

```
In [152]: ▶ #Import Libraries  
import pandas as pd  
import numpy as np  
import matplotlib.pyplot as plt  
import seaborn as sns  
  
from sklearn import tree, metrics, preprocessing  
from sklearn.model_selection import train_test_split  
from sklearn.naive_bayes import MultinomialNB  
from collections import defaultdict  
from sklearn.linear_model import LinearRegression  
from sklearn.preprocessing import StandardScaler, LabelEncoder  
from sklearn.metrics import precision_score, accuracy_score, recall_score, f1  
  
from dmba import liftChart , gainsChart  
from dmba import regressionSummary , classificationSummary, exhaustive_search  
  
from sklearn.neural_network import MLPClassifier
```

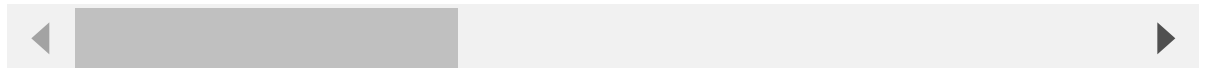
Dataset reading, data explanation and data cleaning

```
In [153]: ▶ supply_df = pd.read_csv('DataCoSupplyChainDataset.csv', encoding='latin-1')
supply_df.head(10)
```

Out[153]:

	Type	Days for shipping (real)	Days for shipment (scheduled)	Benefit per order	Sales per customer	Delivery Status	Late_delivery_risk	Ca
0	DEBIT	3	4	91.250000	314.640015	Advance shipping	0	
1	TRANSFER	5	4	-249.089996	311.359985	Late delivery	1	
2	CASH	4	4	-247.779999	309.720001	Shipping on time	0	
3	DEBIT	3	4	22.860001	304.809998	Advance shipping	0	
4	PAYMENT	2	4	134.210007	298.250000	Advance shipping	0	
5	TRANSFER	6	4	18.580000	294.980011	Shipping canceled	0	
6	DEBIT	2	1	95.180000	288.420013	Late delivery	1	
7	TRANSFER	2	1	68.430000	285.140015	Late delivery	1	
8	CASH	3	2	133.720001	278.589996	Late delivery	1	
9	CASH	2	1	132.149994	275.309998	Late delivery	1	

10 rows × 53 columns



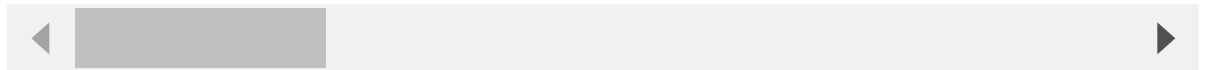
```
In [154]: ▶ #renames columns: replace spaces with _
supply_df.columns = [s.strip().replace(' ','_') for s in supply_df.columns]
```

```
supply_df.head(10)
```

Out[155]:

0	DEBIT	3	4	91.250000
1	TRANSFER	5	4	-249.089996
2	CASH	4	4	-247.779999
3	DEBIT	3	4	22.860001
4	PAYMENT	2	4	134.210007
5	TRANSFER	6	4	18.580000
6	DEBIT	2	1	95.180000
7	TRANSFER	2	1	68.430000
8	CASH	3	2	133.720001
9	CASH	2	1	132.149994

10 rows × 53 columns

[illegible]

In [157]: `df_drop.head(10)`

Out[157]:


	Days_for_shipping_(real)	Days_for_shipment_(scheduled)	Late_delivery_risk	Customer_City
0	3	4	0	Caguas
1	5	4	1	Caguas
2	4	4	0	San Jose
3	3	4	0	Los Angeles
4	2	4	0	Caguas
5	6	4	0	Tonawanda
6	2	1	1	Caguas
7	2	1	1	Miami
8	3	2	1	Caguas
9	2	1	1	San Ramon

In [158]: `df_drop.info()`

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 180519 entries, 0 to 180518
Data columns (total 8 columns):
#   Column                                Non-Null Count  Dtype
---  -
0   Days_for_shipping_(real)              180519 non-null int64
1   Days_for_shipment_(scheduled)         180519 non-null int64
2   Late_delivery_risk                    180519 non-null int64
3   Customer_City                         180519 non-null object
4   Customer_Country                     180519 non-null object
5   Order_City                           180519 non-null object
6   Order_Country                        180519 non-null object
7   Shipping_Mode                        180519 non-null object
dtypes: int64(3), object(5)
memory usage: 11.0+ MB
```

In [159]: `#Encoding of columns with data type being object`


