

4.417486					
std	357.978317	9.996441	10.716328	11.610246	4.286208
1.685804					
min	0.000000	7.500000	8.400000	8.800000	1.728400
1.047600					
25%	120.000000	19.050000	21.000000	23.150000	5.944800
3.385650					
50%	273.000000	25.200000	27.300000	29.400000	7.786000
4.248500					
75%	650.000000	32.700000	35.500000	39.650000	12.365900
5.584500					
max	1650.000000	59.000000	63.400000	68.000000	18.957000
8.142000					

```
numerical_cols = ['Weight', 'Length1', 'Length2', 'Length3', 'Height', 'Width']
```

```
df_regression = df[numerical_cols]
```

```
missing_values_count = df_regression.isnull().sum()
```

```
if missing_values_count.sum() > 0:
    print("Missing values found in the following columns:")
    print(missing_values_count[missing_values_count > 0])
    df_regression_cleaned = df_regression.dropna()
    print("Rows with missing values have been dropped.")
    df = df_regression_cleaned.copy()
else:
    print("No missing values found in the selected numerical columns.")
    df = df_regression.copy()
```

```
print("\nUpdated DataFrame for regression:")
```

```
print(df.head())
```

```
print(f"New shape of DataFrame: {df.shape}")
```

No missing values found in the selected numerical columns.

Updated DataFrame for regression:

	Weight	Length1	Length2	Length3	Height	Width
0	242.0	23.2	25.4	30.0	11.5200	4.0200
1	290.0	24.0	26.3	31.2	12.4800	4.3056
2	340.0	23.9	26.5	31.1	12.3778	4.6961
3	363.0	26.3	29.0	33.5	12.7300	4.4555
4	430.0	26.5	29.0	34.0	12.4440	5.1340

New shape of DataFrame: (159, 6)

```
from sklearn.linear_model import LinearRegression
from sklearn.metrics import r2_score
import matplotlib.pyplot as plt
```

```

# Define dependent and independent variables for the first set of
regressions
y = df['Weight']
independent_vars_set1 = ['Length1', 'Length2', 'Length3', 'Height',
'Width']

print(" Performing Linear Regressions with 'Weight' as Dependent
Variable ")

for ind_var in independent_vars_set1:
    X = df[[ind_var]].values.reshape(-1, 1)

    model = LinearRegression()
    model.fit(X, y)

    y_pred = model.predict(X)

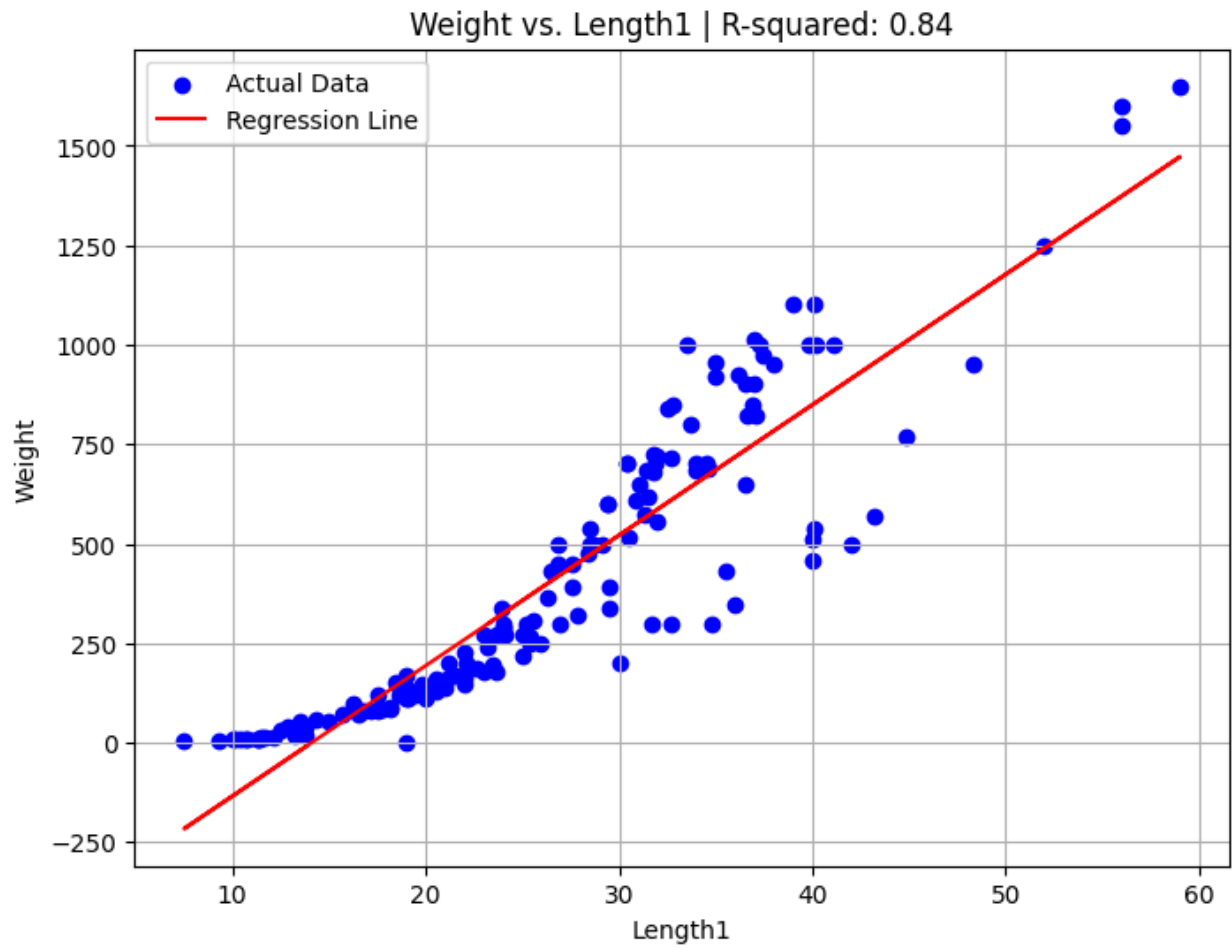
    r2 = r2_score(y, y_pred)

    plt.figure(figsize=(8, 6))
    plt.scatter(X, y, color='blue', label='Actual Data')
    plt.plot(X, y_pred, color='red', label='Regression Line')
    plt.title(f'Weight vs. {ind_var} | R-squared: {r2:.2f}')
    plt.xlabel(ind_var)
    plt.ylabel('Weight')
    plt.legend()
    plt.grid(True)
    plt.show()

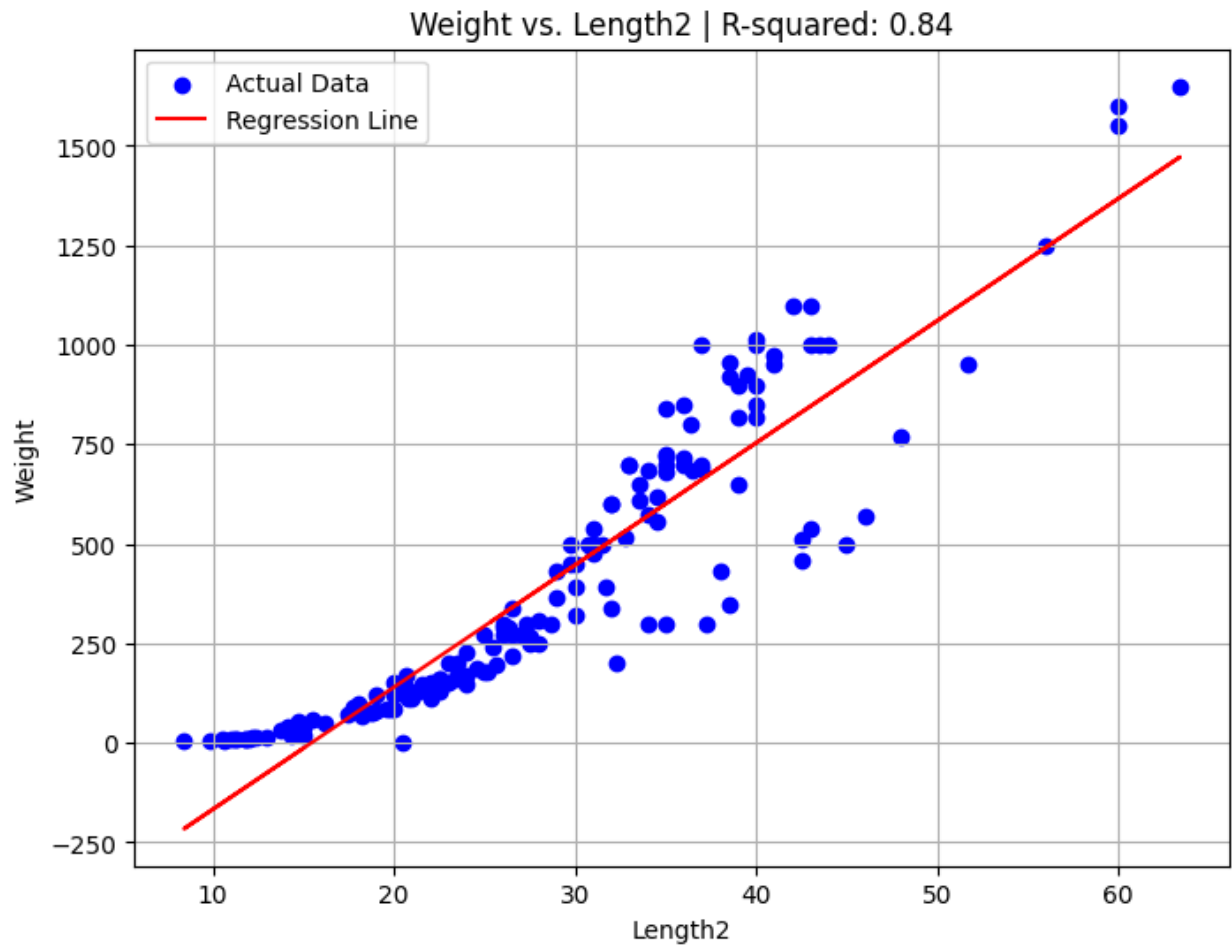
    print(f"Regression for Weight vs. {ind_var}: R-squared =
{r2:.4f}")

--- Performing Linear Regressions with 'Weight' as Dependent Variable
---

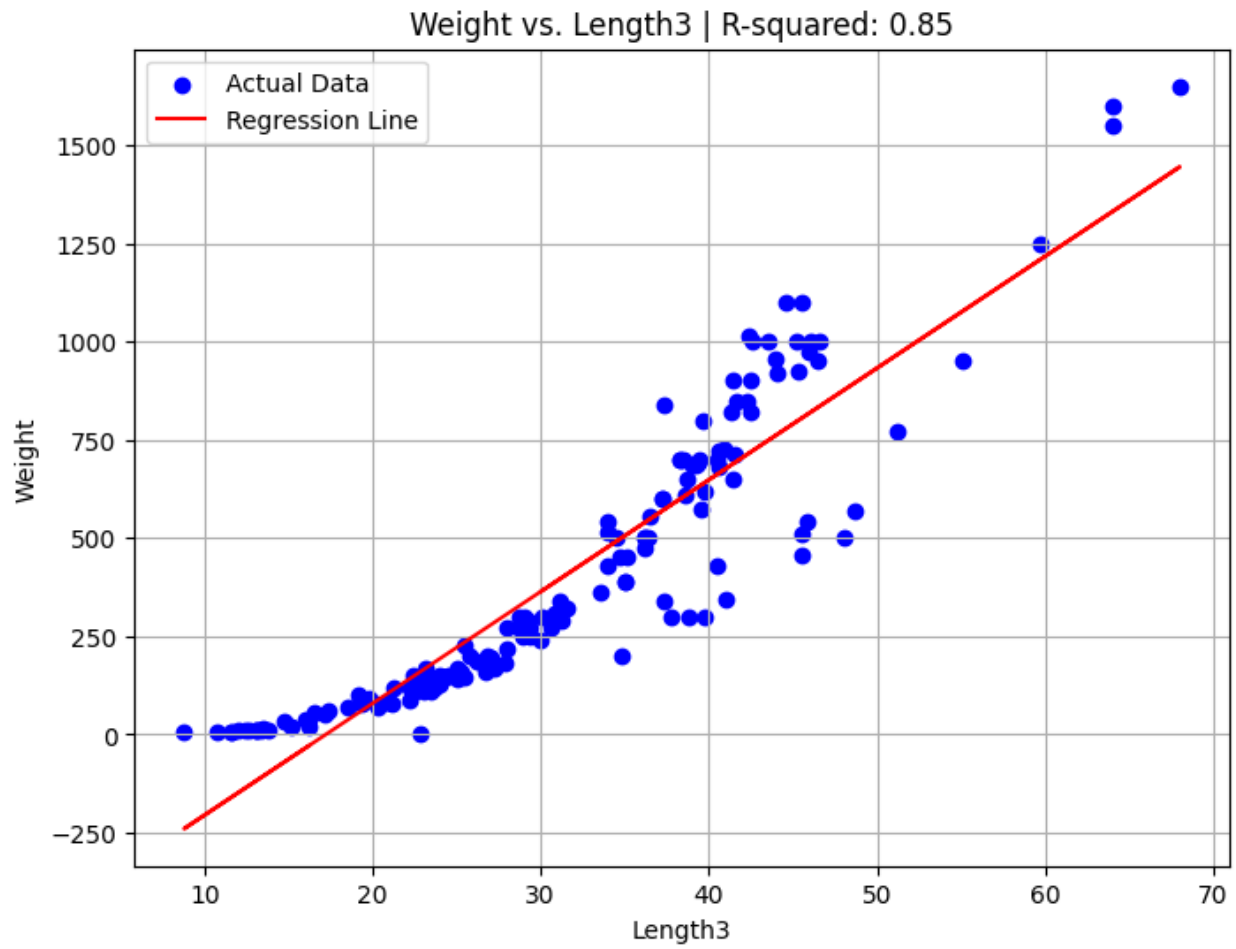
```



