

☐ Agenda

- Encoder
- Decoder
- Multiplexer
- Demultiplexer

☐ Introduction

- In a digital system, discrete quantities of information are represented with binary codes. Binary code of N digits can be used to store 2^N distinct elements of coded information.
- This is what encoders and decoders are used for. **Encoders** convert 2^N lines of input into a code of N bits and **Decoders** decode the N bits into 2^N lines.
- A binary code of n bits can represent up to 2ⁿ distinct elements of the coded information.

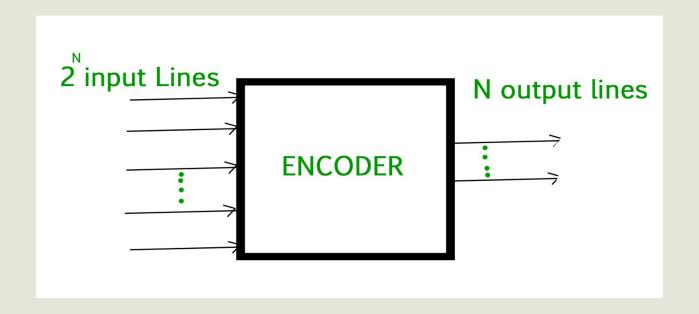
Encoder

- An Encoder is a device that converts the active data signal into a coded message format or it is a device that converts analogue signal to digital signals.
- It is a combinational circuit, that converts binary information in the form of a 2N input lines into N output lines which represent N bit code for the input.
- When an input signal is applied to an encoder then logic circuitry involved within it converts that particular input into coded binary output.

Encoder

- An Encoder is a **combinational circuit** that performs the reverse operation of Decoder.
- It has maximum of **2^n input lines** and **'n' output lines**, hence it encodes the information from 2^n inputs into an n-bit code.
- It will produce a binary code equivalent to the input. Therefore, the encoder encodes 2^n input lines with 'n' bits.
- The encoders and decoders play an essential role in digital electronics projects; encoders & decoders are used to convert data from one form to another form.

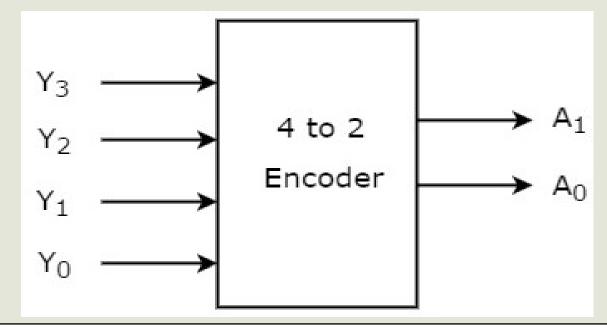
These are frequently used in communication system such as telecommunication, networking, etc. to transfer data from one end to the other end.



4 to 2 Encoder

• 4 to 2 Encoder has four inputs Y_3 , Y_2 , Y_1 & Y_0 and two outputs A_1 & A_0 . The **block diagram** of 4 to 2 Encoder is shown in the

following figure.



• At any time, only one of these 4 inputs can be '1' in order to get the respective binary code at the output. The **Truth table** of 4 to 2 encoder is shown below.

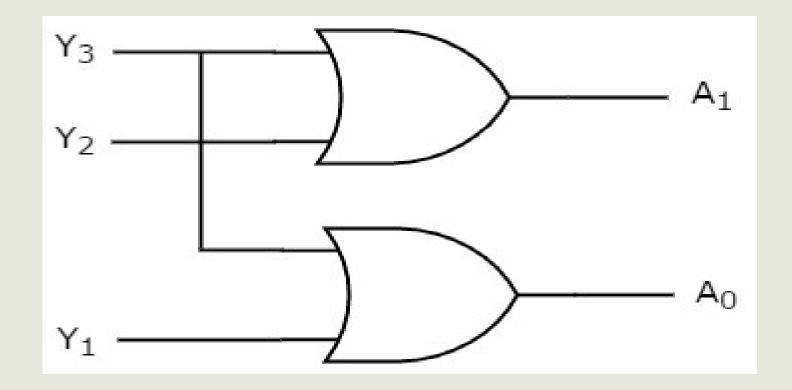
	Inp	Out	puts		
Y3	Y ₂	Y ₁	Y ₀	A_1	A ₀
0	0	0	1	0	0
0	0	1	0	0	1
0	1	0	0	1	0
1	0	0	0	1	1

From Truth table, we can write the Boolean functions for each output as

$$A_1 = Y_3 + Y_2$$

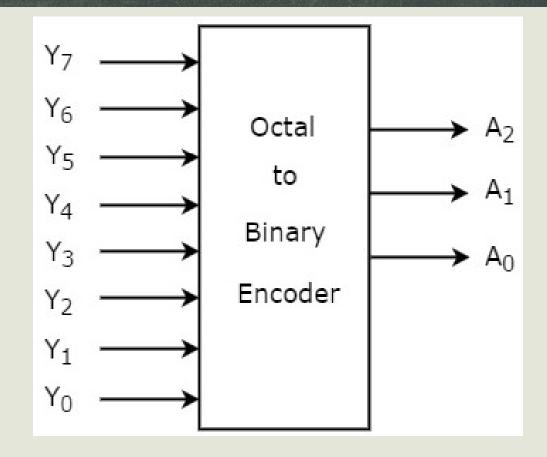
$$A_0 = Y_3 + Y_1$$

We can implement the above two Boolean functions by using two input OR gates. The **circuit diagram** of 4 to 2 encoder is shown in the following figure.



