

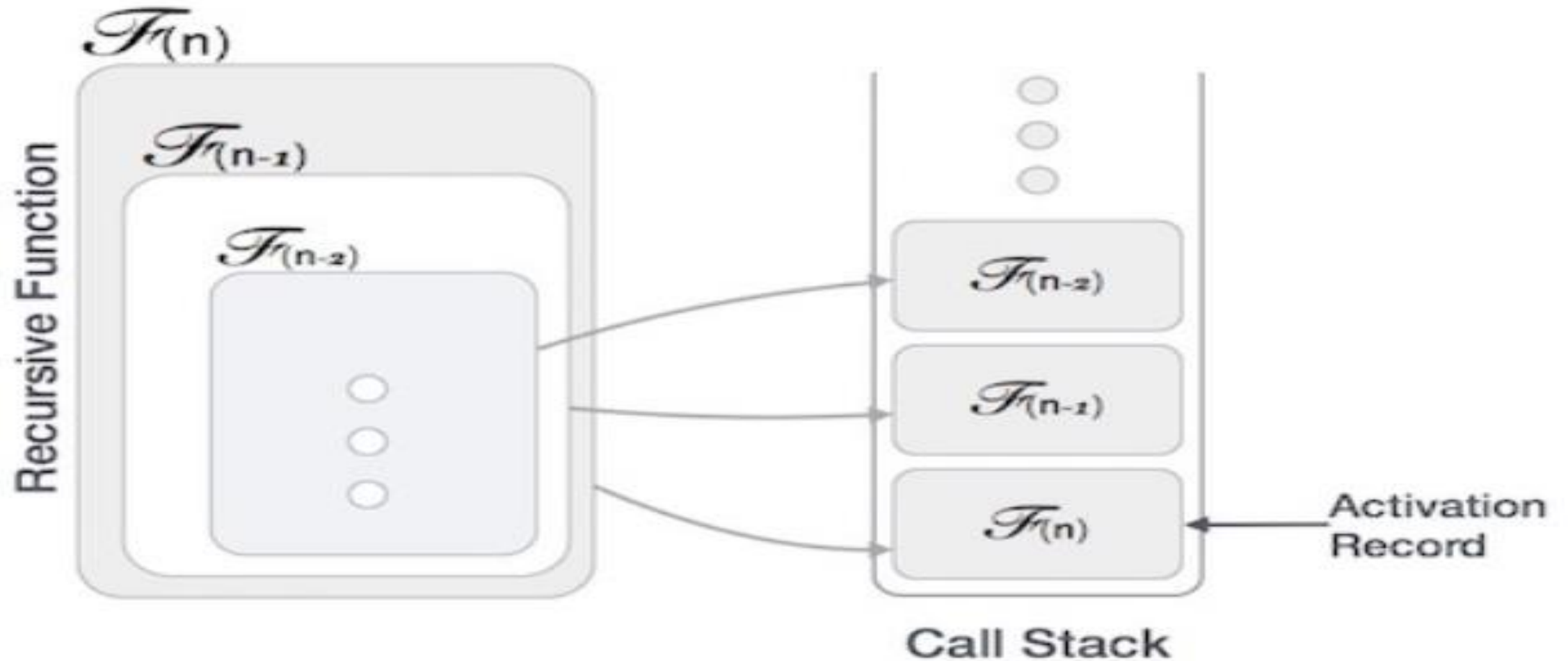
The background of the slide features a complex, abstract network of glowing blue and purple lines and nodes, resembling a data structure or a neural network, set against a dark, textured background.

Data Structure

Sep23 : Day 2

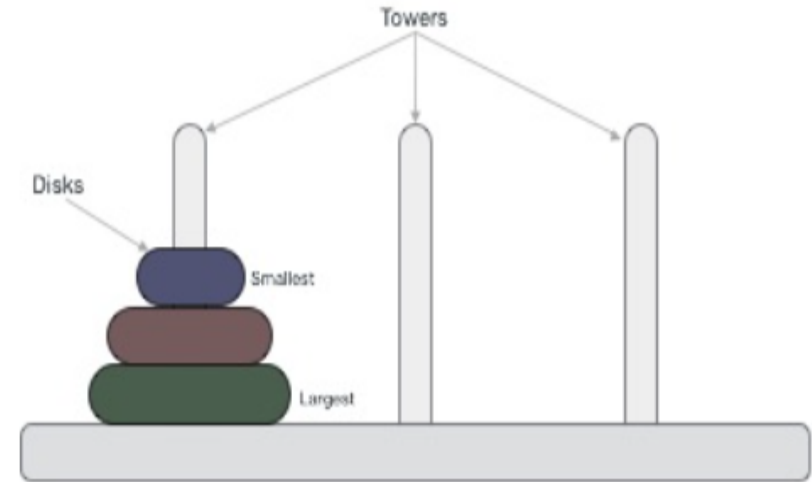
Kiran Waghmare
CDAC Mumbai

How Data Structure Recursive function is implemented?



What is Tower of Hanoi?

