# exploring\_word\_vectors

August 20, 2024

# 1 CS224N Assignment 1: Exploring Word Vectors (25 Points)

#### 1.0.1 Due 3:15pm, Tue Jan 16 2024

Welcome to CS224N!

Before you start, make sure you read the README.md in the same directory as this notebook for important setup information. A lot of code is provided in this notebook, and we highly encourage you to read and understand it as part of the learning:)

If you aren't super familiar with Python, Numpy, or Matplotlib, we recommend you check out the review session on Friday. The session will be recorded and the material will be made available on our website. The CS231N Python/Numpy tutorial is also a great resource.

**Assignment Notes:** Please make sure to save the notebook as you go along. Submission Instructions are located at the bottom of the notebook.

```
[1]: # All Import Statements Defined Here
     # Note: Do not add to this list.
     # -----
     import sys
     assert sys.version info[0] == 3
     assert sys.version info[1] >= 8
     from platform import python version
     assert int(python_version().split(".")[1]) >= 5, "Please upgrade your Python⊔
      ⇔version following the instructions in \
        the README.md file found in the same directory as this notebook. Your_{\sqcup}
      →Python version is " + python_version()
     from gensim.models import KeyedVectors
     from gensim.test.utils import datapath
     import pprint
     import matplotlib.pyplot as plt
     plt.rcParams['figure.figsize'] = [10, 5]
     import nltk
     nltk.download('reuters') #to specify download location, optionally add the
      →argument: download_dir='/specify/desired/path/'
```

```
[nltk_data] Downloading package reuters to
[nltk_data] /Users/runqiuye/nltk_data...
[nltk_data] Package reuters is already up-to-date!
```

#### 1.1 Word Vectors

Word Vectors are often used as a fundamental component for downstream NLP tasks, e.g. question answering, text generation, translation, etc., so it is important to build some intuitions as to their strengths and weaknesses. Here, you will explore two types of word vectors: those derived from co-occurrence matrices, and those derived via GloVe.

**Note on Terminology:** The terms "word vectors" and "word embeddings" are often used interchangeably. The term "embedding" refers to the fact that we are encoding aspects of a word's meaning in a lower dimensional space. As Wikipedia states, "conceptually it involves a mathematical embedding from a space with one dimension per word to a continuous vector space with a much lower dimension".

## 1.2 Part 1: Count-Based Word Vectors (10 points)

Most word vector models start from the following idea:

You shall know a word by the company it keeps (Firth, J. R. 1957:11)

Many word vector implementations are driven by the idea that similar words, i.e., (near) synonyms, will be used in similar contexts. As a result, similar words will often be spoken or written along with a shared subset of words, i.e., contexts. By examining these contexts, we can try to develop embeddings for our words. With this intuition in mind, many "old school" approaches to constructing word vectors relied on word counts. Here we elaborate upon one of those strategies, co-occurrence matrices (for more information, see here or here).

#### 1.2.1 Co-Occurrence

A co-occurrence matrix counts how often things co-occur in some environment. Given some word  $w_i$  occurring in the document, we consider the *context window* surrounding  $w_i$ . Supposing our fixed window size is n, then this is the n preceding and n subsequent words in that document,

i.e. words  $w_{i-n} \dots w_{i-1}$  and  $w_{i+1} \dots w_{i+n}$ . We build a co-occurrence matrix M, which is a symmetric word-by-word matrix in which  $M_{ij}$  is the number of times  $w_j$  appears inside  $w_i$ 's window among all documents.

#### Example: Co-Occurrence with Fixed Window of n=1:

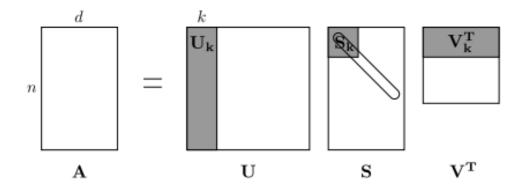
Document 1: "all that glitters is not gold"

Document 2: "all is well that ends well"

*	<staf< th=""><th>RT&gt; all</th><th>that</th><th>glitters</th><th>is</th><th>not</th><th>gold</th><th>well</th><th>ends</th><th><end></end></th></staf<>	RT> all	that	glitters	is	not	gold	well	ends	<end></end>
<start></start>	0	2	0	0	0	0	0	0	0	0
all	2	0	1	0	1	0	0	0	0	0
that	0	1	0	1	0	0	0	1	1	0
glitters	0	0	1	0	1	0	0	0	0	0
is	0	1	0	1	0	1	0	1	0	0
not	0	0	0	0	1	0	1	0	0	0
gold	0	0	0	0	0	1	0	0	0	1
well	0	0	1	0	1	0	0	0	1	1
ends	0	0	1	0	0	0	0	1	0	0
<end></end>	0	0	0	0	0	0	1	1	0	0

Note: In NLP, we often add <START> and <END> tokens to represent the beginning and end of sentences, paragraphs or documents. In this case we imagine <START> and <END> tokens encapsulating each document, e.g., "<START> All that glitters is not gold <END>", and include these tokens in our co-occurrence counts.

