. \sqrt{\cos[c+dx]} \operatorname{EllipticPi}\left[\frac{2a}{a+b}, \frac{1}{2}(c+dx), 2\right] \sqrt{\sec[c+dx]} \right) / \\ & \quad (4a^2(a-b)^2b(a+b)^3d) + \frac{a(Ab - aB) \sqrt{\sec[c+dx]} \sin[c+dx]}{2b(a^2-b^2)d(a+b \sec[c+dx])^2} + \\ & \quad \frac{(3a^2Ab + 3Ab^3 + a^3B - 7ab^2B) \sqrt{\sec[c+dx]} \sin[c+dx]}{4b(a^2-b^2)^2d(a+b \sec[c+dx])} \end{aligned}$$

Result (type 4, 887 leaves):

$$\begin{aligned}
& \frac{1}{16 (a-b)^2 b (a+b)^2 d (B+A \cos[c+dx]) (a+b \sec[c+dx])^3} \\
& \left( (b+a \cos[c+dx])^3 \sec[c+dx]^2 (A+B \sec[c+dx]) \right. \\
& \left( - \left( \left( 2 (-24 a A b^2 + 8 a^2 b B + 16 b^3 B) \cos[c+dx]^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c+dx]}]\right], \right. \right. \right. \\
& \left. \left. \left. -1 \right) (a+b \sec[c+dx]) \sqrt{1-\sec[c+dx]^2} \sin[c+dx] \right) \right) / \\
& \left( a (b+a \cos[c+dx]) (1-\cos[c+dx]^2) \right) \Bigg) + \\
& \left( 2 (a^2 A b + 5 A b^3 + 3 a^3 B - 9 a b^2 B) \cos[c+dx]^2 \left( \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\sec[c+dx]}], -1] + \right. \right. \\
& \left. \left. \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c+dx]}], -1\right] \right) (a+b \sec[c+dx]) \right. \\
& \left. \sqrt{1-\sec[c+dx]^2} \sin[c+dx] \right) / \left( b (b+a \cos[c+dx]) (1-\cos[c+dx]^2) \right) - \\
& \left( 2 (-5 a^2 A b - A b^3 + a^3 B + 5 a b^2 B) \cos[2(c+dx)] (a+b \sec[c+dx]) \right. \\
& \left( 2 a b - 2 a b \sec[c+dx]^2 + 2 a b \operatorname{EllipticE}[\operatorname{ArcSin}[\sqrt{\sec[c+dx]}], -1] \sqrt{\sec[c+dx]} \right. \\
& \left. \sqrt{1-\sec[c+dx]^2} + a (a-2b) \operatorname{EllipticF}[\operatorname{ArcSin}[\sqrt{\sec[c+dx]}], -1] \sqrt{\sec[c+dx]} \right. \\
& \left. \sqrt{1-\sec[c+dx]^2} + a^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c+dx]}], -1\right] \sqrt{\sec[c+dx]} \right. \\
& \left. \sqrt{1-\sec[c+dx]^2} - 2 b^2 \operatorname{EllipticPi}\left[-\frac{b}{a}, -\operatorname{ArcSin}[\sqrt{\sec[c+dx]}], -1\right] \right. \\
& \left. \left. \sqrt{\sec[c+dx]} \sqrt{1-\sec[c+dx]^2} \right) \sin[c+dx] \right) / \\
& \left( a^2 b (b+a \cos[c+dx]) (1-\cos[c+dx]^2) \sqrt{\sec[c+dx]} (2-\sec[c+dx]^2) \right) \Bigg) + \\
& \left( (b+a \cos[c+dx])^3 \sec[c+dx]^{5/2} (A+B \sec[c+dx]) \right. \\
& \left( \frac{(5 a^2 A b + A b^3 - a^3 B - 5 a b^2 B) \sin[c+dx]}{4 a b (-a^2 + b^2)^2} - \frac{-A b^2 \sin[c+dx] + a b B \sin[c+dx]}{2 a (a^2 - b^2) (b+a \cos[c+dx])^2} + \right. \\
& \left. (-7 a^2 A b \sin[c+dx] + A b^3 \sin[c+dx] + 3 a^3 B \sin[c+dx] + 3 a b^2 B \sin[c+dx]) \right) / \\
& \left( 4 a (a^2 - b^2)^2 (b+a \cos[c+dx]) \right) \Bigg) \Bigg) / \\
& \left( d (B+A \cos[c+dx]) (a+b \sec[c+dx])^3 \right)
\end{aligned}$$

**Problem 432: Result more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\sec[c+dx]} (A+B \sec[c+dx])}{(a+b \sec[c+dx])^3} dx$$

Optimal (type 4, 402 leaves, 10 steps):

$$\begin{aligned}
& \frac{1}{4 a^2 (a^2 - b^2)^2 d} (9 a^2 A b - 3 A b^3 - 5 a^3 B - a b^2 B) \\
& \sqrt{\cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]} + \frac{1}{4 a^3 (a^2 - b^2)^2 d} \\
& (8 a^4 A - 5 a^2 A b^2 + 3 A b^4 - 7 a^3 b B + a b^3 B) \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]} - \\
& \left( (15 a^4 A b - 6 a^2 A b^3 + 3 A b^5 - 3 a^5 B - 10 a^3 b^2 B + a b^4 B) \sqrt{\cos[c + d x]} \right. \\
& \left. \operatorname{EllipticPi}\left[\frac{2 a}{a + b}, \frac{1}{2}(c + d x), 2\right] \sqrt{\sec[c + d x]} \right) / \left( 4 a^3 (a - b)^2 (a + b)^3 d \right) - \\
& \frac{(A b - a B) \sqrt{\sec[c + d x]} \sin[c + d x]}{2 (a^2 - b^2) d (a + b \sec[c + d x])^2} - \frac{(7 a^2 A b - A b^3 - 3 a^3 B - 3 a b^2 B) \sqrt{\sec[c + d x]} \sin[c + d x]}{4 a (a^2 - b^2)^2 d (a + b \sec[c + d x])}
\end{aligned}$$

Result (type 4, 890 leaves):

$$\begin{aligned}
& \frac{1}{16 a (a-b)^2 (a+b)^2 d (B+A \cos [c+d x]) (a+b \sec [c+d x])^3} \\
& (b+a \cos [c+d x])^3 \sec [c+d x]^2 (A+B \sec [c+d x]) \\
& \left( - \left( \left( 2 (16 a^3 A + 8 a A b^2 - 24 a^2 b B) \cos [c+d x]^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right] \right. \right. \\
& \quad \left. \left. (a+b \sec [c+d x]) \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) \right) / \\
& \quad \left( a (b+a \cos [c+d x]) (1-\cos [c+d x]^2) \right) + \\
& \quad \left( 2 (-5 a^2 A b - A b^3 + a^3 B + 5 a b^2 B) \cos [c+d x]^2 \left( \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c+d x]}], -1] + \right. \right. \\
& \quad \left. \left. \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) (a+b \sec [c+d x]) \right. \\
& \quad \left. \sqrt{1-\sec [c+d x]^2} \sin [c+d x] \right) / (b (b+a \cos [c+d x]) (1-\cos [c+d x]^2)) - \\
& \quad \left( 2 (9 a^2 A b - 3 A b^3 - 5 a^3 B - a b^2 B) \cos [2 (c+d x)] (a+b \sec [c+d x]) \right. \\
& \quad \left( 2 a b - 2 a b \sec [c+d x]^2 + 2 a b \operatorname{EllipticE} [\operatorname{ArcSin} [\sqrt{\sec [c+d x]}], -1] \sqrt{\sec [c+d x]} \right. \\
& \quad \left. \sqrt{1-\sec [c+d x]^2} + a (a-2 b) \operatorname{EllipticF} [\operatorname{ArcSin} [\sqrt{\sec [c+d x]}], -1] \sqrt{\sec [c+d x]} \right. \\
& \quad \left. \sqrt{1-\sec [c+d x]^2} + a^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) \sqrt{\sec [c+d x]} \\
& \quad \left. \sqrt{1-\sec [c+d x]^2} - 2 b^2 \operatorname{EllipticPi} \left[ -\frac{b}{a}, -\operatorname{ArcSin} [\sqrt{\sec [c+d x]}] \right], -1 \right) \\
& \quad \left. \sqrt{\sec [c+d x]} \sqrt{1-\sec [c+d x]^2} \right) \sin [c+d x] \Big) / \\
& \quad \left( a^2 b (b+a \cos [c+d x]) (1-\cos [c+d x]^2) \sqrt{\sec [c+d x]} (2-\sec [c+d x]^2) \right) + \\
& \quad \left( (b+a \cos [c+d x])^3 \sec [c+d x]^{5/2} (A+B \sec [c+d x]) \right. \\
& \quad \left( \frac{(-9 a^2 A b + 3 A b^3 + 5 a^3 B + a b^2 B) \sin [c+d x]}{4 a^2 (-a^2 + b^2)^2} - \frac{A b^3 \sin [c+d x] - a b^2 B \sin [c+d x]}{2 a^2 (a^2 - b^2) (b+a \cos [c+d x])^2} + \right. \\
& \quad \left. (11 a^2 A b^2 \sin [c+d x] - 5 A b^4 \sin [c+d x] - 7 a^3 b B \sin [c+d x] + a b^3 B \sin [c+d x]) \right. \\
& \quad \left. (4 a^2 (a^2 - b^2)^2 (b+a \cos [c+d x])) \right) \Big) / \\
& \quad (d (B+A \cos [c+d x]) (a+b \sec [c+d x])^3)
\end{aligned}$$

**Problem 435: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sec [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]) dx$$

Optimal (type 4, 336 leaves, 13 steps):



$$\begin{aligned}
& \left( (4 A b + 3 a B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
& \left( 4 d \sqrt{a + b \sec [c + d x]} \right) + \\
& \left( (4 a A b - a^2 B + 4 b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
& \left( 4 b d \sqrt{a + b \sec [c + d x]} \right) - \frac{(4 A b + a B) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]}}{4 b d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]}} + \\
& \frac{(4 A b + a B) \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{4 b d} + \\
& \frac{B \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{2 d}
\end{aligned}$$

Result (type 4, 578 leaves):

$$\begin{aligned}
 & - \frac{1}{16 b d \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]}} \\
 & \sqrt{a+b \sec [c+d x]} \left( - \frac{8 a b B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \right. \\
 & \left( 2(-4 a A b+3 a^2 B-8 b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\
 & \left( \sqrt{b+a \cos [c+d x]} \right) + \left( 2 i(4 a A b+a^2 B) \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [ \right. \\
 & 2(c+d x) ] \left( -2 b(a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
 & a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
 & \left. \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right) \\
 & \sin [c+d x] \left) / \left( \sqrt{\frac{1}{a-b}} b \sqrt{1-\cos [c+d x]^2} \sqrt{\frac{a^2-a^2 \cos [c+d x]^2}{a^2}} \right. \right. \\
 & \left. \left. \left( -a^2+2 b^2-4 b(b+a \cos [c+d x])+2(b+a \cos [c+d x])^2 \right) \right) \right) + \\
 & \frac{1}{d \sqrt{\sec [c+d x]}} \sqrt{a+b \sec [c+d x]} \left( \frac{\sec [c+d x](4 A b \sin [c+d x]+a B \sin [c+d x])}{4 b} + \right. \\
 & \left. \frac{1}{2} B \sec [c+d x] \tan [c+d x] \right)
 \end{aligned}$$

**Problem 436: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sqrt{\sec [c+d x]} \sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]) d x$$

Optimal (type 4, 253 leaves, 12 steps):

$$\begin{aligned}
& \frac{(2 a A + b B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{d \sqrt{a+b \sec [c+d x]}} + \\
& \left( (2 A b + a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]} \right) / \\
& \left( d \sqrt{a+b \sec [c+d x]} \right) - \frac{B \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \sqrt{\sec [c+d x]}} + \\
& \frac{B \sqrt{\sec [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{d}
\end{aligned}$$

Result(type 4, 377 leaves):

$$\begin{aligned}
& \left( \sqrt{a+b \sec [c+d x]} \right. \\
& \left( \frac{8 a A \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{(a+b) \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} + \frac{2 (4 A b + a B) \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{(a+b) \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} - \right. \\
& \left( 2 i B \sqrt{-\frac{a(-1+\cos [c+d x])}{a+b}} \sqrt{\frac{a(1+\cos [c+d x])}{a-b}} \operatorname{Csc}[c+d x] \right. \\
& \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
& a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
& \left. \left. \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right]\right) \right) \right) / \\
& \left. \left( a \sqrt{\frac{1}{a-b}} b \sqrt{b+a \cos [c+d x]} \right) + 4 B \tan [c+d x] \right) / \left( 4 d \sqrt{\sec [c+d x]} \right)
\end{aligned}$$

**Problem 441: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sec[c + dx]^{3/2} (a + b \sec[c + dx])^{3/2} (A + B \sec[c + dx]) dx$$

Optimal (type 4, 421 leaves, 14 steps):

$$\begin{aligned} & \left( (42 a A b + 17 a^2 B + 16 b^2 B) \sqrt{\frac{b + a \cos[c + dx]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), \frac{2a}{a + b}\right] \sqrt{\sec[c + dx]} \right) / \\ & (24 d \sqrt{a + b \sec[c + dx]}) + \left( (6 a^2 A b + 8 A b^3 - a^3 B + 12 a b^2 B) \sqrt{\frac{b + a \cos[c + dx]}{a + b}} \right. \\ & \left. \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + dx), \frac{2a}{a + b}\right] \sqrt{\sec[c + dx]} \right) / (8 b d \sqrt{a + b \sec[c + dx]}) - \\ & \left( (30 a A b + 3 a^2 B + 16 b^2 B) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), \frac{2a}{a + b}\right] \sqrt{a + b \sec[c + dx]} \right) / \\ & \left( 24 b d \sqrt{\frac{b + a \cos[c + dx]}{a + b}} \sqrt{\sec[c + dx]} \right) + \frac{1}{24 b d} \\ & \frac{(30 a A b + 3 a^2 B + 16 b^2 B) \sqrt{\sec[c + dx]} \sqrt{a + b \sec[c + dx]} \sin[c + dx] + (6 A b + 7 a B) \sec[c + dx]^{3/2} \sqrt{a + b \sec[c + dx]} \sin[c + dx]}{12 d} + \\ & \frac{b B \sec[c + dx]^{5/2} \sqrt{a + b \sec[c + dx]} \sin[c + dx]}{3 d} \end{aligned}$$

Result (type 4, 673 leaves):

$$\begin{aligned}
& - \frac{1}{96 b d (b + a \cos [c + d x])^{3/2} \sec [c + d x]^{3/2}} (a + b \sec [c + d x])^{3/2} \\
& \left( \left( 2 (-24 a A b^2 - 28 a^2 b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \right. \\
& \left( \sqrt{b + a \cos [c + d x]} \right) + \left( 2 (-6 a^2 A b - 48 A b^3 + 9 a^3 B - 56 a b^2 B) \right. \\
& \left. \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( \sqrt{b + a \cos [c + d x]} \right) + \\
& \left( 2 i (30 a^2 A b + 3 a^3 B + 16 a b^2 B) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [2 (c + d x)] \right. \\
& \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \left. \right) \\
& \sin [c + d x] \left. \right) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \\
& \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2 \right) \right) \left. \right) + \\
& \left( (a + b \sec [c + d x])^{3/2} \left( \frac{1}{12} \sec [c + d x]^2 (6 A b \sin [c + d x] + 7 a B \sin [c + d x]) + \frac{1}{24 b} \right. \right. \\
& \left. \sec [c + d x] (30 a A b \sin [c + d x] + 3 a^2 B \sin [c + d x] + 16 b^2 B \sin [c + d x]) + \right. \\
& \left. \left. \frac{1}{3} b B \sec [c + d x]^2 \tan [c + d x] \right) \right) / \\
& (d (b + a \cos [c + d x]) \sec [c + d x]^{3/2})
\end{aligned}$$

**Problem 442: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sqrt{\sec [c + d x]} (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x]) dx$$

Optimal (type 4, 339 leaves, 13 steps):

$$\begin{aligned}
& \left( (8 a^2 A + 4 A b^2 + 7 a b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
& (4 d \sqrt{a + b \sec [c + d x]}) + \\
& \left( (12 a A b + 3 a^2 B + 4 b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
& (4 d \sqrt{a + b \sec [c + d x]}) - \frac{(4 A b + 5 a B) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]}}{4 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]}} + \\
& \frac{(4 A b + 5 a B) \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{4 d} + \\
& \frac{b B \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{2 d}
\end{aligned}$$

Result (type 4, 595 leaves):

$$\begin{aligned}
& \frac{1}{16 d (b + a \cos [c + d x])^{3/2} \sec [c + d x]^{3/2}} \\
& (a + b \sec [c + d x])^{3/2} \left( \frac{2 (16 a^2 A + 4 a b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right]}{\sqrt{b + a \cos [c + d x]}} + \right. \\
& \left( 2 (20 a A b + a^2 B + 8 b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \\
& \left( \sqrt{b + a \cos [c + d x]} \right) + \left( 2 i (-4 a A b - 5 a^2 B) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [ \right. \\
& 2 (c + d x) ] \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \right) \\
& \sin [c + d x] \left) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \right. \\
& \left. \left. (-a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2) \right) \right) + \\
& \left( (a + b \sec [c + d x])^{3/2} \left( \frac{1}{4} \sec [c + d x] (4 A b \sin [c + d x] + 5 a B \sin [c + d x]) + \right. \right. \\
& \left. \left. \frac{1}{2} b B \sec [c + d x] \tan [c + d x] \right) \right) / (d (b + a \cos [c + d x]) \sec [c + d x]^{3/2})
\end{aligned}$$

**Problem 443: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x])}{\sqrt{\sec [c + d x]}} dx$$

Optimal (type 4, 272 leaves, 12 steps):

$$\begin{aligned}
& \left( (2 a A b + 2 a^2 B + b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
& \left( d \sqrt{a + b \sec [c + d x]} \right) + \\
& \left( b (2 A b + 3 a B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
& \left( d \sqrt{a + b \sec [c + d x]} \right) + \frac{(2 a A - b B) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]}}{d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]}} + \\
& \frac{b B \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{d}
\end{aligned}$$

Result (type 4, 554 leaves):



$$\begin{aligned}
& \frac{b B (a + b \sec[c + d x])^{3/2} \sin[c + d x]}{d (b + a \cos[c + d x]) \sqrt{\sec[c + d x]}} + \\
& \frac{1}{4 d (b + a \cos[c + d x])^{3/2} \sec[c + d x]^{3/2}} (a + b \sec[c + d x])^{3/2} \\
& \left( \frac{2 (8 a A b + 4 a^2 B) \sqrt{\frac{b + a \cos[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right]}{\sqrt{b + a \cos[c + d x]}} + \left( 2 (2 a^2 A + 4 A b^2 + 5 a b B) \right. \right. \\
& \left. \left. \sqrt{\frac{b + a \cos[c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / (\sqrt{b + a \cos[c + d x]}) + \right. \\
& \left( 2 i (2 a^2 A - a b B) \sqrt{\frac{a - a \cos[c + d x]}{a + b}} \sqrt{\frac{a + a \cos[c + d x]}{a - b}} \cos[2 (c + d x)] \right. \\
& \left. \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos[c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \\
& \left. \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos[c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \right. \\
& \left. \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos[c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \right) \right) \\
& \sin[c + d x] \Bigg) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos[c + d x]^2} \sqrt{\frac{a^2 - a^2 \cos[c + d x]^2}{a^2}} \right. \\
& \left. \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos[c + d x]) + 2 (b + a \cos[c + d x])^2 \right) \right) \right)
\end{aligned}$$

**Problem 444: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{(a + b \sec[c + d x])^{3/2} (A + B \sec[c + d x])}{\sec[c + d x]^{3/2}} dx$$

Optimal (type 4, 276 leaves, 12 steps):

$$\begin{aligned}
& \left( 2 (a^2 A - A b^2 + 3 a b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
& \left( 3 d \sqrt{a + b \sec [c + d x]} \right) + \frac{2 b^2 B \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]}}{d \sqrt{a + b \sec [c + d x]}} + \\
& \frac{2 (4 A b + 3 a B) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]}}{3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]}} + \\
& \frac{2 a A \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{3 d \sqrt{\sec [c + d x]}}
\end{aligned}$$

Result (type 4, 563 leaves):

$$\begin{aligned}
& \frac{2 a A (a+b \operatorname{Sec}[c+d x])^{3/2} \operatorname{Sin}[c+d x]}{3 d (b+a \operatorname{Cos}[c+d x]) \operatorname{Sec}[c+d x]^{3/2}} + \\
& \frac{1}{6 d (b+a \operatorname{Cos}[c+d x])^{3/2} \operatorname{Sec}[c+d x]^{3/2}} (a+b \operatorname{Sec}[c+d x])^{3/2} \\
& \left( \left( 2 (2 a^2 A + 6 A b^2 + 12 a b B) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \right. \\
& \left( \sqrt{b+a \operatorname{Cos}[c+d x]} \right) + \left( 2 (4 a A b + 3 a^2 B + 6 b^2 B) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \right. \\
& \left. \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \left( \sqrt{b+a \operatorname{Cos}[c+d x]} \right) + \\
& \left( 2 i (4 a A b + 3 a^2 B) \sqrt{\frac{a-a \operatorname{Cos}[c+d x]}{a+b}} \sqrt{\frac{a+a \operatorname{Cos}[c+d x]}{a-b}} \operatorname{Cos}[2(c+d x)] \right. \\
& \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \operatorname{Cos}[c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
& a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \operatorname{Cos}[c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
& \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \operatorname{Cos}[c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \left. \right) \\
& \operatorname{Sin}[c+d x] \left. \right) / \left( \sqrt{\frac{1}{a-b}} b \sqrt{1-\operatorname{Cos}[c+d x]^2} \sqrt{\frac{a^2-a^2 \operatorname{Cos}[c+d x]^2}{a^2}} \right. \\
& \left. \left( -a^2+2 b^2-4 b (b+a \operatorname{Cos}[c+d x]) + 2 (b+a \operatorname{Cos}[c+d x])^2 \right) \right) \left. \right)
\end{aligned}$$

**Problem 448: Result unnecessarily involves imaginary or complex numbers.**

$$\int \operatorname{Sec}[c+d x]^{3/2} (a+b \operatorname{Sec}[c+d x])^{5/2} (A+B \operatorname{Sec}[c+d x]) dx$$

Optimal (type 4, 513 leaves, 15 steps):

$$\begin{aligned}
& \left( (472 a^2 A b + 128 A b^3 + 133 a^3 B + 356 a b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
& \quad \left. \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / (192 d \sqrt{a + b \sec [c + d x]}) + \\
& \left( (40 a^3 A b + 160 a A b^3 - 5 a^4 B + 120 a^2 b^2 B + 48 b^4 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
& \quad \left. \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / (64 b d \sqrt{a + b \sec [c + d x]}) - \\
& \left( (264 a^2 A b + 128 A b^3 + 15 a^3 B + 284 a b^2 B) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\
& \left( 192 b d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \frac{1}{192 b d} \\
& (264 a^2 A b + 128 A b^3 + 15 a^3 B + 284 a b^2 B) \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
& \frac{1}{96 d} (104 a A b + 59 a^2 B + 36 b^2 B) \sec [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
& \frac{b (8 A b + 11 a B) \sec [c + d x]^{5/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{24 d} + \\
& \frac{b B \sec [c + d x]^{5/2} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{4 d}
\end{aligned}$$

Result (type 4, 768 leaves):

$$\begin{aligned}
& - \frac{1}{768 b d (b + a \cos [c + d x])^{5/2} \sec [c + d x]^{5/2}} (a + b \sec [c + d x])^{5/2} \\
& \left( \left( 2 (-416 a^2 A b^2 - 236 a^3 b B - 144 a b^3 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2a}{a + b}\right] \right) / \right. \\
& \quad \left( \sqrt{b + a \cos [c + d x]} \right) + \left( 2 (24 a^3 A b - 832 a A b^3 + 45 a^4 B - 436 a^2 b^2 B - 288 b^4 B) \right. \\
& \quad \left. \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2a}{a + b}\right] \right) / \left( \sqrt{b + a \cos [c + d x]} \right) + \\
& \quad \left( 2 i (264 a^3 A b + 128 a A b^3 + 15 a^4 B + 284 a^2 b^2 B) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \right. \\
& \quad \cos [2(c + d x)] \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \right. \right. \\
& \quad \left. \left. \frac{-a + b}{a + b}\right] + a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \\
& \quad \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \right) \\
& \quad \sin [c + d x] \left) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \right. \\
& \quad \left. \left. (-a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2) \right) \right) + \\
& \quad \left( (a + b \sec [c + d x])^{5/2} \left( \frac{1}{24} \sec [c + d x]^3 (8 A b^2 \sin [c + d x] + 17 a b B \sin [c + d x]) + \right. \right. \\
& \quad \frac{1}{96} \sec [c + d x]^2 (104 a A b \sin [c + d x] + 59 a^2 B \sin [c + d x] + 36 b^2 B \sin [c + d x]) + \\
& \quad \frac{1}{192 b} \sec [c + d x] \\
& \quad (264 a^2 A b \sin [c + d x] + 128 A b^3 \sin [c + d x] + 15 a^3 B \sin [c + d x] + 284 a b^2 B \sin [c + d x]) + \\
& \quad \left. \left. \frac{1}{4} b^2 B \sec [c + d x]^3 \tan [c + d x] \right) \right) / \left( d (b + a \cos [c + d x])^2 \sec [c + d x]^{5/2} \right)
\end{aligned}$$

**Problem 449: Result unnecessarily involves imaginary or complex numbers.**

$$\int \sqrt{\sec[c+dx]} (a+b \sec[c+dx])^{5/2} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 422 leaves, 14 steps):

$$\begin{aligned} & \left( (48 a^3 A + 66 a A b^2 + 59 a^2 b B + 16 b^3 B) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \right. \\ & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\sec[c+dx]} \right) / (24 d \sqrt{a+b \sec[c+dx]}) + \\ & \left( (30 a^2 A b + 8 A b^3 + 5 a^3 B + 20 a b^2 B) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \right. \\ & \quad \left. \sqrt{\sec[c+dx]} \right) / (8 d \sqrt{a+b \sec[c+dx]}) - \\ & \left( (54 a A b + 33 a^2 B + 16 b^2 B) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]} \right) / \\ & \left( 24 d \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \sqrt{\sec[c+dx]} \right) + \frac{1}{24 d} \\ & \frac{(54 a A b + 33 a^2 B + 16 b^2 B) \sqrt{\sec[c+dx]} \sqrt{a+b \sec[c+dx]} \sin[c+dx] +}{4 d} \\ & \frac{b (2 A b + 3 a B) \sec[c+dx]^{3/2} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{4 d} + \\ & \frac{b B \sec[c+dx]^{3/2} (a+b \sec[c+dx])^{3/2} \sin[c+dx]}{3 d} \end{aligned}$$

Result (type 4, 678 leaves):

$$\begin{aligned}
& \frac{1}{96 d (b + a \cos [c + d x])^{5/2} \sec [c + d x]^{5/2}} (a + b \sec [c + d x])^{5/2} \\
& \left( \left( 2 (96 a^3 A + 24 a A b^2 + 52 a^2 b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \right. \\
& \left( \sqrt{b + a \cos [c + d x]} \right) + \left( 2 (126 a^2 A b + 48 A b^3 - 3 a^3 B + 104 a b^2 B) \right. \\
& \left. \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( \sqrt{b + a \cos [c + d x]} \right) + \\
& \left( 2 i (-54 a^2 A b - 33 a^3 B - 16 a b^2 B) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [2 (c + d x)] \right. \\
& \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \left. \right) \\
& \sin [c + d x] \left. \right) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \\
& \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2 \right) \right) \left. \right) + \\
& \left( (a + b \sec [c + d x])^{5/2} \left( \frac{1}{12} \sec [c + d x]^2 (6 A b^2 \sin [c + d x] + 13 a b B \sin [c + d x]) + \right. \right. \\
& \frac{1}{24} \sec [c + d x] (54 a A b \sin [c + d x] + 33 a^2 B \sin [c + d x] + 16 b^2 B \sin [c + d x]) + \\
& \left. \left. \frac{1}{3} b^2 B \sec [c + d x]^2 \tan [c + d x] \right) \right) / \\
& \left( d (b + a \cos [c + d x])^2 \sec [c + d x]^{5/2} \right)
\end{aligned}$$

**Problem 450: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + b \sec[c + d x])^{5/2} (A + B \sec[c + d x])}{\sqrt{\sec[c + d x]}} dx$$

Optimal (type 4, 359 leaves, 13 steps):

$$\begin{aligned} & \left( (16 a^2 A b + 4 A b^3 + 8 a^3 B + 11 a b^2 B) \sqrt{\frac{b + a \cos[c + d x]}{a + b}} \right. \\ & \quad \left. \text{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec[c + d x]} \right) / (4 d \sqrt{a + b \sec[c + d x]}) + \\ & \left( b (20 a A b + 15 a^2 B + 4 b^2 B) \sqrt{\frac{b + a \cos[c + d x]}{a + b}} \text{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right. \\ & \quad \left. \sqrt{\sec[c + d x]} \right) / (4 d \sqrt{a + b \sec[c + d x]}) + \\ & \left( (8 a^2 A - 4 A b^2 - 9 a b B) \text{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec[c + d x]} \right) / \\ & \left( 4 d \sqrt{\frac{b + a \cos[c + d x]}{a + b}} \sqrt{\sec[c + d x]} \right) + \\ & \frac{b (4 A b + 7 a B) \sqrt{\sec[c + d x]} \sqrt{a + b \sec[c + d x]} \sin[c + d x]}{4 d} + \\ & \frac{b B \sqrt{\sec[c + d x]} (a + b \sec[c + d x])^{3/2} \sin[c + d x]}{2 d} \end{aligned}$$

