

$v$  at "-" terminal is  $v_s$  because we have an op-amp with negative feedback.

KCL at "-" terminal:

$$\frac{(v_s - 0)}{R_1} = \frac{v_o - v_s}{R_2}$$

Solving this for  $v_o$ :

$$\frac{v_o}{R_2} = \frac{v_s}{R_1} + \frac{v_s}{R_2} \Rightarrow v_o = v_s \frac{R_2}{R_1} + v_s$$

$$v_o = v_s \left( \frac{R_2}{R_1} + 1 \right)$$

b)  $\frac{v_s}{i_s} = R_{eq}$  By KCL @ "+" terminal:

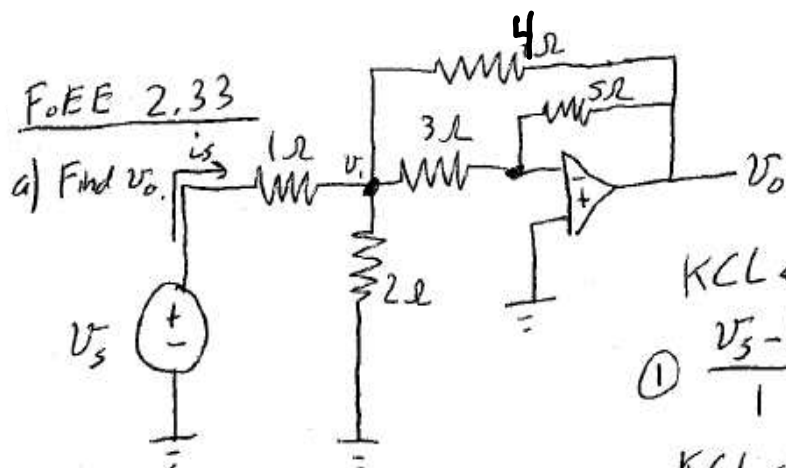
$$i_s = \frac{v_s - v_o}{R}$$

substituting above for  $v_o$

$$\begin{aligned} i_s &= \frac{v_s}{R} - \frac{v_s \left( \frac{R_2}{R_1} + 1 \right)}{R} \\ &= \frac{v_s}{R} \left( 1 - \frac{R_2}{R_1} - 1 \right) \\ &= v_s \left( \frac{-R_2}{R R_1} \right) \end{aligned}$$

$$\text{So, } \frac{v_s}{i_s} = \frac{v_s}{v_s \left( \frac{-R_2}{R R_1} \right)} = \frac{-R R_1}{R_2}$$

2)

KCL at  $v_1$  yields:

$$\textcircled{1} \frac{v_s - v_1}{1} = \frac{v_1}{2} + \frac{v_1}{3} + \frac{v_1 - v_o}{4}$$

KCL at  $v_o$  yields

$$\textcircled{2} \frac{v_1}{3} = \frac{-v_o}{5} \Rightarrow v_o = -\frac{5}{3}v_1$$

So,  $\textcircled{1}$  becomes  $v_s - v_1 = \frac{v_1}{2} + \frac{v_1}{3} + \frac{v_1 - (-\frac{5}{3}v_1)}{4}$

$$12v_s - 12v_1 = 6v_1 + 4v_1 + 3\left(\frac{8}{3}v_1\right) = 18v_1$$

$$12v_s = 30v_1 \Rightarrow v_1 = \frac{12}{30}v_s = \frac{2}{5}v_s$$

Since  $v_o = -\frac{5}{3}v_1 = -\frac{5}{3}\left(\frac{2}{5}v_s\right) = -\frac{2}{3}v_s$

b) Find  $\frac{v_s}{i_s}$ , the resistance as seen by the source.

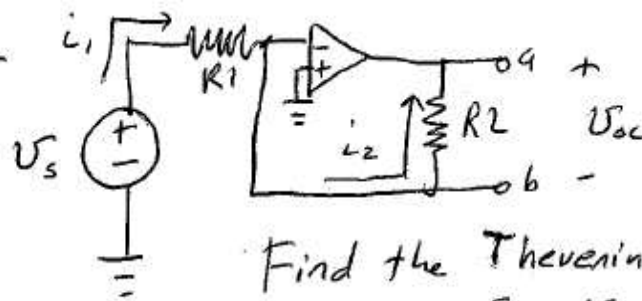
Since  $v_1 = \frac{2}{5}v_s$  and  $v_o = -\frac{2}{3}v_s \Rightarrow v_1 = \frac{2}{5}v_s$  (also found here)

$$i_s = \frac{v_s - v_1}{1} = \frac{v_s - \frac{2}{5}v_s}{1} = \frac{3}{5}v_s$$

So,  $\frac{v_s}{i_s} = \frac{v_s}{3/5 v_s} = \frac{5}{3} \Omega$

3)

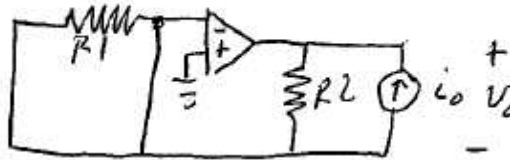
F0EE 2.46



Find the Thevenin Equivalent at a & b.