Octal to Binary Encoder

Octal to binary Encoder has eight inputs, Y₇ to Y₀ and three outputs A₂, A₁ & A₀.
Octal to binary encoder is nothing but 8 to 3 encoder.
The **block diagram** of octal to binary Encoder is shown in the following figure.



At any time, only one of these eight inputs can be '1' in order to get the respective binary code. The **Truth table** of octal to binary encoder is shown below.

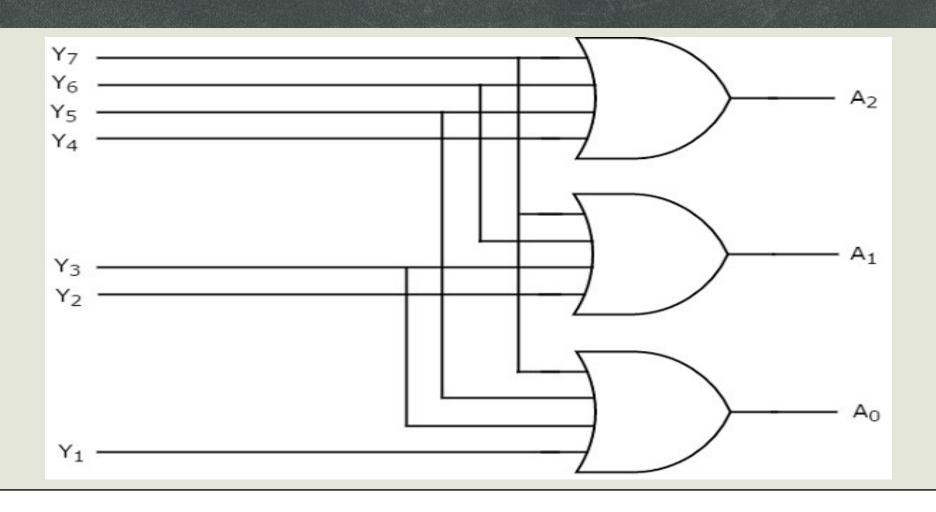
			Inp	outs				Outputs			
Y7	Y ₆	Y ₅	Y4	Y3	Y ₂	Y ₁	Yo	A ₂	A ₁	A ₀	
0	0	0	0	0	0	0	1	0	0	0	
0	0	0	0	0	0	1	0	0	0	1	
0	0	0	0	0	1	0	0	0	1	0	
0	0	0	0	1	0	0	0	0	1	1	
0	0	0	1	0	0	0	0	1	0	0	
0	0	1	0	0	0	0	0	1	0	1	
0	1	0	0	0	0	0	0	1	1	0	
1	0	0	0	0	0	0	0	1	1	1	

From Truth table, we can write the Boolean functions for each output as

$$A_2 = Y_7 + Y_6 + Y_5 + Y_4$$

$$A_1 = Y_7 + Y_6 + Y_3 + Y_2$$

$$A_0 = Y_7 + Y_5 + Y_3 + Y_1$$



Drawbacks of Encoder

- There is an ambiguity, when all outputs of encoder are equal to zero. Because, it could be the code corresponding to the inputs, when only least significant input is one or when all inputs are zero.
- If more than one input is active High, then the encoder produces an output, which may not be the correct code.
- For **example**, if both Y_3 and Y_6 are '1', then the encoder produces 111 at the output. This is neither equivalent code corresponding to Y_3 , when it is '1' nor the equivalent code corresponding to Y_6 , when it is '1'.

- So, to overcome these difficulties, we should assign priorities to each input of encoder.
- Then, the output of encoder will be the (binary) code corresponding to the active High input(s), which has higher priority.
- This encoder is called as **priority encoder**.

Priority Encoder

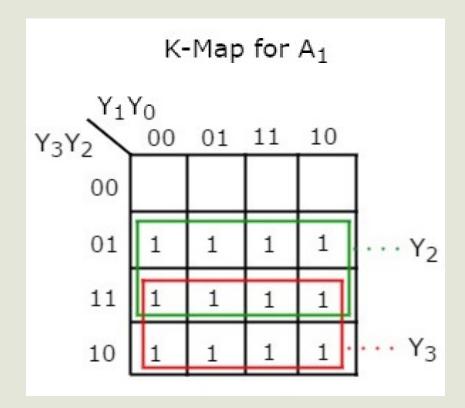
- A 4 to 2 priority encoder has four inputs Y_3 , Y_2 , Y_1 & Y_0 and two outputs A_1 & A_0 .
- Here, the input, Y_3 has the highest priority, whereas the input, Y_0 has the lowest priority.
- In this case, even if more than one input is '1' at the same time, the output will be the (binary) code corresponding to the input, which is having **higher priority**.

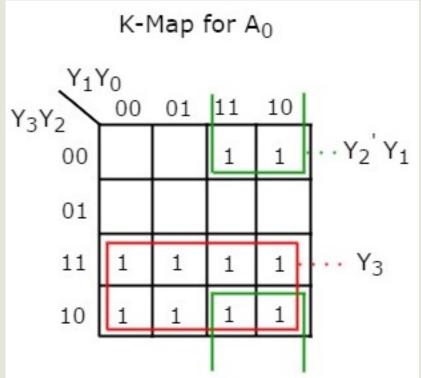
- We considered one more **output**, **V** in order to know, whether the code available at outputs is valid or not.
 - If at least one input of the encoder is '1', then the code available at outputs is a valid one. In this case, the output, V will be equal to 1.
 - If all the inputs of encoder are '0', then the code available at outputs is not a valid one. In this case, the output, V will be equal to 0.

