EXAMINER: Xiaowei Huang DEPARTMENT: Computer Science

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FIRST SEMESTER EXAMINATIONS 2020/21

Advanced Artificial Intelligence

TIME ALLOWED: TWO Hours and Thirty Minutes

INSTRUCTIONS TO CA	ANDIDATES	
NAME OF CANDIDATE		SEAT NO
USUAL SIGNATURE		

READ THE FOLLOWING CAREFULLY:

- 1. Each of the following questions comprise 5 statements, from which you should select one appropriate answer by placing ticks in the appropriate boxes.
- 2. The exam mark is based on the overall number of correctly answered questions. The more questions you answer correctly the higher your mark, incorrectly answered questions do not count against you.
- 3. Enter your name and examination number IN PENCIL on the computer answer sheet according to the instructions on that sheet.
- 4. When you have completed this exam paper, read the instructions on the computer answer sheet carefully and transfer your answers from the exam paper. Use a HB pencil to mark the computer answer sheet and if you change your mind be sure to erase the mark you have made. You may then mark the alternative answer.
- 5. At the end of the examination, be absolutely sure to hand in BOTH this exam paper AND the computer answer sheet.
- 6. Calculators are permitted.

THIS PAPER MUST NOT BE REMOVED FROM THE EXAMINATION ROOM



Part 1: Basic Knowledge

1.	$\{(x^{(1)}, y^{(i)} \text{ is seve}\}$	In learning task best suits the following description: given a set of training instances $\{x_i, y_i^{(1)}\},, \{x_i^{(n)}, y_i^{(n)}\}\}$ of an unknown target function f , where f is the feature vector and f the label for f is the instances into a group such that those instances within a group are similar and those instances as groups are dissimilar.
	□ A.	Anomaly Detection
	□ B .	Supervised learning
	□ C .	Reinforcement learning
	□ D.	Dimensionality Reduction
	■E.	none of the above
2.	Whic	h of the following statements is incorrect?
	□ A.	In an active learning scheme, the learner can actively select instances for training.
	□ B .	The hypothesis space of a learning algorithm is the function space $\mathcal H$ such that each element in $\mathcal H$ is a possible model the learning algorithm will end up with.
	□ C .	dimensionality reduction is to find a model $f \in \mathcal{H}$ that represents each instance \mathbf{x} with a lower-dimension feature vector while still preserving key properties of \mathbf{x} .
	■ D.	Training, test, and validation datasets cannot overlap to make sure that a training algorithm is not biased.
	□ E.	Anomaly detection is to learn model $f \in \mathcal{H}$ that represents "normal" instances, so that the model can later be used to determine whether a new data x looks normal or anomalous.



	Intelligence = Low	Intelligence = High
Grade = A	0.07	0.21
Grade = B	0.28	0.09
Grade = C	0.27	0.08

Table 1: Joint probability for student grade and intelligence

3. According to the table in Table 1 about two random variables *Intelligence* and *Grade*, please select a value for x to make the following expression hold (rounded to 2 decimal places):

$$P(Grade = C \mid Intelligence = High) = x$$

- \Box **A.** x = 0.27
- □ **B.** x = 0.44
- □ **C.** x = 0.65
- □ **D.** x = 0.35
- **E.** x = 0.21
- **4.** Compute the following conditional probability according to the table in Table 1 (rounded to 2 decimal places)

$$P(Intelligence = low \mid Grade \in \{A, B\}) =$$

- **A.** 0.54
- □ **B.** 0.33
- □ **C.** 0.77
- □ **D.** 0.76
- □ **E.** 0.65



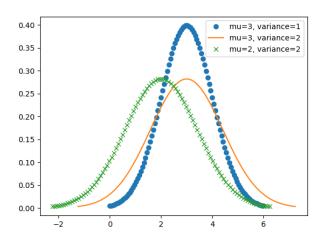
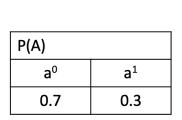
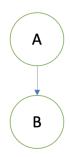