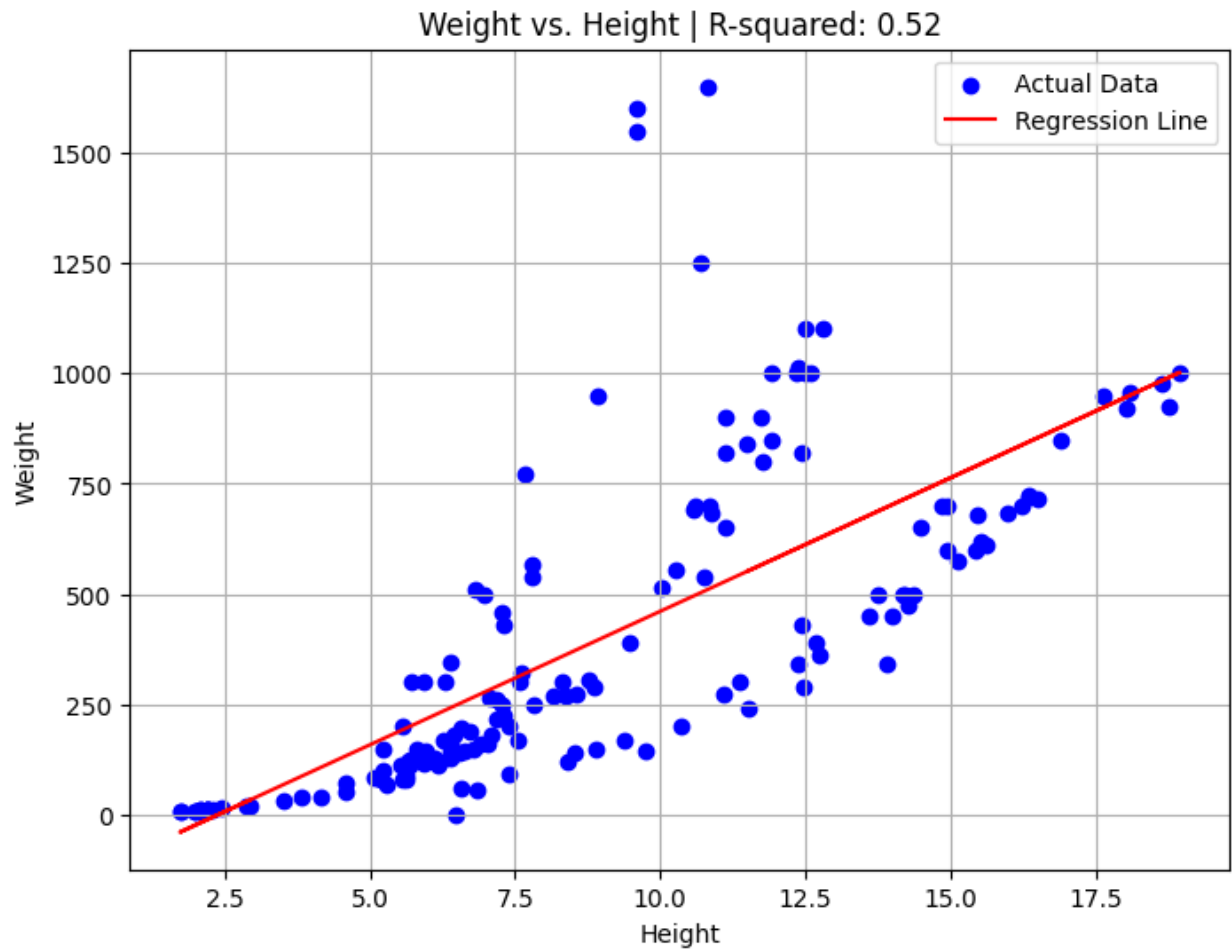
Regression for Weight vs. Length1: R-squared = 0.8385