First, we need  $V_{oc}$ :  $i_1 = i_2 = \frac{V_s}{R_1} = \frac{-V_{oc}}{R_2} \Rightarrow V_{oc} = -\frac{R_2}{R_1} V_s$

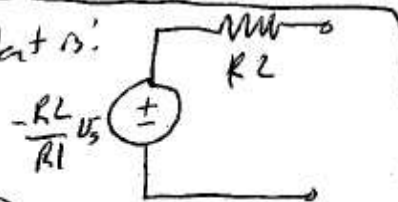
As suggested in the problem statement, we'll apply a current source at a/b and calculate the resulting voltage. When we do this, we still need to short  $V_s$ !



here,  $V_o = i_o R_2$

So,  $R_o = \frac{V_o}{i_o} = R_2$

$\therefore$  the Thevenin Equivalent is:



4)

3.5 For the circuit shown in Fig. P3.5, suppose that  $i(t)$  is described by the function given in Fig. P3.1b. Sketch (a)  $v_R(t)$ , (b)  $v_L(t)$ , and (c)  $v(t)$ .

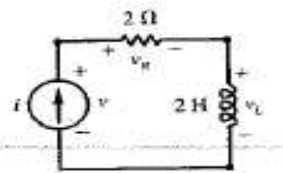
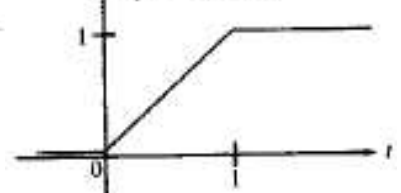


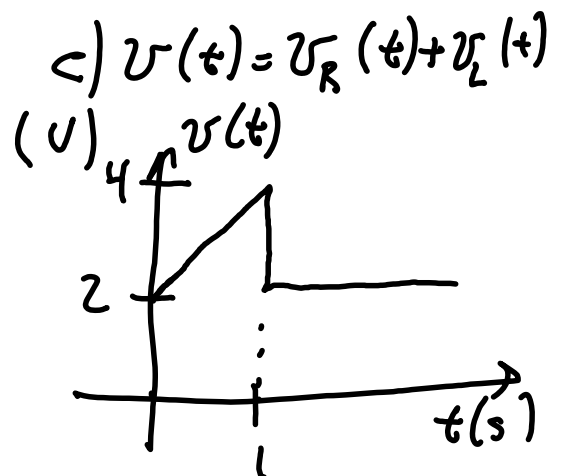
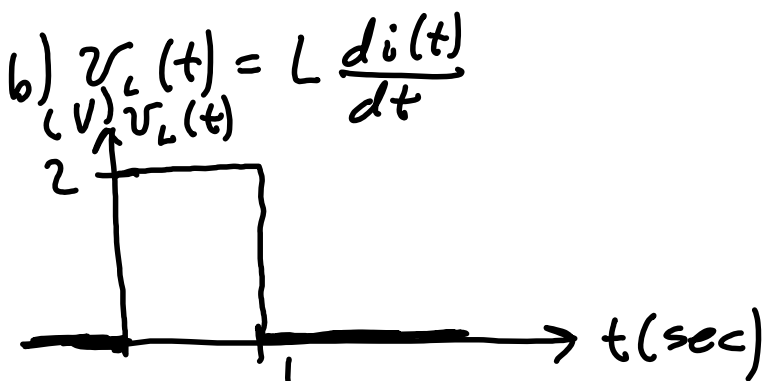
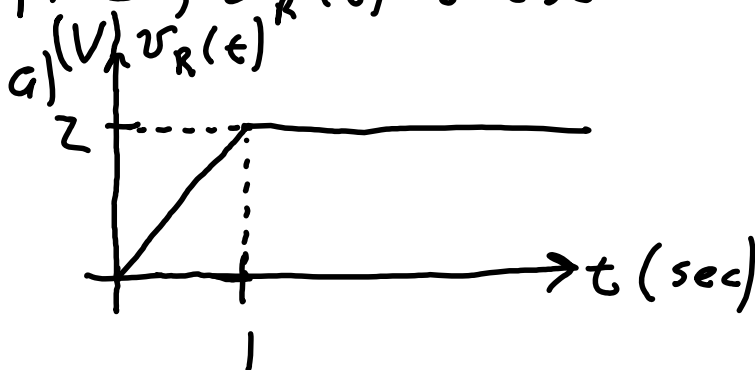
Fig. P3.5

