# ACM/ICPC Template Manaual

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#### 1 头文件模板

```
#include <bits/stdc++.h> // c++0x only
 #include <iostream>
 #include <cstdio>
 #include <cstring>
 #include <algorithm>
 #include <string>
#include <vector>
#include <queue>
 #include <stack>
#include <set>
 #include <map>
#include <cmath>
#include <iomanip>
 #include <functional>
#include <cstdlib>
#include <climits>
#include <cctype>
using namespace std;
using namespace std;
#define REP(i,x) for(int i = 0; i < (x); i++)
#define DEP(i,x) for(int i = (x) - 1; i >= 0; i--)
#define FOR(i,x) for(__typeof(x.begin())i=x.begin(); i!=x.end(); i++)
#define CLR(a,x) memset(a, x, sizeof(a))
#define MO(a,b) (((a)%(b)+(b))%(b))
#define ALL(x) (x).begin(), (x).end()
#define SZ(v) ((int)v.size())
#define UNIQUE(v) sort(ALL(v)); v.erase(unique(ALL(v)), v.end())
#define out(x) cout << #x << ": " << x << endl;
#define fastcin ios_base::sync_with_stdio(0);cin.tie(0);
typedef long long long ull;</pre>
 typedef unsigned long long ull;
typedef pair<int, int> PII;
typedef vector<int> VI;
#define INF 0x3f3f3f3f
#define MOD 1000000007
#define EPS 1e-8
 #define MP(x,y) make_pair(x,y)
 #define MT(x,y...) make_tuple(x,y) // c++0x only
 #define PB(x) push_back(x)
#define IT iterator
#define X first
#define Y second
```

#### 2 数学

#### 2.1素数

#### 2.1.1 埃氏筛

```
O(n \log \log n) 筛出 MAXN 内所有素数
notprime[i] = 0/1 0 为素数 1 为非素数
const int MAXN = 1000100;
bool notprime[MAXN] = {1, 1}; // 0 && 1 为非素数
void GetPrime() {
  for (int i = 2; i < MAXN; i++)</pre>
         if (!notprime[i] && i <= MAXN / i) // 筛到√n为止 for (int j = i * i; j < MAXN; j += i) notprime[j] = 1;
}
2.1.2 欧拉筛
O(n) 得到欧拉函数 phi[]、素数表 prime[]、素数个数 tot
传入的 n 为函数定义域上界
const int MAXN = 100010;
bool vis[MAXN];
int tot, phi[MAXN], prime[MAXN];
void CalPhi(int n) {
   set(vis, 0); phi[1] = 1; tot = 0;
   for (int i = 2; i < n; i++) {</pre>
         if (!vis[i]) {
              prime[tot++] = i;
              phi[i] = i - 1;
         for (int j = 0; j < tot; j++) {
   if (i * prime[j] > n) break;
   vis[i * prime[j]] = 1;
   if (i % prime[j] == 0) {
                  phi[i * prime[j]] = phi[i] * prime[j];
                  break:
              else phi[i * prime[j]] = phi[i] * (prime[j] - 1);
    }
}
2.1.3 随机素数判定
O(s \log n) 内判定 2^{63} 内的数是不是素数, s 为测定次数
bool Miller_Rabin(ll n, int s) {
     if (n == 2) return 1;
     if (n < 2 | | !(n & 1)) return 0;</pre>
    if (n < 2 | 1 | !(n & 1)) return 0;
int t = 0; ll x, y, u = n - 1;
while ((u & 1) == 0) t++, u >>= 1;
for (int i = 0; i < s; i++) {
    ll a = rand() % (n - 1) + 1;
    ll x = Pow(a, u, n);
    for (int j = 0; j < t; j++) {
        ll y = Mul(x, x, n);
        if (y == 1 && x != 1 && x != n - 1) return 0;
        y = y ...</pre>
              x = y;
         if (x != 1) return 0;
     return 1;
}
```

#### 2.1.4 分解质因数

```
函数返回素因数个数
数组以 fact[i][0]^{fact[i][1]} 的形式保存第 i 个素因数
ll fact[100][2];
int getFactors(ll x) {
    int cnt = 0;
    for (int i = 0; prime[i] <= x / prime[i]; i++) {
   fact[cnt][1] = 0;</pre>
        if (x % prime[i] == 0 ) {
            fact[cnt][0] = prime[i];
            while (x % prime[i] == 0) {
  fact[cnt][1]++;
               x /= prime[i];
            }
            cnt++;
       }
    if (x != 1) {
        fact[cnt][0] = x;
        fact[cnt++][1] = 1;
    return cnt;
2.2 欧拉函数
2.2.1 求一个数的欧拉函数
long long Euler(long long n) {
    long long rt = n;
for (int i = 2; i * i <= n; i++)</pre>
        i\hat{f} (n % i = 0) {
            rt -= rt / i;
while (n % i == 0) n /= i;
    if (n > 1) rt -= rt / n;
    return rt;
2.2.2 筛法求欧拉函数
const int MAXN = 10001;
int phi[MAXN] = \{0, 1\};
int pnt[maxn] = ie, if,
void CalEuler() {
  for (int i = 2; i < MAXN; i++)
    if (!phi[i]) for (int j = i; j < MAXN; j += i) {
        if (!phi[j]) phi[j] = j;
        phi[j] = phi[j] / i * (i - 1);
    }
}</pre>
            }
}
        扩展欧几里得-乘法逆元
2.3
2.3.1 扩展欧几里得
void exgcd(ll a, ll b, ll &d, ll &x, ll &y) {
    if (!b) {d = a; x = 1; y = 0;}
else {exgcd(b, a % b, d, y, x); y -= x * (a / b);}
```

