Cryptography Engineering

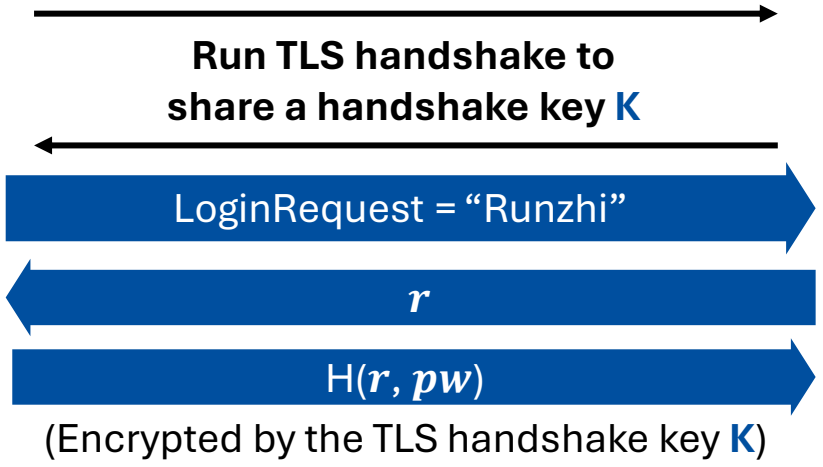
- Lecture 8 (Dec 11, 2024)
- Today's notes:
  - Protocol Study: The SCRAM protocol
  - Password-based Authenticated Key Exchange (PAKE)
  - An (In)secure Example: Encrypted-key-exchange protocol
  - Protocol study: The SRP protocol

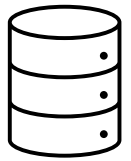
- Coding tasks/Homework:
  - Implement the SCRAM protocol
  - **Bonus**: Informal analysis of SRP
  - **Bonus**: Implement pre-computation attacks on SRP

TLS + Salted Hashes of Passwords

- TLS + salted & hashed passwords
  - Use TLS to protect the transmission of pw
  - No TLS handshake key => Cannot launch offline dictionary attacks

Account = "Runzhi"
password = pw
where pw is some string





User	password_file
Runzhi	$r, H(r, pw)$
Tom	$r_2, H(r_2, pw_2)$
…	…

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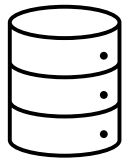
Run TLS handshake to share a handshake key K

LoginRequest = "Runzhi"

r



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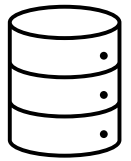

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Is it possible to increase the difficulty of offline attacks?

The SCRAM protocol

- Salted Challenge Response Authentication Mechanism

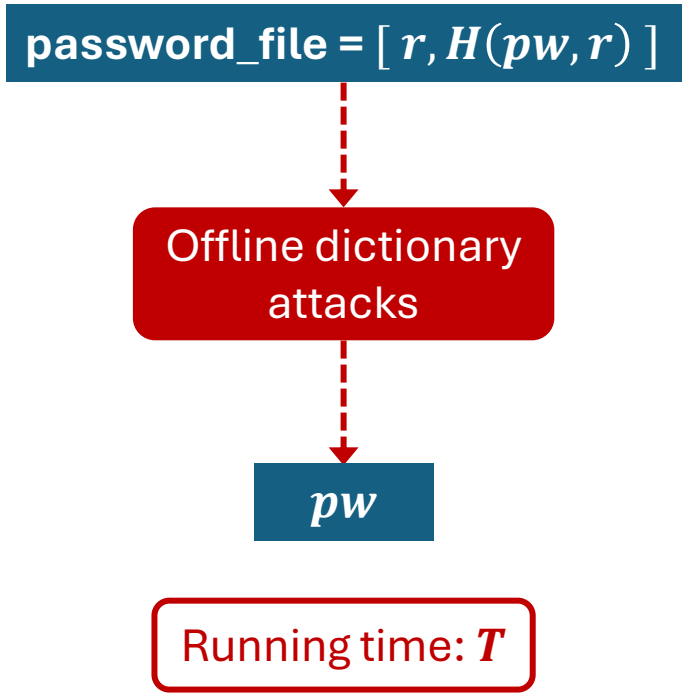
- Main idea:
  1. Add iteration in computing salted & hashed password
  2. Challenge-response Mechanism
  3. Run over TLS

- Other Important Features:
  - ➢ Inherent Resistance to Replay Attacks

    (TLS + salted & hashed passwords resists replay attacks because of TLS, while SCRAM resists replay attacks inherently, independent of the transport layer.)
  - ➢ Mutual Authentication

The SCRAM protocol

- Add iteration in computing salted & hashed password:



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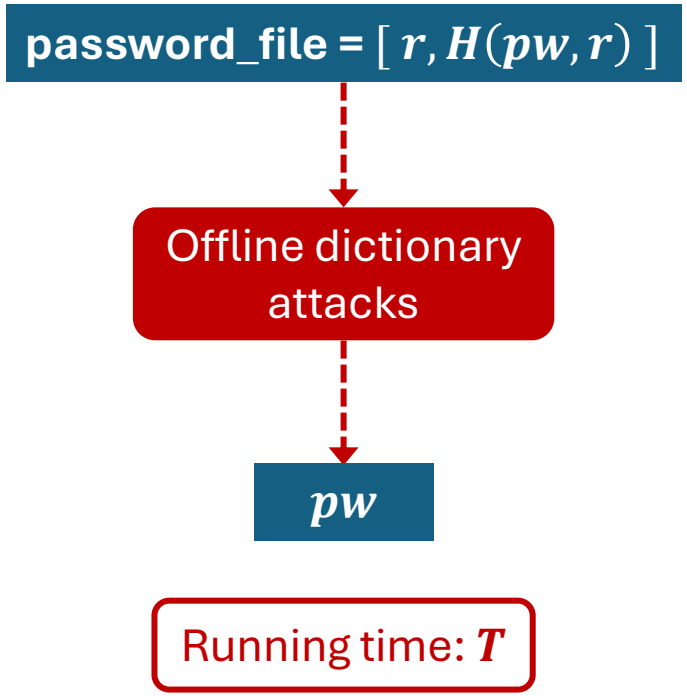

password_file = [$r, H^2(pw, r)$]
where $H^2(pw, r) = H(pw, H(pw, r))$

The SCRAM protocol

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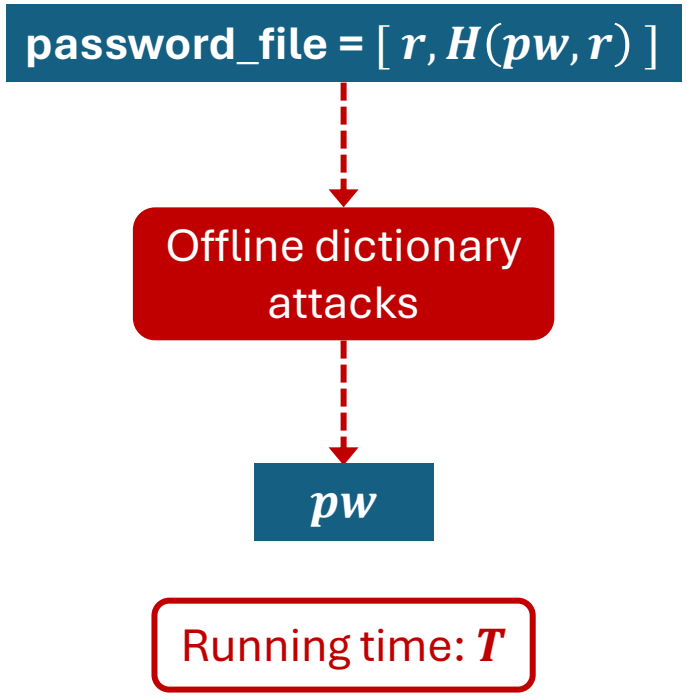
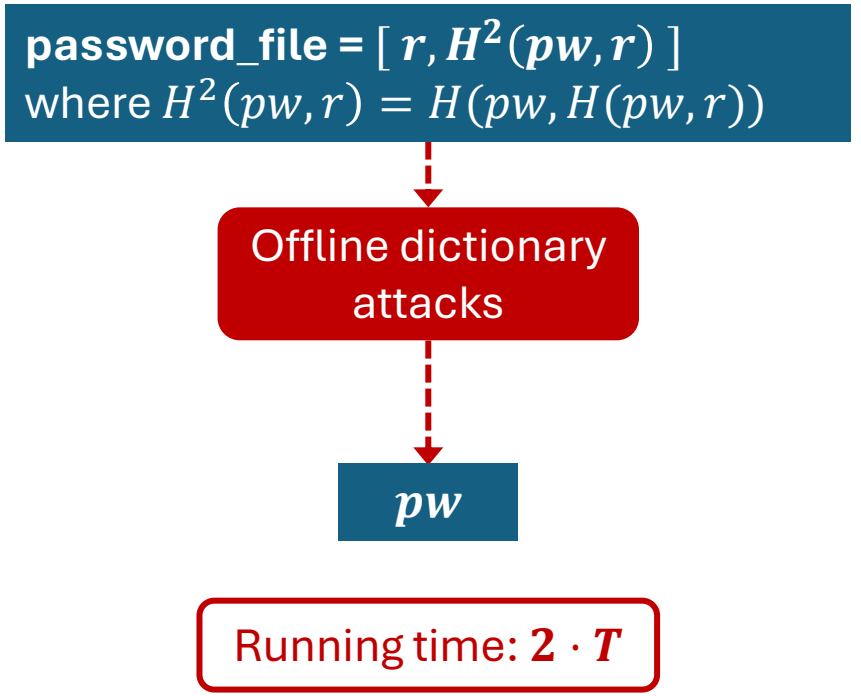




