P8106 Final Project: Predicting COVID-19 Recovery Time and Identifying Significant Risk Factors

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Background

[Check the report]

Data:

[Description check the report]

```
# For primary analysis:
# Dataset Loading:
load("data/recovery.Rdata")
set.seed(3521) # Runze Cui's uni(2183):
# Create a first random sample of 2000 participants:
dat1 <- dat[sample(1:10000, 2000),]</pre>
set.seed(3555) # Yuchen Hua's uni(3555)
# Create a second random sample of 2000 participants:
dat2 <- dat[sample(1:10000, 2000),]</pre>
# Merged the two datasets and remove repeated observations:
dat <- unique(rbind(dat1, dat2))</pre>
# Get rid of the id variable from the merged dataset and do the data cleaning:
dat <- dat %>%
 select(-id) %>%
 mutate(gender = as.factor(gender)) %>%
 mutate(race = as.factor(race)) %>%
 mutate(smoking = as.factor(smoking)) %>%
 mutate(hypertension = as.factor(hypertension)) %>%
 mutate(diabetes = as.factor(diabetes)) %>%
 mutate(vaccine = as.factor(vaccine)) %>%
 mutate(severity = as.factor(severity)) %>%
 mutate(study = as.factor(study)) %>%
 na.omit() %>%
 relocate(recovery_time)
head(dat)
       recovery_time age gender race smoking height weight bmi hypertension
## 8158
                 52 61 0 1 1 169.9 87.6 30.4
## 3387
                  24 60
                             1
                                  1
                                         2 173.4
                                                     70.6 23.5
                                                                         0
                  36 60
                            1
                                          1 178.2
                                                     79.9 25.1
                                                                         0
## 1709
                                  1
                            1
## 4051
                  23 70
                                  4
                                          0 167.4
                                                     77.7 27.7
                                                                         1
## 954
                  24 63
                                          0 175.4
                                                     88.7 28.8
                                                                         1
                 36 65
                            0
                                          0 160.4
                                                     74.4 28.9
## 531
                                  1
## diabetes SBP LDL vaccine severity study
          0 118 103 0
## 8158
                                   0
## 3387
             0 129 101
             0 130 107
## 1709
                             1
                                      0
                                            Α
## 4051
              0 145 128
                             1
                                            В
                              0
## 954
              0 131 100
                                      0
                                            Α
         0 137 153
## 531
```

```
# Separate the data as training and test data:
set.seed(3521)
# Specify rows of training data:
trRows <- createDataPartition(dat$recovery_time, p = 0.7, list = FALSE)
# Training data:
training <- dat[trRows, ]</pre>
## Covariates' matrix:
x <- model.matrix(recovery_time ~ ., dat)[trRows, -1]</pre>
## Response's vector:
y <- dat$recovery_time[trRows]</pre>
# Test data:
test <- dat[-trRows, ]</pre>
## Covariates' matrix:
x2 <- model.matrix(recovery_time ~ ., dat)[-trRows, -1]</pre>
## Response's vector:
y2 <- dat$recovery_time[-trRows]
# For secondary analysis:
dat 2 <- dat %>%
  mutate(recovery_time = ifelse(recovery_time > 30, "great", "less")) %%
  mutate(recovery_time = as.factor(recovery_time))
# Training data:
training_sec <- dat_2[trRows, ]</pre>
## Covariates' matrix:
x_sec <- model.matrix(recovery_time ~ ., dat_2)[trRows, -1]</pre>
## Response's vector:
y_sec <- dat_2$recovery_time[trRows]</pre>
# Test data:
test_sec <- dat_2[-trRows, ]</pre>
## Covariates' matrix:
x2_sec <- model.matrix(recovery_time ~ ., dat_2)[-trRows, -1]</pre>
## Response's vector:
y2_sec <- dat_2$recovery_time[-trRows]</pre>
```

Exploratory Analysis and Data Visualization

[Description check the report]

Exploratory Analysis

```
# Summary tables separated by continuous/categorical variables:
skimr::skim(dat)
```

Table 1: Data summary

Name	dat
Number of rows	3587
Number of columns	15
Column type frequency:	
factor	8
numeric	7
Group variables	None

Variable type: factor

skim_variable	n_missing	$complete_rate$	ordered	n_unique	top_counts
gender	0	1	FALSE	2	0: 1847, 1: 1740
race	0	1	FALSE	4	1: 2332, 3: 731, 4: 350, 2: 174
smoking	0	1	FALSE	3	0: 2191, 1: 1044, 2: 352
hypertension	0	1	FALSE	2	0: 1817, 1: 1770
diabetes	0	1	FALSE	2	0: 3045, 1: 542
vaccine	0	1	FALSE	2	1: 2174, 0: 1413
severity	0	1	FALSE	2	0: 3236, 1: 351
study	0	1	FALSE	3	B: 2129, A: 737, C: 721

Variable type: numeric

skim_variable	n_missing	complete_	rate	mean	sd	p0	p25	p50	p75	p100	hist
recovery_time	0		1	43.27	29.57	2.0	28.0	39.0	50.0	365.0	
age	0		1	60.09	4.48	45.0	57.0	60.0	63.0	75.0	
height	0		1	169.94	6.00	149.7	165.9	169.9	173.9	189.6	
weight	0		1	79.93	7.02	57.2	75.2	80.0	84.7	105.7	
$_{ m bmi}$	0		1	27.74	2.77	18.8	25.8	27.7	29.5	38.1	
SBP	0		1	130.28	7.96	102.0	125.0	130.0	136.0	158.0	
LDL	0		1	110.16	19.75	47.0	97.0	110.0	124.0	178.0	

skimr::skim(dat2)

Table 4: Data summary

Name	dat2
Number of rows	2000
Number of columns	16
Column type frequency:	
character	1
factor	2
numeric	13

Table 4: Data summary

Group variables	None

Variable type: character

skim_variable	$n_{missing}$	$complete_rate$	min	max	empty	n_unique	whitespace
study	0	1	1	1	0	3	0

Variable type: factor

$skim_variable$	n_missing	$complete_rate$	ordered	n _unique	top_counts
race	0	1	FALSE	4	1: 1281, 3: 411, 4: 207, 2: 101
$\operatorname{smoking}$	0	1	FALSE	3	0: 1242, 1: 562, 2: 196

