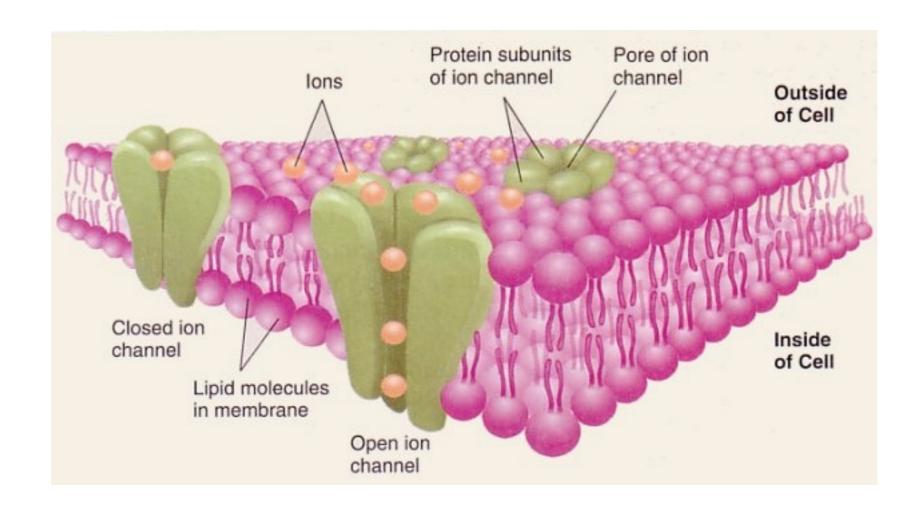
Single Neuron Dynamics

— point neuron model



What determines the resting potential of a neuron?

$$[K^{+}]_{outside} = [K^{+}]_{inside} P(E > -qV_{K})$$

$$p(E)dE = \frac{1}{Z} \exp(-\beta E) dE \qquad Z = 1/\beta = k_{B}T$$

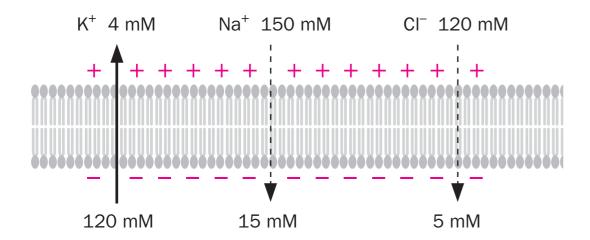
$$P(E > -qV_{K}) = \int_{-qV_{K}}^{\infty} p(E)dE = \exp\left(\frac{qV_{K}}{k_{B}T}\right)$$

$$[K^{+}]_{outside} = [K^{+}]_{inside} \exp(qV_{K}/k_{B}T)$$

$$V_{K} = \frac{k_{B}T}{q} \ln \frac{[K^{+}]_{outside}}{[K^{+}]_{inside}}$$

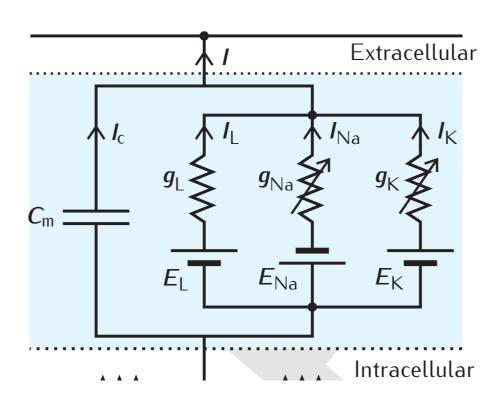
$$E_{A} = \frac{k_{B}T}{q} \ln \frac{[A]_{outside}}{[A]_{inside}} \qquad V = \frac{k_{B}T}{e} \ln \left(\frac{\sum_{i=1}^{N} P_{M_{i}^{+}}[M_{i}^{+}]_{out} + \sum_{j=1}^{N} P_{A_{j}^{-}}[A_{j}^{-}]_{in}}{\sum_{i=1}^{N} P_{M_{i}^{+}}[M_{i}^{+}]_{in} + \sum_{j=1}^{N} P_{A_{j}^{-}}[A_{j}^{-}]_{out}} \right)$$