The SCRAM protocol

- Add iteration in computing salted & hashed password:

Iterate_hash_with_salt(*password*, *salt*, *num_of_iteration*):

// *salt* can be **16- or 32**-byte

// *num_of_iteration* can be **4096** or even **100,000**

// All variable are bytes with big-endian order

pw = *password*

padded_salt = *salt* || b'\x00\x00\x00\x01' // Append a 4-byte string 0x00000001 (in hex)

$hash_1 = \mathrm{HMAC}(pw, padded\_salt)$ // We use keyed HMAC, where the key to HMAC is the password

For i from 2 to *num_of_iteration*: // Iteratively evaluate the HMAC of pw and previous HMAC

$hash_i = \mathrm{HMAC}(pw, hash_{i-1})$

Password_file = $hash_1 \oplus hash_2 \oplus \cdots \oplus hash_{\mathrm{num\_of\_iteration}}$ // One integrate this part into the loop

return Password_file

The SCRAM protocol

- Add iteration in computing salted & hashed password:

A simpler description:
(using the notation $H^n(pw, r)$ = Iterate_hash_with_salt(pw, r, n)

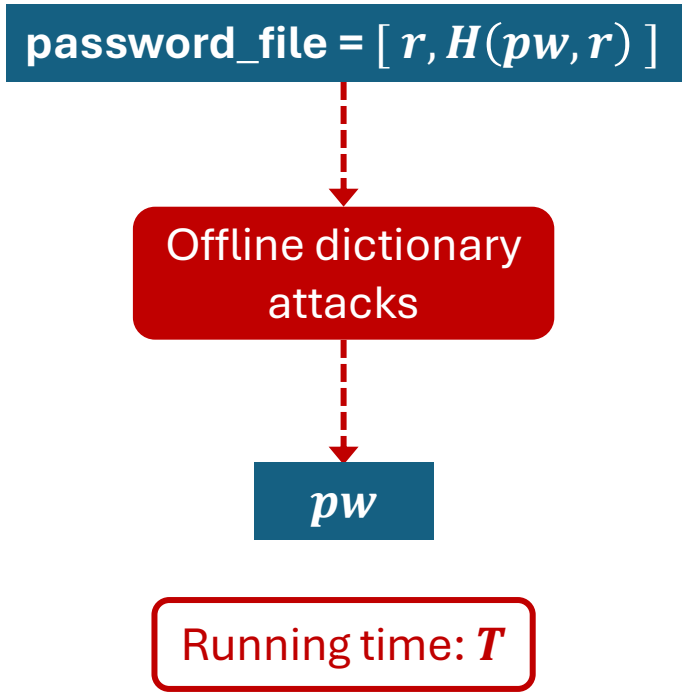
Given r, n, pw**:**

$$
\begin{aligned}
\mathrm{U}_1 &= \mathbf{HMAC}(pw, r \,||\, \text{b'\x00\x00\x00\x01'}) \\
\mathrm{U}_2 &= \mathbf{HMAC}(pw, \mathrm{U}_1) \\
&\vdots \\
\mathrm{U}_{n-1} &= \mathbf{HMAC}(pw, \mathrm{U}_{n-2}) \\
\mathrm{U}_n &= \mathbf{HMAC}(pw, \mathrm{U}_{n-1})
\end{aligned}
$$

We compute $H^n(pw, r) = \mathrm{U}_1 \oplus \mathrm{U}_2 \oplus \cdots \oplus \mathrm{U}_{n-1} \oplus \mathrm{U}_n$

The SCRAM protocol

- Add iteration in computing salted & hashed password:



The SCRAM protocol

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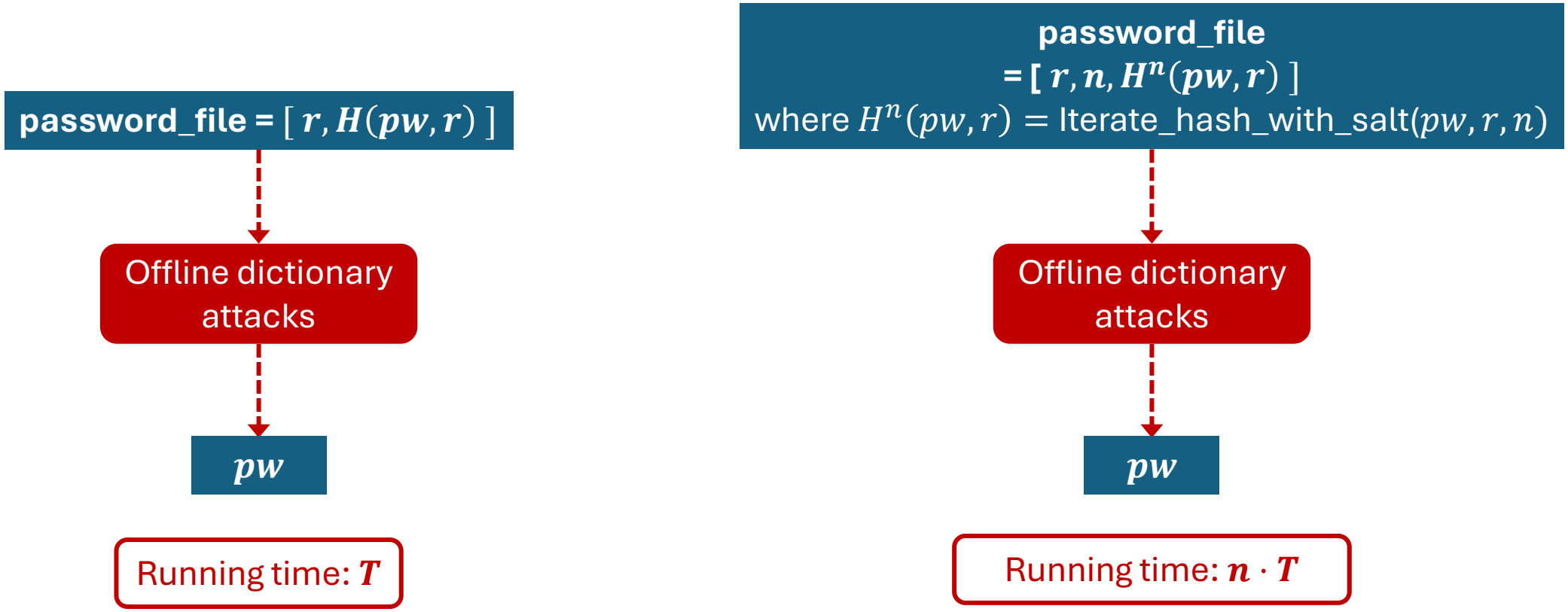

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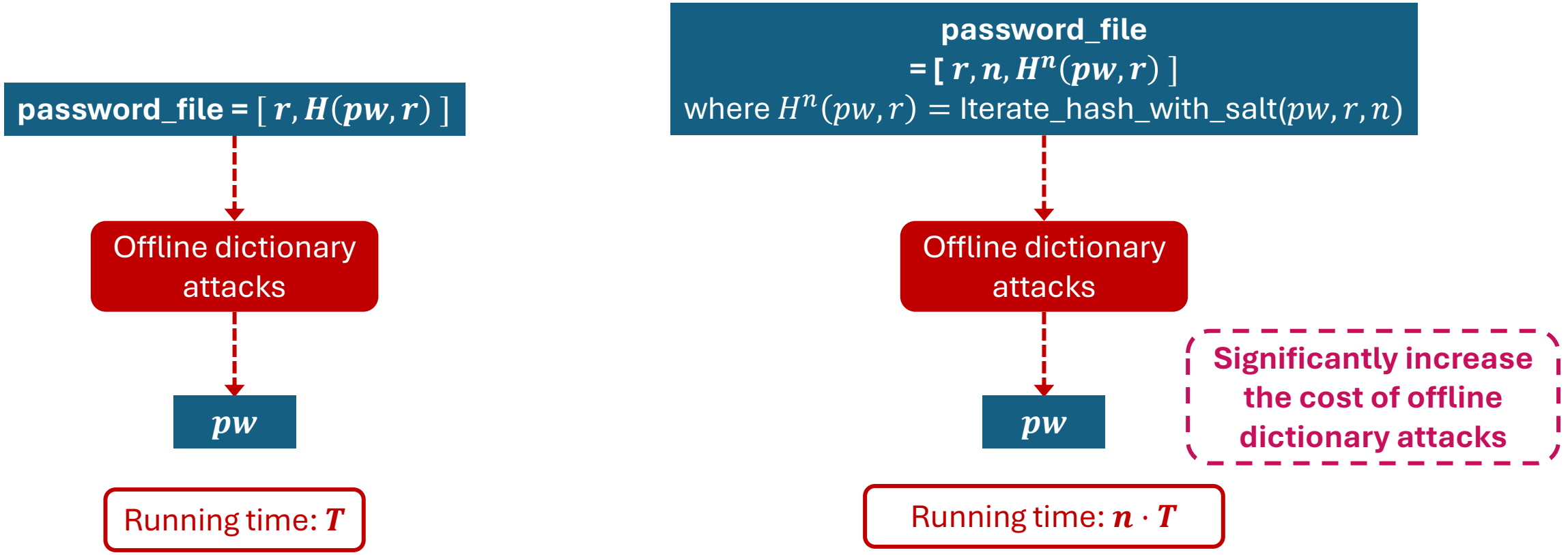
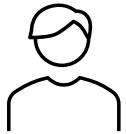
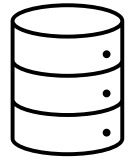