Result (type 4, 628 leaves):



$$\begin{aligned}
& \frac{1}{16 d (b + a \cos [c + d x])^{5/2} \sec [c + d x]^{5/2}} (a + b \sec [c + d x])^{5/2} \\
& \left( \left( 2 (48 a^2 A b + 16 a^3 B + 4 a b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \right. \\
& \left( \sqrt{b + a \cos [c + d x]} \right) + \left( 2 (8 a^3 A + 36 a A b^2 + 21 a^2 b B + 8 b^3 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
& \left. \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( \sqrt{b + a \cos [c + d x]} \right) + \\
& \left( 2 i (8 a^3 A - 4 a A b^2 - 9 a^2 b B) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [2 (c + d x)] \right. \\
& \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]} \right], \frac{-a + b}{a + b}\right] + \right. \\
& a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]} \right], \frac{-a + b}{a + b}\right] + \right. \\
& \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]} \right], \frac{-a + b}{a + b}\right] \right) \left. \right) \\
& \sin [c + d x] \left. \right) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \\
& \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2 \right) \right) \left. \right) + \\
& \left( (a + b \sec [c + d x])^{5/2} \left( \frac{1}{4} \sec [c + d x] (4 A b^2 \sin [c + d x] + 9 a b B \sin [c + d x]) + \right. \right. \\
& \left. \left. \frac{1}{2} b^2 B \sec [c + d x] \tan [c + d x] \right) \right) / \\
& (d (b + a \cos [c + d x])^2 \sec [c + d x]^{5/2})
\end{aligned}$$

**Problem 451: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x])}{\sec [c + d x]^{3/2}} dx$$

Optimal (type 4, 349 leaves, 13 steps):

$$\begin{aligned}
 & \left( (2 a^3 A + 4 a A b^2 + 12 a^2 b B + 3 b^3 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
 & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / (3 d \sqrt{a + b \sec [c + d x]}) + \\
 & \left( b^2 (2 A b + 5 a B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{\sec [c + d x]} \right) / \\
 & \quad (d \sqrt{a + b \sec [c + d x]}) + \\
 & \left( (14 a A b + 6 a^2 B - 3 b^2 B) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\
 & \quad \left( 3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) - \\
 & \frac{b (2 a A - 3 b B) \sqrt{\sec [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{3 d} + \\
 & \frac{2 a A (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{3 d \sqrt{\sec [c + d x]}}
 \end{aligned}$$

Result (type 4, 599 leaves):

$$\begin{aligned}
& \frac{1}{12 d (b + a \cos [c + d x])^{5/2} \sec [c + d x]^{5/2}} (a + b \sec [c + d x])^{5/2} \\
& \left( \left( 2 (4 a^3 A + 36 a A b^2 + 36 a^2 b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \right. \\
& \quad \left( \sqrt{b + a \cos [c + d x]} \right) + \left( 2 (14 a^2 A b + 12 A b^3 + 6 a^3 B + 27 a b^2 B) \right. \\
& \quad \left. \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( \sqrt{b + a \cos [c + d x]} \right) + \\
& \quad \left( 2 i (14 a^2 A b + 6 a^3 B - 3 a b^2 B) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [2 (c + d x)] \right. \\
& \quad \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& \quad a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& \quad \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \right) \\
& \quad \sin [c + d x] \Bigg) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \\
& \quad \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2 \right) \right) \Bigg) + \\
& \frac{(a + b \sec [c + d x])^{5/2} \left( \frac{2}{3} a^2 A \sin [c + d x] + b^2 B \tan [c + d x] \right)}{d (b + a \cos [c + d x])^2 \sec [c + d x]^{5/2}}
\end{aligned}$$

**Problem 452: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{(a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x])}{\sec [c + d x]^{5/2}} dx$$

Optimal (type 4, 342 leaves, 13 steps):

$$\begin{aligned}
& \left( 2 \left( 8 a^2 A b - 8 A b^3 + 5 a^3 B + 10 a b^2 B \right) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
& \quad \left. \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{\sec [c + d x]} \right) / \left( 15 d \sqrt{a + b \sec [c + d x]} \right) + \\
& \quad \frac{2 b^3 B \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi} \left[ 2, \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{\sec [c + d x]} }{d \sqrt{a + b \sec [c + d x]}} + \\
& \quad \left( 2 \left( 9 a^2 A + 23 A b^2 + 35 a b B \right) \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{a + b \sec [c + d x]} \right) / \\
& \quad \left( 15 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \sqrt{\sec [c + d x]} \right) + \\
& \quad \frac{2 a \left( 8 A b + 5 a B \right) \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{15 d \sqrt{\sec [c + d x]}} + \frac{2 a A \left( a + b \sec [c + d x] \right)^{3/2} \sin [c + d x]}{5 d \sec [c + d x]^{3/2}}
\end{aligned}$$

Result (type 4, 616 leaves):

$$\begin{aligned}
& \frac{1}{30 d (b + a \cos [c + d x])^{5/2} \sec [c + d x]^{5/2}} (a + b \sec [c + d x])^{5/2} \\
& \left( \left( 2 (34 a^2 A b + 30 A b^3 + 10 a^3 B + 90 a b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \right. \\
& \quad \left( \sqrt{b + a \cos [c + d x]} \right) + \left( 2 (9 a^3 A + 23 a A b^2 + 35 a^2 b B + 30 b^3 B) \right. \\
& \quad \left. \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( \sqrt{b + a \cos [c + d x]} \right) + \\
& \quad \left( 2 i (9 a^3 A + 23 a A b^2 + 35 a^2 b B) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [2 (c + d x)] \right. \\
& \quad \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& \quad a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \\
& \quad \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \right) \\
& \quad \left. \sin [c + d x] \right) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \\
& \quad \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2 \right) \right) + \\
& \quad \left( (a + b \sec [c + d x])^{5/2} \left( \frac{2}{15} a (11 A b + 5 a B) \sin [c + d x] + \frac{1}{5} a^2 A \sin [2 (c + d x)] \right) \right) / \\
& \quad \left( d (b + a \cos [c + d x])^2 \sec [c + d x]^{5/2} \right)
\end{aligned}$$

**Problem 456: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c + d x]^{5/2} (A + B \sec [c + d x])}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 344 leaves, 13 steps):

$$\begin{aligned}
 & \frac{(4 A b - a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{4 b d \sqrt{a+b \sec [c+d x]}} - \\
 & \left( (4 a A b - 3 a^2 B - 4 b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]} \right) / \\
 & (4 b^2 d \sqrt{a+b \sec [c+d x]}) - \frac{(4 A b - 3 a B) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{4 b^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \sqrt{\sec [c+d x]}} + \\
 & \frac{(4 A b - 3 a B) \sqrt{\sec [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 b^2 d} + \\
 & \frac{B \sec [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 b d}
 \end{aligned}$$

Result (type 4, 593 leaves):

$$\begin{aligned}
& \frac{1}{16 b^2 d \sqrt{a+b \sec [c+d x]}} \\
& \sqrt{b+a \cos [c+d x]} \sqrt{\sec [c+d x]} \left( \frac{8 a b B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \right. \\
& \left( 2(-12 a A b+9 a^2 B+8 b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\
& \left( \sqrt{b+a \cos [c+d x]} \right) + \left( 2 i(-4 a A b+3 a^2 B) \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos \left[ \right. \right. \\
& \left. \left. 2(c+d x) \right] \left( -2 b(a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \\
& \left. \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \right. \\
& \left. \left. \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right) \right) \\
& \sin [c+d x] \left) / \left( \sqrt{\frac{1}{a-b}} b \sqrt{1-\cos [c+d x]^2} \sqrt{\frac{a^2-a^2 \cos [c+d x]^2}{a^2}} \right. \right. \\
& \left. \left. \left( -a^2+2 b^2-4 b(b+a \cos [c+d x])+2(b+a \cos [c+d x])^2 \right) \right) \right) + \\
& \left( (b+a \cos [c+d x]) \sqrt{\sec [c+d x]} \left( \frac{\sec [c+d x] (4 A b \sin [c+d x]-3 a B \sin [c+d x])}{4 b^2} + \right. \right. \\
& \left. \left. \frac{B \sec [c+d x] \tan [c+d x]}{2 b} \right) \right) / \left( d \sqrt{a+b \sec [c+d x]} \right)
\end{aligned}$$

**Problem 457: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c+d x]^{3/2} (A+B \sec [c+d x])}{\sqrt{a+b \sec [c+d x]}} dx$$

Optimal (type 4, 256 leaves, 12 steps):

$$\begin{aligned}
& \frac{B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{d \sqrt{a+b \sec [c+d x]}} + \\
& \left( (2 A b - a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]} \right) / \\
& \left( b d \sqrt{a+b \sec [c+d x]} \right) - \frac{B \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{b d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \sqrt{\sec [c+d x]}} + \\
& \frac{B \sqrt{\sec [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{b d}
\end{aligned}$$

Result(type 4, 339 leaves):

$$\begin{aligned}
& \frac{1}{4 b d \sqrt{a+b \sec [c+d x]}} \\
& \sqrt{\sec [c+d x]} \left( 2 (4 A b - 3 a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] - \right. \\
& \frac{1}{a \sqrt{\frac{1}{a-b}} b} 2 i B \sqrt{-\frac{a(-1+\cos [c+d x])}{a+b}} \sqrt{\frac{a(1+\cos [c+d x])}{a-b}} \sqrt{b+a \cos [c+d x]} \\
& \csc [c+d x] \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
& a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
& \left. \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right]\right) \right) + \\
& \left. 4 B (b+a \cos [c+d x]) \tan [c+d x] \right)
\end{aligned}$$



**Problem 462: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec[c+dx]^{5/2} (A+B \sec[c+dx])}{(a+b \sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 371 leaves, 13 steps):

$$\begin{aligned} & \frac{B \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\sec[c+dx]}}{b d \sqrt{a+b \sec[c+dx]}} + \\ & \left( (2Ab-3aB) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\sec[c+dx]} \right) / \\ & \left( b^2 d \sqrt{a+b \sec[c+dx]} \right) + \\ & \left( (2aAb-3a^2B+b^2B) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]} \right) / \\ & \left( b^2 (a^2-b^2) d \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \sqrt{\sec[c+dx]} \right) + \frac{2a(Ab-aB) \sec[c+dx]^{3/2} \sin[c+dx]}{b(a^2-b^2) d \sqrt{a+b \sec[c+dx]}} - \\ & \frac{(2aAb-3a^2B+b^2B) \sqrt{\sec[c+dx]} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{b^2 (a^2-b^2) d} \end{aligned}$$

Result (type 4, 647 leaves):

$$\begin{aligned}
& - \frac{1}{4 (a-b) b^2 (a+b) d (a+b \sec [c+d x])^{3/2}} (b+a \cos [c+d x])^{3/2} \\
& \sec [c+d x]^{3/2} \left( \frac{2 (-4 a A b^2 + 4 a^2 b B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right]}{\sqrt{b+a \cos [c+d x]}} + \right. \\
& \left( 2 (-6 a^2 A b + 4 A b^3 + 9 a^3 B - 7 a b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right. \\
& \left. \operatorname{EllipticPi}\left[2, \frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \right) / (\sqrt{b+a \cos [c+d x]}) + \\
& \left( 2 i (-2 a^2 A b + 3 a^3 B - a b^2 B) \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2 (c+d x)] \right. \\
& \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
& a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \\
& \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \left. \right) \\
& \sin [c+d x] \left. \right) / \left( \sqrt{\frac{1}{a-b}} b \sqrt{1 - \cos [c+d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c+d x]^2}{a^2}} \right. \\
& \left. \left( -a^2 + 2 b^2 - 4 b (b+a \cos [c+d x]) + 2 (b+a \cos [c+d x])^2 \right) \right) + \\
& \left( (b+a \cos [c+d x])^2 \sec [c+d x]^{3/2} \left( \frac{2 (a^2 A b \sin [c+d x] - a^3 B \sin [c+d x])}{b^2 (-a^2 + b^2) (b+a \cos [c+d x])} + \frac{B \tan [c+d x]}{b^2} \right) \right) / \\
& \left( d (a+b \sec [c+d x])^{3/2} \right)
\end{aligned}$$

**Problem 463: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.**

$$\int \frac{\sec[c+dx]^{3/2} (A+B \sec[c+dx])}{(a+b \sec[c+dx])^{3/2}} dx$$

Optimal (type 4, 220 leaves, 9 steps):

$$\frac{2 B \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{\sec[c+dx]}}{b d \sqrt{a+b \sec[c+dx]}} - \frac{2 (A b - a B) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]}}{b (a^2 - b^2) d \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \sqrt{\sec[c+dx]}} + \frac{2 a (A b - a B) \sqrt{\sec[c+dx]} \sin[c+dx]}{b (a^2 - b^2) d \sqrt{a+b \sec[c+dx]}}$$

Result (type 4, 595 leaves):

$$\begin{aligned}
 & - \left( \left( 2 (b + a \cos [c + d x]) \sec [c + d x]^{3/2} (a A b \sin [c + d x] - a^2 B \sin [c + d x]) \right) / \right. \\
 & \quad \left. (b (-a^2 + b^2) d (a + b \sec [c + d x])^{3/2}) \right) + \\
 & \quad \frac{1}{2 b (-a + b) (a + b) d (a + b \sec [c + d x])^{3/2}} (b + a \cos [c + d x])^{3/2} \sec [c + d x]^{3/2} \\
 & \quad \left( \frac{2 (2 A b^2 - 2 a b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right]}{\sqrt{b + a \cos [c + d x]}} + \right. \\
 & \quad \left. \left( 2 (a A b - 3 a^2 B + 2 b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] / \right. \right. \\
 & \quad \left. \left( \sqrt{b + a \cos [c + d x]} \right) + \left( 2 i (a A b - a^2 B) \sqrt{\frac{a - a \cos [c + d x]}{a + b}} \sqrt{\frac{a + a \cos [c + d x]}{a - b}} \cos [ \right. \right. \\
 & \quad \left. \left. 2 (c + d x) \right] \left( -2 b (a + b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \\
 & \quad \left. \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. a \operatorname{EllipticPi}\left[1 - \frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a - b}} \sqrt{b + a \cos [c + d x]}\right], \frac{-a + b}{a + b}\right] \right) \right) \right) \\
 & \quad \left. \sin [c + d x] \right) / \left( \sqrt{\frac{1}{a - b}} b \sqrt{1 - \cos [c + d x]^2} \sqrt{\frac{a^2 - a^2 \cos [c + d x]^2}{a^2}} \right. \\
 & \quad \left. \left( -a^2 + 2 b^2 - 4 b (b + a \cos [c + d x]) + 2 (b + a \cos [c + d x])^2 \right) \right) \Bigg)
 \end{aligned}$$

**Problem 468: Result unnecessarily involves imaginary or complex numbers.**

$$\int \frac{\sec [c + d x]^{5/2} (A + B \sec [c + d x])}{(a + b \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 399 leaves, 13 steps):

$$\begin{aligned}
& \frac{2 (A b - a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{3 b \left(a^2 - b^2\right) d \sqrt{a+b \sec [c+d x]}} + \\
& \frac{2 B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \sqrt{\sec [c+d x]}}{b^2 d \sqrt{a+b \sec [c+d x]}} + \\
& \left(2 \left(4 A b^3 + 3 a^3 B - 7 a b^2 B\right) \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) / \\
& \left(3 b^2 \left(a^2 - b^2\right)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \sqrt{\sec [c+d x]}\right) + \\
& \frac{2 a (A b - a B) \sec [c+d x]^{3/2} \sin [c+d x]}{3 b \left(a^2 - b^2\right) d \left(a+b \sec [c+d x]\right)^{3/2}} - \frac{2 a \left(4 A b^3 + 3 a^3 B - 7 a b^2 B\right) \sqrt{\sec [c+d x]} \sin [c+d x]}{3 b^2 \left(a^2 - b^2\right)^2 d \sqrt{a+b \sec [c+d x]}}
\end{aligned}$$

Result (type 4, 726 leaves):

$$\begin{aligned}
 & \frac{1}{6 (a-b)^2 b^2 (a+b)^2 d (a+b \sec [c+d x])^{5/2}} (b+a \cos [c+d x])^{5/2} \sec [c+d x]^{5/2} \\
 & \left( \left( 2 (2 a^2 A b^2 + 6 A b^4 + 4 a^3 b B - 12 a b^3 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \right) / \right. \\
 & \left( \sqrt{b+a \cos [c+d x]} \right) + \left( 2 (4 a A b^3 + 9 a^4 B - 19 a^2 b^2 B + 6 b^4 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right. \\
 & \left. \operatorname{EllipticPi}\left[2, \frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \right) / \left( \sqrt{b+a \cos [c+d x]} \right) + \\
 & \left( 2 i (4 a A b^3 + 3 a^4 B - 7 a^2 b^2 B) \sqrt{\frac{a-a \cos [c+d x]}{a+b}} \sqrt{\frac{a+a \cos [c+d x]}{a-b}} \cos [2 (c+d x)] \right. \\
 & \left. \left( -2 b (a+b) \operatorname{EllipticE}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \\
 & \left. a \left( 2 b \operatorname{EllipticF}\left[i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] + \right. \right. \\
 & \left. \left. a \operatorname{EllipticPi}\left[1-\frac{a}{b}, i \operatorname{ArcSinh}\left[\sqrt{\frac{1}{a-b}} \sqrt{b+a \cos [c+d x]}\right], \frac{-a+b}{a+b}\right] \right) \right) \\
 & \left. \sin [c+d x] \right) / \left( \sqrt{\frac{1}{a-b}} b \sqrt{1-\cos [c+d x]^2} \sqrt{\frac{a^2-a^2 \cos [c+d x]^2}{a^2}} \right. \\
 & \left. \left( -a^2+2 b^2-4 b (b+a \cos [c+d x]) + 2 (b+a \cos [c+d x])^2 \right) \right) + \\
 & \left( (b+a \cos [c+d x])^3 \sec [c+d x]^{5/2} \left( -\frac{2 (a A b \sin [c+d x] - a^2 B \sin [c+d x])}{3 b (-a^2+b^2) (b+a \cos [c+d x])^2} - \right. \right. \\
 & \left. \left( 2 (4 a A b^3 \sin [c+d x] + 3 a^4 B \sin [c+d x] - 7 a^2 b^2 B \sin [c+d x]) \right) / \right. \\
 & \left. \left. (3 b^2 (-a^2+b^2)^2 (b+a \cos [c+d x])) \right) \right) / \left( d (a+b \sec [c+d x])^{5/2} \right)
 \end{aligned}$$

**Problem 479: Unable to integrate problem.**

$$\int \sec [c+d x]^m (a+b \sec [c+d x])^4 (A+B \sec [c+d x]) dx$$

Optimal (type 5, 544 leaves, 9 steps):

$$\begin{aligned}
 & \left( b \left( A b^3 (8 + 6 m + m^2) + 4 a b^2 B (8 + 6 m + m^2) + 2 a^3 B (19 + 8 m + m^2) + a^2 A b (68 + 37 m + 5 m^2) \right) \right. \\
 & \quad \left. \text{Sec}[c + d x]^{1+m} \text{Sin}[c + d x] \right) / \left( d (1 + m) (3 + m) (4 + m) \right) + \\
 & \left( b^2 \left( b^2 B (3 + m)^2 + 2 a A b (4 + m)^2 + a^2 B (26 + 9 m + m^2) \right) \text{Sec}[c + d x]^{2+m} \text{Sin}[c + d x] \right) / \\
 & \quad \left( d (2 + m) (3 + m) (4 + m) \right) + \frac{1}{d (3 + m) (4 + m)} \\
 & b \left( A b (4 + m) + a B (7 + m) \right) \text{Sec}[c + d x]^{1+m} (a + b \text{Sec}[c + d x])^2 \text{Sin}[c + d x] + \\
 & \frac{b B \text{Sec}[c + d x]^{1+m} (a + b \text{Sec}[c + d x])^3 \text{Sin}[c + d x]}{d (4 + m)} - \\
 & \left( \left( A b^4 m (2 + m) + 4 a b^3 B m (2 + m) + 6 a^2 A b^2 m (3 + m) + 4 a^3 b B m (3 + m) + a^4 A (3 + 4 m + m^2) \right) \right. \\
 & \quad \left. \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1-m}{2}, \frac{3-m}{2}, \text{Cos}[c + d x]^2\right] \text{Sec}[c + d x]^{-1+m} \text{Sin}[c + d x] \right) / \\
 & \left( d (1 - m) (1 + m) (3 + m) \sqrt{\text{Sin}[c + d x]^2} \right) + \\
 & \left( \left( b^4 B (3 + 4 m + m^2) + 4 a A b^3 (4 + 5 m + m^2) + 6 a^2 b^2 B (4 + 5 m + m^2) + 4 a^3 A b (8 + 6 m + m^2) + \right. \right. \\
 & \quad \left. \left. a^4 B (8 + 6 m + m^2) \right) \text{Hypergeometric2F1}\left[\frac{1}{2}, -\frac{m}{2}, \frac{2-m}{2}, \text{Cos}[c + d x]^2\right] \right. \\
 & \quad \left. \text{Sec}[c + d x]^m \text{Sin}[c + d x] \right) / \left( d m (2 + m) (4 + m) \sqrt{\text{Sin}[c + d x]^2} \right)
 \end{aligned}$$

Result (type 8, 33 leaves):

$$\int \text{Sec}[c + d x]^m (a + b \text{Sec}[c + d x])^4 (A + B \text{Sec}[c + d x]) \, dx$$

Problem 480: Unable to integrate problem.

$$\int \text{Sec}[c + d x]^m (a + b \text{Sec}[c + d x])^3 (A + B \text{Sec}[c + d x]) \, dx$$

Optimal (type 5, 366 leaves, 8 steps):

$$\frac{1}{d(1+m)(3+m)} b \left( b^2 B(2+m) + 3aAb(3+m) + 2a^2 B(4+m) \right) \sec[c+dx]^{1+m} \sin[c+dx] +$$

$$\frac{b^2 (Ab(3+m) + aB(5+m)) \sec[c+dx]^{2+m} \sin[c+dx]}{d(2+m)(3+m)} +$$

$$\frac{bB \sec[c+dx]^{1+m} (a+b \sec[c+dx])^2 \sin[c+dx]}{d(3+m)} -$$

$$\left( (b^3 Bm(2+m) + 3aAb^2 m(3+m) + 3a^2 bBm(3+m) + a^3 A(3+4m+m^2)) \right.$$

$$\left. \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1-m}{2}, \frac{3-m}{2}, \cos[c+dx]^2\right] \sec[c+dx]^{-1+m} \sin[c+dx] \right) /$$

$$\left( d(3+m)(1-m^2) \sqrt{\sin[c+dx]^2} \right) +$$

$$\left( (Ab^3(1+m) + 3ab^2B(1+m) + 3a^2Ab(2+m) + a^3B(2+m)) \text{Hypergeometric2F1}\left[\frac{1}{2}, \right. \right.$$

$$\left. \left. -\frac{m}{2}, \frac{2-m}{2}, \cos[c+dx]^2\right] \sec[c+dx]^m \sin[c+dx] \right) / \left( dm(2+m) \sqrt{\sin[c+dx]^2} \right)$$

Result(type 8, 33 leaves):

$$\int \sec[c+dx]^m (a+b \sec[c+dx])^3 (A+B \sec[c+dx]) dx$$

**Problem 483: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c+dx]^{7/2} (a+a \sec[c+dx]) (A+B \sec[c+dx]) dx$$

Optimal (type 4, 132 leaves, 8 steps):

$$\frac{6a(A+B) \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5d} +$$

$$\frac{2a(5A+7B) \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{21d} + \frac{2a(5A+7B) \sqrt{\cos[c+dx]} \sin[c+dx]}{21d} +$$

$$\frac{2a(A+B) \cos[c+dx]^{3/2} \sin[c+dx]}{5d} + \frac{2aA \cos[c+dx]^{5/2} \sin[c+dx]}{7d}$$

Result(type 5, 872 leaves):

$$a \left( \sqrt{\cos[c+dx]} (1+\cos[c+dx]) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( -\frac{3(A+B) \cot[c]}{5d} + \right. \right.$$

$$\left. \frac{(23A+28B) \cos[dx] \sin[c]}{84d} + \frac{(A+B) \cos[2dx] \sin[2c]}{10d} + \frac{A \cos[3dx] \sin[3c]}{28d} + \right.$$

$$\left. \frac{(23A+28B) \cos[c] \sin[dx]}{84d} + \frac{(A+B) \cos[2c] \sin[2dx]}{10d} + \frac{A \cos[3c] \sin[3dx]}{28d} \right) -$$



$$\begin{aligned}
& \left( 5 A (1 + \cos [c + d x]) \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \right. \\
& \quad \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
& \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
& \quad \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right) / \left( 21 d \sqrt{1 + \cot [c]^2} \right) - \\
& \left( B (1 + \cos [c + d x]) \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \right. \\
& \quad \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \\
& \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right) / \\
& \left( 3 d \sqrt{1 + \cot [c]^2} \right) - \frac{1}{10 d} 3 A (1 + \cos [c + d x]) \csc [c] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^2 \\
& \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2\right] \right. \\
& \quad \left. \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \\
& \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right. \\
& \quad \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) - \\
& \quad \frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}} \right) - \frac{1}{10 d} \\
& 3 B (1 + \cos [c + d x]) \csc [c] \sec \left[\frac{c}{2} + \frac{d x}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right.
\end{aligned}$$

$$\left\{ \frac{3}{4}, \cos [d x + \operatorname{ArcTan}[\tan [c]]]^2 \sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c] \right\} /$$

$$\left( \sqrt{1 - \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \right.$$

$$\left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) -$$

$$\frac{\frac{\sin [d x + \operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan}[\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan}[\tan [c]]]} \sqrt{1 + \tan [c]^2}} \Bigg)$$

**Problem 484: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c + d x]^{5/2} (a + a \sec [c + d x]) (A + B \sec [c + d x]) dx$$

Optimal (type 4, 101 leaves, 7 steps):

$$\frac{2 a (3 A + 5 B) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{2 a (A + B) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} +$$

$$\frac{2 a (A + B) \sqrt{\cos [c + d x]} \sin [c + d x]}{3 d} + \frac{2 a A \cos [c + d x]^{3/2} \sin [c + d x]}{5 d}$$

Result (type 5, 830 leaves):

$$a \left( \sqrt{\cos [c + d x]} (1 + \cos [c + d x]) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \left( - \frac{(3 A + 5 B) \cot [c]}{5 d} + \frac{(A + B) \cos [d x] \sin [c]}{3 d} + \right. \right.$$

$$\left. \frac{A \cos [2 d x] \sin [2 c]}{10 d} + \frac{(A + B) \cos [c] \sin [d x]}{3 d} + \frac{A \cos [2 c] \sin [2 d x]}{10 d} \right) -$$

$$\left( A (1 + \cos [c + d x]) \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin [d x - \operatorname{ArcTan}[\cot [c]]]^2\right] \right.$$

$$\left. \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sec [d x - \operatorname{ArcTan}[\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right.$$

$$\left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right.$$

$$\left. \sqrt{1 + \sin [d x - \operatorname{ArcTan}[\cot [c]]]} \right) / \left( 3 d \sqrt{1 + \cot [c]^2} \right) -$$

$$\begin{aligned}
& \left( B \left( 1 + \cos[c + dx] \right) \csc[c] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]] \right]^2 \right. \\
& \quad \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \\
& \quad \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) / \\
& \quad \left( 3d \sqrt{1 + \cot[c]^2} \right) - \frac{1}{10d} 3A \left( 1 + \cos[c + dx] \right) \csc[c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \\
& \quad \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos[dx + \operatorname{ArcTan}[\tan[c]]] \right]^2 \right. \\
& \quad \left. \sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right) / \\
& \quad \left( \sqrt{1 - \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \right. \\
& \quad \left. \sqrt{\cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
& \quad \frac{\frac{\sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \right) - \frac{1}{2d} \\
& B \left( 1 + \cos[c + dx] \right) \csc[c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \right. \right. \\
& \quad \left. \left. \cos[dx + \operatorname{ArcTan}[\tan[c]]]^2 \sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right) \right) / \\
& \quad \left( \sqrt{1 - \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \right. \\
& \quad \left. \sqrt{\cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) -
\end{aligned}$$

$$\left( \frac{\frac{\sin[d x + \arctan[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \arctan[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \arctan[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right)$$

**Problem 485: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos[c + d x]^{3/2} (a + a \sec[c + d x]) (A + B \sec[c + d x]) dx$$

Optimal (type 4, 70 leaves, 6 steps):

$$\frac{2 a (A + B) \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{d} + \frac{2 a (A + 3 B) \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 d} + \frac{2 a A \sqrt{\cos[c + d x]} \sin[c + d x]}{3 d}$$