• **Truth table** of 4 to 2 priority encoder is shown below.

	Inp	outs		Outputs			
Y 3	Y ₂	Υ ₁	Yo	A ₁	A ₀	V	
0	0	0	0	0	0	0	
0	0	0	1	0	0	1	
0	0	1	х	0	1	1	
0	1	х	x	1	0	1	
1	x	X	X	1	1	1	

Use 4 variable K-maps for getting simplified expressions for each output.





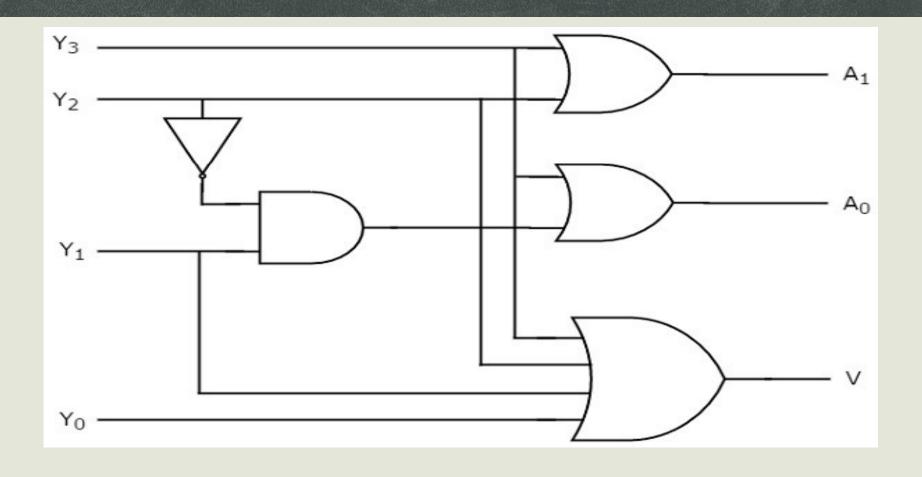
The simplified Boolean functions are

$$A_1 = Y_3 + Y_2$$

$$A_0 = Y_3 + Y_2'Y_1$$

Similarly, we will get the Boolean function of output, V as

$$V = Y_3 + Y_2 + Y_1 + Y_0$$



- The above circuit diagram contains two 2-input OR gates, one 4-input OR gate, one 2-input AND gate & an inverter.
- Here AND gate & inverter combination are used for producing a valid code at the outputs, even when multiple inputs are equal to '1' at the same time.
- Hence, this circuit encodes the four inputs with two bits based on the priority assigned to each input.

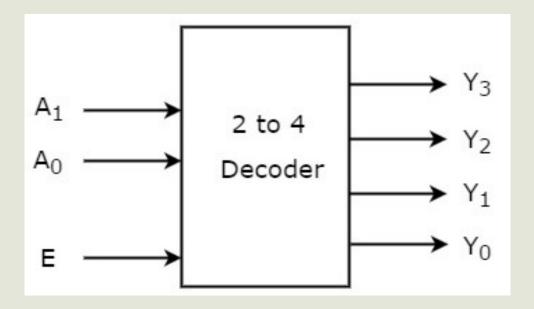
Decoder

- A decoder is also a combinational circuit as encoder but its operation is exactly reverse as that of the encoder.
- A decoder is a device that generates the original signal as output from the coded input signal and converts n lines of input into 2n lines of output.
- An AND gate can be used as the basic decoding element because it produces a high output only when all inputs are high.

Decoder

- **Decoder** is a combinational circuit that has 'n' input lines and maximum of 2ⁿ output lines.
- One of these outputs will be active High based on the combination of inputs present, when the decoder is enabled. That means decoder detects a particular code.
- The outputs of the decoder are nothing but the **min terms** of 'n' input variables (lines), when it is enabled.

- 2 to 4 Decoder
- Let 2 to 4 Decoder has two inputs $A_1 & A_0$ and four outputs $Y_3, Y_2, Y_1 & Y_0$. The **block diagram** of 2 to 4 decoder is shown in the following figure.



• One of these four outputs will be '1' for each combination of inputs when enable, E is '1'. The **Truth table** of 2 to 4 decoder is shown

below.

Enable	Inp	outs	Outputs				
E	A ₁	A ₀	Y 3	Y ₂	Y ₁	Yo	
0	×	х	0	0	0	0	
1	0	0	0	0	0	1	
1	0	1	0	0	1	0	
1	1	0	0	1	0	0	
1	1	1	1	0	0	0	