```
le = preprocessing.LabelEncoder()
df_drop['Customer_City'] = le.fit_transform(df_drop['Customer_City'])
df_drop['Customer_Country'] = le.fit_transform(df_drop['Customer_Country'])
df_drop['Order_City'] = le.fit_transform(df_drop['Order_City'])
df_drop['Order_Country'] = le.fit_transform(df_drop['Order_Country'])
df_drop['Shipping_Mode'] = le.fit_transform(df_drop['Shipping_Mode'])
```

```
In [160]:  #Gives a summary of the data being analysed  
df_drop.describe()
```

Out[160]:

	Days_for_shipping_(real)	Days_for_shipment_(scheduled)	Late_delivery_risk	Customer_C
count	180519.000000	180519.000000	180519.000000	180519.000000
mean	3.497654	2.931847	0.548291	193.986000
std	1.623722	1.374449	0.497664	160.930000
min	0.000000	0.000000	0.000000	0.000000
25%	2.000000	2.000000	0.000000	66.000000
50%	3.000000	4.000000	1.000000	98.000000
75%	5.000000	4.000000	1.000000	324.000000
max	6.000000	4.000000	1.000000	562.000000



```
In [161]:  #creates a correlation chart for the qualitative fields  
supply_cor=df_drop.corr().round(2)  
supply_cor
```

Out[161]:

	Days_for_shipping_(real)	Days_for_shipment_(scheduled)	Late_
Days_for_shipping_(real)	1.00		0.52
Days_for_shipment_(scheduled)	0.52	1.00	
Late_delivery_risk	0.40		-0.37
Customer_City	-0.00		-0.01
Customer_Country	0.00		0.01
Order_City	0.00		-0.00
Order_Country	0.00		0.00
Shipping_Mode	0.52		0.92



In [162]: `df_drop`

Out[162]:

	Days_for_shipping_(real)	Days_for_shipment_(scheduled)	Late_delivery_risk	Customer_
0	3	4	0	
1	5	4	1	
2	4	4	0	
3	3	4	0	
4	2	4	0	
...
180514	4	4	0	
180515	3	2	1	
180516	5	4	1	
180517	3	4	0	
180518	4	4	0	

180519 rows × 8 columns



In [163]: `df_drop.info()`

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 180519 entries, 0 to 180518
Data columns (total 8 columns):
#   Column                                Non-Null Count  Dtype
---  -
0   Days_for_shipping_(real)              180519 non-null int64
1   Days_for_shipment_(scheduled)         180519 non-null int64
2   Late_delivery_risk                   180519 non-null int64
3   Customer_City                        180519 non-null int32
4   Customer_Country                    180519 non-null int32
5   Order_City                          180519 non-null int32
6   Order_Country                      180519 non-null int32
7   Shipping_Mode                       180519 non-null int32
dtypes: int32(5), int64(3)
memory usage: 7.6 MB
```

Neural Network Implementation

Selecting Predictors and Outcome

```
In [164]: outcome = 'Late_delivery_risk'
predictors = [c for c in df_drop.columns if c != outcome]
```

```
In [165]: #Data Partition with test size = 40%
X = df_drop[predictors]
y = df_drop[outcome]
train_X, valid_X, train_y, valid_y = train_test_split(X, y, test_size=0.4, ra
```

1) NN model run using most popular, one hidden layer with 1 hidden node

```
In [166]: # train neural network with 1 hidden nodes
clf = MLPClassifier(hidden_layer_sizes=(1), activation='logistic', solver='lb
clf.fit(train_X, train_y.values)
```

```
Out[166]: MLPClassifier(activation='logistic', hidden_layer_sizes=1, max_iter=1000,
random_state=1, solver='lbfgs')
```

```
In [167]: clf.predict(X)
```

```
Out[167]: array([1, 1, 1, ..., 1, 1, 1], dtype=int64)
```

```
In [168]: #NN Model Evaluation
# training performance
classificationSummary(train_y, clf.predict(train_X))

# validation performance
classificationSummary(valid_y, clf.predict(valid_X))
```

Confusion Matrix (Accuracy 0.5487)

	Prediction	
Actual	0	1
0	0 48884	
1	0 59427	

Confusion Matrix (Accuracy 0.5477)