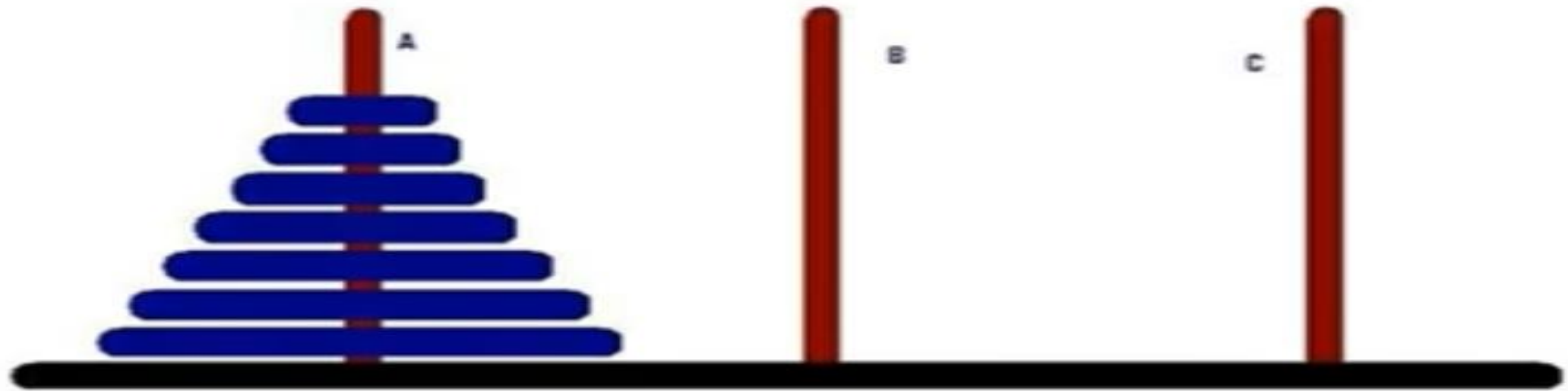
- A mathematical puzzle consisting of three towers and more than one ring is known as Tower of Hanoi.
- Tower of Hanoi
- The rings are of different sizes and are stacked in ascending order, i.e., the smaller one sits over the larger one. In some of the puzzles, the number of rings may increase, but the count of the tower remains the same.



Tower of Hanoi

Tower oh Hanoi

- The tower of Hanoi is mathematical puzzle.



- The objective of the puzzle is to move the entire stack to another rod.

What are the rules to be followed by Tower of Hanoi?

- **The Tower of Hanoi puzzle is solved by moving all the disks to another tower by not violating the sequence of the arrangements.**

The rules to be followed by the Tower of Hanoi are -

1. Only one disk can be moved among the towers at any given time.
2. Only the "top" disk can be removed.
3. No large disk can sit over a small disk.

Algorithm 1: Recursive algorithm for solving Towers of Hanoi

```
1 function recursiveHanoi( $n$ ,  $s$ ,  $a$ ,  $d$ )
2   if  $n == 1$  then
3      $\text{print}(s + \text{ " to " } + d);$ 
4     return;
5   end
6   recursiveHanoi( $n - 1$ ,  $s$ ,  $d$ ,  $a$ );
7    $\text{print}(s + \text{ " to " } + d);$ 
8   recursiveHanoi( $n - 1$ ,  $a$ ,  $s$ ,  $d$ );
9 end
```

```
class Recursion8{
```

```
static void toh(int n,char s,char inter, char d){
    if(n==1)
        System.out.println("Disk from " +s+ "to" +d);
    else
    {
        toh(n-1, s, d, inter);
        System.out.println("Disk from " +s+ "to" +d);
        toh(n-1, inter,s, d);
    }
}
```

```
public static void main(String args[]){
```

```
    int n=3;
    toh(n,'A','B','C');
}
```

```
Disk fromCtoA
Disk fromBtoC
Disk fromAtoB
Disk fromAtoC
Disk fromBtoC
```

```
D:\Test>javac Recursion8.java
```

```
D:\Test>java Recursion8
Disk fromAtoC
```

```
D:\Test>javac Recursion8.java
```

```
D:\Test>java Recursion8
Disk from AtoB
Disk from AtoC
Disk from BtoC
```

```
D:\Test>javac Recursion8.java
```

```
D:\Test>java Recursion8
Disk from AtoC
Disk from AtoB
Disk from CtoB
Disk from AtoC
Disk from BtoA
Disk from BtoC
Disk from AtoC
```

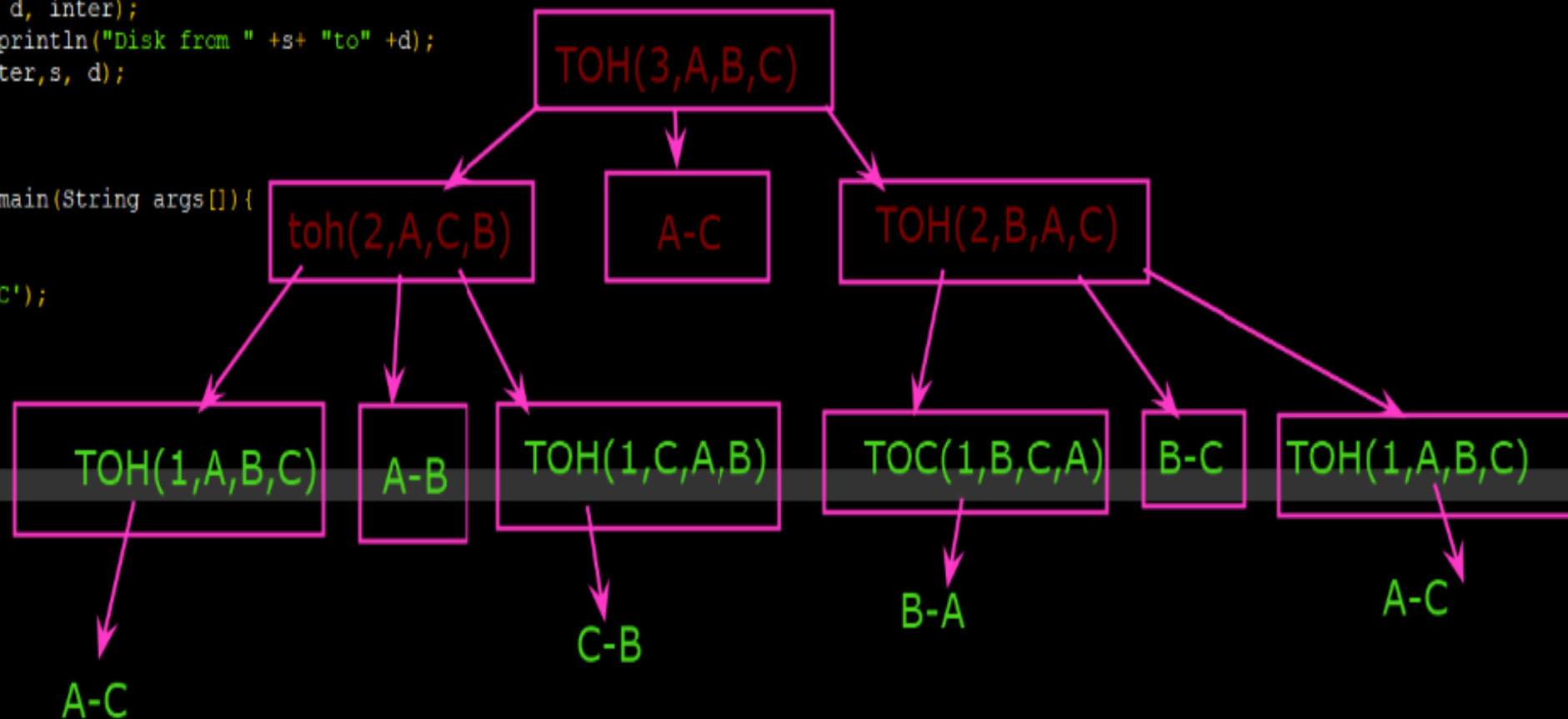
```
D:\Test>
```

```
static void toh(int n,char s,char inter, char d){  
    if(n==1)  
        System.out.println("Disk from " +s+ "to" +d);  
    else  
    {  
        toh(n-1, s, d, inter);  
        System.out.println("Disk from " +s+ "to" +d);  
        toh(n-1, inter,s, d);  
    }  
}
```

```
public static void main(String args[]){
```

```
    int n=3;  
    toh(n, 'A', 'B', 'C');
```

```
}
```




```
class Recursion8{
```