$$i(t) = \begin{cases} 0 \text{ A for } t \leq 0 \text{ s} \\ t \text{ A for } 0 < t \leq 1 \text{ s} \\ 1 \text{ A for } t > 1 \text{ s} \end{cases}$$



(b)

$i$  is the same all around the loop. So,  $V_R(t) = i \cdot 2 \Omega$



5)

3.9 For the op-amp circuit shown in Fig. P3.9, suppose that  $v(t)$  is described by the function given in Fig. P3.7b. Sketch (a)  $i(t)$ , (b)  $i_R(t)$ , (c)  $v_R(t)$ , (d)  $v_s(t)$ , and (e)  $v_o(t)$ .

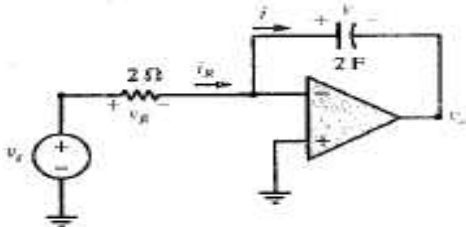
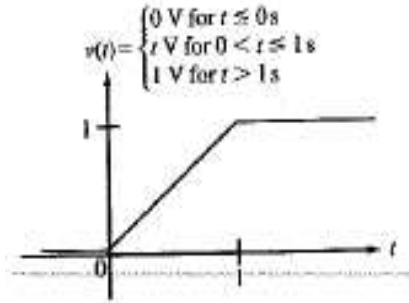
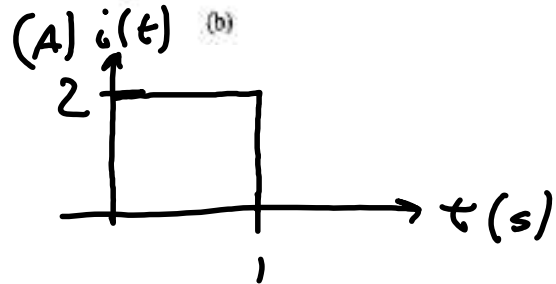