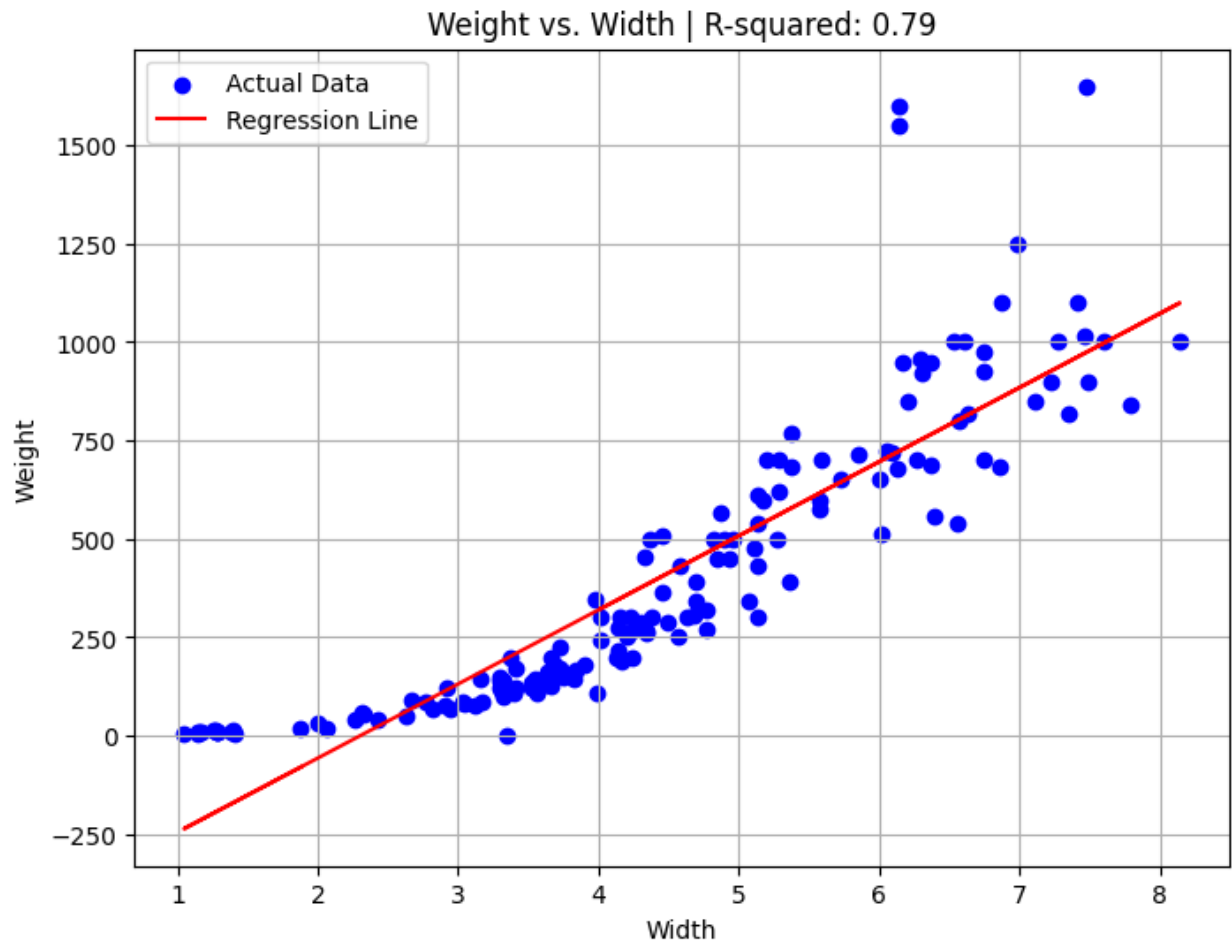
Regression for Weight vs. Length2: R-squared = 0.8439



Regression for Weight vs. Length3: R-squared = 0.8520



Regression for Weight vs. Height: R-squared = 0.5247



Regression for Weight vs. Width: R-squared = 0.7859

```
y = df['Length1']
independent_vars_set2 = ['Length2', 'Length3', 'Height', 'Width',
                          'Weight']

print("\n--- Performing Linear Regressions with 'Length1' as Dependent
Variable ---")

for ind_var in independent_vars_set2:
    X = df[[ind_var]].values.reshape(-1, 1)

    model = LinearRegression()
    model.fit(X, y)

    y_pred = model.predict(X)

    r2 = r2_score(y, y_pred)

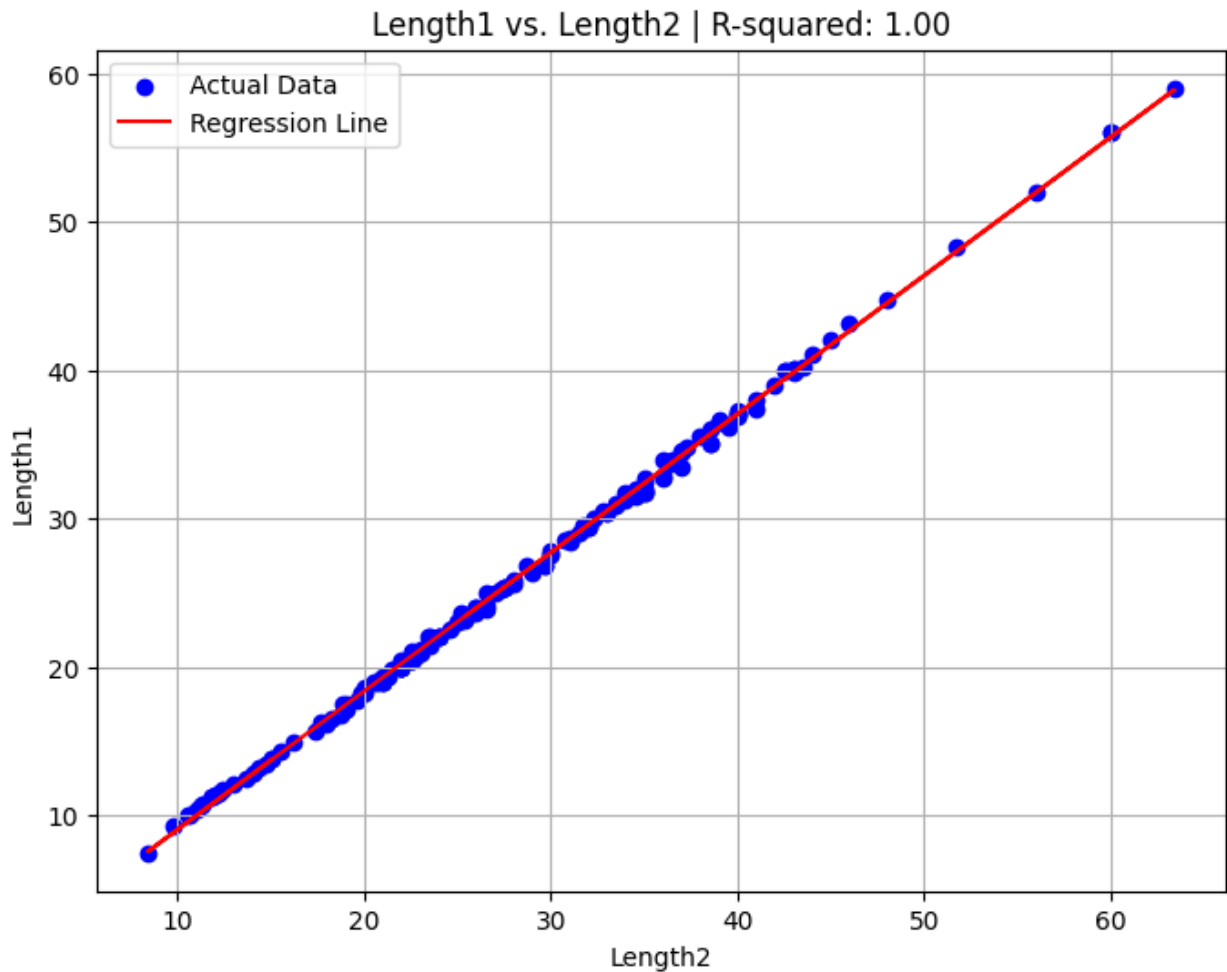
    plt.figure(figsize=(8, 6))
    plt.scatter(X, y, color='blue', label='Actual Data')
```



