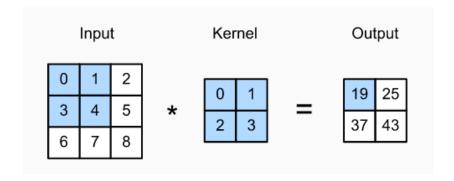
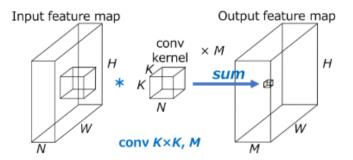
Pixel-Adaptive Convolutional Neural Networks (CVPR 2019)

Hang Su¹, Varun Jampani², Deqing Sun², Orazio Gallo², Erik Learned-Miller¹, and Jan Kautz²

¹UMass Amherst ²NVIDIA

standard convolution





Convolution is spatially-shared





https://www.youtube.com/watch?v=gsQZbHuR64o

Convolution is content-agnostic





Dynamic Filter Networks (NIPS 2016)

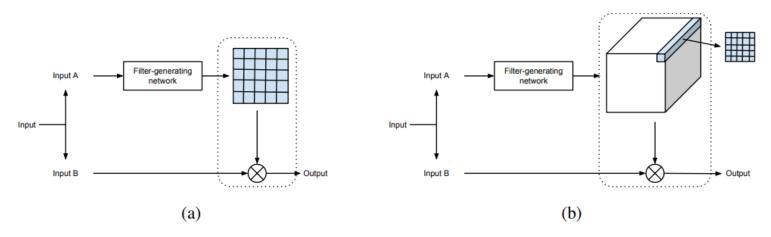
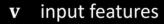
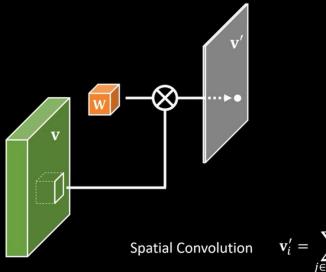
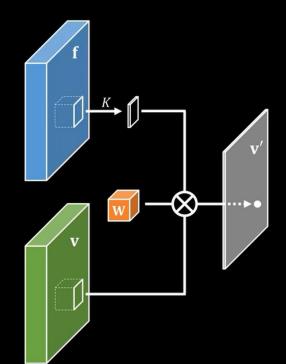


Figure 2: Left: Dynamic convolution: the filter-generating network produces a single filter that is applied convolutionally on I_B . Right: Dynamic local filtering: each location is filtered with a location-specific dynamically generated filter.

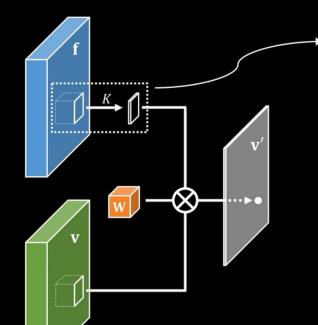


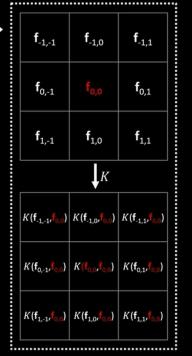
- \mathbf{v}' output features
- p (x, y) coordinates
- W filter weights





- v input features
- \mathbf{v}' output features
- p(x,y) coordinates
- W filter weights
- f adapting features



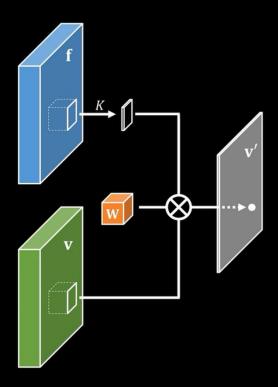


- v input features
- \mathbf{v}' output features
- p(x,y) coordinates
- W filter weights
- f adapting features
- K adapting kernel

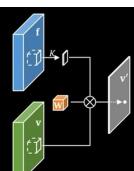
Pixel Adaptive Convolution (PAC)

$$\mathbf{v}_i' = \sum_{j \in \Omega(i)} K(\mathbf{f}_i, \mathbf{f}_j) \mathbf{W}[\mathbf{p}_i - \mathbf{p}_j] \mathbf{v}_j + \mathbf{b}$$

Spatial Convolution $\mathbf{v}_i' = \sum_{i=1}^{n} \mathbf{W}[\mathbf{p}_i - \mathbf{p}_j]\mathbf{v}_j + \mathbf{b}$



$$\mathbf{v}_i' = \sum_{j \in \Omega(i)} K(\mathbf{f}_i, \mathbf{f}_j) \mathbf{W}[\mathbf{p}_i - \mathbf{p}_j] \mathbf{v}_j + \mathbf{b}$$



