# Rule-based Agents, Compliance, and Intention Reconsideration in Defeasible Logic

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**Motivation**: So far research in MAS (cognitive agents) has overlooked intention reconsideration to achieve norm compliance

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  - Adding new rules to remove intentions from theory extensions
  - Removing intention rules remove intentions from theory extensions
- Properties and future work

$$(\textit{F}, \textit{R}^{\textbf{B}}, \textit{R}^{\textbf{O}}, \textit{R}^{\textbf{I}}, \succ)$$

An agent theory D is a structure

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- $\succ$  is an acyclic (superiority) relation over  $(R^{\mathbf{B}} \times R^{\mathbf{B}}) \cup (R^{\mathbf{I}} \times R^{\mathbf{I}}) \cup (R^{\mathbf{O}} \times R^{\mathbf{O}}).$

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 $MiddleEarth \rightarrow_{\mathbf{O}} DestroyRing$   $Mordor \Rightarrow_{\mathbf{I}} BackToShire$  $Nazgul \Rightarrow_{\mathbf{B}} Danger$ 

Different rules for each kind of modality; e.g.,

$$MiddleEarth \rightarrow_{\mathbf{O}} DestroyRing$$
  
 $Mordor \Rightarrow_{\mathbf{I}} BackToShire$   
 $Nazgul \Rightarrow_{\mathbf{B}} Danger$ 

• As in DL, different types of provability:

$$+\Delta^{\mathbf{O}}$$
 DestroyRing  $+\partial^{\mathbf{I}}$  BackToShire

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 Provability in an agent theory D is used for introducing modalities in the theory extension

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 Provability in an agent theory D is used for introducing modalities in the theory extension

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  $MiddleEarth$   
 $+\partial^{\mathbf{0}} DestroyRing$   $D \triangleright_{\mathbf{0}} DestroyRing$ 

Facts: Entrusted, Hobbit

```
Rules: r_1:OMordor \Rightarrow_{\mathbf{0}} DestroyRing r_2:RingBearer \Rightarrow_{\mathbf{0}} Mordor r_3:RingBearer \rightarrow_{\mathbf{I}} \negDestroyRing r_4:Entrusted \rightarrow_{\mathbf{B}} RingBearer r_5:Hobbit \Rightarrow_{\mathbf{0}} \negMordor
```

$$r_5 \succ r_2$$

Phase 1: Prove OMordor

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Rules:  $r_1$ :**O**Mordor  $\Rightarrow_{\mathbf{0}}$  DestroyRing  $r_2$ :RingBearer  $\Rightarrow_{\mathbf{0}}$  Mordor  $r_3$ :RingBearer  $\rightarrow_{\mathbf{I}}$   $\neg$ DestroyRing  $r_4$ :Entrusted  $\rightarrow_{\mathbf{B}}$  RingBearer  $r_5$ :Hobbit  $\Rightarrow_{\mathbf{0}}$   $\neg$ Mordor

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Phase 1: Prove OMordor Facts+ $r_4 + r_2$ 

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Phase 2: Attacks

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Superiority relation:

$$r_5 \succ r_2$$

Phase 1: Prove OMordor

 $Facts+r_4+r_2$ 

Phase 2: Attacks

 $Facts+r_5$ 

Phase 3: Rebut attacks

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 $r_5$  weaker than  $r_2$ 

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Facts $+r_4+r_3$ 

Phase 2: Attacks

No argument

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See above

Phase 1: Prove I¬DestroyRing

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Phase 2: Attacks

No argument

Phase 3: Rebut attacks

Not needed



# **Is Frodo Compliant?**

Suppose we have  $\mathbf{O}b$ 

Suppose we have **O**b

• Case 1—unchangeable intentions:

$$\mathbf{I}b \qquad \mathbf{I}\neg b \qquad \qquad (1)$$

#### Suppose we have **O**b

• Case 1—unchangeable intentions:

$$\mathbf{I}b \qquad \mathbf{I}\neg b \qquad (1)$$

• Case 2—strong intentions:

$$r_1: a \rightarrow_{\mathsf{I}} b \qquad \qquad r_2: c \rightarrow_{\mathsf{I}} \neg b \qquad \qquad (2)$$