The SCRAM protocol

- Challenge-response paradigm



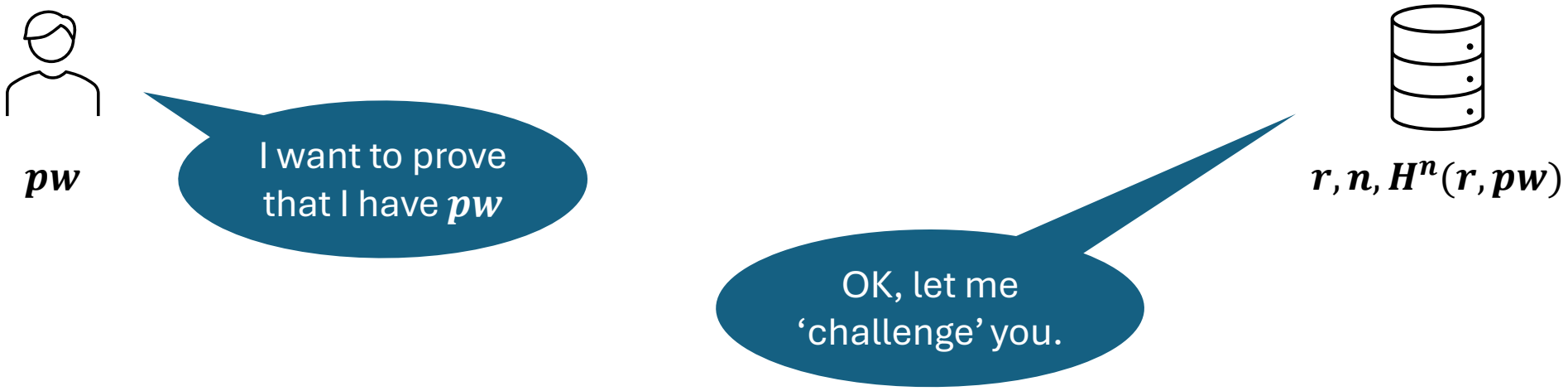
pw



$r, n, H^n(r, pw)$

The SCRAM protocol

- Challenge-response paradigm



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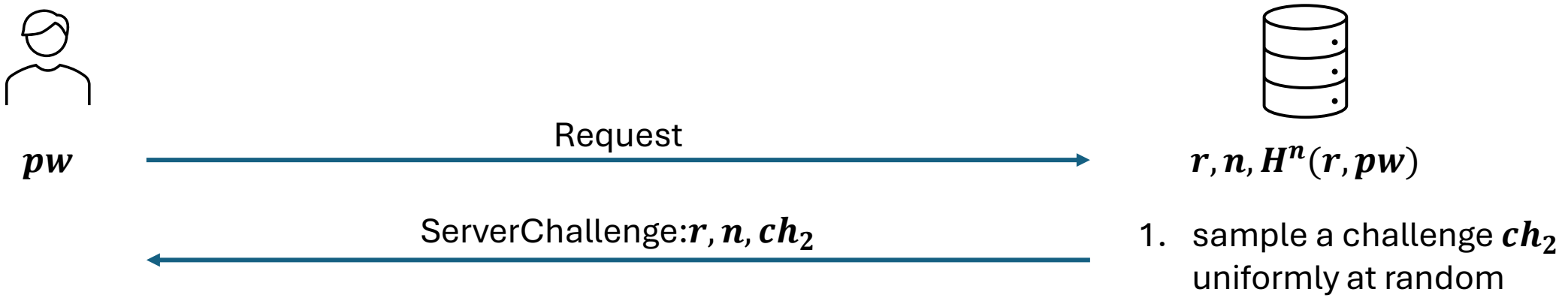

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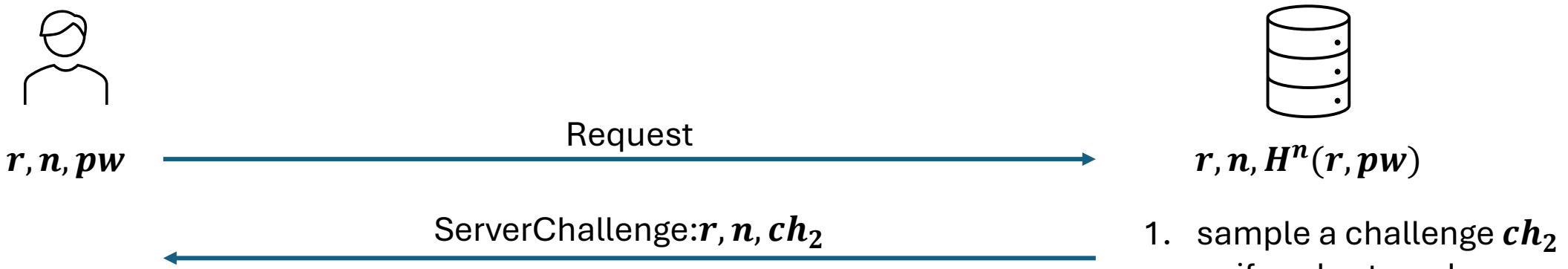

2. *Salted_pw* = $H^n(r, pw)$
3. *Client_key* = $\mathbf{HMAC}$(*Salted_pw*, 'Client key')
4. *Auth_msg* = [Client's Name] || r, n, ch_2
5. *Client_sign* = $\mathbf{HMAC}(\mathbf{H}(Client\_key), Auth\_msg)$ // Here $\mathbf{H}$ is the hash function used in $\mathbf{HMAC}$
6. ***Client_proof*** = *Client_key* $\oplus$ *Client_sign*

The SCRAM protocol

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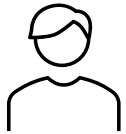
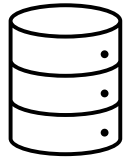


r, n, pw

Request



$r, n, H^n(r, pw)$

ServerChallenge:r, n, ch_2

1. sample a challenge ch_2 uniformly at random

2. *Salted_pw* = $H^n(r, pw)$
3. *Client_key* = $\mathbf{HMAC}$(*Salted_pw*, 'Client key')
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6. ***Client_proof*** = *Client_key* $\oplus$ *Client_sign*

ClientProof: ***Client_proof***

6. Verify ***Client_proof***

The SCRAM protocol

- Challenge-response paradigm

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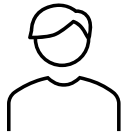
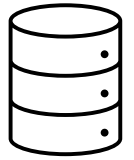


r, n, pw

1. sample a challenge ch_1 uniformly at random

ClientChallenge: ch_1



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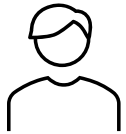

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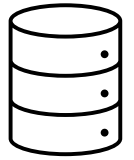

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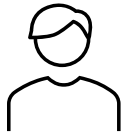
ServerSign: ***Server_sign***

The SCRAM protocol

- Challenge-response paradigm



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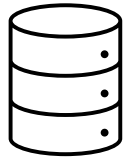

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Run TLS handshake to share a handshake key K and some channel binding info TLS_INFO

1. Pick a random client challenge"ch_1

ClientFirst: [ClientName], ch_1

2. Pick a random server challenge"ch_2

ServerFirst: $ch_1||ch_2, r, n$

3. Compute ***Client_proof*** using **Auth_msg**

ClientFinal: TLS_INFO, $ch_1||ch_2$, ***Client_proof***

4. Verify ***Client_proof.***
If valid:
Compute ***Server_sign*** using **Auth_msg**

5. Verify ***Server_sign***

ServerFinal: ***Server_sign***

Auth_msg = [ClientName] || $ch_1||ch_2$ || r || n || TLS_INFO

The SCRAM protocol

- Main idea:
  1. Add iteration in computing salted & hashed password
  2. Challenge-response Mechanism
  3. Run over TLS