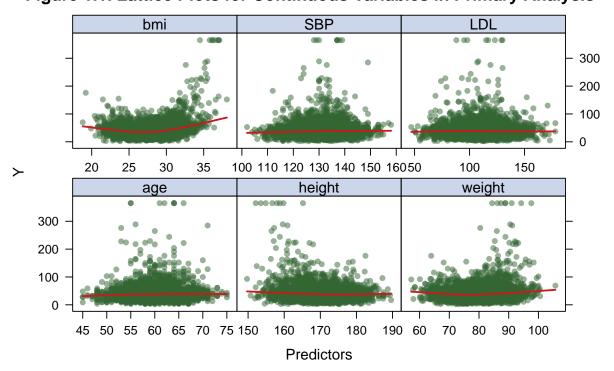
Variable type: numeric

skim_variable n	_missing comple	ete_rat	e mean	sd	p0	p25	p50	p75	p100	hist
id	0	1	4902.78	2915.29	1.0	2344.75	4849.5	7410.0	9995.0	
age	0	1	60.02	4.50	45.0	57.00	60.0	63.0	75.0	
gender	0	1	0.49	0.50	0.0	0.00	0.0	1.0	1.0	
height	0	1	170.03	6.03	151.9	166.00	169.9	174.1	189.6	
weight	0	1	79.85	7.00	57.2	75.20	79.9	84.5	100.6	
bmi	0	1	27.69	2.78	20.5	25.80	27.5	29.5	38.1	
hypertension	0	1	0.50	0.50	0.0	0.00	0.0	1.0	1.0	
diabetes	0	1	0.14	0.35	0.0	0.00	0.0	0.0	1.0	
SBP	0	1	130.36	8.04	102.0	125.00	130.0	136.0	155.0	
LDL	0	1	110.43	19.30	47.0	97.00	111.0	124.0	171.0	
vaccine	0	1	0.61	0.49	0.0	0.00	1.0	1.0	1.0	
severity	0	1	0.10	0.29	0.0	0.00	0.0	0.0	1.0	
recovery_time	0	1	42.41	28.90	2.0	28.00	38.0	49.0	365.0	

Data Visualization

```
span = .5,
labels = c("Predictors","Y"),
main = "Figure 1.1. Lattice Plots for Continuous Variables in Primary Analysis",
type = c("p", "smooth"))
```

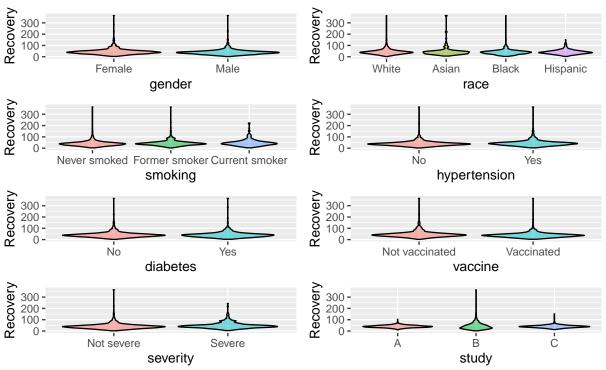
Figure 1.1. Lattice Plots for Continuous Variables in Primary Analysis

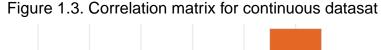


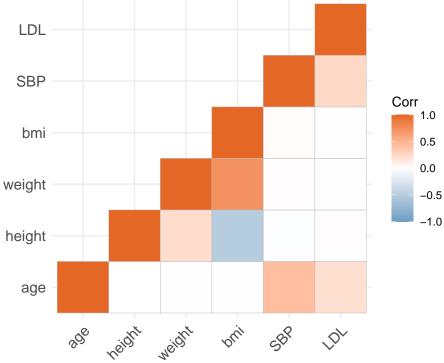
```
## For categorical variables:
gender plot = dat %>%
  ggplot(aes(x = gender, y = recovery_time, fill = gender)) +
  geom violin(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('Female','Male')) +
  ylab("Recovery") +
  theme(legend.position = "none")
race_plot = dat %>%
  ggplot(aes(x = race, y = recovery_time, fill = race)) +
  geom_violin(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('White', 'Asian', 'Black', 'Hispanic')) +
  ylab("Recovery") +
  theme(legend.position = "none")
smoking_plot = dat %>%
  ggplot(aes(x = smoking, y = recovery_time, fill = smoking)) +
  geom_violin(color = "black", alpha = .5) +
  scale x discrete(labels = c('Never smoked', 'Former smoker', 'Current smoker')) +
  ylab("Recovery") +
  theme(legend.position = "none")
```

```
hyper_plot = dat %>%
  ggplot(aes(x = hypertension, y = recovery_time, fill = hypertension)) +
  geom_violin(color = "black", alpha = .5) +
  ylab("Recovery") +
  scale_x_discrete(labels = c('No', 'Yes')) +
  theme(legend.position = "none")
diabetes plot = dat %>%
  ggplot(aes(x = diabetes, y = recovery_time, fill = diabetes)) +
  geom_violin(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('No', 'Yes')) +
  ylab("Recovery") +
  theme(legend.position = "none")
vac_plot = dat %>%
  ggplot(aes(x = vaccine, y = recovery_time, fill = vaccine)) +
  geom_violin(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('Not vaccinated','Vaccinated')) +
  ylab("Recovery") +
  theme(legend.position = "none")
severity_plot = dat %>%
  ggplot(aes(x = severity, y = recovery_time, fill = severity)) +
  geom_violin(color = "black", alpha = .5) +
  scale x discrete(labels = c('Not severe', 'Severe')) +
  ylab("Recovery") +
  theme(legend.position = "none")
study_plot = dat %>%
  ggplot(aes(x = study, y = recovery_time, fill = study)) +
  geom_violin(color = "black", alpha = .5) +
  ylab("Recovery") +
  theme(legend.position = "none")
(gender_plot + race_plot + smoking_plot + hyper_plot) / (diabetes_plot + vac_plot + severity_plot + stu
  plot_layout(guides = "collect") +
  plot_annotation(title = "Figure 1.2. Violin Plots for Categorical Variables in Primary Analysis")
```