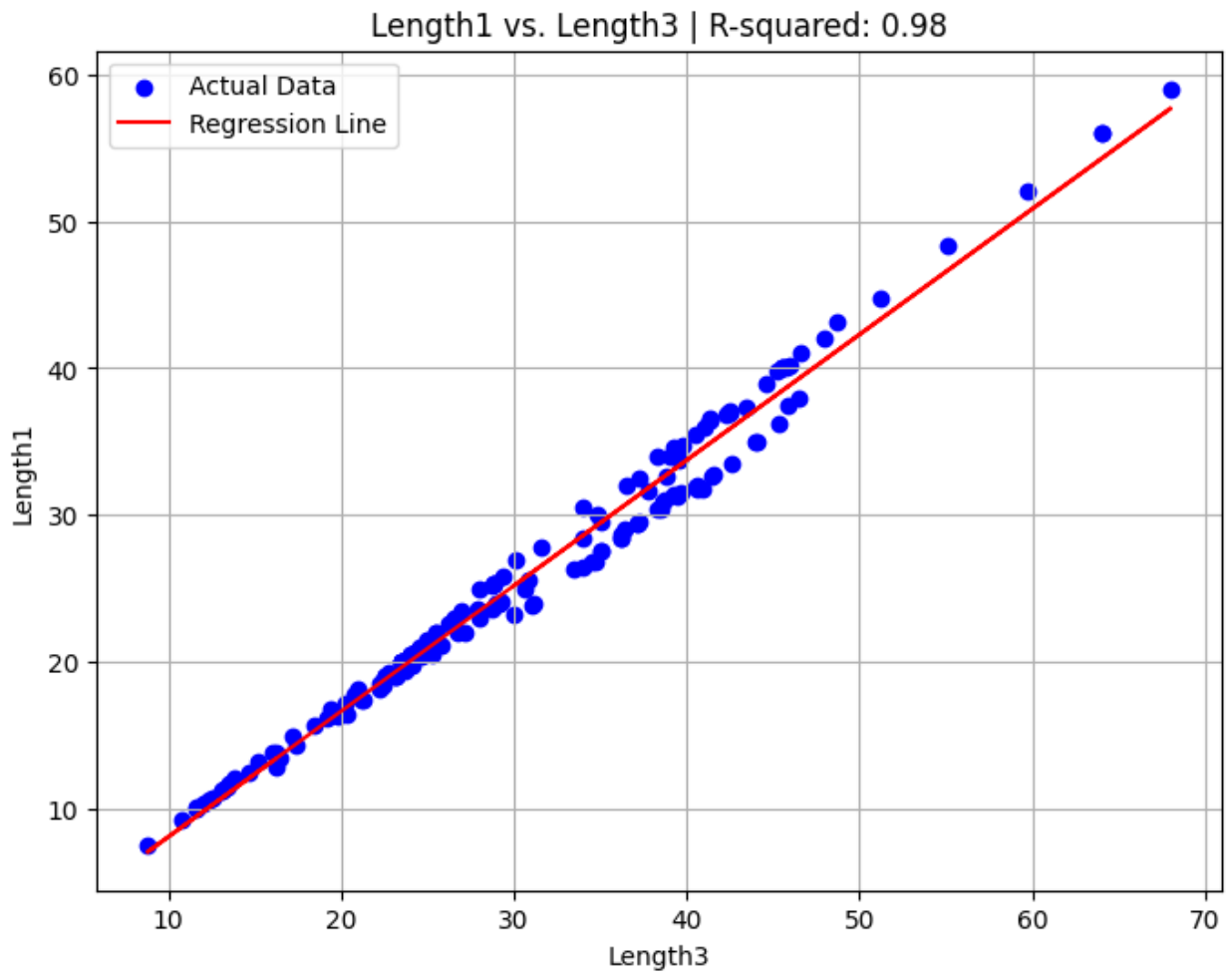
```
plt.plot(X, y_pred, color='red', label='Regression Line')
plt.title(f'Length1 vs. {ind_var} | R-squared: {r2:.2f}')
plt.xlabel(ind_var)
plt.ylabel('Length1')
plt.legend()
plt.grid(True)
plt.show()

print(f"Regression for Length1 vs. {ind_var}: R-squared = {r2:.4f}")

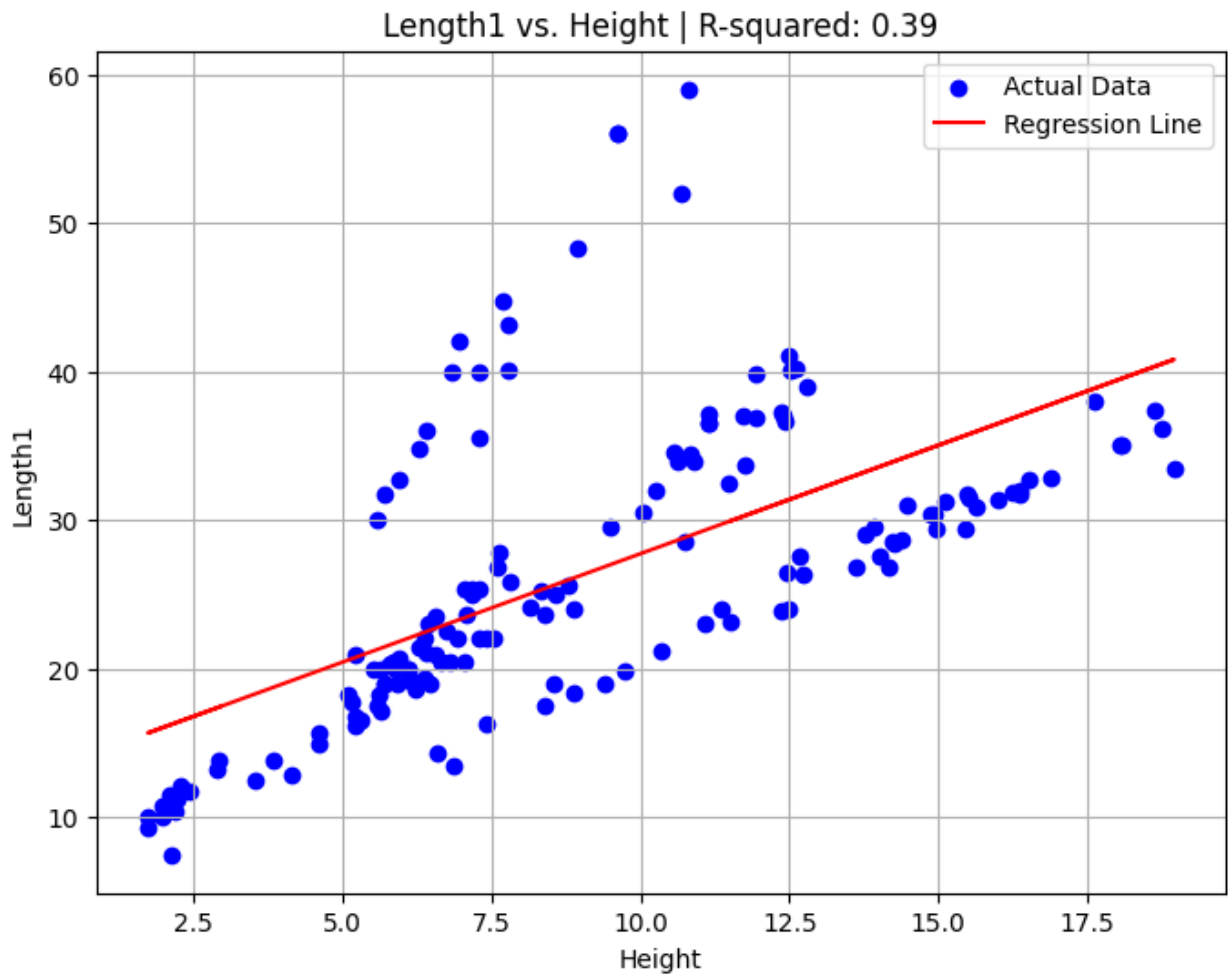
--- Performing Linear Regressions with 'Length1' as Dependent Variable
---
```