#### 2.3.2 求 ax+by=c 的解

```
// 引用返回通解: X = x + k * dx, Y = y - k * dy // 引用返回的x是最小非负整数解,方程无解函数返回0
#define Mod(a,b) (((a)%(b)+(b))%(b))
bool solve(ll a, ll b, ll c, ll &x, ll &y, ll &dx, ll &dy) {
    if (a == 0 && b == 0) return 0;
    ll d, x0, y0; exgcd(a, b, d, x0, y0); if (c % d != 0) return 0;
dx = b / d; dy = a / d;
x = Mod(x0 * c / d, dx); y = (c - a * x) / b;
// y = Mod(y0 * c / d, dy); x = (c - b * y) / a;
    return 1;
2.3.3 乘法逆元
// 利用exgcd求a在模m下的逆元,需要保证gcd(a, m) == 1.
ll inv(ll a, ll m) {
    ll x, y, d; exgcd(a, m, d, x, y);
    return d == 1 ? (x + m) % m : -1;
// a < m 且 m为素数时,有以下两种求法
ll inv(ll a, ll m) {
    return a == 1 ? 1 : inv(m % a, m) * (m - m / a) % m;
Il inv(ll a, ll m) {
    return Pow(a, m - 2, m);
}
2.4 模线性方程组
2.4.1 中国剩余定理
// X = r[i] \pmod{m[i]}; 要求m[i]两两互质 // 引用返回通解X = re + k * mo;
void crt(ll r[], ll m[], ll n, ll &re, ll &mo) {
    mo = 1, re = 0;
    for (int i = 0; i < n; i++) mo *= m[i];</pre>
    for (int i = 0; i < n; i++) {
    ll x, y, d, tm = mo / m[i];
    exgcd(tm, m[i], d, x, y);
    re = (re + tm * x * r[i]) % mo;</pre>
    re = (re + mo) \% mo;
2.4.2 一般模线性方程组
// X = r[i] (mod m[i]); m[i]可以不两两互质
// 引用返回通解X = re + k * mo; 函数返回是否有解
bool excrt(ll r[], ll m[], ll n, ll &re, ll &mo) {
    ll x, y, d; mo = m[0], re = r[0];
for (int i = 1; i < n; i++) {
         exgcd(mo, m[i], d, x, y);
if ((r[i] - re) % d != 0) return 0;
        x = (r[i] - re) / d * x % (m[i] / d);
re += x * mo;
mo = mo / d * m[i];
    re %= mo;
} re = (re + mo) % mo;
    return 1;
}
```

#### 2.5 组合数

#### 2.5.1 一般组合数

```
// 0 <= m <= n <= 1000
const int maxn = 1010;
11 C[maxn][maxn];
void CalComb() {
   C[0][0] = 1;
for (int i = 1; i < maxn; i++) {
      C[i][0] = 1;
      for (int j = 1; j <= i; j++)
          C[i][j] = (C[i - 1][j - 1] + C[i - 1][j]) \% mod;
   }
}
// 0 <= m <= n <= 105, 模p为素数
const int maxn = 100010;
11 f[maxn];
void CalFact() {
   f[0] = 1;
for (int i = 1; i < maxn; i++)
f[i] = (f[i - 1] * i) % mod;
il C(int n, int m) {
   return f[n] * inv(f[m] * f[n - m] % mod, mod) % mod;
2.5.2 Lucas 定理
// 1 <= n, m <= 10000000000, 1 < p < 100000, p是素数
const int maxp = 100010;
11 f[maxp];
void CalFact(ll p) {
   f[0] = 1;
   for (int i = 1; i <= p; i++)
f[i] = (f[i - 1] * i) % p;
Il Lucas(ll n, ll m, ll p) {
   ll ret = 1;
   while (n && m) {
      ll a = n \% p, b = m \% p;
      if (a < b) return 0;
ret = (ret * f[a] * Pow(f[b] * f[a - b] % p, p - 2, p)) % p;</pre>
      n /= p; m /= p;
   return ret;
}
2.5.3 大组合数
// 0 <= n <= 109, 0 <= m <= 104, 1 <= k <= 109+7
vector<int> v;
int dp[110];
11 Cal(int 1, int r, int k, int dis) {
   11 \text{ res} = 1;
   for (int i = l; i <= r; i++) {
      int t = i;
for (int j = 0; j < v.size(); j++) {
          int y = v[j];
          while (t \% y == 0) {
             dp[j] += dis;
             t /= y;
          }
      res = res * (ll)t % k;
   }
   return res;
int num = 0;
```

#### 2.6 快速乘-快速幂

```
ll Mul(ll a, ll b, ll mod) {
    ll t = 0;
    for (; b; b >>= 1, a = (a << 1) % mod)
        if (b & 1) t = (t + a) % mod;
    return t;
}
ll Pow(ll a, ll n, ll mod) {
    ll t = 1;
    for (; n; n >>= 1, a = (a * a % mod))
        if (n & 1) t = (t * a % mod);
    return t;
}
```