Figure 1: Diagram of three Gaussian distributions with different means and variances

- **5.** Assume we have three functions f_1 , f_2 and f_3 , representing the three Gaussian distributions as in Figure 1. Specifically, we have $f_1 = \mathcal{N}(3, 1^2)$, $f_2 = \mathcal{N}(3, 2^2)$, and $f_3 = \mathcal{N}(2, 2^2)$. Which of the following statements is correct.
 - \square **A.** arg max_x $f_1(x) \approx 0.4$
 - \square **B.** $\max_{x} f_1(x) = \max_{x} f_2(x)$
 - \Box **C.** $\forall x : f_1(x) \geq f_2(x)$
 - **D.** $\forall x : f_2(x) = f_3(x-1)$
 - \square **E.** arg max_x $f_2(x) = \arg \max_x f_3(x)$







P(B A)		
	þ ^o	b^1
a ⁰	0.1	0.9
a ¹	0.4	0.6

Figure 2: Probabilistic Graph of Diseases (A) and Symptom (B)

6. Use the information provided in Figure 2 to compute the following joint probability

$$P(A = a^1, B = b^1) =$$

- □ **A.** 0.12
- □ **B.** 0.36
- □ **C.** 0.3
- □ **D.** 0.48
- **E.** 0.18

7. Use the information provided in Figure 2 to compute the following expression

$$\max_{A,B} P(A,B) =$$

- □ **A.** 0.48
- \Box **B.** a^1, b^1
- **C.** 0.63
- □ **D.** 0.5
- \Box **E.** a^0, b^1



8.	Use the information	provided in	n Figure	2 to	compute	the	following	maximum	а	posteriori
	expression									

MAP(A, B) =

- □ **A.** 0.36
- \Box **B.** a^1, b^1
- □ **C.** 0.5
- **D.** a^0, b^1
- \Box **E.** a^1, b^1
- 9. Understanding simple numpy command.

Assume that a = np.arange(100).reshape((4, 25)). Then a[:, 3:5].T.shape =

- □ **A.** (3,5)
- □ **B.** 10
- □ **C**. (2,5)
- □ **D.** (5,2)
- **E.** (2,4)
- **10.** Let x = (-5, 2, 3, -6) be a vector. Then its L^2 norm $||x||_2 =$
 - A. $\sqrt{74}$
 - □ **B.** $\sqrt{30}$
 - □ **C.** 10
 - \Box **D.** $\sqrt{22}$
 - \Box **E.** $\sqrt{54}$
- **11.** Let x = (-1, 3, -4, 5) be a vector. Then its L^1 norm $||x||_1 =$
 - □ **A.** $\sqrt{30}$
 - □ **B**. 5
 - □ **C.** 6
 - □ **D**. 10
 - **E.** 13



Part 2: Simple Learning Models

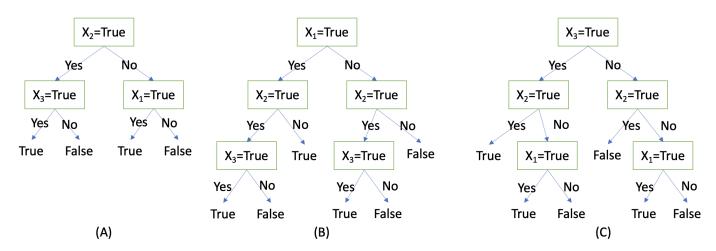


Figure 3: Decision Trees

- **12.** Which decision trees in Figure 3 cannot represent the Boolean formula $(x_1 \land \neg x_2) \lor (x_2 \land x_3)$?
 - □ **A.** A and B
 - □**B.** B
 - □ **C.** C
 - □ **D.** A and C
 - E. none of the above answers is correct



Index	Sepal Length	Sepal Width	Pedal Length	Pedal Width	Iris Class
1	5	3	1	0.5	0
2	4	3	1	0.5	0
3	4	3	1	0.5	0
4	5	3	1	0.5	0
5	4	3	1	0.5	0
6	7	3	4	1	1
7	6	3	4	1	1
8	6	3	4	1	1
9	4	2	3	1	1
10	6	3	6	2	2
11	5	2	5	2	2
12	7	3	5	2	2
13	5	2	5	2	2
14	6	2	5	1	2