You are screen sharing

Stop Share

050_Jaywant Manurkar_Kh raised hand

View

X

C:\Windows\system32\cmd.e

+

▼

```
D:\Test>javac Recursion8.java
```

```
D:\Test>java Recursion8
```

```
Disk from AtoB
```

```
Disk from AtoC
```

```
Disk from BtoC
```

```
D:\Test>javac Recursion8.java
```

```
D:\Test>java Recursion8
```

```
Disk from AtoC
```

```
Disk from AtoB
```

```
Disk from CtoB
```

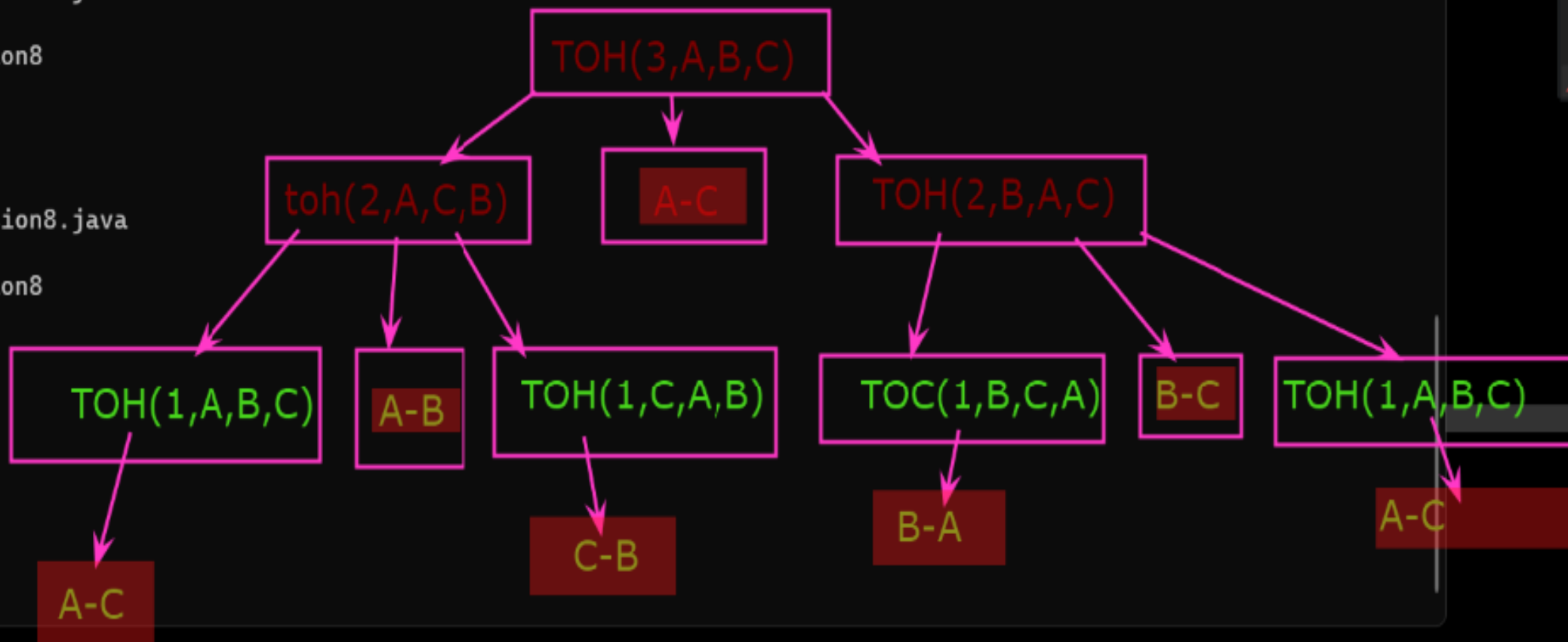
```
Disk from AtoC
```

```
Disk from BtoA
```

```
Disk from BtoC
```