#### 2.7 其他

#### 2.7.1 Josephus 问题

```
#include <iostream>
using namespace std;
int main() {
   int num, m, r
   while (cin >> num >> m) {
      r = 0;
      for (int k = 1; k <= num; ++k)
           r = (r + m) % k;
      cout << r + 1 << endl;
   }
   return 0;
}</pre>
```

#### 3 字符串

#### 3.1 KMP

#### 3.2 Manacher 最长回文子串

```
const int MAXN = 110010;
char Ma[MAXN * 2];
int Mp[MAXN * 2];
void Manacher(char s[], int len) {
   int l = 0; Ma[l++] = '$'; Ma[l++] = '#';
   for (int i = 0; i < len; i++) {
      Ma[l++] = s[i]; Ma[l++] = '#';
   }
   Ma[l] = 0; int mx = 0, id = 0;
   for (int i = 0; i < l; i++) {
      Mp[i] = mx > i ? min(Mp[2 * i d - i], mx - i) : 1;
      while (Ma[i + Mp[i]] == Ma[i - Mp[i]]) Mp[i]++;
      if (i + Mp[i] > mx) {
            mx = i + Mp[i]; id = i;
      }
   }
}
```

### 4 数据结构

#### 4.1 树状数组

```
O(\log n) 查询和修改数组的前缀和
// 注意下标应从1开始
#define lowbit(i) (i&(-i))
int bit[maxn], n;
int query(int i){
    int s = 0;
    while(i){
        s += bit[i];
         i -= lowbit(i);
    return s;
void add(int i, int x){
  while(i<=n){</pre>
        bit[i] += x;
         i += lowbit(i);
}
4.2
         线段树
4.2.1 声明
#define lson rt<<1 // 左儿子
#define rson rt<<1|1 // 右儿子
#define Lson l,m,lson // 左子树
#define Rson m+1,r,rson // 右子树
void PushUp(int rt); // 用lson和rson更新rt
void PushDown(int rt[, int m]); // rt的标记下移, m为区间长度(若与标记有关)
void build(int l, int r, int rt); // 以下为根节点,对区间[1, r]建立线段树
void update([...,] int l, int r, int rt) // rt[l, r] h 寻找目标并更新 int query(int L, int R, int l, int r, int rt) // rt-[l, r] h 告询[L, R]
4.2.2 单点更新-区间查询
const int maxn = 50010;
int sum[maxn << 2];
void PushUp(int rt) {</pre>
    sum[rt] = sum[lson] + sum[rson];
void build(int l, int r, int rt) {
    if (l == r) {scanf("%d", &sum[rt]); return;} // 建立的时候直接输入叶节点
    int m = (l + r) >> 1;
build(Lson); build(Rson);
    PushUp(rt);
void update(int p, int add, int l, int r, int rt) {
    if (l == r) {sum[rt] += add; return;}
     int m = (l + r) >> 1;
    if (p <= m) update(p, add, Lson);
else update(p, add, Rson);</pre>
    PushUp(rt);
int query(int L, int R, int l, int r, int rt) {
   if (L <= 1 && r <= R) {return sum[rt];}</pre>
    int m = (l + r) >> 1, s = 0;
if (L <= m) s += query(L, R, Lson);
if (m < R) s += query(L, R, Rson);</pre>
    return s;
```

#### 4.2.3 区间更新-区间查询

```
// seg[rt]用于存放懒惰标记,注意PushDown时标记的传递
const int maxn = 101010;
int seg[maxn << 2], sum[maxn << 2];
void PushUp(int rt) {</pre>
    sum[rt] = sum[lson] + sum[rson];
void PushDown(int rt, int m) {
  if (seg[rt] == 0) return;
    seg[lson] += seg[rt];
seg[rson] += seg[rt];
sum[lson] += seg[rt] * (m - (m >> 1));
sum[rson] += seg[rt] * (m >> 1);
    seg[rt] = 0;
void build(int 1, int r, int rt) {
    seg[rt] = 0;
if (l == r) {scanf("%lld", &sum[rt]); return;}
    int m = (l + r) >> 1;
    build(Lson); build(Rson);
    PushUp(rt);
void update(int L, int R, int add, int l, int r, int rt) {
    if (L <= 1 && r <= R) {
         seg[rt] += add;
sum[rt] += add * (r - l + 1);
         return;
    PushDown(rt, r - l + 1);
    int m = (1 + r) >> 1;
if (L <= m) update(L, R, add, Lson);
    if (m < R) update(L, R, add, Rson);</pre>
    PushUp(rt);
int query(int L, int R, int l, int r, int rt) {
   if (L <= l && r <= R) return sum[rt];
   PushDown(rt, r - l + 1);</pre>
    int m = (l + r) >> 1, ret = 0;
if (L <= m) ret += query(L, R, Lson);
if (m < R) ret += query(L, R, Rson);</pre>
    return ret;
}
```