Result (type 5, 784 leaves):

$$\begin{aligned} & a \left( \sqrt{\cos[c + d x]} (1 + \cos[c + d x]) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \right. \\ & \quad \left( -\frac{(A + B) \cot[c]}{d} + \frac{A \cos[d x] \sin[c]}{3 d} + \frac{A \cos[c] \sin[d x]}{3 d} \right) - \\ & \quad \left( A (1 + \cos[c + d x]) \operatorname{Csc}[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \arctan[\cot[c]]]^2\right] \right. \\ & \quad \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sec[d x - \arctan[\cot[c]]] \sqrt{1 - \sin[d x - \arctan[\cot[c]]]} \\ & \quad \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \arctan[\cot[c]]] \sqrt{1 + \sin[d x - \arctan[\cot[c]]}} \right) \Big/ \\ & \quad \left( 3 d \sqrt{1 + \cot[c]^2} \right) - \frac{1}{d \sqrt{1 + \cot[c]^2}} B (1 + \cos[c + d x]) \operatorname{Csc}[c] \\ & \quad \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \arctan[\cot[c]]]^2\right] \\ & \quad \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \sec[d x - \arctan[\cot[c]]] \sqrt{1 - \sin[d x - \arctan[\cot[c]]]} \\ & \quad \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \arctan[\cot[c]]] \sqrt{1 + \sin[d x - \arctan[\cot[c]]}} - \right. \\ & \quad \left. \frac{1}{2 d} A (1 + \cos[c + d x]) \operatorname{Csc}[c] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \right) \end{aligned}$$

$$\begin{aligned}
& \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\tan [c]]]^2 \right] \right. \\
& \quad \left. \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\tan [c]]]} \right. \\
& \quad \sqrt{1 + \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \\
& \quad \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2}}} \left. \right) - \\
& \quad \frac{1}{2 d} B (1 + \cos [c + d x]) \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \right. \right. \\
& \quad \left. \left. \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\tan [c]]]^2 \right] \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\tan [c]]]} \right. \\
& \quad \left. \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) - \\
& \quad \left. \frac{\frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2}}} \right) \right)
\end{aligned}$$

**Problem 486: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \sqrt{\cos [c + d x]} (a + a \sec [c + d x]) (A + B \sec [c + d x]) dx$$

Optimal (type 4, 66 leaves, 6 steps):

$$\frac{2 a (A - B) \text{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{d} + \frac{2 a (A + B) \text{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{d} + \frac{2 a B \sin [c + d x]}{d \sqrt{\cos [c + d x]}}$$

Result (type 5, 783 leaves):

$$\begin{aligned}
& a \left( \sqrt{\cos[c+dx]} (1+\cos[c+dx]) \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \right. \\
& \quad \left( -\frac{(A-2B+A\cos[2c])\csc[c]\sec[c]}{2d} + \frac{B\sec[c]\sec[c+dx]\sin[dx]}{d} \right) - \frac{1}{d\sqrt{1+\cot[c]^2}} \\
& \quad A(1+\cos[c+dx])\csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \\
& \quad \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \operatorname{ArcTan}[\cot[c]]]} \\
& \quad \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \\
& \quad \sqrt{1+\sin[dx - \operatorname{ArcTan}[\cot[c]]]} - \frac{1}{d\sqrt{1+\cot[c]^2}} \\
& \quad B(1+\cos[c+dx])\csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]\right]^2 \\
& \quad \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \operatorname{ArcTan}[\cot[c]]]} \\
& \quad \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \operatorname{ArcTan}[\cot[c]]]} - \\
& \quad \frac{1}{2d} A(1+\cos[c+dx])\csc[c] \sec\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \\
& \quad \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \operatorname{ArcTan}[\tan[c]]]\right]^2 \right. \\
& \quad \left. \sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c] \right) / \left( \sqrt{1-\cos[dx + \operatorname{ArcTan}[\tan[c]]]} \right. \\
& \quad \sqrt{1+\cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2} \\
& \quad \left. \sqrt{1+\tan[c]^2} \right) - \frac{\frac{\sin[dx + \operatorname{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1+\tan[c]^2}} + \frac{2\cos[c]^2 \cos[dx + \operatorname{ArcTan}[\tan[c]]] \sqrt{1+\tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \operatorname{ArcTan}[\tan[c]]]} \sqrt{1+\tan[c]^2}} \Bigg) +
\end{aligned}$$

$$\frac{1}{2d} B (1 + \cos[c + dx]) \csc[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]^2\right] \sin[dx + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \left( \sqrt{1 - \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}}} \right)$$

**Problem 487: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + dx]) (A + B \sec[c + dx])}{\sqrt{\cos[c + dx]}} dx$$

Optimal (type 4, 95 leaves, 7 steps):

$$-\frac{2a(A+B) \text{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{d} + \frac{2a(3A+B) \text{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3d} + \frac{2aB \sin[c+dx]}{3d \cos[c+dx]^{3/2}} + \frac{2a(A+B) \sin[c+dx]}{d \sqrt{\cos[c+dx]}}$$

Result (type 5, 813 leaves):

$$a \left( \sqrt{\cos[c+dx]} (1 + \cos[c+dx]) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \frac{(A+B) \csc[c] \sec[c]}{d} + \frac{B \sec[c] \sec[c+dx]^2 \sin[dx]}{3d} + \frac{\sec[c] \sec[c+dx] (B \sin[c] + 3A \sin[dx] + 3B \sin[dx])}{3d} \right) - \frac{1}{d \sqrt{1 + \cot[c]^2}} \right) A (1 + \cos[c+dx]) \csc[c] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right]$$

$$\begin{aligned}
& \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sec[dx - \arctan[\cot[c]]] \sqrt{1 - \sin[dx - \arctan[\cot[c]]]} \\
& \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \arctan[\cot[c]]] \sqrt{1 + \sin[dx - \arctan[\cot[c]]]} -} \\
& \left( B(1 + \cos[c + dx]) \csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \arctan[\cot[c]]]^2\right] \right. \\
& \left. \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sec[dx - \arctan[\cot[c]]] \sqrt{1 - \sin[dx - \arctan[\cot[c]]]} \right. \\
& \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \arctan[\cot[c]]] \sqrt{1 + \sin[dx - \arctan[\cot[c]]]} \right) / \\
& \left( 3d\sqrt{1 + \cot[c]^2} \right) + \frac{1}{2d} A(1 + \cos[c + dx]) \csc[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \\
& \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \arctan[\tan[c]]]^2\right] \right. \\
& \left. \sin[dx + \arctan[\tan[c]]] \tan[c] \right) / \left( \sqrt{1 - \cos[dx + \arctan[\tan[c]]]} \right. \\
& \left. \sqrt{1 + \cos[dx + \arctan[\tan[c]]]} \sqrt{\cos[c] \cos[dx + \arctan[\tan[c]]] \sqrt{1 + \tan[c]^2}} \right. \\
& \left. \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[dx + \arctan[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \arctan[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \arctan[\tan[c]]] \sqrt{1 + \tan[c]^2}}} + \\
& \frac{1}{2d} B(1 + \cos[c + dx]) \csc[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \right. \right. \\
& \left. \left. \left\{\frac{3}{4}\right\}, \cos[dx + \arctan[\tan[c]]]^2\right] \sin[dx + \arctan[\tan[c]]] \tan[c] \right) / \\
& \left( \sqrt{1 - \cos[dx + \arctan[\tan[c]]]} \sqrt{1 + \cos[dx + \arctan[\tan[c]]]} \right. \\
& \left. \sqrt{\cos[c] \cos[dx + \arctan[\tan[c]]] \sqrt{1 + \tan[c]^2}} \sqrt{1 + \tan[c]^2} \right) -
\end{aligned}$$



$$\left( \frac{\frac{\sin[d x + \arctan[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[d x + \arctan[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[d x + \arctan[\tan[c]]] \sqrt{1 + \tan[c]^2}}} \right)$$

**Problem 488: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{(a + a \sec[c + d x]) (A + B \sec[c + d x])}{\cos[c + d x]^{3/2}} dx$$

Optimal (type 4, 132 leaves, 8 steps):

$$-\frac{2a(5A+3B)\operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{5d} + \frac{2a(A+B)\operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3d} +$$

$$\frac{2aB\sin[c+dx]}{5d\cos[c+dx]^{5/2}} + \frac{2a(A+B)\sin[c+dx]}{3d\cos[c+dx]^{3/2}} + \frac{2a(5A+3B)\sin[c+dx]}{5d\sqrt{\cos[c+dx]}}$$

Result (type 5, 865 leaves):

$$a \left( \sqrt{\cos[c+dx]} (1 + \cos[c+dx]) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \right.$$

$$\left( \frac{(5A+3B)\csc[c]\sec[c]}{5d} + \frac{B\sec[c]\sec[c+dx]^3\sin[dx]}{5d} + \right.$$

$$\left. \frac{\sec[c]\sec[c+dx]^2(3B\sin[c] + 5A\sin[dx] + 5B\sin[dx])}{15d} + \frac{1}{15d} \right.$$

$$\left. \sec[c]\sec[c+dx](5A\sin[c] + 5B\sin[c] + 15A\sin[dx] + 9B\sin[dx]) \right) -$$

$$\left( A(1 + \cos[c+dx])\csc[c]\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \arctan[\cot[c]]]^2\right] \right.$$

$$\sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \sec[dx - \arctan[\cot[c]]] \sqrt{1 - \sin[dx - \arctan[\cot[c]]]} \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \arctan[\cot[c]]]} \sqrt{1 + \sin[dx - \arctan[\cot[c]]]} \right) / \left( 3d\sqrt{1 + \cot[c]^2} \right) -$$

$$\left( B(1 + \cos[c+dx])\csc[c]\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \arctan[\cot[c]]]^2\right] \right.$$

$$\begin{aligned}
 & \left( \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \sec [dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin [dx - \text{ArcTan}[\text{Cot}[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin [c] \sin [dx - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 + \sin [dx - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
 & \left( 3d \sqrt{1 + \text{Cot}[c]^2} \right) + \frac{1}{2d} A (1 + \cos [c + dx]) \csc [c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \\
 & \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [dx + \text{ArcTan}[\text{Tan}[c]]]^2 \right] \right. \\
 & \left. \sin [dx + \text{ArcTan}[\text{Tan}[c]]] \tan [c] \right) / \\
 & \left( \sqrt{1 - \cos [dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \cos [dx + \text{ArcTan}[\text{Tan}[c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\frac{\sin [dx + \text{ArcTan}[\text{Tan}[c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}} \right) + \frac{1}{10d} \\
 & 3B (1 + \cos [c + dx]) \csc [c] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \right. \right. \\
 & \left. \left. \left\{ \frac{3}{4} \right\}, \cos [dx + \text{ArcTan}[\text{Tan}[c]]]^2 \right] \sin [dx + \text{ArcTan}[\text{Tan}[c]]] \tan [c] \right) / \\
 & \left( \sqrt{1 - \cos [dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \cos [dx + \text{ArcTan}[\text{Tan}[c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2}} \right) - \\
 & \left( \frac{\frac{\sin [dx + \text{ArcTan}[\text{Tan}[c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [dx + \text{ArcTan}[\text{Tan}[c]]] \sqrt{1 + \tan [c]^2}}} \right)
 \end{aligned}$$

Problem 489: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^{9/2} (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) dx$$

Optimal (type 4, 194 leaves, 9 steps):

$$\frac{4a^2(8A+9B) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{15d} + \frac{4a^2(5A+6B) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{21d} +$$

$$\frac{4a^2(5A+6B) \sqrt{\cos[c+dx]} \sin[c+dx]}{21d} + \frac{4a^2(8A+9B) \cos[c+dx]^{3/2} \sin[c+dx]}{45d} +$$

$$\frac{2a^2(11A+9B) \cos[c+dx]^{5/2} \sin[c+dx]}{63d} + \frac{2A \cos[c+dx]^{5/2} (a^2 + a^2 \cos[c+dx]) \sin[c+dx]}{9d}$$

Result (type 5, 1086 leaves):

$$\frac{1}{B+A \cos[c+dx]} \cos[c+dx]^{7/2} \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx])$$

$$\left( -\frac{(8A+9B) \cot[c]}{15d} + \frac{(46A+51B) \cos[dx] \sin[c]}{168d} + \frac{(37A+36B) \cos[2dx] \sin[2c]}{360d} + \right.$$

$$\frac{(2A+B) \cos[3dx] \sin[3c]}{56d} + \frac{A \cos[4dx] \sin[4c]}{144d} + \frac{(46A+51B) \cos[c] \sin[dx]}{168d} +$$

$$\left. \frac{(37A+36B) \cos[2c] \sin[2dx]}{360d} + \frac{(2A+B) \cos[3c] \sin[3dx]}{56d} + \frac{A \cos[4c] \sin[4dx]}{144d} \right) -$$

$$\frac{1}{21d(B+A \cos[c+dx])} \sqrt{1+\cot[c]^2} 5A \cos[c+dx]^3 \csc[c]$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]^2\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4$$

$$(a+a \sec[c+dx])^2 (A+B \sec[c+dx]) \sec[dx - \operatorname{ArcTan}[\cot[c]]]$$

$$\frac{\sqrt{1-\sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1+\sin[dx - \operatorname{ArcTan}[\cot[c]]]} - \frac{1}{7d(B+A \cos[c+dx]) \sqrt{1+\cot[c]^2}}}$$

$$2B \cos[c+dx]^3 \csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]^2\right]$$

$$\sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx])$$

$$\sec[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1-\sin[dx - \operatorname{ArcTan}[\cot[c]]]}$$

$$\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \operatorname{ArcTan}[\cot[c]]]} -$$

$$\begin{aligned}
 & \left( 4 A \cos [c+d x]^3 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \right. \\
 & \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2 \right] \right. \\
 & \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right. \\
 & \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \left. \right) / \\
 & (15 d (B+A \cos [c+d x])) - \left( 3 B \cos [c+d x]^3 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 \right. \\
 & (A+B \sec [c+d x]) \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2 \right] \right. \\
 & \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \\
 & \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2} \right) - \\
 & \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \left. \right) / (10 d (B+ \\
 & A \cos [c+d x]))
 \end{aligned}$$

Problem 490: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^{7 / 2} (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) d x$$

Optimal (type 4, 161 leaves, 8 steps):

$$\frac{4 a^2 (3 A+4 B) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d} + \frac{4 a^2 (6 A+7 B) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{21 d} +$$

$$\frac{4 a^2 (6 A+7 B) \sqrt{\cos [c+d x]} \sin [c+d x]}{21 d} + \frac{2 a^2 (9 A+7 B) \cos [c+d x]^{3 / 2} \sin [c+d x]}{35 d} +$$

$$\frac{2 A \cos [c+d x]^{3 / 2} \left(a^2+a^2 \cos [c+d x]\right) \sin [c+d x]}{7 d}$$

Result (type 5, 1040 leaves):

$$\frac{1}{B+A \cos [c+d x]}$$

$$\cos [c+d x]^{7 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \left(-\frac{(3 A+4 B) \cot [c]}{5 d} +\right.$$

$$\frac{(51 A+56 B) \cos [d x] \sin [c]}{168 d} + \frac{(2 A+B) \cos [2 d x] \sin [2 c]}{20 d} + \frac{A \cos [3 d x] \sin [3 c]}{56 d} +$$

$$\left.\frac{(51 A+56 B) \cos [c] \sin [d x]}{168 d} + \frac{(2 A+B) \cos [2 c] \sin [2 d x]}{20 d} + \frac{A \cos [3 c] \sin [3 d x]}{56 d}\right) -$$

$$\frac{1}{7 d(B+A \cos [c+d x]) \sqrt{1+\cot [c]^2}} 2 A \cos [c+d x]^3 \csc [c]$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4$$

$$(a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \sec [d x-\operatorname{ArcTan}[\cot [c]]]$$

$$\frac{\sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]}}{\sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \frac{1}{3 d(B+A \cos [c+d x]) \sqrt{1+\cot [c]^2}}}$$

$$B \cos [c+d x]^3 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x])$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} -$$

$$\begin{aligned}
 & \left( 3 A \cos [c+d x]^3 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \right. \\
 & \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]] \right]^2 \right. \\
 & \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \left. \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \right. \\
 & \left. \sqrt{1+\tan [c]^2} \right) - \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}}} \left. \right) / \\
 & (10 d (B+A \cos [c+d x])) - \left( 2 B \cos [c+d x]^3 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 \right. \\
 & (A+B \sec [c+d x]) \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]] \right]^2 \right. \\
 & \left. \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) / \\
 & \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2} \right) - \\
 & \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}}} \left. \right) / (5 d (B+A \cos [c+d x]))
 \end{aligned}$$

**Problem 491: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \cos [c+d x]^{5 / 2} \left(a+a \sec [c+d x]\right)^2 (A+B \sec [c+d x]) d x$$

Optimal (type 4, 126 leaves, 7 steps):

$$\frac{4 a^2 (4 A+5 B) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d}+\frac{4 a^2 (A+2 B) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d}+\frac{2 a^2 (7 A+5 B) \sqrt{\cos [c+d x]} \sin [c+d x]}{15 d}+\frac{2 A \sqrt{\cos [c+d x]} \left(a^2+a^2 \cos [c+d x]\right) \sin [c+d x]}{5 d}$$

Result (type 5, 994 leaves):

$$\frac{1}{B+A \cos [c+d x]} \cos [c+d x]^{7 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \left(a+a \sec [c+d x]\right)^2 (A+B \sec [c+d x])$$

$$\left(-\frac{(4 A+5 B) \cot [c]}{5 d}+\frac{(2 A+B) \cos [d x] \sin [c]}{6 d}+\frac{A \cos [2 d x] \sin [2 c]}{20 d}+\frac{(2 A+B) \cos [c] \sin [d x]}{6 d}+\frac{A \cos [2 c] \sin [2 d x]}{20 d}\right)-\frac{1}{3 d(B+A \cos [c+d x]) \sqrt{1+\cot [c]^2}}$$

$$A \cos [c+d x]^3 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \left(a+a \sec [c+d x]\right)^2 (A+B \sec [c+d x]) \sec [d x-\operatorname{ArcTan}[\cot [c]]]$$

$$\sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-\frac{1}{3 d(B+A \cos [c+d x]) \sqrt{1+\cot [c]^2}}$$

$$2 B \cos [c+d x]^3 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right]$$

$$\sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \left(a+a \sec [c+d x]\right)^2 (A+B \sec [c+d x])$$

$$\sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]}$$

$$\sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]}-$$

$$\left(2 A \cos [c+d x]^3 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \left(a+a \sec [c+d x]\right)^2 (A+B \sec [c+d x])\right)$$

$$\begin{aligned}
& \left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\tan [c]]] \right]^2 \right) \right. \\
& \quad \left. \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\tan [c]]]} \right. \\
& \quad \left. \sqrt{1 + \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right. \\
& \quad \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2}}} \left. \right) / \\
& (5 d (B + A \cos [c + d x])) - \left( B \cos [c + d x]^3 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a + a \sec [c + d x])^2 \right. \\
& (A + B \sec [c + d x]) \left( \left( \text{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \text{ArcTan} [\tan [c]]] \right]^2 \right) \right. \\
& \quad \left. \sin [d x + \text{ArcTan} [\tan [c]]] \tan [c] \right) / \\
& \left( \sqrt{1 - \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \cos [d x + \text{ArcTan} [\tan [c]]]} \right. \\
& \quad \left. \sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) - \\
& \frac{\frac{\sin [d x + \text{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \text{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \text{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2}}} \left. \right) / (2 d (B + A \cos [c + d x]))
\end{aligned}$$

Problem 492: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.



$$\int \cos [c+d x]^{3 / 2} (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) d x$$

Optimal (type 4, 116 leaves, 7 steps):

$$\frac{4 a^2 A \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d} + \frac{4 a^2 (2 A+3 B) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d} +$$

$$\frac{2 a^2 (A-3 B) \sqrt{\cos [c+d x]} \sin [c+d x]}{3 d} + \frac{2 B \left(a^2+a^2 \cos [c+d x]\right) \sin [c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 5, 735 leaves):

$$\begin{aligned}
& \frac{1}{B+A \cos [c+d x]} \cos [c+d x]^{7 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \\
& \left( -\frac{(2 A-B+2 A \cos [2 c]+B \cos [2 c]) \csc [c] \sec [c]}{4 d} + \frac{A \cos [d x] \sin [c]}{6 d} + \right. \\
& \quad \left. \frac{A \cos [c] \sin [d x]}{6 d} + \frac{B \sec [c] \sec [c+d x] \sin [d x]}{2 d} \right) - \frac{1}{3 d (B+A \cos [c+d x]) \sqrt{1+\cot [c]^2}} \\
& 2 A \cos [c+d x]^3 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\
& \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \sec [d x-\operatorname{ArcTan}[\cot [c]]] \\
& \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
& \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \frac{1}{d (B+A \cos [c+d x]) \sqrt{1+\cot [c]^2}} \\
& B \cos [c+d x]^3 \csc [c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\},\left\{\frac{5}{4}\right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2\right] \\
& \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \\
& \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
& \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\
& \left( A \cos [c+d x]^3 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \right. \\
& \quad \left( \operatorname{HypergeometricPFQ}\left[\left\{-\frac{1}{2},-\frac{1}{4}\right\},\left\{\frac{3}{4}\right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2\right] \sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c] \right) \\
& \quad \left. \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
& \quad \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2} \right) - \\
& \quad \left. \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) / (2 d (B+A \cos [c+d x]))
\end{aligned}$$

Problem 493: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{\cos[c+dx]} (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) dx$$

Optimal (type 4, 120 leaves, 7 steps):

$$-\frac{4a^2B \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{d} + \frac{4a^2(3A+2B) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3d} +$$

$$\frac{2a^2(3A+5B) \sin[c+dx]}{3d\sqrt{\cos[c+dx]}} + \frac{2B(a^2+a^2\cos[c+dx]) \sin[c+dx]}{3d\cos[c+dx]^{3/2}}$$

Result (type 5, 736 leaves):

$$\begin{aligned}
& \frac{1}{B+A \cos [c+d x]} \cos [c+d x]^{7 / 2} \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \\
& \left( -\frac{(-A-4 B+A \cos [2 c]) \csc [c] \sec [c]}{4 d} + \frac{B \sec [c] \sec [c+d x]^2 \sin [d x]}{6 d} + \right. \\
& \quad \left. \frac{\sec [c] \sec [c+d x] (B \sin [c]+3 A \sin [d x]+6 B \sin [d x])}{6 d} \right) - \\
& \frac{1}{d (B+A \cos [c+d x]) \sqrt{1+\cot [c]^2}} A \cos [c+d x]^3 \csc [c] \operatorname{HypergeometricPFQ} \left[ \right. \\
& \quad \left. \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2 \right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\
& \quad (A+B \sec [c+d x]) \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
& \quad \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} - \\
& \frac{1}{3 d (B+A \cos [c+d x]) \sqrt{1+\cot [c]^2}} 2 B \cos [c+d x]^3 \csc [c] \operatorname{HypergeometricPFQ} \left[ \right. \\
& \quad \left. \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x-\operatorname{ArcTan}[\cot [c]]]^2 \right] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 \\
& \quad (A+B \sec [c+d x]) \sec [d x-\operatorname{ArcTan}[\cot [c]]] \sqrt{1-\sin [d x-\operatorname{ArcTan}[\cot [c]]]} \\
& \quad \sqrt{-\sqrt{1+\cot [c]^2} \sin [c] \sin [d x-\operatorname{ArcTan}[\cot [c]]]} \sqrt{1+\sin [d x-\operatorname{ArcTan}[\cot [c]]]} + \\
& \left( B \cos [c+d x]^3 \csc [c] \sec \left[\frac{c}{2}+\frac{d x}{2}\right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \right. \\
& \quad \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x+\operatorname{ArcTan}[\tan [c]]]^2 \right] \sin [d x+\operatorname{ArcTan}[\tan [c]]] \right. \\
& \quad \left. \left. \tan [c] \right) \right) / \left( \sqrt{1-\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\cos [d x+\operatorname{ArcTan}[\tan [c]]]} \right. \\
& \quad \left. \sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2} \sqrt{1+\tan [c]^2} \right) - \\
& \quad \left. \frac{\frac{\sin [d x+\operatorname{ArcTan}[\tan [c]]] \tan [c]}{\sqrt{1+\tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x+\operatorname{ArcTan}[\tan [c]]] \sqrt{1+\tan [c]^2}}{\cos [c]^2+\sin [c]^2}}{\sqrt{\cos [c] \cos [d x+\operatorname{ArcTan}[\tan [c]]]} \sqrt{1+\tan [c]^2}} \right) / (2 d (B+A \cos [c+d x]))
\end{aligned}$$

Problem 494: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sec[c + d x])^2 (A + B \sec[c + d x])}{\sqrt{\cos[c + d x]}} dx$$

Optimal (type 4, 159 leaves, 8 steps):

$$-\frac{4 a^2 (5 A + 4 B) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{4 a^2 (2 A + B) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 d} +$$

$$\frac{2 a^2 (5 A + 7 B) \sin[c + d x]}{15 d \cos[c + d x]^{3/2}} + \frac{4 a^2 (5 A + 4 B) \sin[c + d x]}{5 d \sqrt{\cos[c + d x]}} + \frac{2 B (a^2 + a^2 \cos[c + d x]) \sin[c + d x]}{5 d \cos[c + d x]^{5/2}}$$

Result (type 5, 1025 leaves):

$$\frac{1}{B + A \cos[c + d x]} \cos[c + d x]^{7/2} \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2$$

$$(A + B \sec[c + d x]) \left( \frac{(5 A + 4 B) \csc[c] \sec[c]}{5 d} + \frac{B \sec[c] \sec[c + d x]^3 \sin[d x]}{10 d} + \right.$$

$$\frac{\sec[c] \sec[c + d x]^2 (3 B \sin[c] + 5 A \sin[d x] + 10 B \sin[d x])}{30 d} + \frac{1}{30 d}$$

$$\left. \sec[c] \sec[c + d x] (5 A \sin[c] + 10 B \sin[c] + 30 A \sin[d x] + 24 B \sin[d x]) \right) -$$

$$\frac{1}{3 d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2}} 2 A \cos[c + d x]^3 \csc[c]$$

$$\operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4$$

$$(a + a \sec[c + d x])^2 (A + B \sec[c + d x]) \sec[d x - \operatorname{ArcTan}[\cot[c]]]$$

$$\sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]}$$

$$\sqrt{1 + \sin[d x - \operatorname{ArcTan}[\cot[c]]]} - \frac{1}{3 d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2}}$$

$$B \cos[c + d x]^3 \csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right]$$

$$\sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 (A + B \sec[c + d x])$$

$$\sec[d x - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]}$$

$$\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[d x - \operatorname{ArcTan}[\cot[c]]]} +$$

$$\begin{aligned}
 & \left( A \cos[c+dx]^3 \csc[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 (A+B \sec[c+dx]) \right. \\
 & \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]\right]^2 \right. \\
 & \left. \sin[dx + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \left( \sqrt{1 - \cos[dx + \text{ArcTan}[\tan[c]]]} \right. \\
 & \left. \sqrt{1 + \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \right. \\
 & \left. \sqrt{1 + \tan[c]^2} \right) - \frac{\frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \left. \right) / \\
 & (2d(B + A \cos[c+dx])) + \left( 2B \cos[c+dx]^3 \csc[c] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (a+a \sec[c+dx])^2 \right. \\
 & (A+B \sec[c+dx]) \left( \text{HypergeometricPFQ}\left[\left\{-\frac{1}{2}, -\frac{1}{4}\right\}, \left\{\frac{3}{4}\right\}, \cos[dx + \text{ArcTan}[\tan[c]]]\right]^2 \right. \\
 & \left. \sin[dx + \text{ArcTan}[\tan[c]]] \tan[c] \right) / \\
 & \left( \sqrt{1 - \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \cos[dx + \text{ArcTan}[\tan[c]]]} \right. \\
 & \left. \sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2} \sqrt{1 + \tan[c]^2} \right) - \\
 & \frac{\frac{\sin[dx + \text{ArcTan}[\tan[c]]] \tan[c]}{\sqrt{1 + \tan[c]^2}} + \frac{2 \cos[c]^2 \cos[dx + \text{ArcTan}[\tan[c]]] \sqrt{1 + \tan[c]^2}}{\cos[c]^2 + \sin[c]^2}}{\sqrt{\cos[c] \cos[dx + \text{ArcTan}[\tan[c]]]} \sqrt{1 + \tan[c]^2}} \left. \right) / (5d(B + A \cos[c+dx]))
 \end{aligned}$$

Problem 495: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sec[c + d x])^2 (A + B \sec[c + d x])}{\cos[c + d x]^{3/2}} dx$$

Optimal (type 4, 194 leaves, 9 steps):

$$\begin{aligned} & -\frac{4 a^2 (4 A + 3 B) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{5 d} + \frac{4 a^2 (7 A + 6 B) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d} + \\ & \frac{2 a^2 (7 A + 9 B) \sin[c + d x]}{35 d \cos[c + d x]^{5/2}} + \frac{4 a^2 (7 A + 6 B) \sin[c + d x]}{21 d \cos[c + d x]^{3/2}} + \\ & \frac{4 a^2 (4 A + 3 B) \sin[c + d x]}{5 d \sqrt{\cos[c + d x]}} + \frac{2 B (a^2 + a^2 \cos[c + d x]) \sin[c + d x]}{7 d \cos[c + d x]^{7/2}} \end{aligned}$$