	Prediction	
Actual	0	1
0	0 32658	
1	0 39550	

In [169]: `# Network structure`

```
print('Intercepts')
print(clf.intercepts_)

print('Weights')
print(clf.coefs_)

# Prediction

print(pd.concat([df_drop,pd.DataFrame(clf.predict_proba(X))], axis=1))
```

Intercepts

[array([-0.15443927]), array([0.19528739])]

Weights

[array([[-0.08297799],
[0.22032449],
[-0.49988562],
[-0.19766743],
[-0.35324411],
[-0.4076614],
[-0.31373979]]), array([[-0.20646505]])]

	Days_for_shipping_(real)	Days_for_shipment_(scheduled)	\
0	3	4	
1	5	4	
2	4	4	
3	3	4	
4	2	4	
...	
180514	4	4	
180515	3	2	
180516	5	4	
180517	3	4	
180518	4	4	

	Late_delivery_risk	Customer_City	Customer_Country	Order_City
\				
0	0	66	1	331
1	1	66	1	391
2	0	452	0	391
3	0	285	0	3226
4	0	66	1	3226
...
180514	0	59	0	2922
180515	1	26	0	1362
180516	1	55	0	25
180517	0	66	1	25
180518	0	66	1	2203

	Order_Country	Shipping_Mode	0	1
0	70	3	0.451333	0.548667
1	69	3	0.451333	0.548667
2	69	3	0.451333	0.548667
3	8	3	0.451333	0.548667
4	8	3	0.451333	0.548667


```

...
180514      31      3  0.451333  0.548667
180515      77      2  0.451333  0.548667
180516       8      3  0.451333  0.548667
180517       8      3  0.451333  0.548667
180518      69      3  0.451333  0.548667

```

[180519 rows x 10 columns]

In [170]: `clf.predict(X)`

Out[170]: `array([1, 1, 1, ..., 1, 1, 1], dtype=int64)`

In [171]: `#NN Model Evaluation`
`# training performance`
`classificationSummary(train_y, clf.predict(train_X))`

`# validation performance`
`classificationSummary(valid_y, clf.predict(valid_X))`

Confusion Matrix (Accuracy 0.5487)

	Prediction	
Actual	0	1
0	0 48884	
1	0 59427	

Confusion Matrix (Accuracy 0.5477)

	Prediction	
Actual	0	1
0	0 32658	
1	0 39550	

2) NN Model Run using - Midway between input and output layers - 4 nodes (1HL + 4 nodes)

In [172]: `# train neural network with 4 hidden nodes`
`clf = MLPClassifier(hidden_layer_sizes=(4), activation='logistic', solver='lb`
`clf.fit(train_X, train_y.values)`

Out[172]: `MLPClassifier(activation='logistic', hidden_layer_sizes=4, max_iter=1000,`
`random_state=1, solver='lbfgs')`

In [173]: `clf.predict(X)`

Out[173]: `array([1, 1, 1, ..., 1, 1, 1], dtype=int64)`

```
In [174]: ▶ #NN Model Evaluation  
# training performance  
classificationSummary(train_y, clf.predict(train_X))  
  
# validation performance  
classificationSummary(valid_y, clf.predict(valid_X))
```

Confusion Matrix (Accuracy 0.5489)

	Prediction	
Actual	0	1
0	304 48580	
1	282 59145	

Confusion Matrix (Accuracy 0.5472)

	Prediction	
Actual	0	1
0	163 32495	
1	204 39346	

In [175]: `# Network structure`

```
print('Intercepts')
print(clf.intercepts_)

print('Weights')
print(clf.coefs_)

# Prediction

print(pd.concat([df_drop, pd.DataFrame(clf.predict_proba(X))], axis=1))
```

Intercepts

```
[array([-0.28141245,  0.32248063, -0.34251368, -0.06639009]), array([0.19503204])]
```

Weights

```
[array([[ -0.01207942,  0.18789204, -0.42626937, -0.19190578],
        [ -0.3421372 , -0.34765781, -0.26754279, -0.10656541],
        [  0.00720763,  0.03306329, -0.06849163,  0.08155611],
        [ -0.25341969,  0.32245875, -0.40304458,  0.14681218],
        [ -0.21381403,  0.05004637, -0.30667889, -0.31062711],
        [  0.23248867,  0.39933333, -0.15907733,  0.24068873],
        [  0.29008214,  0.33651878, -0.35387732, -0.37312586]]), array([[
0.26694911],
        [ 0.00137467],
        [ 0.24278099],
        [-0.23761444]])]
```