Figure 4: Dataset for Iris Flowers

13. Figure 4 gives an example dataset D about Iris flowers. Please indicate which of the following expressions is used to compute its entropy $H_D(Y)$, where Y is the random variable for labelling:

$$\Box \mathbf{A.} \ \frac{8}{14} \log_2(\frac{8}{14}) + \frac{6}{14} \log_2(\frac{6}{14})$$

$$\square \, \mathbf{B.} \, -\frac{4}{14} \log_2(\frac{4}{14}) - \frac{4}{14} \log_2(\frac{4}{14}) - \frac{4}{14} \log_2(\frac{4}{14}) - \frac{2}{14} \log_2(\frac{2}{14})$$

$$\Box$$
 C. $\frac{4}{14} \log_2(\frac{4}{14}) + \frac{10}{14} \log_2(\frac{10}{14})$

D.
$$-\frac{5}{14}\log_2(\frac{5}{14}) - \frac{5}{14}\log_2(\frac{5}{14}) - \frac{4}{14}\log_2(\frac{4}{14})$$

 \square **E.** none of the above



- **14.** Figure 4 gives an example dataset D about Iris flower. Please compute the information gain of splitting over the feature Sepal Length, i.e., $InfoGain(D, SepalLength) = H_D(Y) H_D(Y \mid SepalLength)$ (over two decimal places):
 - □ **A.** 0.98
 - □ **B.** −0.18
 - □ **C.** 0.46
 - **D.** 0.63
 - □ **E.** 0.05
- **15.** Figure 4 gives an example dataset D about Iris flowers. Please compute the information gain of splitting over the feature Sepal Width $InfoGain(D, SepalWidth) = H_D(Y) H_D(Y \mid SepalWidth)$ (rounded to two decimal places):
 - **A.** 0.28
 - □ **B.** −0.19
 - □**C.** 0.12
 - □ **D.** 0.15
 - □ **E.** 0.13



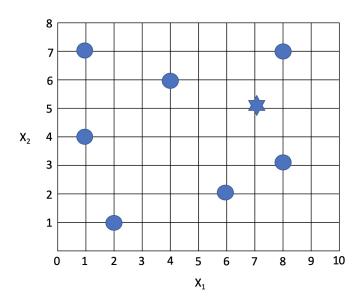


Figure 5: A set of two-dimensional input samples

16. Assume that, as shown in Figure 5, we have a set of training instances with two features X_1 and X_2 :

$$\{(1,7), (1,4), (2,1), (4,6), (6,1.9), (8,3), (8,7)\}$$

such that

- the instance (1, 7) is labeled with value 0,
- the instances (1, 4), (2, 1) are labeled with value 1,
- the two instances (6, 1.9), (8, 3) are labeled with value 2, and
- the instances (4, 6), (8, 7) are labeled with value 3.

Now, we have a new input (7.1,5.1). Please indicate which of the following statements is correct, according to the L^{∞} distance.

- \square **A.** Both (4, 6) and (6,2) are *not* considered for the 3-nn (3-nearest neighbor) classification
- \square **B.** Both (8,3) and (8,7) are *not* considered for the 3-nn (3-nearest neighbor) classification
- □ **C.** (8,3) is *not* considered for the 3-nn (3-nearest neighbor) classification
- □ **D.** Both (6, 2) and (8,3) are *not* considered for the 3-nn (3-nearest neighbor) classification
- E. Both (2,1) and (6,2) are *not* considered for the 3-nn (3-nearest neighbor) classification
- **17.** Continue with the above. Now, for new input (7.1, 5.1), please compute its regression result for the 3-nn (3-nearest neighbor) regression, according to the L^{∞} distance.
 - □ **A.** 5/3
 - \Box **B.** 6.1/3
 - **C.** 8/3
 - □ **D.** 2.1
 - □ **E.** 7/3