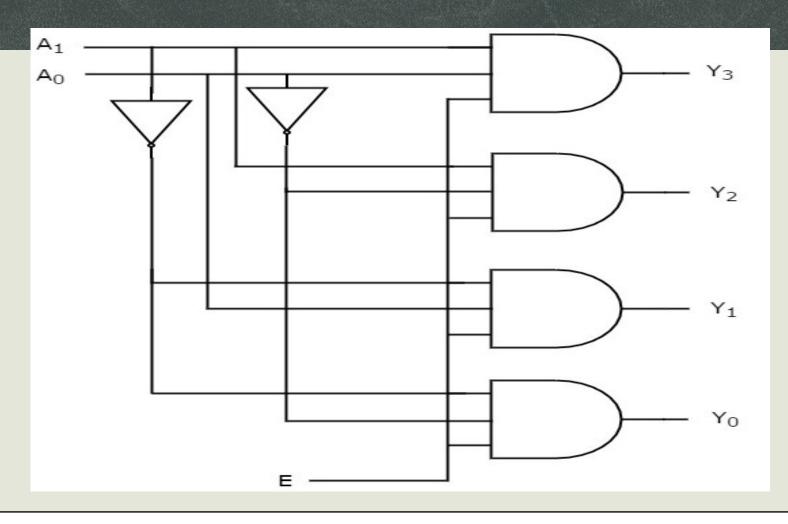
From Truth table, we can write the Boolean functions for each output as

$$Y_3 = E. A_1. A_0$$

$$Y_2 = E. A_1. A_0'$$

$$Y_1 = E. A_1'. A_0$$

$$Y_0 = E. A_1'. A_0'$$

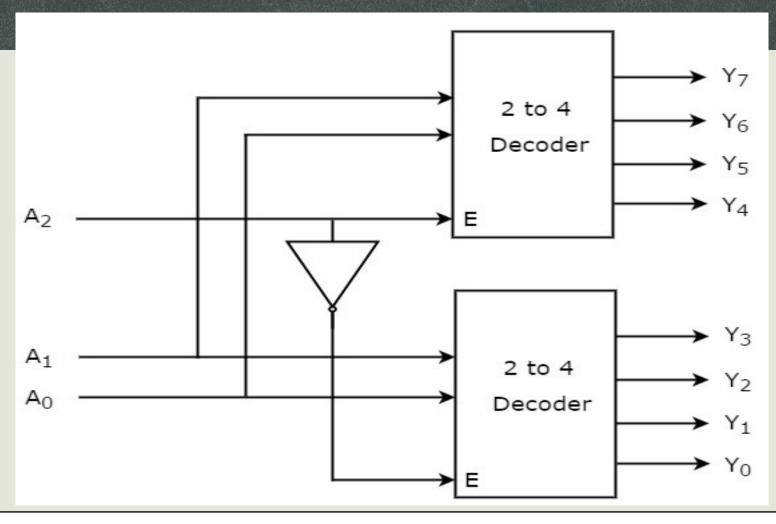


- Therefore, the outputs of 2 to 4 decoder are nothing but the **min terms** of two input variables $A_1 & A_0$, when enable, E is equal to one.
- If enable, E is zero, then all the outputs of decoder will be equal to zero.

3 to 8 Decoder

- We know that 2 to 4 Decoder has two inputs, $A_1 \& A_0$ and four outputs, Y_3 to Y_0 . Whereas, 3 to 8 Decoder has three inputs A_2 , $A_1 \& A_0$ and eight outputs, Y_7 to Y_0 .
- We can find the number of lower order decoders required for implementing higher order decoder using the following formula.
 - Required number of lower order decoders = m2/m1
- Where, m1 is the number of outputs of lower order decoder.
- m2 is the number of outputs of higher order decoder.

- Here, m1 = 4 and m2 = 8. Substitute, these two values in the above formula.
 - Required number of 2 to 4 decoders = 8/4 = 2
- Therefore, we require two 2 to 4 decoders for implementing one 3 to 8 decoder.
- The **block diagram** of 3 to 8 decoder using 2 to 4 decoders is shown in the following figure.



		Outputs								
Y7	Y ₆	Y ₅	Y ₄	Y ₃	Y ₂	Y ₁	Y ₀	A ₂	A ₁	A ₀
0	0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	0	1	0	0	0	1
0	0	0	0	0	1	0	0	0	1	0
0	0	0	0	1	0	0	0	0	1	1
0	0	0	1	0	0	0	0	1	0	0
0	0	1	0	0	0	0	0	1	0	1
0	1	0	0	0	0	0	0	1	1	0
1	0	0	0	0	0	0	0	1	1	1

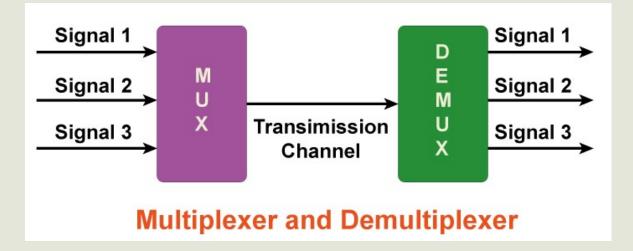
- The parallel inputs $A_1 & A_0$ are applied to each 2 to 4 decoder. The complement of input A_2 is connected to Enable, E of lower 2 to 4 decoder in order to get the outputs, Y_3 to Y_0 .
- These are the **lower four min terms**. The input, A_2 is directly connected to Enable, E of upper 2 to 4 decoder in order to get the outputs, Y_7 to Y_4 . These are the **higher four min terms**.

S.No.	ENCODER	DECODER
1	Encoder circuit basically converts the applied information signal into a coded digital bit stream.	Decoder performs reverse operation and recovers the original information signal from the coded bits.
2	In case of encoder, the applied signal is the active signal input.	Decoder accepts coded binary data as it input.
3	The number of inputs accepted by an encoder is 2n.	The number of input accepted by decode is only n inputs.
4	The output lines for an encoder is n.	The output lines of an decoder is 2n.
5	The encoder generates coded data bits as its output.	The decoder generates an active output signal in response to the coded data bits
6	The operation performed is simple.	The operation performed is complex.
7	The encoder circuit is installed at the transmitting end.	The decoder circuit is installed at the receiving side.
8	OR gate is the basic logic element used in it.	AND gate along with NOT gate is the basic logic element used in it.