(A)



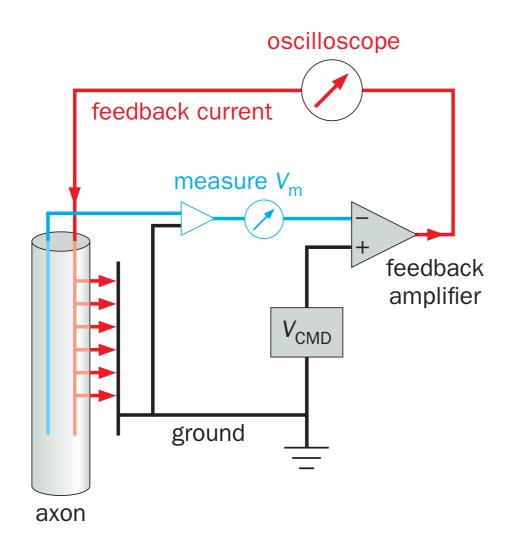
$$E_K = -70mV$$
 $E_{Cl} = -60mV$
 $I_{Na} = g_{Na}(V - E_{Na})$
 $I_{Vrest} = -60mV$
 $I_{K} = g_{K}(V - E_{K})$
 $I_{Na} = g_{K}(V - E_{K})$

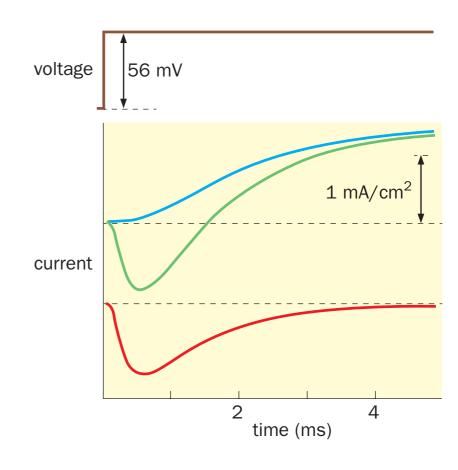
The Equivalent Electronic Circuit of a Neuron



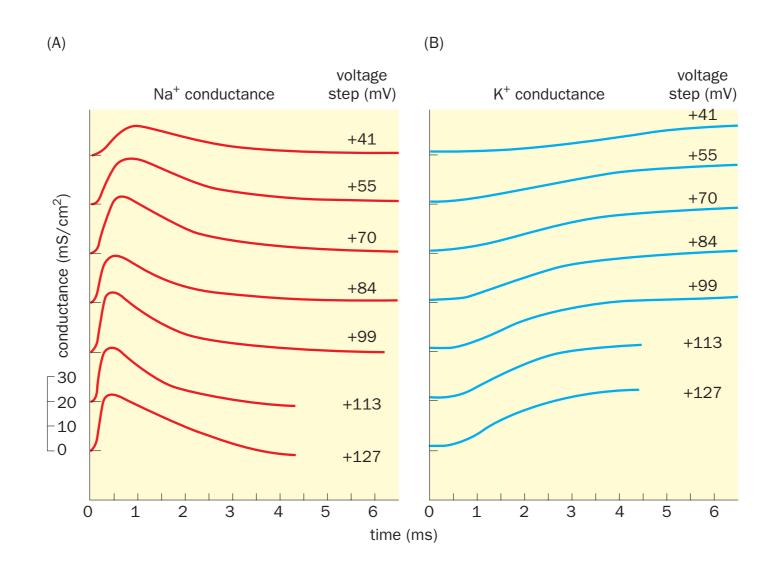
$$C_m \frac{dV}{dt} = -\sum_i g_i(V)(V - E_i) - \bar{g}_L(V - E_L) + I_e$$

Voltage Clamp Recording





Voltage-gated Conductance



Qualitative explanation of action potential generation

