

C O Tutorial 4

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Sol-1

Program	time on M ₁	time on M ₂
1	2.0	1.5
2	5.0	10.8

① For program 1

$$(\text{performance of } M_1) = \frac{1}{2.0} = 0.5$$

$$\text{performance of } M_2 = \frac{1}{1.5} = 0.666$$

M₂ is faster to M₁ by n

$$n = \frac{\text{execution times } M_1}{\text{execution times } M_2} = \frac{2}{1.5} = 1.33$$

② for M₁ is faster by n

$$n = \frac{\text{execution time } M_2}{\text{execution time } M_1}$$

$$= \frac{10}{5} = 2.0$$

Sol-2 ① CPU execute time A

$$= \frac{\text{CPU clock cycles A}}{\text{clock rate A}}$$

~~Sol-2~~ = 12 sec = $\frac{\text{CPU clock cycles}}{5 \text{ GHz}}$

CPU clock cycles A = 60 G Cycles

② CPU execute time B

$$= 1.2 \times \frac{\text{CPU clock cycles A}}{\text{clock rate B}}$$

$$\Rightarrow 10 \text{ sec} = \frac{1.2 \times 60 \text{ G Cycles}}{\text{clock rate B}}$$

$$\text{CPU rate B} = \frac{72}{10} = 7.2 \text{ GHz}$$

so desired rate is 7.2 GHz

Sol-3

Comp A \rightarrow 250 ps clock cycle time
CPI 3.0 for some program

Comp B \rightarrow 500 ps clock cycle time
CPI 2.2 for same program

I = no. of instructions for program

$$\text{CPU clock cycles}_A = I \times 3.0$$

$$\text{CPU clock cycles}_B = I \times 2.2$$

Now we can compute CPU time for each computer

$$\text{CPU time}_A = \text{CPU clock cycles}_A \times \text{clock cycle time}$$

$$= I \times 3.0 \times 250 \text{ ps} = 750 I \text{ ps}$$

likewise for B

$$\text{CPU time}_B = I \times 2.2 \times 500 = 1100 I \text{ ps}$$

Clearly A is faster. The amount faster is given by ratio of execution times.

$$\frac{\text{CPU performance}_A}{\text{CPU performance}_B} = \frac{\text{Execution time}_B}{\text{Execution time}_A}$$

$$= \frac{1100 I \text{ ps}}{750 I \text{ ps}} = 1.466$$

A is 1.466 times faster than B

Sol-4:- $\text{CPU clock cycles} = \sum_{i=1}^n (\text{CPI}_i \times \text{Instruction count})$

$$\begin{aligned} (\text{CPU clock cycles})_1 &= (6 \times 2 + 1 \times 1 + 2 \times 4) \times 10^9 \\ &= (12 + 1 + 8) \times 10^9 \\ &= 21 \times 10^9 \end{aligned}$$

$$\begin{aligned} (\text{CPU clock cycles})_2 &= (12 \times 2 + 2 \times 1 + 1 \times 4) \times 10^9 \\ &= (24 + 2 + 4) \times 10^9 \\ &= 30 \times 10^9 \end{aligned}$$

$\text{Execution time} = \frac{\text{CPU clock cycle}}{\text{clock rate}}$

$$(\text{Ex. time})_1 = \frac{21 \times 10^9}{700 \times 10^6} = 30 \text{ sec}$$

$$(\text{Ex. time})_2 = \frac{30 \times 10^9}{700 \times 10^6} = 42.85 \text{ sec}$$

Compiler 1 generates faster program

$$\text{MIPS} = \frac{\text{Instruction count}}{\text{Execution time} \times 10^6}$$

$$(\text{MIPS})_1 = \frac{(6 + 1 + 2) \times 10^9}{30 \times 10^6} = 300$$

$$(\text{MIPS})_2 = \frac{(12 + 2 + 1) \times 10^9}{42.85 \times 10^6} = 350.05$$

thus Compiler 2 or ~~MIPS~~ MIPS_2 has higher MIPS rating but compiler 1 runs faster

⑤ Amdahl's law:

It is named after computer scientist Gene Amdahl (IBM). also known as Amdahl's argument. It is formula which gives the theoretical speedup in latency of the execution of a task at a fixed workload that can be expected of a system whose resources are improved. It's formula for finding maximum improvement possible by just improving particular part of system.

$$\text{Speedup} = \frac{P_e \text{ (Performance with enhancement)}}{P_w \text{ (Performance without enhancement)}}$$

$$= \frac{E_w \text{ (execution without enhancement)}}{E_e \text{ (execution with enhancement)}}$$

$$S = \frac{1}{(1 - f_{\text{enhanced}}) + \frac{\text{Fraction enhanced}}{\text{Speedup enhancement}}}$$

$$S = \frac{1}{1 - f + \frac{f}{F}}$$

examples:- ① FP Instruction improved to run 2x as fast but only 10% of all executed instruction order

$$S = \frac{1}{1 - 0.1 + \frac{0.1}{2}} = 1.053$$

② we want overall speedup of 2, FP instruction by 4x find FP instruction fraction

$$S = \frac{1}{1 - f + \frac{f}{F}} = 2 = \frac{1}{1 - f + \frac{f}{4}} \Rightarrow \boxed{f = 0.667}$$