Result (type 5, 1067 leaves):

$$\begin{aligned} & \frac{1}{B + A \cos[c + d x]} \cos[c + d x]^{7/2} \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 \\ & (A + B \sec[c + d x]) \left( \frac{(4 A + 3 B) \csc[c] \sec[c]}{5 d} + \frac{B \sec[c] \sec[c + d x]^4 \sin[d x]}{14 d} + \right. \\ & \quad \frac{\sec[c] \sec[c + d x]^3 (5 B \sin[c] + 7 A \sin[d x] + 14 B \sin[d x])}{70 d} + \frac{1}{210 d} \\ & \quad \sec[c] \sec[c + d x]^2 (21 A \sin[c] + 42 B \sin[c] + 70 A \sin[d x] + 60 B \sin[d x]) + \frac{1}{105 d} \\ & \quad \left. \sec[c] \sec[c + d x] (35 A \sin[c] + 30 B \sin[c] + 84 A \sin[d x] + 63 B \sin[d x]) \right) - \\ & \frac{1}{3 d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2}} A \cos[c + d x]^3 \csc[c] \\ & \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \\ & (a + a \sec[c + d x])^2 (A + B \sec[c + d x]) \sec[d x - \operatorname{ArcTan}[\cot[c]]] \\ & \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\ & \sqrt{1 + \sin[d x - \operatorname{ArcTan}[\cot[c]]]} - \frac{1}{7 d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2}} \\ & 2 B \cos[c + d x]^3 \csc[c] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right] \\ & \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (a + a \sec[c + d x])^2 (A + B \sec[c + d x]) \\ & \sec[d x - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\ & \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[d x - \operatorname{ArcTan}[\cot[c]]]} + \end{aligned}$$

$$\begin{aligned}
 & \left( 2 A \cos [c+d x]^3 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 (A+B \sec [c+d x]) \right. \\
 & \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \operatorname{ArcTan} [\tan [c]]] \right]^2 \right. \\
 & \left. \sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c] \right) / \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan} [\tan [c]]]} \right. \\
 & \left. \sqrt{1 + \cos [d x + \operatorname{ArcTan} [\tan [c]]]} \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \right. \\
 & \left. \sqrt{1 + \tan [c]^2} \right) - \frac{\frac{\sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2}}} \left. \right) / \\
 & (5 d (B + A \cos [c+d x])) + \left( 3 B \cos [c+d x]^3 \csc [c] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (a+a \sec [c+d x])^2 \right. \\
 & (A+B \sec [c+d x]) \left( \operatorname{HypergeometricPFQ} \left[ \left\{ -\frac{1}{2}, -\frac{1}{4} \right\}, \left\{ \frac{3}{4} \right\}, \cos [d x + \operatorname{ArcTan} [\tan [c]]] \right]^2 \right. \\
 & \left. \sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c] \right) / \\
 & \left( \sqrt{1 - \cos [d x + \operatorname{ArcTan} [\tan [c]]]} \sqrt{1 + \cos [d x + \operatorname{ArcTan} [\tan [c]]]} \right. \\
 & \left. \sqrt{\cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2} \sqrt{1 + \tan [c]^2} \right) - \\
 & \frac{\frac{\sin [d x + \operatorname{ArcTan} [\tan [c]]] \tan [c]}{\sqrt{1 + \tan [c]^2}} + \frac{2 \cos [c]^2 \cos [d x + \operatorname{ArcTan} [\tan [c]]] \sqrt{1 + \tan [c]^2}}{\cos [c]^2 + \sin [c]^2}}{\sqrt{\cos [c] \cos [d x + \operatorname{ArcTan} [\tan [c]]]} \sqrt{1 + \tan [c]^2}}} \left. \right) / (10 d (B + \\
 & A \cos [c+d x]))
 \end{aligned}$$



Problem 496: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx]^{5/2} (A + B \sec[c + dx])}{a + a \sec[c + dx]} dx$$

Optimal (type 4, 157 leaves, 7 steps):

$$\frac{3(7A - 5B) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{5ad} - \frac{5(A - B) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{3ad} - \frac{5(A - B) \sqrt{\cos[c + dx]} \sin[c + dx]}{3ad} + \frac{(7A - 5B) \cos[c + dx]^{3/2} \sin[c + dx]}{5ad} - \frac{(A - B) \cos[c + dx]^{5/2} \sin[c + dx]}{d(a + a \cos[c + dx])}$$

Result (type 5, 1292 leaves):

$$\frac{1}{20(B + A \cos[c + dx])(a + a \sec[c + dx])} 21i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Csc}\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx]) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \sqrt{e^{-ix}(2(1 + e^{2ix})\cos[c] + 2i(-1 + e^{2ix})\sin[c])} \sqrt{1 + e^{2ix}\cos[2c] + i e^{2ix}\sin[2c]} \right) / \right. \\ \left. (3id(1 + e^{2ix})\cos[c] - 3d(-1 + e^{2ix})\sin[c]) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \sqrt{e^{-ix}(2(1 + e^{2ix})\cos[c] + 2i(-1 + e^{2ix})\sin[c])} \sqrt{1 + e^{2ix}\cos[2c] + i e^{2ix}\sin[2c]} \right) / \right. \\ \left. (-id(1 + e^{2ix})\cos[c] + d(-1 + e^{2ix})\sin[c]) \right) - \frac{1}{4(B + A \cos[c + dx])(a + a \sec[c + dx])} \frac{3}{i} B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Csc}\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] (A + B \sec[c + dx]) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\begin{aligned}
& \left( \frac{\sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
& \left( 3 i d \left( 1 + e^{2 i d x} \right) \cos [c] - 3 d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \\
& \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} \left( \cos [c] + i \sin [c] \right)^2 \right] \right. \\
& \left. \frac{\sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
& \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) \Bigg) + \\
& \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sqrt{\cos [c + d x]} \left( A + B \sec [c + d x] \right) \right. \\
& \left( \frac{2 \left( -5 A + 5 B - 16 A \cos [c] + 10 B \cos [c] \right) \csc [c]}{5 d} + \frac{4 (-A + B) \cos [d x] \sin [c]}{3 d} + \right. \\
& \frac{2 A \cos [2 d x] \sin [2 c]}{5 d} + \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( -A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right] \right)}{d} + \\
& \left. \frac{4 (-A + B) \cos [c] \sin [d x]}{3 d} + \frac{2 A \cos [2 c] \sin [2 d x]}{5 d} \right) \Bigg) / \\
& \left( (B + A \cos [c + d x]) (a + a \sec [c + d x]) \right) + \\
& \left( 5 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]]^2 \right] \right. \\
& \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x]) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
& \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
& \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
& \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) / \\
& \left( 3 d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x]) \right) - \\
& \left( 5 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]]^2 \right] \right. \\
& \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x]) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
& \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) /
\end{aligned}$$

$$\left( 3 d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x]) \right)$$

**Problem 497: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c + d x]^{3/2} (A + B \sec [c + d x])}{a + a \sec [c + d x]} dx$$

Optimal (type 4, 124 leaves, 6 steps):

$$-\frac{3(A-B) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{ad} + \frac{(5A-3B) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3ad} +$$

$$\frac{(5A-3B) \sqrt{\cos [c+dx]} \sin [c+dx]}{3ad} - \frac{(A-B) \cos [c+dx]^{3/2} \sin [c+dx]}{d(a+a \cos [c+dx])}$$

Result (type 5, 1239 leaves):

$$-\frac{1}{4(B+A \cos [c+dx])(a+a \sec [c+dx])} 3 \operatorname{Im} A \cos \left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]$$

$$(A+B \sec [c+dx]) \left( \left( 2 e^{2 \operatorname{Im} dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 \operatorname{Im} dx} (\cos [c] + \operatorname{Im} \sin [c])^2\right] \right. \right.$$

$$\frac{\sqrt{e^{-\operatorname{Im} dx} (2 (1 + e^{2 \operatorname{Im} dx}) \cos [c] + 2 \operatorname{Im} (-1 + e^{2 \operatorname{Im} dx}) \sin [c])}}{\sqrt{1 + e^{2 \operatorname{Im} dx} \cos [2c] + \operatorname{Im} e^{2 \operatorname{Im} dx} \sin [2c]}} \Bigg) /$$

$$(3 \operatorname{Im} d (1 + e^{2 \operatorname{Im} dx}) \cos [c] - 3 d (-1 + e^{2 \operatorname{Im} dx}) \sin [c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 \operatorname{Im} dx} (\cos [c] + \operatorname{Im} \sin [c])^2\right] \right.$$

$$\frac{\sqrt{e^{-\operatorname{Im} dx} (2 (1 + e^{2 \operatorname{Im} dx}) \cos [c] + 2 \operatorname{Im} (-1 + e^{2 \operatorname{Im} dx}) \sin [c])}}{\sqrt{1 + e^{2 \operatorname{Im} dx} \cos [2c] + \operatorname{Im} e^{2 \operatorname{Im} dx} \sin [2c]}} \Bigg) /$$

$$\left. (-\operatorname{Im} d (1 + e^{2 \operatorname{Im} dx}) \cos [c] + d (-1 + e^{2 \operatorname{Im} dx}) \sin [c]) \right) +$$

$$\frac{1}{4(B+A \cos [c+dx])(a+a \sec [c+dx])}$$

$$3$$

$$\operatorname{Im}$$

$$B$$

$$\cos \left[\frac{c}{2} + \frac{dx}{2}\right]^2$$

$$\operatorname{Csc}\left[\frac{c}{2}\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}\right]$$

$$(A+B \sec [c+dx])$$

$$\left( \left( 2 e^{2 \operatorname{Im} dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 \operatorname{Im} dx} (\cos [c] + \operatorname{Im} \sin [c])^2\right] \right. \right.$$

$$\begin{aligned}
& \frac{\sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \Bigg/ \\
& \left( 3 i d \left( 1 + e^{2 i d x} \right) \cos [c] - 3 d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \\
& \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} \left( \cos [c] + i \sin [c] \right)^2 \right] \right. \\
& \left. \frac{\sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \Bigg/ \\
& \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) \Bigg) + \\
& \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sqrt{\cos [c + d x]} \left( A + B \sec [c + d x] \right) \right. \\
& \left( -\frac{2 (-A + B) (1 + 2 \cos [c]) \csc [c]}{d} + \frac{4 A \cos [d x] \sin [c]}{3 d} - \right. \\
& \left. \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( -A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right] \right)}{d} + \frac{4 A \cos [c] \sin [d x]}{3 d} \right) \Bigg) \Bigg/ \\
& \left( (B + A \cos [c + d x]) (a + a \sec [c + d x]) \right) - \\
& \left( 5 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \right. \\
& \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]]^2 \right] \\
& \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x]) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
& \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
& \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
& \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) \Bigg/ \\
& \left( 3 d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x]) \right) + \\
& \left( B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]]^2 \right] \right. \\
& \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x]) \sec [d x - \operatorname{ArcTan} [\cot [c]]] \\
& \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
& \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right)
\end{aligned}$$

$$\left. \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} \right) /$$

$$\left( d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + d x]) \right)$$

**Problem 498: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cos[c + d x]} (A + B \sec[c + d x])}{a + a \sec[c + d x]} dx$$

Optimal (type 4, 88 leaves, 5 steps):

$$\frac{(3A - B) \text{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{ad} -$$

$$\frac{(A - B) \text{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{ad} - \frac{(A - B) \sqrt{\cos[c + dx]} \sin[c + dx]}{d(a + a \cos[c + dx])}$$

Result (type 5, 1208 leaves):

$$\frac{1}{4 (B + A \cos[c + d x]) (a + a \sec[c + d x])} 3 i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right]$$

$$(A + B \sec[c + d x]) \left( \left( 2 e^{2 i dx} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2c] + i e^{2 i dx} \sin[2c]}} \right) /$$

$$(3 i d (1 + e^{2 i dx}) \cos[c] - 3 d (-1 + e^{2 i dx}) \sin[c]) -$$

$$\left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\cos[c] + i \sin[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \cos[c] + 2 i (-1 + e^{2 i dx}) \sin[c])}}{\sqrt{1 + e^{2 i dx} \cos[2c] + i e^{2 i dx} \sin[2c]}} \right) /$$

$$(-i d (1 + e^{2 i dx}) \cos[c] + d (-1 + e^{2 i dx}) \sin[c]) \Big) -$$

$$\frac{1}{4 (B + A \cos[c + d x]) (a + a \sec[c + d x])}$$

$$i$$

$$B$$

$$\cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2$$

$$\csc\left[\frac{c}{2}\right]$$

$$\sec\left[\frac{c}{2}\right]$$

$$(A + B \sec[c + d x])$$

$$\begin{aligned}
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right. \right. \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right. \\
 & \quad \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) + \\
 & \quad \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sqrt{\cos[c + d x]} (A + B \sec[c + d x]) \right. \\
 & \quad \left. \left( -\frac{2 (A - B + 2 A \cos[c]) \csc[c]}{d} + \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] (-A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right])}{d} \right) \right) / \\
 & \quad ((B + A \cos[c + d x]) (a + a \sec[c + d x])) + \\
 & \quad \left( A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin[d x - \text{ArcTan}[\cot[c]]] \right]^2 \right. \\
 & \quad \sec \left[ \frac{c}{2} \right] (A + B \sec[c + d x]) \sec[d x - \text{ArcTan}[\cot[c]]] \\
 & \quad \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \\
 & \quad \left. \left. \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} \right) \right) / \\
 & \quad \left( d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + d x]) \right) - \\
 & \quad \left( B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin[d x - \text{ArcTan}[\cot[c]]] \right]^2 \right. \\
 & \quad \sec \left[ \frac{c}{2} \right] (A + B \sec[c + d x]) \sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \quad \left( d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + d x]) \right)
 \end{aligned}$$

Problem 499: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\sqrt{\operatorname{Cos}[c + d x]} (a + a \operatorname{Sec}[c + d x])} dx$$

Optimal (type 4, 83 leaves, 5 steps):

$$-\frac{(A-B) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{ad} + \frac{(A+B) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{ad} + \frac{(A-B) \sqrt{\operatorname{Cos}[c+dx]} \operatorname{Sin}[c+dx]}{d(a+a \operatorname{Cos}[c+dx])}$$

Result (type 5, 1204 leaves):

$$\begin{aligned} & -\frac{1}{4(B+A \operatorname{Cos}[c+dx])(a+a \operatorname{Sec}[c+dx])} \operatorname{Im} A \operatorname{Cos}\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A+B \operatorname{Sec}[c+dx]) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\operatorname{Cos}[c]+i \operatorname{Sin}[c])^2\right] \right. \right. \\ & \quad \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \operatorname{Cos}[c]+2 i\left(-1+e^{2 i d x}\right) \operatorname{Sin}[c]\right)} \right. \\ & \quad \left. \sqrt{1+e^{2 i d x} \operatorname{Cos}[2 c]+i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \\ & \quad \left( 3 i d\left(1+e^{2 i d x}\right) \operatorname{Cos}[c]-3 d\left(-1+e^{2 i d x}\right) \operatorname{Sin}[c]\right)- \\ & \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x}(\operatorname{Cos}[c]+i \operatorname{Sin}[c])^2\right] \right. \\ & \quad \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \operatorname{Cos}[c]+2 i\left(-1+e^{2 i d x}\right) \operatorname{Sin}[c]\right)} \right. \\ & \quad \left. \sqrt{1+e^{2 i d x} \operatorname{Cos}[2 c]+i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \\ & \quad \left. \left(-i d\left(1+e^{2 i d x}\right) \operatorname{Cos}[c]+d\left(-1+e^{2 i d x}\right) \operatorname{Sin}[c]\right) \right) + \\ & \frac{1}{4(B+A \operatorname{Cos}[c+dx])(a+a \operatorname{Sec}[c+dx])} \\ & \operatorname{Im} \\ & B \\ & \operatorname{Cos}\left[\frac{c}{2}+\frac{dx}{2}\right]^2 \\ & \operatorname{Csc}\left[\frac{c}{2}\right] \\ & \operatorname{Sec}\left[\frac{c}{2}\right] \\ & (A+B \operatorname{Sec}[c+dx]) \\ & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x}(\operatorname{Cos}[c]+i \operatorname{Sin}[c])^2\right] \right. \right. \\ & \quad \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \operatorname{Cos}[c]+2 i\left(-1+e^{2 i d x}\right) \operatorname{Sin}[c]\right)} \right. \\ & \quad \left. \sqrt{1+e^{2 i d x} \operatorname{Cos}[2 c]+i e^{2 i d x} \operatorname{Sin}[2 c]} \right) / \\ & \quad \left( 3 i d\left(1+e^{2 i d x}\right) \operatorname{Cos}[c]-3 d\left(-1+e^{2 i d x}\right) \operatorname{Sin}[c]\right)- \end{aligned}$$

$$\begin{aligned}
& \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2 \right] \right. \\
& \quad \sqrt{e^{-i d x} \left( 2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c] \right)} \\
& \quad \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
& \quad \left( -i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c] \right) + \\
& \quad \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sqrt{\cos[c + d x]} (A + B \sec[c + d x]) \right. \\
& \quad \left. \left( -\frac{2 (-A + B) \csc[c]}{d} - \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] (-A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right])}{d} \right) \right) / \\
& \quad \left( (B + A \cos[c + d x]) (a + a \sec[c + d x]) \right) - \\
& \quad \left( A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]] \right]^2 \right. \\
& \quad \sec \left[ \frac{c}{2} \right] (A + B \sec[c + d x]) \sec[d x - \operatorname{ArcTan}[\cot[c]]] \\
& \quad \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\
& \quad \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\
& \quad \left. \left. \sqrt{1 + \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \right) \right) / \\
& \quad \left( d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + d x]) \right) - \\
& \quad \left( B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]] \right]^2 \right. \\
& \quad \sec \left[ \frac{c}{2} \right] (A + B \sec[c + d x]) \sec[d x - \operatorname{ArcTan}[\cot[c]]] \\
& \quad \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\
& \quad \left. \left. \sqrt{1 + \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \right) \right) / \\
& \quad \left( d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + d x]) \right)
\end{aligned}$$

**Problem 500:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.



$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\cos[c + d x]^{3/2} (a + a \operatorname{Sec}[c + d x])} dx$$

Optimal (type 4, 113 leaves, 6 steps):

$$\frac{(A - 3B) \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{a d} + \frac{(A - B) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{a d} - \frac{(A - 3B) \operatorname{Sin}[c + d x]}{a d \sqrt{\cos[c + d x]}} + \frac{(A - B) \operatorname{Sin}[c + d x]}{d \sqrt{\cos[c + d x]} (a + a \cos[c + d x])}$$

Result (type 5, 1240 leaves):

$$\frac{1}{4 (B + A \cos[c + d x]) (a + a \operatorname{Sec}[c + d x])} \operatorname{Im} A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + d x]) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \right. \\ \left. (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \right. \\ \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) - \frac{1}{4 (B + A \cos[c + d x]) (a + a \operatorname{Sec}[c + d x])} \frac{3}{i} B \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (A + B \operatorname{Sec}[c + d x]) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \right. \\ \left. (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \right. \\ \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right)$$

$$\begin{aligned}
 & \frac{\sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \Bigg/ \\
 & \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sqrt{\cos [c + d x]} \left( A + B \sec [c + d x] \right) \right. \\
 & \left( \frac{\left( 2 B - A \cos [c] + B \cos [c] \right) \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c]}{d} + \right. \\
 & \left. \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( -A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right] \right)}{d} + \frac{4 B \sec [c] \sec [c + d x] \sin [d x]}{d} \right) \Bigg/ \\
 & \left( \left( B + A \cos [c + d x] \right) \left( a + a \sec [c + d x] \right) \right) - \\
 & \left( A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \sec \left[ \frac{c}{2} \right] \left( A + B \sec [c + d x] \right) \sec [d x - \text{ArcTan} [\cot [c]]] \\
 & \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) \Bigg/ \\
 & \left( d \left( B + A \cos [c + d x] \right) \sqrt{1 + \cot [c]^2} \left( a + a \sec [c + d x] \right) \right) + \\
 & \left( B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \sec \left[ \frac{c}{2} \right] \left( A + B \sec [c + d x] \right) \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) \Bigg/ \\
 & \left( d \left( B + A \cos [c + d x] \right) \sqrt{1 + \cot [c]^2} \left( a + a \sec [c + d x] \right) \right)
 \end{aligned}$$

**Problem 501:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \sec [c + d x]}{\cos [c + d x]^{5/2} (a + a \sec [c + d x])} dx$$

Optimal (type 4, 152 leaves, 7 steps):

$$-\frac{3(A-B) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{ad} - \frac{(3A-5B) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3ad} -$$

$$\frac{(3A-5B) \sin[c+dx]}{3ad \cos[c+dx]^{3/2}} + \frac{3(A-B) \sin[c+dx]}{ad \sqrt{\cos[c+dx]}} + \frac{(A-B) \sin[c+dx]}{d \cos[c+dx]^{3/2} (a+a \cos[c+dx])}$$

Result (type 5, 1277 leaves):

$$-\frac{1}{4(B+A \cos[c+dx])(a+a \sec[c+dx])} 3iA \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right]$$

$$(A+B \sec[c+dx]) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\cos[c] + 2i(-1+e^{2ix})\sin[c])}}{\sqrt{1+e^{2ix}\cos[2c] + i e^{2ix}\sin[2c]}} \right) /$$

$$(3id(1+e^{2ix})\cos[c] - 3d(-1+e^{2ix})\sin[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\cos[c] + 2i(-1+e^{2ix})\sin[c])}}{\sqrt{1+e^{2ix}\cos[2c] + i e^{2ix}\sin[2c]}} \right) /$$

$$(-id(1+e^{2ix})\cos[c] + d(-1+e^{2ix})\sin[c]) \Big) +$$

$$\frac{1}{4(B+A \cos[c+dx])(a+a \sec[c+dx])}$$

$$3$$

$$i$$

$$B$$

$$\cos\left[\frac{c}{2} + \frac{dx}{2}\right]^2$$

$$\operatorname{Csc}\left[\frac{c}{2}\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}\right]$$

$$(A+B \sec[c+dx])$$

$$\left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\cos[c] + 2i(-1+e^{2ix})\sin[c])}}{\sqrt{1+e^{2ix}\cos[2c] + i e^{2ix}\sin[2c]}} \right) /$$

$$(3id(1+e^{2ix})\cos[c] - 3d(-1+e^{2ix})\sin[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\cos[c] + 2i(-1+e^{2ix})\sin[c])}}{\sqrt{1+e^{2ix}\cos[2c] + i e^{2ix}\sin[2c]}} \right) /$$

$$\begin{aligned}
 & \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \sqrt{\cos [c + d x]} (A + B \sec [c + d x]) \right. \\
 & \left( -\frac{(-A + B) (2 + \cos [c]) \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c]}{d} - \right. \\
 & \left. \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( -A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right] \right)}{d} + \frac{4 B \sec [c] \sec [c + d x]^2 \sin [d x]}{3 d} + \right. \\
 & \left. \left. \frac{4 \sec [c] \sec [c + d x] (B \sin [c] + 3 A \sin [d x] - 3 B \sin [d x])}{3 d} \right) \right) / \\
 & \left( (B + A \cos [c + d x]) (a + a \sec [c + d x]) \right) + \\
 & \left( A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]]^2 \right] \right. \\
 & \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x]) \sec [d x - \text{ArcTan} [\cot [c]]] \\
 & \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x]) \right) - \\
 & \left( 5 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]]^2 \right] \right. \\
 & \sec \left[ \frac{c}{2} \right] (A + B \sec [c + d x]) \sec [d x - \text{ArcTan} [\cot [c]]] \\
 & \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x]) \right)
 \end{aligned}$$

**Problem 502:** Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^{5 / 2} (A+B \sec [c+d x])}{(a+a \sec [c+d x])^2} d x$$

Optimal (type 4, 204 leaves, 8 steps):

$$\frac{7 (8 A-5 B) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 a^2 d}-\frac{5 (3 A-2 B) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 a^2 d}-\frac{5 (3 A-2 B) \sqrt{\cos [c+d x]} \sin [c+d x]}{3 a^2 d}+\frac{7 (8 A-5 B) \cos [c+d x]^{3 / 2} \sin [c+d x]}{15 a^2 d}-\frac{(3 A-2 B) \cos [c+d x]^{5 / 2} \sin [c+d x]}{a^2 d(1+\cos [c+d x])}-\frac{(A-B) \cos [c+d x]^{7 / 2} \sin [c+d x]}{3 d(a+a \cos [c+d x])^2}$$

Result (type 5, 1396 leaves):

$$\frac{1}{5(B+A \cos [c+d x])(a+a \sec [c+d x])^2} 28 i A \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \sec \left[\frac{c}{2}\right] \sec [c+d x] \\ (A+B \sec [c+d x])\left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\ \left. \left.\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right. \\ \left. \left.\sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right)\right) / \\ \left(3 i d\left(1+e^{2 i d x}\right) \cos [c]-3 d\left(-1+e^{2 i d x}\right) \sin [c]\right)- \\ \left(2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \\ \left. \sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \\ \left. \sqrt{1+e^{2 i d x} \cos [2 c]+i e^{2 i d x} \sin [2 c]}\right) / \\ \left.\left(-i d\left(1+e^{2 i d x}\right) \cos [c]+d\left(-1+e^{2 i d x}\right) \sin [c]\right)\right)- \\ \frac{1}{2(B+A \cos [c+d x])(a+a \sec [c+d x])^2} \\ 7 \\ i \\ B \\ \cos \left[\frac{c}{2}+\frac{d x}{2}\right]^4 \\ \operatorname{Csc}\left[\frac{c}{2}\right] \\ \sec \left[\frac{c}{2}\right] \\ \sec [c+d x] \\ (A+B \sec [c+d x]) \\ \left(\left(2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4},-e^{2 i d x}(\cos [c]+i \sin [c])^2\right] \right. \right. \\ \left. \left.\sqrt{e^{-i d x}\left(2\left(1+e^{2 i d x}\right) \cos [c]+2 i\left(-1+e^{2 i d x}\right) \sin [c]\right)} \right. \right.$$

$$\begin{aligned}
& \left( \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
& \left( 3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c] \right) - \\
& \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
& \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
& \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
& \left( -i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c] \right) + \\
& \left( 10 A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right] \right. \\
& \sec\left[\frac{c}{2}\right] \sec[c + d x] (A + B \sec[c + d x]) \\
& \sec[d x - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\
& \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\
& \left. \sqrt{1 + \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \right) / \\
& \left( d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + d x])^2 \right) - \\
& \left( 20 B \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right] \right. \\
& \sec\left[\frac{c}{2}\right] \sec[c + d x] (A + B \sec[c + d x]) \\
& \sec[d x - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \\
& \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \right) / \\
& \left( 3 d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + d x])^2 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (A + B \sec[c + d x]) \right. \\
& \left( \frac{4 (-20 A + 15 B - 36 A \cos[c] + 20 B \cos[c]) \csc[c]}{5 d} + \frac{8 (-2 A + B) \cos[d x] \sin[c]}{3 d} + \right. \\
& \frac{4 A \cos[2 d x] \sin[2 c]}{5 d} - \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^3 (-A \sin\left[\frac{d x}{2}\right] + B \sin\left[\frac{d x}{2}\right])}{3 d} + \\
& \left. \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right] (-4 A \sin\left[\frac{d x}{2}\right] + 3 B \sin\left[\frac{d x}{2}\right])}{d} + \frac{8 (-2 A + B) \cos[c] \sin[d x]}{3 d} + \right.
\end{aligned}$$

$$\left. \left. \left. \frac{4 A \cos [2 c] \sin [2 d x]}{5 d} - \frac{2 (-A+B) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3 d} \right) \right) \right/$$

$$\left( \sqrt{\cos [c+d x]} (B+A \cos [c+d x]) (a+a \sec [c+d x])^2 \right)$$

**Problem 503: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos [c+d x]^{3/2} (A+B \sec [c+d x])}{(a+a \sec [c+d x])^2} dx$$

Optimal (type 4, 171 leaves, 7 steps):

$$-\frac{(7 A-4 B) \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{a^2 d} +$$

$$\frac{5(2 A-B) \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 a^2 d} + \frac{5(2 A-B) \sqrt{\cos [c+d x]} \sin [c+d x]}{3 a^2 d} -$$

$$\frac{(7 A-4 B) \cos [c+d x]^{3/2} \sin [c+d x]}{3 a^2 d (1+\cos [c+d x])} - \frac{(A-B) \cos [c+d x]^{5/2} \sin [c+d x]}{3 d (a+a \cos [c+d x])^2}$$

Result (type 5, 1352 leaves):

$$-\frac{1}{2(B+A \cos [c+d x])(a+a \sec [c+d x])^2} 7 i A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \operatorname{Csc} \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c+d x]$$

$$(A+B \sec [c+d x]) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c] + 2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) /$$

$$(3 i d (1+e^{2 i d x}) \cos [c] - 3 d (-1+e^{2 i d x}) \sin [c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos [c] + 2 i (-1+e^{2 i d x}) \sin [c])}}{\sqrt{1+e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) /$$

$$(-i d (1+e^{2 i d x}) \cos [c] + d (-1+e^{2 i d x}) \sin [c]) \Big) +$$

$$\frac{1}{2(B+A \cos [c+d x])(a+a \sec [c+d x])^2}$$

$$\frac{i}{B}$$

$$\cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4$$

$$\begin{aligned}
 & \text{Csc}\left[\frac{c}{2}\right] \\
 & \text{Sec}\left[\frac{c}{2}\right] \\
 & \text{Sec}[c+dx] \\
 & (A+B \text{Sec}[c+dx]) \\
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) - \\
 & \left( 20 A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \right. \\
 & \quad \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c+dx] (A+B \text{Sec}[c+dx]) \\
 & \quad \text{Sec}[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right. \\
 & \quad \left. \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 3 d (B + A \cos[c+dx]) \sqrt{1 + \cot[c]^2} (a + a \text{Sec}[c+dx])^2 \right) + \\
 & \left( 10 B \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \right. \\
 & \quad \text{Sec}\left[\frac{c}{2}\right] \text{Sec}[c+dx] (A+B \text{Sec}[c+dx]) \\
 & \quad \text{Sec}[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right. \\
 & \quad \left. \sqrt{1 + \sin[d x - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 3 d (B + A \cos[c+dx]) \sqrt{1 + \cot[c]^2} (a + a \text{Sec}[c+dx])^2 \right) +
 \end{aligned}$$



$$\left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (A + B \sec[c + dx]) \left( -\frac{4(-3A + 2B - 4A \cos[c] + 2B \cos[c]) \csc[c]}{d} + \frac{8A \cos[dx] \sin[c]}{3d} + \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3d} - \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-3A \sin\left[\frac{dx}{2}\right] + 2B \sin\left[\frac{dx}{2}\right])}{d} + \frac{8A \cos[c] \sin[dx]}{3d} + \frac{2(-A + B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right) \right) / \left( \sqrt{\cos[c + dx]} (B + A \cos[c + dx]) (a + a \sec[c + dx])^2 \right)$$

