

# Incomplete and uncertain data handling in context-aware rule-based systems with modified certainty factors algebra

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<http://geist.agh.edu.pl>



# Outline I

- 1 Introduction
- 2 Motivation
- 3 Proposed solution
- 4 Dynamics of uncertainty
- 5 Simple use case scenario
- 6 Summary and future work

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# Mobile context-aware systems (mCAS)

## Context

- Where you are, who you are with, what resources are nearby (Schillit)
- Any information that can be used to characterize the situation of an entity (Dey)
- Individuality, activity, location, time, relations (Zimmerman)
- Set of variables that may be of interest for an agent and that influence its actions (Bolchini)

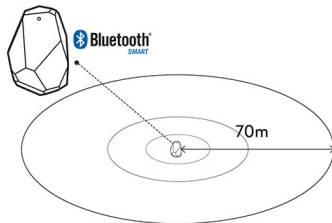
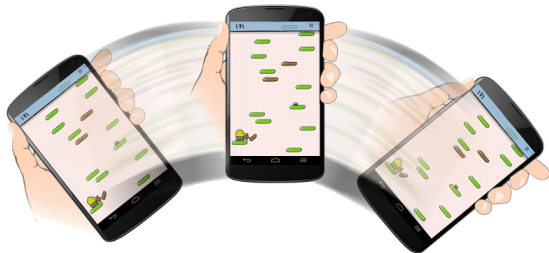
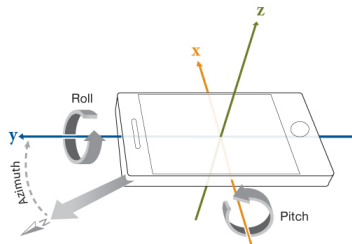
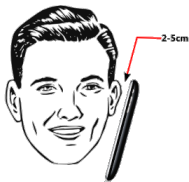
## Aware

- Artificial intelligence methods

## Systems

- Intelligent homes, intelligent cars, robotics
- Ambient intelligence, pervasive environments, ubiquitous computing
- Mobile computing (location aware mobile applications)
- Intelligent software (contextual advertising, etc.)

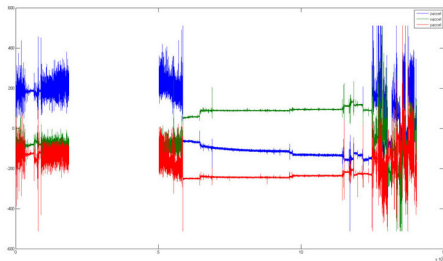
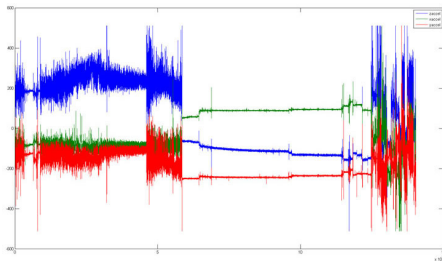
# Mobile environment and uncertainty



# Different types of uncertainty

## High-level classification

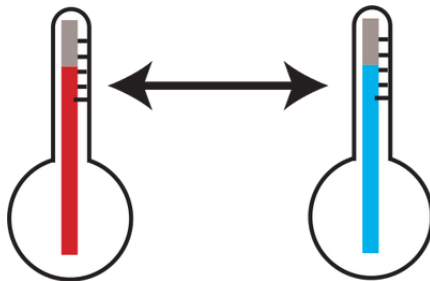
- 1 Uncertainty due to lack of knowledge – that comes from incomplete information both at the model level or if the information is not provided by the sensors,
- 2 Uncertainty due to lack of semantic precision – that may appear due to semantic mismatch in the notion of the information,
- 3 Uncertainty due to lack of machine precision – which covers machine sensors imprecision and ambiguity.



# Different types of uncertainty

## High-level classification

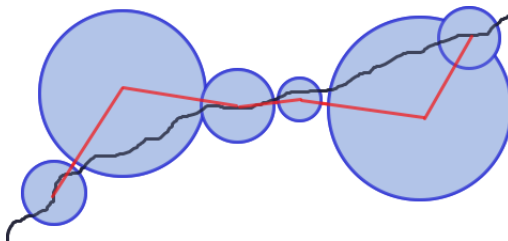
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# Different uncertainty modelling and handling mechanisms

	Uncertainty source			Implementation effort
	Lack of knowledge	Semantic imprecision	Machine imprecision	
Probabilistic	●	○	●	High
Fuzzy Logic	○	●	●	Medium
Certainty Factors	●	○	●	Low
Machine learning	●	○	●	High