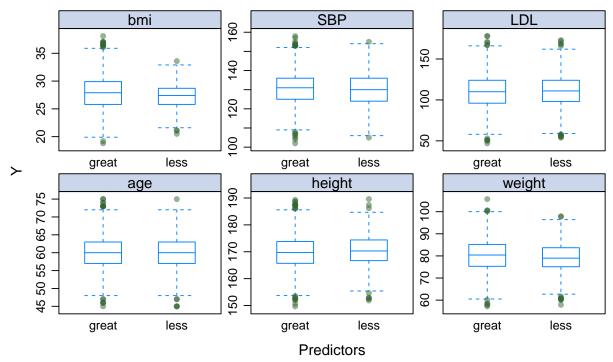






```
# For secondary analysis:
## For continuous variables:
theme = trellis.par.get()
themeplot.symbol\\col = rgb(.2, .4, .2, .5)
themeplot.symbol\\pch = 16
themeplot.line col = rgb(.8, .1, .1, 1)
theme$plot.line$lwd = 2
theme$strip.background$col = rgb(.0, .2, .6, .2)
trellis.par.set(theme)
featurePlot(x = dat_2 %>% dplyr::select(age, height, weight, bmi, SBP, LDL),
            y = dat_2$recovery_time,
            plot = "box", pch = "|",
            scales = list(x = list(relation = "free"),
                         y = list(relation = "free")),
            labels = c("Predictors","Y"),
            main = "Figure 1.4. Lattice Plots for Continuous Variables in Secondary Analysis",
            auto.key = list(columns = 2))
```





```
## For categorical variables:
gender_plot_sec = dat_2 %>%
  ggplot(aes(x = gender, fill = recovery_time)) +
  geom_bar(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('Female','Male')) +
  ylab("Recovery") +
  theme(legend.position = "none")
race_plot_sec = dat_2 %>%
  ggplot(aes(x = race, fill = recovery_time)) +
  geom_bar(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('White','Asian','Black', 'Hispanic')) +
  ylab("Recovery") +
  theme(legend.position = "none")
smoking_plot_sec = dat_2 %>%
  ggplot(aes(x = smoking, fill = recovery_time)) +
  geom_bar(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('Never smoked', 'Former smoker', 'Current smoker')) +
  ylab("Recovery") +
  theme(legend.position = "none")
hyper_plot_sec = dat_2 %>%
  ggplot(aes(x = hypertension, fill = recovery_time)) +
  geom_bar(color = "black", alpha = .5) +
  ylab("Recovery") +
  scale_x_discrete(labels = c('No', 'Yes')) +
```

```
theme(legend.position = "none")
diabetes_plot_sec = dat_2 %>%
  ggplot(aes(x = diabetes, fill = recovery_time)) +
  geom_bar(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('No','Yes')) +
 ylab("Recovery") +
 theme(legend.position = "none")
vac_plot_sec = dat_2 %>%
  ggplot(aes(x = vaccine, fill = recovery_time)) +
  geom_bar(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('Not vaccinated','Vaccinated')) +
 ylab("Recovery") +
  theme(legend.position = "none")
severity_plot_sec = dat_2 %>%
  ggplot(aes(x = severity, fill = recovery_time)) +
  geom_bar(color = "black", alpha = .5) +
  scale_x_discrete(labels = c('Not severe','Severe')) +
 ylab("Recovery") +
 theme(legend.position = "none")
study_plot_sec = dat_2 %>%
  ggplot(aes(x = study, fill = recovery_time)) +
  geom_bar(color = "black", alpha = .5) +
 ylab("Recovery") +
 theme(legend.position = "none")
(gender_plot_sec + race_plot_sec + smoking_plot_sec + hyper_plot_sec) / (diabetes_plot_sec + vac_plot_s
 plot_layout(guides = "collect") +
 plot_annotation(title = "Figure 1.5. Bar Plots for Categorical Variables in Secondary Analysis")
```

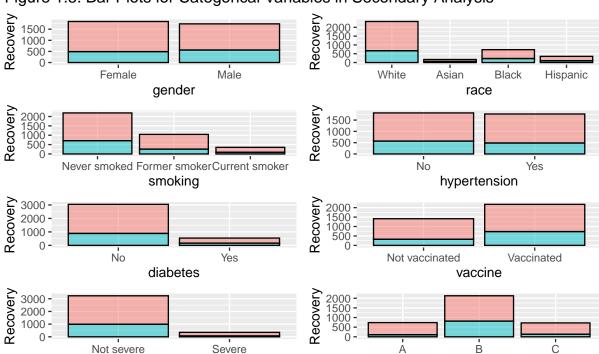


Figure 1.5. Bar Plots for Categorical Variables in Secondary Analysis

Note: Red is recovery time less than and equal to 30. Blue is greater than 30. ctrl and parallel computing setup:

severity

study

Primary Analysis

Recovery time as continuous variable.

Linear methods:

Linear model:

```
trControl = ctrl)
summary(lm)
##
## Call:
## lm(formula = .outcome ~ ., data = dat)
## Residuals:
             1Q Median
## Min
                             3Q
## -62.043 -13.881 -1.317 10.006 236.072
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) -2.460e+03 1.398e+02 -17.598 < 2e-16 ***
             2.353e-01 1.205e-01 1.952 0.051045 .
## age
## gender1
              -5.201e+00 9.521e-01 -5.462 5.17e-08 ***
## race2
               7.627e-01 2.226e+00 0.343 0.731920
## race3
               -1.850e+00 1.214e+00 -1.524 0.127587
## race4
               -1.890e+00 1.639e+00 -1.153 0.248913
## smoking1
               4.200e+00 1.067e+00 3.938 8.46e-05 ***
               8.195e+00 1.651e+00 4.963 7.43e-07 ***
## smoking2
## height
               1.433e+01 8.213e-01 17.442 < 2e-16 ***
## weight
               -1.541e+01 8.717e-01 -17.682 < 2e-16 ***
## bmi
               4.676e+01 2.499e+00 18.713 < 2e-16 ***
## hypertension1 3.050e+00 1.574e+00 1.938 0.052794 .
## diabetes1 -1.085e+00 1.328e+00 -0.817 0.413725
## SBP
              -4.700e-02 1.039e-01 -0.452 0.651026
## LDL
              -3.455e-02 2.466e-02 -1.401 0.161337
## vaccine1
               -7.333e+00 9.768e-01 -7.508 8.33e-14 ***
## severity1
               7.807e+00 1.644e+00 4.750 2.15e-06 ***
                4.365e+00 1.216e+00 3.590 0.000337 ***
## studyB
## studyC
               -5.355e-01 1.499e+00 -0.357 0.720955
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 23.81 on 2494 degrees of freedom
## Multiple R-squared: 0.2355, Adjusted R-squared: 0.23
## F-statistic: 42.68 on 18 and 2494 DF, p-value: < 2.2e-16
# Importances:
plot(varImp(lm, scale = TRUE), main = "Figure 2. Linear Model Variable's Importance Plot")
```

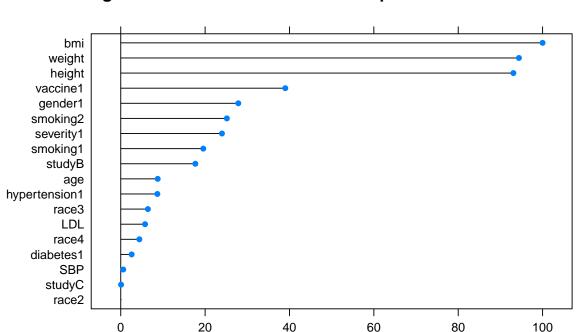


Figure 2. Linear Model Variable's Importance Plot

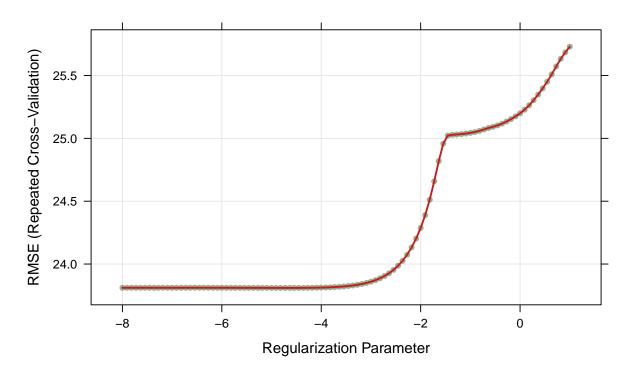
```
# Report the CV error:
lm$results$RMSE
## [1] 23.81421
# Report the test error:
lm_pred = predict(lm, newdata = test) ## Test dataset
lm_mse = sqrt(mean((lm_pred - y2)^2))
lm_mse
## [1] 29.06371
```

Importance

[Describe the outputs above]

LASSO model:



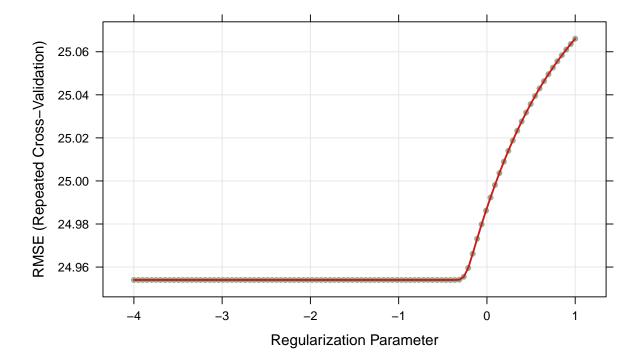


```
# Choose best tuning parameter value:
lasso$bestTune
      alpha
                 lambda
          1 0.008850576
## 37
# Report the coefficients after applying the best tuning parameter:
coef(lasso$finalModel, lasso$bestTune$lambda)
## 19 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                -2.326105e+03
## age
                  2.302849e-01
## gender1
                 -5.174310e+00
## race2
                  6.917049e-01
## race3
                 -1.881002e+00
## race4
                 -1.852093e+00
## smoking1
                  4.170664e+00
## smoking2
                  8.130377e+00
## height
                  1.353195e+01
## weight
                 -1.457152e+01
## bmi
                  4.434163e+01
## hypertension1 2.956707e+00
## diabetes1
                -1.028034e+00
## SBP
                 -3.873666e-02
## LDL
                 -3.421155e-02
                 -7.301952e+00
## vaccine1
## severity1
                  7.790966e+00
## studyB
                  4.368825e+00
## studyC
                 -4.916229e-01
```

```
# Report the CV error:
lasso$results[37, ]$RMSE
## [1] 23.80994
# Report the test error:
lasso_pred = predict(lasso, newdata = x2) ## Test dataset
lasso_mse = sqrt(mean((lasso_pred - y2)^2))
lasso_mse
## [1] 29.16892
```

Ridge model:

Figure 4. Ridge Model CV RMSE Plot

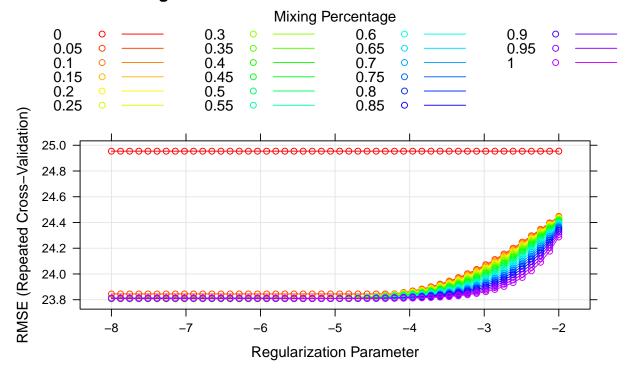


```
# Choose best tuning parameter value:
ridge$bestTune
     alpha
              lambda
## 73 0 0.6951439
# Report the coefficients after applying the best tuning parameter:
coef(ridge$finalModel, ridge$bestTune$lambda)
## 19 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept) -1.149931e+02
## age
                2.064306e-01
## smoking1 ## smoking2 ## bc.
## height
                4.750406e-01
## weight
               -6.857228e-01
## bmi
                4.479836e+00
## hypertension1 2.800025e+00
## severity1
                7.819336e+00
## studyB
                4.395135e+00
## studyC
                -2.104760e-01
# Report the CV error:
ridge$results[73, ]$RMSE
## [1] 24.95401
# Report the test error:
ridge_pred = predict(ridge, newdata = x2) ## Test dataset
ridge_mse = sqrt(mean((ridge_pred - y2)^2))
ridge_mse
## [1] 32.00583
```

Elastic net model:

```
superpose.line = list(col = myCol))
plot(enet, par.settings = myPar, main = "Figure 5. Elastic Net Model CV RMSE Plot", xTrans = log)
```

Figure 5. Elastic Net Model CV RMSE Plot



```
# Choose best tuning parameter value:
enet$bestTune
       alpha
                  lambda
## 220 0.2 0.003435924
# Report the coefficients after applying the best tuning parameter:
coef(enet$finalModel, enet$bestTune$lambda)
## 19 x 1 sparse Matrix of class "dgCMatrix"
## (Intercept)
                 -2.282729e+03
## age
                  2.333649e-01
## gender1
                 -5.189117e+00
## race2
                  7.082009e-01
## race3
                 -1.922687e+00
## race4
                 -1.886490e+00
## smoking1
                  4.193610e+00
## smoking2
                  8.158687e+00
## height
                  1.327902e+01
## weight
                 -1.430227e+01
                  4.356889e+01
## bmi
## hypertension1 3.037924e+00
## diabetes1
                 -1.039260e+00
## SBP
                 -4.372863e-02
## LDL
                 -3.464473e-02
## vaccine1 -7.312501e+00
```

Partial least squares model (PLS):

```
set.seed(3521)
# Fit a PLS model:
pls = train(x, y, ## training dataset
          method = "pls",
          tuneGrid = data.frame(ncomp = 1:18),
          trControl = ctrl,
          preProcess = c("center", "scale"))
summary(pls)
## Data:
          X dimension: 2513 18
## Y dimension: 2513 1
## Fit method: oscorespls
## Number of components considered: 11
## TRAINING: % variance explained
##
      1 comps 2 comps 3 comps 4 comps 5 comps 6 comps 7 comps
## X
             9.44 16.31
                            26.35
                                    31.00
                                            35.86
                                                     41.51
                                                             45.81
## .outcome 12.45
                   13.46
                            13.57
                                      13.71
                                              13.99
                                                       14.69
                                                               16.91
##
      8 comps 9 comps 10 comps 11 comps
## X
           49.91
                   52.62
                            56.45
                                       61.63
## .outcome 19.43
                     22.34
                               23.49
                                        23.55
# Choose best tuning parameter value:
pls$bestTune
## ncomp
## 11
        11
# Plot for the number of components:
ggplot(pls, highlight = T) +
 theme_bw() +
 ggtitle("Figure 6. PLS Model CV RMSE Plot")
```

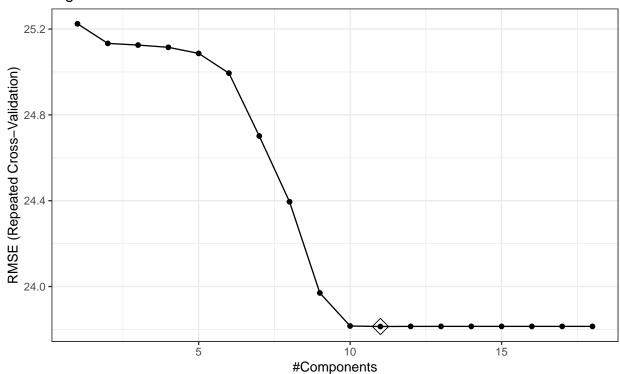


Figure 6. PLS Model CV RMSE Plot

```
# Report the CV error:
pls$results[11, ]$RMSE
## [1] 23.81368
# Report the test error:
pls_pred = predict(pls, newdata = x2) ## Test dataset
pls_mse = sqrt(mean((pls_pred - y2)^2))
pls_mse
## [1] 29.06252
```