#### Suppose we have $\mathbf{O}b$

• Case 1—unchangeable intentions:

$$\mathbf{I}b \qquad \mathbf{I}\neg b \qquad \qquad (1)$$

• Case 2—strong intentions:

$$r_1: a \rightarrow_{\mathsf{I}} b \qquad \qquad r_2: c \rightarrow_{\mathsf{I}} \neg b \qquad \qquad (2)$$

• Case 3—weak intentions:

$$r_1: a \Rightarrow_{\mathsf{I}} b \qquad \qquad r_2: c \Rightarrow_{\mathsf{I}} \neg b$$
 (3)

#### Suppose we have $\mathbf{O}b$

• Case 1—unchangeable intentions:

$$\mathbf{I}b \qquad \mathbf{I}\neg b \qquad \qquad (1)$$

• Case 2—strong intentions:

$$r_1: a \rightarrow_{\mathsf{I}} b \qquad \qquad r_2: c \rightarrow_{\mathsf{I}} \neg b \qquad \qquad (2)$$

• Case 3—weak intentions:

$$r_1: a \Rightarrow_{\mathsf{I}} b$$
  $r_2: c \Rightarrow_{\mathsf{I}} \neg b$   $r_2 \succ r_1$  (3)

$$F = \{a, b\}$$

$$R = \{r_1 : a \rightarrow_{l} \neg c,$$

$$r_2 : b \Rightarrow_{0} c,$$

$$r_3 : b \rightarrow_{l} d,$$

$$r_4 : d, a \rightarrow_{l} \neg c\}$$

$$\succ = \emptyset$$

$$F = \{a, \mathbf{l}b\}$$

$$R = \{r_1 : a \to_{\mathbf{l}} \neg c,$$

$$r_2 : \mathbf{l}b \Rightarrow_{\mathbf{0}} c,$$

$$r_3 : \mathbf{l}b \to_{\mathbf{l}} d,$$

$$r_4 : \mathbf{l}d, a \to_{\mathbf{l}} \neg c\}$$

$$\succ = \emptyset$$

Intention reconsideration here amounts, e.g., to

$$R - \{r_1, r_4\}$$

$$F = \{a, \mathbf{I}d\}$$

$$R = \{r_1 : a \to_{\mathbf{I}} b,$$

$$r_2 : \mathbf{I}b \Rightarrow_{\mathbf{O}} c,$$

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$$\succ = \emptyset$$

```
F = \{a, \mathbf{I}d\}
R = \{r_1 : a \rightarrow_{\mathbf{I}} b,
r_2 : \mathbf{I}b \Rightarrow_{\mathbf{O}} c,
r_3 : \mathbf{I}d \Rightarrow_{\mathbf{I}} \neg c, \}
 \succ = \emptyset
```

$$F = \{a, \frac{\mathsf{I}d}{\mathsf{I}d}\}$$

$$R = \{r_1 : a \to_{\mathsf{I}} b, r_2 : \mathsf{I}b \Rightarrow_{\mathsf{O}} c, r_3 : \mathsf{I}d \Rightarrow_{\mathsf{I}} \neg c, \}$$

$$F = \emptyset$$

Intention reconsideration here amounts to

$$\begin{split} D_{\mathbf{I}p_1,\dots\mathbf{I}p_n}^- &= \begin{cases} D & \text{if } \mathbf{I}p_1,\dots,\mathbf{I}p_n \text{ not provable} \\ (F,R^{\mathbf{O}}R^{\mathbf{I}'},\succ') & \text{otherwise} \end{cases} \\ & \text{where} \\ R^{\mathbf{I}'} &= R^{\mathbf{I}} \cup \{s: \mathbf{I}p_1,\dots,\mathbf{I}p_{i-1},\mathbf{I}p_{i+1},\dots,\mathbf{I}p_n \leadsto_{\mathbf{I}} \sim p_i | \\ 1 \leq i \leq n \} \\ & \succ' = \succ - \{r \succ s \mid r \in R^{\mathbf{I}'} - R^{\mathbf{I}} \}. \end{split}$$