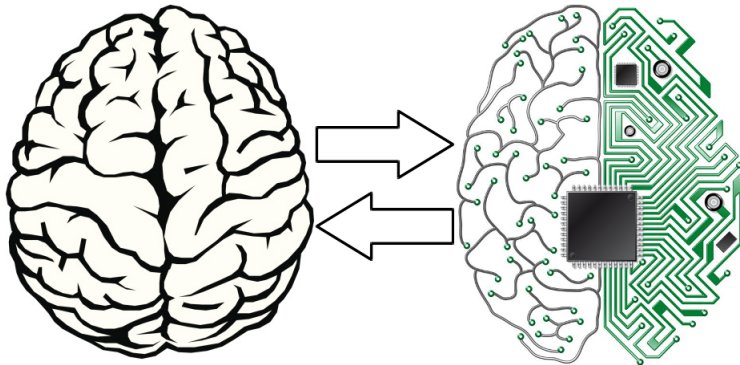
**Table :** Comparison of uncertainty handling mechanisms. Full circles represent full support, whereas empty circles represent low or no support.

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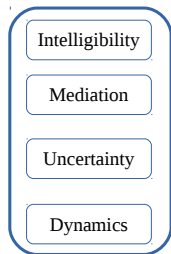
## Nature of mCAS

- mCAS are build usually as a user centric systems
- Intelligibility is very important as it may improve users trust to the system
- Mediation may help resolve ambiguity
- The uncertainty is dynamic and such a dynamic should be modelled

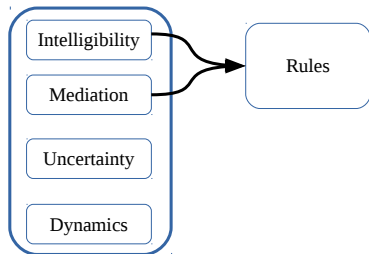


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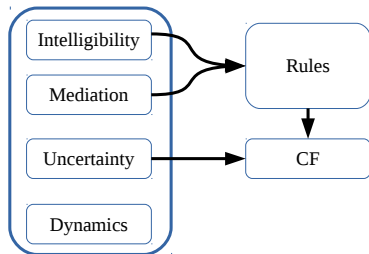
# Overall idea



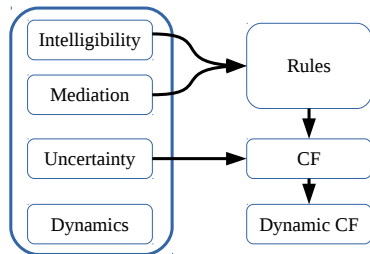
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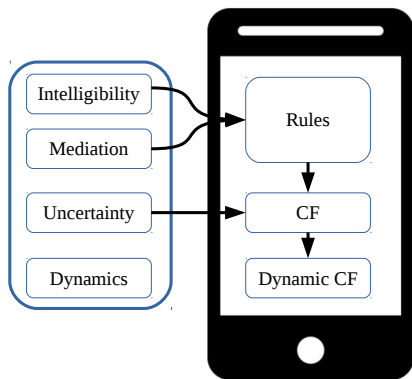


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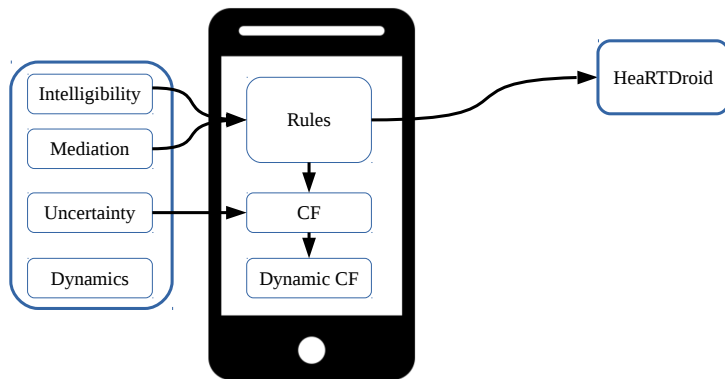




