

1 Practice Problems

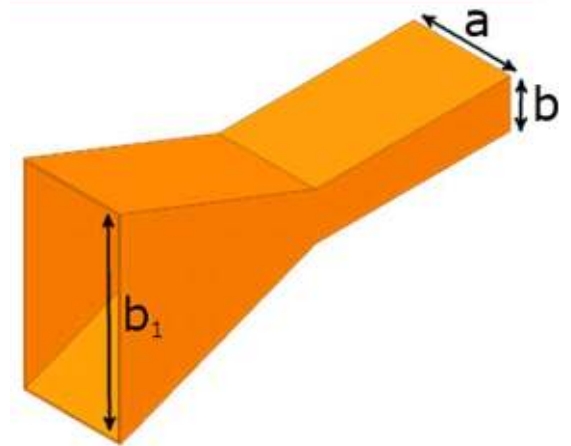


Practice Problem 1

- Find the flare angle of an E-plane sectoral horn antenna such that the maximum phase deviation across the aperture is 60° and with physical dimensions of $a = 0.75\lambda$, $b = 0.25\lambda$, and $b_1 = 1\lambda$

- $$\Delta\phi_{max} = k\delta(y')\big|_{y'=b_1/2} = \frac{k(b_1/2)^2}{2\rho_1}$$
- $$(60^\circ) \left(\frac{\pi}{180}\right) = \frac{k(b_1/2)^2}{2\rho_1}$$
- $$\frac{k}{2\rho_1} = \left(\frac{60\pi}{180}\right) \left(\frac{4}{b_1^2}\right)$$
- $$\frac{1}{\rho_1} = \left(\frac{60\pi}{180}\right) \left(\frac{8}{kb_1^2}\right)$$
- $$\rho_1 = \left(\frac{180}{60\pi}\right) \left(\frac{(2\pi\lambda)b_1^2}{8}\right) = \left(\frac{180}{60}\right) \left(\frac{\lambda b_1^2}{4}\right) = 0.75\lambda$$

$$\Delta\phi_{max} = k\delta(y')\big|_{y'=b_1/2} = \frac{ky'^2}{2\rho_1}$$
$$2\psi_e = 2\tan^{-1}\left(\frac{b_1/2}{\rho_1}\right)$$





Practice Problem 1 cont.

- $2\psi_e = 2 \tan^{-1} \left(\frac{b_1/2}{\rho_1} \right)$
- $2\psi_e = 2 \tan^{-1} \left(\frac{0.5}{0.75} \right)$
- $2\psi_e = 67.38^\circ$

Practice Problem 2

2. Design a Yagi antenna using a half-wave dipole as the driven element with one reflector and one director, as well as find the F/B ratio given the forward and backward power of $P_f = 20dB$ and $P_b = -5dB$ at 5GHz

- $DE = 0.5\lambda = 0.5 \left(\frac{c}{5GHz} \right) = 30mm$
- $RE = 1.05(30mm) = 33mm$
- $DI = 0.95(30mm) = 27mm$
- $F/B = 10 \log(20dB / -5dB) = 10 \log(10 / 0.562)$
- $F/B = 12.503dB$

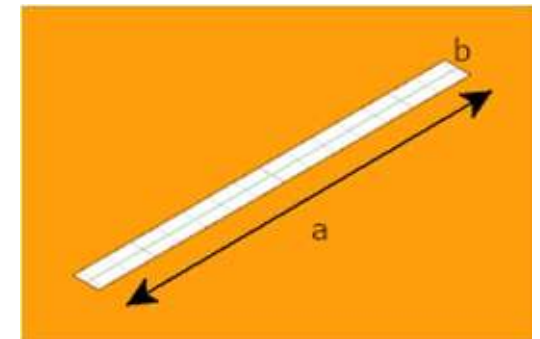
$$\begin{aligned} F/B &= 10 \log \left(\frac{P_f}{P_b} \right) \\ RE &= 1.05 * DE \\ DI &= 0.95 * DE \end{aligned}$$

Practice Problem 3

3. With a rectangular aperture situated on a ground plane with lengths $a = 4\lambda$ and $b = 1.5\lambda$, find the directivity, half power bandwidth, and first null beam width at 10GHz