The rows (or columns) of this matrix provide one type of word vectors (those based on word-word co-occurrence), but the vectors will be large in general (linear in the number of distinct words in a corpus). Thus, our next step is to run dimensionality reduction. In particular, we will run SVD (Singular Value Decomposition), which is a kind of generalized PCA (Principal Components Analysis) to select the top k principal components. Here's a visualization of dimensionality reduction with SVD. In this picture our co-occurrence matrix is A with n rows corresponding to n words. We obtain a full matrix decomposition, with the singular values ordered in the diagonal S matrix, and our new, shorter length-k word vectors in  $U_k$ .



This reduced-dimensionality co-occurrence representation preserves semantic relationships between words, e.g. doctor and hospital will be closer than doctor and dog.

Notes: If you can barely remember what an eigenvalue is, here's a slow, friendly introduction to SVD. If you want to learn more thoroughly about PCA or SVD, feel free to check out lectures 7, 8, and 9 of CS168. These course notes provide a great high-level treatment of these general purpose algorithms. Though, for the purpose of this class, you only need to know how to extract the k-dimensional embeddings by utilizing pre-programmed implementations of these algorithms from the numpy, scipy, or sklearn python packages. In practice, it is challenging to apply full SVD to large corpora because of the memory needed to perform PCA or SVD. However, if you only want the top k vector components for relatively small k— known as Truncated SVD— then there are reasonably scalable techniques to compute those iteratively.

#### 1.2.2 Plotting Co-Occurrence Word Embeddings

Here, we will be using the Reuters (business and financial news) corpus. If you haven't run the import cell at the top of this page, please run it now (click it and press SHIFT-RETURN). The corpus consists of 10,788 news documents totaling 1.3 million words. These documents span 90 categories and are split into train and test. For more details, please see https://www.nltk.org/book/ch02.html. We provide a read\_corpus function below that pulls out only articles from the "gold" (i.e. news articles about gold, mining, etc.) category. The function also adds <START> and <END> tokens to each of the documents, and lowercases words. You do not have to perform any other kind of pre-processing.

```
[2]: def read_corpus(category="gold"):
    """ Read files from the specified Reuter's category.
    Params:
        category (string): category name
    Return:
        list of lists, with words from each of the processed files
    """
    files = reuters.fileids(category)
    return [[START_TOKEN] + [w.lower() for w in list(reuters.words(f))] + \
        [END_TOKEN] for f in files]
```

Let's have a look what these documents are like....

```
[3]: reuters_corpus = read_corpus()
pprint.pprint(reuters_corpus[:3], compact=True, width=100)
```

```
[['<START>', 'western', 'mining', 'to', 'open', 'new', 'gold', 'mine', 'in',
   'australia', 'western',
   'mining', 'corp', 'holdings', 'ltd', '&', 'lt', ';', 'wmng', '.', 's', '>',
   '(', 'wmc', ')',
   'said', 'it', 'will', 'establish', 'a', 'new', 'joint', 'venture', 'gold',
   'mine', 'in', 'the',
   'northern', 'territory', 'at', 'a', 'cost', 'of', 'about', '21', 'mln',
   'dlrs', '.', 'the',
   'mine', ',', 'to', 'be', 'known', 'as', 'the', 'goodall', 'project', ',',
```

```
'will', 'be', 'owned',
  '60', 'pct', 'by', 'wmc', 'and', '40', 'pct', 'by', 'a', 'local', 'w', '.',
'r', '.', 'grace',
  'and', 'co', '&', 'lt', ';', 'gra', '>', 'unit', '.', 'it', 'is', 'located',
'30', 'kms', 'east',
  'of', 'the', 'adelaide', 'river', 'at', 'mt', '.', 'bundey', ',', 'wmc',
'said', 'in', 'a',
  'statement', 'it', 'said', 'the', 'open', '-', 'pit', 'mine', ',', 'with',
'a', 'conventional',
  'leach', 'treatment', 'plant', ',', 'is', 'expected', 'to', 'produce',
'about', '50', ',', '000',
  'ounces', 'of', 'gold', 'in', 'its', 'first', 'year', 'of', 'production',
'from', 'mid', '-',
  '1988', '.', 'annual', 'ore', 'capacity', 'will', 'be', 'about', '750', ',',
'000', 'tonnes', '.',
  '<END>'],
 ['<START>', 'belgium', 'to', 'issue', 'gold', 'warrants', ',', 'sources',
'say', 'belgium',
  'plans', 'to', 'issue', 'swiss', 'franc', 'warrants', 'to', 'buy', 'gold',
',', 'with', 'credit',
  'suisse', 'as', 'lead', 'manager', ',', 'market', 'sources', 'said', '.',
'no', 'confirmation',
  'or', 'further', 'details', 'were', 'immediately', 'available', '.', '<END>'],
['<START>', 'belgium', 'launches', 'bonds', 'with', 'gold', 'warrants', 'the',
'kingdom', 'of',
  'belgium', 'is', 'launching', '100', 'mln', 'swiss', 'francs', 'of', 'seven',
'year', 'notes',
  'with', 'warrants', 'attached', 'to', 'buy', 'gold', ',', 'lead', 'mananger',
'credit', 'suisse',
  'said', '.', 'the', 'notes', 'themselves', 'have', 'a', '3', '-', '3', '/',
'8', 'pct', 'coupon',
  'and', 'are', 'priced', 'at', 'par', '.', 'payment', 'is', 'due', 'april',
'30', ',', '1987',
  'and', 'final', 'maturity', 'april', '30', ',', '1994', '.', 'each', '50',
',', '000', 'franc',
  'note', 'carries', '15', 'warrants', '.', 'two', 'warrants', 'are',
'required', 'to', 'allow',
  'the', 'holder', 'to', 'buy', '100', 'grammes', 'of', 'gold', 'at', 'a',
'price', 'of', '2', ',',
  '450', 'francs', ',', 'during', 'the', 'entire', 'life', 'of', 'the', 'bond',
'.', 'the',
 'latest', 'gold', 'price', 'in', 'zurich', 'was', '2', ',', '045', '/', '2',
',', '070', 'francs',
  'per', '100', 'grammes', '.', '<END>']]
```

#### 1.2.3 Question 1.1: Implement distinct words [code] (2 points)

Write a method to work out the distinct words (word types) that occur in the corpus.