18.	Please select the correct statem	nent from the	e following:		
	□ A. Validation dataset is anoth■ B. Validation dataset is often		-	dataset	
	☐ C. Validation dataset is part of	of the test da	taset		
	□ D. Validation dataset cannot	be used for r	egularization		
	☐ E. Test dataset can be overla	apped with th	e training data	aset	
			Actua	l Class	
			positive	negative	
	Predicted Class	positive	а	b	
	Predicted Class	negative	С	d	
	Figure 6: A con	fusion matrix	x for the two-c	class problem	
19.	9. Assume a two-class problem where each instance is classified as either 1 (positive) or -1 (negative). We have a training dataset of 1,000 instances, such that 500 of them are labeled as 1 and 500 of them are labeled as -1. After training, we apply the trained model to classify the 1,000 instances and find that 900 instances are classified correctly. Moreover, we know that, 500 instances are classified as 1 and, within the 500 instances, 50 instances are actually labeled as -1. Please indicate which numbers should be filled in to (a, b, c, d) in Figure 6.				
	□ A. (450, 50, 150, 350) □ B. (450, 50, 100, 400)				
	□ C. (400, 100, 100, 400)				
	■ D. (450, 50, 50, 450)				
	□ E. (400, 50, 150, 400)				
20.	Continue with the above question	on. Please co	ompute the er	ror rate of the	trained model.
	□ A. 50/1000				
	□ B. 150/1000				
	■ C. 100/1000				

□ **D.** 150/2000□ **E.** 150/850



- **21.** Given a set of 4 training data $\{((0,0),0),(0,1),0),(1,0),0),(1,1),1)\}$, where each instance has two features X_1 and X_2 and a label y, linear regression is used to find a linear function $f(\mathbf{x}) = \mathbf{w}^T \mathbf{x} + \mathbf{b}$. Please indicate which of the following statement is correct:
 - \square **A.** if $f(\mathbf{x}) = 2X_1 + X_2 1.2$ then the training accuracy is 1.0.
 - B. if $f(\mathbf{x}) = X_1 + 2X_2 2.5$ then the training accuracy is 1.0.
 - \Box **C.** if $f(\mathbf{x}) = 2X_1 + X_2 + 1.5$ then the training accuracy is 1.0.
 - \square **D.** if $f(\mathbf{x}) = X_1 + X_2$ then the training accuracy is 1.0.
 - \square **E.** none of the above statement is correct.
- **22.** Let $f(X) = 3X_1^2 + 4e^{\sin(X_2)} + 5e^{-X_3}$ be a function, where X_1 , X_2 and X_3 are three variables. Please indicate which of the following gradient expressions is correct:
 - **A.** $\nabla_X f(X) = (6X_1, 4\cos(X_2)e^{\sin(X_2)}, -5e^{-X_3})$
 - \Box **B.** $\nabla_X f(X) = (6, 4\cos(X_2)e^{\sin(X_2)}, -5e^{-X_3})$
 - \Box **C.** $\nabla_X f(X) = (6X_1, 4\sin(X_2)e^{\sin(X_2)}, -5e^{-X_3})$
 - \Box **D.** $\nabla_X f(X) = (6X_1, 4e^{\sin(X_2)}, 5e^{-X_3})$
 - \Box **E.** $\nabla_X f(X) = (6X_1, 4\cos(X_2)e^{\sin(X_2)}, 5e^{-X_3})$



Index	Sepal Length	Sepal Width	Pedal Length	Pedal Width	Iris Class
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4	5	3	1	0.5	0
5	4	3	1	0.5	0
6	7	3	4	1	1
7	6	3	4	1	1
8	6	3	4	1	1
9	4	2	3	1	1
10	6	3	6	2	2
11	5	2	5	2	2
12	7	3	5	2	2
13	5	2	5	2	2
14	6	2	5	1	2