- Multiplexer and Demultiplexer are Combinational Logic Circuits
- A Multiplexer is a circuit that accept many inputs but gives only one output. A Demultiplexer functions exactly in the reverse way of a multiplexer i.e., a demultiplexer accepts only one input and gives many outputs.

• Generally, multiplexer and demultiplexer are used together in many

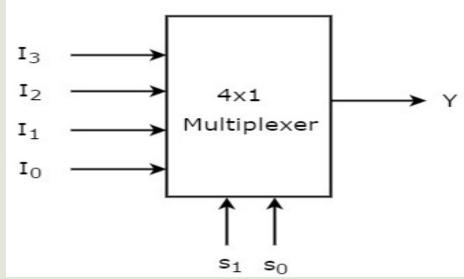
communication systems.



- **Multiplexer** is a combinational circuit that has maximum of 2ⁿ data inputs, 'n' selection lines and single output line. One of these data inputs will be connected to the output based on the values of selection lines.
- Since there are 'n' selection lines, there will be 2ⁿ possible combinations of zeros and ones. So, each combination will select only one data input. Multiplexer is also called as **Mux**.

4x1 Multiplexer

• 4x1 Multiplexer has four data inputs I_3 , I_2 , I_1 & I_0 , two selection lines s_1 & s_0 and one output Y. The **block diagram** of 4x1 Multiplexer is shown in the following diagram.



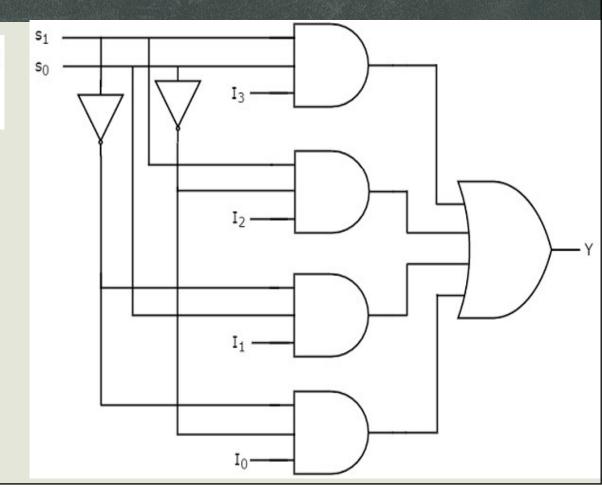
• One of these 4 inputs will be connected to the output based on the combination of inputs present at these two selection lines. **Truth table** of 4x1 Multiplexer is shown below.

Selection	Output		
S ₁	S ₀	Υ	
0	0	I ₀	
0	1	I ₁	
1	0	I ₂	
1	1	I3	

From Truth table, we can directly write the Boolean function for output, Y as

$$Y = S_1'S_0'I_0 + S_1'S_0I_1 + S_1S_0'I_2 + S_1S_0I_2$$

For instance, as shown in figure, when $S_1S_2 = 00$, the upper AND gate is enabled, while all other AND gates are disabled. Therefore, data bit I_0 is transmitted to the output, giving $Y = I_0$.

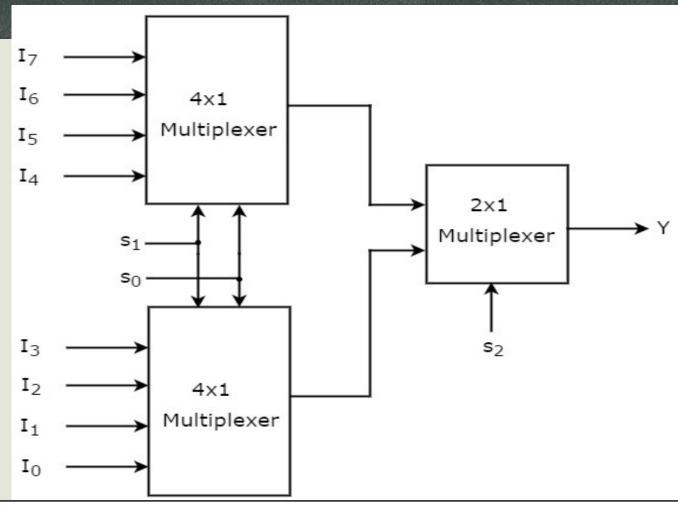


8x1 Multiplexer

- We know that 4x1 Multiplexer has 4 data inputs, 2 selection lines and one output. Whereas, 8x1 Multiplexer has 8 data inputs, 3 selection lines and one output.
- So, we require two **4x1 Multiplexers** in first stage in order to get the 8 data inputs. Since, each 4x1 Multiplexer produces one output, we require a **2x1 Multiplexer** in second stage by considering the outputs of first stage as inputs and to produce the final output.