$$F = \{a, \mathbf{Id}\}\$$

$$R = \{r_1 : a \rightarrow_{\mathbf{I}} b,$$

$$r_2 : \mathbf{I}b \Rightarrow_{\mathbf{O}} c,$$

$$r_3 : \mathbf{Id} \Rightarrow_{\mathbf{I}} \neg c, r_4 : \rightsquigarrow_{\mathbf{I}} c\}$$

$$\succ = \emptyset$$

Intention reconsideration here amounts to

$$D_{\mathbf{I}p_{1},\dots\mathbf{I}p_{n}}^{-} = \begin{cases} D & \text{if } \mathbf{I}p_{1},\dots,\mathbf{I}p_{n} \text{ not provable} \\ (F,R^{\mathbf{O}}R^{\mathbf{I}'},\succ') & \text{otherwise} \end{cases}$$

$$\text{where}$$

$$R^{\mathbf{I}'} = R^{\mathbf{I}} \cup \{s: \mathbf{I}p_{1},\dots,\mathbf{I}p_{i-1},\mathbf{I}p_{i+1},\dots,\mathbf{I}p_{n} \leadsto_{\mathbf{I}} \sim p_{i} | 1 \leq i \leq n \}$$

$$\succ' = \succ - \{r \succ s \mid r \in R^{\mathbf{I}'} - R^{\mathbf{I}} \}.$$

 A similar procedure can be devised to derive new intentions, i.e., by adding new defeasible rules (AGM revision)

$$F = \{a\}$$

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 However, all the above operations apply only to the last rule of the reasoning chains supporting "illegal" intentions

```
F = \{ \textbf{O}\textit{GoToSpain}, \textbf{I}\textit{Sarsuela}, \textit{Hungry} \}
R = \{ r_1 : \textbf{I}\textit{Sarsuela} \rightarrow_{\textbf{I}} \textit{GoToBarcelona},
r_2 : \textbf{I}\textit{GoToBarcelona} \rightarrow_{\textbf{I}} \textit{GoToSpain},
r_3 : \rightsquigarrow_{\textbf{O}} \neg \textit{EatModerately},
r_4 : \textbf{I}\textit{Sarsuela} \Rightarrow_{\textbf{O}} \textit{EatModerately},
r_5 : \textit{Hungry} \Rightarrow_{\textbf{I}} \neg \textit{EatModerately},
r_6 : \Rightarrow_{\textbf{I}} \neg \textit{EatModerately},
r_7 : \textbf{I} \neg \textit{EatModerately}, \textbf{I}\textit{Sarsuela} \Rightarrow_{\textbf{O}} \textit{Abstinence} \}
\succ = \{ r_3 \succ r_4 \}
```

```
F = \{ \textbf{O} \textit{GoToSpain}, \textbf{I} \textit{Sarsuela}, \textit{Hungry} \} 
R = \{ r_1 : \textbf{I} \textit{Sarsuela} \rightarrow_{\textbf{I}} \textit{GoToBarcelona}, 
r_2 : \textbf{I} \textit{GoToBarcelona} \rightarrow_{\textbf{I}} \textit{GoToSpain}, 
r_3 : \rightsquigarrow_{\textbf{O}} \neg \textit{EatModerately}, 
r_4 : \textbf{I} \textit{Sarsuela} \Rightarrow_{\textbf{O}} \textit{EatModerately}, 
r_5 : \textit{Hungry} \Rightarrow_{\textbf{I}} \neg \textit{EatModerately}, 
r_6 : \Rightarrow_{\textbf{I}} \neg \textit{EatModerately}, 
r_7 : \textbf{I} \neg \textit{EatModerately}, \textbf{I} \textit{Sarsuela} \Rightarrow_{\textbf{O}} \textit{Abstinence} \} 
 \succ = \{ r_3 \succ r_4 \}
```