You can use for loops to process the input corpus (a list of list of strings), but try using Python list comprehensions (which are generally faster). In particular, this may be useful to flatten a list of lists. If you're not familiar with Python list comprehensions in general, here's more information.

Your returned corpus\_words should be sorted. You can use python's sorted function for this.

You may find it useful to use Python sets to remove duplicate words.

```
[4]: def distinct_words(corpus):
         """ Determine a list of distinct words for the corpus.
             Params:
                 corpus (list of list of strings): corpus of documents
             Return:
                 corpus_words (list of strings): sorted list of distinct words⊔
      ⇔across the corpus
                 n corpus words (integer): number of distinct words across the corpus
         11 11 11
        corpus_words = []
        n_corpus_words = -1
         # -----
         # Write your implementation here.
        S = set()
        for sublist in corpus:
            S = S.union(sublist)
        corpus_words = list(S)
        corpus words.sort()
        n_corpus_words = len(S)
        return corpus_words, n_corpus_words
```

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Passed All Tests!

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#### 1.2.4 Question 1.2: Implement compute\_co\_occurrence\_matrix [code] (3 points)

Write a method that constructs a co-occurrence matrix for a certain window-size n (with a default of 4), considering words n before and n after the word in the center of the window. Here, we start to use numpy (np) to represent vectors, matrices, and tensors. If you're not familiar with NumPy, there's a NumPy tutorial in the second half of this cs231n Python NumPy tutorial.

```
[6]: def compute_co_occurrence_matrix(corpus, window_size=4):
          """ Compute co-occurrence matrix for the given corpus and window_size_{\sqcup}
      \hookrightarrow (default of 4).
              Note: Each word in a document should be at the center of a window. \Box
      \hookrightarrow Words near edges will have a smaller
                    number of co-occurring words.
                    For example, if we take the document "<START> All that glitters_{\sqcup}
      ⇒is not gold <END>" with window size of 4,
                    "All" will co-occur with "<START>", "that", "qlitters", "is", and
      ⇔"not".
              Params:
                  corpus (list of list of strings): corpus of documents
                  window_size (int): size of context window
                  M (a symmetric numpy matrix of shape (number of unique words in the \Box
      ⇔corpus , number of unique words in the corpus)):
                      Co-occurence matrix of word counts.
```

```
The ordering of the words in the rows/columns should be the ...
same as the ordering of the words given by the distinct words function.
          word2ind (dict): dictionary that maps word to index (i.e. row/
⇔column number) for matrix M.
  words, n_words = distinct_words(corpus)
  M = None
  word2ind = {}
  # -----
  # Write your implementation here.
  M = np.zeros((n words, n words))
  for i in range(n_words):
      word2ind[words[i]] = i
  for document in corpus:
      doc len = len(document)
      for center_loc in range(doc_len):
          center = document[center_loc]
          i = word2ind[center]
          for context_loc in range(max(0, center_loc - window_size),__
context = document[context loc]
              j = word2ind[context]
              M[i][j] += 1
          for context_loc in range(center_loc + 1, min(doc_len, center_loc +__
→window size + 1)):
              context = document[context_loc]
              j = word2ind[context]
              M[i][j] += 1
  # -----
  return M, word2ind
```

```
M_test_ans = np.array(
    [[0., 0., 0., 0., 0., 0., 1., 0., 0., 1.,],
     [0., 0., 1., 1., 0., 0., 0., 0., 0., 0., ],
     [0., 1., 0., 0., 0., 0., 0., 0., 1., 0.,],
     [0., 1., 0., 0., 0., 0., 0., 0., 1.,],
     [0., 0., 0., 0., 0., 0., 0., 0., 1., 1.,],
     [0., 0., 0., 0., 0., 0., 0., 1., 1., 0.,],
     [1., 0., 0., 0., 0., 0., 0., 1., 0., 0.,],
     [0., 0., 0., 0., 0., 1., 1., 0., 0., 0.,],
     [0., 0., 1., 0., 1., 1., 0., 0., 0., 1.,],
     [1., 0., 0., 1., 1., 0., 0., 0., 1., 0.,]]
ans_test_corpus_words = sorted([START_TOKEN, "All", "ends", "that", "gold", "
→"All's", "glitters", "isn't", "well", END_TOKEN])
word2ind_ans = dict(zip(ans_test_corpus_words,__
 →range(len(ans_test_corpus_words))))
# Test correct word2ind
assert (word2ind_ans == word2ind_test), "Your word2ind is incorrect:\nCorrect:\_
 →{}\nYours: {}".format(word2ind_ans, word2ind_test)
# Test correct M shape
assert (M_test.shape == M_test_ans.shape), "M matrix has incorrect shape.
 →\nCorrect: {}\nYours: {}".format(M_test.shape, M_test_ans.shape)
# Test correct M values
for w1 in word2ind_ans.keys():
    idx1 = word2ind_ans[w1]
    for w2 in word2ind_ans.keys():
        idx2 = word2ind_ans[w2]
        student = M_test[idx1, idx2]
        correct = M_test_ans[idx1, idx2]
        if student != correct:
            print("Correct M:")
            print(M test ans)
            print("Your M: ")
            print(M_test)
            raise AssertionError("Incorrect count at index ({}, {})=({}, {}) in

∪
 ⇒matrix M. Yours has {} but should have {}.".format(idx1, idx2, w1, w2, ⊔
 ⇔student, correct))
# Print Success
print ("-" * 80)
print("Passed All Tests!")
print ("-" * 80)
```

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Passed All Tests!