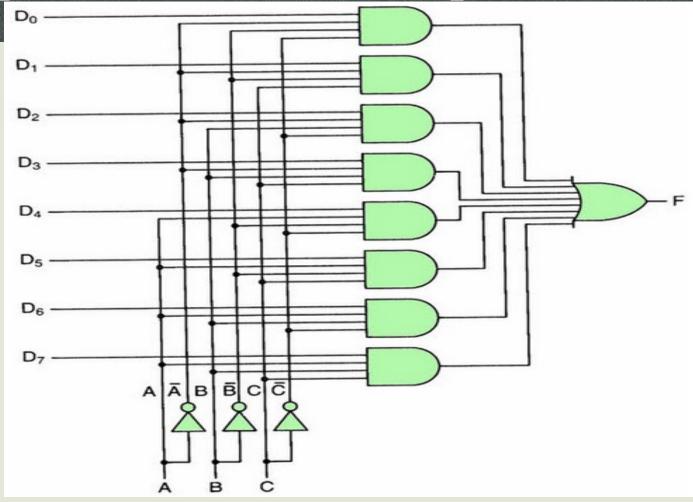
- Let the 8x1 Multiplexer has eight data inputs I_7 to I_0 , three selection lines s_2 , s_1 & s0 and one output Y.
- The **Truth table** of 8x1 Multiplexer is shown below.

	Selection Inputs		Output			
s ₂	S ₁	S ₀	Υ			
0	0	0	I ₀			
0	0	1	I ₁			
0	1	0	I ₂			
0	1	1	I ₃			
1	0	0	I ₄			
1	0	1	I ₅			
1	1	0	I ₆			
1	1	1	I ₇			



- The same **selection lines**, s_1 & s_0 are applied to both 4x1 Multiplexers. The data inputs of upper 4x1 Multiplexer are I_7 to I_4 and the data inputs of lower 4x1 Multiplexer are I_3 to I_0 . Therefore, each 4x1 Multiplexer produces an output based on the values of selection lines, s_1 & s_0 .
- The outputs of first stage 4x1 Multiplexers are applied as inputs of 2x1 Multiplexer that is present in second stage. The other **selection line**, $\mathbf{s_2}$ is applied to 2x1 Multiplexer.

- If s_2 is zero, then the output of 2x1 Multiplexer will be one of the 4 inputs I_3 to I_0 based on the values of selection lines $s_1 \& s_0$.
- If s_2 is one, then the output of 2x1 Multiplexer will be one of the 4 inputs I_7 to I_4 based on the values of selection lines $s_1 \& s_0$.



16x1 Multiplexer

- Let us implement 16x1 Multiplexer using 8x1 Multiplexers and 2x1 Multiplexer. We know that 8x1 Multiplexer has 8 data inputs, 3 selection lines and one output. Whereas, 16x1 Multiplexer has 16 data inputs, 4 selection lines and one output.
- So, we require two **8x1 Multiplexers** in first stage in order to get the 16 data inputs. Since, each 8x1 Multiplexer produces one output, we require a 2x1 Multiplexer in second stage by considering the outputs of first stage as inputs and to produce the final output.
- Let the 16x1 Multiplexer has sixteen data inputs I_{15} to I_0 , four selection lines s_3 to s_0 and one output Y. The **Truth table** of 16x1 Multiplexer is shown below.

	Selection	n Inputs		Output				
}	S ₂	S ₁	S ₀	Υ				
)	0	0	0	I ₀	1	0	0	0 0
)	0	0	1	I ₁	1	0	0	0 1
0	0	1	0	I ₂	1	0	1	1 0
0	0	1	1	I ₃	1	0	1	1 1
0	1	0	0	I ₄	1	1	0	0 0
0	1	0	1	I ₅	1	1	0	0 1
0	1	1	0	I ₆	1	1	1	1 0
0	1	1	1	I ₇	1	1	1	1 1

☐ Multiplexers and De-Multiplexers I₁₅ ____ I₁₄ -I₁₃ -8x1 $I_{12} -$ Multiplexer I_{11} — I₁₀ -19 I_8 2x1 s2 -Multiplexer s₁-17 16 15 8×1 I_4 Multiplexer IЗ I_2 I₁ Io

- The **same selection lines**, $\mathbf{s_2}$, $\mathbf{s_1}$ & $\mathbf{s_0}$ are applied to both 8x1 Multiplexers. The data inputs of upper 8x1 Multiplexer are I_{15} to I_{8} and the data inputs of lower 8x1 Multiplexer are I_{7} to I_{9} .
- Therefore, each 8x1 Multiplexer produces an output based on the values of selection lines, s_2 , s_1 & s_0 .
- The outputs of first stage 8x1 Multiplexers are applied as inputs of 2x1 Multiplexer that is present in second stage. The other **selection line**, $\mathbf{s_3}$ is applied to 2x1 Multiplexer.

- If s_3 is zero, then the output of 2x1 Multiplexer will be one of the 8 inputs Is_7 to I_0 based on the values of selection lines s_2 , $s_1 \& s_0$.
- If s_3 is one, then the output of 2x1 Multiplexer will be one of the 8 inputs I_{15} to I_8 based on the values of selection lines s_2 , $s_1 & s_0$.

