



# Lecture 12

Reproductive value, sensitivity, and elasticity

WILD3810 (Spring 2020)

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# Readings

Mills 103-109

# Management questions

What is the short-term growth of this population given the current age/stage structure?

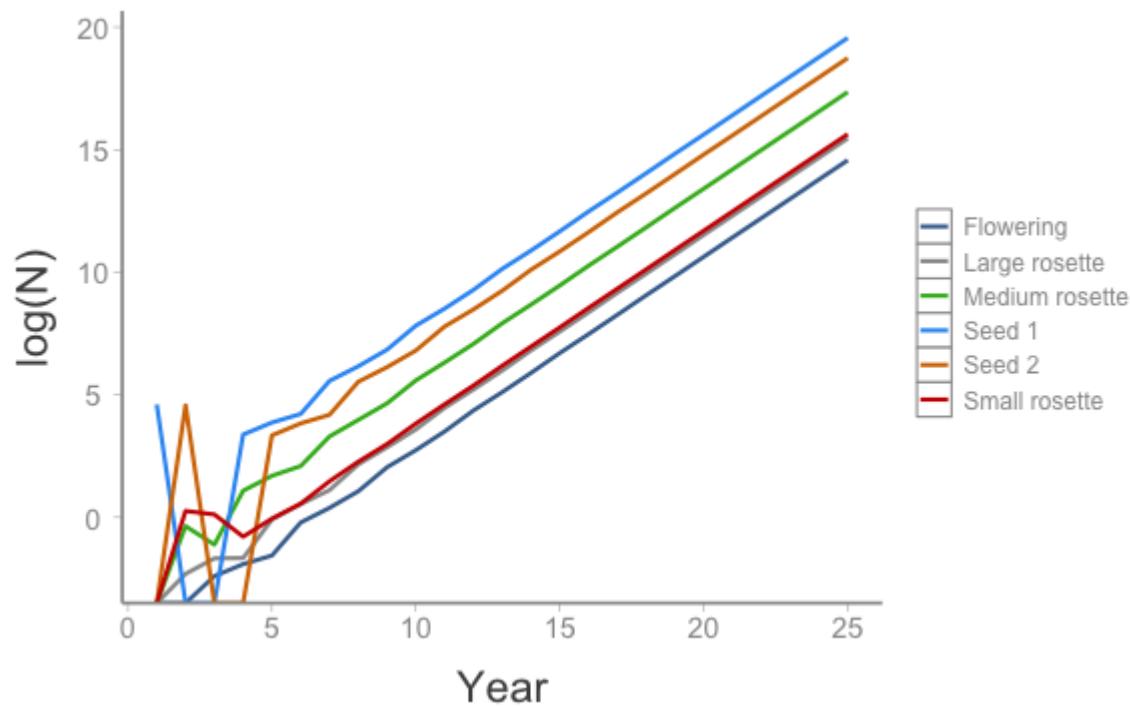
What is the long-term growth of this population given the current vital rates?

Which age/stage contributes most to future population growth?

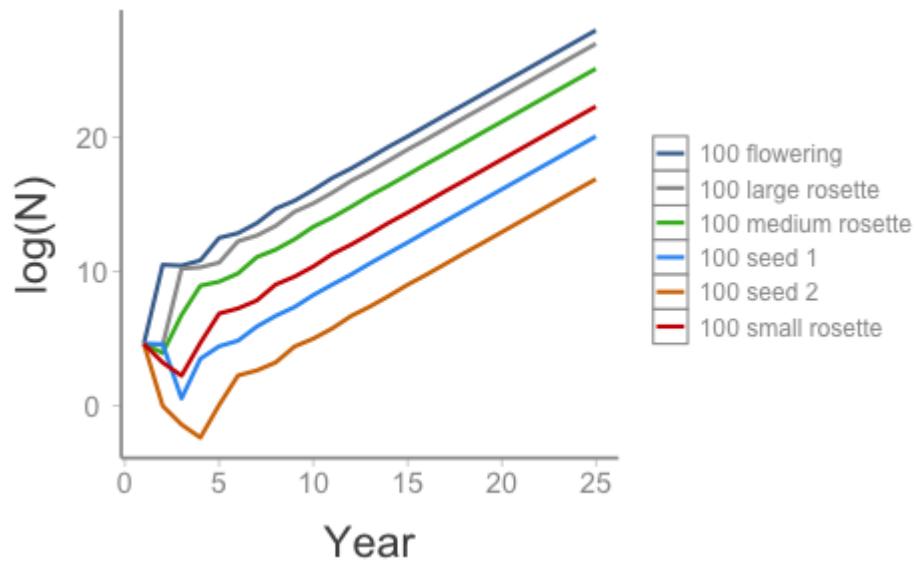
Which vital rates have the biggest effect on future growth?