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#### 1.2.5 Question 1.3: Implement reduce\_to\_k\_dim [code] (1 point)

Construct a method that performs dimensionality reduction on the matrix to produce k-dimensional embeddings. Use SVD to take the top k components and produce a new matrix of k-dimensional embeddings.

**Note:** All of numpy, scipy, and scikit-learn (sklearn) provide *some* implementation of SVD, but only scipy and sklearn provide an implementation of Truncated SVD, and only sklearn provides an efficient randomized algorithm for calculating large-scale Truncated SVD. So please use sklearn.decomposition.TruncatedSVD.

```
[8]: def reduce to k dim(M, k=2):
         """ Reduce a co-occurence count matrix of dimensionality (num_corpus_words, __
      →num_corpus_words)
             to a matrix of dimensionality (num_corpus_words, k) using the following_
      \hookrightarrow SVD function from Scikit-Learn:
                  - http://scikit-learn.org/stable/modules/generated/sklearn.
      \neg decomposition. Truncated SVD. html
             Params:
                 M (numpy matrix of shape (number of unique words in the corpus ,_{\sqcup}
      ⇔number of unique words in the corpus)): co-occurence matrix of word counts
                  k (int): embedding size of each word after dimension reduction
             Return:
                 M_reduced (numpy matrix of shape (number of corpus words, k)):
      \negmatrix of k-dimensioal word embeddings.
                          In terms of the SVD from math class, this actually returns.
      \hookrightarrow U * S
         11 11 11
         n iters = 10
                          # Use this parameter in your call to `TruncatedSVD`
         M reduced = None
         print("Running Truncated SVD over %i words..." % (M.shape[0]))
         # -----
         # Write your implementation here.
         svd = TruncatedSVD(n_components=k, n_iter=n_iters)
         M_reduced = svd.fit_transform(M)
         print("Done.")
         return M_reduced
```

```
[9]:  # ------ # Run this sanity check
```

```
# Note that this is not an exhaustive check for correctness
# In fact we only check that your M reduced has the right dimensions.
# Define toy corpus and run student code
test_corpus = ["{} All that glitters isn't gold {}".format(START_TOKEN,__
 ⇔END_TOKEN).split(" "), "{} All's well that ends well {}".format(START_TOKEN, _
→END_TOKEN).split(" ")]
M_test, word2ind_test = compute_co_occurrence_matrix(test_corpus, window_size=1)
M_test_reduced = reduce_to_k_dim(M_test, k=2)
# Test proper dimensions
assert (M_test_reduced.shape[0] == 10), "M_reduced has {} rows; should have {}".
 →format(M_test_reduced.shape[0], 10)
assert (M_test_reduced.shape[1] == 2), "M_reduced has {} columns; should have_
→{}".format(M_test_reduced.shape[1], 2)
# Print Success
print("-" * 80)
print("Passed All Tests!")
print("-" * 80)
```

Running Truncated SVD over 10 words...

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Passed All Tests!

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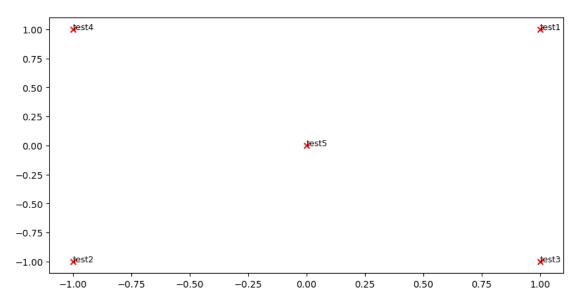
#### 1.2.6 Question 1.4: Implement plot\_embeddings [code] (1 point)

Here you will write a function to plot a set of 2D vectors in 2D space. For graphs, we will use Matplotlib (plt).

For this example, you may find it useful to adapt this code. In the future, a good way to make a plot is to look at the Matplotlib gallery, find a plot that looks somewhat like what you want, and adapt the code they give.

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#### Outputted Plot:



#### 1.2.7 Question 1.5: Co-Occurrence Plot Analysis [written] (3 points)

Now we will put together all the parts you have written! We will compute the co-occurrence matrix with fixed window of 4 (the default window size), over the Reuters "gold" corpus. Then we will use TruncatedSVD to compute 2-dimensional embeddings of each word. TruncatedSVD returns U\*S, so we need to normalize the returned vectors, so that all the vectors will appear around the unit circle (therefore closeness is directional closeness). **Note**: The line of code below that does the normalizing uses the NumPy concept of *broadcasting*. If you don't know about broadcasting, check out Computation on Arrays: Broadcasting by Jake VanderPlas.