**Problem 504: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cos[c + dx]} (A + B \sec[c + dx])}{(a + a \sec[c + dx])^2} dx$$

Optimal (type 4, 137 leaves, 6 steps):

$$\frac{(4A - B) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{a^2 d} - \frac{(5A - 2B) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{3a^2 d} - \frac{(5A - 2B) \sqrt{\cos[c + dx]} \sin[c + dx]}{3a^2 d (1 + \cos[c + dx])} - \frac{(A - B) \cos[c + dx]^{3/2} \sin[c + dx]}{3d (a + a \cos[c + dx])^2}$$

Result (type 5, 1318 leaves):

$$\frac{1}{(B + A \cos[c + dx]) (a + a \sec[c + dx])^2} \frac{2i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c + dx]}{(A + B \sec[c + dx]) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])} \right. \right. \right. \\ \left. \left. \left. \sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]} \right) \right) / \left( 3i d (1 + e^{2ix}) \cos[c] - 3d (-1 + e^{2ix}) \sin[c] \right) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \sqrt{e^{-ix} (2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c])} \right. \right. \\ \left. \left. \left. \sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]} \right) \right) / \left( -i d (1 + e^{2ix}) \cos[c] + d (-1 + e^{2ix}) \sin[c] \right) \right) - \frac{1}{2(B + A \cos[c + dx]) (a + a \sec[c + dx])^2}$$

$$\begin{aligned}
 & \frac{i}{B} \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \\
 & \csc\left[\frac{c}{2}\right] \\
 & \sec\left[\frac{c}{2}\right] \\
 & \sec[c+dx] \\
 & (A+B \sec[c+dx]) \\
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) + \\
 & \left( 10 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right. \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \\
 & \quad \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1 + \sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
 & \left( 3 d (B + A \cos[c+dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c+dx])^2 \right) - \\
 & \left( 4 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right. \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \\
 & \quad \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]} \\
 & \quad \left. \frac{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \right) /
 \end{aligned}$$

$$\left( 3 d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^2 \right) +$$

$$\left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 (A + B \sec [c + d x]) \right.$$

$$\left( -\frac{4 (2 A - B + 2 A \cos [c]) \csc [c]}{d} + \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( -2 A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right] \right)}{d} - \right.$$

$$\left. \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 \left( -A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right] \right)}{3 d} - \frac{2 (-A + B) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3 d} \right) \Bigg) /$$

$$\left( \sqrt{\cos [c + d x]} (B + A \cos [c + d x]) (a + a \sec [c + d x])^2 \right)$$

**Problem 505: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x]}{\sqrt{\cos [c + d x]} (a + a \sec [c + d x])^2} dx$$

Optimal (type 4, 121 leaves, 6 steps):

$$-\frac{A \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{a^2 d} + \frac{(2 A + B) \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{3 a^2 d} +$$

$$\frac{A \sqrt{\cos [c + d x]} \sin [c + d x]}{a^2 d (1 + \cos [c + d x])} - \frac{(A - B) \sqrt{\cos [c + d x]} \sin [c + d x]}{3 d (a + a \cos [c + d x])^2}$$

Result (type 5, 921 leaves):

$$-\frac{1}{2 (B + A \cos [c + d x]) (a + a \sec [c + d x])^2} \Im A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c + d x]$$

$$(A + B \sec [c + d x]) \left( \left( 2 e^{2 \Im d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 \Im d x} (\cos [c] + \Im \sin [c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-\Im d x} (2 (1 + e^{2 \Im d x}) \cos [c] + 2 \Im (-1 + e^{2 \Im d x}) \sin [c])}}{\sqrt{1 + e^{2 \Im d x} \cos [2 c] + \Im e^{2 \Im d x} \sin [2 c]}} \right) /$$

$$(3 \Im d (1 + e^{2 \Im d x}) \cos [c] - 3 d (-1 + e^{2 \Im d x}) \sin [c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 \Im d x} (\cos [c] + \Im \sin [c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-\Im d x} (2 (1 + e^{2 \Im d x}) \cos [c] + 2 \Im (-1 + e^{2 \Im d x}) \sin [c])}}{\sqrt{1 + e^{2 \Im d x} \cos [2 c] + \Im e^{2 \Im d x} \sin [2 c]}} \right) /$$

$$(-\Im d (1 + e^{2 \Im d x}) \cos [c] + d (-1 + e^{2 \Im d x}) \sin [c]) \Bigg) -$$

$$\begin{aligned}
 & \left( 4 A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \text{ArcTan} [\cot [c]]]^2 \right] \right. \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + dx] \\
 & \quad (A + B \sec [c + dx]) \\
 & \quad \sec [dx - \text{ArcTan} [\cot [c]]] \\
 & \quad \sqrt{1 - \sin [dx - \text{ArcTan} [\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \text{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{1 + \sin [dx - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 d (B + A \cos [c + dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx])^2 \right) - \\
 & \left( 2 B \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [dx - \text{ArcTan} [\cot [c]]]^2 \right] \right. \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + dx] (A + B \sec [c + dx]) \\
 & \quad \sec [dx - \text{ArcTan} [\cot [c]]] \sqrt{1 - \sin [dx - \text{ArcTan} [\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [dx - \text{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{1 + \sin [dx - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \left( 3 d (B + A \cos [c + dx]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + dx])^2 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 (A + B \sec [c + dx]) \left( \frac{4 A \csc [c]}{d} + \frac{4 A \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right] \sin \left[ \frac{dx}{2} \right]}{d} + \right. \right. \\
 & \quad \left. \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 (-A \sin \left[ \frac{dx}{2} \right] + B \sin \left[ \frac{dx}{2} \right])}{3 d} + \frac{2 (-A + B) \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3 d} \right) \left. \right) / \\
 & \left( \sqrt{\cos [c + dx]} (B + A \cos [c + dx]) (a + a \sec [c + dx])^2 \right)
 \end{aligned}$$

**Problem 506: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + dx]}{\cos [c + dx]^{3/2} (a + a \sec [c + dx])^2} dx$$

Optimal (type 4, 121 leaves, 6 steps):

$$\frac{B \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{a^2 d} + \frac{(A+2B) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3 a^2 d} -$$

$$\frac{B \sqrt{\cos[c+dx]} \sin[c+dx]}{a^2 d (1+\cos[c+dx])} + \frac{(A-B) \sqrt{\cos[c+dx]} \sin[c+dx]}{3 d (a+a \cos[c+dx])^2}$$

Result (type 5, 921 leaves):

$$\frac{1}{2 (B+A \cos[c+dx]) (a+a \sec[c+dx])^2} \operatorname{Im} B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]$$

$$(A+B \sec[c+dx]) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos[c] + 2 i (-1+e^{2 i d x}) \sin[c])}}{\sqrt{1+e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) /$$

$$(3 i d (1+e^{2 i d x}) \cos[c] - 3 d (-1+e^{2 i d x}) \sin[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-i d x} (2 (1+e^{2 i d x}) \cos[c] + 2 i (-1+e^{2 i d x}) \sin[c])}}{\sqrt{1+e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) /$$

$$(-i d (1+e^{2 i d x}) \cos[c] + d (-1+e^{2 i d x}) \sin[c]) -$$

$$\left( 2 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]^2\right] \right.$$

$$\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A+B \sec[c+dx])$$

$$\operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}$$

$$\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]}$$

$$\left. \frac{\sqrt{1+\sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) /$$

$$\left( 3 d (B+A \cos[c+dx]) \sqrt{1+\cot[c]^2} (a+a \sec[c+dx])^2 \right) -$$

$$\left( 4 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \operatorname{ArcTan}[\cot[c]]]^2\right] \right.$$

$$\operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx] (A+B \sec[c+dx])$$

$$\operatorname{Sec}[dx - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \operatorname{ArcTan}[\cot[c]]]}$$

$$\left. \frac{\sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \sqrt{1+\sin[dx - \operatorname{ArcTan}[\cot[c]]]}}{\sqrt{1+\cot[c]^2} \sin[c] \sin[dx - \operatorname{ArcTan}[\cot[c]]]} \right) /$$

$$\left( 3 d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^2 \right) + \left( \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 (A + B \sec [c + d x]) \left( -\frac{4 B \csc [c]}{d} - \frac{4 B \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right] \sin \left[ \frac{dx}{2} \right]}{d} - \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^3 (-A \sin \left[ \frac{dx}{2} \right] + B \sin \left[ \frac{dx}{2} \right])}{3 d} - \frac{2 (-A + B) \sec \left[ \frac{c}{2} + \frac{dx}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{3 d} \right) \right) / \left( \sqrt{\cos [c + d x]} (B + A \cos [c + d x]) (a + a \sec [c + d x])^2 \right)$$

**Problem 507: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec [c + d x]}{\cos [c + d x]^{5/2} (a + a \sec [c + d x])^2} dx$$

Optimal (type 4, 164 leaves, 7 steps):

$$\frac{(A - 4 B) \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), 2 \right]}{a^2 d} + \frac{(2 A - 5 B) \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), 2 \right]}{3 a^2 d} - \frac{(A - 4 B) \sin [c + d x]}{a^2 d \sqrt{\cos [c + d x]}} + \frac{(2 A - 5 B) \sin [c + d x]}{3 a^2 d \sqrt{\cos [c + d x]} (1 + \cos [c + d x])} + \frac{(A - B) \sin [c + d x]}{3 d \sqrt{\cos [c + d x]} (a + a \cos [c + d x])^2}$$

Result (type 5, 1351 leaves):

$$\frac{1}{2 (B + A \cos [c + d x]) (a + a \sec [c + d x])^2} \left( A \cos \left[ \frac{c}{2} + \frac{dx}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c + d x] \right. \\ \left. (A + B \sec [c + d x]) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \right. \\ \left. \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \right. \\ \left. \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) \right) / \\ \left( 3 i d (1 + e^{2 i d x}) \cos [c] - 3 d (-1 + e^{2 i d x}) \sin [c] \right) - \\ \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\ \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos [c] + 2 i (-1 + e^{2 i d x}) \sin [c])} \right. \\ \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\ \left. \left( -i d (1 + e^{2 i d x}) \cos [c] + d (-1 + e^{2 i d x}) \sin [c] \right) \right) - \\ \frac{1}{2 (B + A \cos [c + d x]) (a + a \sec [c + d x])^2} \\ i \\ B$$

$$\begin{aligned}
& \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \\
& \csc\left[\frac{c}{2}\right] \\
& \sec\left[\frac{c}{2}\right] \\
& \sec[c + dx] \\
& (A + B \sec[c + dx]) \\
& \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
& \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
& \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
& \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
& \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
& \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) - \\
& \left( 4 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right. \\
& \quad \sec\left[\frac{c}{2}\right] \sec[c + dx] (A + B \sec[c + dx]) \\
& \quad \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]} \\
& \quad \left. \frac{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1 + \sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
& \left( 3 d (B + A \cos[c + dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx])^2 \right) + \\
& \left( 10 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]^2\right] \right. \\
& \quad \sec\left[\frac{c}{2}\right] \sec[c + dx] (A + B \sec[c + dx]) \\
& \quad \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]} \\
& \quad \left. \frac{\sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \sqrt{1 + \sin[dx - \text{ArcTan}[\cot[c]]]}}{\sqrt{1 + \sin[dx - \text{ArcTan}[\cot[c]]]}} \right) / \\
& \left( 3 d (B + A \cos[c + dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + dx])^2 \right) +
\end{aligned}$$

$$\left( \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 (A+B \sec[c+dx]) \left( \frac{2(2B-A \cos[c] + 2B \cos[c]) \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c]}{d} + \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^3 (-A \sin\left[\frac{dx}{2}\right] + B \sin\left[\frac{dx}{2}\right])}{3d} + \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{dx}{2}\right] (-A \sin\left[\frac{dx}{2}\right] + 2B \sin\left[\frac{dx}{2}\right])}{d} + \frac{8B \sec[c] \sec[c+dx] \sin[dx]}{d} + \frac{2(-A+B) \sec\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3d} \right) \right) / \left( \sqrt{\cos[c+dx]} (B+A \cos[c+dx]) (a+a \sec[c+dx])^2 \right)$$

**Problem 508: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx]}{\cos[c+dx]^{7/2} (a+a \sec[c+dx])^2} dx$$

Optimal (type 4, 197 leaves, 8 steps):

$$-\frac{(4A-7B) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{a^2 d} - \frac{5(A-2B) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3a^2 d} - \frac{5(A-2B) \sin[c+dx]}{3a^2 d \cos[c+dx]^{3/2}} + \frac{(4A-7B) \sin[c+dx]}{a^2 d \sqrt{\cos[c+dx]}} + \frac{(4A-7B) \sin[c+dx]}{3a^2 d \cos[c+dx]^{3/2} (1+\cos[c+dx])} + \frac{(A-B) \sin[c+dx]}{3d \cos[c+dx]^{3/2} (a+a \cos[c+dx])^2}$$

Result (type 5, 1392 leaves):

$$-\frac{1}{(B+A \cos[c+dx]) (a+a \sec[c+dx])^2} 2i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c+dx] (A+B \sec[c+dx]) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \sqrt{e^{-ix} (2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])} \sqrt{1+e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]} \right) / \left( 3i d (1+e^{2ix}) \cos[c] - 3d (-1+e^{2ix}) \sin[c] \right) - \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix} (\cos[c] + i \sin[c])^2\right] \sqrt{e^{-ix} (2(1+e^{2ix}) \cos[c] + 2i(-1+e^{2ix}) \sin[c])} \sqrt{1+e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]} \right) / \left( -i d (1+e^{2ix}) \cos[c] + d (-1+e^{2ix}) \sin[c] \right) \right) +$$



$$\begin{aligned}
& \frac{1}{2 \left( B + A \cos \left[ c + d x \right] \right) \left( a + a \sec \left[ c + d x \right] \right)^2} \\
& \frac{7}{B} \\
& \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \\
& \csc \left[ \frac{c}{2} \right] \\
& \sec \left[ \frac{c}{2} \right] \\
& \sec \left[ c + d x \right] \\
& \left( A + B \sec \left[ c + d x \right] \right) \\
& \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} \left( \cos [c] + i \sin [c] \right)^2 \right] \right. \right. \\
& \quad \left. \frac{\sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \Bigg/ \\
& \quad \left( 3 i d \left( 1 + e^{2 i d x} \right) \cos [c] - 3 d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \\
& \quad \left( 2 \operatorname{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} \left( \cos [c] + i \sin [c] \right)^2 \right] \right. \\
& \quad \left. \frac{\sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) \Bigg/ \\
& \quad \left. \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) \right) + \\
& \left( 10 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right) \\
& \sec \left[ \frac{c}{2} \right] \sec [c + d x] \left( A + B \sec [c + d x] \right) \\
& \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
& \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \\
& \left. \sqrt{1 + \sin [d x - \operatorname{ArcTan} [\cot [c]]]} \right) \Bigg/ \\
& \left( 3 d \left( B + A \cos [c + d x] \right) \sqrt{1 + \cot [c]^2} \left( a + a \sec [c + d x] \right)^2 \right) - \\
& \left( 20 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \csc \left[ \frac{c}{2} \right] \operatorname{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \operatorname{ArcTan} [\cot [c]]] \right]^2 \right) \\
& \sec \left[ \frac{c}{2} \right] \sec [c + d x] \left( A + B \sec [c + d x] \right) \\
& \sec [d x - \operatorname{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \operatorname{ArcTan} [\cot [c]]]}
\end{aligned}$$

$$\begin{aligned} & \left( \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right. \\ & \left. \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]} \right) / \\ & \left( 3 d (B + A \cos[c + d x]) \sqrt{1+\cot[c]^2} (a + a \sec[c + d x])^2 \right) + \\ & \left( \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^4 (A + B \sec[c + d x]) \right. \\ & \left( -\frac{2(-2A + 4B - 2A \cos[c] + 3B \cos[c]) \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c]}{d} - \right. \\ & \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^3 (-A \sin\left[\frac{d x}{2}\right] + B \sin\left[\frac{d x}{2}\right])}{3 d} - \\ & \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right] (-2A \sin\left[\frac{d x}{2}\right] + 3B \sin\left[\frac{d x}{2}\right])}{d} + \frac{8B \sec[c] \sec[c + d x]^2 \sin[d x]}{3 d} + \\ & \frac{8 \sec[c] \sec[c + d x] (B \sin[c] + 3A \sin[d x] - 6B \sin[d x])}{3 d} - \\ & \left. \left. \frac{2(-A + B) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{3 d} \right) \right) / \\ & \left( \sqrt{\cos[c + d x]} (B + A \cos[c + d x]) (a + a \sec[c + d x])^2 \right) \end{aligned}$$

**Problem 509: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\cos[c + d x]^{3/2} (A + B \sec[c + d x])}{(a + a \sec[c + d x])^3} dx$$

Optimal (type 4, 221 leaves, 8 steps):

$$\begin{aligned} & -\frac{7(17A - 7B) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^3 d} + \frac{(33A - 13B) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{6 a^3 d} + \\ & \frac{(33A - 13B) \sqrt{\cos[c + d x]} \sin[c + d x]}{6 a^3 d} - \frac{(A - B) \cos[c + d x]^{7/2} \sin[c + d x]}{5 d (a + a \cos[c + d x])^3} - \\ & \frac{(2A - B) \cos[c + d x]^{5/2} \sin[c + d x]}{3 a d (a + a \cos[c + d x])^2} - \frac{7(17A - 7B) \cos[c + d x]^{3/2} \sin[c + d x]}{30 d (a^3 + a^3 \cos[c + d x])} \end{aligned}$$

Result (type 5, 1448 leaves):

$$-\frac{1}{10 (B + A \cos[c + d x]) (a + a \sec[c + d x])^3} 119 \sqrt{A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c + d x]^2}$$

$$\begin{aligned}
& (A + B \operatorname{Sec}[c + d x]) \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
& \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
& \quad \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
& \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
& \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
& \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
& \quad \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
& \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) + \\
& \quad \frac{1}{10 (B + A \cos[c + d x]) (a + a \operatorname{Sec}[c + d x])^3} \\
& \quad 49 \\
& \quad i \\
& \quad B \\
& \quad \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \\
& \quad \csc\left[\frac{c}{2}\right] \\
& \quad \sec\left[\frac{c}{2}\right] \\
& \quad \sec[c + d x]^2 \\
& \quad (A + B \operatorname{Sec}[c + d x]) \\
& \quad \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
& \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
& \quad \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
& \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
& \quad \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
& \quad \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
& \quad \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
& \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) - \\
& \quad \left( 22 A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right] \right. \\
& \quad \left. \sec\left[\frac{c}{2}\right] \sec[c + d x]^2 (A + B \operatorname{Sec}[c + d x]) \right. \\
& \quad \left. \sec[d x - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right. \\
 & \left. \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( d (B + A \cos[c + d x]) \sqrt{1+\cot[c]^2} (a + a \sec[c + d x])^3 + \right. \\
 & \left( 26 B \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\cot[c]]]^2\right] \right. \\
 & \sec\left[\frac{c}{2}\right] \sec[c + d x]^2 (A + B \sec[c + d x]) \\
 & \sec[d x - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\cot[c]]]} \\
 & \left. \sqrt{-\sqrt{1+\cot[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\cot[c]]]} \right. \\
 & \left. \sqrt{1+\sin[d x - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 3 d (B + A \cos[c + d x]) \sqrt{1+\cot[c]^2} (a + a \sec[c + d x])^3 + \right. \\
 & \left( \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (A + B \sec[c + d x]) \left( -\frac{4 (-59 A + 29 B - 60 A \cos[c] + 20 B \cos[c]) \csc[c]}{5 d} + \right. \right. \\
 & \frac{16 A \cos[d x] \sin[c]}{3 d} - \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^5 (-A \sin\left[\frac{d x}{2}\right] + B \sin\left[\frac{d x}{2}\right])}{5 d} + \\
 & \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^3 (-19 A \sin\left[\frac{d x}{2}\right] + 14 B \sin\left[\frac{d x}{2}\right])}{15 d} - \\
 & \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right] (-59 A \sin\left[\frac{d x}{2}\right] + 29 B \sin\left[\frac{d x}{2}\right])}{5 d} + \frac{16 A \cos[c] \sin[d x]}{3 d} + \\
 & \left. \left. \frac{4 (-19 A + 14 B) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15 d} - \frac{2 (-A + B) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5 d} \right) \right) / \\
 & \left( \cos[c + d x]^{3/2} (B + A \cos[c + d x]) (a + a \sec[c + d x])^3 \right)
 \end{aligned}$$

**Problem 510: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{\sqrt{\cos[c + d x]} (A + B \sec[c + d x])}{(a + a \sec[c + d x])^3} dx$$

Optimal (type 4, 188 leaves, 7 steps):

$$\frac{(49A - 9B) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{10a^3d} - \frac{(13A - 3B) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{6a^3d} - \frac{(A - B) \cos[c + dx]^{5/2} \sin[c + dx]}{5d(a + a \cos[c + dx])^3} - \frac{(8A - 3B) \cos[c + dx]^{3/2} \sin[c + dx]}{15ad(a + a \cos[c + dx])^2} - \frac{(13A - 3B) \sqrt{\cos[c + dx]} \sin[c + dx]}{6d(a^3 + a^3 \cos[c + dx])}$$

Result (type 5, 1415 leaves):

$$\frac{1}{10(B + A \cos[c + dx])(a + a \sec[c + dx])^3} 49iA \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^2$$

$$(A + B \sec[c + dx]) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-ix} \left( 2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c] \right)}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) /$$

$$(3id(1 + e^{2ix}) \cos[c] - 3d(-1 + e^{2ix}) \sin[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-ix} \left( 2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c] \right)}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) /$$

$$(-id(1 + e^{2ix}) \cos[c] + d(-1 + e^{2ix}) \sin[c]) \Big) -$$

$$\frac{1}{10(B + A \cos[c + dx])(a + a \sec[c + dx])^3}$$

$$9$$

$$i$$

$$B$$

$$\cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6$$

$$\operatorname{Csc}\left[\frac{c}{2}\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}\right]$$

$$\operatorname{Sec}[c + dx]^2$$

$$(A + B \sec[c + dx])$$

$$\left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-ix} \left( 2(1 + e^{2ix}) \cos[c] + 2i(-1 + e^{2ix}) \sin[c] \right)}}{\sqrt{1 + e^{2ix} \cos[2c] + i e^{2ix} \sin[2c]}} \right) /$$

$$(3id(1 + e^{2ix}) \cos[c] - 3d(-1 + e^{2ix}) \sin[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right.$$

$$\begin{aligned}
 & \frac{\sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \Bigg/ \\
 & \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) + \\
 & \left( 26 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x]) \\
 & \quad \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) \Bigg/ \\
 & \left( 3 d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) - \\
 & \left( 2 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]] \right]^2 \right. \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x]) \\
 & \quad \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) \Bigg/ \\
 & \left( d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (A + B \sec [c + d x]) \right. \\
 & \quad \left( -\frac{4 (29 A - 9 B + 20 A \cos [c]) \csc [c]}{5 d} + \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 (-A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right])}{5 d} \right. \\
 & \quad \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] (-29 A \sin \left[ \frac{d x}{2} \right] + 9 B \sin \left[ \frac{d x}{2} \right])}{5 d} - \\
 & \quad \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 (-14 A \sin \left[ \frac{d x}{2} \right] + 9 B \sin \left[ \frac{d x}{2} \right])}{15 d} - \\
 & \quad \left. \frac{4 (-14 A + 9 B) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{15 d} + \frac{2 (-A + B) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \tan \left[ \frac{c}{2} \right]}{5 d} \right) \Bigg/ \\
 & \left( \cos [c + d x]^{3/2} (B + A \cos [c + d x]) (a + a \sec [c + d x])^3 \right)
 \end{aligned}$$

Problem 511: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{A + B \sec[c + d x]}{\sqrt{\cos[c + d x]} (a + a \sec[c + d x])^3} dx$$

Optimal (type 4, 182 leaves, 7 steps):

$$\begin{aligned} & - \frac{(9A + B) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{10a^3d} + \\ & \frac{(3A + B) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{6a^3d} - \frac{(A - B) \cos[c + dx]^{3/2} \sin[c + dx]}{5d(a + a \cos[c + dx])^3} - \\ & \frac{(6A - B) \sqrt{\cos[c + dx]} \sin[c + dx]}{15ad(a + a \cos[c + dx])^2} + \frac{(9A + B) \sqrt{\cos[c + dx]} \sin[c + dx]}{10d(a^3 + a^3 \cos[c + dx])} \end{aligned}$$

Result (type 5, 1407 leaves):

$$\begin{aligned} & - \frac{1}{10(B + A \cos[c + dx])(a + a \sec[c + dx])^3} 9i A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^2 \\ & (A + B \sec[c + dx]) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-ix}(2(1 + e^{2ix})\cos[c] + 2i(-1 + e^{2ix})\sin[c])}}{\sqrt{1 + e^{2ix}\cos[2c] + i e^{2ix}\sin[2c]}} \right) \right. \\ & \quad \left. (3i d(1 + e^{2ix})\cos[c] - 3d(-1 + e^{2ix})\sin[c]) - \right. \\ & \quad \left. \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\cos[c] + i \sin[c])^2\right] \right. \right. \\ & \quad \left. \left. \frac{\sqrt{e^{-ix}(2(1 + e^{2ix})\cos[c] + 2i(-1 + e^{2ix})\sin[c])}}{\sqrt{1 + e^{2ix}\cos[2c] + i e^{2ix}\sin[2c]}} \right) \right. \\ & \quad \left. (-i d(1 + e^{2ix})\cos[c] + d(-1 + e^{2ix})\sin[c]) \right) - \\ & \frac{1}{10(B + A \cos[c + dx])(a + a \sec[c + dx])^3} \\ & i \\ & B \\ & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \\ & \operatorname{Csc}\left[\frac{c}{2}\right] \\ & \operatorname{Sec}\left[\frac{c}{2}\right] \\ & \operatorname{Sec}[c + dx]^2 \\ & (A + B \sec[c + dx]) \end{aligned}$$

$$\begin{aligned}
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1} \left[ \frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \right. \\
 & \quad \sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \quad \left( 3 i d \left( 1 + e^{2 i d x} \right) \cos [c] - 3 d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \\
 & \quad \left( 2 \text{Hypergeometric2F1} \left[ -\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\
 & \quad \sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)} \\
 & \quad \left. \sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]} \right) / \\
 & \quad \left. \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) \right) - \\
 & \left( 2 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]] \right]^2 \right) \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x]) \\
 & \quad \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \quad \left( d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) - \\
 & \left( 2 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]] \right]^2 \right) \\
 & \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x]) \\
 & \quad \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \quad \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \\
 & \quad \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
 & \quad \left( 3 d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) + \\
 & \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (A + B \sec [c + d x]) \right. \\
 & \quad \left. \left( \frac{4 (9 A + B) \csc [c]}{5 d} - \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 (-A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right])}{5 d} \right) + \right.
 \end{aligned}$$



$$\frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right] \left(9 A \operatorname{Sin}\left[\frac{dx}{2}\right] + B \operatorname{Sin}\left[\frac{dx}{2}\right]\right)}{5 d} +$$

$$\frac{4 \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^3 \left(-9 A \operatorname{Sin}\left[\frac{dx}{2}\right] + 4 B \operatorname{Sin}\left[\frac{dx}{2}\right]\right)}{15 d} +$$

$$\left. \frac{4 (-9 A + 4 B) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^2 \operatorname{Tan}\left[\frac{c}{2}\right]}{15 d} - \frac{2 (-A + B) \operatorname{Sec}\left[\frac{c}{2} + \frac{dx}{2}\right]^4 \operatorname{Tan}\left[\frac{c}{2}\right]}{5 d} \right) \Bigg/$$

$$\left(\operatorname{Cos}[c + dx]^{3/2} (B + A \operatorname{Cos}[c + dx]) (a + a \operatorname{Sec}[c + dx])^3\right)$$

**Problem 512: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \operatorname{Sec}[c + dx]}{\operatorname{Cos}[c + dx]^{3/2} (a + a \operatorname{Sec}[c + dx])^3} dx$$

Optimal (type 4, 178 leaves, 7 steps):

$$- \frac{(A - B) \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{10 a^3 d} +$$

$$\frac{(A + B) \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{6 a^3 d} - \frac{(A - B) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}[c + dx]}{5 d (a + a \operatorname{Cos}[c + dx])^3} +$$

$$\frac{(4 A + B) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}[c + dx]}{15 a d (a + a \operatorname{Cos}[c + dx])^2} + \frac{(A - B) \sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}[c + dx]}{10 d (a^3 + a^3 \operatorname{Cos}[c + dx])}$$