#### 图论 5

#### 5.1 并查集

```
const int MAXN = 128;
int fa[MAXN], ra[MAXN];
void init(int n) {
    for (int i = 0; i <= n; i++) {
        fa[i] = i; ra[i] = 0;
int find(int x) {
   if (fa[x] != x) fa[x] = find(fa[x]);
    return fa[x];
void unite(int x, int y) {
    x = find(x); y = find(y); if (x == y) return;
    if (ra[x] < ra[y]) fa[x] = y;</pre>
    else {
        fa[y] = x; if (ra[x] == ra[y]) ra[x]++;
bool same(int x, int y) {
    return find(x) == find(y);
        最小生成树
5.2
5.2.1 Kruskal
vector<pair<int, PII> > G;
void add_edge(int u, int v, int d) {
```

```
G.push_back(make_pair(d, make_pair(u, v)));
int Kruskal(int n) {
   init(n);
   sort(G.begin(), G.end());
   int m = G.size();
   int num = 0, ret = 0;
   for (int i = 0; i < m; i++) {
    pair<int, PII> p = G[i];
    int x = p.Y.X;
       int y = p.Y.Y;
int d = p.X;
if (!same(x, y)) {
           unite(x, y);
           num++;
           ret += d;
           printf("(%d, %d) %d\n", x, y, d);
       if (num == n - 1) break;
   return ret;
```

#### 5.2.2 Prim

```
// 耗费矩阵cost[][],标号从0开始,0~n-1
// 返回最小生成树的权值,返回-1表示原图不连通 const int INF = 0x3f3f3f3f;
const int MAXN = 110;
bool vis[MAXN];
int lowc[MAXN];
int Prim(int cost[][MAXN], int n) {
   int ans = 0;
   set(vis, 0);
   vis[0] = 1;
   for (int i = 1; i < n; i++)
      lowc[i] = cost[0][i];
```

```
for (int i = 1; i < n; i++) {
   int minc = INF;
   int p = -1;
   for (int j = 0; j < n; j++)
       if (!vis[j] && minc > lowc[j]) {
       minc = lowc[j];
       p = j;
       }
   if (minc == INF) return -1;
   vis[p] = 1;
   for (int j = 0; j < n; j++)
       if (!vis[j] && lowc[j] > cost[p][j]) lowc[j] = cost[p][j];
   }
   return ans;
}

5.3 最短路

5.3.1 Dijkstra-邻接矩阵
```

```
// MAXN为点数最大值 求S到所有点的最短路
// 要求边权值为非负数 模板为有向边
// dis[x]为起点到点x的最短路 inf表示无法走到
// 记得初始化
const int MAXN = 100; // 点数最大值
const int INF = 0x3F3F3F3F;
int G[MAXN][MAXN], dis[MAXN];
bool vis[MAXN];
void init(int n) {
  memset(G, 0x3F, sizeof(G));
void add_edge(int u, int v, int w) {
   G[u][v] = min(G[u][v], w);
void Dijkstra(int s, int n) {
   memset(vis, 0, sizeof(vis));
memset(dis, 0x3F, sizeof(dis));
   dis[s] = 0;
   for (int i = 0; i < n; i++) {
       int x, min_dis = INF;
for (int j = 0; j < n; j++) {
   if (!vis[j] && dis[j] <= min_dis) {</pre>
             min_dis = dis[j];
          }
       vis[x] = 1;
       for (int j = 0; j < n; j++)
          dis[j] = min(dis[j], dis[x] + G[x][j]);
   }
}
```