 $+ \Delta^{I}[ISarsuela][r_{1}]GoToBarcelona + \Delta^{I}[ISarsuela][r_{1}][r_{2}]GoToSpain$ 

```
F = \{ \mathbf{O} GoToSpain, \mathbf{I} Sarsuela, Hungry \}
R = \{r_1 : ISarsuela \rightarrow_I GoToBarcelona,
          r_2: IGoToBarcelona \rightarrow_1 GoToSpain,
          r_3: \leadsto_{\mathbf{0}} \neg EatModeratelv.
          r_4: ISarsuela \Rightarrow_{\mathbf{0}} EatModerately.
          r_5: Hungry \Rightarrow_{\mathbf{I}} \neg EatModerately,
          r_6:\Rightarrow_{\mathbf{I}} \neg EatModerately.
          r_7: \mathbf{I} \neg EatModerately, \mathbf{I}Sarsuela \Rightarrow_{\mathbf{0}} Abstinence
\succ = \{r_3 \succ r_4\}
```

```
+\Delta^{\mathbf{I}}[\mathbf{I}Sarsuela][r_1]GoToBarcelona\\ +\partial^{\mathbf{I}}[\mathbf{I}Sarsuela][r_1][r_2]GoToSpain\\ +\partial^{\mathbf{I}}[\mathbf{I}Sarsuela][r_4]EatModerately\\ +\partial^{\mathbf{I}}[r_6]\neg EatModerately
```

```
F = \{ \mathbf{O} GoToSpain, \mathbf{I} Sarsuela, Hungry \}
R = \{r_1 : ISarsuela \rightarrow_I GoToBarcelona,
         r_2: IGoToBarcelona \rightarrow_1 GoToSpain,
         r_3: \leadsto_{\mathbf{0}} \neg EatModerately.
         r_4: ISarsuela \Rightarrow_{\mathbf{0}} EatModerately.
         r_5: Hungry \Rightarrow_1 \neg EatModerately,
         r_6 : \Rightarrow_{\mathbf{I}} \neg EatModerately,
         r_7: \mathbf{I} \neg EatModerately, \mathbf{I} Sarsuela \Rightarrow_{\mathbf{0}} Abstinence
\succ = \{r_3 \succ r_4\}
```

```
+\Delta^{\mathbf{I}}[\mathbf{I}Sarsuela][r_1]GoToBarcelona\\ +\partial^{\mathbf{O}}[\mathbf{I}Sarsuela][r_4]EatModerately\\ +\partial^{\mathbf{I}}[r_6]\neg EatModerately\\ +\partial^{\mathbf{O}}[Hungry][r_5,\mathbf{I}Sarsuela][r_7]Abstinence\\ +\partial^{\mathbf{O}}[r_6,\mathbf{I}Sarsuela]Abstinence\\ +\partial^{\mathbf{O}}[r_6,\mathbf{I}Sarsuela]Abstinence
```

```
F = \{ \mathbf{O} GoToSpain, \mathbf{I} Sarsuela, Hungry \}
R = \{r_1 : ISarsuela \rightarrow_I GoToBarcelona,
         r_2: IGoToBarcelona \rightarrow_1 GoToSpain,
         r_3: \leadsto_{\mathbf{0}} \neg EatModerately.
         r_4: ISarsuela \Rightarrow_{\mathbf{0}} EatModerately.
         r_5: Hungry \Rightarrow_1 \neg EatModerately,
         r_6 : \Rightarrow_{\mathbf{I}} \neg EatModerately,
         r_7: \mathbf{I} \neg EatModerately, \mathbf{I} Sarsuela \Rightarrow_{\mathbf{0}} Abstinence
\succ = \{r_3 \succ r_4\}
```

```
+\Delta^{\mathbf{I}}[\mathbf{I}Sarsuela][r_1]GoToBarcelona\\ +\partial^{\mathbf{O}}[\mathbf{I}Sarsuela][r_4]EatModerately\\ +\partial^{\mathbf{I}}[r_6]\neg EatModerately\\ +\partial^{\mathbf{O}}[Hungry][r_5,\mathbf{I}Sarsuela][r_7]Abstinence\\ +\partial^{\mathbf{O}}[r_6,\mathbf{I}Sarsuela]Abstinence\\ +\partial^
```