Result (type 5, 1406 leaves):

$$- \frac{1}{10 (B + A \operatorname{Cos}[c + dx]) (a + a \operatorname{Sec}[c + dx])^3} \operatorname{I} A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c + dx]^2$$

$$(A + B \operatorname{Sec}[c + dx]) \left( \left( 2 e^{2 i dx} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])} \right.$$

$$\left. \sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]} \right) \Bigg/$$

$$(3 i d (1 + e^{2 i dx}) \operatorname{Cos}[c] - 3 d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i dx} (\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \sqrt{e^{-i dx} (2 (1 + e^{2 i dx}) \operatorname{Cos}[c] + 2 i (-1 + e^{2 i dx}) \operatorname{Sin}[c])} \right.$$

$$\left. \sqrt{1 + e^{2 i dx} \operatorname{Cos}[2 c] + i e^{2 i dx} \operatorname{Sin}[2 c]} \right) \Bigg/$$

$$(-i d (1 + e^{2 i dx}) \operatorname{Cos}[c] + d (-1 + e^{2 i dx}) \operatorname{Sin}[c]) \Bigg) +$$

$$\frac{1}{10 (B + A \operatorname{Cos}[c + dx]) (a + a \operatorname{Sec}[c + dx])^3}$$

$$\begin{aligned}
 & \frac{i}{B} \\
 & \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \\
 & \csc\left[\frac{c}{2}\right] \\
 & \sec\left[\frac{c}{2}\right] \\
 & \sec[c+dx]^2 \\
 & (A+B \sec[c+dx]) \\
 & \left( \left( 2 e^{2 i d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad (3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c]) - \\
 & \quad \left( 2 \text{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \quad \left. \frac{\sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])}}{\sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]}} \right) / \\
 & \quad \left. (-i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c]) \right) - \\
 & \left( 2 A \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]\right]^2 \right. \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \\
 & \quad \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \right. \\
 & \quad \left. \sqrt{1 + \sin[dx - \text{ArcTan}[\cot[c]]]} \right) / \\
 & \left( 3 d (B + A \cos[c+dx]) \sqrt{1 + \cot[c]^2} (a + a \sec[c+dx])^3 \right) - \\
 & \left( 2 B \cos\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \csc\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[dx - \text{ArcTan}[\cot[c]]]\right]^2 \right. \\
 & \quad \sec\left[\frac{c}{2}\right] \sec[c+dx]^2 (A+B \sec[c+dx]) \\
 & \quad \sec[dx - \text{ArcTan}[\cot[c]]] \sqrt{1 - \sin[dx - \text{ArcTan}[\cot[c]]]} \\
 & \quad \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[dx - \text{ArcTan}[\cot[c]]]} \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \sqrt{1 + \sin[d x - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
& \left( 3 d (B + A \cos[c + d x]) \sqrt{1 + \cot[c]^2} (a + a \sec[c + d x])^3 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (A + B \sec[c + d x]) \right. \\
& \left( -\frac{4(-A + B) \csc[c]}{5 d} - \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right] (-A \sin\left[\frac{d x}{2}\right] + B \sin\left[\frac{d x}{2}\right])}{5 d} + \right. \\
& \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^5 (-A \sin\left[\frac{d x}{2}\right] + B \sin\left[\frac{d x}{2}\right])}{5 d} + \\
& \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^3 (4 A \sin\left[\frac{d x}{2}\right] + B \sin\left[\frac{d x}{2}\right])}{15 d} + \\
& \left. \left. \frac{4(4 A + B) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15 d} + \frac{2(-A + B) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5 d} \right) \right) / \\
& (\cos[c + d x])^{3/2} (B + A \cos[c + d x]) (a + a \sec[c + d x])^3
\end{aligned}$$

**Problem 513: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + d x]}{\cos[c + d x]^{5/2} (a + a \sec[c + d x])^3} dx$$

Optimal (type 4, 180 leaves, 7 steps):

$$\begin{aligned}
& \frac{(A + 9 B) \text{EllipticE}\left[\frac{1}{2}(c + d x), 2\right]}{10 a^3 d} + \\
& \frac{(A + 3 B) \text{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{6 a^3 d} + \frac{(A - B) \sqrt{\cos[c + d x]} \sin[c + d x]}{5 d (a + a \cos[c + d x])^3} + \\
& \frac{(A - 6 B) \sqrt{\cos[c + d x]} \sin[c + d x]}{15 a d (a + a \cos[c + d x])^2} - \frac{(A + 9 B) \sqrt{\cos[c + d x]} \sin[c + d x]}{10 d (a^3 + a^3 \cos[c + d x])}
\end{aligned}$$

Result (type 5, 1407 leaves):

$$\begin{aligned}
& \frac{1}{10 (B + A \cos[c + d x]) (a + a \sec[c + d x])^3} \Im A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \csc\left[\frac{c}{2}\right] \sec\left[\frac{c}{2}\right] \sec[c + d x]^2 \\
& (A + B \sec[c + d x]) \left( \left( 2 e^{2 \Im d x} \text{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 \Im d x} (\cos[c] + \Im \sin[c])^2\right] \right. \right. \\
& \left. \left. \sqrt{e^{-\Im d x} (2 (1 + e^{2 \Im d x}) \cos[c] + 2 \Im (-1 + e^{2 \Im d x}) \sin[c])} \right) \right)
\end{aligned}$$

$$\begin{aligned}
 & \left( \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
 & \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \left( -i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c] \right) + \\
 & \frac{1}{10 (B + A \cos[c + d x]) (a + a \sec[c + d x])^3} \\
 & 9 \\
 & i \\
 & B \\
 & \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \\
 & \csc\left[\frac{c}{2}\right] \\
 & \sec\left[\frac{c}{2}\right] \\
 & \sec[c + d x]^2 \\
 & (A + B \sec[c + d x]) \\
 & \left( \left( 2 e^{2 i d x} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \right. \\
 & \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
 & \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \left( 3 i d (1 + e^{2 i d x}) \cos[c] - 3 d (-1 + e^{2 i d x}) \sin[c] \right) - \\
 & \left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos[c] + i \sin[c])^2\right] \right. \\
 & \left. \sqrt{e^{-i d x} (2 (1 + e^{2 i d x}) \cos[c] + 2 i (-1 + e^{2 i d x}) \sin[c])} \right. \\
 & \left. \sqrt{1 + e^{2 i d x} \cos[2 c] + i e^{2 i d x} \sin[2 c]} \right) / \\
 & \left( -i d (1 + e^{2 i d x}) \cos[c] + d (-1 + e^{2 i d x}) \sin[c] \right) - \\
 & \left( 2 A \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \csc\left[\frac{c}{2}\right] \operatorname{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \operatorname{ArcTan}[\cot[c]]]^2\right] \right. \\
 & \left. \sec\left[\frac{c}{2}\right] \sec[c + d x]^2 (A + B \sec[c + d x]) \right. \\
 & \left. \sec[d x - \operatorname{ArcTan}[\cot[c]]] \sqrt{1 - \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \right. \\
 & \left. \sqrt{-\sqrt{1 + \cot[c]^2} \sin[c] \sin[d x - \operatorname{ArcTan}[\cot[c]]]} \right)
 \end{aligned}$$

$$\begin{aligned}
& \left. \sqrt{1 + \sin[d x - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
& \left( 3 d (B + A \cos[c + d x]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c + d x])^3 \right) - \\
& \left( 2 B \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 \text{Csc}\left[\frac{c}{2}\right] \text{HypergeometricPFQ}\left[\left\{\frac{1}{4}, \frac{1}{2}\right\}, \left\{\frac{5}{4}\right\}, \sin[d x - \text{ArcTan}[\text{Cot}[c]]]^2\right] \right. \\
& \quad \sec\left[\frac{c}{2}\right] \sec[c + d x]^2 (A + B \sec[c + d x]) \\
& \quad \sec[d x - \text{ArcTan}[\text{Cot}[c]]] \sqrt{1 - \sin[d x - \text{ArcTan}[\text{Cot}[c]]]} \\
& \quad \left. \sqrt{-\sqrt{1 + \text{Cot}[c]^2} \sin[c] \sin[d x - \text{ArcTan}[\text{Cot}[c]]]} \sqrt{1 + \sin[d x - \text{ArcTan}[\text{Cot}[c]]]} \right) / \\
& \left( d (B + A \cos[c + d x]) \sqrt{1 + \text{Cot}[c]^2} (a + a \sec[c + d x])^3 \right) + \\
& \left( \cos\left[\frac{c}{2} + \frac{d x}{2}\right]^6 (A + B \sec[c + d x]) \right. \\
& \quad \left( -\frac{4 (A + 9 B) \text{Csc}[c]}{5 d} - \frac{2 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^5 (-A \sin\left[\frac{d x}{2}\right] + B \sin\left[\frac{d x}{2}\right])}{5 d} - \right. \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^3 (-A \sin\left[\frac{d x}{2}\right] + 6 B \sin\left[\frac{d x}{2}\right])}{15 d} - \\
& \quad \frac{4 \sec\left[\frac{c}{2}\right] \sec\left[\frac{c}{2} + \frac{d x}{2}\right] (A \sin\left[\frac{d x}{2}\right] + 9 B \sin\left[\frac{d x}{2}\right])}{5 d} - \\
& \quad \left. \frac{4 (-A + 6 B) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^2 \tan\left[\frac{c}{2}\right]}{15 d} - \frac{2 (-A + B) \sec\left[\frac{c}{2} + \frac{d x}{2}\right]^4 \tan\left[\frac{c}{2}\right]}{5 d} \right) \left. \right) / \\
& \left( \cos[c + d x]^{3/2} (B + A \cos[c + d x]) (a + a \sec[c + d x])^3 \right)
\end{aligned}$$

**Problem 514: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.**

$$\int \frac{A + B \sec[c + d x]}{\cos[c + d x]^{7/2} (a + a \sec[c + d x])^3} dx$$

Optimal (type 4, 221 leaves, 8 steps):

$$\frac{(9A - 49B) \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), 2\right]}{10a^3d} + \frac{(3A - 13B) \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{6a^3d} -$$

$$\frac{(9A - 49B) \operatorname{Sin}[c+dx]}{10a^3d\sqrt{\operatorname{Cos}[c+dx]}} + \frac{(A - B) \operatorname{Sin}[c+dx]}{5d\sqrt{\operatorname{Cos}[c+dx]}(a+a\operatorname{Cos}[c+dx])^3} +$$

$$\frac{(3A - 8B) \operatorname{Sin}[c+dx]}{15ad\sqrt{\operatorname{Cos}[c+dx]}(a+a\operatorname{Cos}[c+dx])^2} + \frac{(3A - 13B) \operatorname{Sin}[c+dx]}{6d\sqrt{\operatorname{Cos}[c+dx]}(a^3+a^3\operatorname{Cos}[c+dx])}$$

Result (type 5, 1447 leaves):

$$\frac{1}{10(B + A \operatorname{Cos}[c+dx])(a + a \operatorname{Sec}[c+dx])^3} 9i A \operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \operatorname{Sec}[c+dx]^2$$

$$(A + B \operatorname{Sec}[c+dx]) \left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\operatorname{Cos}[c] + 2i(-1+e^{2ix})\operatorname{Sin}[c])}}{\sqrt{1+e^{2ix}\operatorname{Cos}[2c] + i e^{2ix}\operatorname{Sin}[2c]}} \right) /$$

$$(3id(1+e^{2ix})\operatorname{Cos}[c] - 3d(-1+e^{2ix})\operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\operatorname{Cos}[c] + 2i(-1+e^{2ix})\operatorname{Sin}[c])}}{\sqrt{1+e^{2ix}\operatorname{Cos}[2c] + i e^{2ix}\operatorname{Sin}[2c]}} \right) /$$

$$(-id(1+e^{2ix})\operatorname{Cos}[c] + d(-1+e^{2ix})\operatorname{Sin}[c]) \Big) -$$

$$\frac{1}{10(B + A \operatorname{Cos}[c+dx])(a + a \operatorname{Sec}[c+dx])^3}$$

$$49$$

$$i$$

$$B$$

$$\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right]^6$$

$$\operatorname{Csc}\left[\frac{c}{2}\right]$$

$$\operatorname{Sec}\left[\frac{c}{2}\right]$$

$$\operatorname{Sec}[c+dx]^2$$

$$(A + B \operatorname{Sec}[c+dx])$$

$$\left( \left( 2e^{2ix} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2ix}(\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right. \right.$$

$$\left. \frac{\sqrt{e^{-ix}(2(1+e^{2ix})\operatorname{Cos}[c] + 2i(-1+e^{2ix})\operatorname{Sin}[c])}}{\sqrt{1+e^{2ix}\operatorname{Cos}[2c] + i e^{2ix}\operatorname{Sin}[2c]}} \right) /$$

$$(3id(1+e^{2ix})\operatorname{Cos}[c] - 3d(-1+e^{2ix})\operatorname{Sin}[c]) -$$

$$\left( 2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2ix}(\operatorname{Cos}[c] + i \operatorname{Sin}[c])^2\right] \right.$$

$$\begin{aligned}
& \left( \frac{\sqrt{e^{-i d x} \left( 2 \left( 1 + e^{2 i d x} \right) \cos [c] + 2 i \left( -1 + e^{2 i d x} \right) \sin [c] \right)}}{\sqrt{1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c]}} \right) / \\
& \left( -i d \left( 1 + e^{2 i d x} \right) \cos [c] + d \left( -1 + e^{2 i d x} \right) \sin [c] \right) - \\
& \left( 2 A \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]] \right]^2 \right. \\
& \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x]) \\
& \quad \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
& \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \right. \\
& \quad \left. \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
& \left( d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) + \\
& \left( 26 B \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 \csc \left[ \frac{c}{2} \right] \text{HypergeometricPFQ} \left[ \left\{ \frac{1}{4}, \frac{1}{2} \right\}, \left\{ \frac{5}{4} \right\}, \sin [d x - \text{ArcTan} [\cot [c]]] \right]^2 \right. \\
& \quad \sec \left[ \frac{c}{2} \right] \sec [c + d x]^2 (A + B \sec [c + d x]) \\
& \quad \sec [d x - \text{ArcTan} [\cot [c]]] \sqrt{1 - \sin [d x - \text{ArcTan} [\cot [c]]]} \\
& \quad \left. \sqrt{-\sqrt{1 + \cot [c]^2} \sin [c] \sin [d x - \text{ArcTan} [\cot [c]]]} \sqrt{1 + \sin [d x - \text{ArcTan} [\cot [c]]]} \right) / \\
& \left( 3 d (B + A \cos [c + d x]) \sqrt{1 + \cot [c]^2} (a + a \sec [c + d x])^3 \right) + \\
& \left( \cos \left[ \frac{c}{2} + \frac{d x}{2} \right]^6 (A + B \sec [c + d x]) \left( \frac{2 (20 B - 9 A \cos [c] + 29 B \cos [c]) \csc \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} \right] \sec [c]}{5 d} + \right. \right. \\
& \quad \frac{2 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^5 \left( -A \sin \left[ \frac{d x}{2} \right] + B \sin \left[ \frac{d x}{2} \right] \right)}{5 d} + \\
& \quad \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^3 \left( -6 A \sin \left[ \frac{d x}{2} \right] + 11 B \sin \left[ \frac{d x}{2} \right] \right)}{15 d} + \\
& \quad \frac{4 \sec \left[ \frac{c}{2} \right] \sec \left[ \frac{c}{2} + \frac{d x}{2} \right] \left( -9 A \sin \left[ \frac{d x}{2} \right] + 29 B \sin \left[ \frac{d x}{2} \right] \right)}{5 d} + \frac{16 B \sec [c] \sec [c + d x] \sin [d x]}{d} \\
& \quad \left. \left. \frac{4 (-6 A + 11 B) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^2 \tan \left[ \frac{c}{2} \right]}{15 d} + \frac{2 (-A + B) \sec \left[ \frac{c}{2} + \frac{d x}{2} \right]^4 \tan \left[ \frac{c}{2} \right]}{5 d} \right) \right) / \\
& \left( \cos [c + d x]^{3/2} (B + A \cos [c + d x]) (a + a \sec [c + d x])^3 \right)
\end{aligned}$$

### Problem 519: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{\cos[c+dx]} \sqrt{a+a \sec[c+dx]} (A+B \sec[c+dx])}{dx}$$

Optimal (type 3, 96 leaves, 4 steps):

$$\frac{2 \sqrt{a} B \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{d} + \frac{2 a A \sin[c+dx]}{d \sqrt{\cos[c+dx]} \sqrt{a+a \sec[c+dx]}}$$

Result (type 5, 135 leaves):

$$-\frac{1}{3 d \left(1+e^{i(c+dx)}\right)} + 2 i \sqrt{\cos[c+dx]} \left(3 A \left(-1+e^{i(c+dx)}\right)+6 B e^{i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+dx)}\right]\right. \\ \left.+2 B e^{2 i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+dx)}\right]\right) \sqrt{a(1+\sec[c+dx])}$$

### Problem 520: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{a+a \sec[c+dx]} (A+B \sec[c+dx])}{\sqrt{\cos[c+dx]}} dx$$

Optimal (type 3, 98 leaves, 4 steps):

$$\frac{\sqrt{a} (2 A+B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{d} + \frac{a B \sin[c+dx]}{d \cos[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}}$$

Result (type 5, 157 leaves):

$$\frac{1}{3 d} \sqrt{\cos[c+dx]} \sqrt{a(1+\sec[c+dx])} - \left(-3 i (2 A+B) e^{\frac{1}{2} i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+dx)}\right] \sec\left[\frac{1}{2}(c+dx)\right] - \right. \\ \left. i (2 A+B) e^{\frac{3}{2} i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+dx)}\right] \sec\left[\frac{1}{2}(c+dx)\right] + \right. \\ \left. 3 B \sec[c+dx] \tan\left[\frac{1}{2}(c+dx)\right]\right)$$

### Problem 521: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{a+a \sec[c+dx]} (A+B \sec[c+dx])}{\cos[c+dx]^{3/2}} dx$$

Optimal (type 3, 151 leaves, 5 steps):



$$\frac{\sqrt{a} (4A + 3B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{4d} +$$

$$\frac{aB \sin[c+dx]}{2d \cos[c+dx]^{5/2} \sqrt{a+a \sec[c+dx]}} + \frac{a(4A + 3B) \sin[c+dx]}{4d \cos[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}}$$

Result (type 5, 166 leaves):

$$\frac{1}{12d} \sqrt{\cos[c+dx]} \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\sec[c+dx])}$$

$$\left( -3i(4A + 3B) e^{\frac{1}{2}i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] - \right.$$

$$i(4A + 3B) e^{\frac{3}{2}i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] +$$

$$\left. 3 \sec[c+dx] (4A + 3B + 2B \sec[c+dx]) \sin\left[\frac{1}{2}(c+dx)\right] \right)$$

Problem 522: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{a+a \sec[c+dx]} (A+B \sec[c+dx])}{\cos[c+dx]^{5/2}} dx$$

Optimal (type 3, 196 leaves, 6 steps):

$$\frac{\sqrt{a} (6A + 5B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{8d} +$$

$$\frac{aB \sin[c+dx]}{3d \cos[c+dx]^{7/2} \sqrt{a+a \sec[c+dx]}} +$$

$$\frac{a(6A + 5B) \sin[c+dx]}{12d \cos[c+dx]^{5/2} \sqrt{a+a \sec[c+dx]}} + \frac{a(6A + 5B) \sin[c+dx]}{8d \cos[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}}$$

Result (type 5, 185 leaves):

$$\frac{1}{24d} \sqrt{\cos[c+dx]} \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{a(1+\sec[c+dx])}$$

$$\left( -3i(6A + 5B) e^{\frac{1}{2}i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] - \right.$$

$$i(6A + 5B) e^{\frac{3}{2}i(c+dx)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] +$$

$$\left. \sec[c+dx] (3(6A + 5B) + 2(6A + 5B) \sec[c+dx] + 8B \sec[c+dx]^2) \sin\left[\frac{1}{2}(c+dx)\right] \right)$$

Problem 527: Result unnecessarily involves higher level functions.

$$\int \cos[c+dx]^{3/2} (a+a \sec[c+dx])^{3/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 145 leaves, 5 steps):

$$\frac{2 a^{3/2} B \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{d} + \frac{2 a^2 (4 A+3 B) \sin [c+d x]}{3 d \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]}} + \frac{2 a A \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{3 d}$$

Result (type 5, 157 leaves):

$$\frac{1}{3 d} a \sqrt{\cos [c+d x]} (1+\cos [c+d x]) \sec \left[\frac{1}{2}(c+d x)\right]^3 \sqrt{a(1+\sec [c+d x])} \\ \left(-3 \operatorname{Im} B e^{\frac{1}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - \operatorname{Im} B e^{\frac{3}{2} i(c+d x)} \right. \\ \left. \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + (5 A+3 B+A \cos [c+d x]) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 528: Result unnecessarily involves higher level functions.**

$$\int \sqrt{\cos [c+d x]} (a+a \sec [c+d x])^{3/2} (A+B \sec [c+d x]) dx$$

Optimal (type 3, 144 leaves, 5 steps):

$$\frac{a^{3/2} (2 A+3 B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{d} + \frac{a^2 (2 A-B) \sin [c+d x]}{d \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]}} + \frac{a B \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 5, 178 leaves):

$$\left(a(1+\cos [c+d x]) \sec \left[\frac{1}{2}(c+d x)\right]^3 \sqrt{a(1+\sec [c+d x])} \right. \\ \left(-3 \operatorname{Im} (2 A+3 B) e^{\frac{1}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - \right. \\ \left. \operatorname{Im} (2 A+3 B) e^{\frac{3}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + \right. \\ \left. \left. 3(B+2 A \cos [c+d x]) \sin \left[\frac{1}{2}(c+d x)\right]\right)\right) / (6 d \sqrt{\cos [c+d x]})$$

**Problem 529: Result unnecessarily involves higher level functions.**

$$\int \frac{(a+a \sec [c+d x])^{3/2} (A+B \sec [c+d x])}{\sqrt{\cos [c+d x]}} dx$$

Optimal (type 3, 153 leaves, 5 steps):

$$\frac{a^{3/2} (12A + 7B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{4d} +$$

$$\frac{a^2 (4A + 5B) \sin[c+dx]}{4d \cos[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}} + \frac{aB \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{2d \cos[c+dx]^{3/2}}$$

Result (type 5, 189 leaves):

$$\left( a \left( 1 + \cos[c+dx] \right) \sec\left[\frac{1}{2}(c+dx)\right]^3 \sqrt{a(1+\sec[c+dx])} \right.$$

$$\left( -3i(12A+7B) e^{\frac{1}{2}i(c+dx)} \cos[c+dx]^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] - \right.$$

$$i(12A+7B) e^{\frac{3}{2}i(c+dx)} \cos[c+dx]^2 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] +$$

$$\left. \left. 3(2B + (4A+7B) \cos[c+dx]) \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / (24d \cos[c+dx]^{3/2})$$

Problem 530: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \sec[c+dx])^{3/2} (A + B \sec[c+dx])}{\cos[c+dx]^{3/2}} dx$$

Optimal (type 3, 200 leaves, 6 steps):

$$\frac{a^{3/2} (14A + 11B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{8d} +$$

$$\frac{a^2 (6A + 7B) \sin[c+dx]}{12d \cos[c+dx]^{5/2} \sqrt{a+a \sec[c+dx]}} +$$

$$\frac{a^2 (14A + 11B) \sin[c+dx]}{8d \cos[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}} + \frac{aB \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{3d \cos[c+dx]^{5/2}}$$

Result (type 5, 205 leaves):

$$\frac{1}{48d \cos[c+dx]^{5/2}} a \left( 1 + \cos[c+dx] \right) \sec\left[\frac{1}{2}(c+dx)\right]^3 \sqrt{a(1+\sec[c+dx])}$$

$$\left( -3i(14A+11B) e^{\frac{1}{2}i(c+dx)} \cos[c+dx]^3 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] - \right.$$

$$i(14A+11B) e^{\frac{3}{2}i(c+dx)} \cos[c+dx]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] +$$

$$\left. \left( 8B + 2(6A+11B) \cos[c+dx] + (42A+33B) \cos[c+dx]^2 \right) \sin\left[\frac{1}{2}(c+dx)\right] \right)$$

Problem 531: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \sec[c+dx])^{3/2} (A + B \sec[c+dx])}{\cos[c+dx]^{5/2}} dx$$

Optimal (type 3, 247 leaves, 7 steps):

$$\frac{a^{3/2} (88 A + 75 B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{64 d} +$$

$$\frac{a^2 (8 A + 9 B) \sin[c+dx]}{24 d \cos[c+dx]^{7/2} \sqrt{a+a \sec[c+dx]}} + \frac{a^2 (88 A + 75 B) \sin[c+dx]}{96 d \cos[c+dx]^{5/2} \sqrt{a+a \sec[c+dx]}} +$$

$$\frac{a^2 (88 A + 75 B) \sin[c+dx]}{64 d \cos[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}} + \frac{a B \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{4 d \cos[c+dx]^{7/2}}$$

Result (type 5, 223 leaves):

$$\frac{1}{384 d \cos[c+dx]^{7/2}} a (1 + \cos[c+dx]) \sec\left[\frac{1}{2} (c+dx)\right]^3 \sqrt{a (1 + \sec[c+dx])}$$

$$\left( -3 i (88 A + 75 B) e^{\frac{1}{2} i (c+dx)} \cos[c+dx]^4 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c+dx)}\right] - \right.$$

$$i (88 A + 75 B) e^{\frac{3}{2} i (c+dx)} \cos[c+dx]^4 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c+dx)}\right] +$$

$$(48 B + 8 (8 A + 15 B) \cos[c+dx] + 2 (88 A + 75 B) \cos[c+dx]^2 + 3 (88 A + 75 B) \cos[c+dx]^3)$$

$$\left. \sin\left[\frac{1}{2} (c+dx)\right] \right)$$

**Problem 535: Result unnecessarily involves higher level functions.**

$$\int \cos[c+dx]^{5/2} (a+a \sec[c+dx])^{5/2} (A+B \sec[c+dx]) dx$$

Optimal (type 3, 192 leaves, 6 steps):

$$\frac{2 a^{5/2} B \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{d} +$$

$$\frac{2 a^3 (32 A + 35 B) \sin[c+dx]}{15 d \sqrt{\cos[c+dx]} \sqrt{a+a \sec[c+dx]}} +$$

$$\frac{2 a^2 (8 A + 5 B) \sqrt{\cos[c+dx]} \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{15 d} +$$

$$\frac{2 a A \cos[c+dx]^{3/2} (a+a \sec[c+dx])^{3/2} \sin[c+dx]}{5 d}$$

Result (type 5, 179 leaves):

$$\frac{1}{60 d} a^2 \sqrt{\cos [c+d x]} \left(1+\cos [c+d x]\right)^2 \sec \left[\frac{1}{2}(c+d x)\right]^5$$

$$\sqrt{a\left(1+\sec [c+d x]\right)}\left(-30 i B e^{\frac{1}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4},-e^{2 i(c+d x)}\right]-\right.$$

$$10 i B e^{\frac{3}{2} i(c+d x)} \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4},-e^{2 i(c+d x)}\right]+$$

$$\left.\left(89 A+80 B+2\left(14 A+5 B\right) \cos [c+d x]+3 A \cos [2(c+d x)]\right) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 536: Result unnecessarily involves higher level functions.**

$$\int \cos [c+d x]^{3 / 2}\left(a+a \sec [c+d x]\right)^{5 / 2}(A+B \sec [c+d x]) d x$$

Optimal (type 3, 197 leaves, 6 steps):

$$\frac{a^{5 / 2}(2 A+5 B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{d} +$$

$$\frac{a^3(14 A+3 B) \sin [c+d x]}{3 d \sqrt{\cos [c+d x]} \sqrt{a+a \sec [c+d x]}} - \frac{a^2(2 A-3 B) \sqrt{a+a \sec [c+d x]} \sin [c+d x]}{3 d \sqrt{\cos [c+d x]}} +$$

$$\frac{2 a A \sqrt{\cos [c+d x]}(a+a \sec [c+d x])^{3 / 2} \sin [c+d x]}{3 d}$$

Result (type 5, 200 leaves):

$$\frac{1}{12 d \sqrt{\cos [c+d x]}} a^2\left(1+\cos [c+d x]\right)^2 \sec \left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a\left(1+\sec [c+d x]\right)}$$

$$\left(-3 i(2 A+5 B) e^{\frac{1}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4},-e^{2 i(c+d x)}\right]-\right.$$

$$i(2 A+5 B) e^{\frac{3}{2} i(c+d x)} \cos [c+d x] \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4},-e^{2 i(c+d x)}\right]+$$

$$\left.\left(A+3 B+2(8 A+3 B) \cos [c+d x]+A \cos [2(c+d x)]\right) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 537: Result unnecessarily involves higher level functions.**

$$\int \sqrt{\cos [c+d x]}(a+a \sec [c+d x])^{5 / 2}(A+B \sec [c+d x]) d x$$

Optimal (type 3, 200 leaves, 6 steps):

$$\frac{a^{5/2} (20A + 19B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{4d} +$$

$$\frac{a^3 (4A - 9B) \sin[c+dx]}{4d \sqrt{\cos[c+dx]} \sqrt{a+a \sec[c+dx]}} +$$

$$\frac{a^2 (4A + 7B) \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{4d \sqrt{\cos[c+dx]}} + \frac{aB (a+a \sec[c+dx])^{3/2} \sin[c+dx]}{2d \sqrt{\cos[c+dx]}}$$

Result (type 5, 204 leaves):

$$\frac{1}{48d \cos[c+dx]^{3/2}} a^2 (1 + \cos[c+dx])^2 \sec\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{a(1 + \sec[c+dx])}$$

$$\left( -3i (20A + 19B) e^{\frac{1}{2}i(c+dx)} \cos[c+dx]^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] - \right.$$

$$i (20A + 19B) e^{\frac{3}{2}i(c+dx)} \cos[c+dx]^2 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] +$$

$$\left. 3(2B + (4A + 11B) \cos[c+dx] + 8A \cos[c+dx]^2) \sin\left[\frac{1}{2}(c+dx)\right] \right)$$

**Problem 538: Result unnecessarily involves higher level functions.**

$$\int \frac{(a + a \sec[c+dx])^{5/2} (A + B \sec[c+dx])}{\sqrt{\cos[c+dx]}} dx$$