- Used in some systems that require higher security guarantees…
  - ➢ IMAP / POP / SMTP / …
  - ➢ Database Authentication (e.g., MongoDB)…

Password-based Authenticated Key Exchange

- Previous protocols: TLS + salted & hashed (& iterated) passwords
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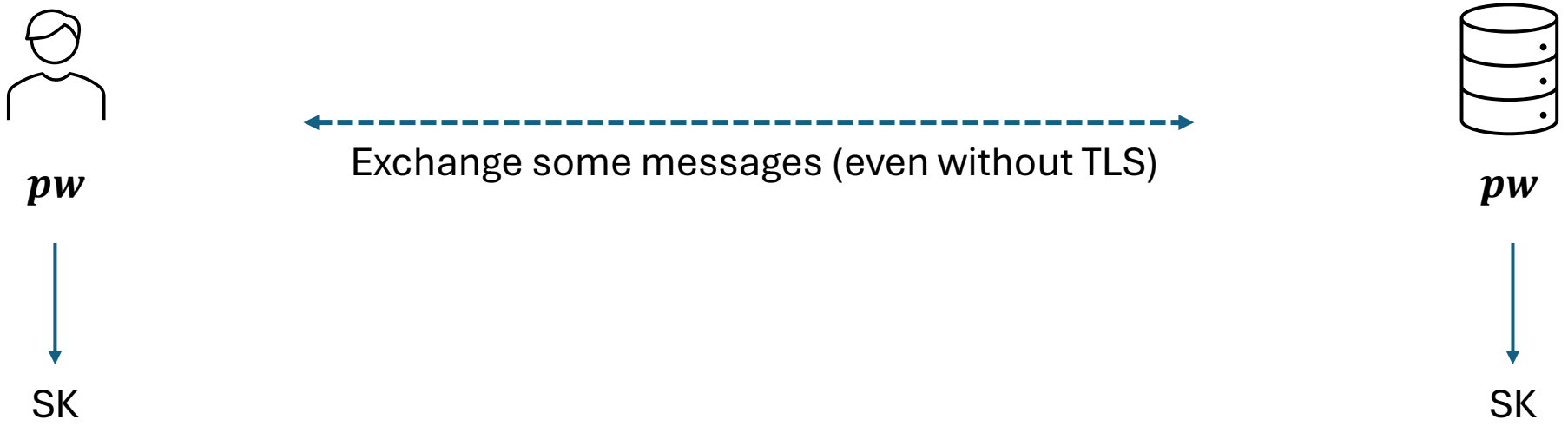
- **An alternative solution: Password-based Authenticated Key Exchange (PAKE)**

Password-based Authenticated Key Exchange

- **(Symmetric) PAKE:**



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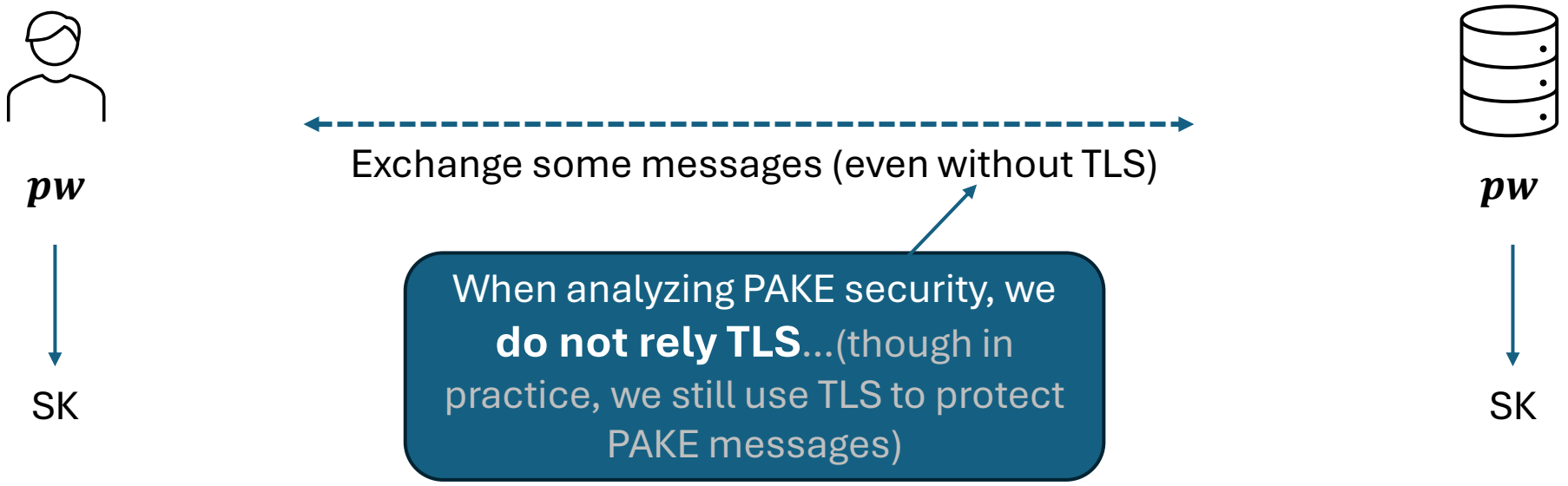

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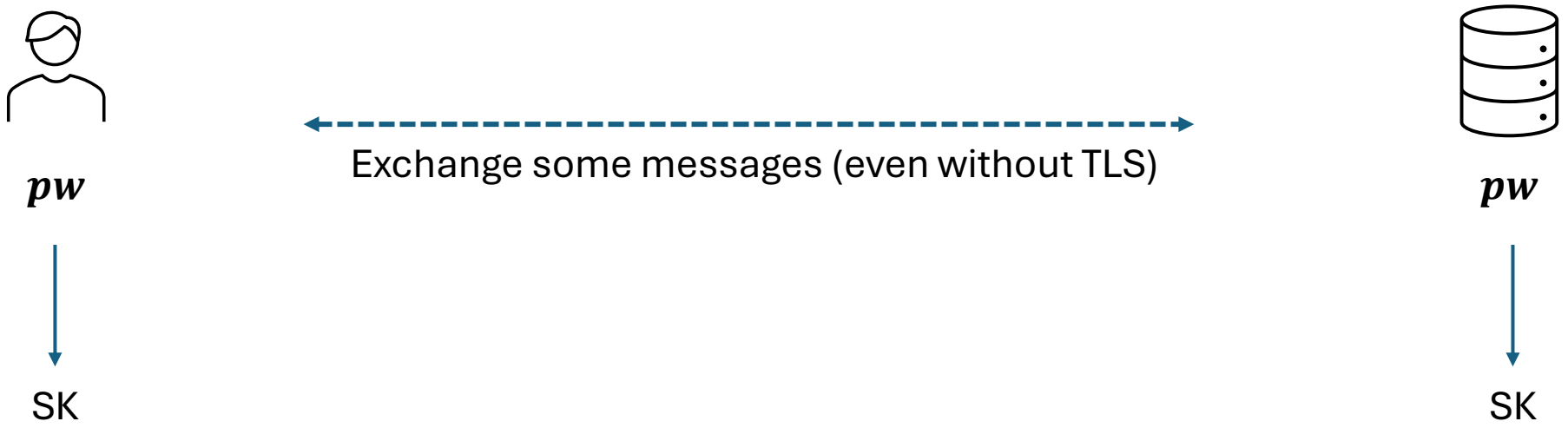
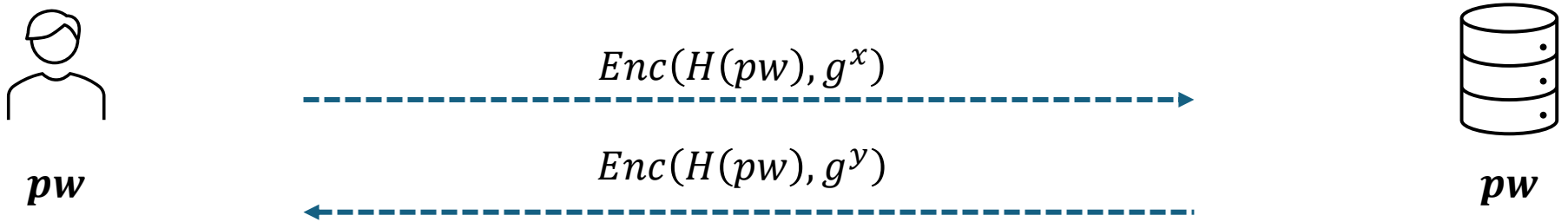


Primary Goals:

- **(1) Resistance to Offline Dictionary attacks (2) The shared key SK is *pseudorandom***

Password-based Authenticated Key Exchange

- **Encrypted-Key-Exchange DH (EKE-DH) protocols:**
  - **Main idea:** Use pw to encrypt the underlying DH key exchange



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- Is it secure?

