

# **ECS 132 Term Project**

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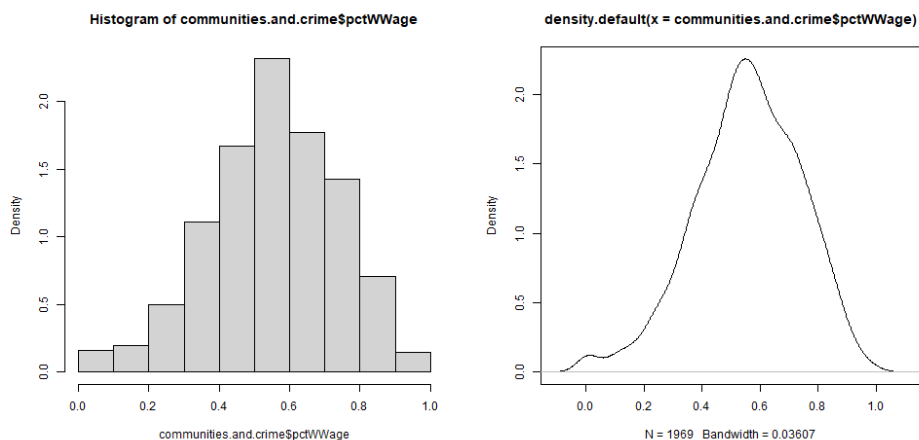
June 2023

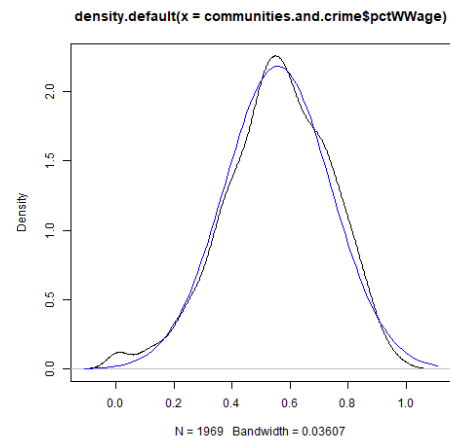
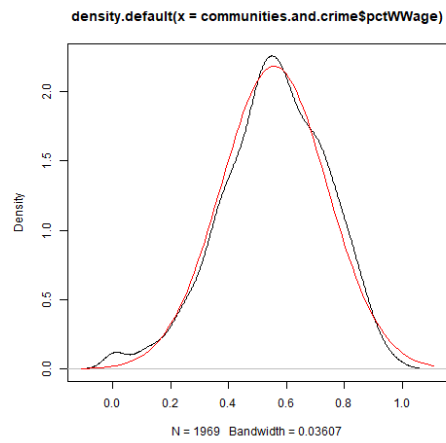
# Chapter 1

## The Normal Family

### 1.1 Communities and Crime: pctWWage

Our group observed that the variable **pctWWage** of the Communities and Crime dataset seemed well-approximated by the normal family of continuous distributions. According to the UCI Machine Learning Repository, **pctWWage** is described as the percentage of households within the United States with wage or salary income in 1989.