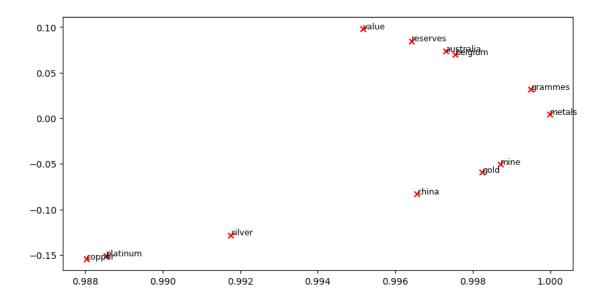
Run the below cell to produce the plot. It'll probably take a few seconds to run.

```
# Run This Cell to Produce Your Plot
# co-----
reuters_corpus = read_corpus()
M_co_occurrence, word2ind_co_occurrence = compute_co_occurrence = reduce_to_k_dim(M_co_occurrence, k=2)

# Rescale (normalize) the rows to make them each of unit-length
M_lengths = np.linalg.norm(M_reduced_co_occurrence, axis=1)
M_normalized = M_reduced_co_occurrence / M_lengths[:, np.newaxis] # broadcasting

words = ['value', 'gold', 'platinum', 'reserves', 'silver', 'metals', 'copper', copper', co
```

Running Truncated SVD over 2830 words... Done.



Verify that your figure matches "question\_1.5.png" in the assignment zip. If not, use the figure in "question\_1.5.png" to answer the next two questions.

a. Find at least two groups of words that cluster together in 2-dimensional embedding space. Give an explanation for each cluster you observe.

Write your answer here. "copper" and "platinum" cluster together in the 2d embedding space. This is because they are both metals.

"australia" and "belgium" cluster together in the 2d embedding space. This is because they are both country names.

b. What doesn't cluster together that you might think should have? Describe at least two examples.

Write your answer here. "silver" does not cluster with "copper" and "platinum" even though "silver" is also a metal, just like "copper" and "platinum".

"china" does not cluster with "australia" and "belgium" even though "china" is also a country name, just like "australia" and "belgium".

#### 1.3 Part 2: Prediction-Based Word Vectors (15 points)

As discussed in class, more recently prediction-based word vectors have demonstrated better performance, such as word2vec and GloVe (which also utilizes the benefit of counts). Here, we shall explore the embeddings produced by GloVe. Please revisit the class notes and lecture slides for more details on the word2vec and GloVe algorithms. If you're feeling adventurous, challenge yourself and try reading GloVe's original paper.

Then run the following cells to load the GloVe vectors into memory. **Note**: If this is your first time to run these cells, i.e. download the embedding model, it will take a couple minutes to run. If

you've run these cells before, rerunning them will load the model without redownloading it, which will take about 1 to 2 minutes.

Loaded vocab size 400000

Note: If you are receiving a "reset by peer" error, rerun the cell to restart the download.

#### 1.3.1 Reducing dimensionality of Word Embeddings

Let's directly compare the GloVe embeddings to those of the co-occurrence matrix. In order to avoid running out of memory, we will work with a sample of 10000 GloVe vectors instead. Run the following cells to:

- 1. Put 10000 Glove vectors into a matrix M
- 2. Run reduce\_to\_k\_dim (your Truncated SVD function) to reduce the vectors from 200-dimensional to 2-dimensional.

```
[21]: def get_matrix_of_vectors(wv_from_bin, required_words):
          """ Put the GloVe vectors into a matrix M.
              Param:
                  wv_from_bin: KeyedVectors object; the 400000 GloVe vectors loaded_
       ⇔from file
              Return:
                  M: numpy matrix shape (num words, 200) containing the vectors
                  word2ind: dictionary mapping each word to its row number in M
          11 11 11
          import random
          words = list(wv_from_bin.index_to_key)
          print("Shuffling words ...")
          random.seed(225)
          random.shuffle(words)
          words = words[:10000]
          print("Putting %i words into word2ind and matrix M..." % len(words))
          word2ind = {}
          M = []
          curInd = 0
          for w in words:
```

```
try:
        M.append(wv_from_bin.get_vector(w))
        word2ind[w] = curInd
        curInd += 1
    except KeyError:
        continue
for w in required words:
    if w in words:
        continue
    try:
        M.append(wv_from_bin.get_vector(w))
        word2ind[w] = curInd
        curInd += 1
    except KeyError:
        continue
M = np.stack(M)
print("Done.")
return M, word2ind
```

Shuffling words ...
Putting 10000 words into word2ind and matrix M...
Done.
Running Truncated SVD over 10012 words...
Done.

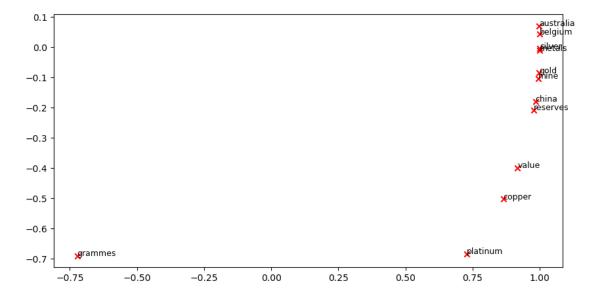
Note: If you are receiving out of memory issues on your local machine, try closing other applications to free more memory on your device. You may want to try restarting your machine so that you can free up extra memory. Then immediately run the jupyter notebook and see if you can load the word vectors properly. If you still have problems with loading the embeddings onto your local machine after this, please go to office hours or contact course staff.