Password-based Authenticated Key Exchange

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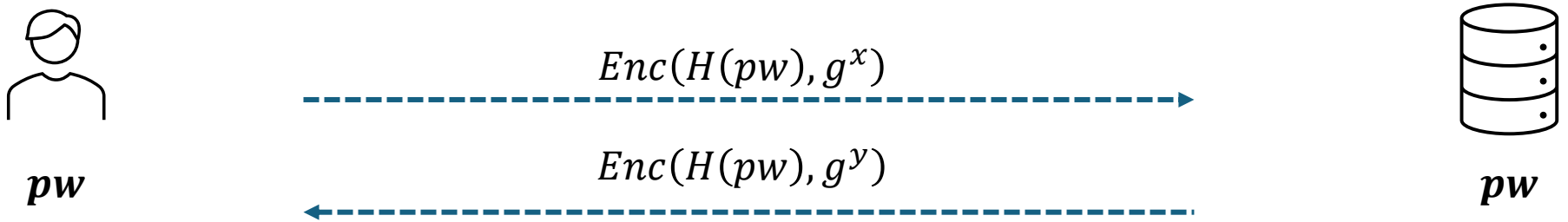

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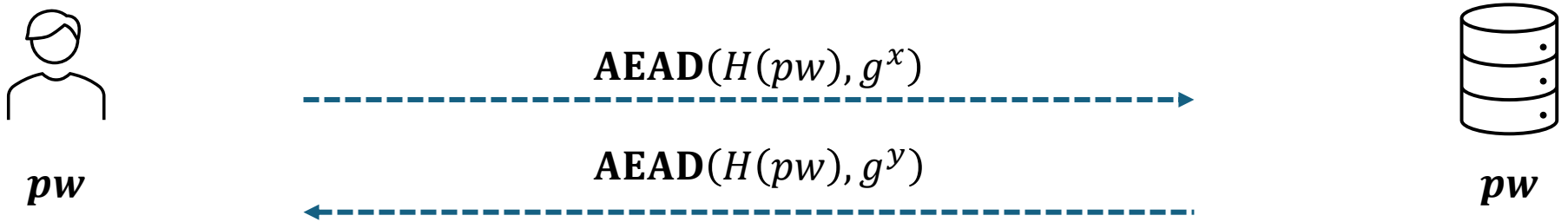
- Is it secure? **Depends on the encryption!**

Password-based Authenticated Key Exchange

- EKE-DH protocols **based on AEAD:**



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Password-based Authenticated Key Exchange

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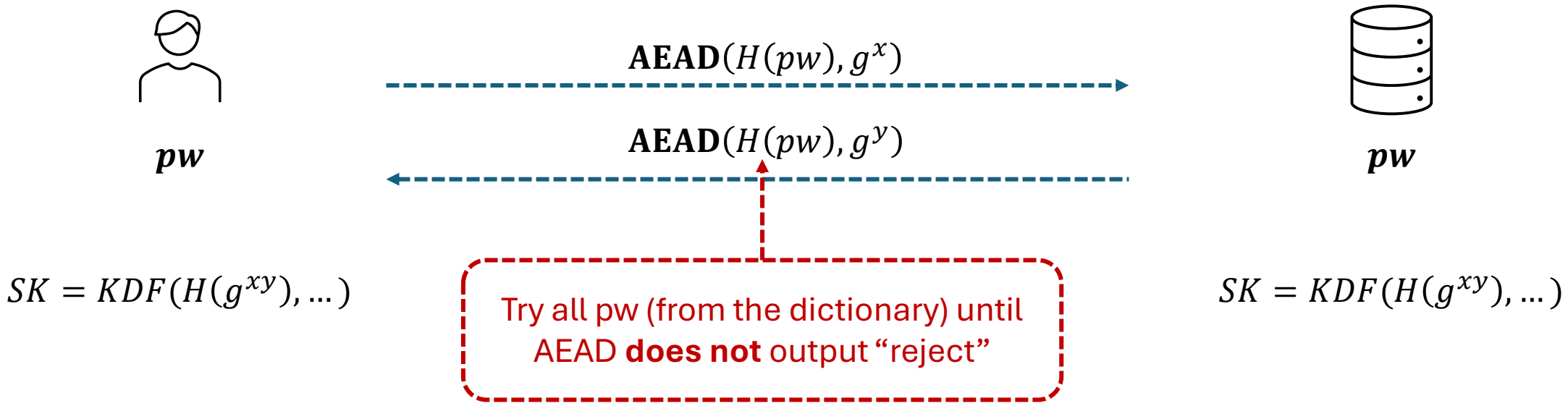

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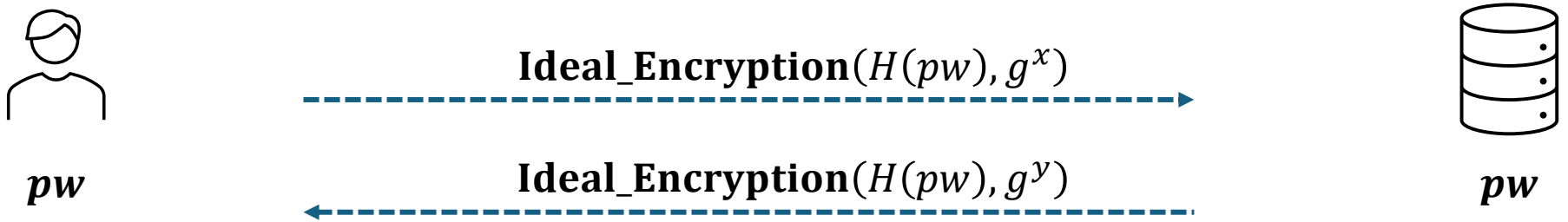
Password-based Authenticated Key Exchange

- EKE-DH protocols **based on an "ideal" encryption:**



$SK = KDF(H(g^{xy}), \dots)$ $\qquad$ $SK = KDF(H(g^{xy}), \dots)$

- The **ideal encryption** has the following properties:
  - Outputs of encryption and decryption **are (pseudo)random *even if the key has low entropy***
  - Namely, if the adversary does not have the correct pw, the outputs of encryption/decryption are some random group elements.

Password-based Authenticated Key Exchange

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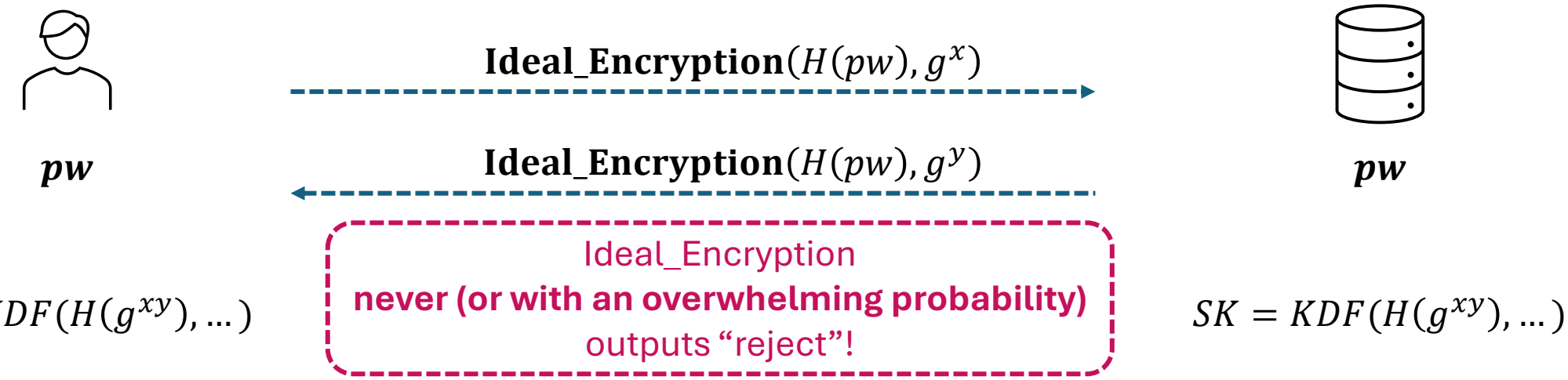