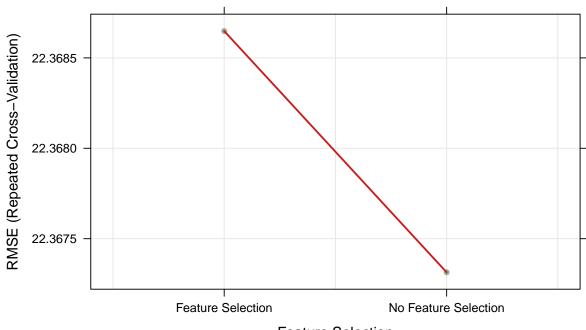
Nonlinear Methods:

Generalized additive model (GAM):

```
## .outcome ~ gender1 + race3 + race4 + smoking1 + smoking2 + hypertension1 +
      diabetes1 + vaccine1 + severity1 + studyB + studyC + s(age) +
      s(SBP) + s(LDL) + s(bmi) + s(height) + s(weight)
## Parametric coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 43.2614 1.5011 28.820 < 2e-16 ***
## gender1
                -4.8382
                          0.8761 -5.523 3.68e-08 ***
                           1.1066 -1.782 0.074945 .
## race3
                -1.9715
## race4
                -2.2377
                          1.5006 -1.491 0.136053
## smoking1
                4.7304 0.9809 4.823 1.50e-06 ***
                8.4125 1.5209 5.531 3.51e-08 ***
## smoking2
## hypertension1 4.0622 1.5700 2.587 0.009728 **
               -0.1520 1.2212 -0.124 0.900971
## diabetes1
## vaccine1
                -7.4441
                          0.8996 -8.275 < 2e-16 ***
                          1.5105 5.305 1.23e-07 ***
## severity1
                8.0127
                 3.9614
                        1.1211 3.533 0.000418 ***
## studyB
                -1.1218 1.3803 -0.813 0.416468
## studyC
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Approximate significance of smooth terms:
             edf Ref.df F p-value
           1.000 1.000 3.717 0.053976 .
## s(age)
          2.033 2.564 1.853 0.161840
## s(SBP)
## s(LDL) 1.000 1.000 0.929 0.335229
## s(bmi) 8.079 8.737 84.927 < 2e-16 ***
## s(height) 1.000 1.000 0.591 0.442071
## s(weight) 6.720 7.840 3.688 0.000309 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## R-sq.(adj) = 0.351 Deviance explained = 35.9%
## GCV = 483.87 Scale est. = 477.74  n = 2513
# Report the model:
gam$bestTune
## select method
## 1 FALSE GCV.Cp
gam$finalModel
## Family: gaussian
## Link function: identity
##
## Formula:
## .outcome ~ gender1 + race3 + race4 + smoking1 + smoking2 + hypertension1 +
      diabetes1 + vaccine1 + severity1 + studyB + studyC + s(age) +
      s(SBP) + s(LDL) + s(bmi) + s(height) + s(weight)
## Estimated degrees of freedom:
## 1.00 2.03 1.00 8.08 1.00 6.72 total = 31.83
## GCV score: 483.8652
```

```
# Plot for tuning parameter selection:
plot(gam, main = "Figure 7. GAM Model CV RMSE Plot")
```

Figure 7. GAM Model CV RMSE Plot



Feature Selection

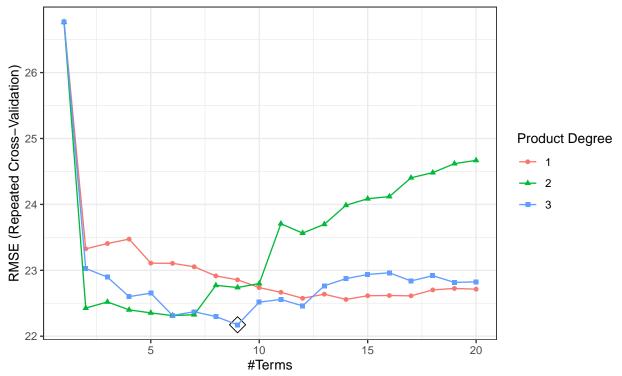
```
# Report the CV error:
gam$results$RMSE
## [1] 22.36731 22.36865
# Report the test error:
gam_pred = predict(gam, newdata = x2) ## Test dataset
gam_mse = sqrt(mean((gam_pred - y2)^2))
gam_mse
## [1] 25.85336
```

[Describe the outputs above]

Multivariate adaptive regression spline (MARS) model:

```
method = "earth",
              tuneGrid = mars_grid,
              trControl = ctrl)
stopCluster(cl)
registerDoSEQ()
# Report the coefficients:
coef(mars$finalModel)
                         (Intercept)
                                                            h(30.5-bmi)
##
                           12.631786
                                                               5.164229
                                           race2 * h(bmi-30.5) * studyB
##
                h(bmi-30.5) * studyB
##
                           22.177779
                                                              22.832642
##
                            vaccine1
                                                            h(bmi-25.4)
                            -7.057776
                                                               6.227136
## h(bmi-30.5) * h(SBP-128) * studyB h(bmi-30.5) * h(SBP-130) * studyB
                           24.889685
## h(bmi-30.5) * h(SBP-124) * studyB
                           -7.493282
# Plot for tuning parameter selection:
ggplot(mars, highlight = T) +
 theme_bw() +
 ggtitle("Figure 8. MARS Model CV RMSE Plot")
```

Figure 8. MARS Model CV RMSE Plot

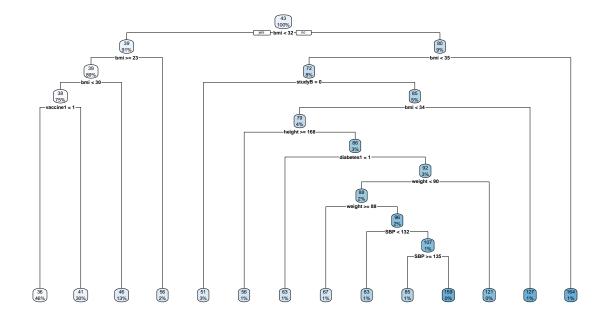


```
# Choose best tuning parameter value:
mars$bestTune
## nprune degree
## 49 9 3
```

```
# Report the CV error:
mars$results[27, ]$RMSE
## [1] 22.17363
# Report test error:
mars_pred = predict(mars, newdata = x2) ## Test dataset
mars_mse = sqrt(mean((mars_pred - y2)^2))
mars_mse
## [1] 27.02613
```