	Days_for_shipping_(real)	Days_for_shipment_(scheduled) \
0	3	4
1	5	4
2	4	4
3	3	4
4	2	4
...
180514	4	4
180515	3	2
180516	5	4
180517	3	4
180518	4	4

	Late_delivery_risk	Customer_City	Customer_Country	Order_City
\				
0	0	66	1	331
1	1	66	1	391
2	0	452	0	391
3	0	285	0	3226
4	0	66	1	3226
...
180514	0	59	0	2922
180515	1	26	0	1362
180516	1	55	0	25
180517	0	66	1	25
180518	0	66	1	2203

	Order_Country	Shipping_Mode	0	1
0	70	3	0.451056	0.548944

1	69	3	0.451056	0.548944
2	69	3	0.451056	0.548944
3	8	3	0.451056	0.548944
4	8	3	0.451056	0.548944
...
180514	31	3	0.451056	0.548944
180515	77	2	0.451056	0.548944
180516	8	3	0.450919	0.549081
180517	8	3	0.454428	0.545572
180518	69	3	0.451056	0.548944

[180519 rows x 10 columns]

In [176]: `clf.predict(X)`

Out[176]: `array([1, 1, 1, ..., 1, 1, 1], dtype=int64)`

In [177]: `#NN Model Evaluation`
`# training performance`
`classificationSummary(train_y, clf.predict(train_X))`

`# validation performance`
`classificationSummary(valid_y, clf.predict(valid_X))`

Confusion Matrix (Accuracy 0.5489)

	Prediction	
Actual	0	1
0	304 48580	
1	282 59145	

Confusion Matrix (Accuracy 0.5472)

	Prediction	
Actual	0	1
0	163 32495	
1	204 39346	

3) NN model run using - Less than 2X the input nodes = [12 < 14 (2*7) nodes] [1 HL + 12 nodes]

In [178]: `# train neural network with 12 hidden nodes`
`clf = MLPClassifier(hidden_layer_sizes=(12), activation='logistic', solver='lbfgs')`
`clf.fit(train_X, train_y.values)`

Out[178]: `MLPClassifier(activation='logistic', hidden_layer_sizes=12, max_iter=1000, random_state=1, solver='lbfgs')`

In [179]: `clf.predict(X)`

Out[179]: `array([0, 1, 0, ..., 1, 0, 0], dtype=int64)`

```
In [180]: ► #NN Model Evaluation  
# training performance  
classificationSummary(train_y, clf.predict(train_X))  
  
# validation performance  
classificationSummary(valid_y, clf.predict(valid_X))
```

Confusion Matrix (Accuracy 0.9756)

	Prediction	
Actual	0	1
0	46243	2641
1	0	59427

Confusion Matrix (Accuracy 0.9753)

	Prediction	
Actual	0	1
0	30876	1782
1	0	39550

In [181]: `# Network structure`

```
print('Intercepts')
print(clf.intercepts_)

print('Weights')
print(clf.coefs_)

# Prediction

print(pd.concat([df_drop, pd.DataFrame(clf.predict_proba(X))], axis=1))
```

Intercepts

```
[array([-1.09814394e-04,  3.34981375e-01, -8.12853508e-02,  3.41051254e-01,
        1.05940525e-01,  4.88013057e-02, -4.03912945e-01,  3.02632189e-01,
        -3.24695183e-02,  5.30223197e-02, -6.27318052e-02, -7.42228428e-02]), array([-2.47954353])]
```