# 1.3.2 Question 2.1: GloVe Plot Analysis [written] (3 points)

```
Run the cell below to plot the 2D GloVe embeddings for ['value', 'gold', 'platinum', 'reserves', 'silver', 'metals', 'copper', 'belgium', 'australia', 'china', 'grammes', "mine"].
```

```
[23]: words = ['value', 'gold', 'platinum', 'reserves', 'silver', 'metals', 'copper', \( \times'\) belgium', 'australia', 'china', 'grammes', "mine"]

plot_embeddings(M_reduced_normalized, word2ind, words)
```



Verify that your figure matches "question\_2.1.png" in the assignment zip. If not, use the figure in "question\_2.1.png" (and the figure in "question\_1.5.png", if applicable) to answer the next two questions.

a. What is one way the plot is different from the one generated earlier from the co-occurrence matrix? What is one way it's similar?

Write your answer here. The plot is similar in terms of that it also clusters words that has similar meaning.

The plot generated by GloVe is different in terms of that it has linear structure in the vector space.

b. Why might the GloVe plot (question\_2.1.png) differ from the plot generated earlier from the co-occurrence matrix (question\_1.5.png)?

Write your answer here. The co-occurrence only take advantage of global statistics, while GloVe on top of that, take local context into account. This helps generate a linear structure in the embedding vector space.

#### 1.3.3 Cosine Similarity

Now that we have word vectors, we need a way to quantify the similarity between individual words, according to these vectors. One such metric is cosine-similarity. We will be using this to find words that are "close" and "far" from one another.

We can think of n-dimensional vectors as points in n-dimensional space. If we take this perspective L1 and L2 Distances help quantify the amount of space "we must travel" to get between these two points. Another approach is to examine the angle between two vectors. From trigonometry we know that:

Instead of computing the actual angle, we can leave the similarity in terms of  $similarity = cos(\Theta)$ . Formally the Cosine Similarity s between two vectors p and q is defined as:

$$s = \frac{p \cdot q}{||p||||q||}, \text{ where } s \in [-1, 1]$$

## 1.3.4 Question 2.2: Words with Multiple Meanings (1.5 points) [code + written]

Polysemes and homonyms are words that have more than one meaning (see this wiki page to learn more about the difference between polysemes and homonyms). Find a word with at least two different meanings such that the top-10 most similar words (according to cosine similarity) contain related words from both meanings. For example, "leaves" has both "go\_away" and "a\_structure\_of\_a\_plant" meaning in the top 10, and "scoop" has both "handed\_waffle\_cone" and "lowdown". You will probably need to try several polysemous or homonymic words before you find one.

Please state the word you discover and the multiple meanings that occur in the top 10. Why do you think many of the polysemous or homonymic words you tried didn't work (i.e. the top-10 most similar words only contain **one** of the meanings of the words)?

Note: You should use the wv\_from\_bin.most\_similar(word) function to get the top 10 similar words. This function ranks all other words in the vocabulary with respect to their cosine similarity to the given word. For further assistance, please check the **GenSim documentation**.

```
[('ends', 0.6128067970275879), ('leaf', 0.6027014851570129), ('stems',
0.5998532772064209), ('takes', 0.5902854800224304), ('leaving',
0.5761634111404419), ('grows', 0.5663397312164307), ('flowers',
0.5600922703742981), ('turns', 0.5536050796508789), ('leave',
0.5496847629547119), ('goes', 0.5434925556182861)]
[('banks', 0.7625692486763), ('banking', 0.6818838119506836), ('central',
0.6283639073371887), ('financial', 0.6166563034057617), ('credit',
0.6049750447273254), ('lending', 0.5980608463287354), ('monetary',
0.5963003635406494), ('bankers', 0.5913101434707642), ('loans',
0.5802940130233765), ('investment', 0.574020266532898)]
[('bright', 0.6242774724960327), ('dark', 0.6141001582145691), ('lights',
0.6013951897621155), ('lighter', 0.5581753253936768), ('heavy',
```

```
0.5408365726470947), ('sunlight', 0.5362918972969055), ('blue',
0.5349379777908325), ('colored', 0.5282375812530518), ('sky',
0.5239452719688416), ('color', 0.513929009437561)]
[('hits', 0.7869389653205872), ('hitting', 0.783338725566864), ('struck',
0.7397956848144531), ('off', 0.6183231472969055), ('single',
0.5938534736633301), ('out', 0.5775773525238037), ('came', 0.5734131932258606),
('got', 0.5691716074943542), ('went', 0.561163067817688), ('shot',
0.5591346621513367)]
```

Write your answer here. "light" has multiple meanings that occur in the top 10 — it can represent both opposite of heavy and opposite of dark.

"hit" has multiple meaning that occur in the top 10 — it can represent both strike with object and baseball term.

Many of the polysemous or homonymic words do not work since one meaning is much more common than the other.

# 1.3.5 Question 2.3: Synonyms & Antonyms (2 points) [code + written]

When considering Cosine Similarity, it's often more convenient to think of Cosine Distance, which is simply 1 - Cosine Similarity.

Find three words  $(w_1, w_2, w_3)$  where  $w_1$  and  $w_2$  are synonyms and  $w_1$  and  $w_3$  are antonyms, but Cosine Distance  $(w_1, w_3) <$  Cosine Distance  $(w_1, w_2)$ .

