



## A rule-based deontic reasoner

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**X. Parent**

RuleML Webinar 26th January 2018  
University of Luxembourg

Department of Computer Science

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<sup>1</sup>Joint work with L. van der Torre



# Talk layout

① Introduction

② Benchmark problems

③ Our tool

④ How our solution works (roughly)

⑤ Conclusion



## Introduction



# Background: AI & law

## MIREL

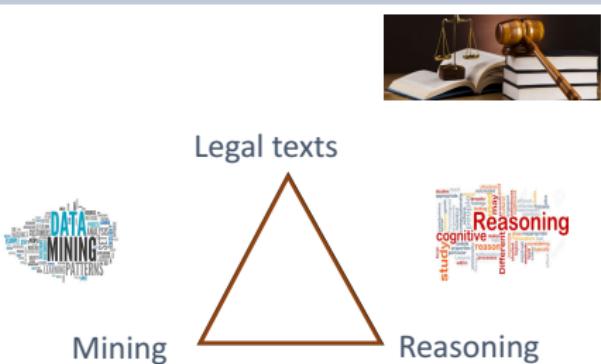


MINING AND REASONING WITH LEGAL TEXTS.



EU Horizon 2020 research and innovation programme—Marie Skłodowska-Curie

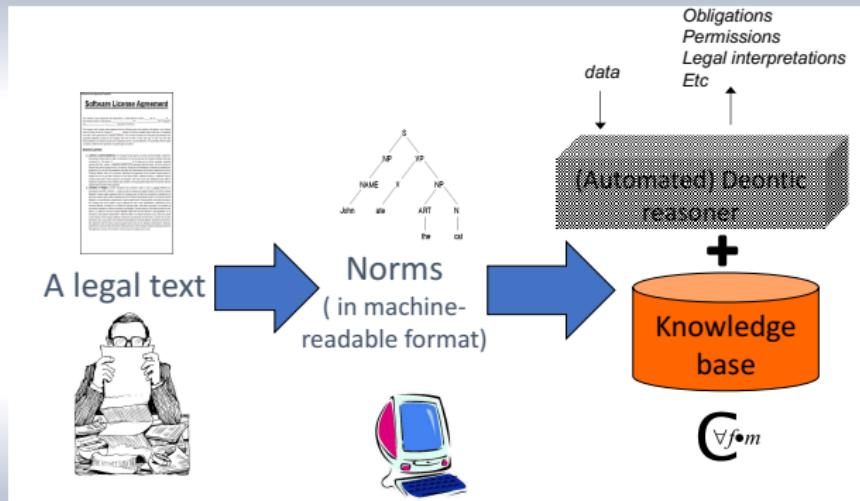
Grant agreement No 690974.





## Introduction

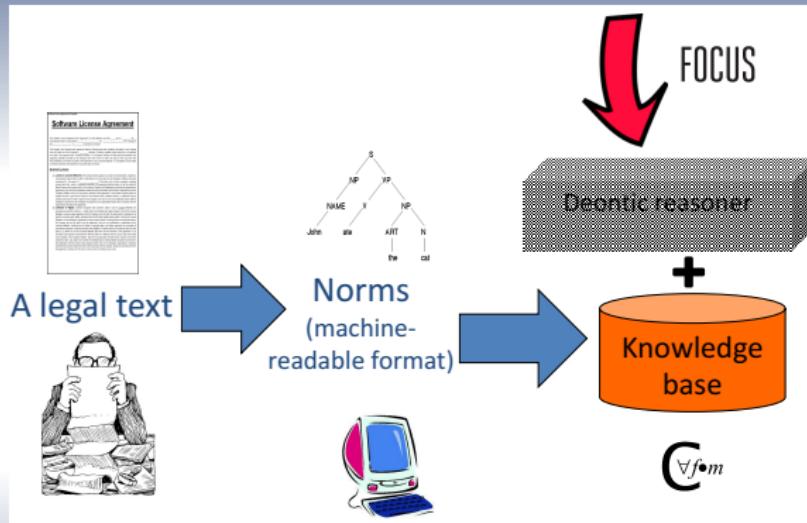
# Mining and reasoning



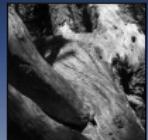


## Introduction

# Mining and reasoning



Long term-goal: automated tool support  
Norm-compliance checking  
Consistency checking



## Introduction

## Example





## Introduction

## Example



L. Robaldo



# Deontic logic

## Deontic logic

- Concerned with obligation, permission and related concepts
- Normative reasoning in law
  - Sergot, McCarthy, Jones, Governatori, Sartor, ...
  - Law as a logical theory

## Two research traditions

- Possible worlds semantics (mid 50s)
  - Deontic logic as a branch of modal logic
- “Norm-based” semantics (Hansen, 00s)
  - Roots in Alchourrón and Bulygin’s approach to normative systems





# Deontic logic

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Rule-based systems





## Introduction

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The pragmatic oddity in a norm-based deontic logic.

