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**ECS 140A: Fall 2023**  
**Homework Assignment 1**

**Due Date:** No later than Monday, October 23, 11:00pm PDT

This assignment asks you to prepare written answers to questions on BNF and EBNF. Make sure your written work is very readable. We will not grade what we cannot read. Make sure you follow the new policy regarding the use of outside sources such as ChatGPT. **Make sure your answers are contained in the answer box corresponding to each question. Do not submit any other pages or parts of your answers outside the answer boxes. You must only submit these assignment sheets. After you are done, scan them into a PDF file and turn it in via Gradescope by the due date above.**

1. (15 pts) Consider the following BNF grammar:

$\langle S \rangle ::= a \langle S \rangle c \langle B \rangle \mid \langle A \rangle \mid b$

$\langle A \rangle ::= c \langle A \rangle \mid c$

$\langle B \rangle ::= d \mid \langle A \rangle$

For each of the strings below, indicate whether or not the string can be derived from the grammar ("yes" or "no"). If the string can be derived from the grammar, provide a left-most derivation that shows all derivation steps. Otherwise, simply indicate "no."

(a) (5 pts) aabccd

no

(b) (5 pts) accbcc

no

(c) (5 pts) accccc

yes

```
<S> := a <S> c <B>
::= a <A> c <A>
::= a c <A> c c <A>
::= a c c c c c
```

2. (20 pts) Convert the following BNF grammar into EBNF.

```
<integer> ::= <unsigned> | <sign> <unsigned>
<unsigned> ::= <digits> | <unsigned> <digits>
<digits> ::= <digits> <digit> | <digit>
<digit> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
<sign> ::= + | -
```

```
<integer> ::= [<sign>] <unsigned>
<unsigned> ::= [<unsigned>] <digits>
<digits> ::= <digit> {<digit>}
<digit> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
<sign> ::= + | -
```

3. (25 pts) What language is generated by each of the BNF grammars below (assuming that  $\langle S \rangle$  is the start symbol)? You may describe the language in plain English, math notations, or a combination of both.

(a) (5 pts)

$\langle S \rangle ::= ab \mid a \langle S \rangle b$

all strings starting with  $n$  a's and ending with  $n$  b's,  
where  $n$  is non negative integer

(b) (10 pts)

$\langle S \rangle ::= \langle A \rangle \langle B \rangle \langle C \rangle$

$\langle A \rangle ::= a \langle A \rangle \mid a$

$\langle B \rangle ::= b \langle B \rangle \mid b$

$\langle C \rangle ::= c \langle C \rangle \mid c$

all strings with  $x$  a's, followed by  $y$  b's, ending with  $z$  c's,  
where  $x$ ,  $y$ , and  $z$  are non negative integers

(c) (10 pts)

$\langle S \rangle ::= \langle x \rangle \mid \langle y \rangle$

$\langle x \rangle ::= 0 \langle x \rangle 1 \mid \langle x1 \rangle$

$\langle x1 \rangle ::= 0 \langle x1 \rangle \mid 0$

$\langle y \rangle ::= 0 \langle y \rangle 1 1 \mid \langle y1 \rangle$

$\langle y1 \rangle ::= \langle y1 \rangle 1 \mid 1$

all strings starting with x 0's followed by y 1's,  
where x and y are non negative integers

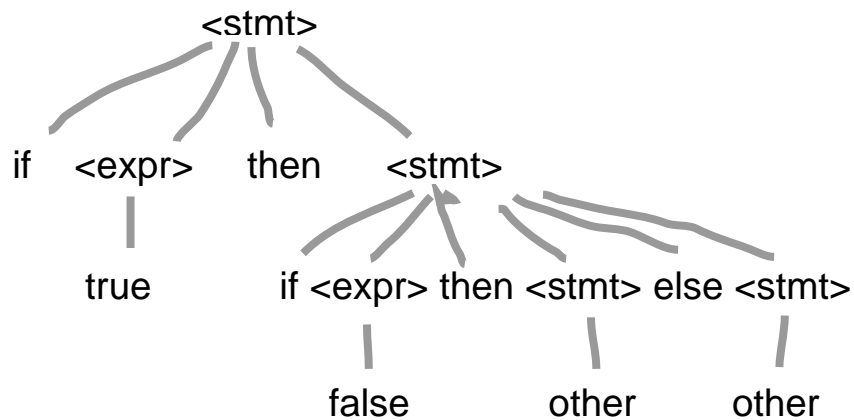
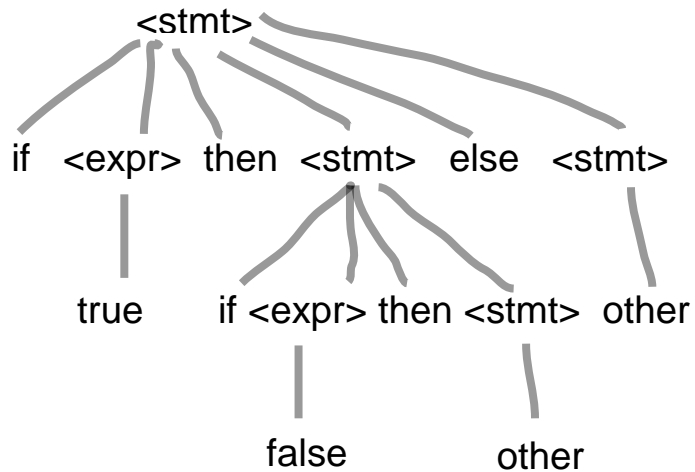
4. (20 pts) Given the following grammar:

$\langle \text{stmt} \rangle ::= \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stmt} \rangle$   
                   $| \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stmt} \rangle \text{ else } \langle \text{stmt} \rangle$   
                   $| \text{other}$   
 $\langle \text{expr} \rangle ::= \text{true} \mid \text{false}$

where other is a terminal that stands for any other kinds of statements.

(a) (10 pts) This grammar is ambiguous. Give a string having two different parse trees and draw the parse trees.

if true then if false then other else other



(b) (10 pts) If we adopt the disambiguating rule (used in most languages) “match each else with the closest previous unmatched then,” write an equivalent, un-ambiguous grammar.

$\langle \text{stmt} \rangle ::= \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stmt} \rangle \langle \text{elsestmt} \rangle \mid \text{other}$

$\langle \text{elsestmt} \rangle ::= \text{else } \langle \text{stmt} \rangle \mid ""$

$\langle \text{expr} \rangle ::= \text{true} \mid \text{false}$

5. (20 pts) Give a BNF and an EBNF for each of the languages below.

(a) (10 pts) The set of all strings consisting of zero or more **a**'s.

BNF:  $\langle S \rangle ::= "" \mid a \langle S \rangle$

EBNF:  $\langle S \rangle ::= \{a\}$

(b) (10 pts) The set of all strings consisting of one or more **a**'s, where there is a comma in between each **a** and the following **a**. Note that there is no comma before the first **a** or after the last **a**.

BNF:  $\langle S \rangle ::= a \mid a , \langle S \rangle$

EBNF:  $\langle S \rangle ::= a \{ , a \}$