PROBABILITY

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13.1.3 [1] If $\Pr(A) = 0.8$, $\Pr(B) = 0.5$ and $\Pr(B|A = 0.4)$, find
(i)$\Pr(AB)$
(ii)$\Pr(A|B)$
(iii)$\Pr(A + B)$

Solution:

13.2.3 $\Pr(AB)$
Now, we know that

$$\Pr(B|A) = \frac{\Pr(AB)}{\Pr(A)} \tag{13.2.3.1}$$

$$0.4 = \frac{\Pr(AB)}{\Pr(A)} \tag{13.2.3.2}$$

$$0.4 = \frac{\Pr(AB)}{0.8} \tag{13.2.3.3}$$

$$\Pr(AB) = 0.4 \times 0.8 \tag{13.2.3.4}$$

$$\Pr(AB) = 0.32 \tag{13.2.3.5}$$

13.3.3 $\Pr(A|B)$

$$\Pr(A|B) = \frac{\Pr(AB)}{\Pr(B)} \tag{13.3.3.1}$$

$$= \frac{\Pr(B|A)\Pr(A)}{\Pr(B)}. \tag{13.3.3.2}$$

$$= \frac{0.4 \times 0.8}{0.5} \tag{13.3.3.3}$$

$$= \frac{0.32}{0.5} \tag{13.3.3.4}$$

$$= 0.64 \tag{13.3.3.5}$$

$$\Pr(A|B) = 0.64 \tag{13.3.3.6}$$

[1] Read question numbers as (CHAPTER NUMBER).(EXERCISE NUMBER).(QUESTION NUMBER)

13.4.3 $\Pr(A+B)$

$$\Pr(A+B) = \Pr(A) + \Pr(B) - \Pr(AB) \quad (13.4.3.1)$$

$$Substitute(13.2.3.5)in(13.4.3.1) \quad (13.4.3.2)$$

$$= 0.8 + 0.5 - 0.32 \quad (13.4.3.3)$$

$$= 1.3 - 0.32 \quad (13.4.3.4)$$

$$= 0.98 \quad (13.4.3.5)$$

$$\Pr(A+B) = 0.98 \quad (13.4.3.6)$$