#### 5.3.2 Dijkstra-邻接表数组

```
// 点最大值: MAX_N 边最大值: MAX_E
// 求起点s到每个点x的最短路dis[x]
const int MAX_N = "Edit"; // 点数最大值
const int MAX_E = "Edit";
const int INF = 0x3F3F3F3F;
int tot;
int Head[MAX_N], vis[MAX_N], dis[MAX_N];
int Next[MAX_E], To[MAX_E], W[MAX_E];
void init() {
   tot = 0;
   memset(Head, -1, sizeof(Head));
}
void add_edge(int u, int v, int d) {
   W[tot] = d;
   To[tot] = v;
   Next[tot] = Head[u];
```

```
Head[u] = tot++;
void Dijkstra(int s, int n) {
   memset(vis, 0, sizeof(vis));
memset(dis, 0x3F, sizeof(dis));
    dis[s] = 0;
    for (int i = 0; i < n; i++) {
       int x, min_dis = INF;
for (int j = 0; j < n; j++) {
    if (!vis[j] && dis[j] <= min_dis) {</pre>
               x = j;
min_dis = dis[j];
           }
        vis[x] = 1;
       for (int j = Head[x]; j != -1; j = Next[j]) {
  int y = To[j];
  dis[y] = min(dis[y], dis[x] + W[j]);
        }
   }
}
5.3.3 Dijkstra-邻接表向量
// MAXN: 点数最大值
// 求起点S到所有点X的最短路dis[x]
// 记得初始化
const int MAXN = "Edit"
const int INF = 0x3F3F3F3F;
vector<int> G[MAXN];
vector<int> GW[MAXN];
bool vis[MAXN];
int dis[MAXN];
void init(int n) {
    for (int i = 0; i < n; i++) {
   G[i].clear();</pre>
        GW[i].clear();
void add_edge(int u, int v, int w) {
    G[u].push_back(v);
    GW[u].push_back(w);
void Dijkstra(int s, int n) {
  memset(vis, false, sizeof(vis));
  memset(dis, 0x3F, sizeof(dis));
    dis[s] = 0;
    for (int i = 0; i < n; i++) {</pre>
       int x;
        int min_dis = INF;
        for (int j = 0; j < n; j++) {
   if (!vis[j] && dis[j] <= min_dis) {</pre>
               x = j;
               min_dis = dis[j];
           }
        vis[x] = true;
        for (int j = 0; j < (int)G[x].size(); j++) {
  int y = G[x][j];</pre>
            int W = GW[x][j];
            dis[y] = min(dis[y], dis[x] + w);
        }
   }
}
5.3.4 Dijkstra-优先队列
// pair<权值, 点>
// 记得初始化
const int MAXN = "Edit";
```

```
const int INF = 0x3F3F3F3F;
typedef pair<int, int> PII;
typedef vector<PII> VII;
VII G[MAXN];
int vis[MAXN], dis[MAXN];
void init(int n) {
    for (int i = 0; i < n; i++)
   G[i].clear();</pre>
void_add_edge(int u, int v, int w) {
    G[u].push_back(make_pair(w, v));
dis[s] = 0;
    priority_queue<PII, VII, greater<PII> > PQ;
PQ.push(make_pair(dis[s], s));
    while (!PQ.empty()) {
       PII t = PQ.top();
       int x = t.second;
        PQ.pop();
        if (vis[x]) continue;
       vis[x] = 1;
       for (int i = 0; i < (int)G[x].size(); i++) {
  int y = G[x][i].second;
  int w = G[x][i].first;</pre>
           if (!vis[y] && dis[y] > dis[x] + w) {
                dis[y] = dis[x] + w;
               PQ.push(make_pair(dis[y], y));
           }
       }
   }
}
5.3.5 Bellman-Ford(可判负环)
// 求出起点S到每个点X的最短路dis[x]
// 存在负环返回1 否则返回0
// 记得初始化
const int MAX_N = "Edit"; // 点数最大值const int MAX_E = "Edit"; // 边数最大值
const int INF = 0x3F3F3F3F;
int From[MAX_E], To[MAX_E], W[MAX_E];
int dis[MAX_N], tot;
void init() {tot = 0;}
void add_edge(int u, int v, int d) {
    From[tot] = u;
    To[tot] = v;
    W[tot++] = d;
bool Bellman_Ford(int s, int n) {
    memset(dis, 0x3F, sizeof(dis));
    dis[s] = 0;
for (int k = 0; k < n - 1; k++) {
       bool relaxed = 0;
for (int i = 0; i < tot; i++) {
  int x = From[i], y = To[i];
  if (dis[y] > dis[x] + W[i]) {
    dis[y] = dis[x] + W[i];
  relaxed 1;
               relaxed = 1;
           }
        if (!relaxed) break;
    for (int i = 0; i < tot; i++)</pre>
        if (dis[To[i]] > dis[From[i]] + W[i])
           return 1;
    return 0;
```

#### 5.3.6 SPFA

```
// G[u] = mp(v, w)
// SPFA()返回0表示存在负环
const int MAXN = "Edit";
const int INF = 0x3F3F3F3F;
vector<pair<int, int> > G[MAXN];
bool vis[MAXN];
int dis[MAXN];
int inqueue[MAXN];
void init(int n) {
  for (int i = 0; i < n; i++)</pre>
        G[i].clear();
void add_edge(int u, int v, int w) {
   G[u].push_back(make_pair(v, w));
bool SPFA(int s, int n) {
  memset(vis, 0, sizeof(vis));
  memset(dis, 0x3F, sizeof(dis));
  memset(inqueue, 0, sizeof(inqueue));
    dis[s] = 0;
    queue<int> q; // 待优化的节点入队
    q.push(s);
    while (!q.empty()) {
        int x = q.front();
        q.pop();
        dis[y] = dis[x] + w;
                if (!vis[y]) {
                    q.push(y);
                    vis[y] = true;
                    if (++inqueue[y] >= n) return 0;
                }
            }
        }
    return 1;
5.3.7 Floyd 算法
O(n^3) 求出任意两点间最短路
const int MAXN = "Edit";
const int INF = 0x3F3F3F3F;
int G[MAXN][MAXN];
void init(int n) {
  memset(G, 0x3F, sizeof(G));
  for (int i = 0; i < n; i++)</pre>
        G[i][i] = 0;
void add_edge(int u, int v, int w) {
    G[u][v] = min(G[u][v], w);
void Floyd(int n) {
   for (int k = 0; k < n; k++)</pre>
        for (int i = 0; i < n; i++)
  for (int j = 0; j < n; j++)
    G[i][j] = min(G[i][j], G[i][k] + G[k][j]);</pre>
}
5.4 拓扑排序
```

