$$A = \begin{pmatrix} 1 & 2 \\ 1 & 0 \end{pmatrix} \quad det(A - \lambda 1) = det \cdot \begin{pmatrix} 1 - \lambda & 2 \\ 1 & -\lambda \end{pmatrix} = \lambda^2 - \lambda - 2 = (\lambda + 1)(\lambda - 2)$$

$$\lambda_1 = -1, \quad \lambda_2 = 2.$$

$$(\mathbf{A} - \lambda_1 \mathbf{I}) = \begin{pmatrix} 1 & 2 \\ 1 & 0 \end{pmatrix} - \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} = \begin{pmatrix} 2 & 2 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} X_{11} \\ X_{12} \end{pmatrix} = 0 \quad X_1 = \begin{pmatrix} -1 & 1 \end{pmatrix}^T$$

$$A - \lambda_2 \mathbf{1} = \begin{pmatrix} 1 & 2 \\ 1 & 0 \end{pmatrix} - \begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix} = \begin{pmatrix} 7 & 2 \\ 1 & -2 \end{pmatrix} \begin{pmatrix} X_{22} \\ X_{122} \end{pmatrix} = 0 \qquad X_{22} = (2_{11})^T$$

.. A has real eigenvalues & vectors, but Aisn't Symmetre. cbs True.

$$A = S \wedge S^{T}$$
. Six orthonormal. & $S^{T} = S^{T}$
 $A^{T} = (S^{T})^{T} \wedge^{T} S^{T} = S \wedge S^{T} = A$.

(s) if A is symmetric. O A can be decomposed by an orthograf

:, A camba is a matrix with real eigenvalues & orthonormal eigenvectors

i, from (b). At is symmetric.

(d) False.

$$A = \begin{pmatrix} 1 & 2 \\ 2 & 4 \end{pmatrix}$$
. $\lambda_1 = 0$ $X_1 = (2, -1)^T$ $\lambda_2 = 5$ $X_2 = (1, 2)^T$
 $\therefore S = \begin{pmatrix} 2 & 1 \\ -1 & 2 \end{pmatrix}$ is not symmetric.

2. For positive demfinite matrix, 4x, XAX must be positive

Assume that Air = 0 or < 0 let x = (0 - ... 1 -... 0) (only xi = 1)

10)
$$(x_1 x_2 + x_3)$$
 $(\frac{1}{1} 0) \frac{1}{2} \frac{1}{2} (\frac{x_2}{x_3}) = 4x_1 + 2x_1x_2 + 2x_1x_3 + 4x_2x_3 + 5x_3x_3^2 + 5x_3x_3^2$

 dz_2 dusi313 1
d22523 (d11512 d11512 (d22521 d22522 d23522 dz3 d1 933 243 d 11 d 22 S 2 d233 523 033 = 1 SE C13 = S13 S153 CIZ