Figure 7: Dataset for Iris Flowers

- 23. Assume a dataset as in Figure 7, and a new data instance (6, 3, 4, 1), please indicate which class the new data instance will be classified into, if we consider Naive Bayes method:
 - □ A. Class 0
 - ■B. Class 1
 - □ **C.** Class 2
 - □ **D.** Either Class 1 or 2
 - ☐ E. Naive Bayes cannot be applied to this dataset



Part 3: Deep Learning

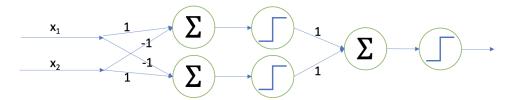


Figure 8: A simple two-layer perceptron

- **24.** Given a simple two-layer perceptron as in Figure 8, where each layer has a linear transformation denoted as Σ in the figure together with an activation function ReLU. ReLU activation function is defined as ReLU = max(0, x). Assume that we have a data instance (1, 3), please indicate which of the following options is the output of the network:
 - □ **A.** 0
 - □ **B**. 1
 - **C**. 2
 - \Box **D**. 3
 - ☐ **E.** None of the above is correct
- **25.** Given a simple two-layer perceptron as in Figure 8, where each layer has a linear transformation denoted as Σ in the figure together with a Sigmoid activation function. Sigmoid activation function is defined as $S(x) = \frac{e^x}{e^x + 1}$. Assume that we have a data instance (1, -1), please indicate which of the following options is the output of the network:
 - \Box **A.** $\frac{1}{1+e}$
 - □ **B.** 1
 - C. $\frac{e}{1+e}$
 - \Box **D.** $\frac{e^2}{1+e^2}$
 - \square **E.** none of the above
- **26.** Which of the following statements is correct?
 - ☐ A. The success of deep learning is based on various architectures such as the well-known recurrent neural network LSTM
 - ☐ **B.** Exclusive or (XOR) can be solved by single perceptron
 - ☐ **C.** One of the main contributions of Frank Rosenblatt is the concept of Perceptron
 - □ **D.** Rosenblatt's algorithm can be applied to train deep neural networks
 - **E.** None of the above statement is correct



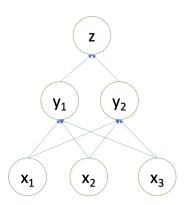


Figure 9: A simple 3-layer neural network

- **27.** Figure 9 gives a simple 3-layer neural network with 3 inputs x_1, x_2, x_3 and a single output z. Let $z = 3y_1 + 4y_2 + 2$, $y_1 = 2x_1 + 3x_2 + x_3 + 1$, $y_2 = 3x_1 + x_2 + 5x_3 2$. Please indicate which of the following expressions is correct for the gradient?
 - $\Box \mathbf{A.} \ \frac{\partial z}{\partial x_1} = 17$
 - \Box **B.** $\frac{\partial z}{\partial x_3} = 6$
 - $\Box \mathbf{C.} \ \frac{\partial z}{\partial x_2} = 12$
 - $\Box \, \mathbf{D}. \ \frac{\partial z}{\partial x_2} = 18$
 - E. $\frac{\partial z}{\partial x_3}$ = 23



input					
4	0	1	7		
5	6	9	-5		
-3	8	3	6		
2	2	1	4		



Figure 10: A two-dimensional input and a convolutional filter

28.	The following four questions are related to Figure 10. In Figure 10, we have a two-dimensional input and a convolutional filter. Given stride = 2, please indicate which of the following statements is correct if zero-padding is not applied?
	\Box A. the result is a one dimensional array of length 9
	■ B. the result is a two dimensional array of shape (2, 2)
	\Box C. the result is a two dimensional array of shape (3, 3)
	\Box D. the result is a two dimensional array of shape (4, 3)
	□ E. None of the above is correct
29.	Continue with the above question related to Figure 10, where there are a two-dimensional input and a convolutional filter. Given stride=2, please indicate which of the following statements is correct for the result of applying the convolutional filter on the input if zero-padding is not applied?
	□ A. there is an element 45
	□ B. the smallest element is 39
	□ C. there is an element 49
	□ D. the greatest element is 69
	■ E. None of the above is correct
30.	Take the same input as in Figure 10 and apply max-pooling on 2×2 filter with a stride 2. Please indicate which of the following statements is correct?
	\Box A. the result is a one dimensional array of length 2
	\square B. the result is a one dimensional array of length 4
	■ C. the result is a two dimensional array of shape (2, 2)
	\Box D. the result is a two dimensional array of shape (3, 3)
	☐ E. None of the above is correct