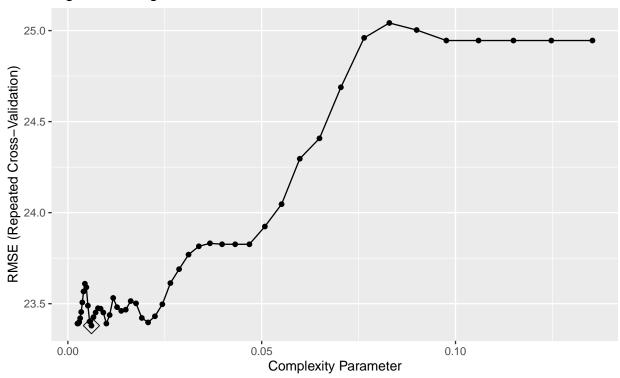
Regression Tree:

Figure 9.1. Regression Tree



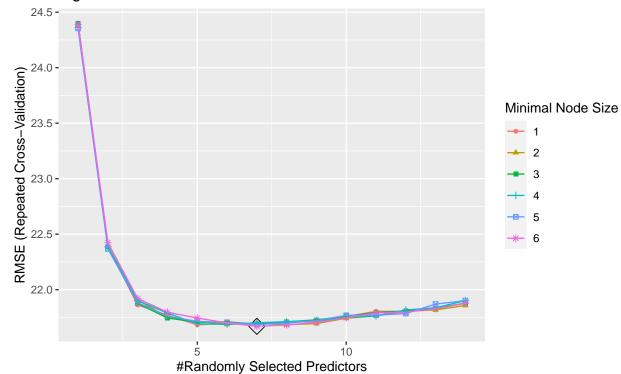
```
# Plot for tuning parameter selection:
ggplot(reg_tree, highlight = TRUE) + ggtitle("Figure 9.2 Regression Tree Model CV RMSE Plot")
```





Random Forests:

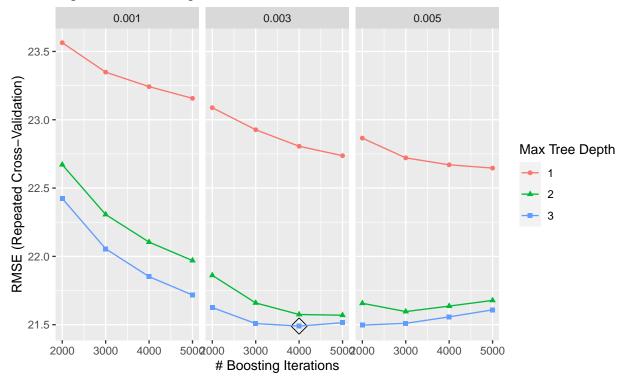
Figure 10. Random Forests CV RMSE Plot



Boosting:

```
set.seed(3521)
boosting.grid = expand.grid(n.trees = c(2000, 3000, 4000, 5000),
                       interaction.depth = 1:3,
                       shrinkage = c(0.001, 0.003, 0.005),
                       n.minobsinnode = 1)
set.seed(3521)
cl = makePSOCKcluster(no_cores)
registerDoParallel(cl)
boosting = train(x, y,
                method = "gbm",
                tuneGrid = boosting.grid,
                trControl = ctrl,
                verbose = FALSE)
stopCluster(cl)
registerDoSEQ()
# Plot for tuning parameter selection:
ggplot(boosting, highlight = TRUE) + ggtitle("Figure 11. Boosting CV RMSE Plot")
```

Figure 11. Boosting CV RMSE Plot



```
# Choose best tuning parameter value:
boosting$bestTune
## n.trees interaction.depth shrinkage n.minobsinnode
```

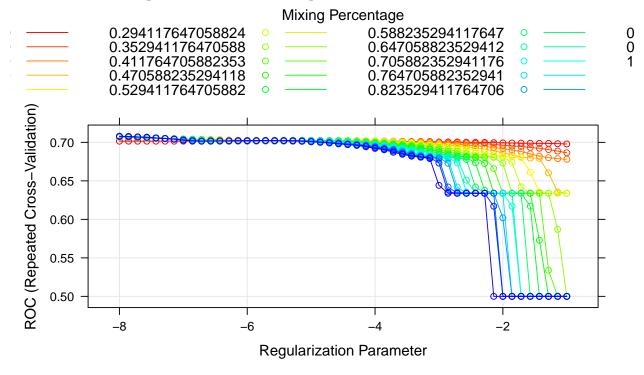
Secondary Analysis

Logistic Model:

```
set.seed(3521)
glm = train(recovery_time ~ .,
           data = training_sec,
           method = "glm",
           metric = "ROC",
           trControl = ctrl1)
glm$finalModel
##
## Call: NULL
##
## Coefficients:
                                     gender1
   (Intercept)
                                                      race2
                                                                    race3
                           age
                                   2.843e-01
##
     7.736e+01
                   -3.527e-02
                                                3.878e-01
                                                                 1.411e-01
                                 smoking2 height
-4.431e-01 -4.425e-01
          race4
                    smoking1
                                                                    weight
                  -4.077e-01
##
      7.673e-03
                                                                 4.718e-01
                                  diabetes1
##
            bmi hypertension1
                                                        SBP
##
                                   4.339e-02
                                                 -6.311e-05
                                                                 4.684e-03
     -1.453e+00 -1.643e-01
##
                                      studyB
                                                     studyC
      vaccine1
                    severity1
##
      5.229e-01
                   -6.944e-01
                                   1.335e+00
                                                  1.320e-01
## Degrees of Freedom: 2512 Total (i.e. Null); 2494 Residual
## Null Deviance:
                       3039
## Residual Deviance: 2725 AIC: 2763
# Report the CV ROC:
glm$results$ROC
## [1] 0.7095743
```

Penalized Logistic Model:

Figure I. Penalized Logistic Model CV ROC Plot

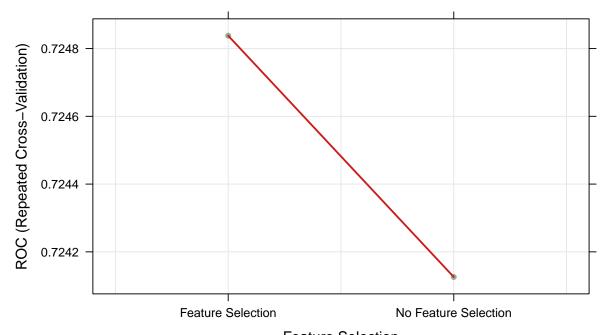


```
# Choose best tuning parameter value:
glmn$bestTune
## alpha lambda
## 851 1 0.0003354626

# Report the CV ROC:
glmn$results[851, ]$ROC
## [1] 0.7079283
```

GAM model for binary response:

Figure II. GAM Model CV ROC Plot



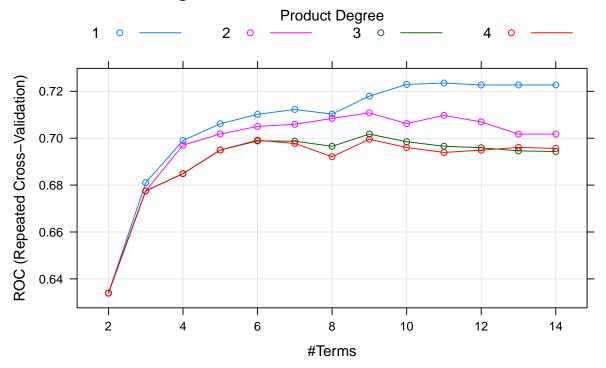
Feature Selection

```
# Report the final model:
gam_2$bestTune
## select method
## 2 TRUE GCV.Cp
coef(gam_2$finalModel)
## (Intercept) gender1 race3 race4 smoking1
## -2.094415e+00 2.880745e-01 9.310134e-02 6.559474e-03 -4.371700e-01
## smoking2 hypertension1 diabetes1 vaccine1 severity1
## -4.784380e-01 -1.857253e-01 1.970598e-02 5.356926e-01 -7.120308e-01
```

```
studyB
                      studyC
                                  s(age).1
                                               s(age).2
                                                             s(age).3
   1.373336e+00 1.675730e-01 -3.547967e-04 1.690790e-03 -1.838724e-03
##
       s(age).4
                    s(age).5
                                  s(age).6
                                               s(age).7
                                                             s(age).8
## -5.165523e-03 1.730323e-03 -4.076744e-03 2.181238e-03 -2.341176e-02
##
       s(age).9
                    s(SBP).1
                                  s(SBP).2
                                               s(SBP).3
                                                             s(SBP).4
## -1.313838e-01 5.677327e-06 3.678094e-07 -1.373775e-07 -4.587642e-07
##
       s(SBP).5
                                               s(SBP).8
                    s(SBP).6
                                  s(SBP).7
                                                             s(SBP).9
## -1.936734e-07 3.521817e-07 3.268165e-07 4.034795e-07 1.063455e-06
##
       s(LDL).1
                   s(LDL).2
                                  s(LDL).3
                                               s(LDL).4
                                                            s(LDL).5
##
  9.888402e-06 9.235410e-07 2.118225e-06 -5.184814e-07 -6.001575e-07
       s(LDL).6
                                  s(LDL).8
                                             s(LDL).9
##
                   s(LDL).7
                                                             s(bmi).1
## -1.067971e-07 3.793180e-07 -2.515578e-06 6.736418e-02 2.008212e-01
##
       s(bmi).2
                s(bmi).3
                                  s(bmi).4
                                               s(bmi).5
                                                             s(bmi).6
## 6.053645e-02 4.628156e-02 -3.554393e-01 9.872649e-02 2.925849e-01
##
       s(bmi).7
                  s(bmi).8
                                  s(bmi).9 s(height).1 s(height).2
## 6.796104e-02 1.848588e+00 -2.913658e-01 -3.745810e-06 -1.490001e-08
##
    s(height).3
                s(height).4
                              s(height).5
                                           s(height).6
                                                         s(height).7
## 7.316762e-07 -6.473545e-07 4.594748e-07 5.722461e-07 3.972392e-07
   s(height).8
                s(height).9
                              s(weight).1
                                           s(weight).2
                                                         s(weight).3
## -2.537800e-06 -1.011582e-06 1.537831e-06 1.359224e-07 3.751313e-07
   s(weight).4
                 s(weight).5
                              s(weight).6
                                           s(weight).7
                                                        s(weight).8
## 3.344343e-07 -2.836629e-07 -2.968417e-07 2.050625e-07 1.225004e-06
   s(weight).9
## -4.006080e-06
# Report the CV ROC:
gam 2$results[2, ]$ROC
## [1] 0.7248379
```

MARS model for binary response:

Figure III. MARS Model CV ROC Plot



```
# Report the final model:
mars 2$bestTune
     nprune degree
## 10
         11
                 1
coef(mars_2$finalModel)
## (Intercept)
                   studyB h(bmi-27.8) h(27.8-bmi)
                                                   vaccine1
                                                                severity1
  -1.5347506
               1.2977373 -0.4282987 -0.1841055
                                                    0.5316052 -0.7196799
                              gender1
    h(61-age)
                 smoking1
                                         smoking2
##
     0.0590261 -0.4376436
                           0.2849957 -0.4923424
# Report the CV ROC:
mars_2$results[37, ]$ROC
## [1] 0.7235168
```

Linear discriminant analysis (LDA):

```
## age
               -4.414766e-02
## gender1
               3.483168e-01
## race2
               5.127539e-01
## race3
               2.087032e-01
## race4
               1.652280e-02
## smoking1 -5.093387e-01
## smoking2
             -5.565945e-01
## height
               -4.842308e-01
## weight
               5.127571e-01
## bmi
               -1.587689e+00
## hypertension1 -2.035363e-01
## diabetes1 5.532383e-02
## SBP
               -7.703822e-06
              6.184843e-03
## LDL
## vaccine1
               6.694769e-01
## severity1
               -7.851869e-01
## studyB
               1.615000e+00
## studyC
               1.104844e-01
# Report the CV ROC:
lda$results$ROC
## [1] 0.7100636
```

Quadratic discriminant analysis (QDA):

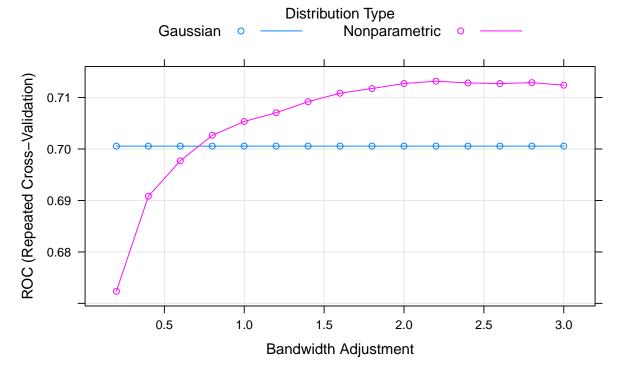
```
set.seed(3521)
qda = train(recovery_time ~ .,
           data = training_sec,
           method = "qda",
           metric = "ROC",
           trControl = ctrl1)
# Report the final model:
qda$finalModel
## Call:
## qda(x, grouping = y)
##
## Prior probabilities of groups:
## great less
## 0.707123 0.292877
##
## Group means:
             age gender1 race2
                                        race3 race4 smoking1
                                                                    smoking2
## great 60.29994 0.4687676 0.04614519 0.1963984 0.09848059 0.3168261 0.10298255
## less 59.69429 0.5339674 0.05706522 0.2146739 0.09375000 0.2500000 0.08016304
         height weight
                          bmi hypertension1 diabetes1
                                                             SBP
## great 169.7715 80.20096 27.89994 0.5098481 0.1508160 130.5093 109.5937
## less 170.3648 79.04755 27.26454 0.4538043 0.1535326 129.6087 110.7527
        vaccine1 severity1 studyB studyC
## great 0.5751266 0.10635903 0.5160383 0.2341024
```

```
## less 0.6942935 0.05842391 0.7839674 0.1127717

# Report the CV ROC:
qda$results$ROC
## [1] 0.6965235
```

Naive Bayes:

Figure IV. NB Model CV ROC Plot

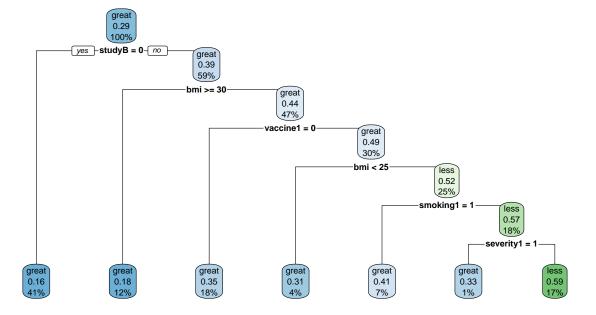


```
# Report the final model:
nb$bestTune
## fL usekernel adjust
## 26 1 TRUE 2.2

# Report the CV ROC:
nb$results[26, ]$ROC
## [1] 0.7131731
```

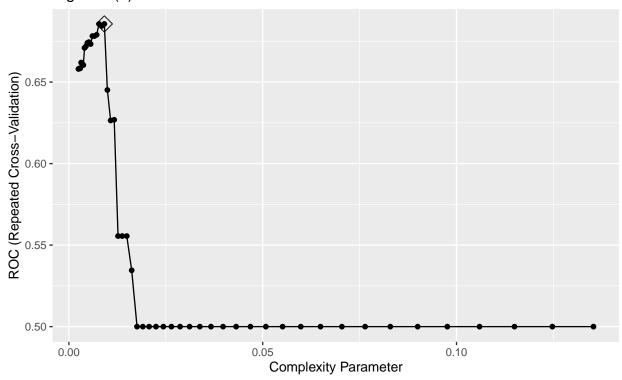
Classification tree:

Figure V(I). Classification Tree

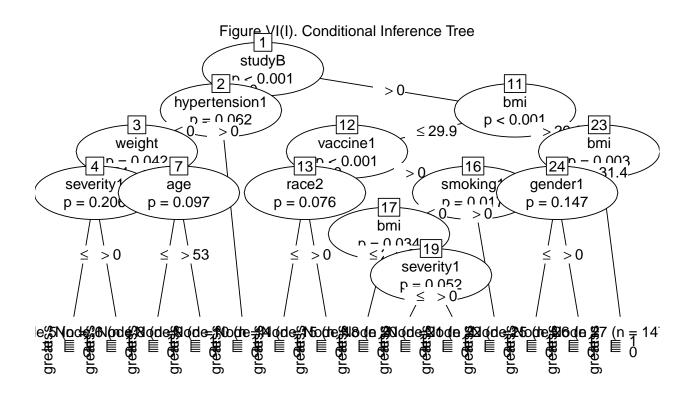


```
# Plot for tuning parameter selection:
ggplot(rpart, highlight = TRUE) + ggtitle("Figure V(II). Classification Tree Model CV ROC Plot")
```

Figure V(II). Classification Tree Model CV ROC Plot

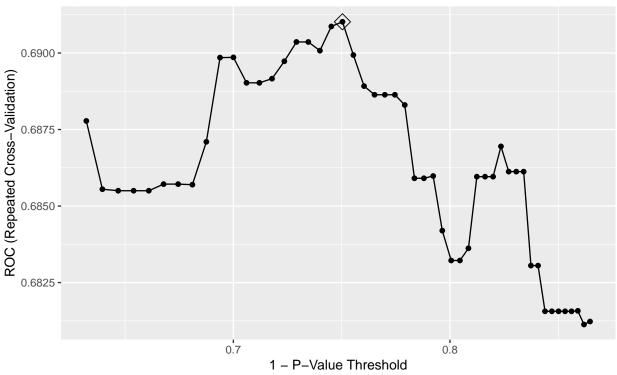


Conditional Inference Tree:



Plot for tuning parameter selection:
ggplot(ctree, highlight = T) + ggtitle("Figure VI(II). CIT Model CV ROC Plot")

Figure VI(II). CIT Model CV ROC Plot



```
# Choose best tuning parameter value:
ctree$bestTune
## mincriterion
## 20  0.7503649

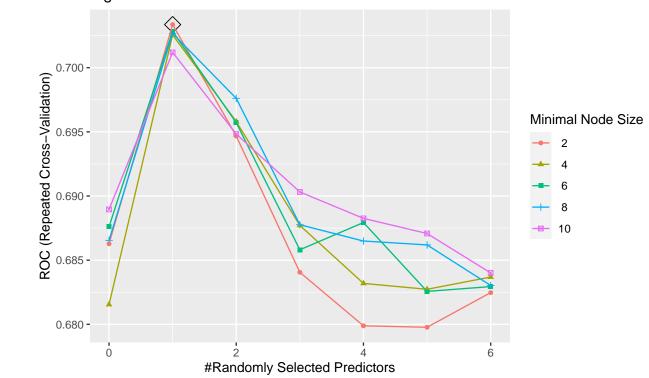
# Report the CV ROC
ctree$results[20, ]$ROC
## [1] 0.6910193
```

Random Forests for binary response:

```
registerDoSEQ()

# Plot for tuning parameter selection:
ggplot(rf_2, highlight = TRUE) + ggtitle("Figure VII. Random Forests Model CV ROC Plot")
```

Figure VII. Random Forests Model CV ROC Plot

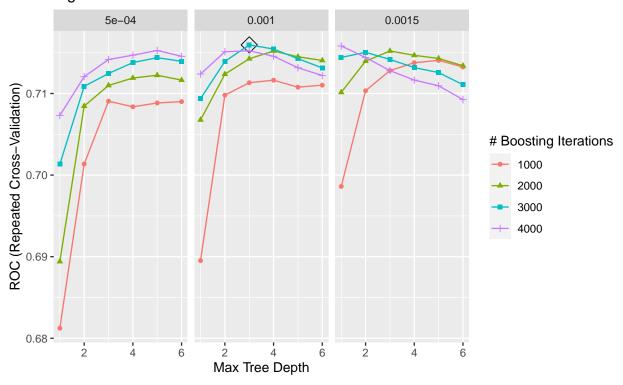


```
# Choose best tuning parameter value:
rf_2$bestTune
## mtry splitrule min.node.size
## 6 1 gini 2

# Report the CV ROC
rf_2$results[6,]$ROC
## [1] 0.703361
```

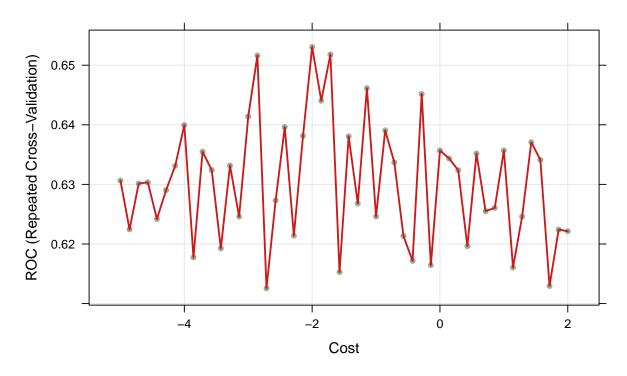
Adaboost Model:

Figure VIII. Adaboost Model CV ROC Plot



Support Vector Machine (linear kernel):

Figure IX. SVM(linear) Model CV ROC Plot



Support Vector Machine (radical kernel):

Figure X. SVM(radical) Model CV ROC Plot