- Applications of Multiplexer
- Communication System, Telephone Network, Computer Memory, Transmission from the Computer System of a Satellite

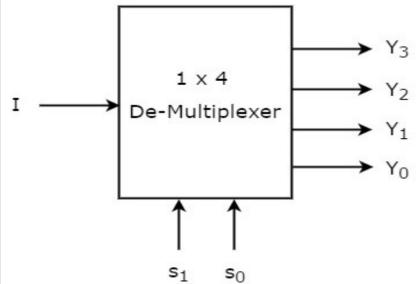
De-Multiplexers

- **De-Multiplexer** is a combinational circuit that performs the reverse operation of Multiplexer. It has single input, 'n' selection lines and maximum of 2ⁿ outputs.
- The input will be connected to one of these outputs based on the values of selection lines.
- Since there are 'n' selection lines, there will be 2ⁿ possible combinations of zeros and ones. So, each combination can select only one output. De-Multiplexer is also called as **De-Mux**.

1x4 De-Multiplexer

■ 1x4 De-Multiplexer has one input I, two selection lines, $s_1 \& s_0$ and four outputs Y_3 , Y_2 , $Y_1 \& Y_0$. The **block diagram** of 1x4 De-Multiplexer is shown in the fallowing diagram

in the following diagram.



• The single input 'I' will be connected to one of the four outputs, Y_3 to Y_0 based on the values of selection lines $s_1 & s_0$. The **Truth table** of 1x4 De-Multiplexer is shown below.

Selectio	n Inputs	Outputs					
s_1	S ₀	Y 3	Y ₂	Υ ₁	Yo		
0	0	0	0	0	I		
0	1	0	0	I	0		
1	0	0	I	0	0		
1	1	I	0	0	0		

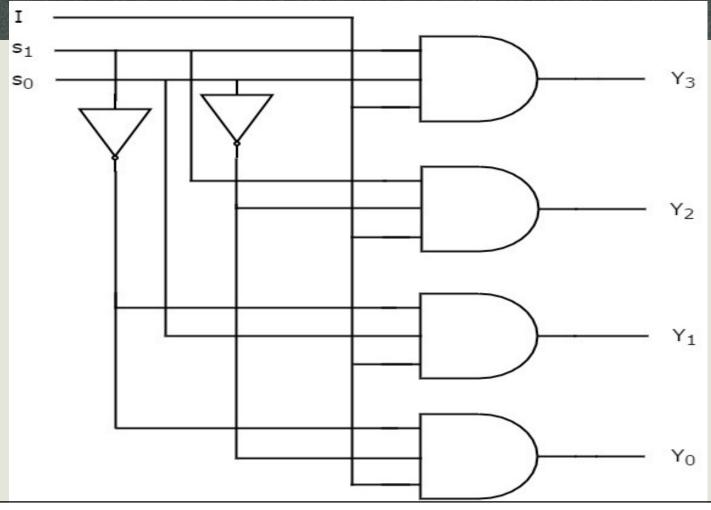
From the above Truth table, we can directly write the **Boolean functions** for each output as

$$Y_3 = s_1 s_0 I$$

$$Y_2 = s_1 s_0' I$$

$$Y_1 = s_1' s_0 I$$

$$Y_0 = s_1' s_0' I$$



1x8 De-Multiplexer

- Let us implement 1x8 De-Multiplexer using 1x4 De-Multiplexers and 1x2 De-Multiplexer.
- We know that 1x4 De-Multiplexer has single input, two selection lines and four outputs. Whereas, 1x8 De-Multiplexer has single input, three selection lines and eight outputs.
- So, we require two **1x4 De-Multiplexers** in second stage in order to get the final eight outputs. Since, the number of inputs in second stage is two, we require **1x2 DeMultiplexer** in first stage so that the outputs of first stage will be the inputs of second stage.
- Input of this 1x2 De-Multiplexer will be the overall input of 1x8 De-Multiplexer.

Let the 1x8 De-Multiplexer has one input I, three selection lines s₂, s₁ & s₀ and outputs Y₇ to Y₀. The **Truth table** of 1x8 De-Multiplexer is shown below.

Sele	ection In	Outputs								
52	s ₁	s ₀	Y7	Y ₆	Y ₅	Y ₄	Y 3	Y ₂	Y ₁	Υ0
0	0	0	0	0	0	0	0	0	0	I
0	0	1	0	0	0	0	0	0	I	0
0	1	0	0	0	0	0	0	I	0	0
0	1	1	0	0	0	0	I	0	0	0
1	0	0	0	0	0	I	0	0	0	0
1	0	1	0	0	I	0	0	0	0	0
1	1	0	0	I	0	0	0	0	0	0
1	1	1	I	0	0	0	0	0	0	0