#### 5.4.1 邻接矩阵

```
// 存图前记得初始化
// 存图前记得初始化
// Ans存放拓排结果, G为邻接矩阵, deg为入度信息
// 排序成功返回1, 存在环返回0
const int MAXN = "Edit";
int Ans[MAXN]; // 存放拓扑排序结果
int G[MAXN][MAXN]; // 存放图信息
int deg[MAXN]; // 存放点入度信息
void init()
void init() {
  memset(G, 0, sizeof(G));
  memset(deg, 0, sizeof(deg));
  memset(Ans, 0, sizeof(Ans));
void add_edge(int u, int v) {
     if (G[u][v]) return;
     G[u][v] = 1;
     deg[v]++;
bool Toposort(int n) {
     int int = 0;
     queue<int> que;
     for (int i = 0; i < n; ++i)
   if (deg[i] == 0) que.push(i);</pre>
     while (!que.empty()) {
         int v = que.front(); que.pop();
         Ans[tot++] = v;
for (int i = 0; i < n; ++i)
if (G[v][i] == 1)
                  if(--deg[t] == 0) que.push(t);
     if (tot < n) return false;</pre>
     return true;
5.4.2 邻接表
// 存图前记得初始化
// Ans排序结果, G邻接表, deg入度, map用于判断重边
// 排序成功返回1, 存在环返回0
const int MAXN = "Edit";___
typedef pair<int, int> PII;
int Ans[MAXN];
vector<int> G[MAXN];
int deg[MAXN];
map<PII, bool > S;
void init(int n) {
     S.clear();
    for (int i = 0; i < n; i++)G[i].clear();
memset(deg, 0, sizeof(deg));
memset(Ans, 0, sizeof(Ans));</pre>
void add_edge(int u, int v) {
   if (S[make_pair(u, v)]) return;
     G[u].push_back(v);
     S[make_pair(u, v)] = 1;
     deg[v]++;
bool Toposort(int n) {
     int tot = 0; queue<int> que;
     for (int i = 0; i < n; ++i)
        if (deg[i] == 0) que.push(i);
     while (!que.empty()) {
         int v = que.front(); que.pop();
         Ans[tot++] = v;
for (int i = 0; i < G[v].size(); ++i) {
   int t = G[v][i];
   if (--deg[t] == 0) que.push(t);</pre>
     if (tot < n) return false;
     return true;
}
```

### 6 计算几何

#### 6.1 基本函数

```
#define eps 1e-8
#define pi M_PI
#define zero(x) ((fabs(x)<eps?1:0))</pre>
#define sgn(x) (fabs(x)<eps?0:((x)<0?-1:1))
#define mp make_pair
#define X first
#define Y second
struct point {
   double x, y;
   point(double a = 0, double b = 0) {x = a; y = b;}
point operator - (const point& b) const {
       return point(x - b.x, y - b.y);
   point operator + (const point &b) const {
      return point(x + b.x, y + b.y);
   // 两点是否重合
   bool operator == (point& b) {
       return zero(x - b.x) && zero(y - b.y);
   // 点积(以原点为基准)
   double operator * (const point &b) const {
      return x * b.x + y * b.y;
   // 叉积(以原点为基准)
   double operator ^ (const point &b) const {
  return x * b.y - y * b.x;
   // 绕P点逆时针旋转a弧度后的点
   point rotate(point b, double a) {
       double dx, dy; (*this - b).split(dx, dy);
double tx = dx * cos(a) - dy * sin(a);
double ty = dx * sin(a) + dy * cos(a);
return point(tx, ty) + b;
    // 点坐标分别赋值到a和b
   void split(double &a, double &b) {
       a = x; b = y;
};
struct line {
   point s, e;
    line() {}
   line(point ss, point ee) {s = ss; e = ee;}
};
6.2 位置关系
6.2.1 两点间距离
double dist(point a, point b) {
   return sqrt((a - b) * (a - b));
6.2.2 直线与直线的交点
// <0, *> 表示重合; <1, *> 表示平行; <2, P> 表示交点是P;
pair<int, point> spoint(line l1, line l2) {
   point res = l1.s;
   if (sgn((l1.s - l1.e) ^ (l2.s - l2.e)) == 0)
  return mp(sgn((l1.s - l2.e) ^ (l2.s - l2.e)) != 0, res);
   double t = ((l1.s - l2.s) \land (l2.s - l2.e)) / ((l1.s - l1.e) \land (l2.s - l2.e));
   res.x += (11.e.x - 11.s.x) * t;
```

```
res.y += (l1.e.y - l1.s.y) * t;
    return mp(2, res);
6.2.3 判断线段与线段相交
bool segxseg(line l1, line l2) {
    return
        max(l1.s.x, l1.e.x) >= min(l2.s.x, l2.e.x) &&
        max(12.s.x, 12.e.x) >= min(11.s.x, 11.e.x) &&
        max(l1.s.y, l1.e.y) >= min(l2.s.y, l2.e.y) &&
max(l2.s.y, l2.e.y) >= min(l1.s.y, l1.e.y) &&
sgn((l2.s - l1.e) ^ (l1.s - l1.e)) * sgn((l2.e-l1.e) ^ (l1.s - l1.e)) <= 0 &&
sgn((l1.s - l2.e) ^ (l2.s - l2.e)) * sgn((l1.e-l2.e) ^ (l2.s - l2.e)) <= 0;</pre>
}
6.2.4 判断线段与直线相交
bool segxline(line l1, line l2) {
    return sgn((l2.s - l1.e) ^ (l1.s - l1.e)) * sgn((l2.e-l1.e) ^ (l1.s - l1.e)) <= 0;
6.2.5 点到直线距离
point pointtoline(point P, line L) {
    point res;
    double t = ((P - L.s) * (L.e-L.s)) / ((L.e-L.s) * (L.e-L.s));
    res.x = L.s.x + (L.e.x - L.s.x) * t;
res.y = L.s.y + (L.e.y - L.s.y) * t;
return dist(P, res);
6.2.6 点到线段距离
point pointtosegment(point p, line l) {
    point res;
    double t = ((p - l.s) * (l.e-l.s)) / ((l.e-l.s) * (l.e-l.s));
    if (t >= 0 && t <= 1) {
   res.x = l.s.x + (l.e.x - l.s.x) * t;
   res.y = l.s.y + (l.e.y - l.s.y) * t;</pre>
    else res = dist(p, l.s) < dist(p, l.e) ? l.s : l.e;
    return res;
}
6.2.7 点在线段上
bool PointOnSeg(point p, line l) {
        sgn((l.s - p) \wedge (l.e-p)) == 0 \&\& sgn((p.x - l.s.x) * (p.x - l.e.x)) <= 0 \&\& sgn((p.y - l.s.y) * (p.y - l.e.y)) <= 0;
}
       多边形
6.3
6.3.1 多边形面积
double area(point p[], int n) {
    double res = 0;
    for (int i = 0; i < n; i++)
res += (p[i] ^ p[(i + 1) % n]) / 2;
    return fabs(res);
}
```