31.		inue with the above question. Please indicate which of the following statements is correct e result of applying max-pooling on 2×2 filter (stride 2) on the input ?
	□ A.	there is a single element with value 7
	■ B.	there is a single element with value 9
	□ C .	there are two elements with value 7
	□ D.	there are three elements with value 9
	□ E .	None of the above is correct
32.		h of the following statements is incorrect with respect to the features and the feature folds?
	□ A.	In an end-to-end learning of feature hierarchy, initial modules capture low-level features, middle modules capture mid-level features, and last modules capture high level, class specific features.
	□ B .	The computation of the coordinates of the data with respect to feature manifolds enables an easy separation of the data.
	□ C .	Generation of feature manifolds for a given dataset is a non-trivial task, and the dimensionality reduction techniques such as PCA and t-SNE cannot work well on complex datasets.
	□ D .	It is very often that high-dimensional data lie on lower dimensional feature manifolds.
	■ E.	All of the above statements are correct.



Part 4: Probabilistic Graphical Models

33.	Which of the following statements is correct:
	□ A. Naive Bayes cannot be represented as a Bayesian network
	■ B. Bayesian network is not an alias of Bayesian neural network
	\Box C. Every node a in a Bayesian network is associated with a conditional probability table $P(a S)$ with S being a nonempty set of other nodes
	□ D. Graph and joint probability distribution are two key factors for Bayesian networks to represent joint probability distribution
	□ E. None of the above statement is correct



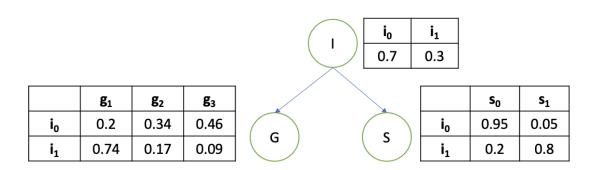


Figure 11: Simple Probabilistic Graphical Model

34. Figure 11 provides a simple probabilistic graphical model of three variables S, G, and I. We already know that

$$P \models (S \perp G \mid I)$$

Which of the following is the value of $P(i_0, s_1, g_3)$?

- **A.** 0.0161
- □ **B.** 0.246
- □ **C.** 0.408
- □ **D.** 0.0216
- □ **E.** 0.0317



Х	Y	Z	P(X,Y,Z)
x ₀	y ₀	z ₀	0.02
x ₀	y ₁	z ₀	0.08
X ₁	y ₀	z ₀	0.03
X ₁	y ₁	z ₀	0.12
x ₀	y ₀	\mathbf{z}_1	0.06
x ₀	y ₁	\mathbf{z}_1	0.24
X ₁	y ₀	z ₁	0.09
x ₁	y ₁	z ₁	0.36

X	Y	Z	P(X,Y,Z)
x _o	y ₀	z _o	0.01
x _o	y ₁	z _o	0.04
x ₁	y ₀	z ₀	0.015
X ₁	y ₁	z ₀	0.06
x _o	y ₀	z ₁	0.07
x _o	y ₁	z ₁	0.28
x ₁	y ₀	z ₁	0.105
x ₁	y ₁	z_1	0.42

(a) (b)

