

Parcial #1

Cálculo I

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$$1) \lim_{x \rightarrow 2} \frac{x^3 - 8}{x - 2} = 12 \rightarrow \lim_{x \rightarrow 2} \frac{(x-2)(x^2 + 2x + 4)}{x-2} = \lim_{x \rightarrow 2} x^2 + 2x + 4$$

$$= (2)^2 + 2(2) + 4 = 4 + 4 + 4 = 12$$

$$2) \lim_{x \rightarrow 0} \frac{x}{|x|} = \lim_{x \rightarrow 0^+} \frac{x}{|x|} = \frac{0.1}{|0.1|} = \frac{0}{0} = \infty$$

$$\lim_{x \rightarrow 0^-} \frac{-0.99}{|-0.99|} = \frac{-0.99}{0.99} = \frac{-0}{0} = -\infty$$

$$\left| \lim_{x \rightarrow 0} \frac{x}{|x|} = \text{no existe} \right|$$

$$5) \lim_{z \rightarrow 1} \frac{z^3 + 8z - 2}{z^2 + 9z - 10} = \frac{1^3 + 8(1) - 2}{1^2 + 9(1) - 10} = \frac{1 + 8 - 2}{1 + 9 - 10} = \frac{7}{0} = \infty$$

$$\lim_{z \rightarrow 1^-} \frac{z^3 + 8z - 2}{z^2 + 9z - 10} = \frac{(0.9)^3 + 8(0.9) - 2}{(0.9)^2 + 9(0.9) - 10} = \frac{1 + 8 - 2}{1 + 9 - 10} = \frac{7}{0} = \infty \rightarrow \text{existe}$$

$$8) \lim_{x \rightarrow 2} (3x^2 - 4x) = 4 = (3(2)^2 - 4(2)) = 3(4) - 8 = 12 - 8 = 4$$

$$9) f(x) = \frac{x^2 - 4}{x - 2} \rightarrow x - 2 = 0 \rightarrow x = 2$$

$$11) \text{Si } \lim_{x \rightarrow 2} g(x) = -2 \rightarrow \lim_{x \rightarrow 2} \sqrt{g(x)^2 + 12} = (-2)^2 + 12 = \sqrt{4 + 12} = \sqrt{16} = 4$$

$$13) \lim_{x \rightarrow 9} \frac{(x+1)^2}{2x^2} \rightarrow \text{no es una función constante.} \\ \text{Y no se aproxima a nada.}$$

$$14) \lim_{x \rightarrow \infty} \sqrt{x^2 - x} - x = \sqrt{x^2 - x} - x \cdot \frac{\sqrt{x^2 - x} + x}{\sqrt{x^2 - x} + x} = \frac{x^2 - x - x^2}{\sqrt{x^2 - x} + x} = \frac{-x}{\sqrt{x^2 - x} + x} = \frac{-x}{x - \sqrt{x} + x} \\ = \frac{-x}{x - \sqrt{x} + x} = \frac{\frac{-x}{x}}{\frac{x}{x} - \frac{\sqrt{x}}{x} + \frac{x}{x}} = \frac{-1}{1 - \frac{1}{\sqrt{x}} + 1} = \frac{-1}{2}$$

$$15) \lim_{x \rightarrow 0} \frac{x}{1 - \sqrt{1+x}} = \frac{x}{1 - \sqrt{1+x}} \cdot \frac{1 + \sqrt{1+x}}{1 + \sqrt{1+x}} = \frac{x(1 + \sqrt{1+x})}{1 - 1 - x} = \frac{x(1 + \sqrt{1+x})}{-x}$$

$$= -(1 + \sqrt{1+x}) = -1 + \sqrt{1+0} = -1 - \sqrt{1} = -1 - 1 = -2$$

$$16) \lim_{x \rightarrow -1} \frac{x^3 + 1}{x + 1} = \lim_{x \rightarrow -1} \frac{(x+1)(x^2 - x + 1)}{x+1} = x^2 - x + 1 = (-1)^2 - (-1) + 1 = 1 + 1 + 1 = 3$$

$$18) f(x) = \frac{x^2}{x+2}$$

$$A.V = x = -2$$

$$A.H = \text{no line}$$

$$A.O = y = x - 2$$

$$x = -2$$

$$A.O = \lim_{x \rightarrow \infty} \frac{f(x)}{x} = \lim_{x \rightarrow \infty} \frac{\frac{x^2}{x+2}}{x} = \lim_{x \rightarrow \infty} \frac{x^2}{x^2 + 2x} = \frac{\frac{x^2}{x^2} + \frac{2x}{x^2}}{\frac{x^2}{x^2} + \frac{2x}{x^2}} = \frac{1 + 0}{1 + 0} = 1$$

$$\lim_{x \rightarrow \infty} \left[\frac{x^2}{x+2} - \frac{x}{1} \right] = \lim_{x \rightarrow \infty} \frac{x^2 - x^2 - 2x}{x+2} = \frac{-2x}{x+2}$$

$$\lim_{x \rightarrow \infty} \frac{-2x}{x+2} = \frac{-2}{1+0} = -2$$

$$\lim_{x \rightarrow -2^+} \frac{x^2}{x+2} = \frac{(-1.99)^2}{-1.99+2} = \frac{4}{0} = \infty$$

$$\lim_{x \rightarrow -2^-} \frac{(-2.1)^2}{-2.1+2} = \frac{4}{-0} = -\infty$$

$$\lim_{x \rightarrow \infty} \frac{x^2}{x+2} = \frac{\frac{x^2}{x^2}}{\frac{x}{x^2} + \frac{2}{x^2}} = \frac{1}{\frac{1}{x} + \frac{2}{x^2}} = \frac{1}{0} = \infty$$

$$\lim_{x \rightarrow -\infty} \frac{x^2}{x+2} = \frac{\frac{x^2}{x^2}}{\frac{x}{x^2} + \frac{2}{x^2}} = \frac{1}{\frac{1}{x} + \frac{2}{x^2}} = \frac{-1}{0} = -\infty$$

$$19) f(t) = \begin{cases} t+4 & \text{si } t \leq -4 \\ 4-t & \text{si } t > -4 \end{cases}$$

$$\lim_{t \rightarrow -4^+} (4-t) = 4 - (-3.99) = 4 + 4 = 8$$

$$\lim_{t \rightarrow -4} f(t) = \text{no existe}$$

$$\lim_{t \rightarrow -4^-} (t+4) = -4 + 4 = 0$$