How would future population dynamics change if different vital rates were changed?

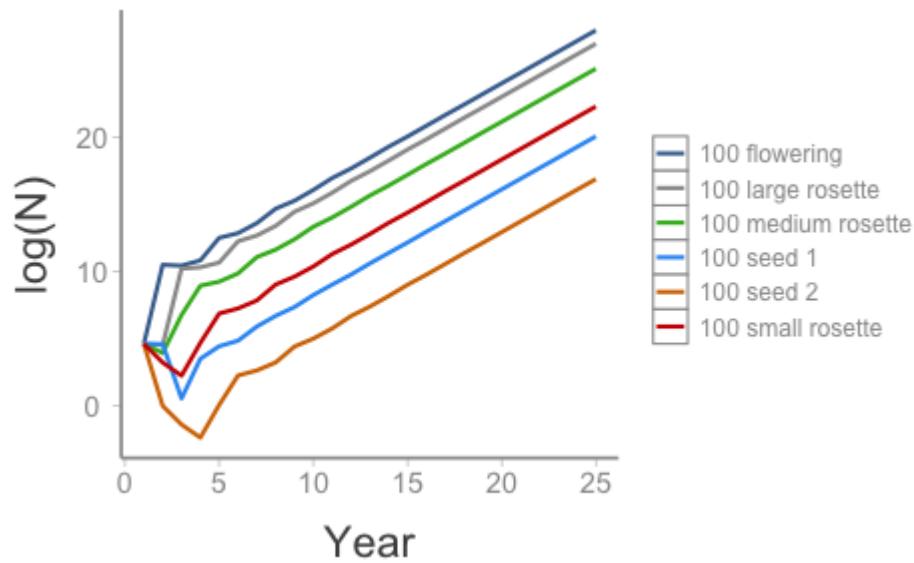
# Common teasel example



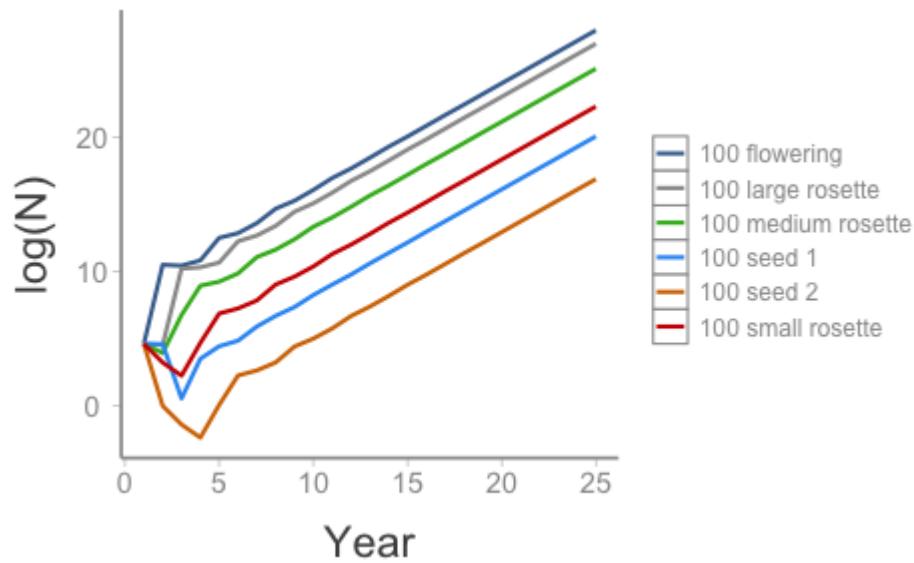
# How does initial stage-distribution effect growth?



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# Reproductive value

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Factors that influence reproductive value:

- Expected future reproductive output
- Survival probability
- Age at maturity
- Population growth rate
  - if a population is growing, future offspring will be smaller contribution to