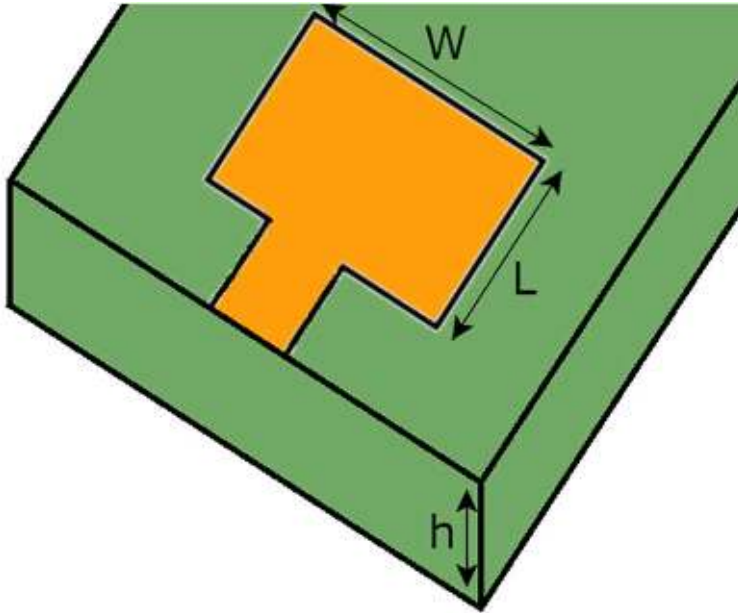
- $D_0 = \frac{4\pi}{\lambda^2} Area = \frac{4\pi ab}{\lambda^2} = \frac{4\pi(4\lambda)(1.5\lambda)}{\lambda^2}$
- $D_0 = 4\pi(4)(1.5) = 75.4$
- $HPBW = \frac{50.6}{b/\lambda} = \frac{50.6}{(1.5\lambda)/\lambda} = \frac{50.6}{1.5} = 33.33^\circ$
- $FNBW = \frac{114.6}{b/\lambda} = \frac{114.6}{(1.5\lambda)/\lambda} = \frac{114.6}{1.5} = 76.4^\circ$

$$D_0 = \frac{4\pi}{\lambda^2} Area$$
$$HPBW = \frac{50.6}{b/\lambda}$$
$$FNBW = \frac{114.6}{b/\lambda}$$



Practice Problem 4

4. Design a rectangular, microstrip patch antenna placed on a substrate with $\epsilon_r = 2.5$ and thickness of $h = 5\text{mm}$ at 5GHz, with no inset feeding



$$\epsilon_{\text{eff}} = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \frac{1}{\sqrt{1 + 12h/W}}$$

$$W = \frac{\lambda}{2} \sqrt{\frac{2}{\epsilon_r + 1}}$$

$$\Delta L = 0.412h \frac{\epsilon_{\text{eff}} + 0.3 \left(W/h + 0.264 \right)}{\epsilon_{\text{eff}} - 0.258 \left(W/h + 0.8 \right)}$$

$$L = \frac{\lambda}{2\sqrt{\epsilon_{\text{eff}}}} - 2\Delta L$$

Practice Problem 4 cont.

- $W = \frac{\lambda}{2} \sqrt{\frac{2}{\epsilon_r + 1}} = \frac{(0.06m)}{2} \sqrt{\frac{2}{(2.5)+1}}$
- $W = 22.68mm$
- $\epsilon_{reff} = \frac{(2.5)+1}{2} + \frac{(2.5)-1}{2} \frac{1}{\sqrt{1+12^{(5mm)/(22.68mm)}}}$
- $\epsilon_{reff} = 2.143$
- $\Delta L = 0.412(5mm) \frac{(2.143)+0.3\left(\frac{(22.68mm)}{(5mm)}+0.264\right)}{(2.143)-0.258\left(\frac{(22.68mm)}{(5mm)}+0.8\right)}$
- $\Delta L = 9.63mm$
- $L = \frac{\lambda}{2\sqrt{\epsilon_{reff}}} - 2\Delta L = \frac{(0.06m)}{2\sqrt{(2.143)}} - 2(9.63mm)$
- $L = 1.23mm$