Optimal (type 3, 200 leaves, 6 steps):

$$\frac{a^{5/2} (38A + 25B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{8d} +$$

$$\frac{a^3 (54A + 49B) \sin[c+dx]}{24d \cos[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}} +$$

$$\frac{a^2 (2A + 3B) \sqrt{a+a \sec[c+dx]} \sin[c+dx]}{4d \cos[c+dx]^{3/2}} + \frac{aB (a+a \sec[c+dx])^{3/2} \sin[c+dx]}{3d \cos[c+dx]^{3/2}}$$

Result (type 5, 209 leaves):

$$\frac{1}{96d \cos[c+dx]^{5/2}} a^2 (1 + \cos[c+dx])^2 \sec\left[\frac{1}{2}(c+dx)\right]^5 \sqrt{a(1 + \sec[c+dx])}$$

$$\left( -3i (38A + 25B) e^{\frac{1}{2}i(c+dx)} \cos[c+dx]^3 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2i(c+dx)}\right] - \right.$$

$$i (38A + 25B) e^{\frac{3}{2}i(c+dx)} \cos[c+dx]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2i(c+dx)}\right] +$$

$$\left. (8B + 2(6A + 17B) \cos[c+dx] + (66A + 75B) \cos[c+dx]^2) \sin\left[\frac{1}{2}(c+dx)\right] \right)$$

## Problem 539: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \sec[c + d x])^{5/2} (A + B \sec[c + d x])}{\cos[c + d x]^{3/2}} dx$$

Optimal (type 3, 247 leaves, 7 steps):

$$\begin{aligned} & \frac{1}{64 d} a^{5/2} (200 A + 163 B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c + d x]}{\sqrt{a + a \sec[c + d x]}}\right] \sqrt{\cos[c + d x]} \sqrt{\sec[c + d x]} + \\ & \frac{a^3 (104 A + 95 B) \sin[c + d x]}{96 d \cos[c + d x]^{5/2} \sqrt{a + a \sec[c + d x]}} + \frac{a^3 (200 A + 163 B) \sin[c + d x]}{64 d \cos[c + d x]^{3/2} \sqrt{a + a \sec[c + d x]}} + \\ & \frac{a^2 (8 A + 11 B) \sqrt{a + a \sec[c + d x]} \sin[c + d x]}{24 d \cos[c + d x]^{5/2}} + \frac{a B (a + a \sec[c + d x])^{3/2} \sin[c + d x]}{4 d \cos[c + d x]^{5/2}} \end{aligned}$$

Result (type 5, 225 leaves):

$$\begin{aligned} & \frac{1}{768 d \cos[c + d x]^{7/2}} a^2 (1 + \cos[c + d x])^2 \sec\left[\frac{1}{2} (c + d x)\right]^5 \sqrt{a (1 + \sec[c + d x])} \\ & \left( -3 i (200 A + 163 B) e^{\frac{1}{2} i (c + d x)} \cos[c + d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i (c + d x)}\right] - \right. \\ & \quad i (200 A + 163 B) e^{\frac{3}{2} i (c + d x)} \cos[c + d x]^4 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i (c + d x)}\right] + \\ & \quad (48 B + 8 (8 A + 23 B) \cos[c + d x] + (272 A + 326 B) \cos[c + d x]^2 + (600 A + 489 B) \cos[c + d x]^3) \\ & \quad \left. \sin\left[\frac{1}{2} (c + d x)\right] \right) \end{aligned}$$

## Problem 540: Result unnecessarily involves higher level functions.

$$\int \frac{(a + a \sec[c + d x])^{5/2} (A + B \sec[c + d x])}{\cos[c + d x]^{5/2}} dx$$

Optimal (type 3, 294 leaves, 8 steps):

$$\begin{aligned} & \frac{1}{128 d} a^{5/2} (326 A + 283 B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c + d x]}{\sqrt{a + a \sec[c + d x]}}\right] \sqrt{\cos[c + d x]} \sqrt{\sec[c + d x]} + \\ & \frac{a^3 (170 A + 157 B) \sin[c + d x]}{240 d \cos[c + d x]^{7/2} \sqrt{a + a \sec[c + d x]}} + \\ & \frac{a^3 (326 A + 283 B) \sin[c + d x]}{192 d \cos[c + d x]^{5/2} \sqrt{a + a \sec[c + d x]}} + \frac{a^3 (326 A + 283 B) \sin[c + d x]}{128 d \cos[c + d x]^{3/2} \sqrt{a + a \sec[c + d x]}} + \\ & \frac{a^2 (10 A + 13 B) \sqrt{a + a \sec[c + d x]} \sin[c + d x]}{40 d \cos[c + d x]^{7/2}} + \frac{a B (a + a \sec[c + d x])^{3/2} \sin[c + d x]}{5 d \cos[c + d x]^{7/2}} \end{aligned}$$

Result (type 5, 244 leaves):

$$\frac{1}{7680 d \cos [c+d x]^{9/2}} a^2 (1+\cos [c+d x])^2 \sec \left[\frac{1}{2}(c+d x)\right]^5 \sqrt{a(1+\sec [c+d x])} \\ \left(-15 i(326 A+283 B) e^{\frac{1}{2} i(c+d x)} \cos [c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{1}{4}, 1, \frac{5}{4}, -e^{2 i(c+d x)}\right] - \right. \\ \left. 5 i(326 A+283 B) e^{\frac{3}{2} i(c+d x)} \cos [c+d x]^5 \operatorname{Hypergeometric2F1}\left[\frac{3}{4}, 1, \frac{7}{4}, -e^{2 i(c+d x)}\right] + \right. \\ \left. (384 B+48(10 A+29 B) \cos [c+d x]+8(230 A+283 B) \cos [c+d x]^2 + \right. \\ \left. 10(326 A+283 B) \cos [c+d x]^3+15(326 A+283 B) \cos [c+d x]^4) \sin \left[\frac{1}{2}(c+d x)\right]\right)$$

**Problem 546: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{3/2} \sqrt{a+a \sec [c+d x]}} dx$$

Optimal (type 3, 181 leaves, 7 steps):

$$\frac{(2 A-B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan [c+d x]}{\sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}}{\sqrt{a} d}-\frac{1}{\sqrt{a} d} \\ \sqrt{2}(A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec [c+d x]} \sin [c+d x]}{\sqrt{2} \sqrt{a+a \sec [c+d x]}}\right] \sqrt{\cos [c+d x]} \sqrt{\sec [c+d x]}+ \\ \frac{B \sin [c+d x]}{d \cos [c+d x]^{3/2} \sqrt{a+a \sec [c+d x]}}$$

Result (type 3, 402 leaves):

$$\frac{1}{4 d \cos [c+d x]^{3/2} \sqrt{a(1+\sec [c+d x])} \sqrt{\sin [c+d x]^2}} \\ \sin [c+d x] \left(-\cos [c+d x] \sqrt{1+\cos [c+d x]} \left(2 \sqrt{2} B \log [1+\cos [c+d x]]+\right.\right. \\ \left.\left.(8 A-4 B) \log \left[\sqrt{\cos [c+d x]}(1+\cos [c+d x])\right]-2 \sqrt{2} A \log \left[(1+\cos [c+d x])^2\right]+\right.\right. \\ \left.\left.\sqrt{2} B \log \left[(1+\cos [c+d x])^2\right]-2 \sqrt{2} B \log \left[2 \sqrt{1+\cos [c+d x]}+\sqrt{2-2 \cos [c+d x]^2}\right]-\right.\right. \\ \left.\left.8 A \log \left[1+\cos [c+d x]+\sqrt{1+\cos [c+d x]} \sqrt{\sin [c+d x]^2}\right]+\right.\right. \\ \left.\left.4 B \log \left[1+\cos [c+d x]+\sqrt{1+\cos [c+d x]} \sqrt{\sin [c+d x]^2}\right]+\right.\right. \\ \left.\left.2 \sqrt{2} A \log \left[3+2 \cos [c+d x]-\cos [c+d x]^2+2 \sqrt{2} \sqrt{1+\cos [c+d x]} \sqrt{\sin [c+d x]^2}\right]-\right.\right. \\ \left.\left.\sqrt{2} B \log \left[3+2 \cos [c+d x]-\cos [c+d x]^2+2 \sqrt{2} \sqrt{1+\cos [c+d x]} \sqrt{\sin [c+d x]^2}\right]\right)+4\right. \\ \left.B \sqrt{\sin [c+d x]^2}\right)$$

**Problem 547: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{5/2} \sqrt{a+a \sec [c+d x]}} dx$$



Optimal (type 3, 230 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{(4A - 7B) \operatorname{ArcSinh}\left[\frac{\sqrt{a} \tan[c+dx]}{\sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{4\sqrt{a}d} + \frac{1}{\sqrt{a}d} \\
 & + \frac{\sqrt{2}(A-B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\sec[c+dx]} \sin[c+dx]}{\sqrt{2} \sqrt{a+a \sec[c+dx]}}\right] \sqrt{\cos[c+dx]} \sqrt{\sec[c+dx]}}{2d \cos[c+dx]^{5/2} \sqrt{a+a \sec[c+dx]}} + \frac{(4A-B) \sin[c+dx]}{4d \cos[c+dx]^{3/2} \sqrt{a+a \sec[c+dx]}}
 \end{aligned}$$

Result (type 3, 481 leaves):

$$\begin{aligned}
 & \left( \cos\left[\frac{1}{2}(c+dx)\right] \left( B \sec[c+dx]^2 \sin\left[\frac{1}{2}(c+dx)\right] + \frac{1}{2} \sec[c+dx] \left( 4A \sin\left[\frac{1}{2}(c+dx)\right] - B \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \\
 & \left( d \sqrt{\cos[c+dx]} \sqrt{a(1+\sec[c+dx])} \right) + \frac{1}{8d \sqrt{a(1+\sec[c+dx])}} \\
 & \cos\left[\frac{1}{2}(c+dx)\right] \sqrt{\sec[c+dx]} \left( - \left( \left( \sqrt{2}(4A-B) \sqrt{\cos[c+dx]} \sqrt{1+\cos[c+dx]} \right. \right. \right. \\
 & \left. \left. \left( \log[1+\cos[c+dx]] - \log[2\sqrt{1+\cos[c+dx]} + \sqrt{2-2\cos[c+dx]^2}] \right) \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{\sec[c+dx]} \sin[c+dx] \right) / \left( \sqrt{1-\cos[c+dx]^2} \right) \right) - \\
 & \frac{1}{2\sqrt{1-\cos[c+dx]^2}} (-4A+7B) \sqrt{\cos[c+dx]} \sqrt{1+\cos[c+dx]} \\
 & \left( -\sqrt{2} \log[(1+\cos[c+dx])^2] + 4 \log[\sqrt{\cos[c+dx]} + \cos[c+dx]^{3/2}] - \right. \\
 & \left. 4 \log[1+\cos[c+dx] + \sqrt{1+\cos[c+dx]} \sqrt{1-\cos[c+dx]^2}] + \right. \\
 & \left. \sqrt{2} \log[3+2\cos[c+dx] - \cos[c+dx]^2 + 2\sqrt{2} \sqrt{1+\cos[c+dx]} \sqrt{1-\cos[c+dx]^2}] \right) \\
 & \left. \sec\left[\frac{1}{2}(c+dx)\right] \sqrt{\sec[c+dx]} \sin[c+dx] \right)
 \end{aligned}$$

**Problem 560: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \sec[c+dx]}{\cos[c+dx]^{5/2} (a+a \sec[c+dx])^{5/2}} dx$$

Optimal (type 3, 234 leaves, 8 steps):

$$\frac{2 B \operatorname{ArcSinh}\left[\frac{-\sqrt{a} \operatorname{Tan}[c+d x]}{\sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]}}{a^{5/2} d} + \frac{1}{16 \sqrt{2} a^{5/2} d}$$

$$\frac{(3 A-43 B) \operatorname{ArcTanh}\left[\frac{\sqrt{a} \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sec}[c+d x]}}\right] \sqrt{\operatorname{Cos}[c+d x]} \sqrt{\operatorname{Sec}[c+d x]} + (A-B) \operatorname{Sin}[c+d x]}{4 d \operatorname{Cos}[c+d x]^{5/2} (a+a \operatorname{Sec}[c+d x])^{5/2}} + \frac{(3 A-11 B) \operatorname{Sin}[c+d x]}{16 a d \operatorname{Cos}[c+d x]^{3/2} (a+a \operatorname{Sec}[c+d x])^{3/2}}$$

Result (type 3, 505 leaves):

$$\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]\right)^5 \left(\frac{1}{4} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]\right)^2 \left(3 A \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] - 11 B \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right) + \frac{1}{2} \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right]^4 \left(A \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] - B \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right) \Bigg/ \left(d \operatorname{Cos}[c+d x]^{5/2} (a(1+\operatorname{Sec}[c+d x]))^{5/2}\right) + \frac{1}{8 d (a(1+\operatorname{Sec}[c+d x]))^{5/2}}$$

$$\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]^5 \operatorname{Sec}[c+d x]^{5/2}$$

$$\left(-\left(\left(\sqrt{2}(3 A-11 B) \sqrt{\operatorname{Cos}[c+d x]} \sqrt{1+\operatorname{Cos}[c+d x]} \left(\operatorname{Log}[1+\operatorname{Cos}[c+d x]] - \operatorname{Log}\left[2 \sqrt{1+\operatorname{Cos}[c+d x]} + \sqrt{2-2 \operatorname{Cos}[c+d x]^2}\right]\right) \operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]\right) \Bigg/ \left(\sqrt{1-\operatorname{Cos}[c+d x]^2}\right) - \frac{1}{\sqrt{1-\operatorname{Cos}[c+d x]^2}} 16 B \sqrt{\operatorname{Cos}[c+d x]}\right. \right.$$

$$\sqrt{1+\operatorname{Cos}[c+d x]} \left(-\sqrt{2} \operatorname{Log}\left[(1+\operatorname{Cos}[c+d x])^2\right] + 4 \operatorname{Log}\left[\sqrt{\operatorname{Cos}[c+d x]} + \operatorname{Cos}[c+d x]^{3/2}\right] - 4 \operatorname{Log}\left[1+\operatorname{Cos}[c+d x] + \sqrt{1+\operatorname{Cos}[c+d x]} \sqrt{1-\operatorname{Cos}[c+d x]^2}\right] + \sqrt{2} \operatorname{Log}\left[3+2 \operatorname{Cos}[c+d x] - \operatorname{Cos}[c+d x]^2 + 2 \sqrt{2} \sqrt{1+\operatorname{Cos}[c+d x]} \sqrt{1-\operatorname{Cos}[c+d x]^2}\right]\right)$$

$$\left.\operatorname{Sec}\left[\frac{1}{2}(c+d x)\right] \sqrt{\operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]\right)$$

**Problem 578: Result more than twice size of optimal antiderivative.**

$$\int \frac{A+B \operatorname{Sec}[c+d x]}{\operatorname{Cos}[c+d x]^{3/2} (a+b \operatorname{Sec}[c+d x])} dx$$

Optimal (type 4, 86 leaves, 6 steps):

$$-\frac{2 B \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{b d} + \frac{2 (A b-a B) \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2}(c+d x), 2\right]}{b (a+b) d} + \frac{2 B \operatorname{Sin}[c+d x]}{b d \sqrt{\operatorname{Cos}[c+d x]}}$$

Result (type 4, 208 leaves):

$$\frac{1}{2 b d} \left( \frac{2 (2 A b - 3 a B) \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2} (c+d x), 2\right]}{a+b} - \frac{2 b B \left( 2 \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right] - \frac{2 b \operatorname{EllipticPi}\left[\frac{2 a}{a+b}, \frac{1}{2} (c+d x), 2\right]}{a+b} \right)}{a} + \frac{4 B \sin [c+d x]}{\sqrt{\cos [c+d x]}} + \left( 2 B \left( 2 a b \operatorname{EllipticE}\left[\operatorname{ArcSin}\left[\sqrt{\cos [c+d x]}\right], -1\right] - 2 b (a+b) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\cos [c+d x]}\right], -1\right] + (a^2 - 2 b^2) \operatorname{EllipticPi}\left[-\frac{a}{b}, -\operatorname{ArcSin}\left[\sqrt{\cos [c+d x]}\right], -1\right] \sin [c+d x] \right) \right) / \left( a b \sqrt{\sin [c+d x]^2} \right) \right)$$

Problem 594: Unable to integrate problem.

$$\int \cos [c+d x]^{7/2} \sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]) d x$$

Optimal (type 4, 343 leaves, 11 steps):

$$\begin{aligned} & \left( 2 (a^2 - b^2) (25 a^2 A + 8 A b^2 - 14 a b B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \right) / \\ & \left( 105 a^3 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \right) + \\ & \left( 2 (19 a^2 A b + 8 A b^3 + 63 a^3 B - 14 a b^2 B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \right. \\ & \left. \sqrt{a+b \sec [c+d x]} \right) / \left( 105 a^3 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{1}{105 a^2 d} \\ & \frac{2 (25 a^2 A - 4 A b^2 + 7 a b B) \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x] + 2 (A b + 7 a B) \cos [c+d x]^{3/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{35 a d} + \\ & \frac{2 A \cos [c+d x]^{5/2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{7 d} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \cos [c+d x]^{7/2} \sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]) d x$$

## Problem 595: Unable to integrate problem.

$$\int \cos[c+dx]^{5/2} \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 267 leaves, 10 steps):

$$\begin{aligned} & - \frac{2(a^2 - b^2)(2Ab - 5aB) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right]}{15a^2 d \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]}} + \\ & \left( 2(9a^2 A - 2Ab^2 + 5abB) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]} \right) / \\ & \left( 15a^2 d \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \right) + \frac{2(Ab + 5aB) \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{15ad} + \\ & \frac{2A \cos[c+dx]^{3/2} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{5d} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \cos[c+dx]^{5/2} \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) dx$$

## Problem 596: Unable to integrate problem.

$$\int \cos[c+dx]^{3/2} \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 201 leaves, 9 steps):

$$\begin{aligned} & \frac{2A(a^2 - b^2) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right]}{3ad \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]}} + \\ & \left( 2(Ab + 3aB) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]} \right) / \\ & \left( 3ad \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \right) + \frac{2A \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{3d} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \cos[c+dx]^{3/2} \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) dx$$

## Problem 597: Unable to integrate problem.

$$\int \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]} (A+B \sec[c+dx]) dx$$

Optimal (type 4, 208 leaves, 12 steps):

$$\frac{2 a B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\frac{2 b B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\frac{2 A \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}}$$

Result (type 8, 37 leaves):

$$\int \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x]) dx$$

Problem 598: Unable to integrate problem.

$$\int \frac{\sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x])}{\sqrt{\cos [c+d x]}} dx$$

Optimal (type 4, 253 leaves, 13 steps):

$$\frac{(2 a A+b B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\frac{(2 A b+a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} -$$

$$\frac{B \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} +$$

$$\frac{B \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{d \sqrt{\cos [c+d x]}}$$

Result (type 8, 37 leaves):

$$\int \frac{\sqrt{a+b \sec [c+d x]} (A+B \sec [c+d x])}{\sqrt{\cos [c+d x]}} dx$$

### Problem 599: Unable to integrate problem.

$$\int \frac{\sqrt{a+b \operatorname{Sec}[c+d x]} (A+B \operatorname{Sec}[c+d x])}{\operatorname{Cos}[c+d x]^{3/2}} dx$$

Optimal (type 4, 336 leaves, 14 steps):

$$\begin{aligned} & \frac{(4 A b+3 a B) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} + \\ & \frac{(4 a A b-a^2 B+4 b^2 B) \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 b d \sqrt{\operatorname{Cos}[c+d x]} \sqrt{a+b \operatorname{Sec}[c+d x]}} - \\ & \left( (4 A b+a B) \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \operatorname{Sec}[c+d x]} \right) / \\ & \left( 4 b d \sqrt{\frac{b+a \operatorname{Cos}[c+d x]}{a+b}} \right) + \frac{B \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{2 d \operatorname{Cos}[c+d x]^{3/2}} + \\ & \frac{(4 A b+a B) \sqrt{a+b \operatorname{Sec}[c+d x]} \operatorname{Sin}[c+d x]}{4 b d \sqrt{\operatorname{Cos}[c+d x]}} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\sqrt{a+b \operatorname{Sec}[c+d x]} (A+B \operatorname{Sec}[c+d x])}{\operatorname{Cos}[c+d x]^{3/2}} dx$$

### Problem 600: Unable to integrate problem.

$$\int \operatorname{Cos}[c+d x]^{9/2} (a+b \operatorname{Sec}[c+d x])^{3/2} (A+B \operatorname{Sec}[c+d x]) dx$$

Optimal (type 4, 427 leaves, 12 steps):

$$\begin{aligned}
& \left( 2 (a^2 - b^2) (39 a^2 A b + 8 A b^3 + 75 a^3 B - 18 a b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\
& \quad \left. \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 315 a^3 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \\
& \left( 2 (147 a^4 A + 33 a^2 A b^2 + 8 A b^4 + 246 a^3 b B - 18 a b^3 B) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\
& \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 315 a^3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{1}{315 a^2 d} \\
& 2 (88 a^2 A b - 4 A b^3 + 75 a^3 B + 9 a b^2 B) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
& \frac{1}{315 a d} 2 (49 a^2 A + 3 A b^2 + 72 a b B) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
& \frac{2 (10 A b + 9 a B) \cos [c + d x]^{5/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{63 d} + \\
& \frac{2 a A \cos [c + d x]^{7/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{9 d}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \cos [c + d x]^{9/2} (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x]) dx$$

**Problem 601: Unable to integrate problem.**

$$\int \cos [c + d x]^{7/2} (a + b \sec [c + d x])^{3/2} (A + B \sec [c + d x]) dx$$

Optimal (type 4, 342 leaves, 11 steps):

$$\begin{aligned}
& \left( 2 (a^2 - b^2) (25 a^2 A - 6 A b^2 + 21 a b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\
& \quad \left. (105 a^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}) \right) + \\
& \left( 2 (82 a^2 A b - 6 A b^3 + 63 a^3 B + 21 a b^2 B) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\
& \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 105 a^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{1}{105 a d} \\
& 2 (25 a^2 A + 3 A b^2 + 42 a b B) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\
& \frac{2 (8 A b + 7 a B) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{35 d} + \\
& \frac{2 a A \cos [c + d x]^{5/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{7 d}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \cos [c+d x]^{7 / 2} (a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x]) d x$$

Problem 602: Unable to integrate problem.

$$\int \cos [c+d x]^{5 / 2} (a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x]) d x$$

Optimal (type 4, 266 leaves, 10 steps):

$$\begin{aligned} & \frac{2 \left(a^2 - b^2\right) (3 A b + 5 a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{15 a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\ & \left(2 \left(9 a^2 A + 3 A b^2 + 20 a b B\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) / \\ & \left(15 a d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) + \frac{2 (6 A b + 5 a B) \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{15 d} + \\ & \frac{2 a A \cos [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{5 d} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \cos [c+d x]^{5 / 2} (a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x]) d x$$

Problem 603: Unable to integrate problem.

$$\int \cos [c+d x]^{3 / 2} (a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x]) d x$$

Optimal (type 4, 276 leaves, 13 steps):

$$\begin{aligned} & \frac{2 \left(a^2 A - A b^2 + 3 a b B\right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\ & \frac{2 b^2 B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \frac{1}{3 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} \\ & 2 \left(4 A b + 3 a B\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} + \\ & \frac{2 a A \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{3 d} \end{aligned}$$



Result (type 8, 37 leaves):

$$\int \cos [c+d x]^{3 / 2} (a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x]) d x$$

Problem 604: Unable to integrate problem.

$$\int \sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x]) d x$$

Optimal (type 4, 272 leaves, 13 steps):

$$\begin{aligned} & \frac{(2 a A b+2 a^2 B+b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}+ \\ & \frac{b(2 A b+3 a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}+\frac{1}{d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} \\ & \frac{(2 a A-b B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}+}{d \sqrt{\cos [c+d x]}} \\ & \frac{b B \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{d \sqrt{\cos [c+d x]}} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x]) d x$$

Problem 605: Unable to integrate problem.

$$\int \frac{(a+b \sec [c+d x])^{3 / 2} (A+B \sec [c+d x])}{\sqrt{\cos [c+d x]}} d x$$

Optimal (type 4, 339 leaves, 14 steps):

$$\begin{aligned}
& \frac{(8 a^2 A + 4 A b^2 + 7 a b B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
& \left( (12 a A b + 3 a^2 B + 4 b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\
& \left( 4 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \right) - \frac{1}{4 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} \\
& \frac{(4 A b + 5 a B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} +}{2 d \cos [c+d x]^{3/2}} + \frac{(4 A b + 5 a B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 d \sqrt{\cos [c+d x]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{(a+b \sec [c+d x])^{3/2} (A+B \sec [c+d x])}{\sqrt{\cos [c+d x]}} dx$$

Problem 606: Unable to integrate problem.

$$\int \frac{(a+b \sec [c+d x])^{3/2} (A+B \sec [c+d x])}{\cos [c+d x]^{3/2}} dx$$

Optimal (type 4, 421 leaves, 15 steps):

$$\begin{aligned}
& \frac{(42 a A b + 17 a^2 B + 16 b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{24 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
& \left( (6 a^2 A b + 8 A b^3 - a^3 B + 12 a b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\
& \left( 8 b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \right) - \\
& \left( (30 a A b + 3 a^2 B + 16 b^2 B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\
& \left( 24 b d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{b B \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{3 d \cos [c+d x]^{5/2}} + \\
& \frac{(6 A b + 7 a B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{12 d \cos [c+d x]^{3/2}} + \\
& \frac{(30 a A b + 3 a^2 B + 16 b^2 B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{24 b d \sqrt{\cos [c+d x]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{(a + b \operatorname{Sec}[c + d x])^{3/2} (A + B \operatorname{Sec}[c + d x])}{\operatorname{Cos}[c + d x]^{3/2}} dx$$

Problem 607: Unable to integrate problem.

$$\int \operatorname{Cos}[c + d x]^{11/2} (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x]) dx$$

Optimal (type 4, 519 leaves, 13 steps):

$$\begin{aligned} & \left( 2 (a^2 - b^2) (675 a^4 A + 285 a^2 A b^2 + 40 A b^4 + 1254 a^3 b B - 110 a b^3 B) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right. \\ & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2a}{a + b}\right] \right) / \left( 3465 a^3 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \right) + \\ & \left( 2 (3705 a^4 A b + 255 a^2 A b^3 + 40 A b^5 + 1617 a^5 B + 3069 a^3 b^2 B - 110 a b^4 B) \sqrt{\operatorname{Cos}[c + d x]} \right. \\ & \quad \left. \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \left( 3465 a^3 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right) + \\ & \frac{1}{3465 a^2 d} 2 (675 a^4 A + 1025 a^2 A b^2 - 20 A b^4 + 1793 a^3 b B + 55 a b^3 B) \\ & \quad \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x] + \frac{1}{3465 a d} \\ & 2 (1145 a^2 A b + 15 A b^3 + 539 a^3 B + 825 a b^2 B) \operatorname{Cos}[c + d x]^{3/2} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x] + \\ & \frac{1}{693 d} 2 (81 a^2 A + 113 A b^2 + 209 a b B) \operatorname{Cos}[c + d x]^{5/2} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x] + \\ & \frac{2 a (14 A b + 11 a B) \operatorname{Cos}[c + d x]^{7/2} \sqrt{a + b \operatorname{Sec}[c + d x]} \operatorname{Sin}[c + d x]}{99 d} + \\ & \frac{2 a A \operatorname{Cos}[c + d x]^{9/2} (a + b \operatorname{Sec}[c + d x])^{3/2} \operatorname{Sin}[c + d x]}{11 d} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \operatorname{Cos}[c + d x]^{11/2} (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x]) dx$$

Problem 608: Unable to integrate problem.

$$\int \operatorname{Cos}[c + d x]^{9/2} (a + b \operatorname{Sec}[c + d x])^{5/2} (A + B \operatorname{Sec}[c + d x]) dx$$

Optimal (type 4, 425 leaves, 12 steps):

$$\begin{aligned} & \left( 2 (a^2 - b^2) (114 a^2 A b - 10 A b^3 + 75 a^3 B + 45 a b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \left( 315 a^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) + \\ & \left( 2 (147 a^4 A + 279 a^2 A b^2 - 10 A b^4 + 435 a^3 b B + 45 a b^3 B) \sqrt{\cos [c + d x]} \right. \\ & \quad \left. \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \left( 315 a^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{1}{315 a d} \\ & 2 (163 a^2 A b + 5 A b^3 + 75 a^3 B + 135 a b^2 B) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\ & \frac{1}{315 d} 2 (49 a^2 A + 75 A b^2 + 135 a b B) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\ & \frac{2 a (4 A b + 3 a B) \cos [c + d x]^{5/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{21 d} + \\ & \frac{2 a A \cos [c + d x]^{7/2} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{9 d} \end{aligned}$$

Result(type 8, 37 leaves):

$$\int \cos [c + d x]^{9/2} (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x]) dx$$

**Problem 609: Unable to integrate problem.**

$$\int \cos [c + d x]^{7/2} (a + b \sec [c + d x])^{5/2} (A + B \sec [c + d x]) dx$$

Optimal (type 4, 340 leaves, 11 steps):

$$\begin{aligned} & \left( 2 (a^2 - b^2) (25 a^2 A + 15 A b^2 + 56 a b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\ & \quad \left. (105 a d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}) + \right. \\ & \quad \left( 2 (145 a^2 A b + 15 A b^3 + 63 a^3 B + 161 a b^2 B) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\ & \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 105 a d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{1}{105 d} \\ & 2 (25 a^2 A + 45 A b^2 + 77 a b B) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \\ & \frac{2 a (10 A b + 7 a B) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{35 d} + \\ & \frac{2 a A \cos [c + d x]^{5/2} (a + b \sec [c + d x])^{3/2} \sin [c + d x]}{7 d} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \cos [c+d x]^{7 / 2} (a+b \sec [c+d x])^{5 / 2} (A+B \sec [c+d x]) d x$$