#### 6.3.2 点在凸多边形内

```
// 点形成一个凸包,而且按逆时针排序(如果是顺时针把里面的<0改为>0)
// 点的编号: [0,n)
// -1: 点在凸多边形外
// 0: 点在凸多边形边界上
// 1: 点在凸多边形内
int PointInConvex(point a, point p[], int n) {
   for (int i = 0; i < n; i++) {
      if (sgn((p[i] - a) ^ (p[(i + 1) % n] - a)) < 0)</pre>
         return -1;
      else if (PointOnSeg(a, line(p[i], p[(i + 1) % n])))
   return 1;
6.3.3 点在任意多边形内
// 射线法,poly[]的顶点数要大于等于3,点的编号0~n-1
// -1: 点在凸多边形外
// 0: 点在凸多边形边界上
// 1: 点在凸多边形内
int PointInPoly(point p, point poly[], int n) {
   int cnt;
   line ray, side;
   cnt = 0;
   ray.s = p;
   ray.e.y = p.y;
   for (int i = 0; i < n; i++) {
      side.s = poly[i];
      side.e = poly[(i + 1) % n];
      if (PointOnSeg(p, side))return 0;
      //如果平行轴则不考虑
      if (sgn(side.s.y - side.e.y) == 0)
         continue;
      if (PointOnSeg(sid e.s, r ay)) {
         if (sgn(side.s.y - side.e.y) > 0) cnt++;
      else if (PointOnSeg(side.e, ray)) {
         if (sgn(side.e.y - side.s.y) > 0) cnt++;
      else if (segxseg(ray, side)) cnt++;
   return cnt % 2 == 1 ? 1 : -1;
6.3.4 判断凸多边形
//点可以是顺时针给出也可以是逆时针给出
//点的编号1~n-1
bool isconvex(point poly[], int n) {
   bool s[3];
   set(s, 0);
   for (int \ i = 0; \ i < n; \ i++) \{ s[sgn((poly[(i + 1) \% n] - poly[i]) \land (poly[(i + 2) \% n] - poly[i]) ) + 1] = 1;
      if (s[0] && s[2]) return 0;
   return 1;
}
      整数点问题
6.4
6.4.1 线段上整点个数
int OnSegment(line 1) {
   return __gcd(fabs(l.s.x - l.e.x), fabs(l.s.y - l.e.y)) + 1;
```

#### 6.4.2 多边形边上整点个数

```
int OnEdge(point p[], int n) {
    int i, ret = 0;
    for (i = 0; i < n; i++)
        ret += __gcd(fabs(p[i].x - p[(i + 1) % n].x), fabs(p[i].y - p[(i + 1) % n].y));
    return ret;
}

6.4.3 多边形内整点个数
int InSide(point p[], int n) {
    int i, area = 0;
    for (i = 0; i < n; i++)
        area += p[(i + 1) % n].y * (p[i].x - p[(i + 2) % n].x);
    return (fabs(area) - OnEdge(n, p)) / 2 + 1;
}

6.5 圆
6.5.1 过三点求圆心

point waixin(point a, point b, point c) {
    double a1 = b.x - a.x, b1 = b.y - a.y, c1 = (a1 * a1 + b1 * b1) / 2;
    double a2 = c.x - a.x, b2 = c.y - a.y, c2 = (a2 * a2 + b2 * b2) / 2;
    double d = a1 * b2 - a2 * b1;
    return point(a.x + (c1 * b2 - c2 * b1) / d, a.y + (a1 * c2 - a2 * c1) / d);</pre>
```