Figure 12: Joint probability of three random variables

- **35.** Figure 12 (a) provides a joint probability P. Let I(P) to be the set of conditional independence assertions of the form $(X \perp Y | Z)$ that hold in P. Which of the following is correct?
 - \square **A.** $(X \perp Y \mid Z) \notin I(P)$ but $(X \perp Y) \in I(P)$
 - \square **B.** $(Y \perp Z \mid X) \in I(P)$ but $(X \perp Y) \notin I(P)$
 - \blacksquare C. $(X \perp Y) \in I(P)$
 - \square **D.** $I(P) = \emptyset$
 - ☐ **E.** None of the above is correct
- **36.** Figure 12 (b) provides a joint probability P. Let I(P) be the set of conditional independence assertions of the form $(X \perp Y | Z)$ that hold in P. Which of the following is correct?
 - \square **A.** $(X \perp Z \mid Y) \notin I(P)$
 - \Box **B.** $(Y \perp Z \mid X) \notin I(P)$
 - \Box **C.** $(X \perp Y) \notin I(P)$
 - \square **D.** $I(P) = \emptyset$
 - **E.** None of the above is correct



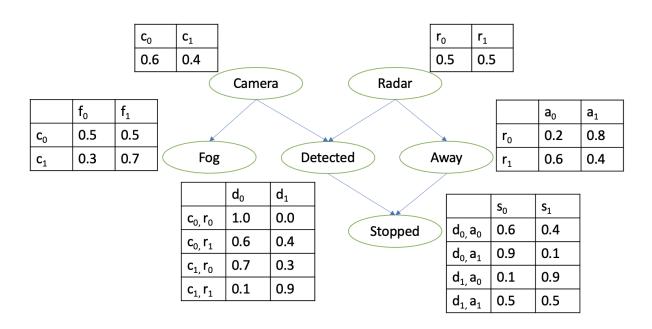


Figure 13: A Bayesian network G

- **37.** Consider the Bayesian network model G in Figure 13 and indicate which of the following is not in the I-map I(G):
 - □ **A.** (Fog⊥Radar, Detected, Away, Stopped | Camera)
 - **B.** (Detected ⊥ Radar, Fog, Stopped | Camera, Away)
 - □ **C.** (Camera⊥Radar)
 - \Box **D.** (Away \bot Camera, Fog, Detected | Radar)
 - \square **E.** All the above are in I(G)
- **38.** Consider the Bayesian network model G in Figure 13 and calculate the following value

$$P(c_1, r_0, a_0, d_1, f_1, s_0) =$$

- □ **A.** 0.0036
- □ **B.** 0.0342
- □ **C.** 0.0024
- □ **D.** 0.0252
- E. none of the above answers is correct



39.	Consider the Bayesian network model G in Figure 13 and calculate the following condition	nal
	probability (rounded to two decimal places)	

 $P(c_0|s_1, d_0, a_1) =$

- **A.** 0.72
- □ **B.** 0.68
- □ **C.** 0.03
- □ **D.** 0.81
- \square **E.** none of the above answers is correct



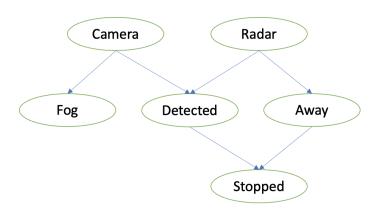


Figure 14: A simple probabilistic graphical model

- **40.** Consider the probabilistic graphical model in Figure 14. Please indicate which of the following statements is incorrect.
 - ☐ **A.** Away can influence Fog when only Stopped and Radar are observed.
 - □ **B.** *Fog* can influence *Radar* when only *Stopped* is observed.
 - ☐ **C.** Camera can influence Radar when only Detected is observed.
 - □ **D.** *Camera* can influence *Away* when only *Detected* is observed.
 - **E.** *Fog* can influence *Radar* when only *Away* is observed.



This page collects some formulas/expressions that may be used in this exam.

1. entropy:

$$-\sum_{y \in values(Y)} P(y) \log_2 P(y)$$

2. conditional entropy:

$$H(Y|X) = \sum_{x \in values(X)} P(X = x)H(Y|X = x)$$

where

$$H(Y|X = x) = -\sum_{y \in values(Y)} P(Y = y|X = x) \log_2 P(Y = y|X = x)$$