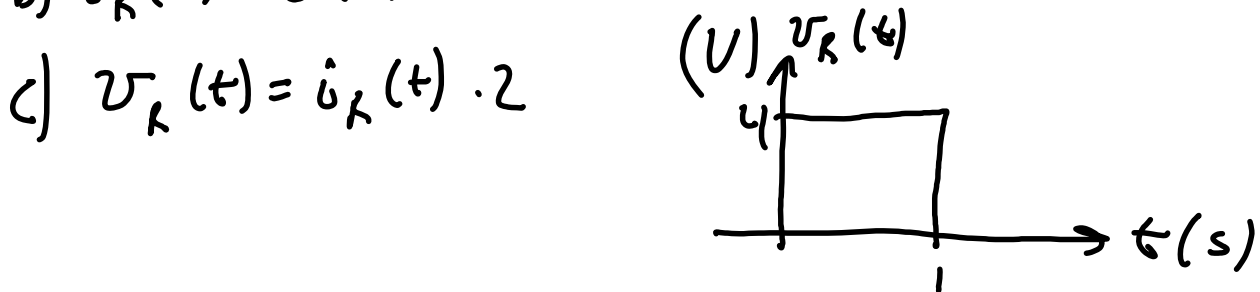
Fig. P3.9



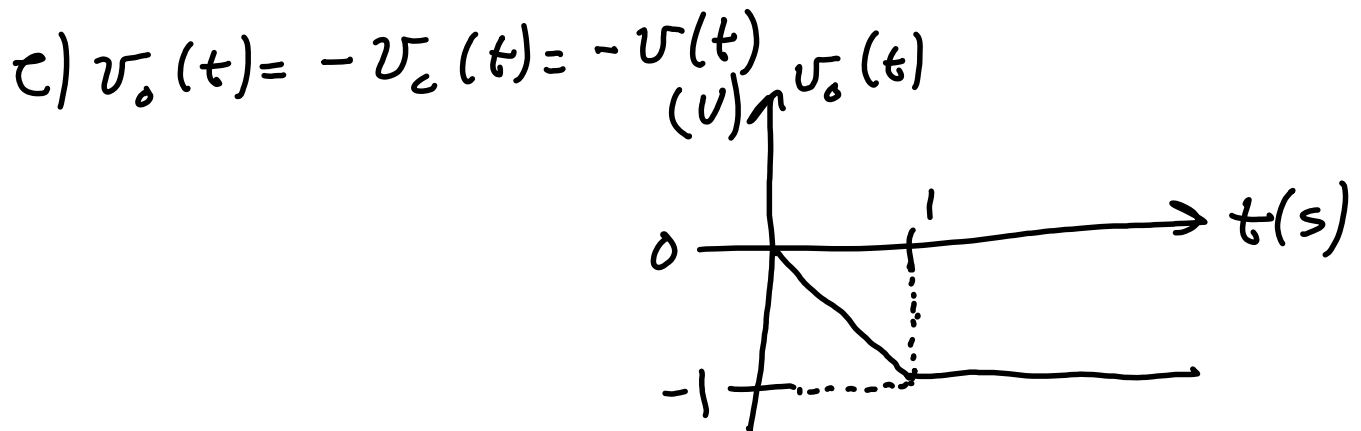
$$a) i(t) = C \frac{dv}{dt} = 2 \cdot \frac{dv}{dt}$$



$$b) i_R(t) = i(t) \longrightarrow \text{plot same as (a)}$$

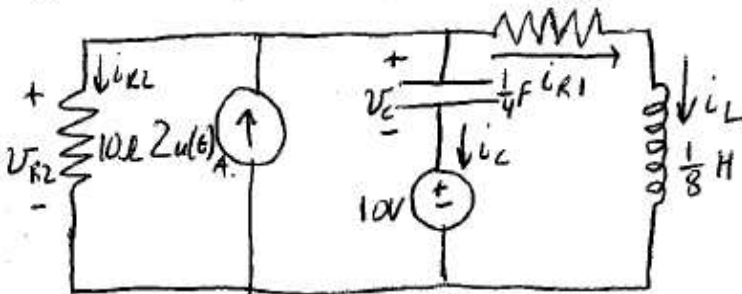


$$d) v_s(t) = v_R(t) \longrightarrow \text{plot same as (c)}$$



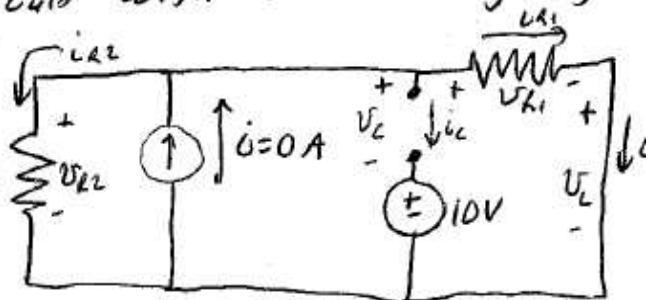
6)

We are asked to analyze the following circuit at  $t=0^-$ ,  $t=0^+$  and  $t=\infty$ .



At  $t=0^-$  we have a DC circuit with no current going up through the current source:

In the DC case, the capacitor is an open circuit and the inductor is a short circuit.



Since no current can flow through an open circuit  $i_C(0^-) = 0A$ .

With no current from the <sup>current</sup> source and no current allowed to flow from the 10V source, all currents are 0A before  $t=0$ . So  $i_{RL}(0^-) = 0A$ .

$i_{R1}(0^-) = 0A$  and  $i_L(0^-) = 0A$ . Ohm's law tells us that

$V_{R1}(0^-) = 0V$  and  $V_{RL}(0^-) = 0V$ . Since no voltage can

drop across a short circuit,  $V_L(0^-) = 0V$ . Finally KVL around the right-most loop gives us:  $10 + V_C = V_{R1} + V_L$

So,  $V_C(0^-) = -10V$

At  $t=0^+$ , our elements are back in our circuit, the current source is outputting 2A and we know that the current across the inductor and the voltage across the capacitor can't change.

So,  $V_C(0^+) = -10V$ ,  $i_L(0^+) = 0A$

Since  $i_{R1}(0^+) = i_L(0^+)$ ;  $i_{R1}(0^+) = 0A$

By Ohm's law

$V_{R1}(0^+) = 0V$

By KVL (same as before)

$$10 + v_c = v_{R1} + v_L$$

So,  $10 + -10 = 0 + v_c \therefore v_c(0^+) = 0V$

$v_{R2}(0^+) = v_{R1}(0^+) + v_c(0^+) \leftarrow$  KVL around outside loop.

