

- Algorithm
- Step 1: Allocate a 8×8 chessboard to initialize state.
- (b) Set up an open set to explore different configurations.
- (c) Set up a visited state to display all different configurations.

Step 2: Calculate the number of attacking pairs that the queens should not be in the same row, same column or same diagonal.

if $state[i] == state[j] \text{ or } abs(state[i] - state[j]) == j - i$ // diagonal

row = i
column = j
Attacks = 1

then we increment the variable attacks to determine attacking pair.

open set = {}

Step 3: Assign initial state to open set for the first iteration. If the node is not visited then first put it to the open set, the open set will push the node to heap (priority queue).

heap = push(open set, Node(new state, g, h))

Step 4: We calculate total estimated cost, $f = g + h$ where g is the cost to reach the current state and h is the number of attacks to reach goal state.

Step 5: In the main loop remove the node with the lowest cost.

Step 6: We have to determine the next row to place the queen.

Step 7: This happens in the main loop after doing this we generate new state.

update g and calculate h .

Hill climbing algorithm

- step 1: Place 8 queens randomly
- step 2: Find the attacking pairs such that no queens are placed in the same row, same column or same diagonal
- step 3: Place 8 queens randomly on the chessboard
state = Random.random(0,7) for in range(8)
current_attack = calculate_attack(state)
- step 4: In the previous state, calculate attacks
choose one with few attacking pairs
- step 5: if next_attack \geq current_attack
break
- delete the current state
state = next_state
current_attack = new_attack
- step 6: display board

| | | | |
|---|---|---|--|
| Q | Q | | |
| | | Q | |
| | | | |
| | | | |

$$g = q + h$$

Proceed →

A star algorithm

import heapq

class Node:

def __init__(self, state, g, h):

self.state = state

self.g = g

self.h = h

self.f = g + h

def __lt__(self, other):

return self.f < other.f

def heuristic(state):

attacks = 0

for i in range(len(state)):

for j in range(i+1, len(state)):

if state[i] == state[j] or abs(state[i] - state[j])

== j - i:

attacks += 1

return attacks

def a_star_8queens():

initial_state = tuple(range(1, 8))

open_set = []

heapq.heappush(open_set, Node(initial_state, 0,

heuristic(initial_state)))

visited = set()

while open_set:

current_node = heapq.heappop(open_set)

current_state = current_node.state

if current_node.h == 0 and -1 not in current_state:

return current_state

if current_state in visited:

continue

visited.add(current_state)

next_row = current_state.index(-1) + 1

current_state = list(current_state)

if next_row < 8:

for col in range(8):

new_state = list(current_state)

new_state[next_row] = col

new_state = tuple(new_state)

if new_state not in visited:

g = current_node.g + 1

h = heuristic(new_state)

heapq.heappush(open_set, Node(new_state, g, h))

return None

def display(state):

for row in range(8):

line = ""

for col in range(8):

if state[row] == col:

line += "Q"

else:

line += "."

print(line)

print()

solution = a_star_8_queens()

if solution:

print("A solution:")

display(solution)

else:

print("No solution found")

Answer

A solution

Q

. Q

. . . Q

Q

. Q

. Q

. Q

. Q

Hill climbing algorithm

import random

def calculate_attacks(state):

attacks = 0

for i in range(len(state)):

for j in range(i+1, len(state)):

if state[i] == state[j] or abs(state[i] - state[j]) == 1:

attacks += 1

return attacks

def hill():

state = random.randint(0, 7) for _ in range(8)

ca = calculate_attacks(state)

for _ in range(100):

n = []

for r in range(8):

for c in range(8):

if state[row] != col:

next_state = []

n[r] = c

n.append(n)

next_state = min(n, key = calculate_attacks)

next_attacks = calculate_attacks(next_state)

if next_attacks <= current_attacks:

break

state = next_state

current_attacks = next_attacks

return state, current_attacks

def display(state):

for r in range(8):

line = ""

for c in range(8):

if state[r] == c:

line += "Q"

line += "

leerit = " "

print (line)

print ()

best_solution : None

best_attacks = float('inf')

attempts = 100

for _ in range (attempts):

s, a = hill ():

if attacks < best_attacks:

best_solution = solution

best_attacks = attacks

if best_attacks == 0:

break

if best_solution:

print ({best_attacks})

display (best_solution)

else:

print ("No solution found")

Output :

Best solution found

• • • • Q • • •
• • • • • Q •
• Q • • • • •
• • • • • Q •
• • Q • • • •
Q • • • • •
• • • Q • • •
• • • • • Q

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A star algorithm output

```
A* Solution:
. . . . . Q
. Q . . . .
. . . Q . .
Q . . . . .
. . . . . Q
. . . . Q .
. . Q . . .
. . . . . Q
```

Hill climbing algorithm output

```
Best solution found (with 0 attacking pairs):
. . . . . Q .
. . Q . . . .
. . . . . Q .
. Q . . . . .
. . . Q . . .
. . . . . Q
Q . . . . .
. . . . Q . .
```