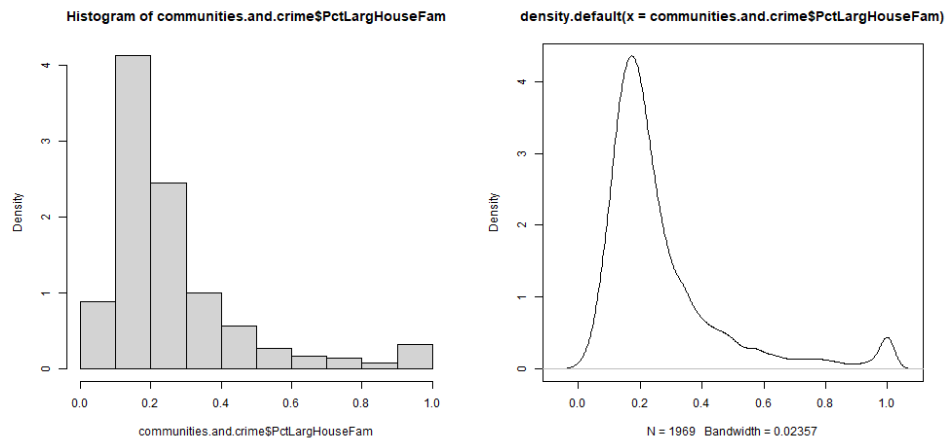


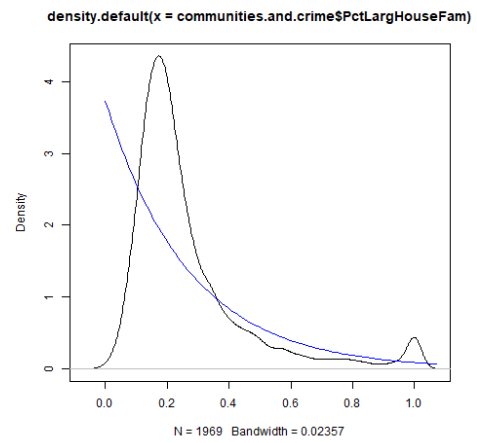
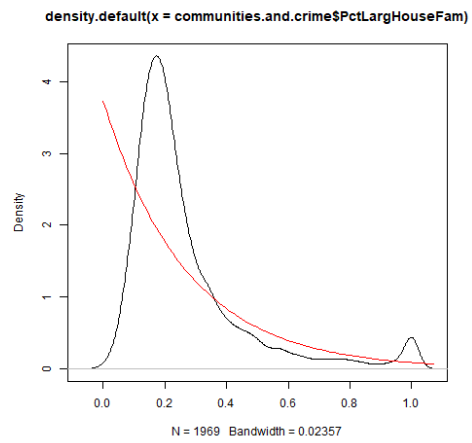
# Chapter 2

## The Exponential Family

### 2.1 Communities and Crime: PctLargHouseFam

For the exponential family of continuous distributions, we observed that the variable **PctLargHouseFam** was a suitable approximation. According to the UCI Machine Learning Repository, **PctLargHouseFam** is described as the percentage of family households with six or more family members.



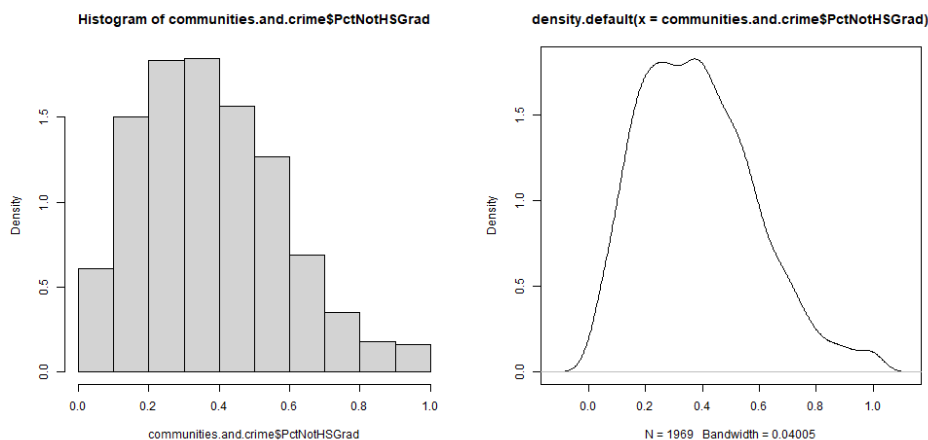


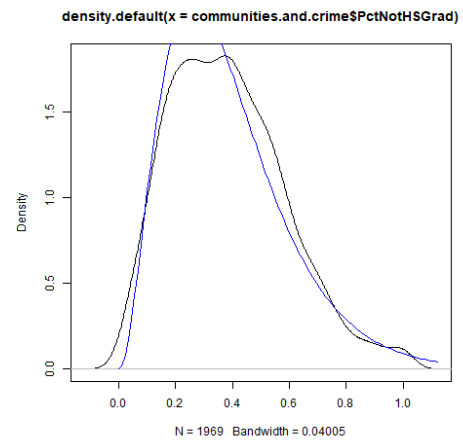
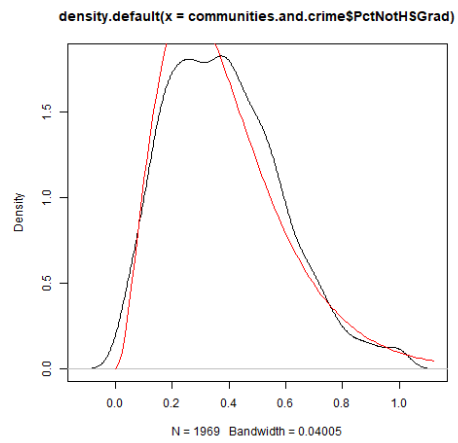
# Chapter 3

## The Gamma Family

### 3.1 Communities and Crime: PctNotHsGrad

We observed that the variable **PctNotHsGrad** of the Communities and Crime dataset seemed well-approximated by the gamma family of continuous distributions. According to the UCI Machine Learning Repository, **PctNotHsGrad** is described as the percentage of people 25 and over that are not high school graduates.