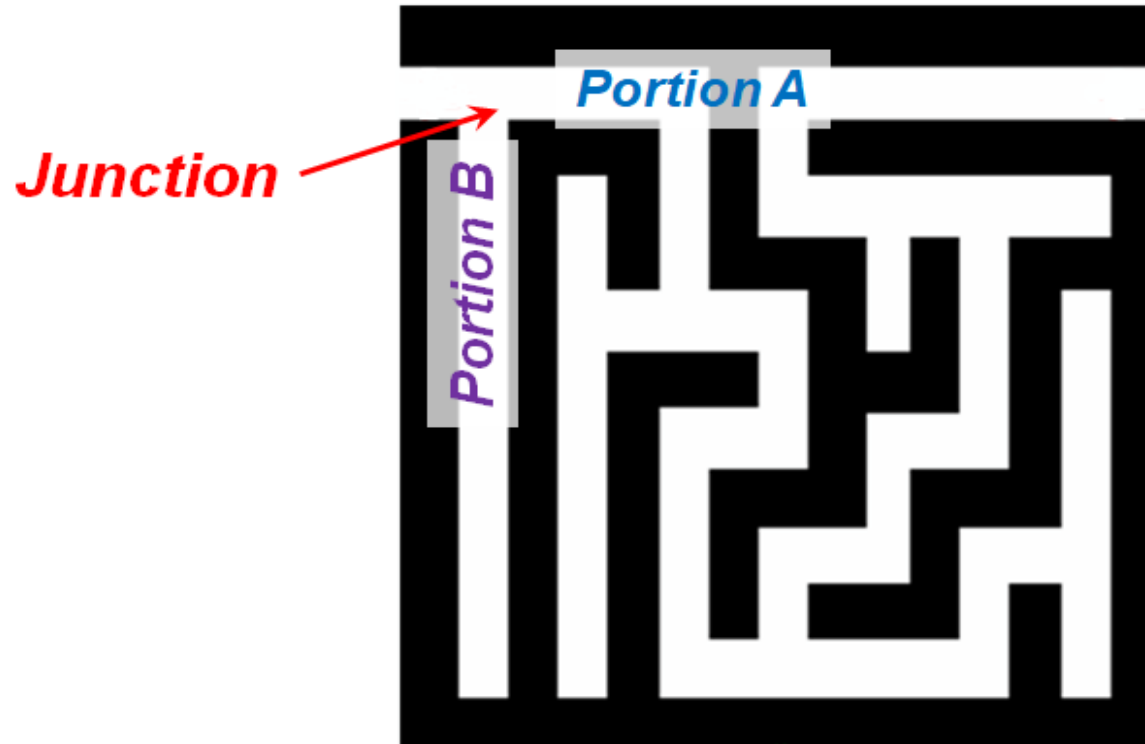
```
Disk from AtoC
```

```
D:\Test>
```



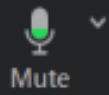
Backtracking: Idea

- Backtracking is a technique used to solve problems with a large search space, by systematically trying and eliminating possibilities.
- A standard example of backtracking would be going through a maze.
 - At some point, you might have two options of which direction to go:



Topic: Backtracking

EVERYDAY IS A NEW BEGINNING. TAKE A DEEP



Mute



Stop Video



Security



Participants

232



Chat



New Share



Pause Share



Start Summary



AI Companion



Annotate



Remote Control



You are screen sharing



Stop Share



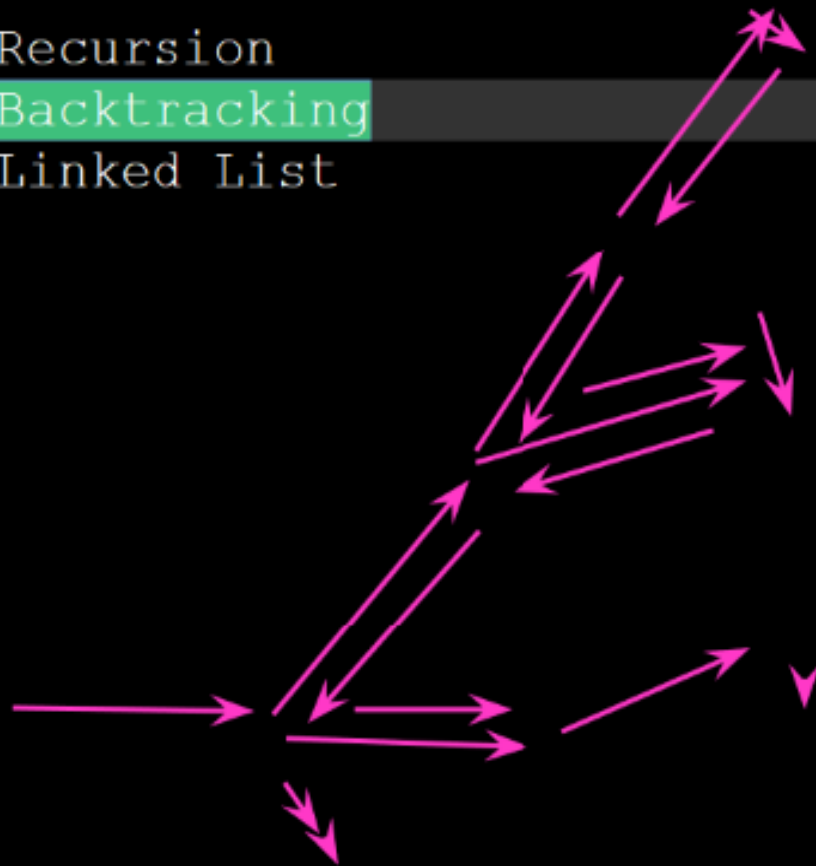
AI AGAIN.

