

Harmonic analysis

Singular integrals

- Recalls on Fourier transform and convolution
- The Hardy-Littlewood maximal operator
The Lebesgue derivation theorem.
- Principal values – Some Fourier transforms
- The Calderón-Zygmund theory
Hilbert and Riesz transforms.
- The Littlewood-Paley theory
- Higher Riesz transforms
Spherical harmonics
Non-smooth kernels.
- BMO and H^1 .
- Interpolation
The Marcinkiewicz interpolation theorem.
The Riesz-Thorin interpolation theorem.
Real and complex interpolation with BMO .

Bibliography

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E.M. Stein, Harmonic Analysis, orthogonality and oscillatory integrals, Princeton University Press 1993.

E.M. Stein and G. Weiss, Introduction to Fourier Analysis on Euclidean Spaces, Princeton University Press 1971

A. Zygmund, Trigonometric Series, Cambridge University Press 2002.