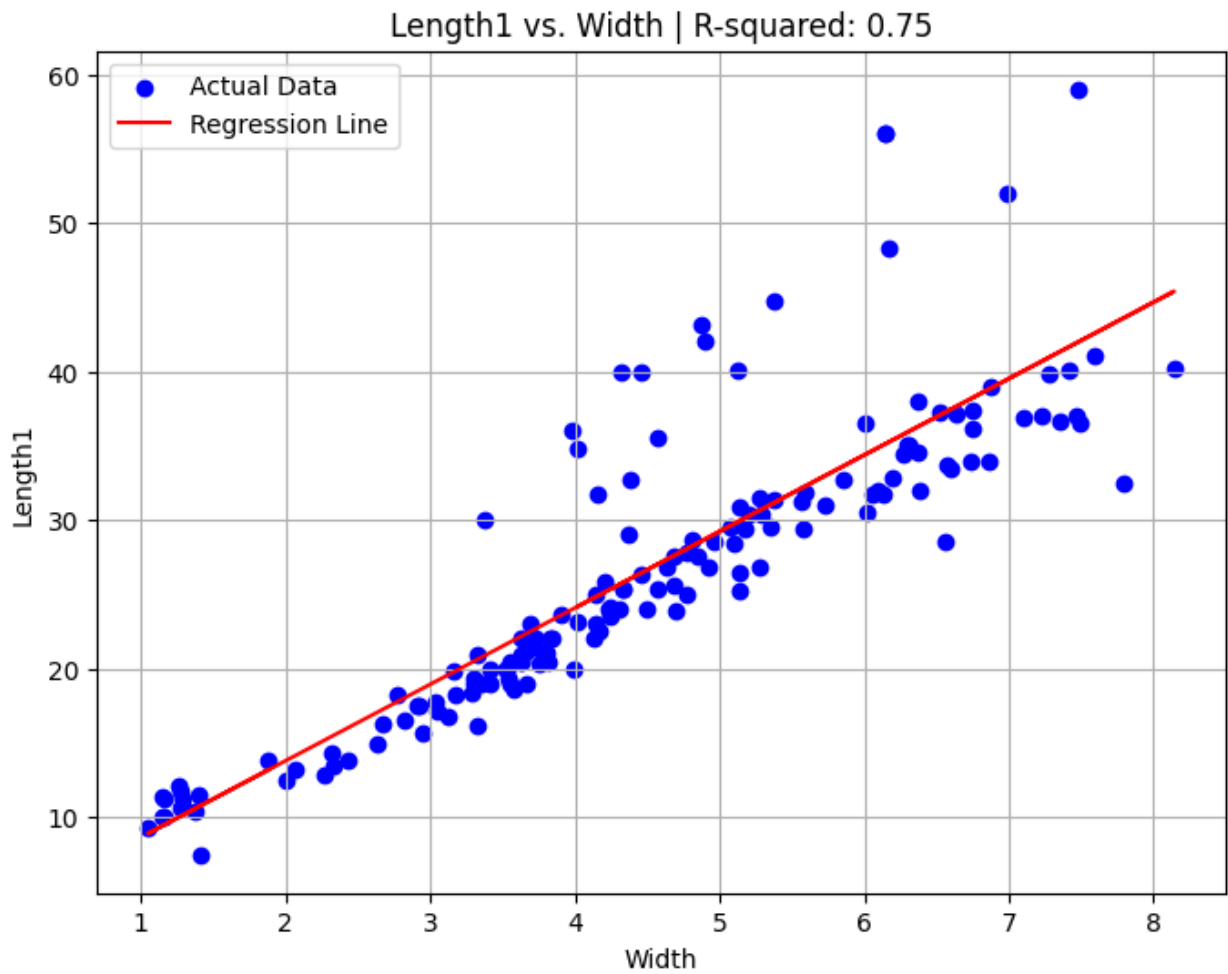
Regression for Length1 vs. Length2: R-squared = 0.9990



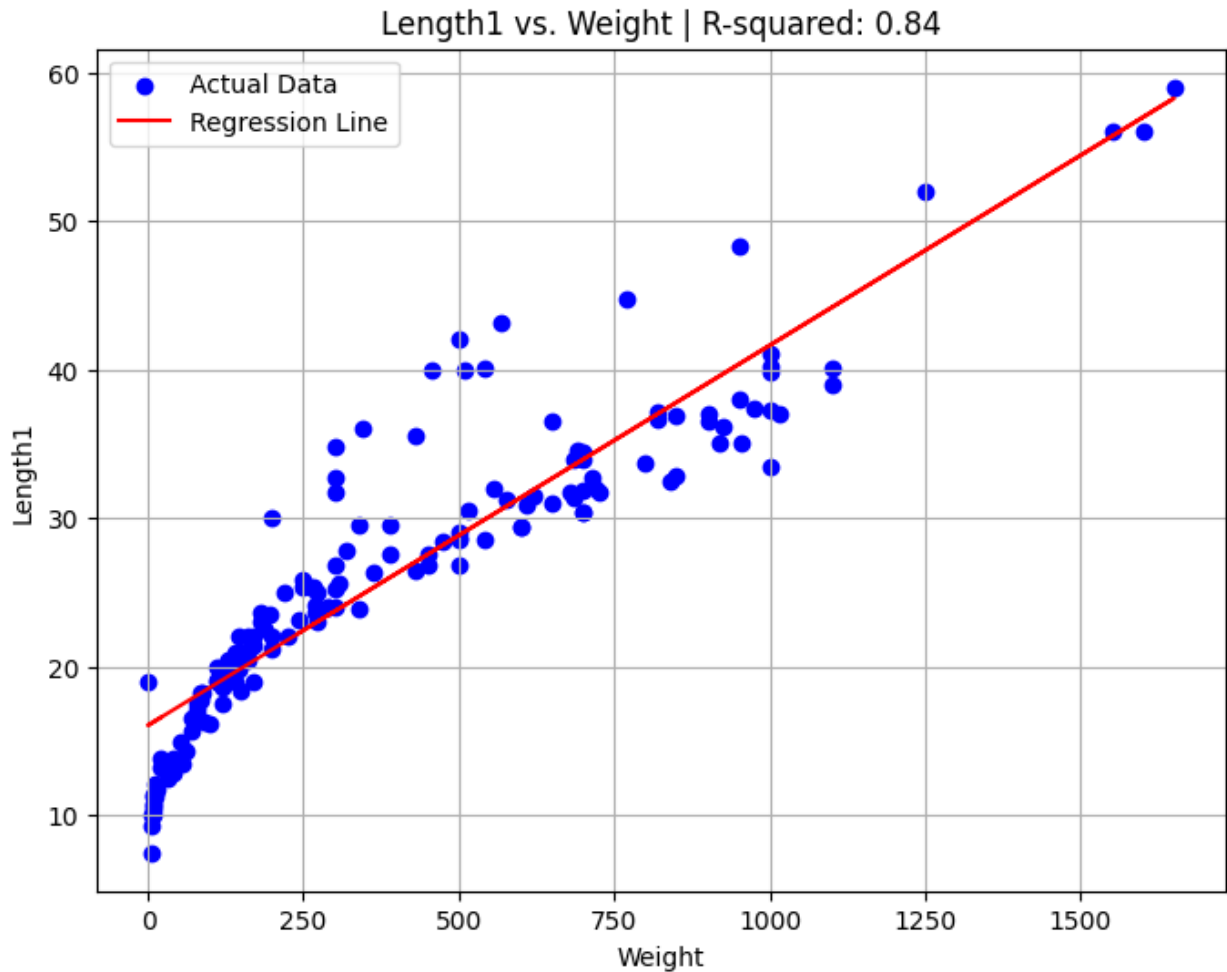
Regression for Length1 vs. Length3: R-squared = 0.9841



Regression for Length1 vs. Height: R-squared = 0.3911



Regression for Length1 vs. Width: R-squared = 0.7518



Regression for Length1 vs. Weight: R-squared = 0.8385

Summary of R-squared Values and Observed Relationships

R-squared Values for 'Weight' as Dependent Variable:

- **Weight vs. Length1:** R-squared = 0.8385
- **Weight vs. Length2:** R-squared = 0.8439
- **Weight vs. Length3:** R-squared = 0.8520
- **Weight vs. Height:** R-squared = 0.5247
- **Weight vs. Width:** R-squared = 0.7859

R-squared Values for 'Length1' as Dependent Variable:

- **Length1 vs. Length2:** R-squared = 0.9990
- **Length1 vs. Length3:** R-squared = 0.9841
- **Length1 vs. Height:** R-squared = 0.3911
- **Length1 vs. Width:** R-squared = 0.7518
- **Length1 vs. Weight:** R-squared = 0.8385

```

r2_values = {
    'Weight vs. Length1': 0.8385,
    'Weight vs. Length2': 0.8439,
    'Weight vs. Length3': 0.8520,
    'Weight vs. Height': 0.5247,
    'Weight vs. Width': 0.7859,
    'Length1 vs. Length2': 0.9990,
    'Length1 vs. Length3': 0.9841,
    'Length1 vs. Height': 0.3911,
    'Length1 vs. Width': 0.7518,
    'Length1 vs. Weight': 0.8385
}

r2_df = pd.DataFrame(r2_values.items(), columns=['Regression', 'R-squared Value'])

print(r2_df.head())

```

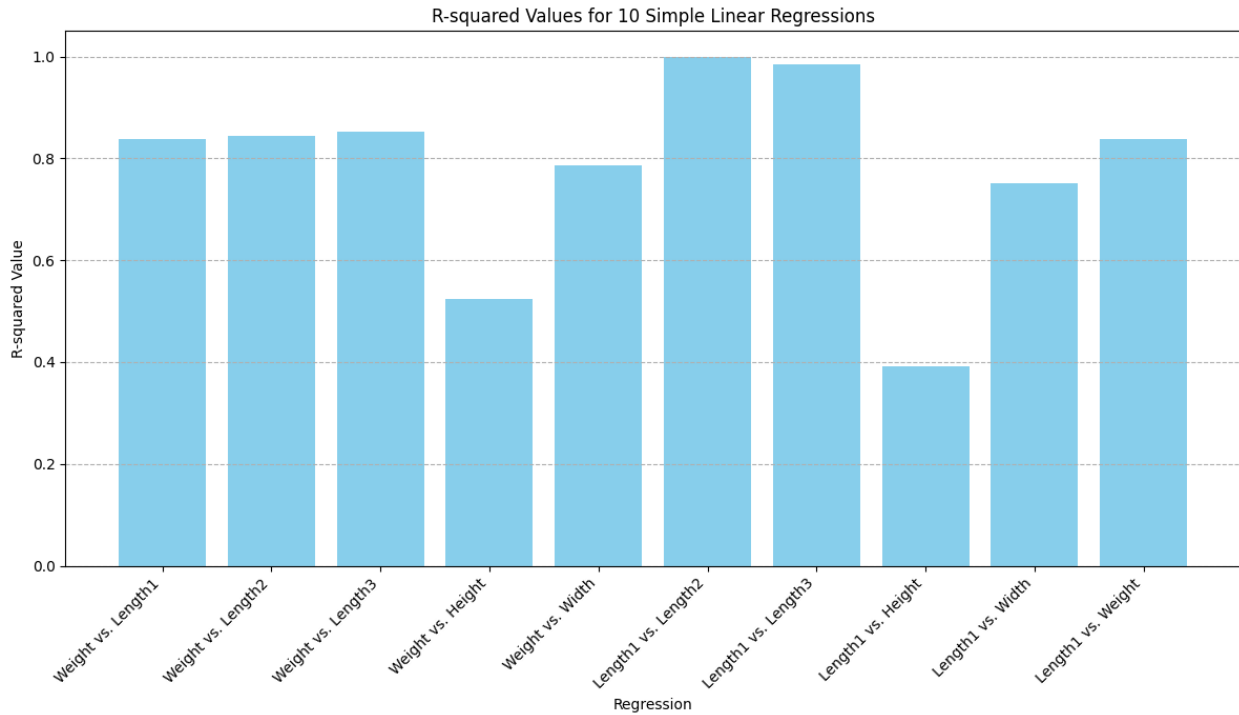
	Regression	R-squared Value
0	Weight vs. Length1	0.8385
1	Weight vs. Length2	0.8439
2	Weight vs. Length3	0.8520
3	Weight vs. Height	0.5247
4	Weight vs. Width	0.7859

```

import matplotlib.pyplot as plt

plt.figure(figsize=(12, 7))
plt.bar(r2_df['Regression'], r2_df['R-squared Value'],
color='skyblue')
plt.xlabel('Regression')
plt.ylabel('R-squared Value')
plt.title('R-squared Values for 10 Simple Linear Regressions')
plt.xticks(rotation=45, ha='right')
plt.ylim(0, 1.05) # R-squared values range from 0 to 1
plt.grid(axis='y', linestyle='--')
plt.tight_layout()
plt.show()

```



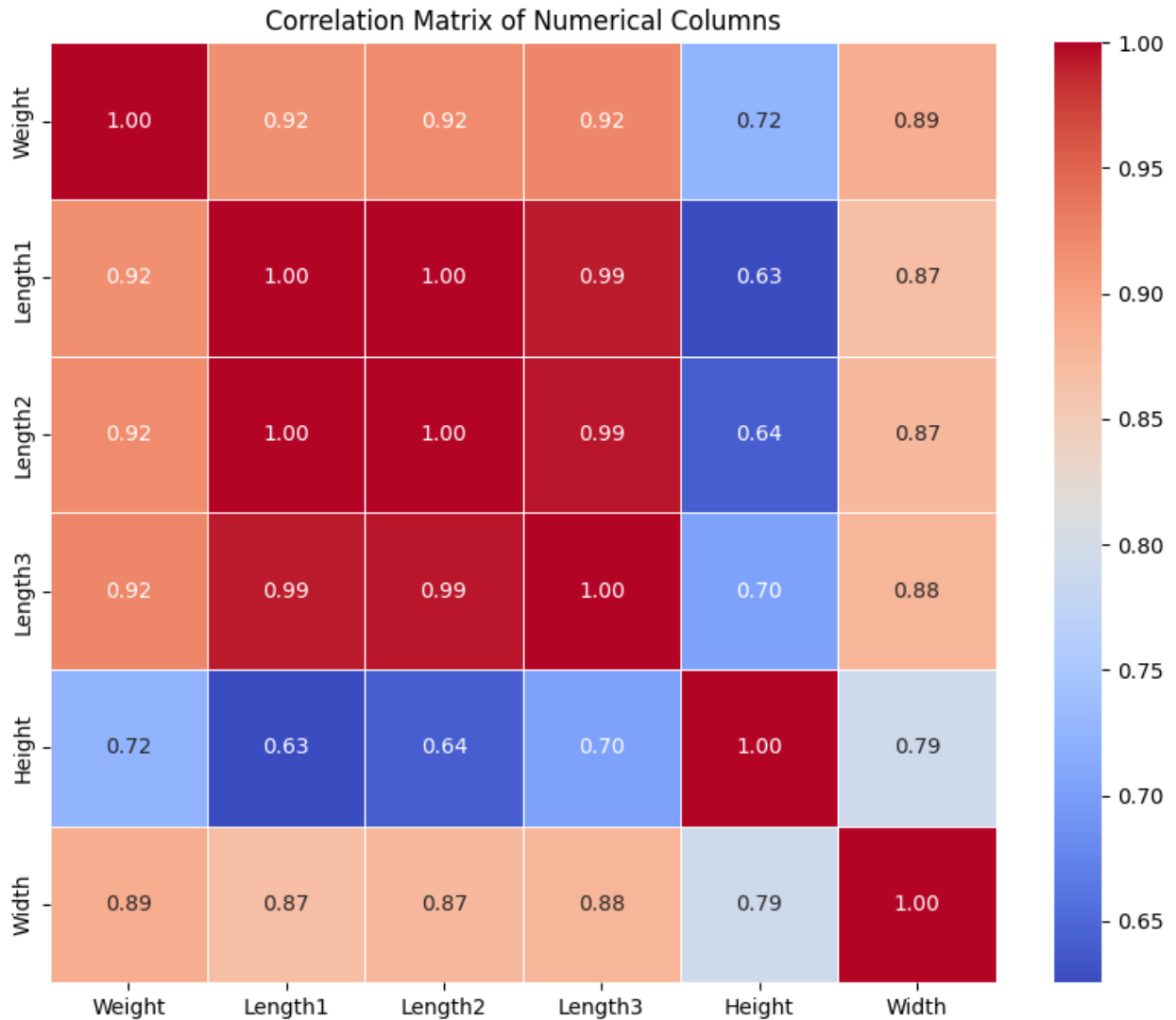
```
correlation_matrix = df.corr()
print("Correlation Matrix:")
print(correlation_matrix.round(2))
```

Correlation Matrix:

	Weight	Length1	Length2	Length3	Height	Width
Weight	1.00	0.92	0.92	0.92	0.72	0.89
Length1	0.92	1.00	1.00	0.99	0.63	0.87
Length2	0.92	1.00	1.00	0.99	0.64	0.87
Length3	0.92	0.99	0.99	1.00	0.70	0.88
Height	0.72	0.63	0.64	0.70	1.00	0.79
Width	0.89	0.87	0.87	0.88	0.79	1.00

```
import seaborn as sns
import matplotlib.pyplot as plt
```

```
plt.figure(figsize=(10, 8))
sns.heatmap(correlation_matrix, annot=True, cmap='coolwarm',
fmt=".2f", linewidths=.5)
plt.title('Correlation Matrix of Numerical Columns')
plt.show()
```



```
from sklearn.metrics import mean_squared_error, mean_absolute_error

# highest R-squared value
best_r2_regression = max(r2_values, key=r2_values.get)
best_r2_value = r2_values[best_r2_regression]

print(f"The regression with the highest R-squared is:
{best_r2_regression} (R-squared: {best_r2_value:.4f})")

# Extract dependent and independent variables for the best regression
if 'Weight vs.' in best_r2_regression:
    dependent_var = 'Weight'
    independent_var = best_r2_regression.replace('Weight vs. ', '')
elif 'Length1 vs.' in best_r2_regression:
    dependent_var = 'Length1'
    independent_var = best_r2_regression.replace('Length1 vs. ', '')
```



```

y_best = df[dependent_var]
X_best = df[[independent_var]].values.reshape(-1, 1)

# Initialize and fit the model for the best regression
best_model = LinearRegression()
best_model.fit(X_best, y_best)

# Make predictions
y_best_pred = best_model.predict(X_best)

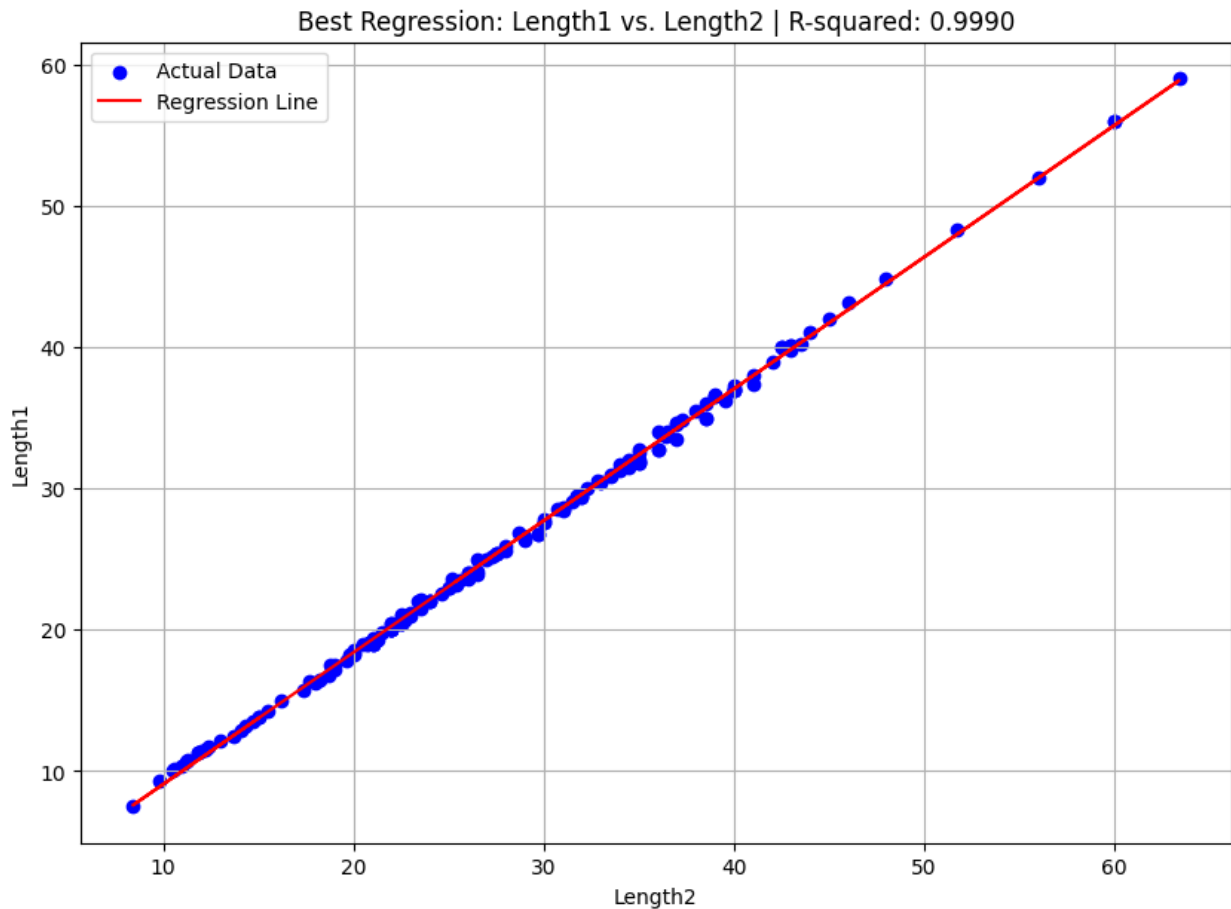
# Calculate additional metrics
mse = mean_squared_error(y_best, y_best_pred)
mae = mean_absolute_error(y_best, y_best_pred)
rmse = np.sqrt(mse) # RMSE is the square root of MSE

# Display the scatter plot for the best regression
plt.figure(figsize=(10, 7))
plt.scatter(X_best, y_best, color='blue', label='Actual Data')
plt.plot(X_best, y_best_pred, color='red', label='Regression Line')
plt.title(f'Best Regression: {dependent_var} vs. {independent_var} |  
R-squared: {best_r2_value:.4f}')
plt.xlabel(independent_var)
plt.ylabel(dependent_var)
plt.legend()
plt.grid(True)
plt.show()

# Print all metrics
print(f"\nMetrics for the best regression ({best_r2_regression}):")
print(f"  R-squared: {best_r2_value:.4f}")
print(f"  Mean Squared Error (MSE): {mse:.4f}")
print(f"  Mean Absolute Error (MAE): {mae:.4f}")
print(f"  Root Mean Squared Error (RMSE): {rmse:.4f}")

```

The regression with the highest R-squared is: Length1 vs. Length2 (R-squared: 0.9990)



Metrics for the best regression (Length1 vs. Length2):