Weights

```
[array([[ 4.90204059e+00, -1.75021186e+00, -6.82621840e-01,
        -2.34211534e+00, -2.29435500e-01, -1.58898249e+00,
         7.68066858e+00, -8.42654572e-02, -6.69157956e-02,
         2.43529923e+00, -5.76275624e-02,  1.97493442e+01],
        [-3.99604001e+00,  2.61274480e+00, -6.50837636e-02,
         1.94308788e+00, -5.37738760e-02,  9.60045358e-01,
        -8.60982386e+00, -1.12404309e-01,  1.95091603e-01,
        -1.19611297e+00, -1.17413789e-01, -1.39600120e+01],
        [-5.48617010e+00, -4.62890440e-01, -2.89374759e+00,
         2.16790896e+00, -2.16890503e-01,  3.02136884e+00,
        -2.47502336e+00,  8.36567781e-01,  2.98115964e-01,
         2.74719388e-01,  1.06548712e-01, -2.85099112e-03],
        [ 1.81814629e-01,  2.79352858e-01, -2.35278446e-01,
         1.94911667e-01,  3.17189958e-01,  1.28885252e-01,
        -1.00812127e-01,  2.24324279e-01, -2.57440258e-01,
        -1.12088148e-01,  2.66692493e-01,  6.71785944e-03],
        [-5.53293479e+00, -3.69017639e-01,  7.42013604e-01,
         3.86170675e+00, -1.87078145e-01,  6.03587346e+00,
         4.76169872e-01, -4.26520288e-01,  4.68160943e-02,
        -3.07265527e+00,  1.11978716e-01,  2.92141399e-03],
        [ 1.22404150e+00, -2.78886244e+00, -1.21751089e+00,
        -6.01109845e-02, -2.92224215e-01,  1.41960026e+00,
         3.85213122e+00, -8.25661524e-01,  2.88405586e-01,
         1.90437301e+00,  2.61485852e-01, -3.42501327e-03],
        [-3.61000762e+00,  2.14536191e+00,  1.52954237e-01,
         1.36456289e+00,  2.77377949e-01,  7.08617575e-01,
        -6.52020254e+00,  2.08217272e-01,  2.48629655e-01,
        -1.13367296e+00,  1.69561173e-01, -1.21959700e+01]])], array([[1
5.3477442 ],
        [-8.01615555],
        [ 0.1868243 ],
        [-1.71493353],
        [-0.13513713],
        [-0.92380687],
        [-0.34239364],
        [-0.2799659 ]],
```

```

[-2.30891622],
[ 0.40786926],
[-3.01973076],
[13.72146452]]])
Days_for_shipping_(real) Days_for_shipment_(scheduled) \
0 3 4
1 5 4
2 4 4
3 3 4
4 2 4
...
180514 4 4
180515 3 2
180516 5 4
180517 3 4
180518 4 4

Late_delivery_risk Customer_City Customer_Country Order_City
\
0 0 66 1 331
1 1 66 1 391
2 0 452 0 391
3 0 285 0 3226
4 0 66 1 3226
...
180514 0 59 0 2922
180515 1 26 0 1362
180516 1 55 0 25
180517 0 66 1 25
180518 0 66 1 2203

Order_Country Shipping_Mode 0 1
0 70 3 0.999979 0.000021
1 69 3 0.042858 0.957142
2 69 3 0.999978 0.000022
3 8 3 0.999975 0.000025
4 8 3 0.999975 0.000025
...
180514 31 3 0.999973 0.000027
180515 77 2 0.042347 0.957653
180516 8 3 0.049034 0.950966
180517 8 3 0.999978 0.000022
180518 69 3 0.999975 0.000025

[180519 rows x 10 columns]

```

In [182]: `clf.predict(X)`

Out[182]: `array([0, 1, 0, ..., 1, 0, 0], dtype=int64)`

```
In [183]: # NN Model Evaluation
# training performance
classificationSummary(train_y, clf.predict(train_X))

# validation performance
classificationSummary(valid_y, clf.predict(valid_X))
```

Confusion Matrix (Accuracy 0.9756)

	Prediction	
Actual	0	1
0	46243	2641
1	0	59427

Confusion Matrix (Accuracy 0.9753)

	Prediction	
Actual	0	1
0	30876	1782
1	0	39550

4) Hidden layer = 2/3 input nodes + output nodes = (2/3)*(7)+1 = 6 nodes [1HL + 6 Nodes]

```
In [184]: # train neural network with 6 hidden nodes
clf = MLPClassifier(hidden_layer_sizes=(6), activation='logistic', solver='lbfgs')
clf.fit(train_X, train_y.values)
```

Out[184]: MLPClassifier(activation='logistic', hidden_layer_sizes=6, max_iter=1000, random_state=1, solver='lbfgs')

```
In [191]: # clf.predict([[1,1,1,0,0,1,0]]).round(2)
```

C:\Users\kadam\anaconda3\lib\site-packages\sklearn\base.py:450: UserWarning: X does not have valid feature names, but MLPClassifier was fitted with feature names
warnings.warn(

Out[191]: array([0], dtype=int64)


```
In [192]: ► #NN Model Evaluation  
# training performance  
classificationSummary(train_y, clf.predict(train_X))  
  
# validation performance  
classificationSummary(valid_y, clf.predict(valid_X))
```