Toh:

Ref: <https://www.mathsisfun.com/games/towerofhanoi.html>

Agenda:

- Recursion
- Backtracking
- Linked List



Permutations

AB
BA

Arrangement

Sequence is important

ABC
ACB
BAC
BCA
CAB
CBA

Combinations

AB/BA

Not consider the sequence

ABC
BAC
CAB



You are screen sharing

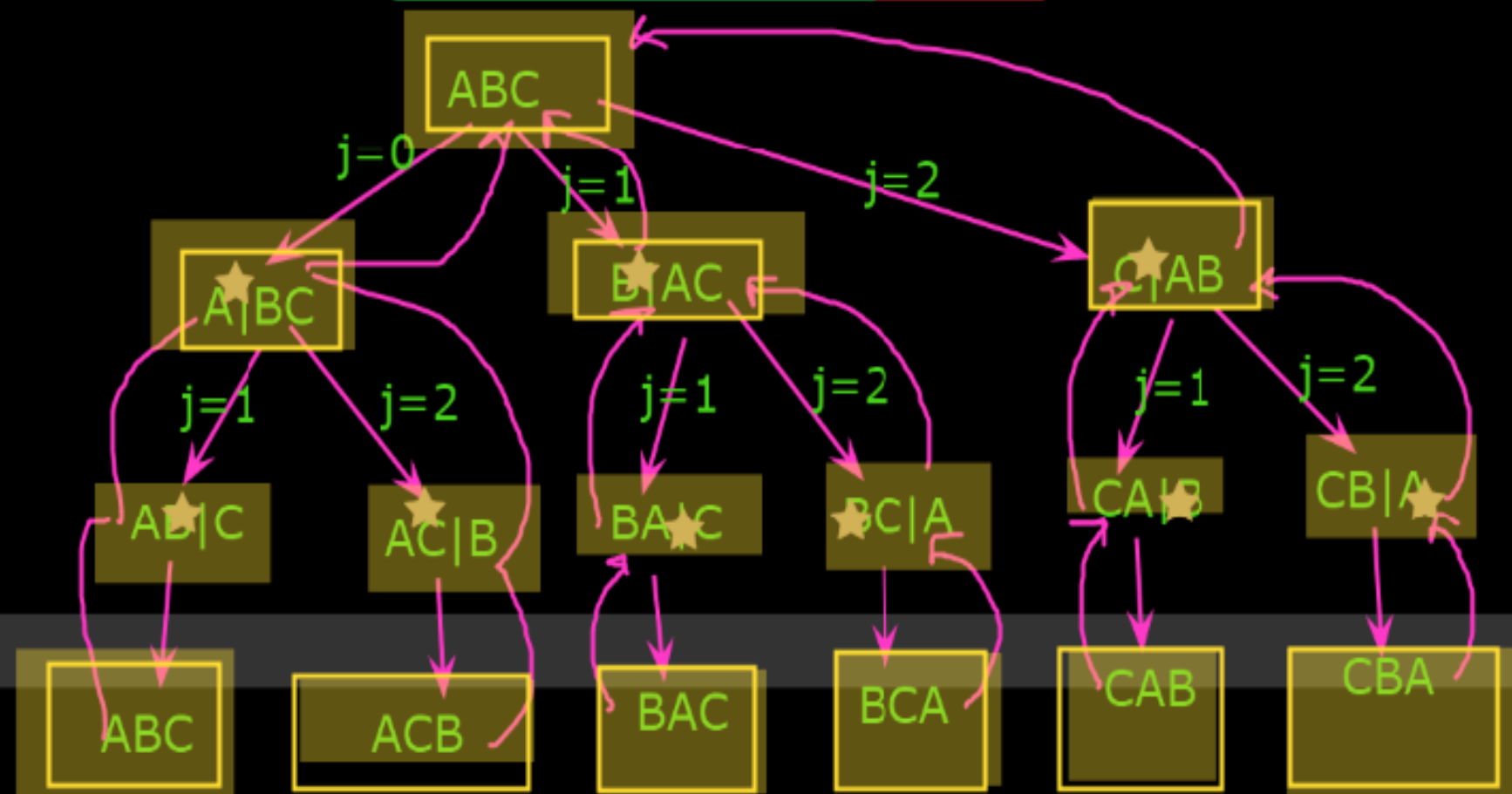


Stop Share

ABC }
ACB }

BAC }
BCA }

CAB }
CBA }



```
class Recursion9{
```

```
static void display(String str,String res)
```

```
{
```

```
    if(str.length() == 0){
```

```
        System.out.println(res+ "");
```

```
        return;
```

```
    }
```

```
    for(int i=0;i<str.length();i++){
```

```
        char ch = str.charAt(i);
```

```
        String ros=str.substring(0,i)+ str.substring(i+1);
```

```
        display(ros, res+ch);
```

```
    }
```

```
}
```

ABC

A|BC

AB|C

ABC|

```
public static void main(String args[]){
```

```
    String s="ABCD";
```

```
    display(s, "");
```

```
}
```

```
}
```

Problem 1

Recursive program to find the Sum of the series $1 - 1/2 + 1/3 - 1/4 \dots 1/N$

Given a positive integer N, the task is to find the sum of the series $1 - (1/2) + (1/3) - (1/4) + \dots (1/N)$ using recursion.

Examples:

Input: N = 3

Output: 0.8333333333333333

Explanation:

$$1 - (1/2) + (1/3) = 0.8333333333333333$$

Input: N = 4

Output: 0.5833333333333333

Explanation:

$$1 - (1/2) + (1/3) - (1/4) = 0.5833333333333333$$

Problem 2

Recursive Program to print multiplication table of a number

Given a number N, the task is to print its multiplication table using recursion.

Examples

Input: N = 5

Output:

5 * 1 = 5

5 * 2 = 10

5 * 3 = 15

5 * 4 = 20

5 * 5 = 25

5 * 6 = 30

5 * 7 = 35

5 * 8 = 40

5 * 9 = 45

5 * 10 = 50

Input: N = 8

Output:

8 * 1 = 8

8 * 2 = 16

8 * 3 = 24

8 * 4 = 32

8 * 5 = 40

8 * 6 = 48

8 * 7 = 56

8 * 8 = 64

8 * 9 = 72

8 * 10 = 80

Problem 3

Recursive program to print formula for GCD of n integers

Given a function gcd(a, b) to find GCD (Greatest Common Divisor) of two number. It is also known that GCD of three elements can be found by gcd(a, gcd(b, c)), similarly for four element it can find the GCD by gcd(a, gcd(b, gcd(c, d))). Given a positive integer n. The task is to print the formula to find the GCD of n integer using given gcd() function.