As an example,  $w_1$ ="happy" is closer to  $w_3$ ="sad" than to  $w_2$ ="cheerful". Please find a different example that satisfies the above. Once you have found your example, please give a possible explanation for why this counter-intuitive result may have happened.

You should use the the wv\_from\_bin.distance(w1, w2) function here in order to compute the cosine distance between two words. Please see the **GenSim documentation** for further assistance.

```
[35]: # ------
# Write your implementation here.
print(wv_from_bin.distance("sad", "happy"))
print(wv_from_bin.distance("sad", "blue"))
# -------
```

- 0.4040136933326721
- 0.7740493416786194

Write your answer here. In the example above, "sad" and "happy" are antonyms, and "sad" and "blue" are synonyms. However, the consine distance between "sad" and "happy" is smaller than the cosine distance between "sad" and "blue". A possible explanation for this is that "blue" is not most used to represent sadness, instead its most common meaning is a color. Hence, "blue" may have another component that is far from "sad".

#### 1.3.6 Question 2.4: Analogies with Word Vectors [written] (1.5 points)

Word vectors have been shown to *sometimes* exhibit the ability to solve analogies.

As an example, for the analogy "man: grandfather: woman: x" (read: man is to grandfather as woman is to x), what is x?

In the cell below, we show you how to use word vectors to find x using the most\_similar function from the **GenSim documentation**. The function finds words that are most similar to the words in the positive list and most dissimilar from the words in the negative list (while omitting the input words, which are often the most similar; see this paper). The answer to the analogy will have the highest cosine similarity (largest returned numerical value).

```
[19]: # Run this cell to answer the analogy -- man : grandfather :: woman : x

pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'grandfather'],

onegative=['man']))
```

```
[('grandmother', 0.7608445882797241),
  ('granddaughter', 0.7200807929039001),
  ('daughter', 0.7168301939964294),
  ('mother', 0.7151536345481873),
  ('niece', 0.7005683183670044),
  ('father', 0.6659886837005615),
  ('aunt', 0.6623409390449524),
  ('grandson', 0.6618767380714417),
  ('grandparents', 0.6446609497070312),
  ('wife', 0.644535481929779)]
```

Let m, g, w, and x denote the word vectors for man, grandfather, woman, and the answer, respectively. Using **only** vectors m, g, w, and the vector arithmetic operators + and - in your answer, what is the expression in which we are maximizing cosine similarity with x?

Hint: Recall that word vectors are simply multi-dimensional vectors that represent a word. It might help to draw out a 2D example using arbitrary locations of each vector. Where would man and woman lie in the coordinate plane relative to grandfather and the answer?

Write your answer here. The objective is m - g = w - x. Hence, the expression we are maximizing consine similarity with is

$$w-m+g$$

## 1.3.7 Question 2.5: Finding Analogies [code + written] (1.5 points)

a. For the previous example, it's clear that "grandmother" completes the analogy. But give an intuitive explanation as to why the most\_similar function gives us words like "granddaughter", "daughter", or "mother"?

Write your answer here. This is because "granddaughter", "daughter", and "mother" have similar meaning and appear in the same context a lot. Hence, these words are pretty similar themselves, and they all have large similarity with the target word for the analogy.

b. Find an example of analogy that holds according to these vectors (i.e. the intended word is ranked top). In your solution please state the full analogy in the form x:y:: a:b. If you believe the analogy is complicated, explain why the analogy holds in one or two sentences.

**Note**: You may have to try many analogies to find one that works!

```
[36]: # For example: x, y, a, b = ("", "", "", "")
# ------
# Write your implementation here.
x, y, a, b = ("man", "grandfather", "woman", "grandmother")
# -------
# Test the solution
assert wv_from_bin.most_similar(positive=[a, y], negative=[x])[0][0] == b
```

Write your answer here.

#### 1.3.8 Question 2.6: Incorrect Analogy [code + written] (1.5 points)

a. Below, we expect to see the intended analogy "hand : glove :: foot : **sock**", but we see an unexpected result instead. Give a potential reason as to why this particular analogy turned out the way it did?

```
[37]: pprint.pprint(wv_from_bin.most_similar(positive=['foot', 'glove'],___
negative=['hand']))

[('45,000-square', 0.4922032058238983),
    ('15,000-square', 0.4649604260921478),
    ('10,000-square', 0.4544755816459656),
    ('6,000-square', 0.44975775480270386),
    ('3,500-square', 0.4441334009170532),
    ('700-square', 0.44257497787475586),
    ('50,000-square', 0.4356396794319153),
    ('3,000-square', 0.43486520648002625),
    ('30,000-square', 0.4330596923828125),
    ('footed', 0.43236875534057617)]
```

Write your answer here. This is probably because "foot" has multiple meanings. Here it is use as a unit for length, and thus constantly appear together with "xx-square" in order to represent area of a house.

