

(C)

$$R = - \int_{w_0}^{w_1} \frac{V}{C_L T} dw$$

(Taken from Notes)

$$\Rightarrow - \int_{w_0}^{w_1} \underbrace{\frac{V}{C_L}}_{\text{TSFC}} \times \underbrace{\frac{C_L}{C_D}}_{\text{Constant}} \times \frac{dw}{w}$$

$$\alpha \rightarrow \text{Const} ; C_L, C_D \rightarrow \text{Const}$$

$$\Rightarrow w_0 = w$$

$$\Rightarrow w_1 = W - w_f$$

$$R = - \frac{V C_L}{C_L C_D} \int_{w_0}^{w_1} \frac{dw}{w}$$

$$\Rightarrow - \frac{V C_L}{C_L C_D} \times \ln \left(\frac{w_1}{w_0} \right)$$

$$R \Rightarrow \frac{V C_L}{C_L C_D} \times \ln \left(\frac{w_0}{w_1} \right)$$

d)

for $R = 100 \text{ km}$

$$\left(\frac{C_L}{C_D}\right)_{\max} \rightarrow \frac{1}{2\sqrt{K C_{D0}}}$$

$$10^5 \Rightarrow \frac{(0.7)(V_{\text{wind}})}{(0.7) \times} \times \left(\frac{1}{2\sqrt{K C_{D0}}}\right) \times \ln\left(\frac{10000}{W_1}\right)$$

$$10^5 = 343 \times \frac{1}{2\sqrt{\frac{C_{D0}}{\pi E A R}}} \times \ln\left(\frac{10000}{W_1}\right)$$

$$\cancel{W_1} \Rightarrow 2 \times 10^5 \Rightarrow \left(343 \times \sqrt{\frac{\pi E A R}{C_{D0}}}\right) \times \ln\left(\frac{10000}{W_1}\right)$$

$$\ln\left(\frac{W_1}{10000}\right) \approx -\frac{2 \times 10^5}{343} \times \sqrt{\frac{C_{D0}}{\pi E A R}}$$