 $Y0 = D \overline{S2} \overline{S1} \overline{S0}$

$$Y1 = D \overline{S2} \overline{S1} S0$$

$$Y2 = D \overline{S2} S1 \overline{S0}$$

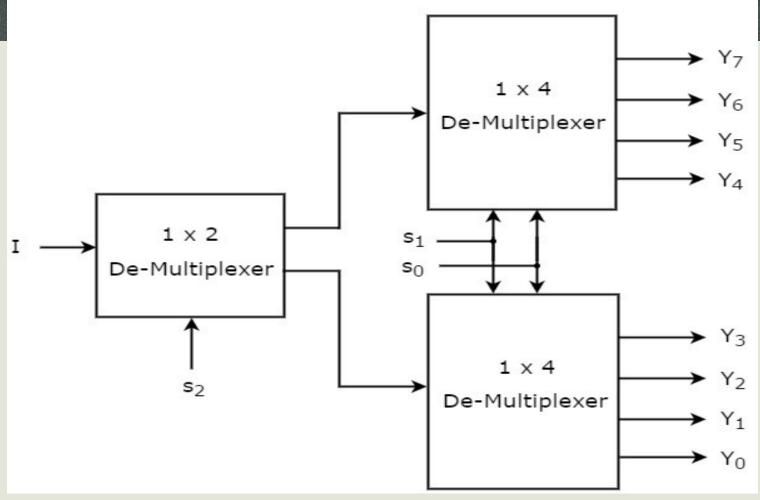
$$Y3 = D \overline{S2} S1 S0$$

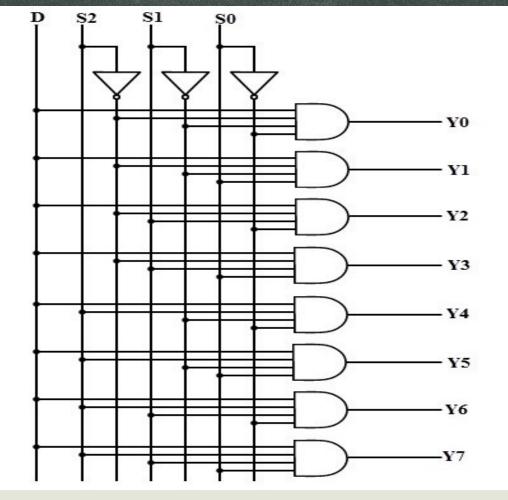
$$Y4 = D S2 \overline{S1} \overline{S0}$$

$$Y5 = D S2 \overline{S1} S0$$

$$Y6 = D S2 S1 \overline{S0}$$

$$Y7 = D S2 S1 S0$$



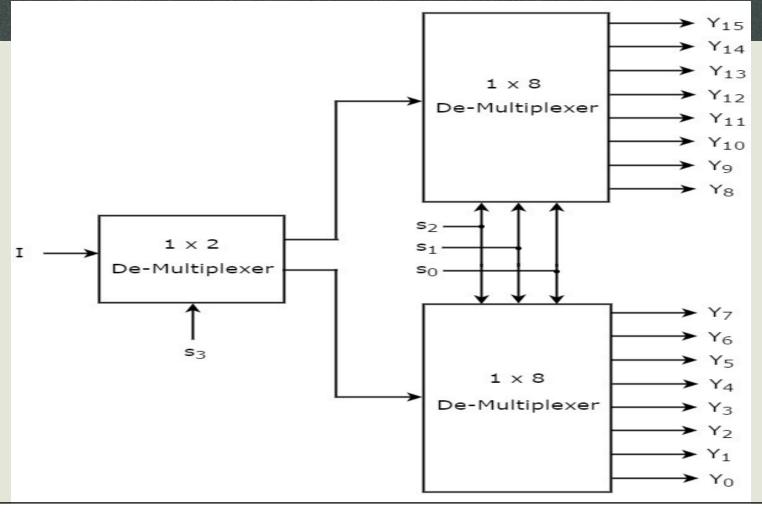


- The common **selection lines,** s_1 & s_0 are applied to both 1x4 De-Multiplexers. The outputs of upper 1x4 De-Multiplexer are Y_7 to Y_4 and the outputs of lower 1x4 De-Multiplexer are Y_3 to Y_0 .
- The other **selection line**, s_2 is applied to 1x2 De-Multiplexer. If s_2 is zero, then one of the four outputs of lower 1x4 De-Multiplexer will be equal to input, I based on the values of selection lines $s_1 \& s_0$.
- Similarly, if s_2 is one, then one of the four outputs of upper 1x4 DeMultiplexer will be equal to input, I based on the values of selection lines $s_1 \& s_0$.

1x16 De-Multiplexer

- Let us implement 1x16 De-Multiplexer using 1x8 De-Multiplexers and 1x2 De-Multiplexer. We know that 1x8 De-Multiplexer has single input, three selection lines and eight outputs.
- Whereas, 1x16 De-Multiplexer has single input, four selection lines and sixteen outputs.
- So, we require two 1x8 De-Multiplexers in second stage in order to get the final sixteen outputs. Since, the number of inputs in second stage is two, we require 1x2 DeMultiplexer in first stage so that the outputs of first stage will be the inputs of second stage.
- Input of this 1x2 De-Multiplexer will be the overall input of 1x16 De-Multiplexer.

- Let the 1x16 De-Multiplexer has one input I, four selection lines s_3 , s_2 , s_1 & s_0 and outputs Y_{15} to Y_0 .
- The **block diagram** of 1x16 De-Multiplexer using lower order Multiplexers is shown in the following figure.



- The common **selection lines** s_2 , s_1 & s_0 are applied to both 1x8 De-Multiplexers. The outputs of upper 1x8 De-Multiplexer are Y_{15} to Y_8 and the outputs of lower 1x8 DeMultiplexer are Y_7 to Y_0 .
- The other **selection line**, s_3 is applied to 1x2 De-Multiplexer. If s_3 is zero, then one of the eight outputs of lower 1x8 De-Multiplexer will be equal to input, I based on the values of selection lines s_2 , $s_1 & s_0$.
- Similarly, if s3 is one, then one of the 8 outputs of upper 1x8 De-Multiplexer will be equal to input, I based on the values of selection lines s_2 , $s_1 \& s_0$.

Applications of Demultiplexer

- Most of the communication system are bidirectional i.e., they function in both ways (transmitting and receiving signals). Hence, for most of the applications, the multiplexer and demultiplexer work in sync.
- Demultiplexer are also used for reconstruction of parallel data and ALU circuits.