R-squared: 0.9990

Mean Squared Error (MSE): 0.0958

Mean Absolute Error (MAE): 0.2479

Root Mean Squared Error (RMSE): 0.3096

```
import seaborn as sns
import matplotlib.pyplot as plt

# 1. Pairplot for the numerical columns of the dataset
print("Generating Pairplot for Numerical Columns:")
sns.pairplot(df[['Weight', 'Length1', 'Length2', 'Length3', 'Height',
'Width']])
plt.suptitle('Pairplot of Numerical Features', y=1.02) # Adjust
suptitle position
plt.show()

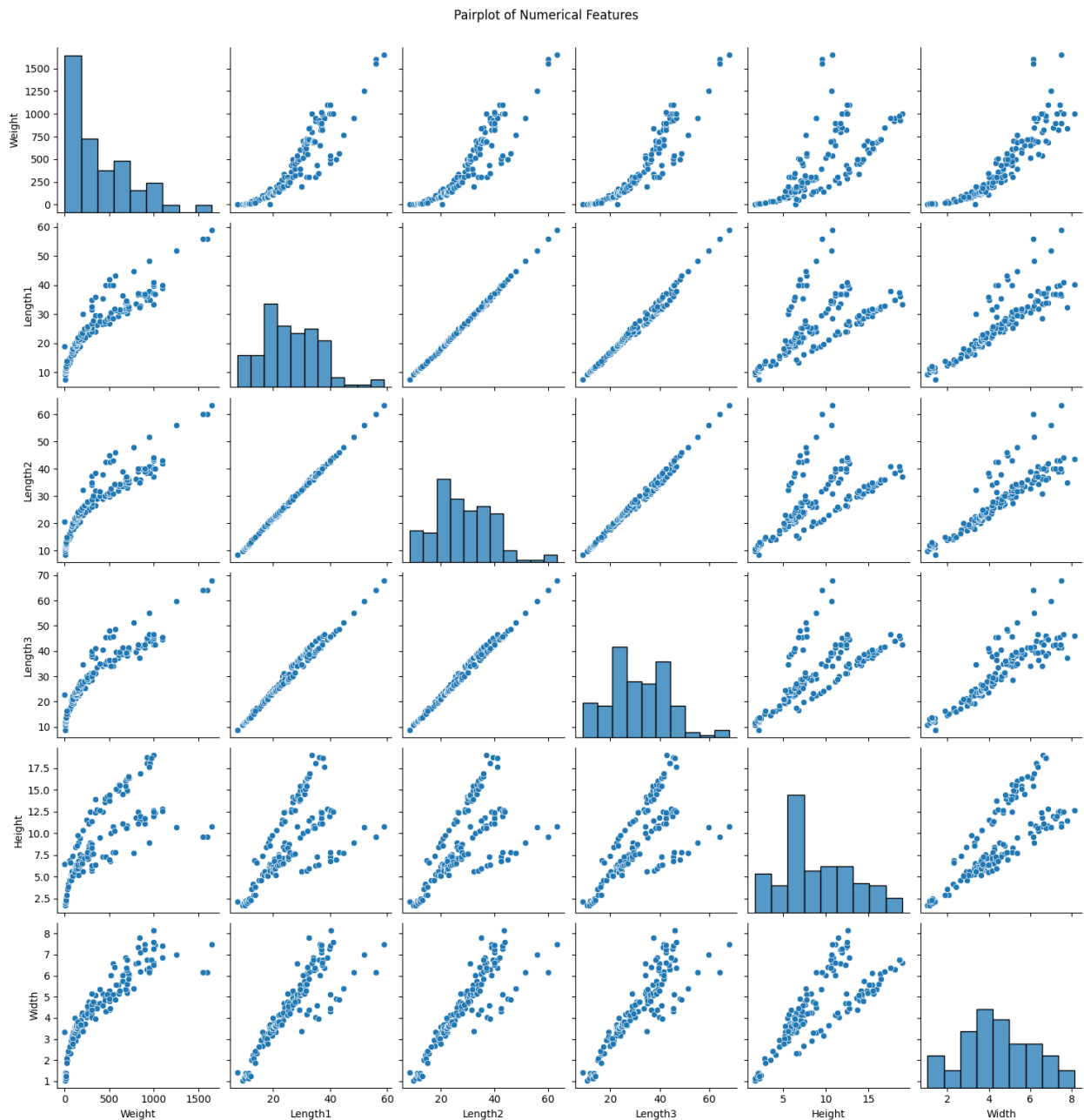
# 2. Distribution plot of residuals from the best model
# 'residuals' variable is already available from the previous best
model calculation (Length1 vs. Length2)
print("\nGenerating Distribution Plot of Residuals for the Best
```

```

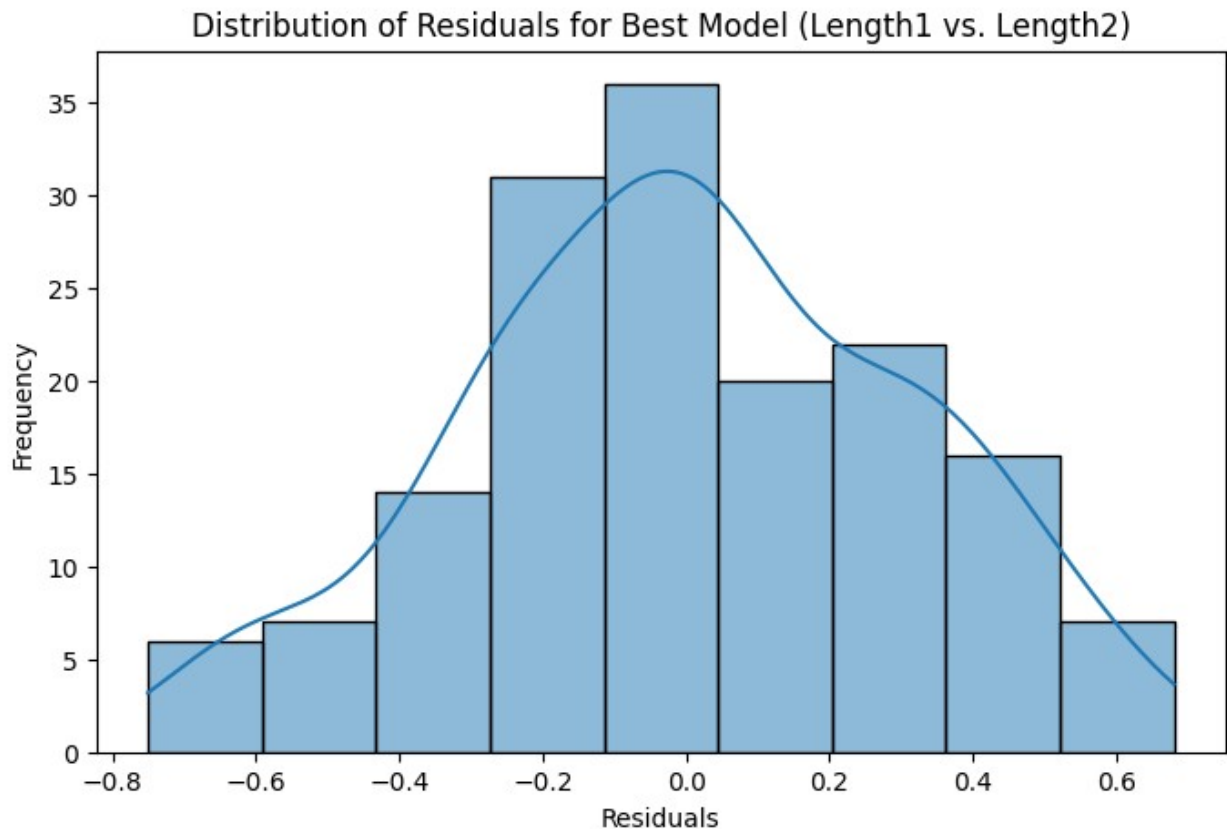
Model:")
plt.figure(figsize=(8, 5))
sns.histplot(residuals, kde=True)
plt.title('Distribution of Residuals for Best Model (Length1 vs.
Length2)')
plt.xlabel('Residuals')
plt.ylabel('Frequency')
plt.show()

```

Generating Pairplot for Numerical Columns:



Generating Distribution Plot of Residuals for the Best Model:



Summary of Simple Linear Regression Analysis

Our Findings from Simple Linear Regression:

1. **Strong Predictors for Weight:** We found that the length measurements (Length1, Length2, Length3) are very strong predictors of fish Weight, with R-squared values consistently above 0.83. This indicates that over 83% of the variance in fish weight can be explained by these individual length measurements. Width also showed a strong relationship with Weight (R-squared = 0.7859).
2. **High Correlation Among Lengths:** There is an extremely high correlation and near-perfect linear relationship among Length1, Length2, and Length3. For instance, the regression of Length1 vs. Length2 yielded an R-squared of **0.9990**, suggesting these measurements are almost interchangeable. This highlights potential multicollinearity if all were used in a multiple regression model.
3. **Weaker Role of Height:** Height proved to be a weaker predictor for both Weight (R-squared = 0.5247) and Length1 (R-squared = 0.3911) compared to the other dimensions.
4. **Best Model Performance:** The best performing simple linear regression model was Length1 vs. Length2, with an R-squared of 0.9990. Its low Mean Squared Error

(MSE: 0.0958), Mean Absolute Error (MAE: 0.2479), and Root Mean Squared Error (RMSE: 0.3096) confirm its excellent predictive accuracy.

What We Did:

1. **Data Loading and Initial Inspection:** We started by loading the `Fish[1].csv` dataset into a pandas DataFrame and displaying its initial rows.
2. **Data Preparation:** We identified and selected the numerical columns relevant for regression (`Weight`, `Length1`, `Length2`, `Length3`, `Height`, `Width`) and confirmed that there were no missing values.
3. **Simple Linear Regression Analysis:** We performed 10 simple linear regressions:
 - **Set 1:** `Weight` as the dependent variable against `Length1`, `Length2`, `Length3`, `Height`, and `Width` individually.
 - **Set 2:** `Length1` as the dependent variable against `Length2`, `Length3`, `Height`, `Width`, and `Weight` individually.
4. **Visualization of Regressions:** For each of the 10 regressions, we generated scatter plots showing the actual data points, the regression line, and the R-squared value.
5. **R-squared Comparison:** We compiled all R-squared values into a DataFrame and visualized them using a bar chart for easy comparison.
6. **Correlation Analysis:** We calculated and visualized the correlation matrix of all numerical columns using a heatmap to understand the pairwise linear relationships.
7. **Best Model Evaluation:** We programmatically identified the regression with the highest R-squared value (`Length1` vs . `Length2`). For this best model, we calculated and displayed detailed performance metrics including R-squared, Mean Squared Error (MSE), Mean Absolute Error (MAE), and Root Mean Squared Error (RMSE).
8. **Model Diagnostics:** We created a residual plot and a distribution plot of the residuals for the best model to assess the model's assumptions and the distribution of its errors.