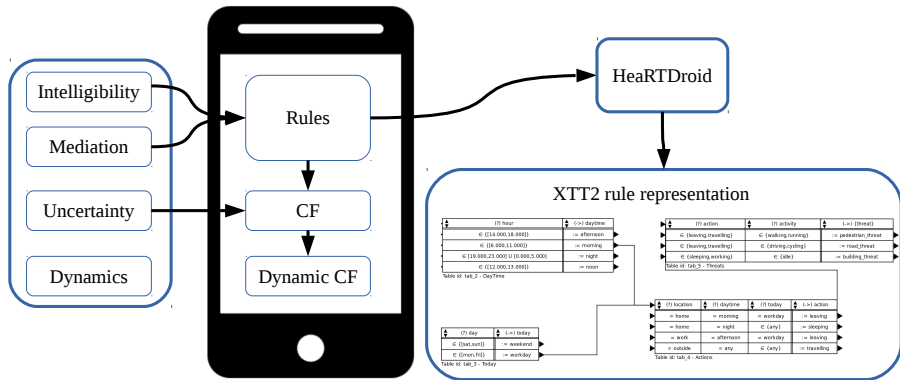
# Overall idea



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# ALSV(FD) logic

## XTT2 rule in ALSV(FD) logic

$$(A_i \propto d_i) \wedge (A_j \propto d_j) \wedge \dots (A_m \propto V_m) \wedge (A_n \propto V_n) \longrightarrow RHS$$

Syntax	Interpretation	Relation
$A_i = d_i$	value of $A_i$ is precisely defined as $d_i$	eq
$A_i \in V_i$	value of $A_i$ is in $V_i$	in
$A_i \neq d_i$	shorthand for $A_i \in (\mathbb{D}_i \setminus \{d_i\})$	neq
$A_i \notin V_i$	shorthand for $A_i \in (\mathbb{D}_i \setminus V_i)$	notin

**Table :** Formulaes for simple attributes

Syntax	Interpretation	Relation
$A_i = V_i$	$A_i$ equal $V_i$	eq
$A_i \neq V_i$	$A_i$ does not equal $V_i$	neq
$A_i \subseteq V_i$	$A_i$ is a subset $V_i$	subset
$A_i \supseteq V_i$	$A_i$ is a superset $V_i$	supset
$A_i \sim V_i$	$A_i$ has non-empty intersection with $V_i$	sim
$A_i \not\sim V_i$	$A_i$ has empty intersection with $V_i$	notsim

**Table :** Formulaes for generalized attributes

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**Table :** Formulae for simple attributes

### Example for simple attribute

*if*(*activity* = *driving*)  $\rightarrow$   
*bluetoothHandset* = *on*

### Uncertainty in such data

*activity* = *walking*(30%)

*activity* = *cycling*(50%)

*activity* = *driving*(20%)

# ALSV(FD) logic

## XTT2 rule in ALSV(FD) logic

$$(A_i \propto d_i) \wedge (A_j \propto d_j) \wedge \dots (A_m \propto V_m) \wedge (A_n \propto V_n) \longrightarrow RHS$$

### Example for generalised attribute

*if* (*language*  $\sim \{en, cz\}$ )  $\rightarrow$   
*recommendConference* = *RuleML*

### Uncertainty in such data

*language* =  
 $\{pl(100\%), en(80\%), cz(2\%)\}$

Syntax	Interpretation	Relation
$A_i = V_i$	$A_i$ equal $V_i$	eq
$A_i \neq V_i$	$A_i$ does not equal $V_i$	neq
$A_i \subseteq V_i$	$A_i$ is a subset $V_i$	subset
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**Table :** Formulae for generalized attributes

# Certainty Factors algebra

## Basic notation

- Rule in CF algebra is represented according to formulae:

$$condition_1 \wedge condition_2 \wedge \dots \wedge condition_k \rightarrow conclusion \quad (1)$$

- Each of the elements of the formulae from equation 1 above can have assigned a certainty factor  $cf(element) \in [-1; 1]$
- CF of a conditional part of a rule is determined by the formulae:

$$cf(condition_1 \wedge \dots \wedge condition_k) = \min_{i \in 1 \dots k} cf(condition_i)$$

- Certainty factor of conclusion  $C$  of a single  $i$ -th rule is calculated according to a formulae:

$$cf_i(C) = cf(condition_1 \wedge \dots \wedge condition_k) * cf(rule) \quad (2)$$

# Cumulative and disjunctive rules

## Disjunctive rules

Disjunctive rules have the same conclusions but are conditionally dependent (i.e. value of any of the conditions determine values of other rules conditions).

$$cf(C) = \max_{i \in 1 \dots k} \{cf_i(C)\} \quad (3)$$

## Cumulative rules

Cumulative rules have the same conclusions and have independent conditions (i.e. value of any of the conditions does not determine values of other rules conditions).

$$cf(C) = \begin{cases} cf_i(C) + cf_j(C) - cf_i(C) * cf_j(C) & \text{if } cf_i(C) \geq 0, cf_j(C) \geq 0 \\ cf_i(C) + cf_j(C) + cf_i(C) * cf_j(C) & \text{if } cf_i(C) \leq 0, cf_j(C) \leq 0 \\ \frac{cf_i(C) + cf_j(C)}{1 - \min\{|cf_i(C)|, |cf_j(C)|\}} & \text{if } cf_i(C)cf_j(C) \notin \{-1, 0\} \end{cases} \quad (4)$$



## Disjunctive rules

In particular the formula  $A_i \in V_i$  can be translated into a form:

$$(A_i = V_i^0) \vee (A_i = V_i^1) \vee \dots \vee (A_i = V_i^k)$$

where the  $V_i^k$  is a  $k$ -th element from a subset  $V_i$  of domain  $D_i$ , and  $A_i$  is a simple attribute.