b. Find another example of analogy that does *not* hold according to these vectors. In your solution, state the intended analogy in the form x:y :: a:b, and state the **incorrect** value of b according to the word vectors (in the previous example, this would be '45,000-square').

```
[38]: # For example: x, y, a, b = ("", "", "", "")
# ------
# Write your implementation here.
x, y, a, b = ("teach", "teacher", "cook", "chef")
# -------
pprint.pprint(wv_from_bin.most_similar(positive=[a, y], negative=[x]))
assert wv_from_bin.most_similar(positive=[a, y], negative=[x])[0] [0] != b
```

```
[('baker', 0.5139527320861816),
  ('fry', 0.47611334919929504),
  ('chef', 0.4755444824695587),
  ('cooked', 0.4582178294658661),
  ('friend', 0.4484547972679138),
  ('lamb', 0.4459801912307739),
  ('linda', 0.43900996446609497),
  ('curry', 0.43433597683906555),
  ('farmer', 0.4311731159687042),
  ('cooking', 0.4265446066856384)]
```

('practitioner', 0.4988412857055664), ('teaching', 0.48292145133018494),

Write your answer here. The intended analogy is teach:teacher :: cook:chef

# 1.3.9 Question 2.7: Guided Analysis of Bias in Word Vectors [written] (1 point)

It's important to be cognizant of the biases (gender, race, sexual orientation etc.) implicit in our word embeddings. Bias can be dangerous because it can reinforce stereotypes through applications that employ these models.

Run the cell below, to examine (a) which terms are most similar to "woman" and "profession" and most dissimilar to "man", and (b) which terms are most similar to "man" and "profession" and most dissimilar to "woman". Point out the difference between the list of female-associated words and the list of male-associated words, and explain how it is reflecting gender bias.

```
[39]: # Run this cell
      # Here `positive` indicates the list of words to be similar to and `negative`
       →indicates the list of words to be
      # most dissimilar from.
      pprint.pprint(wv_from_bin.most_similar(positive=['man', 'profession'],__

¬negative=['woman']))
      print()
      pprint.pprint(wv_from_bin.most_similar(positive=['woman', 'profession'],_
       →negative=['man']))
     [('reputation', 0.5250177383422852),
      ('professions', 0.5178037881851196),
      ('skill', 0.4904696047306061),
      ('skills', 0.49005505442619324),
      ('ethic', 0.4897659420967102),
      ('business', 0.4875850975513458),
      ('respected', 0.485920250415802),
      ('practice', 0.482104629278183),
      ('regarded', 0.47785720229148865),
      ('life', 0.4760662913322449)]
     [('professions', 0.5957458019256592),
```

```
('nursing', 0.48211807012557983),

('vocation', 0.4788966476917267),

('teacher', 0.47160351276397705),

('practicing', 0.46937811374664307),

('educator', 0.46524322032928467),

('physicians', 0.4628995358943939),

('professionals', 0.46013936400413513)]
```

Write your answer here. Here, we can see that professions like "teaching", "nursing" are learned to be most dissimilar to "man" and similar to "woman", while "business" and "respected" are learned to be most dissimilar to "woman" and similar to "man". It reflects the gender bias in the corpus and the learning results.

# 1.3.10 Question 2.8: Independent Analysis of Bias in Word Vectors [code + written] (1 point)

Use the most\_similar function to find another pair of analogies that demonstrates some bias is exhibited by the vectors. Please briefly explain the example of bias that you discover.

```
('hobby', 0.5636109709739685),
('pursuits', 0.4571879804134369),
('golfing', 0.4530138075351715),
('boyhood', 0.44461169838905334),
('kayaking', 0.4393688440322876),
('buddies', 0.4371037781238556),
('woodworking', 0.4333968460559845),
('pastime', 0.42579013109207153),
('gardening', 0.41385868191719055)]
[('pastimes', 0.579139769077301),
('hobby', 0.5000203251838684),
('antiquing', 0.4633525311946869),
('extracurricular', 0.4543994665145874),
('pursuits', 0.44996699690818787),
('obsessions', 0.4408562183380127),
('indulging', 0.440299928188324),
('gardening', 0.43824321031570435),
('socializing', 0.42874059081077576),
```

[('pastimes', 0.5957196354866028),

('sunbathing', 0.4177471697330475)]

Write your answer here. The above code reflect gender bias for hobbies.

#### 1.3.11 Question 2.9: Thinking About Bias [written] (2 points)

a. Give one explanation of how bias gets into the word vectors. Briefly describe a real-world example that demonstrates this source of bias. Your real-world example should be focused on word vectors, as opposed to bias in other AI systems (e.g., ChatGPT).

Write your answer here. The bias may get into the word vector through the corpus. If "man" is often related with "business" while "woman" with "nursing" when it comes to professions in the corpus, results similar to what is shown above will appear.

b. What is one method you can use to mitigate bias exhibited by word vectors? Briefly describe a real-world example that demonstrates this method.

Write your answer here. One method to mitigate bias exhibited by word vectors is to use relatively high quality input corpus. That is, make sure the corpus mitigate bias in the first place.

#### 2 Submission Instructions

- 1. Click the Save button at the top of the Jupyter Notebook.
- 2. Select Cell -> All Output -> Clear. This will clear all the outputs from all cells (but will keep the content of all cells).
- 3. Select Cell -> Run All. This will run all the cells in order, and will take several minutes.
- 4. Once you've rerun everything, select File -> Download as -> PDF via LaTeX (If you have trouble using "PDF via LaTex", you can also save the webpage as pdf. Make sure all your solutions especially the coding parts are displayed in the pdf, it's okay if the provided codes get cut off because lines are not wrapped in code cells).
- 5. Look at the PDF file and make sure all your solutions are there, displayed correctly. The PDF is the only thing your graders will see!
- 6. Submit your PDF on Gradescope.