Confusion Matrix (Accuracy 0.9756)

	Prediction	
Actual	0	1
0	46243	2641
1	0	59427

Confusion Matrix (Accuracy 0.9753)

	Prediction	
Actual	0	1
0	30876	1782
1	0	39550

In [187]: `# Network structure`

```
print('Intercepts')
print(clf.intercepts_)

print('Weights')
print(clf.coefs_)

# Prediction

print(pd.concat([df_drop,pd.DataFrame(clf.predict_proba(X))], axis=1))
```

Intercepts

```
[array([-0.14237831,  0.23479887,  0.40143298, -0.02168071, -0.5127101
        0.17603056]), array([3.8075808])]
```

Weights

```
[array([[ -8.03214864e-01,  2.39485041e-01,  3.20953437e+00,
        -3.10291160e+00, -5.69275097e+00, -7.70366086e+00],
        [ 1.22365119e+00, -1.49702632e-01,  4.02506696e-01,
         3.91619511e+00,  6.01058456e+00,  8.04861297e+00],
        [-4.11261267e+00,  7.25617867e-01,  2.70577460e+01,
        -1.17084881e+01,  7.04913688e-04,  3.89723598e+01],
        [-1.52117329e-01, -2.41030685e-01,  4.71131834e-01,
         5.01912727e-01,  1.93130244e-03,  3.58334768e-01],
        [-1.56234709e+01,  5.95750490e-03,  7.53289802e+00,
        -2.13250692e+00,  6.47314875e-05,  2.21319253e+01],
        [-6.75820774e+00,  1.21578245e-01,  3.65908727e+01,
        -8.37482260e+00, -1.84128238e-03,  3.16439060e+01],
        [ 1.37339671e+00,  2.46259874e-01,  2.68407584e-01,
         3.28626274e+00, -5.63934288e-01,  6.63229412e+00]]), array([[
34.37576706],
        [ 3.44898489],
        [-36.04397664],
        [ 13.33885204],
        [-48.23071457],
        [ 31.96336326]])]
```

	Days_for_shipping_(real)	Days_for_shipment_(scheduled)	\
0	3	4	
1	5	4	
2	4	4	
3	3	4	
4	2	4	
...	
180514	4	4	
180515	3	2	
180516	5	4	
180517	3	4	
180518	4	4	

	Late_delivery_risk	Customer_City	Customer_Country	Order_City
\				
0	0	66	1	331
1	1	66	1	391
2	0	452	0	391
3	0	285	0	3226

4	0	66	1	3226
...
180514	0	59	0	2922
180515	1	26	0	1362
180516	1	55	0	25
180517	0	66	1	25
180518	0	66	1	2203

	Order_Country	Shipping_Mode	0	1
0	70	3	1.000000	4.184614e-20
1	69	3	0.042476	9.575241e-01
2	69	3	0.999997	3.195359e-06
3	8	3	1.000000	3.574326e-20
4	8	3	1.000000	2.712939e-20
...
180514	31	3	0.999995	5.042623e-06
180515	77	2	0.042347	9.576526e-01
180516	8	3	0.042678	9.573216e-01
180517	8	3	1.000000	4.025368e-20
180518	69	3	0.999984	1.552996e-05

[180519 rows x 10 columns]

In [193]: `clf.predict([[1,0,1,0,0,1,0]]).round(2)`

C:\Users\kadam\anaconda3\lib\site-packages\sklearn\base.py:450: UserWarning: X does not have valid feature names, but MLPClassifier was fitted with feature names
warnings.warn(

Out[193]: `array([1], dtype=int64)`

In [194]: `#NN Model Evaluation`
`# training performance`
`classificationSummary(train_y, clf.predict(train_X))`

`# validation performance`
`classificationSummary(valid_y, clf.predict(valid_X))`

Confusion Matrix (Accuracy 0.9756)

	Prediction	
Actual	0	1
0	46243	2641
1	0	59427

Confusion Matrix (Accuracy 0.9753)

	Prediction	
Actual	0	1
0	30876	1782
1	0	39550

Conclusion : Highest accuracy results (out of these 4 NN model runs using different hidden nodes) are obtained with 14 hidden nodes (3rd run - hidden layers = Less than 2X the input

nodes) layers and 6 hidden nodes (4th run - hidden layers = $\frac{2}{3}$ input nodes + output nodes)
[Both the results are same]

In []: ▶