### 7 动态规划

#### 7.1 子序列

#### 7.1.1 最大子序列和

```
// 传入序列a和长度n, 返回最大子序列和
// 限制最短长度:用cnt记录长度, rt更新时判断
int MaxSeqSum(int a[], int n) {
   int rt = 0, cur = 0;
   for (int i = 0; i < n; i++) {
      cur += a[i];
      rt = rt < cur ? cur : rt;
      cur = cur < 0 ? 0 : cur;
   }
   return rt;
}</pre>
```

#### 7.1.2 最长上升子序列 LIS

```
// 序列下标从1开始, LIS()返回长度, 序列存在lis[]中
#define N 100100
int n, len, a[N], b[N], f[N];
int Find(int p, int l, int r) {
    int mid;
    while (l \ll r) {
        mid = (l + r) >> 1;
if (a[p] > b[mid]) l = mid + 1;
        else r = mid - 1;
    }
    return f[p] = 1;
int LIS(int lis[]) {
int len = 1;
f[1] = 1;
b[1] = a[1];
    for (int i = 2; i <= n; i++) {
   if (a[i] > b[len]) b[++len] = a[i], f[i] = len;
   else b[Find(i, 1, len)] = a[i];
    for (int i = n, t = len; i >= 1 && t >= 1; i--)
        if (f[i] == t)
            lis[--t] = a[i];
    return len;
}
```

#### 7.1.3 最长公共上升子序列 LCIS

```
// 序列下标从1开始
int LCIS(int a[], int b[], int n, int m) {
    set(dp, 0);
    for (int i = 1; i <= n; i++) {
        int ma = 0;
        for (int j = 1; j <= m; j++) {
            dp[i][j] = dp[i - 1][j];
            if (a[i] > b[j]) ma = max(ma, dp[i - 1][j]);
            if (a[i] == b[j]) dp[i][j] = ma + 1;
        }
    }
    return *max_element(dp[n] + 1, dp[n] + 1 + m);
}
```

### 8 其他

#### 8.1 矩阵

```
typedef long long ll;
#define REP(i,n) for(int i=0;i<n;i++)</pre>
const ll mod = 1000000007;
class Matrix {
private:
    int r, c;
    11 **m;
public:
    Matrix(int R, int C): r(R), c(C) {
    m = new ll*[r];
    REP(i, r) m[i] = new ll[c];
    REP(i, r) REP(j, c) m[i][j] = 0;
    Matrix(const Matrix& B) {
        r = B.r; c = B.c; m = new ll*[r];
REP(i, r) m[i] = new ll[c];
        REP(i, r) REP(j, c) m[i][j] = B.m[i][j];
    ~Matrix() {REP(i, r) delete[] m[i]; delete[] m;}
void e() {REP(i, r) REP(j, c) m[i][j] = !(i ^ j);}
ll* operator [] (int p) {return m[p];}
ll* operator [] (int p) const {return m[p];}
    Matrix& operator = (const Matrix& B) {
        r = B.r; c = B.c; this->~Matrix(); m = new ll*[r];

REP(i, r) m[i] = new ll[c];

REP(i, r) REP(j, c) m[i][j] = B[i][j];
         return *this;
    Matrix operator * (const Matrix& B) const {
        Matrix rt(r, B.c);
REP(i, r) REP(k, c) if (m[i][k] != 0) REP(j, B.c)
             rt[i][j] = (rt[i][j] + m[i][k] * B[k][j] % mod) % mod;
         return rt;
    Matrix operator ^ (ll n) {
        Matrix rt(r, c); rt.e();
         Matrix ba(*this);
        while (n) {
   if (n & 1) rt = rt * ba;
             ba = ba * ba;
             n >>= 1;
         return rt;
     void out() {
        REP(i, r) REP(j, c)
cout << m[i][j] << (j == c - 1 ? '\n' : ' ');
         cout << endl;</pre>
};
8.2
         高精度
// 加法 乘法 小于号 输出
struct bint {
    int l; short int w[100];
    bint(int x = 0) {
        l = x == 0; memset(w, 0, sizeof(w));
while (x != 0) {w[l++] = x % 10; x /= 10;}
    bool operator < (const bint& x) const {</pre>
        if (l != x.l) return l < x.l;</pre>
        int i = l - 1;
while (i >= 0 && w[i] == x.w[i]) i--;
         return (i >= 0 && \bar{w}[\bar{i}] < x.w[i]);
    bint operator + (const bint& x) const {
```

```
bint ans; ans.l = l > x.l ? l : x.l;
for (int i = 0; i < ans.l; i++) {
    ans.w[i] += w[i] + x.w[i];
    ans.w[i + 1] += ans.w[i] / 10;
    ans.w[i] = ans.w[i] % 10;
}
if (ans.w[ans.l] != 0) ans.l++;
return ans;
}
bint operator * (const bint& x) const {
    bint res; int up, tmp;
    for (int i = 0; i < l; i++) {
        up = 0;
        for (int j = 0; j < x.l; j++) {
            tmp = w[i] * x.w[j] + res.w[i + j] + up;
            res.w[i + j] = tmp % 10;
            up = tmp / 10;
        }
    if (up != 0) res.w[i + x.l] = up;
    } res.l = l + x.l;
    while (res.w[res.l - 1] == 0 && res.l > 1) res.l--;
    return res;
}
void print() {
    for (int i = l - 1; i >= 0 ; i--)
printf("%d", w[i]);
    printf("\n");
}
};
```