In Keppens, J. and Governatori, G., editors, *Proc. of the 16th International Conference on Artificial Intelligence and Law, ICAIL 2017, London, United Kingdom, June 12-16, 2017*, pages 169–178.

## Highlights



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## Highlights

Makinson/van der torre

### A “new” logic—in the rule-based tradition (I/O logic)

- » Well-defined
  - » Performs well w.r.t. benchmark problems of deontic logic
    - Contrary-to-duty (CTD) reasoning
    - Conflict
- (Perform well=return the expected answers to queries)

RuleML 2015



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## Highlights

### Advantage

- ▶ Simple (on the outside)
  - ▶ User-friendly
- Easy to use for non-experts



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## Highlights

### Novelty 1

- ▶ Consistency checks in the semantics
- ▶ Reflected in the proof theory

### Spin-off

- ▶ Handles a recurrent objection against rule-based systems (e.g., Reiter's default logic): lack of a proof-theory



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## Highlights

### Novelty 2

- ▶ A modular treatment of the two categories of benchmarks
  - A unique formalism, not two (separate) formalisms

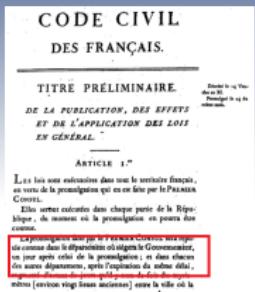
### Spin-off

- ▶ The reasoner able to handle **both** CTDs and conflicts in the text



## Benchmark problems

## Group 1: CTD



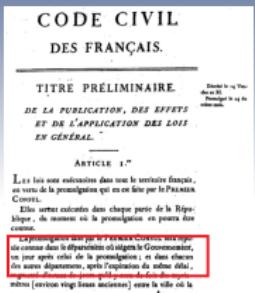
## The standard CTD structure (Chisholm)

- (1)  $a$  is obligatory
- (2) If not- $a$ , then  $b$  is obligatory
- (3) If  $a$ , then not- $b$  is obligatory



## Benchmark problems

## Group 1: CTD



Primary obligation

The standard CTD structure (Chisholm)

- (1)  $a$  is obligatory
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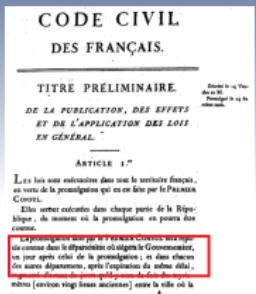
CTD obligation

ATD obligation



## Benchmark problems

## Group 1: CTD



In the old days: SDL  
KD modal logic  
Obligatory : true in  
the ideal worlds



## The standard CTD structure (Chisholm)

- (1)  $a$  is obligatory
- (2) If  $\neg a$ , then  $b$  is obligatory
- (3) If  $a$ , then  $\neg b$  is obligatory
- (4) Not- $a$

## Problem

## Formalisation

- Inconsistent

Overall: problem solved.  
But there are still problems on the periphery.



# CTDs in the GDPR

## Example 1

- Personal data shall be processed lawfully (Art. 5). For example, the data subject must have given consent to the processing of his or her personal data for one or more specific purposes (Art. 6/1.a).
- If the personal data have been processed unlawfully (none of the requirements for a lawful processing applies), the controller has the obligation to erase the personal data in question without delay (Art. 17.d, right to be forgotten).



## Group 2: conflicts (cf. [Goble, 2013])

### Normative conflict

The agent ought to do each of several things, but cannot do them all



**Goble, L. (2013).**

Prima facie norms, normative conflicts, and dilemmas.

In Gabbay, D., Horty, J., Parent, X., van der Meyden, R., and van der Torre, L., editors, *Handbook of Deontic Logic and Normative Systems*, pages 241–352. College Publications, London. UK.



## Group 2: conflicts (cf. [Goble, 2013])

### Normative conflict

The agent ought to do each of several things, but cannot do them all

Strict, or simple, conflicts:  $\bigcirc a, \bigcirc \neg a$

Binary conflicts:  $\bigcirc a, \bigcirc b$  but  $\neg \Diamond(a \wedge b)$

N-ary conflicts (general form):  $\bigcirc a_1, \dots, \bigcirc a_n$  but  $\neg \Diamond(a_1 \wedge \dots \wedge a_n)$



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Conflicts across regulations are common-place:

Must the user expressly provide consent to be tracked?

- ➡ GDPR: yes
- ➡ New EU e-privacy directive : no.

The reasoner must be able to detect/accommodate inconsistencies.