Examples:

Input : n = 3

Output : gcd(int, gcd(int, int))

Input : n = 5

Output : gcd(int, gcd(int, gcd(int, gcd(int, int))))

Problem 4

Java Program to Reverse a Sentence Using Recursion

A sentence is a sequence of characters separated by some delimiter. This sequence of characters starts at the 0th index and the last index is at $\text{len}(\text{string})-1$. By reversing the string, we interchange the characters starting at 0th index and place them from the end. The first character becomes the last, the second becomes the second last, and so on.

Example:

Input : CDAC Mumbai.

Output: .iabmuM CADC

Input : Alice in wonderland.

Output: .dnalrednow ni ecilA

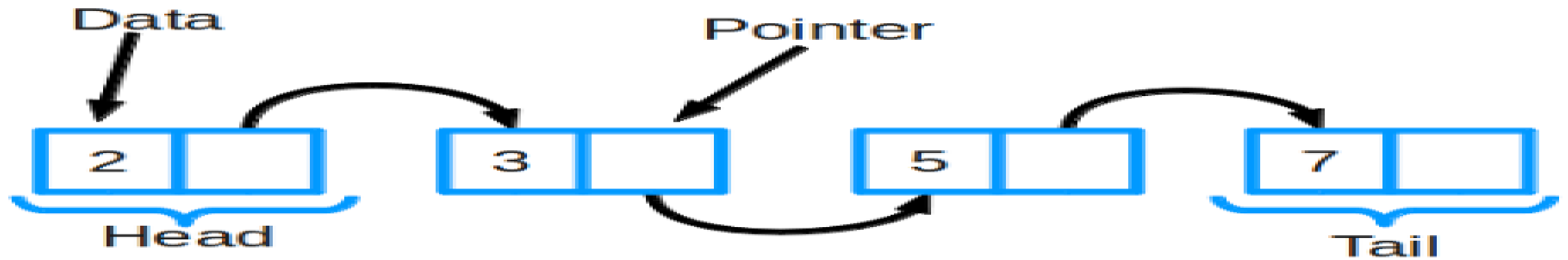
Approach:

Check if the string is empty or not, return null if String is empty.

If the string is empty then return the null string.

Else return the concatenation of sub-string part of the string from index 1 to string length with the first character of a string. e.g. return `substring(1)+str.charAt(0)`; which is for string "Mayur" return will be "ayur" + "M".

Linked list



Linked List:

| | | | | | | |
|----|----|----|----|---|---|----|
| 10 | 20 | 30 | 40 | 0 | 0 | 50 |
|----|----|----|----|---|---|----|