Problem 610: Unable to integrate problem.

$$\int \cos [c+d x]^{5 / 2} (a+b \sec [c+d x])^{5 / 2} (A+B \sec [c+d x]) d x$$

Optimal (type 4, 342 leaves, 14 steps):

$$\begin{aligned} & \left( 2 \left( 8 a^2 A b - 8 A b^3 + 5 a^3 B + 10 a b^2 B \right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\ & \left( 15 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \right) + \frac{2 b^3 B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\ & \left( 2 \left( 9 a^2 A + 23 A b^2 + 35 a b B \right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\ & \left( 15 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{2 a \left( 8 A b + 5 a B \right) \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{15 d} + \\ & \frac{2 a A \cos [c+d x]^{3 / 2} (a+b \sec [c+d x])^{3 / 2} \sin [c+d x]}{5 d} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \cos [c+d x]^{5 / 2} (a+b \sec [c+d x])^{5 / 2} (A+B \sec [c+d x]) d x$$

Problem 611: Unable to integrate problem.

$$\int \cos [c+d x]^{3 / 2} (a+b \sec [c+d x])^{5 / 2} (A+B \sec [c+d x]) d x$$

Optimal (type 4, 349 leaves, 14 steps):

$$\begin{aligned}
& \left( (2a^3A + 4aAb^2 + 12a^2bB + 3b^3B) \sqrt{\frac{b+a\cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \right) / \\
& \left( 3d \sqrt{\cos[c+dx]} \sqrt{a+b\sec[c+dx]} \right) + \\
& \frac{b^2(2Ab + 5aB) \sqrt{\frac{b+a\cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right]}{d \sqrt{\cos[c+dx]} \sqrt{a+b\sec[c+dx]}} + \frac{1}{3d \sqrt{\frac{b+a\cos[c+dx]}{a+b}}} \\
& \frac{(14aAb + 6a^2B - 3b^2B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b\sec[c+dx]} -}{b(2aA - 3bB) \sqrt{a+b\sec[c+dx]} \sin[c+dx]} + \\
& \frac{2aA \sqrt{\cos[c+dx]} (a+b\sec[c+dx])^{3/2} \sin[c+dx]}{3d}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \cos[c+dx]^{3/2} (a+b\sec[c+dx])^{5/2} (A+B\sec[c+dx]) dx$$

### Problem 612: Unable to integrate problem.

$$\int \sqrt{\cos[c+dx]} (a+b\sec[c+dx])^{5/2} (A+B\sec[c+dx]) dx$$

Optimal (type 4, 359 leaves, 14 steps):

$$\begin{aligned}
& \left( (16a^2Ab + 4Ab^3 + 8a^3B + 11ab^2B) \sqrt{\frac{b+a\cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \right) / \\
& \left( 4d \sqrt{\cos[c+dx]} \sqrt{a+b\sec[c+dx]} \right) + \\
& \left( b(20aAb + 15a^2B + 4b^2B) \sqrt{\frac{b+a\cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \right) / \\
& \left( 4d \sqrt{\cos[c+dx]} \sqrt{a+b\sec[c+dx]} \right) + \frac{1}{4d \sqrt{\frac{b+a\cos[c+dx]}{a+b}}} \\
& \frac{(8a^2A - 4Ab^2 - 9abB) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b\sec[c+dx]} +}{b(4Ab + 7aB) \sqrt{a+b\sec[c+dx]} \sin[c+dx]} + \frac{bB(a+b\sec[c+dx])^{3/2} \sin[c+dx]}{2d \sqrt{\cos[c+dx]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \sqrt{\cos[c+dx]} (a+b \sec[c+dx])^{5/2} (A+B \sec[c+dx]) dx$$

Problem 613: Unable to integrate problem.

$$\int \frac{(a+b \sec[c+dx])^{5/2} (A+B \sec[c+dx])}{\sqrt{\cos[c+dx]}} dx$$

Optimal (type 4, 422 leaves, 15 steps):

$$\begin{aligned} & \left( (48 a^3 A + 66 a A b^2 + 59 a^2 b B + 16 b^3 B) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \right) / \\ & \left( 24 d \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]} \right) + \\ & \left( (30 a^2 A b + 8 A b^3 + 5 a^3 B + 20 a b^2 B) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \right) / \\ & \left( 8 d \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]} \right) - \\ & \left( (54 a A b + 33 a^2 B + 16 b^2 B) \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]} \right) / \\ & \left( 24 d \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \right) + \frac{b(2Ab+3aB) \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{4 d \cos[c+dx]^{3/2}} + \\ & \frac{(54 a A b + 33 a^2 B + 16 b^2 B) \sqrt{a+b \sec[c+dx]} \sin[c+dx]}{24 d \sqrt{\cos[c+dx]}} + \frac{b B (a+b \sec[c+dx])^{3/2} \sin[c+dx]}{3 d \cos[c+dx]^{3/2}} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{(a+b \sec[c+dx])^{5/2} (A+B \sec[c+dx])}{\sqrt{\cos[c+dx]}} dx$$

Problem 614: Attempted integration timed out after 120 seconds.

$$\int \frac{(a+b \sec[c+dx])^{5/2} (A+B \sec[c+dx])}{\cos[c+dx]^{3/2}} dx$$

Optimal (type 4, 513 leaves, 16 steps):

$$\begin{aligned}
& \left( (472 a^2 A b + 128 A b^3 + 133 a^3 B + 356 a b^2 B) \sqrt{\frac{b + a \cos[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \\
& \left( 192 d \sqrt{\cos[c + d x]} \sqrt{a + b \sec[c + d x]} \right) + \\
& \left( (40 a^3 A b + 160 a A b^3 - 5 a^4 B + 120 a^2 b^2 B + 48 b^4 B) \sqrt{\frac{b + a \cos[c + d x]}{a + b}} \right. \\
& \left. \operatorname{EllipticPi}\left[2, \frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 64 b d \sqrt{\cos[c + d x]} \sqrt{a + b \sec[c + d x]} \right) - \\
& \left( (264 a^2 A b + 128 A b^3 + 15 a^3 B + 284 a b^2 B) \sqrt{\cos[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right. \\
& \left. \sqrt{a + b \sec[c + d x]} \right) / \left( 192 b d \sqrt{\frac{b + a \cos[c + d x]}{a + b}} \right) + \\
& \frac{b (8 A b + 11 a B) \sqrt{a + b \sec[c + d x]} \sin[c + d x]}{24 d \cos[c + d x]^{5/2}} + \\
& \frac{(104 a A b + 59 a^2 B + 36 b^2 B) \sqrt{a + b \sec[c + d x]} \sin[c + d x]}{96 d \cos[c + d x]^{3/2}} + \\
& \left( (264 a^2 A b + 128 A b^3 + 15 a^3 B + 284 a b^2 B) \sqrt{a + b \sec[c + d x]} \sin[c + d x] \right) / \\
& \left( 192 b d \sqrt{\cos[c + d x]} \right) + \frac{b B (a + b \sec[c + d x])^{3/2} \sin[c + d x]}{4 d \cos[c + d x]^{5/2}}
\end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 615: Unable to integrate problem.

$$\int \frac{\cos[c + d x]^{5/2} (A + B \sec[c + d x])}{\sqrt{a + b \sec[c + d x]}} dx$$

Optimal (type 4, 280 leaves, 10 steps):



$$\begin{aligned}
& - \left( \left( 2 (7 a^2 A b + 8 A b^3 - 5 a^3 B - 10 a b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \right. \\
& \quad \left. \left( 15 a^3 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) \right) + \\
& \left( 2 (9 a^2 A + 8 A b^2 - 10 a b B) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\
& \left( 15 a^3 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) - \\
& \frac{2 (4 A b - 5 a B) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{15 a^2 d} + \\
& \frac{2 A \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{5 a d}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\cos [c + d x]^{5/2} (A + B \sec [c + d x])}{\sqrt{a + b \sec [c + d x]}} dx$$

**Problem 616: Unable to integrate problem.**

$$\int \frac{\cos [c + d x]^{3/2} (A + B \sec [c + d x])}{\sqrt{a + b \sec [c + d x]}} dx$$

Optimal (type 4, 212 leaves, 9 steps):

$$\begin{aligned}
& \frac{2 (a^2 A + 2 A b^2 - 3 a b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right]}{3 a^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}} - \\
& \left( 2 (2 A b - 3 a B) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\
& \left( 3 a^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{2 A \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x]}{3 a d}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\cos [c + d x]^{3/2} (A + B \sec [c + d x])}{\sqrt{a + b \sec [c + d x]}} dx$$

### Problem 617: Unable to integrate problem.

$$\int \frac{\sqrt{\cos[c+dx]} (A+B \sec[c+dx])}{\sqrt{a+b \sec[c+dx]}} dx$$

Optimal (type 4, 150 leaves, 8 steps):

$$\begin{aligned} & -\frac{2(Ab-aB) \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right]}{ad \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]}} + \\ & \frac{2A \sqrt{\cos[c+dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right] \sqrt{a+b \sec[c+dx]}}{ad \sqrt{\frac{b+a \cos[c+dx]}{a+b}}} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\sqrt{\cos[c+dx]} (A+B \sec[c+dx])}{\sqrt{a+b \sec[c+dx]}} dx$$

### Problem 618: Unable to integrate problem.

$$\int \frac{A+B \sec[c+dx]}{\sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]}} dx$$

Optimal (type 4, 138 leaves, 8 steps):

$$\begin{aligned} & \frac{2A \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), \frac{2a}{a+b}\right]}{d \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]}} + \\ & \frac{2B \sqrt{\frac{b+a \cos[c+dx]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+dx), \frac{2a}{a+b}\right]}{d \sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]}} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{A+B \sec[c+dx]}{\sqrt{\cos[c+dx]} \sqrt{a+b \sec[c+dx]}} dx$$

### Problem 619: Unable to integrate problem.

$$\int \frac{A+B \sec[c+dx]}{\cos[c+dx]^{3/2} \sqrt{a+b \sec[c+dx]}} dx$$

Optimal (type 4, 256 leaves, 13 steps):

$$\begin{aligned}
& \frac{B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
& \frac{(2 A b-a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\
& \frac{B \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}}{b d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}} + \\
& \frac{B \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{b d \sqrt{\cos [c+d x]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]}} d x$$

**Problem 620: Unable to integrate problem.**

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{5 / 2} \sqrt{a+b \sec [c+d x]}} d x$$

Optimal (type 4, 344 leaves, 14 steps):

$$\begin{aligned}
& \frac{(4 A b-a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\
& \left( (4 a A b-3 a^2 B-4 b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\
& \left( 4 b^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \right) - \\
& \left( (4 A b-3 a B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\
& \left( 4 b^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{B \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 b d \cos [c+d x]^{3 / 2}} + \\
& \frac{(4 A b-3 a B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 b^2 d \sqrt{\cos [c+d x]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{5 / 2} \sqrt{a+b \sec [c+d x]}} d x$$

### Problem 621: Unable to integrate problem.

$$\int \frac{\cos [c+d x]^{5 / 2} (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{3 / 2}} d x$$

Optimal (type 4, 423 leaves, 11 steps):

$$\begin{aligned} & - \left( \left( 2 \left( 12 a^2 A b + 48 A b^3 - 5 a^3 B - 40 a b^2 B \right) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \right. \\ & \quad \left. \left( 15 a^4 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \right) \right) + \\ & \left( 2 \left( 9 a^4 A + 24 a^2 A b^2 - 48 A b^4 - 25 a^3 b B + 40 a b^3 B \right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right. \\ & \quad \left. \sqrt{a+b \sec [c+d x]} \right) / \left( 15 a^4 \left( a^2 - b^2 \right) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \\ & \frac{2 b (A b - a B) \cos [c+d x]^{3 / 2} \sin [c+d x]}{a \left( a^2 - b^2 \right) d \sqrt{a+b \sec [c+d x]}} - \frac{1}{15 a^3 \left( a^2 - b^2 \right) d} \\ & 2 \left( 9 a^2 A b - 24 A b^3 - 5 a^3 B + 20 a b^2 B \right) \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x] + \\ & \frac{1}{5 a^2 \left( a^2 - b^2 \right) d} 2 \left( a^2 A - 6 A b^2 + 5 a b B \right) \cos [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]} \sin [c+d x] \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\cos [c+d x]^{5 / 2} (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{3 / 2}} d x$$

### Problem 622: Unable to integrate problem.

$$\int \frac{\cos [c+d x]^{3 / 2} (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{3 / 2}} d x$$

Optimal (type 4, 326 leaves, 10 steps):

$$\begin{aligned}
& \frac{2 (a^2 A + 8 A b^2 - 6 a b B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right]}{3 a^3 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\
& \left( 2 (5 a^2 A b - 8 A b^3 - 3 a^3 B + 6 a b^2 B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \right. \\
& \quad \left. \sqrt{a+b \sec [c+d x]} \right) / \left( 3 a^3 (a^2 - b^2) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \\
& \frac{2 b (A b - a B) \sqrt{\cos [c+d x]} \sin [c+d x]}{a (a^2 - b^2) d \sqrt{a+b \sec [c+d x]}} + \frac{1}{3 a^2 (a^2 - b^2) d} \\
& 2 (a^2 A - 4 A b^2 + 3 a b B) \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \sin [c+d x]
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\cos [c+d x]^{3/2} (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{3/2}} dx$$

Problem 623: Unable to integrate problem.

$$\int \frac{\sqrt{\cos [c+d x]} (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{3/2}} dx$$

Optimal (type 4, 235 leaves, 9 steps):

$$\begin{aligned}
& - \frac{2 (2 A b - a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right]}{a^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
& \left( 2 (a^2 A - 2 A b^2 + a b B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\
& \left( a^2 (a^2 - b^2) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{2 b (A b - a B) \sin [c+d x]}{a (a^2 - b^2) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\sqrt{\cos [c+d x]} (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{3/2}} dx$$

Problem 624: Unable to integrate problem.

$$\int \frac{A+B \sec [c+d x]}{\sqrt{\cos [c+d x]} (a+b \sec [c+d x])^{3/2}} dx$$

Optimal (type 4, 215 leaves, 9 steps):

$$\frac{2 A \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{a d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} +$$

$$\left(2(A b-a B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) /$$

$$\left(a\left(a^2-b^2\right) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right)-\frac{2(A b-a B) \sin [c+d x]}{\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}$$

Result (type 8, 37 leaves):

$$\int \frac{A+B \sec [c+d x]}{\sqrt{\cos [c+d x]}(a+b \sec [c+d x])^{3/2}} dx$$

**Problem 625: Unable to integrate problem.**

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{3/2}(a+b \sec [c+d x])^{3/2}} dx$$

Optimal (type 4, 220 leaves, 10 steps):

$$\frac{2 B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} -$$

$$\left(2(A b-a B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) /$$

$$\left(b\left(a^2-b^2\right) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right)+\frac{2 a(A b-a B) \sin [c+d x]}{b\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}$$

Result (type 8, 37 leaves):

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{3/2}(a+b \sec [c+d x])^{3/2}} dx$$

**Problem 626: Unable to integrate problem.**

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{5/2}(a+b \sec [c+d x])^{3/2}} dx$$

Optimal (type 4, 371 leaves, 14 steps):

$$\begin{aligned}
& \frac{B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
& \frac{(2 A b-3 a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
& \left( (2 a A b-3 a^2 B+b^2 B) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\
& \left( b^2 \left(a^2-b^2\right) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{2 a (A b-a B) \sin [c+d x]}{b \left(a^2-b^2\right) d \cos [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]}} - \\
& \frac{(2 a A b-3 a^2 B+b^2 B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{b^2 \left(a^2-b^2\right) d \sqrt{\cos [c+d x]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{5 / 2} (a+b \sec [c+d x])^{3 / 2}} d x$$

**Problem 627:** Attempted integration timed out after 120 seconds.

$$\int \frac{A+B \sec [c+d x]}{\cos [c+d x]^{7 / 2} (a+b \sec [c+d x])^{3 / 2}} d x$$

Optimal (type 4, 487 leaves, 15 steps):

$$\begin{aligned}
& \frac{(4 A b - 5 a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{4 b^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} - \\
& \left( (12 a A b - 15 a^2 B - 4 b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right) / \\
& \left( 4 b^3 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]} \right) - \left( (12 a^2 A b - 4 A b^3 - 15 a^3 B + 7 a b^2 B) \right. \\
& \left. \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]} \right) / \\
& \left( 4 b^3 (a^2 - b^2) d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \frac{2 a (A b - a B) \sin [c+d x]}{b (a^2 - b^2) d \cos [c+d x]^{5/2} \sqrt{a+b \sec [c+d x]}} - \\
& \frac{(4 a A b - 5 a^2 B + b^2 B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{2 b^2 (a^2 - b^2) d \cos [c+d x]^{3/2}} + \\
& \frac{(12 a^2 A b - 4 A b^3 - 15 a^3 B + 7 a b^2 B) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{4 b^3 (a^2 - b^2) d \sqrt{\cos [c+d x]}}
\end{aligned}$$

Result (type 1, 1 leaves):

???

### Problem 628: Unable to integrate problem.

$$\int \frac{\cos [c+d x]^{5/2} (A+B \sec [c+d x])}{(a+b \sec [c+d x])^{5/2}} dx$$

Optimal (type 4, 588 leaves, 12 steps):



$$\begin{aligned}
& - \left( \left( 2 \left( 17 a^4 A b + 116 a^2 A b^3 - 128 A b^5 - 5 a^5 B - 80 a^3 b^2 B + 80 a b^4 B \right) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \right. \\
& \quad \left. \left. \operatorname{EllipticF} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \right) / \left( 15 a^5 (a^2 - b^2) d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) \right) + \\
& \quad \left( 2 \left( 9 a^6 A + 55 a^4 A b^2 - 212 a^2 A b^4 + 128 A b^6 - 40 a^5 b B + 140 a^3 b^3 B - 80 a b^5 B \right) \right. \\
& \quad \left. \sqrt{\cos [c + d x]} \operatorname{EllipticE} \left[ \frac{1}{2} (c + d x), \frac{2 a}{a + b} \right] \sqrt{a + b \sec [c + d x]} \right) / \\
& \quad \left( 15 a^5 (a^2 - b^2)^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{2 b (A b - a B) \cos [c + d x]^{3/2} \sin [c + d x]}{3 a (a^2 - b^2) d (a + b \sec [c + d x])^{3/2}} + \\
& \quad \frac{2 b (12 a^2 A b - 8 A b^3 - 9 a^3 B + 5 a b^2 B) \cos [c + d x]^{3/2} \sin [c + d x]}{3 a^2 (a^2 - b^2)^2 d \sqrt{a + b \sec [c + d x]}} - \\
& \quad \frac{1}{15 a^4 (a^2 - b^2)^2 d} \\
& \quad 2 \left( 14 a^4 A b - 98 a^2 A b^3 + 64 A b^5 - 5 a^5 B + 65 a^3 b^2 B - 40 a b^4 B \right) \\
& \quad \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] + \frac{1}{15 a^3 (a^2 - b^2)^2 d} \\
& \quad 2 \left( 3 a^4 A - 71 a^2 A b^2 + 48 A b^4 + 50 a^3 b B - 30 a b^3 B \right) \cos [c + d x]^{3/2} \sqrt{a + b \sec [c + d x]} \sin [c + d x]
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\cos [c + d x]^{5/2} (A + B \sec [c + d x])}{(a + b \sec [c + d x])^{5/2}} dx$$

Problem 629: Unable to integrate problem.

$$\int \frac{\cos [c + d x]^{3/2} (A + B \sec [c + d x])}{(a + b \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 472 leaves, 11 steps):

$$\begin{aligned} & \left( 2 \left( a^4 A + 16 a^2 A b^2 - 16 A b^4 - 9 a^3 b B + 8 a b^3 B \right) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right. \\ & \quad \left. \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \right) / \left( 3 a^4 (a^2 - b^2) d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) - \\ & \quad \left( 2 \left( 8 a^4 A b - 28 a^2 A b^3 + 16 A b^5 - 3 a^5 B + 15 a^3 b^2 B - 8 a b^4 B \right) \sqrt{\cos [c + d x]} \right. \\ & \quad \left. \operatorname{EllipticE}\left[\frac{1}{2}(c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \sec [c + d x]} \right) / \\ & \quad \left( 3 a^4 (a^2 - b^2)^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \frac{2 b (A b - a B) \sqrt{\cos [c + d x]} \sin [c + d x]}{3 a (a^2 - b^2) d (a + b \sec [c + d x])^{3/2}} + \\ & \quad \frac{2 b (10 a^2 A b - 6 A b^3 - 7 a^3 B + 3 a b^2 B) \sqrt{\cos [c + d x]} \sin [c + d x]}{3 a^2 (a^2 - b^2)^2 d \sqrt{a + b \sec [c + d x]}} + \frac{1}{3 a^3 (a^2 - b^2)^2 d} \\ & \quad 2 \left( a^4 A - 13 a^2 A b^2 + 8 A b^4 + 8 a^3 b B - 4 a b^3 B \right) \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \sin [c + d x] \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\cos [c + d x]^{3/2} (A + B \sec [c + d x])}{(a + b \sec [c + d x])^{5/2}} dx$$

**Problem 630: Unable to integrate problem.**

$$\int \frac{\sqrt{\cos [c + d x]} (A + B \sec [c + d x])}{(a + b \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 368 leaves, 10 steps):

$$\begin{aligned}
& - \left( \left( 2 (9 a^2 A b - 8 A b^3 - 3 a^3 B + 2 a b^2 B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right) / \right. \\
& \quad \left. \left( 3 a^3 (a^2 - b^2) d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]} \right) \right) + \\
& \left( 2 (3 a^4 A - 15 a^2 A b^2 + 8 A b^4 + 6 a^3 b B - 2 a b^3 B) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\
& \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 3 a^3 (a^2 - b^2)^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) + \\
& \frac{2 b (A b - a B) \sin [c + d x]}{3 a (a^2 - b^2) d \sqrt{\cos [c + d x]} (a + b \sec [c + d x])^{3/2}} + \\
& \frac{2 b (8 a^2 A b - 4 A b^3 - 5 a^3 B + a b^2 B) \sin [c + d x]}{3 a^2 (a^2 - b^2)^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{\sqrt{\cos [c + d x]} (A + B \sec [c + d x])}{(a + b \sec [c + d x])^{5/2}} dx$$

**Problem 631: Unable to integrate problem.**

$$\int \frac{A + B \sec [c + d x]}{\sqrt{\cos [c + d x]} (a + b \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 346 leaves, 10 steps):

$$\begin{aligned}
& \frac{2 (3 a^2 A - 2 A b^2 - a b B) \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right]}{3 a^2 (a^2 - b^2) d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}} + \\
& \left( 2 (6 a^2 A b - 2 A b^3 - 3 a^3 B - a b^2 B) \sqrt{\cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \right. \\
& \quad \left. \sqrt{a + b \sec [c + d x]} \right) / \left( 3 a^2 (a^2 - b^2)^2 d \sqrt{\frac{b + a \cos [c + d x]}{a + b}} \right) - \\
& \frac{2 (A b - a B) \sin [c + d x]}{3 (a^2 - b^2) d \sqrt{\cos [c + d x]} (a + b \sec [c + d x])^{3/2}} - \\
& \frac{2 (5 a^2 A b - A b^3 - 2 a^3 B - 2 a b^2 B) \sin [c + d x]}{3 a (a^2 - b^2)^2 d \sqrt{\cos [c + d x]} \sqrt{a + b \sec [c + d x]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\sqrt{\operatorname{Cos}[c + d x]} (a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Problem 632: Unable to integrate problem.

$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\operatorname{Cos}[c + d x]^{3/2} (a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 329 leaves, 10 steps):

$$\begin{aligned} & - \frac{2 (A b - a B) \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right]}{3 a (a^2 - b^2) d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}} - \\ & \left( 2 (3 a^2 A + A b^2 - 4 a b B) \sqrt{\operatorname{Cos}[c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), \frac{2 a}{a + b}\right] \sqrt{a + b \operatorname{Sec}[c + d x]} \right) / \\ & \left( 3 a (a^2 - b^2)^2 d \sqrt{\frac{b + a \operatorname{Cos}[c + d x]}{a + b}} \right) + \frac{2 a (A b - a B) \operatorname{Sin}[c + d x]}{3 b (a^2 - b^2) d \sqrt{\operatorname{Cos}[c + d x]} (a + b \operatorname{Sec}[c + d x])^{3/2}} + \\ & \frac{2 (2 a^2 A b + 2 A b^3 + a^3 B - 5 a b^2 B) \operatorname{Sin}[c + d x]}{3 b (a^2 - b^2)^2 d \sqrt{\operatorname{Cos}[c + d x]} \sqrt{a + b \operatorname{Sec}[c + d x]}} \end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\operatorname{Cos}[c + d x]^{3/2} (a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Problem 633: Unable to integrate problem.

$$\int \frac{A + B \operatorname{Sec}[c + d x]}{\operatorname{Cos}[c + d x]^{5/2} (a + b \operatorname{Sec}[c + d x])^{5/2}} dx$$

Optimal (type 4, 399 leaves, 14 steps):

$$\begin{aligned}
& \frac{2 (A b - a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right]}{3 b \left(a^2 - b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
& \frac{2 B \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2} (c+d x), \frac{2 a}{a+b}\right]}{b^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
& \left(2 \left(4 A b^3 + 3 a^3 B - 7 a b^2 B\right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), \frac{2 a}{a+b}\right] \sqrt{a+b \sec [c+d x]}\right) / \\
& \left(3 b^2 \left(a^2 - b^2\right)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}}\right) + \frac{2 a (A b - a B) \sin [c+d x]}{3 b \left(a^2 - b^2\right) d \cos [c+d x]^{3/2} \left(a+b \sec [c+d x]\right)^{3/2}} - \\
& \frac{2 a \left(4 A b^3 + 3 a^3 B - 7 a b^2 B\right) \sin [c+d x]}{3 b^2 \left(a^2 - b^2\right)^2 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}}
\end{aligned}$$

Result (type 8, 37 leaves):

$$\int \frac{A + B \sec [c + d x]}{\cos [c + d x]^{5/2} (a + b \sec [c + d x])^{5/2}} dx$$

**Problem 634:** Attempted integration timed out after 120 seconds.

$$\int \frac{A + B \sec [c + d x]}{\cos [c + d x]^{7/2} (a + b \sec [c + d x])^{5/2}} dx$$

Optimal (type 4, 526 leaves, 15 steps):

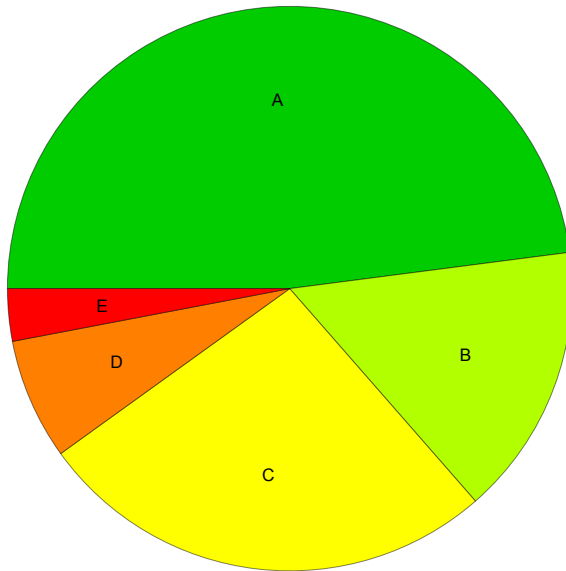
$$\begin{aligned}
 & - \frac{(2 a A b - 5 a^2 B + 3 b^2 B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{3 b^2\left(a^2-b^2\right) d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \frac{(2 A b - 5 a B) \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \operatorname{EllipticPi}\left[2, \frac{1}{2}(c+d x), \frac{2 a}{a+b}\right]}{b^3 d \sqrt{\cos [c+d x]} \sqrt{a+b \sec [c+d x]}} + \\
 & \left( \left( 6 a^3 A b - 14 a A b^3 - 15 a^4 B + 26 a^2 b^2 B - 3 b^4 B \right) \sqrt{\cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), \frac{2 a}{a+b}\right] \right. \\
 & \quad \left. \sqrt{a+b \sec [c+d x]} \right) / \left( 3 b^3\left(a^2-b^2\right)^2 d \sqrt{\frac{b+a \cos [c+d x]}{a+b}} \right) + \\
 & \frac{2 a(A b - a B) \sin [c+d x]}{3 b\left(a^2-b^2\right) d \cos [c+d x]^{5 / 2}(a+b \sec [c+d x])^{3 / 2}} + \\
 & \frac{2 a\left(2 a^2 A b - 6 A b^3 - 5 a^3 B + 9 a b^2 B\right) \sin [c+d x]}{3 b^2\left(a^2-b^2\right)^2 d \cos [c+d x]^{3 / 2} \sqrt{a+b \sec [c+d x]}} - \\
 & \frac{\left(6 a^3 A b - 14 a A b^3 - 15 a^4 B + 26 a^2 b^2 B - 3 b^4 B\right) \sqrt{a+b \sec [c+d x]} \sin [c+d x]}{3 b^3\left(a^2-b^2\right)^2 d \sqrt{\cos [c+d x]}}
 \end{aligned}$$

Result (type 1, 1 leaves):

???

## Summary of Integration Test Results

634 integration problems



- A - 304 optimal antiderivatives
- B - 99 more than twice size of optimal antiderivatives
- C - 168 unnecessarily complex antiderivatives
- D - 44 unable to integrate problems
- E - 19 integration timeouts