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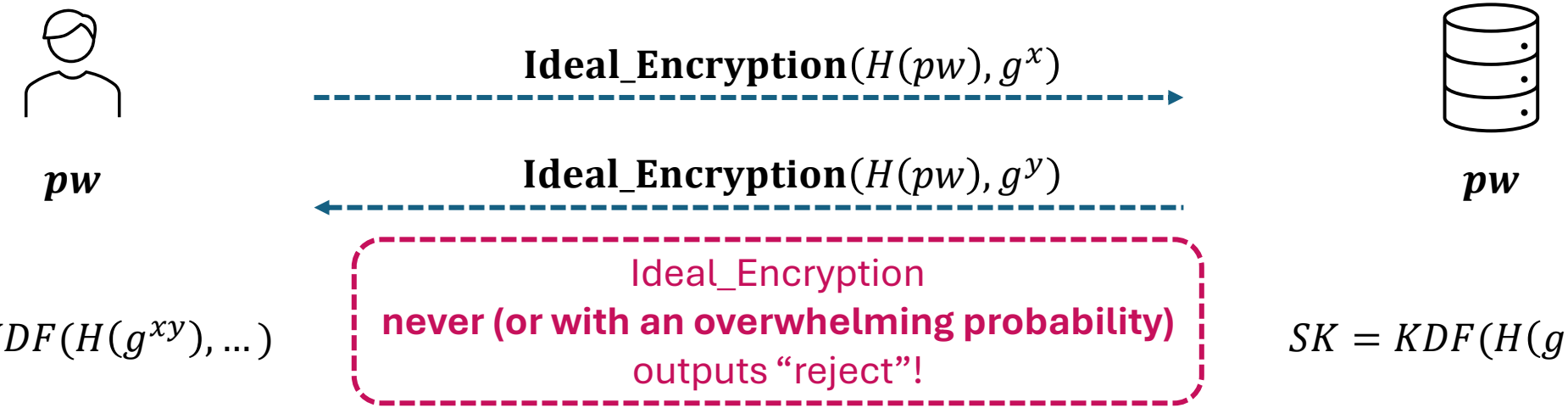

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    random group eleme

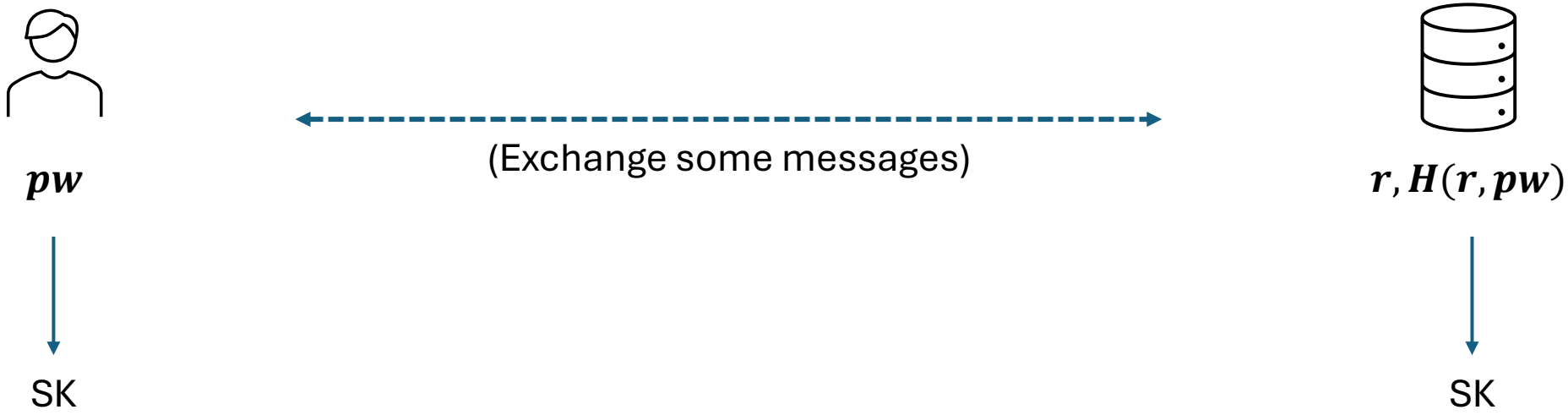
How to design it (with high efficiency & strong security): **Open problem**

has low entropy

tion/decryption are some

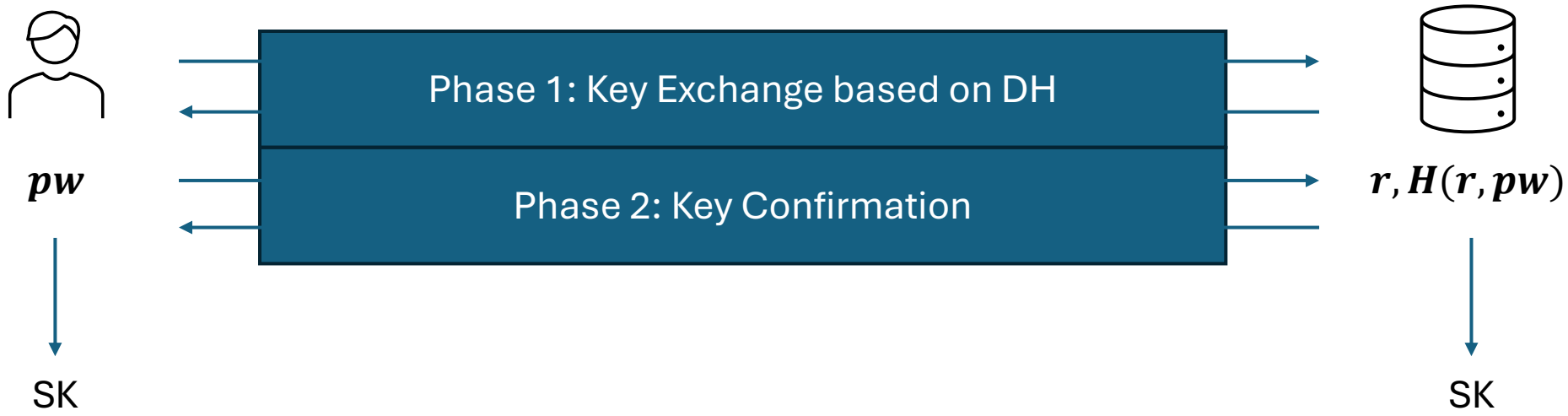
Password-based Authenticated Key Exchange

- **Asymmetric PAKE (aPAKE):**



Password-based Authenticated Key Exchange

- **Secure Remote Password (SRP) Protocol**



- Based on module integer groups / Not directly compatible with Elliptic Curves
- Apple ID Authentication / Blizzard Entertainment

Password-based Authenticated Key Exchange

- **Secure Remote Password (SRP) Protocol (version 6a)**

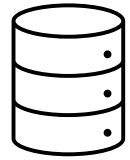
pw

Public Parameters:

q	a large prime
$N = 2q + 1$	a prime (we call it as safe prime)
$\mathbb{G}$	a sub-group of $\mathbb{Z}_N$ with order q
g	the generator of $\mathbb{G}$

Notations:

Let h be an integer in $\mathbb{Z}_N$.
If $h \in \mathbb{G}$ and $x \in \mathbb{Z}_q$, then we denote $h^x := h^x \ mod\ N$



Password file:
$r, v = g^{H(r, [user\_name], pw)}$

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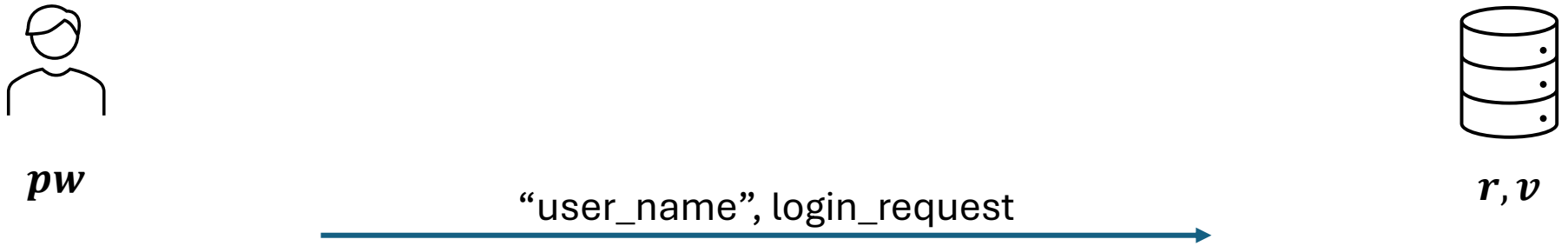
- **SRP-v6a: (1) Key Exchange phase** (2) Key Confirmation phase



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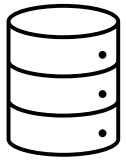

r, v

"user_name", login_request

r, B

$k = H_5(p, g)$

$b \leftarrow_{\$} \mathbb{Z}_{p-1}$

$B = k \cdot v + g^b$

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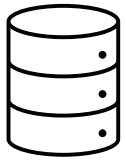

r, v

$k = H_5(p, g)$
$b \leftarrow_\$ \mathbb{Z}_{p-1}$
$B = k \cdot v + g^b$

"user_name", login_request →

← r, B

$rw = H(r, [\text{user\_name}], pw)$
$v = g^{rw}$
$a \leftarrow_\$ \mathbb{Z}_{p-1}, A = g^a$

A →

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- **SRP-v6a: (1) Key Exchange phase** (2) Key Confirmation phase