## Cumulative rules

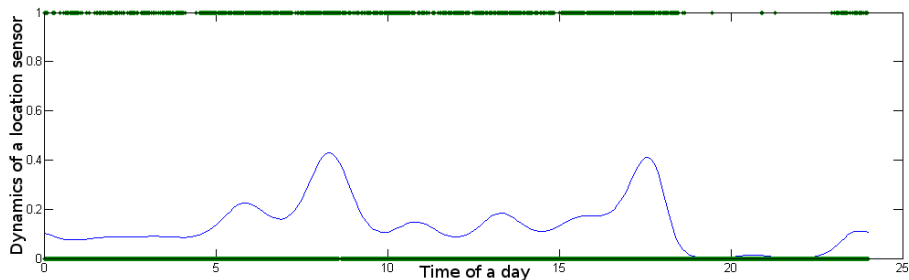
For the general attribute  $A_i$ , the formulae of a form  $A_i \sim V_i$  can be translated into:

$$(A_i^0 \in V_i) \vee (A_i^1 \in V_i) \vee \dots \vee (A_i^k \in V_i)$$

where  $A_i^k$  is a  $k$ -th element of a set representing by the general attribute  $A_i$ .

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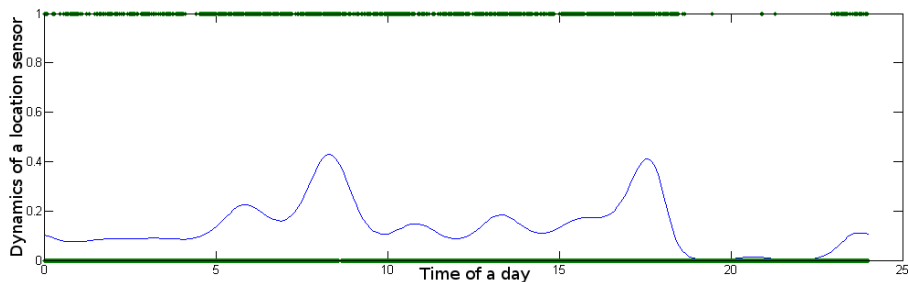
# How certainty may change



## Expiration time functions

$$cf(V, \Delta t) = \begin{cases} cf(V) * \frac{expiration(A) - \Delta t}{expiration(A)} & \text{if } \Delta t \leq expiration(A) \\ 0 & \text{otherwise} \end{cases}$$

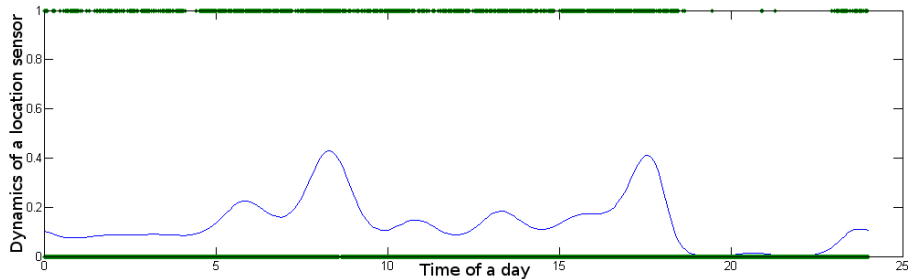
# Dynamic expiration times



## Dynamics of uncertainty

$$\text{expiration}(A, t) = \text{expiration}(A) * (1 - \text{dynamic}(A, t))$$

# Entropy-based expiration times



## Entropy-based dynamics

$$\text{expiration}(A, n) = \text{expiration}(A) * \left( -\log_2 \frac{1}{n} - \text{entropy}(A, n) \right)$$

$$\text{entropy}(A, n) = - \sum_{x \in X} \frac{x}{n} \log_2 \frac{x}{n}$$

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Equal number  
of different  
sensor readings

$$\begin{aligned} \text{entropy}(A, n) &= 1 \\ \text{expiration}(A, n) &= \text{expiration}(A) * 1 \end{aligned}$$