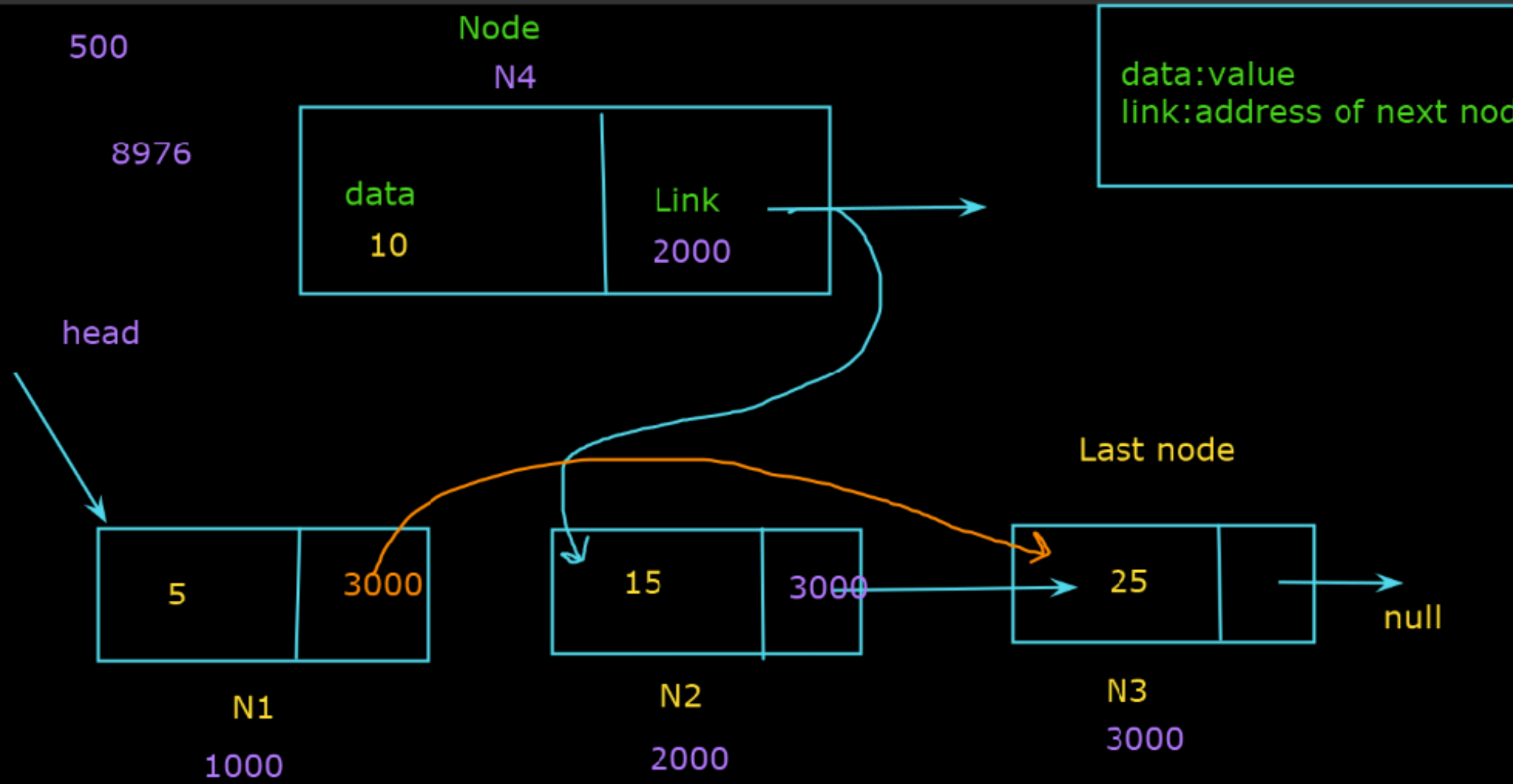
index=> 0 1 2 ~~3~~

homogeneous
continuous
sequential

static => size=100000
fixed



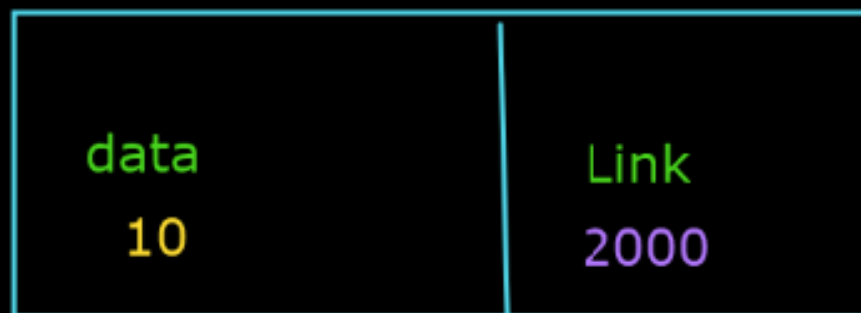
flexibility: no size binding



500

Node 7000

N4



N5



2300

head



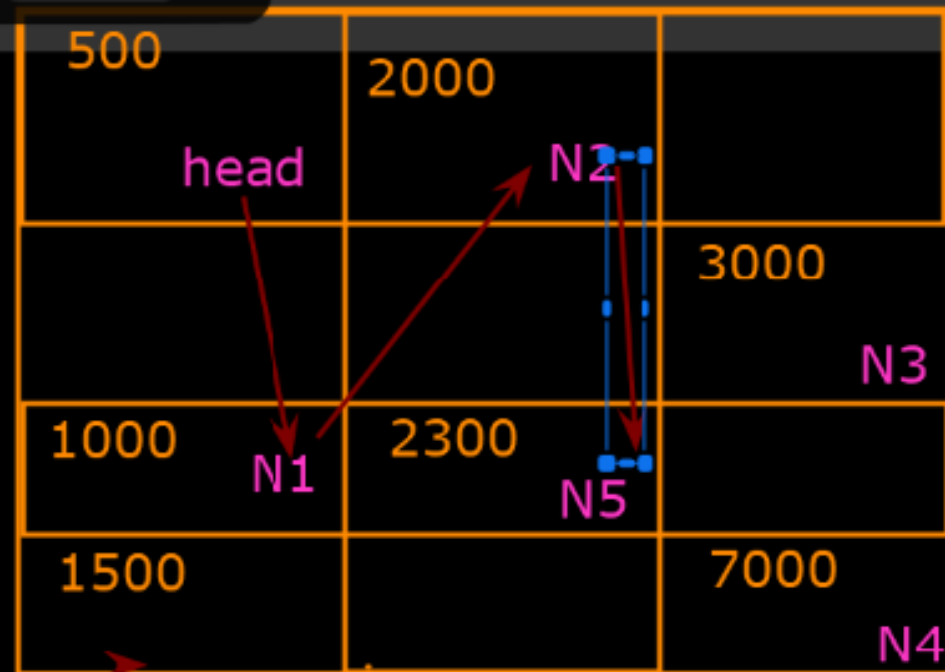
N1

1000



N2

2000



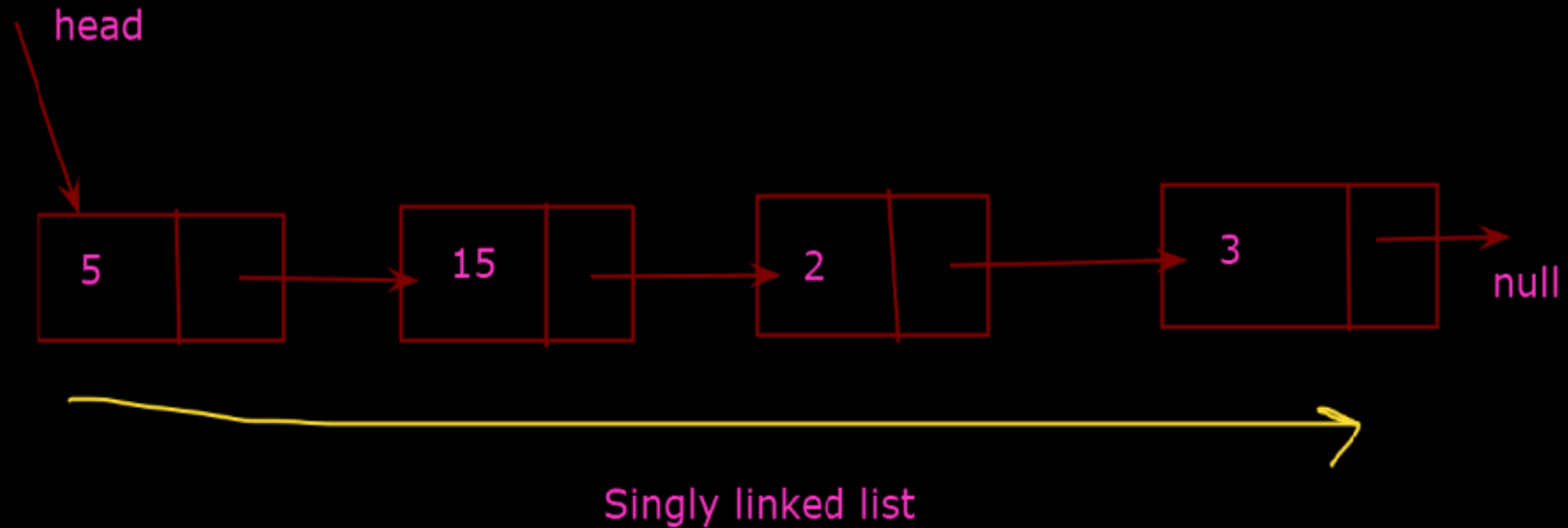
Last node



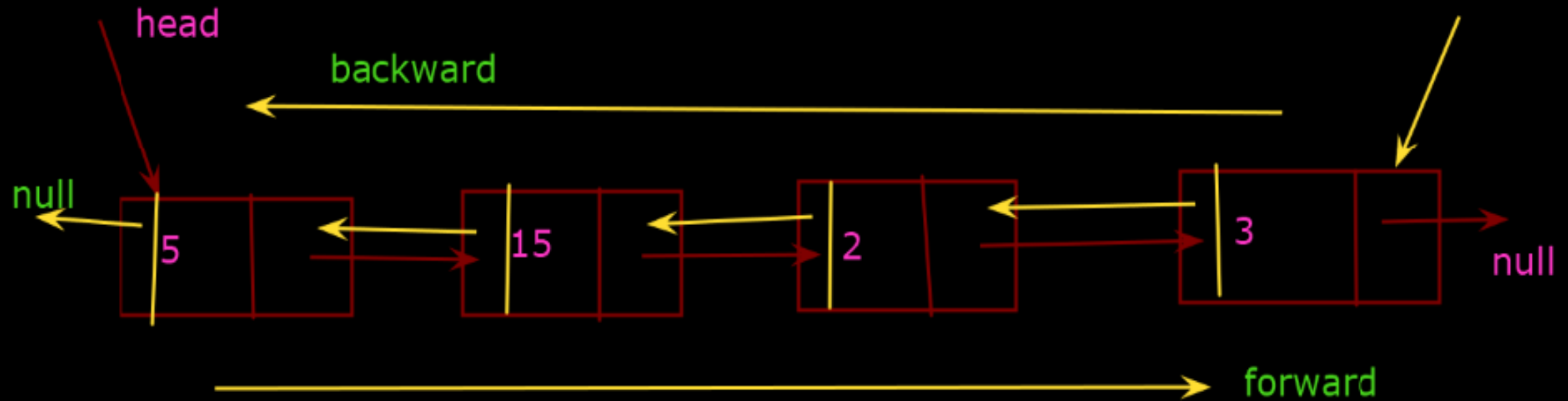
N3

3000

1. singly linked list
2. Doubly linked list
3. Circular linked list
4. Doubly circular linked list.