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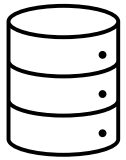

r, v

"user_name", login_request

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$b \leftarrow_\$ \mathbb{Z}_{p-1}$
$B = k \cdot v + g^b$

r, B

$rw = H(r, [\text{user\_name}], pw)$
$v = g^{rw}$
$a \leftarrow_\$ \mathbb{Z}_{p-1}, A = g^a$

A

$k = H_5(p, g), u = H_6(A, B)$
$SS = (B - k \cdot v)^{a+u \cdot rw}$

$u = H_6(A, B)$
$SS = (A \cdot v^u)^b$

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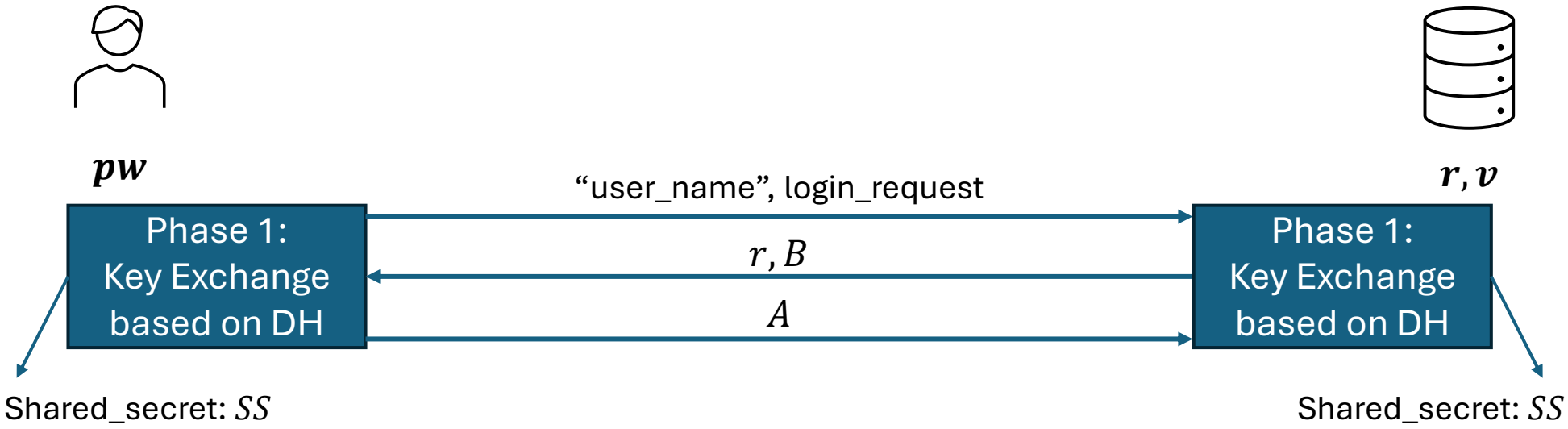
- **SRP-v6a:** (1) Key Exchange phase **(2) Key Confirmation phase**



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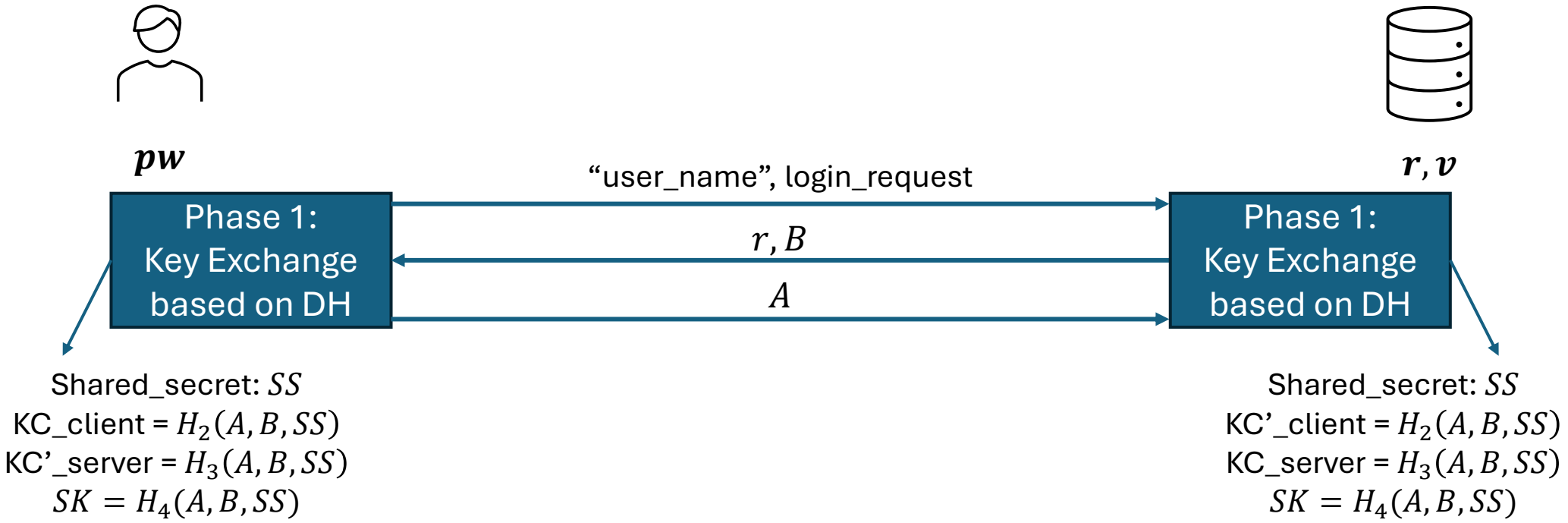

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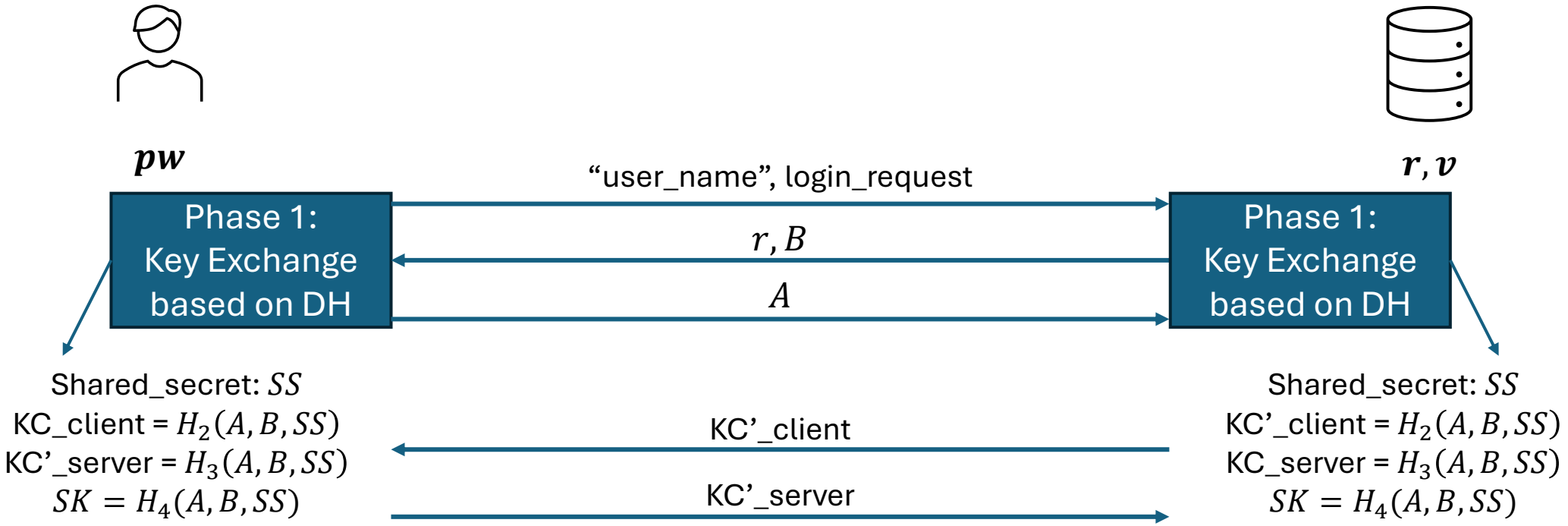

