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http://www.dsi.uclm.es/investigacion/dect/FLOPERpage.htm

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#### **Multi-Adjoint Logic Programs**

**FUZZY LOGIC PROGRAMMING** 



**FUZZY LOGIC** 



LOGIC PROGRAMMING

#### **Multi-Adjoint Logic Programs**

| p(X)                            | <pre><pre>od</pre></pre>                            | q(X,Y) &godel $r(Y)$ | with 0.8 |
|---------------------------------|---|----------------------|----------|
| q(a, Y)                         | <pre><pre>od</pre></pre>                            | s(Y)                 | with 0.7 |
| q(b, Y)                         | <luka< td=""><td>r(Y)</td><td>with 0.8</td></luka<> | r(Y)                 | with 0.8 |
| $r(\underline{\hspace{0.1cm}})$ |   |                      | with 0.6 |
| s(b)                            |   |                      | with 0.9 |

#### **Multi-Adjoint Logic Programs**

```
q(X,Y) &godel r(Y) with 0.8
p(X)
         od
q(a, Y)    s(Y)
                                          with 0.7
q(b, Y) < luka r(Y)
                                          with 0.8
                                          with 0.6
r(\underline{\phantom{a}})
                                          with 0.9
s(b)
```

$$p(X,TV0)$$
 :  $-q(X,Y,TV1), r(Y,TV2), and\_godel(TV1,TV2,TV3)$   $and\_prod(0.8,TV3,TV0).$ 

```
q(a, Y, TV0) :- s(Y, TV1), and\_prod(0.7, TV1, TV0).
q(b, Y, TV0) : - r(Y, TV1), and\_luka(0.8, TV1, TV0).
r(\_, 0.6).
```

s(b, 0.9).

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 The system has been implemented with approximately 300 Sicstus Prolog clauses and it uses DCG's for defining parsing predicates

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- The system has been implemented with approximately 300 Sicstus Prolog clauses and it uses DCG's for defining parsing predicates
- The prelude.pl defines default aggregators
- Options for...
  - Loading a prolog file with extension ".pl"
  - Parsing a ".fpl" fuzzy program. The generated
     Prolog code is also asserted in the system
  - Saving the generated Prolog code into a ".pl" file
  - Listing both the fuzzy and Prolog code
  - Clean, Stop and Quit

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...... by using a PROLOG-based, low level representation of the fuzzy code......

- New DEBUGGING options.....
  - Depth. Fix the maximum evaluation level
  - Tree. Generate the associated evaluation tree (more precise information on computations)
  - Transformations. Open menu for F/U, PE,...

#### **Debugging capabilities of FLOPER**

```
p(X) < prod q(X,Y) \& godel r(Y) with 0.8
p(X,TV0) := q(X,Y,TV1),r(Y,TV2),
  and_g(TV1,TV2,TV3),and_p(0.8,TV3,TV0).
rule(number(1),
     head(atom(pred(p,1),[var('X')])),
     impl(prod),body(and(godel, 2,
     [atom(pred(q,2),[var('X'),var('Y')]),
      atom(pred(r,1),[var('Y')]))),
     td(0.8)).
```

#### **Debugging capabilities of FLOPER**

Trace 1: solutions in presence of infinite branches

R1: p(X) prod q(X) with 0.9.
R2: p(X) godel r(X) with 0.8.

R3: q(X) < luka q(X) with 0.7. R4: r(a) with 0.6.

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• TREE: Execution tree with depth 4 for goal p(a)

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Trace 1: solutions in presence of infinite branches

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#### **Debugging capabilities of FLOPER**

Trace 2: solutions even with unsuccessful atoms

p(a) < prod @aver(1, p(b)) with 0.9

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Trace 2: solutions even with unsuccessful atoms

... remember that the associated Prolog clause is:

```
\begin{aligned} p(a, TV0) : - & \mathbf{p}(\mathbf{b}, \underline{TV1}), agr\_aver(1, \underline{TV1}, \underline{TV2}), \\ & and\_prod(0.9, \underline{TV2}, TV0). \end{aligned}
```

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Trace 2: solutions even with unsuccessful atoms

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#### **Conclusions and Further Research**

Fuzzy Logic Programming LANGUAGE:
 The Multi-Adjoint Logic Programming approach

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- Fuzzy Logic Programming LANGUAGE:
   The Multi-Adjoint Logic Programming approach
- FLOPER provides two implementation techniques
   Compilation to Prolog code [RUN]: simplicity,
   transparency, complete evaluation of goals
   Low level representation [DEBUG]: detailed
   data, unfolding trees, powerful manipulations