1. singly linked list
2. Doubly linked list
3. Circular linked list
4. Doubly circular linked list.

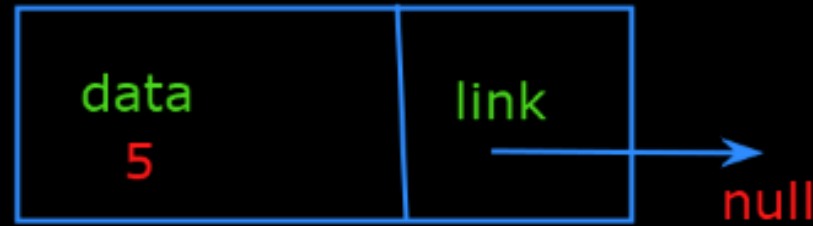


singly linked list:

```
class Node{
```

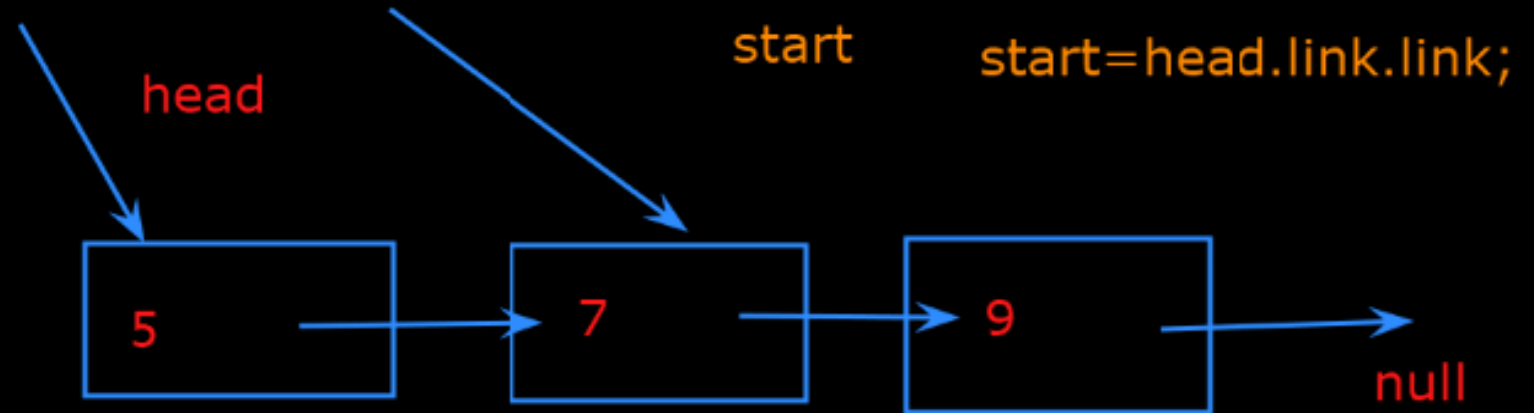
```
    int data;  
    Node link;
```

```
    Node(int d)  
    {  
        data=d;  
        link=null;  
    }  
}
```



head=start

start=head



1200

2300

6500

start=head.link;

head=null;

head.link.data

head.link.link

head.data

head.link

start.data

start.link