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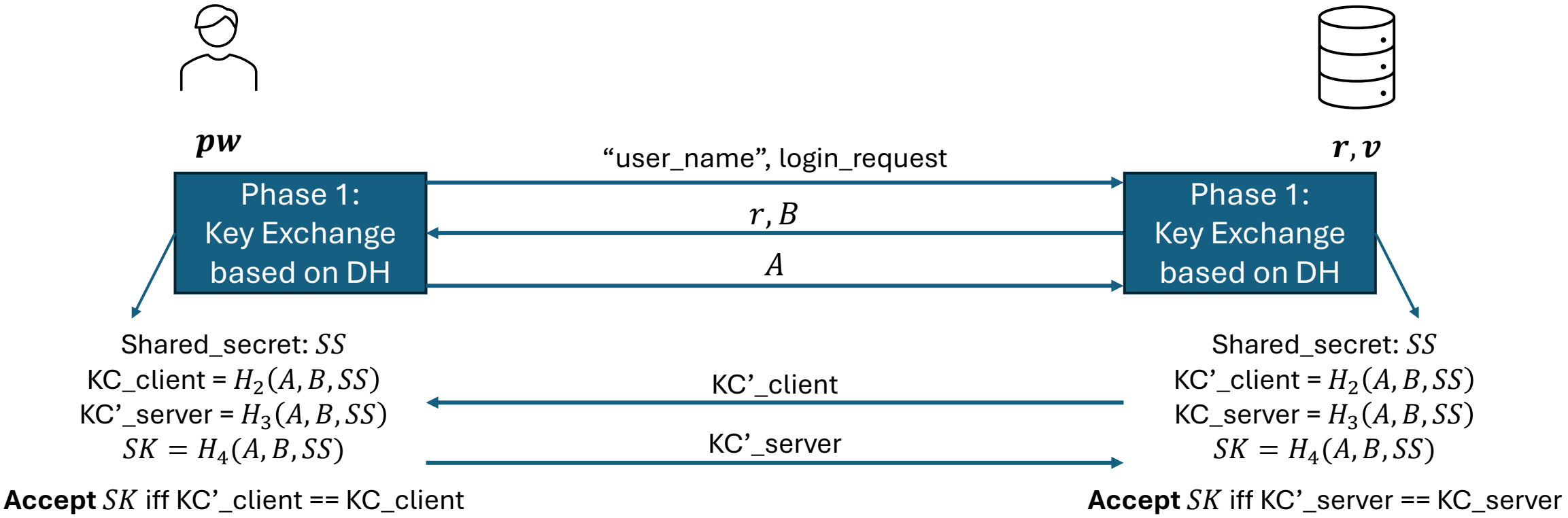

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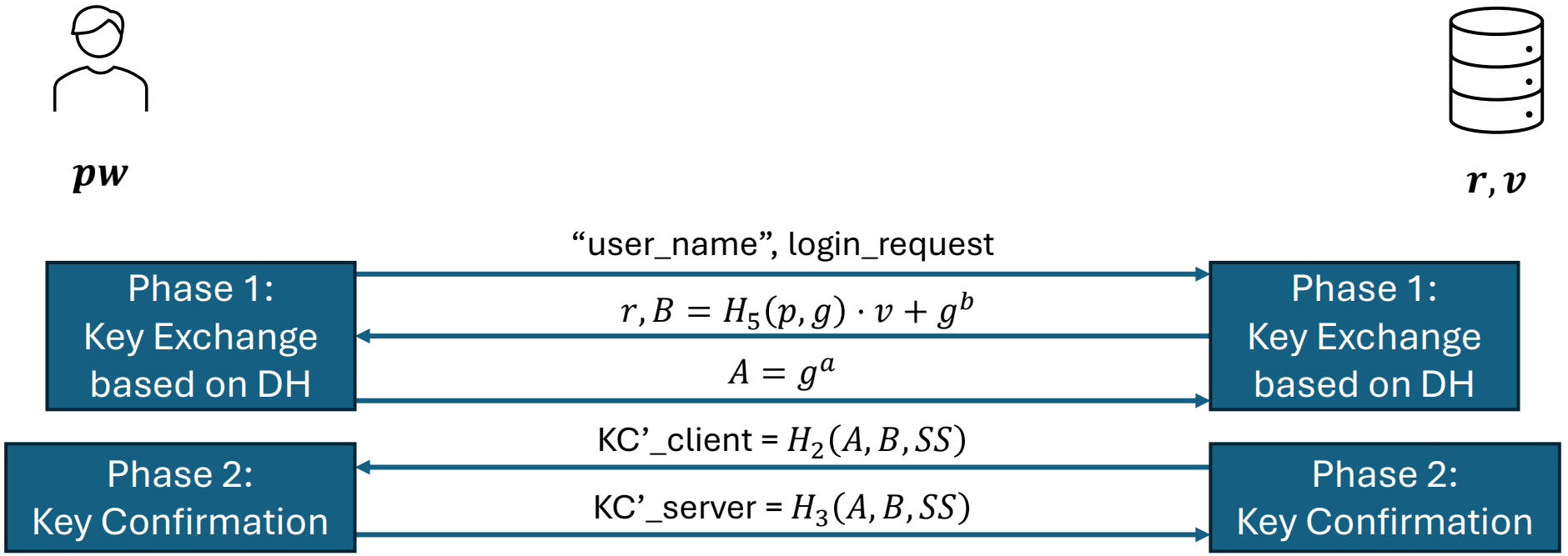
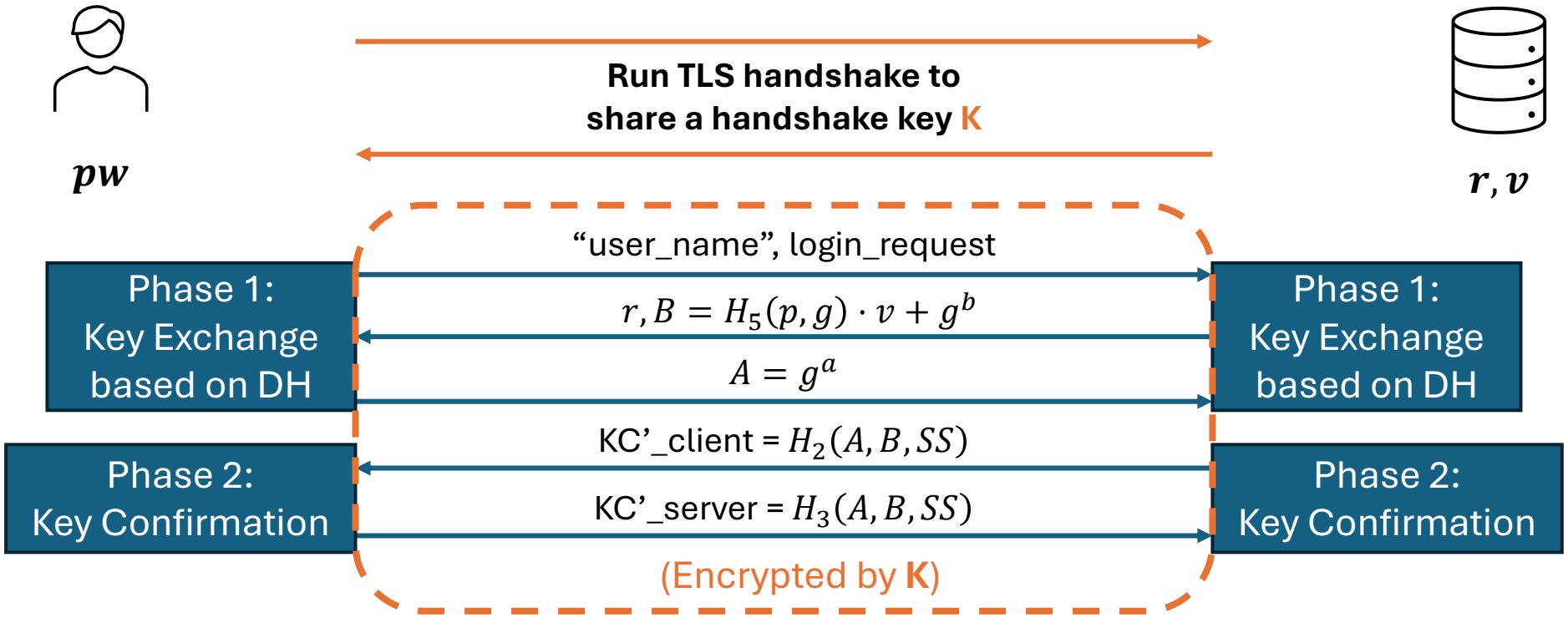
- **SRP-v6a:**



Password-based Authenticated Key Exchange

- **TLS + SRP-v6a:**



Homework

- Implement the SCRAM protocol (You do not need to use sockets, but your program should draw the message flows)
- **Bonus:** Try arguing that, even though SRP-v6a is run without using TLS encrypted channel, the adversary still cannot “easily” launch offline dictionary attacks on it. Just write a simple pdf to argue it. (Hint: Using specific example is better than providing abstract explanations)

  (You can ask AI, but then you should learn its answer and write a human-friendly answer by yourself, since it is not hard to detect that a solution is written from AI)

Further Reading

- RFC document of SRCAM: https://datatracker.ietf.org/doc/html/rfc5802
- Password-Based Key Derivation Function:

  https://datatracker.ietf.org/doc/html/rfc8018#page-11
- Analysis on SRP: *Provable Security Analysis of the Secure Remote Password Protocol,* https://eprint.iacr.org/2023/1457
- Matthew Green's blog: *Should you use SRP?* *https://blog.cryptographyengineering.com/should-you-use-srp/*