# Is Nino compliant?

# Reconsidering intentions: strong intentions

#### Definition (Rule Removal with paths)

Let  $D = (F, R^0, R^I, \succ)$  be an agent theory. For each  $r \in R^0_{\mathrm{sd}}$  such that the paths  $\mathcal{L}_1, \dots \mathcal{L}_n$  such that

$$D \vdash +\Delta^{\mathsf{I}} \mathcal{L}_1 p, \ldots, D \vdash +\Delta^{\mathsf{I}} \mathcal{L}_n p$$

and

$$D \vdash +\partial^{\mathbf{O}} \mathcal{Y} \neg p$$

 $D_{-X}$  is such that

- $X = \{w_1, \dots, w_m\}$  is the smallest set of strict rules in  $R^{\mathbf{I}}$  such that, for each  $k \in \{1, \dots, n\}$ , there is at least a  $w_j \in X$  that occurs in  $\mathcal{L}_k$ ,
- $R_{-X}^{I} = R^{I} X$ , and
- $F_{-X} = F$ ,  $R_{-X}^{0} = R^{0}$ , and  $\succ_{-X} = \succ$ .

#### Definition (Contraction with paths)

Let  $D=(F,R^{\mathbf{0}},R^{\mathbf{I}},\succ)$  be an agent theory. For each  $r\in R^{\mathbf{0}}_{\mathrm{sd}}$  such that the paths  $\mathcal{L}_1,\ldots\mathcal{L}_n$  such that

$$D \vdash +\partial^{\mathsf{I}} \mathcal{L}_{1} p, \dots, D \vdash +\partial^{\mathsf{I}} \mathcal{L}_{n} p$$

and

$$D \vdash +\partial^{\mathbf{O}} \mathcal{Y} \neg p$$

the theory the theory  $D_{\flat p} = (F, R^{\mathbf{0}}, R^{\mathbf{I}'}, \succ')$  is such that

- (i)  $R^{\mathbf{I}'} = R^{\mathbf{I}} \cup \{s : \leadsto_{\mathbf{I}} \sim q\} \cup \{t : \leadsto_{\mathbf{I}} \sim x\},$
- (ii)  $\succ'=\succ -[\{r_k \succ s | r_k \in R^{\mathbf{I}}[q], r_k \text{ occurs in } \mathcal{L}_k \ \forall k \in \{1, \dots, n\}\} \cup \{w \succ t \mid w \text{ is rebutted and is such that its head is } p \text{ or } w \text{ occurs in } \mathcal{L}_k \ \forall k \in \{1, \dots, n\}\}].$

$$F = \{Ib\}$$

$$R = \{r_1 : \Rightarrow_I a,$$

$$r_2 : Ia \Rightarrow_I \neg c,$$

$$r_3 : Ib \Rightarrow_O c,$$

$$r_4 : Ia \Rightarrow_I p,$$

$$r_5 : \Rightarrow_I \neg p,$$

$$r_6 : I \neg p \Rightarrow_I \neg c\}$$

$$\Rightarrow = \{r_5 \succ r_4\}$$

$$+ \partial^{\mathbf{O}}[Ib][r_3]c$$

$$+ \partial^{\mathbf{I}}[r_1][r_2] \neg c$$

$$- \partial^{\mathbf{I}}[-r_5][-r_6] \neg c$$

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- The role of reparative obligations?
- Complexity?
- Revise priorities and not rules?

# Thanks!