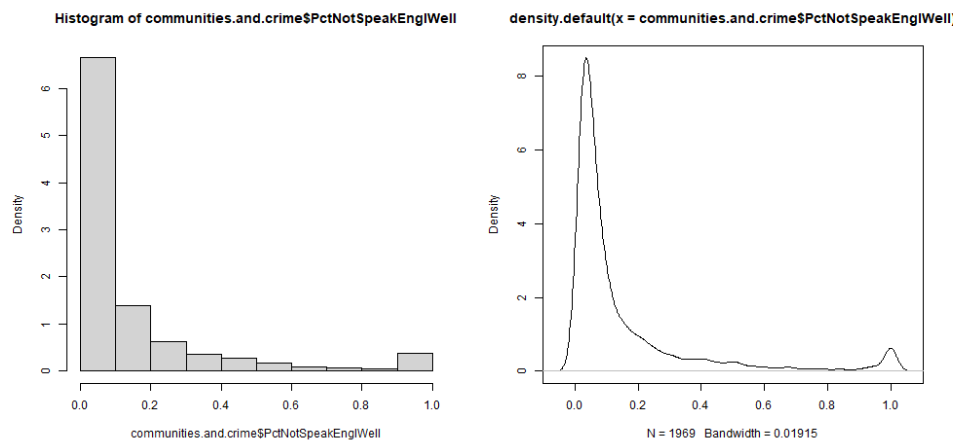
# Chapter 4

## The Beta Family

### 4.1 Communities and Crime: PctNotSpeakEnglWell

For the beta family of continuous distributions, we observed that the variable **PctNotSpeakEnglWell** was a suitable approximation. According to the UCI Machine Learning Repository, **PctNotSpeakEnglWell** is described as the percentage of people who do not speak English well.

### 4.2 Histogram and Density





## 4.3 MLE and MM

To find the MLE of the beta family, we first had to scale our data so it was within the support of  $(0, 1)$ :

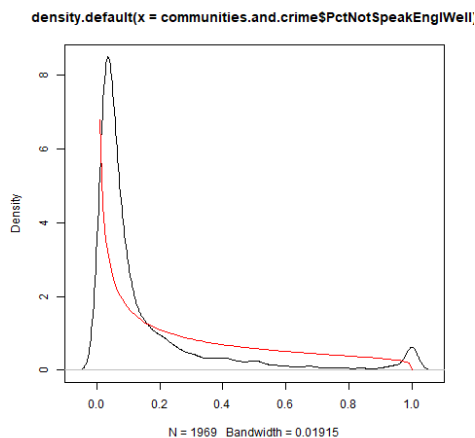
```
1 x[which(x == 0)] <- 0.0001
2 x[which(x == 1)] <- 0.9999
```

We then found the log likelihood function:

$$L(\alpha, \beta) = n \log(\Gamma(\alpha + \beta)) - n \log(\Gamma(\alpha)) - n \log(\Gamma(\beta)) + (\alpha - 1) \sum (\log(x)) + (\beta - 1) \sum (\log(1 - x)) \quad (4.1)$$

To find the MLE, we use R's built in `mle()` function with the negative value of our 4.1 log likelihood function.

```
1 z <- mle(minuslogl = ll, start = c(list(alpha = 1),
  list(beta = 1)))
```



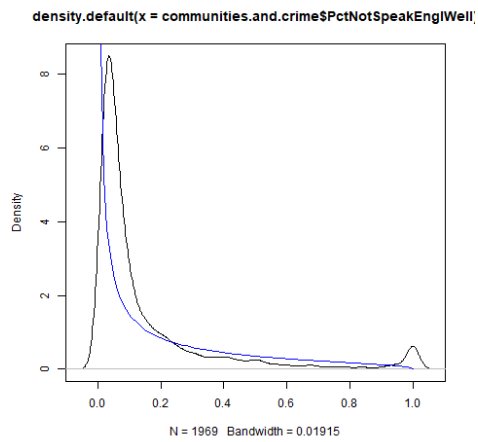
To find the MM of the beta family, we used the following function to estimate the  $\alpha$  and  $\beta$  values:

```
1 mm <- function(x) {
2   mu <- mean(x)
3   var <- var(x)
4   alpha <- mu * (mu * (1 - mu) / var - 1)
```

```

5   beta <- (1 - mu) * (mu * (1 - mu) / var - 1)
6   return(c(alpha, beta))
7 }

```



## 4.4 Conclusion