Equal number  
of different  
sensor readings

$$\begin{aligned} \text{entropy}(A, n) &= 1 \\ \text{expiration}(A, n) &= \text{expiration}(A) * 2,32 \end{aligned}$$



Many different  
readings

$$\begin{aligned} \text{entropy}(A, n) &\approx 3,32 \\ \text{expiration}(A, n) &= \text{expiration}(A) * 0 \end{aligned}$$



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# POI recommender

⬆⬆ (?) weather	⬆⬆ (?) {user_profile}	⬆⬆ (?) activity	⬆⬆ (->) poi
∈ {sunny,cloudy}	~ {eating}	= any	:= outdoor-eating
∈ {rainy}	~ {eating}	∈ {walking,running}	:= indoor-eating
∈ {rainy}	~ {eating}	∈ {driving}	:= drivethrough-eating
∈ {rainy,cloudy}	~ {culture,entertainment}	∈ {walking,driving}	:= theatre-cinema
∈ {rainy,cloudy}	= {culture,sightseeing}	∈ {walking,driving}	:= museum
∈ {sunny}	= {sightseeing,culture}	∈ {any}	:= monuments

Table id: tab\_2 - Recommendations

## Assumed system state

- Weather forecast: *sunny weather* with certainty 0.3, *cloudy* with 0.1, and *rainy* with 0.6.
- How much user is interested in particular POIs: places for eating – 60%, culture – 20%, entertainment – 80%, sightseeing – 20%.
- the user have been recently walking with certainty 0.8, running with 0.1 certainty and driving with certainty 0.1.



# Uncertainties

(?) weather	(?) user_profile	(?) activity	cf(conditions)	cf(rule)	cf(conclusion)
0.3	0.6	0.8	0.3	1	0.3
0.6	0.6	0.8	0.6	1	0.6
0.6	0.6	0.1	0.1	1	0.1
0.6	0.84	0.8	0.6	1	0.6
0.6	0.36	0.8	0.36	1	0.36
0.3	0.36	0.8	0.3	1	0.3

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# Summary and future work

## Summary

- Proposal of uncertainty handling mechanism for mCAS
- Rule-based mechanism ready to easily provide intelligibility and mediation
- Modelling approach for representing dynamic CF

## Future work

- Implementation and evaluation on a real-life example
- User feedback for CF updates
- Handling uncertainty on the level of XTT2 model, by translating XTT2 graph into BN
- Gather more data for testing and evaluation:  
<http://glados.kis.agh.edu.pl>

# Summary and future work

(?) hour	(->) daytime
$\in \{[14.000,18.000]\}$	:= afternoon
$\in \{[6.000,11.000]\}$	:= morning
$\in [19.000,23.000] \cup [0.000,5.000]$	:= night
$\in \{[12.000,13.000]\}$	:= noon

Table id: tab\_2 - DayTime

(?) day	(->) today
$\in \{[sat,sun]\}$	:= weekend
$\in \{[mon,fri]\}$	:= workday

Table id: tab\_3 - Today

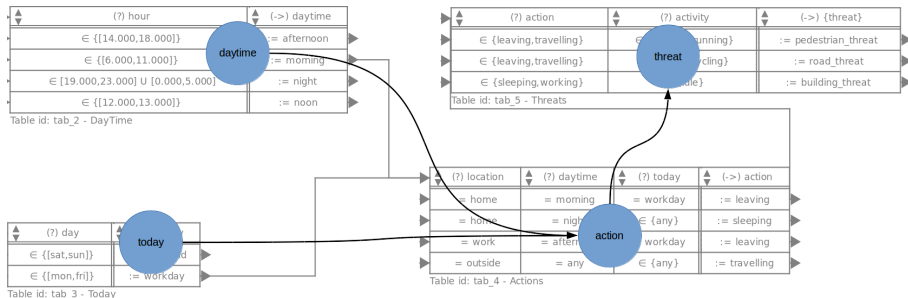
(?) action	(?) activity	(->) {threat}
$\in \{leaving, travelling\}$	$\in \{walking, running\}$	:= pedestrian_threat
$\in \{leaving, travelling\}$	$\in \{driving, cycling\}$	:= road_threat
$\in \{sleeping, working\}$	$\in \{idle\}$	:= building_threat

Table id: tab\_5 - Threats

(?) location	(?) daytime	(?) today	(->) action
= home	= morning	= workday	:= leaving
= home	= night	$\in \{any\}$	:= sleeping
= work	= afternoon	= workday	:= leaving
= outside	= any	$\in \{any\}$	:= travelling

Table id: tab\_4 - Actions

# Summary and future work



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Thank you for your attention!

Do you have any questions?



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