#### **Conclusions and Further Research**

- Fuzzy Logic Programming LANGUAGE:
   The Multi-Adjoint Logic Programming approach
- FLOPER provides two implementation techniques
   Compilation to Prolog code [RUN]: simplicity,
   transparency, complete evaluation of goals
   Low level representation [DEBUG]: detailed
   data, unfolding trees, powerful manipulations
- More efforts are needed for increasing expressivity (new lattices, more computation rules, graphical interface) and including transformation techniques (optimization, specialization, reductants....)

```
SICStus 3.12.1 (x86-win32-nt-4): Mon Apr 18 20:03:40 WEST 2005
File Edit Flags Settings Help
                  ****
                                                   *****
                          PROGRAM
                                      MENU
**
            --> Parse/load a fuzzy prolog file (.fpl)
                                                               **
     parse
            --> Parse/load/save a fuzzy prolog file.
                                                               **
     save
**
     load --> Consult a prolog file (.pl).
                                                               **
                                                               **
**
     list --> Displays the last loaded clauses.
     clean --> Clean the database
                                                               **
                  ****
                          GOAL
                                   MENU
                                                   *****
     intro --> Introduce a new goal (between quotes).
**
                                                               **
**
            --> Execute a goal completely
                                                               **
     run
     depth --> Set the maximum level of execution trees
**
                                                                **
     tree
            --> Generate a partial execution tree
                                                               **
                  ****
                          TRANSFORMATTON MENU
                                                   *****
%%
             --> Partial evaluation
                                                               %%
    pe
%%
            --> Fold/Unfold Transformations
    fu
            --> Reductants Calculus
    red
                                                               **
                --> Stop the execution of the parser.
     stop
     quit
                --> Exit to desktop.
                                                               **
                ICCMSE07
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                                           SICStus 3.12.1 (... ES < 🧼 🦚 👘 🔁 🕪 15:32
```



```
File Edit Flags Settings Help
                                                                                                                                                                                                                                                                         %%
  %% red
                                                       --> Reductants Calculus
                                                                   --> Stop the execution of the parser.
                   quit
                                                                   --> Exit to desktop.
   >> tree.
   R0 < &godel(p(X),r(a)), {} >
                     R1 < godel(prod(0.8, godel(q(X1,Y1),r(Y1))),r(a)), {X/X1} >
                                       R2 < &godel(&prod(0.8,&godel(&prod(0.7,s(Y7)),r(Y7))),r(a)), {X/a,X1/a,Y1/Y7} >
                                                          R5 < \ensuremath{$} < \ensuremath{$} godel(\ensuremath{$} prod(0.8, \ensuremath{$} godel(\ensuremath{$} prod(0.7,0.9),r(b))),r(a)), {X/a,X1/a,Y1/b,Y7/b} >
                                                                             R4 < godel(prod(0.8, godel(prod(0.7, 0.9), 0.6)), r(a)), \{X/a, X1/a, Y1/b, Y7/b, 19/b\} >
                                                                                                R4 < godel(prod(0.8, godel(prod(0.7, 0.9), 0.6)), 0.6), \{X/a, X1/a, Y1/b, Y7/b, 19/b, 24/a, Y1/b, Y1
                                       R3 < \ensuremath{\mathebox{\mathebox{$a$}}\ (%\lambda\), \(\pi_{\ensuremath{\mathebox{$a$}}\), \(\pi_{\ensuremath{\mathebox{$a$}}\}\)), \(\pi_{\ensuremath{\mathebox{$a$}}\}\}\)), \(\pi_{\ensuremath{\mathebox{$a$}}\}\)), \(\pi_{\ensuremath{\mathebox{$a$}}\}\)), \(\pi_{\ensuremath{\mathebox{$a$}}\}\)), \(\pi_{\ensuremath{\mathebox{$a$}}\}\), \(\pi_{\ensuremath{\mathebox{$a$}}\}\)), \(\pi_{\ensuremath{\mathebox{$a$}}\}\
                                                          R4 < \dot{$godel(\&prod(0.8,\&godel(\&luka(0.8,0.6),0.6)),r(a)), {X/b,X1/b,Y1/29,Y8/29}} >
                                                                             R4 < godel(prod(0.8, godel(kluka(0.8, 0.6), 0.6)), (x/b, x1/b, y1/29, y8/29, 34/a) >
                                                                                                                                                                                                                      *****
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