PROBABILITY

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13.1.3 [1] If $\Pr(A) = 0.8$, $\Pr(B) = 0.5$ and $\Pr(B|A = 0.4)$, find

13.2.3 $\Pr(AB)$

13.3.3 $\Pr(A|B)$

13.4.3 $\Pr(A + B)$

Solution:

13.5.3 $\Pr(AB)$
Now, we know that

$$\Pr(B|A) = \frac{\Pr(AB)}{\Pr(A)} \tag{13.5.3.1}$$

$$0.4 = \frac{\Pr(AB)}{\Pr(A)} \tag{13.5.3.2}$$

$$0.4 = \frac{\Pr(AB)}{0.8} \tag{13.5.3.3}$$

$$\Pr(AB) = 0.4 \times 0.8 \tag{13.5.3.4}$$

$$\Pr(AB) = 0.32 \tag{13.5.3.5}$$

13.6.3 $\Pr(A|B)$

$$\Pr(A|B) = \frac{\Pr(AB)}{\Pr(B)} \tag{13.6.3.1}$$

$$= \frac{\Pr(B|A)\Pr(A)}{\Pr(B)}. \tag{13.6.3.2}$$

$$= \frac{0.4 \times 0.8}{0.5} \tag{13.6.3.3}$$

$$= \frac{0.32}{0.5} \tag{13.6.3.4}$$

$$= 0.64 \tag{13.6.3.5}$$

$$\Pr(A|B) = 0.64 \tag{13.6.3.6}$$

[1] Read question numbers as (CHAPTER NUMBER).(EXERCISE NUMBER).(QUESTION NUMBER)

13.7.3 $\Pr(A+B)$

$$\Pr(A+B) = \Pr(A) + \Pr(B) - \Pr(AB) \tag{13.7.3.1}$$

Substitute (13.5.3.5) in (13.7.3.1)

$$= 0.8 + 0.5 - 0.32 \tag{13.7.3.2}$$
$$= 1.3 - 0.32 \tag{13.7.3.3}$$
$$= 0.98 \tag{13.7.3.4}$$
$$\Pr(A+B) = 0.98 \tag{13.7.3.5}$$