

KNN \rightarrow K-Nearest Neighbour

Naive Bayes \rightarrow Probability.

$$\text{Coin} = \underline{\text{Head}} \rightarrow \frac{1}{2}$$

$$\text{Card} = \underline{\text{King.}} \rightarrow \frac{4}{52} \rightarrow \frac{1}{13}$$

① Diamond	9
② Heart	10
③ Spade	11
④ Club	12
	13

$\{2-10\} A, J, K, Q.$

$$\frac{4}{52} = \frac{1}{13}$$

① independent \rightarrow Each event is not affected by other event

② Dependent \rightarrow In dependent event one event is affected by another event.

③ Mutually exclusive \rightarrow

① turning L OR R.

② Head OR tails.

③ King and queen are mutually exclusive

You can't do both at the same time.

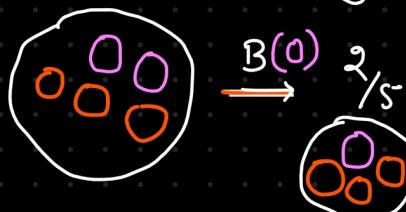


① Coin \Rightarrow H or T

$$\approx 1 \quad \frac{1}{2} = 0.5 = 50\%$$

$$\approx 2 \quad H \text{ or } T = 0.5$$

② Dependent event ex.



First event

①

Second event

②

$$B(0) \xrightarrow{2/5} \frac{1}{4}$$

52

$$\text{event 1: } \frac{4}{52}$$

$$\text{event 2: } \frac{3}{51}$$

Dependent event.



Diffr b/w exclusive and independent event.

ME \Rightarrow Two events can not occur at the same time [T]

IDE \Rightarrow One event remains unaffected by the occurrence of the other event.

$$[T-1] \rightarrow [T]$$

Independent Coin.

Q. find out the probability of getting Blue ball.



$$\begin{aligned} & \xrightarrow{\text{event (A)}} \frac{2}{5} \quad \xrightarrow{\text{event (B)}} \frac{1}{4} \quad \Rightarrow \frac{2}{5} \times \frac{1}{4} = \frac{2}{20} = \frac{1}{10} = 0.1 \\ & P(A) \qquad \qquad \qquad P(B|A) \end{aligned}$$

[B is happening and A is already happened]

"event - B given event A."

$$\Leftrightarrow P(A \text{ and } B) = P(A) \times P(B|A) \quad - \textcircled{1}$$

$$P(B|A) = \frac{P(A \text{ and } B)}{P(A)}$$

$$P(B \text{ and } A) = P(B) \times P(A|B) \quad - \textcircled{2}$$

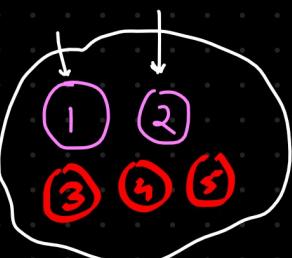
$$P(A \text{ and } B) = P(B \text{ and } A)$$

$$P(A) \times P(B|A) = P(B) \times P(A|B)$$

| Bayes theorem.

$$P(B|A) = \frac{P(B) \times P(A|B)}{P(A)}$$

→ Naive Bayes formula.



$$\begin{aligned} & P(\text{A and B}) \\ & P(\text{Blue}) \rightarrow \frac{2}{5} \quad P(A) \quad P(B|A) \\ & - P(\underline{\text{B and A}}) = \frac{2}{5} \times \frac{1}{2} \end{aligned}$$

⇒ toss the coin 3 times in a consecutive manner and find out the Prob. of getting head.

$$\frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{8}$$

$$P(B|A) = \frac{P(B) \times P(A|B)}{P(A) P(x_i)}$$

Dependent feature.

Dataset \Rightarrow $x_1 \ x_2 \ x_3 \ x_4 \dots x_n$

$y \xrightarrow{\text{OIP}}$

I/P feature. independent

$$P(y/(x_1, x_2, x_3, \dots, x_n)) = \frac{P(y) \times P(x_1, x_2, x_3, \dots, x_n | y)}{P(x_1, x_2, x_3, x_4, x_5, \dots, x_n)}$$

Data $\rightarrow P(y/(x_1, x_2, \dots, x_n)) = \frac{P(y) \times P(x_1 | y) \times P(x_2 | y) \times P(x_3 | y) \times P(x_4 | y) \dots n}{P(x_1) \times P(x_2) \times P(x_3) \dots P(x_n)}$

(classifier model)
(Probability based)
Naive Bayes.

$$\overbrace{\bar{y} \quad \overline{(x_1 \dots x_n)} \quad \overline{(x_1 - x_n)} \quad \overline{P(y)} \quad P(x_1 - x_n)}$$

Scenario:

Binary class problem.