- Spatial convolution
- $K(\mathbf{f}_i, \mathbf{f}_j) = 1$
- Bilateral filtering

$$\mathbf{f} = (r, g, b), K(\mathbf{f}_i, \mathbf{f}_j) = \exp(-\frac{1}{2\alpha_1} \|\mathbf{f}_i - \mathbf{f}_j\|^2)$$

$$\mathbf{W}[p_i - p_j] = \exp(-\frac{1}{2\alpha_2} \|p_i - p_j\|^2)$$

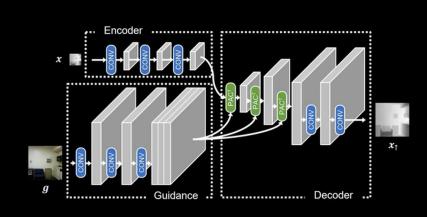
Average pooling

$$K(\mathbf{f}_i, \mathbf{f}_j) = 1, \mathbf{W}[\mathbf{p}_i - \mathbf{p}_j] = \frac{1}{F^2}$$

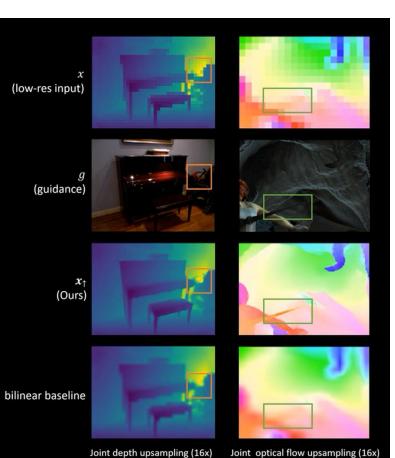
Detail-preserving pooling [1]

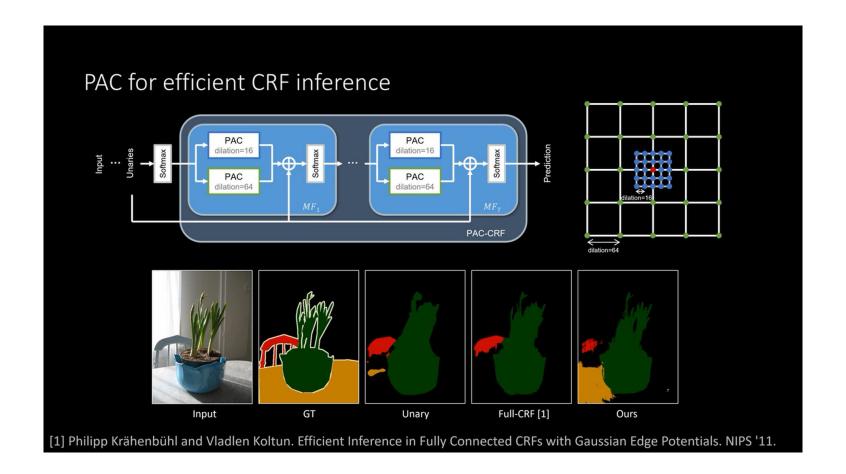
$$K(\mathbf{f}_i, \mathbf{f}_j) = \alpha + (\|\mathbf{f}_i - \mathbf{f}_j\|^2 + \epsilon^2)^{\lambda}$$

PAC generalizes many existing filtering techniques

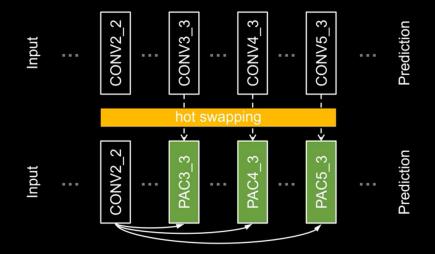


Joint upsampling network with PAC





Layer "hot-swapping" with PAC

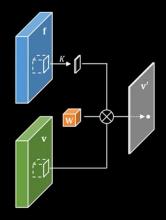


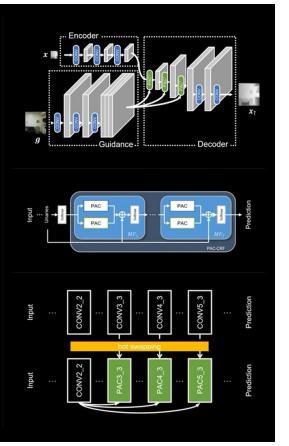
Method	CRF	mloU	Runtime
FCN		67.20	39ms
FCN	\checkmark	69.82	117ms
PAC-FCN		69.18	41ms
PAC-FCN	√	71.34	118ms

^{*}evaluated on Pascal VOC 2012 test set

Summary

- Pixel Adaptive Convolution Sec.3:
 - Content-adaptive
 - Generalizes several existing filtering techniques
- Three use cases:
 - Joint upsampling networks Sec. 4
 - Efficient CRF inference Sec. 5
 - Network layer hot-swapping Sec. 6





```
in ch, g ch = 16, 8
                                       # channel sizes of input and guidance
stride, f, b, h, w = 5, 2, 64, 64
                                       # stride, filter size, batch size, input height and width
input = torch.rand(b, in_ch, h, w)
guide = torch.rand(b, g ch, h, w)
                                  # guidance feature
pool = nn.AvgPool2d(f, stride)
out pool = pool(input)
                                      # standard spatial convolution
pacpool = PacPool2d(f, stride)
out pac = pacpool(input, guide) # PAC
out_pac = pacpool(input, None, guide_k) # alternative interface
                                       # guide k is pre-computed 'K'
                                       # of shape [b, g_ch, f, f, h, w]. packernel2d can be
                                       # used for its creation.
```