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State of the art with the modal logic approach: either the logic is too strong or too weak:

- ➡ Too strong:  $\Box a, \Box \neg a \vdash \Box b$  (deontic explosion)
- ➡ Too weak:  $\Box(a \vee b), \Box \neg a \not\vdash \Box b$

Also missing: an integration with CTDs.



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# I/O logic (in a nutshell)

## One of the success stories of deontic logic

- Devised by Makinson & van der Torre
- Dedicated chapter in the **Handbook of Deontic Logic**



## Conditionals (deontic reading): “If $a$ , then $b$ (obligation)”

- Semantics: “operational”
  - Procedures yielding outputs for inputs
- Proof-theory: generalizes existing ones
  - No axiom of identity (““If  $a$ , then  $a$ ”” )
  - Principle not desirable under a deontic reading



## A parenthesis on LegalRuleML



### List of requirements (from the Oasis LegalRuleML TC)

Support for modelling:

① Different types of rules

- Prescriptive rules : obligations + permissions
- Constitutive rules (counts-as conditionals)
  - Legal definitions ('sensitive personal data')
  - Legal interpretation

② Defeasible reasoning (reasoning about exceptions)

I/O logic ticks all the boxes!

Well-grounded in the legal domain



## Our tool

# A parenthesis on LegalRuleML



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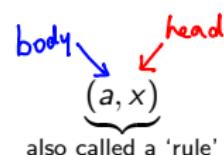
Well-grounded in the legal domain



# Operational semantics

General form

Below: a conditional obligation in the I/O notation



$a$  and  $x$  : two formulae of a base logic



A normative system  $N$  is a set of such pairs.

Main “semantical” construct:

$$x \in O(N, a)$$

Given input  $a$  (state of affairs),  $x$  (obligation) is in the output under norms  $N$

Detachment (modus-ponens) : core mechanism of the semantics

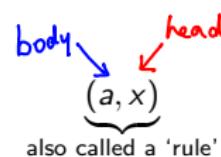


## Our tool

# Operational semantics

General form

Below: a conditional obligation in the I/O notation



$a$  and  $x$  : two formulae of a base logic

PL, FOL, modal logic, ...



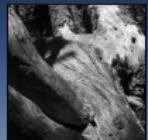
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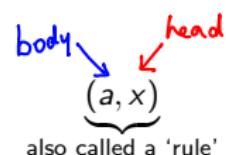


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## Our tool

# Two-sided architecture

## Under the hood

- Semantics

I/O operations



*soundness and completeness results*

## On the outside

## Proof-theory

Derivation tree  
Nodes are pairs of formulas  
Inference rules



( $a, x$ )



But needed for, e.g., decidability  
And hidden to the eyes of users





## Our tool

# A potential misunderstanding



“User-friendly” does not mean trivial.

There is more to I/O logic than just deriving pairs from pairs.

When you see written

$$(a, x)$$



## Our tool

# A potential misunderstanding



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There is more to I/O logic than just deriving pairs from pairs.

When you see written

$$(a, x)$$

Under the hood, the reasoner has calculated that



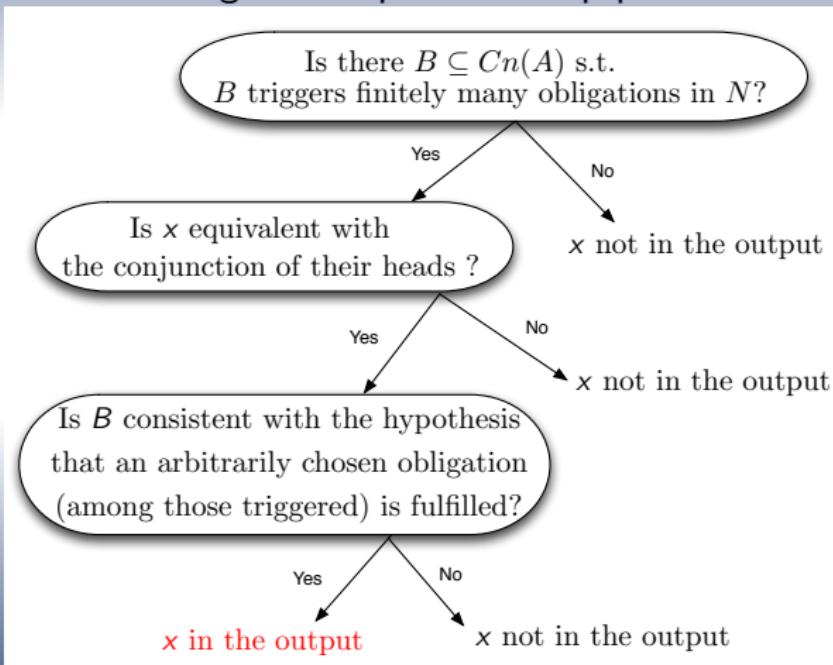
$$x \in O(N, a)$$



# Our proposal: a new I/O operation

## Semantics

Calculating the output: a 3-step procedure





How our solution works (roughly)

## Our take on the benchmarks (roughly)

Proof-theory

### A modular treatment

Weaken the logic, but not too much

The troublemakers:

$$\text{WO } \frac{(a, x) \quad x \vdash y}{(a, y)}$$

$$\text{AND } \frac{(a, x) \quad (a, y)}{(a, x \wedge y)}$$

It is okay to let WO go. It is not okay to let AND go.