$x_1 \quad x_2 \quad x_3 \quad \text{O/P}$

yes

No

$$\underline{y \text{ Yes.}} \quad P(y|x_1 x_2 x_3) = \frac{P(\text{Yes}) \times P(x_1|\text{Yes}) \times P(x_2|\text{Yes}) \times P(x_3|\text{Yes})}{P(x_1) \times P(x_2) \times P(x_3)}$$

$$\underline{No} \quad P(\text{No}|x_1 x_2 x_3) = \frac{P(\text{No}) \times P(x_1|\text{No}) \times P(x_2|\text{No}) \times P(x_3|\text{No})}{P(x_1) \times P(x_2) \times P(x_3)}$$

$$\begin{array}{cccccc} 5 & 10 & 5 & 10 & 50 & \times \frac{1}{2} \\ \underline{\frac{50}{18}} & \underline{\frac{100}{18}} & & & \underline{\frac{1}{18}} & \end{array}$$

$$\underline{\text{Let's assume.}} \quad P(y|x_i) = 0.13 \\ P(N|x_i) = 0.05 \quad \left. \right\} \quad \frac{0.13}{0.13 + 0.05} = \frac{0.13}{0.18} = \underline{72.2\%}$$

$$\frac{0.05}{0.13 + 0.05} = \frac{0.05}{0.18} = \underline{27.8\%}$$

$$P(y|x_i) > P(N|x_i)$$

Yes

$$P(\text{Class}/\text{data}) = (P(\text{data}/\text{Class}) \times P(\text{class})) / P(\text{data})$$

$$P(y|(x_1, x_2, \dots, x_n)) = \frac{P(y) \times P(x_1|y) \times P(x_2|y) \times P(x_3|y) \times P(x_4|y) \dots n}{P(x_1) \times P(x_2) \times P(x_3) \dots P(x_n)}$$

Day	Outlook	Temperature	Humidity	Wind	Play Tennis
D1	Sunny	Hot	High	Weak	No
D2	Sunny	Hot	High	Strong	Yes
D3	Overcast	Hot	High	Weak	Yes
D4	Rain	Mild	High	Weak	Yes
D5	Rain	Cool	Normal	Weak	Yes
D6	Rain	Cool	Normal	Strong	No
D7	Overcast	Cool	Normal	Strong	Yes
D8	Sunny	Mild	High	Weak	No
D9	Sunny	Cool	Normal	Weak	Yes
D10	Rain	Mild	Normal	Weak	Yes
D11	Sunny	Mild	Normal	Strong	Yes
D12	Overcast	Mild	High	Strong	No
D13	Overcast	Hot	Normal	Weak	Yes
D14	Rain	Mild	High	Strong	No

Nine bayes classifier.

$$P(y) = \frac{9}{14} \quad P(n) = \frac{5}{14}$$

(1)

Outlook

	yes	No	$P(y)$	$P(n)$
Sunny	2	3	$\frac{2}{9}$	$\frac{3}{5}$
Overcast	4	0	$\frac{4}{9}$	$0/5$
Rain	3	2	$\frac{3}{9}$	$\frac{2}{5}$
	$\frac{9}{9}$	$\frac{5}{5}$		

Temperature

	Yes	No	$P(y)$	$P(n)$
Hot	2	2	$\frac{2}{9}$	$\frac{2}{5}$
Mild	4	2	$\frac{4}{9}$	$\frac{2}{5}$
Cool	3	1	$\frac{3}{9}$	$\frac{1}{5}$
	$\frac{9}{9}$	$\frac{5}{5}$		

Ques. If $[Sunny, Hot] \rightarrow (O|P) \cap N$

$$P(\text{yes} | [Sunny, Hot]) = \frac{P(\text{yes}) * P(\text{Sunny} | \text{yes}) + P(\text{No} | \text{yes})}{P(\text{Sunny}) * P(\text{hot})}$$

$$P(\text{No} | [Sunny, Hot]) = \frac{P(\text{No}) * P(\text{Sunny} | \text{No}) * P(\text{Hot} | \text{No})}{P(\text{Sunny}) * P(\text{hot})}$$

$$P(\text{yes} | [Sunny, Hot]) = \frac{P(\text{yes}) * P(\text{Sunny} | \text{yes}) + P(\text{No} | \text{yes})}{P(\text{Sunny}) * P(\text{hot})} = \frac{\frac{9}{14} * \frac{2}{9} * \frac{2}{5}}{\frac{9}{14} * \frac{2}{5}} = \frac{2}{63} = 0.031$$

$$P(\text{No} | [Sunny, Hot]) = \frac{P(\text{No}) * P(\text{Sunny} | \text{No}) * P(\text{Hot} | \text{No})}{P(\text{Sunny}) * P(\text{hot})} = \frac{\frac{5}{14} * \frac{3}{5} * \frac{2}{5}}{\frac{9}{14} * \frac{2}{5}} = \frac{-3}{35} = 0.085$$

$$P(\text{yes} | [Sunny, Hot]) = \frac{0.031}{0.031 + 0.085} = \frac{0.031}{0.116} = 0.27 = 27\%$$

$$P(\text{No} \mid (\text{sunny, not})) = \frac{0.085}{0.031 + 0.085} = \frac{0.085}{0.116} = 0.732 \\ = 73\%$$

Task : 1. Expand humidity and wind like i did with outlook and temperature then you have to solve the particular condition.

[Sunny, Hot, High, Strong] \rightarrow OIP

$$P(\text{yes} \mid (\text{sunny, hot, high, strong})) = ?$$

$$P(\text{No} \mid (\text{sunny, hot, high, strong})) = ?$$

task no. 2 \Rightarrow

<https://medium.com/analytics-vidhya/use-naive-bayes-algorithm-for-categorical-and-numerical-data-classification-935d90ab273f>