



link i	θ_i	d_i	a_i	α_i
1	q_1	L_1	0	$\frac{\pi}{2}$
2	$-\frac{\pi}{2} + q_2$	L_7	L_3	$-\pi$
3	$-\frac{\pi}{2} + q_3$	$L_7 - L_1$	0	$\frac{\pi}{2}$
4	$\frac{\pi}{2} + q_4$	$L_5 - L_{12}$	$L_2 - L_{11}$	0
5	$-\frac{\pi}{2} + q_5$	L_{12}	0	$\frac{\pi}{2}$
cf	$0 + q_6$	$L_4 + L_{13}$	0	0
cm1	$0 + q_1$	0	0	0
cm2	$-\frac{\pi}{2} + q_2$	L_7	L_8	0
cm3	$0 + q_3$	$L_7 - L_{11} - L_9$	L_{10}	0

Figure 3.1: 3DOF robot.

3 DOF Jacobian

$$J_{cm1} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} \quad \begin{matrix} & & 0 & 0 \end{matrix}$$

其中

$$\begin{cases} x_{cm2} = L_7 \cdot \sin q_1 - L_8 \sin q_2 \cdot \cos q_1 \\ y_{cm2} = -(L_7 \cdot \cos q_1 + L_8 \sin q_2 \cdot \sin q_1) \\ z_{cm2} = L_6 + L_8 \cos q_2 \end{cases}$$

$$\begin{cases} x_{cm3} = L_{11} \sin q_1 - L_3 \sin q_2 \cos q_1 + L_{10} \sin q_3 \cos q_1 \\ y_{cm3} = -L_3 \sin q_2 \cdot \sin q_1 - L_{11} \cos q_1 + L_{10} \sin q_3 \sin q_1 \\ z_{cm3} = L_6 + L_3 \cos q_2 + L_{10} \cos q_3 \end{cases}$$

$$J_{cm2} = \begin{bmatrix} -y_{cm2} & -\cos q_1 \cdot (z_{cm2} - L_6) \\ -x_{cm2} & \sin q_1 \cdot (z_{cm2} - L_6) \\ 0 & \sin q_1 y_{cm2} + \cos q_1 x_{cm2} & 0 \\ 0 & \sin q_1 \\ 0 & -\cos q_1 \\ 1 & 0 \end{bmatrix}$$

$$J_{cm3} = \begin{bmatrix} -y_{cm3} & -\cos q_1 \cdot (z_{cm3} - L_6) & \cos q_1 \cdot L_{10} \cos q_3 \\ -x_{cm3} & \sin q_1 \cdot (z_{cm3} - L_6) & -\sin q_1 \cdot L_{10} \cos q_3 \\ 0 & \sin q_1 y_{cm3} + \cos q_1 x_{cm3} & -\sin q_1 \cdot [(L_7 - L_{11}) \cos q_1 + L_{10} \sin q_3 \cdot \sin q_1] - \cos q_1 \cdot [L_{10} \sin q_3 \cdot \cos q_1 - (L_7 - L_{11}) \sin q_1] \\ 0 & \sin q_1 & -\sin q_1 \\ 0 & -\cos q_1 & \cos q_1 \\ 1 & 0 & 0 \end{bmatrix}$$