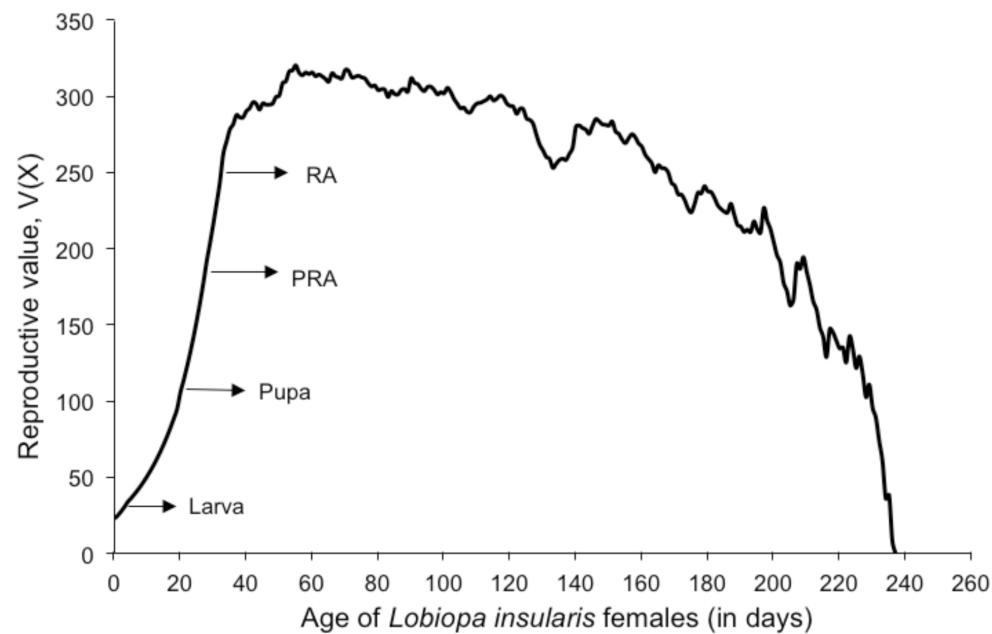
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# Reproductive value

## Teasel example

- Dormant seeds, year 1:
- Dormant seeds, year 2:
- Small rosette:
- Medium rosette:
- Large rosette:
- Flowering plant:

# Reproductive value



# Reproductive value



# Population inertia

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# Population inertia

difference between the long-term population size of a population that experiences transient dynamics and the long-term population size of a population that grows at the SSD

# Population inertia

Grey wolf population matrix

# Population inertia

Grey wolf population matrix

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# Population inertia

Grey wolf population matrix

Reproductive values:

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# Population inertia

What is the projected growth if reintroduced population starts at SAD?

SAD:

# Population inertia

What is the projected growth if reintroduced population starts with all 9 year olds?

# Population inertia

What is the projected growth if reintroduced population starts with all 3 year olds?

# Population inertia and reproductive value in practice

What age/stage distribution will lead to largest  $\lambda$  for introduced population?

What age/stage should be the target for reducing invasive species?

What age/stage distribution can be harvested to maintain stable population of game species?

# Sensitivity and elasticity

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# Sensitivity

Remember that  $\lambda$  is determined by the birth and death rates of a population

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Remember that  $\lambda$  is determined by the birth and death rates of a population

As managers, we might want to increase or decrease  $\lambda$  of certain species by manipulating age-specific birth and death rates

But  $\lambda$  does not respond equally to all vital rates

- in some cases, a small change in adult survival may result in a large change in  $\lambda$
- in other cases, a small change in fecundity or juvenile survival may result in a large change in  $\lambda$

# Sensitivity

## Sensitivity

the change in  $\lambda$  caused by a small change in a vital rate

where  $R_0$  and  $\pi^*$  are the reproductive value and stable stage distribution of stage

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where  $R_0$  and  $\pi^*$  are the reproductive value and stable stage distribution of stage  $j$

- large reproductive values or large stable stage distribution lead to large sensitivity

# Sensitivity



Common frog (*Rana temporaria*)

3 stages:

- pre-juvenile (egg - tadpole)
- juvenile (tadpole - 2 years)
- adult (> 2 years)

# Estimating sensitivity

By hand

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# Estimating sensitivity

By hand

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# Estimating sensitivity

By hand

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Analytically

`popbio::sensitivity(A)[2,1] = 26.05`

# Estimating sensitivity

By hand

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# Estimating sensitivity

By hand

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# Estimating sensitivity

By hand

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Analytically

`popbio::sensitivity(A)[1,2] = 0.006`

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# Elasticity

Does it make sense to compare a change of 0.01 in a survival value to a change of 0.01 in fecundity?

- 0.01 is about 52% of 0.019
- 0.01 is about 0.02% of 52

# Elasticity

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- 0.01 is about 52% of 0.019
- 0.01 is about 0.02% of 52

## Elasticity

the change in  $\ln R_0$  caused by a small *proportional* change in a vital rate

# Elasticity

Common frog example

By hand



# Elasticity

Common frog example

By hand



Analytically

`popbio::elasticity(A)[2,1] = 0.3699`

`popbio::elasticity(A)[1,2] = 0.251`

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# Life history variation

Organisms have limited resources to investment between growth, reproduction, and survivorship

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Evolution selects for different combinations of *life history traits*

- | Demographic traits that influence fitness (i.e., )
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  - growth pattern
  - age at maturity
  - fecundity schedule
  - mortality schedule
  - length of life

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