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It is okay to let WO go. It is not okay to let AND go.

### Against AND: “pragmatic oddity” (Sergot/Prakken)

- $d$ : there is a dog
- $s$ : there is warning sign



$$\text{SI } \frac{(\top, \neg d)}{(d, \neg d)} \quad \text{AND } \frac{\begin{array}{c} (\top, \neg d) \\ \hline (d, \neg d) \end{array}}{\begin{array}{c} (d, s) \\ \hline (d, \neg d \wedge s) \end{array}}$$

No!



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### In support of AND (Horty)

Norms come from different sources  $\Rightarrow$  aggregation

$m$ : military service

$c$ : civilian

$$\frac{(\top, m \vee c) \quad (\top, \neg m)}{(\top, \neg m \wedge c)}$$

Yes!



How our solution works (roughly)

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Proof-theory

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It is okay to let WO go. It is not okay to let AND go.

### A middle way

Consistency checks

$$\text{R-AND } \frac{(a, x) \quad (a, y) \quad a \wedge x \text{ consistent} \quad a \wedge y \text{ consistent}}{(a, x \wedge y)}$$



# Evaluation

Table 1: Deontic benchmark examples

$N$	$A$	yes	no
[5] $(\top, \neg k), (k, k \wedge g)$	$k$	$\neg k, k \wedge g$	$\perp$
[30] $(\top, \neg c), (k, c)$	$k$	$\neg c, c, \perp$	
[18] $(\top, \neg f'), (a, f')$	$a$	$\neg f', f', \perp$	
[30] $(\top, \neg f), (f, f \wedge w), (d, f)$	$d$	$\neg f, f, \perp$	
[37] $(r, c'), \overline{(r, c'), (s, \neg c')}$	$r \wedge s$	$c'$	$\perp$
[35] $(\top, p), (\top, \neg p)$	$\top$	$p, \neg p, \perp$	
[36] $(\top, p)$	$\neg(p \wedge h)$	$p$	
$(\top, p), (\top, h)$	$\neg(p \wedge h)$	$p, h, p \wedge h$	$p \wedge \neg h$
[31] $(\top, \neg d), (d, d \wedge p')$	$d$	$\neg d, d \wedge p', \perp$	
$(\top, \neg(d \wedge p'))$		$\neg(d \wedge p')$	

$k$ : kill	$c$ : cigarette	$p$ : polite
$g$ : gently	$d$ : dog	$h$ : honest
$f$ : fence	$r$ : rain	$a$ : asparagus
$w$ : white	$s$ : sun	$c'$ : close
$f'$ : finger	$p'$ : poodle	

Good news : reasoner returns the expected answers.



## Summary

I have described a deontic reasoner currently under development.

► Well-defined:

- Semantics and proof-theory

- Completeness result linking the two

► Performs well on the two categories of benchmark problems of deontic logic

Spin-off: allows us to address a recurrent objection against rule-based systems

► Lack of proof-theory



## Future work

A big step forward, but only a first step.

### Extensions

- ▶ Time, exceptions and other natural language constructs
- ▶ Permission and constitutive rules

### Automation

- ▶ On-going work, with Benzmüller
  - Embedding into Higher-Order Logic (HOL)
  - Theorem-prover Isabelle/HOL for automation

Thank you!



# Non-monotonic logics & CTDs

Flavored by, e.g., McCarthy (early 90's)

## Bottom line

$$\text{SI} \quad \frac{(\top, \neg d)}{(d, \neg d)}$$

Dashed line: the inference is blocked.

Sergot's view: no good for norm-compliance checking



# Non-monotonic logics & CTDs

Flavored by, e.g., McCarthy (early 90's)

## Bottom line

$$\text{SI} \frac{(\top, \neg d)}{(d, \neg d)}$$

Dashed line: the inference is blocked.

*"The non-monotonic properties of a logic program using negation-by-failure make a consistent representation [of CTDs] possible. However, the program will have certain counter-intuitive properties. For instance, **violated obligations simply vanish**. Nothing more can be inferred about them, as the condition for something being obligatory no longer applies. One might argue that in actual life violated obligations do not vanish." (Herrestad)*