So,  $v_{R2}(0^+) = 0V$ , So, by Ohm's law,  $i_{R2}(0^+) = 0A$

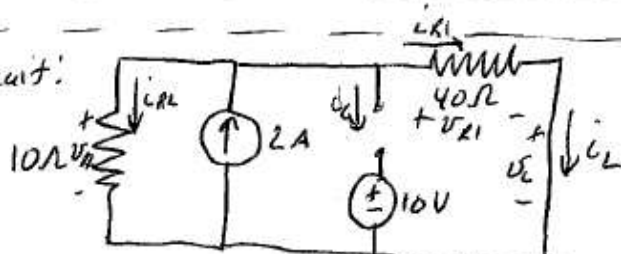
That leaves 2 Amps of current (from the current source) that has to flow somewhere.  $\rightarrow$  KCL at node A we see that:

$$i_{R2} - 2 + i_c + i_{R1} = 0$$

at  $t=0^+$  this is:  $0 - 2 + i_c + 0 = 0$  so,  $i_c(0^+) = 2A$

At  $t=\infty$  we have the following circuit:

We can use DC replacements because the circuit has stabilized.



Again, no current can flow through an open circuit, so  $i_c(\infty) = 0A$

Since there can be no voltage drop over a short:  $v_L(\infty) = 0V$

Using KCL:  $2 = i_{R2} + i_{R1}$  ①

Using KVL:  $v_{R2} = v_{R1} + v_L$ , adding Ohm's Law:  $10i_{R2} = 40i_{R1}$  ②

Combining ① & ② we see that  $10(2 - i_{R1}) = 40i_{R1}$

So,  $20 = 50i_{R1} \Rightarrow$

$i_{R1}(\infty) = 0.4A$

$\therefore i_{R2}(\infty) = 1.6A$

From Ohm's Law:

$v_{R1}(\infty) = 16V$

and

$v_{R2}(\infty) = 16V$

Since,  $i_L(\infty) = i_{R1}(\infty)$ ,  $i_L(\infty) = 0.4A$

Finally, by KVL:  $10 + v_c(\infty) = v_{R1}(\infty) + v_L(\infty)$

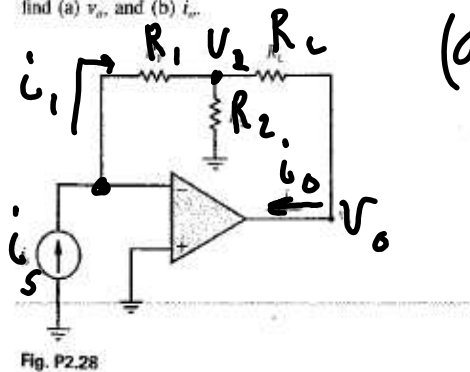
$10 + v_c(\infty) = 16$

$\therefore v_c(\infty) = 6V$

The chart for #1 is shown below:

	$t=0^-$	$t=0^+$	$t=\infty$
$i_L(t)$	0 A	0 A	0.4 A
$i_C(t)$	0 A	2 A	0 A
$i_{R1}(t)$	0 A	0 A	0.4 A
$i_{R2}(t)$	0 A	0 A	1.6 A
$v_L(t)$	0 V	0 V	0 V
$v_C(t)$	-10 V	-10 V	6 V
$v_{R1}(t)$	0 V	0 V	16 V
$v_{R2}(t)$	0 V	0 V	16 V

7. (0 points) FoEE 2.28 2.28 For the op-amp circuit shown in Fig. P2.28, find (a)  $v_o$ , and (b)  $i_o$ .



(a) KCL at  $v_2$ :  $i_s = \frac{0 - v_2}{R_1} \Rightarrow v_2 = -i_s R_1$

KCL at  $v_2$ :  $\frac{0 - v_2}{R_1} = \frac{v_2}{R_2} + \frac{v_2 - v_o}{R_L}$

$\frac{-i_s R_1}{R_1} = \frac{-i_s R_1}{R_2} + \frac{-i_s R_1 - v_o}{R_L}$

$i_s \left( 1 + \frac{R_1}{R_2} + \frac{R_1}{R_L} \right) R_L = -v_o$

So,  $v_o = -i_s R_L \left( 1 + \frac{R_1}{R_2} + \frac{R_1}{R_L} \right)$

(b)  $i_o = \frac{v_2 - v_o}{R_L}$   
 $= \frac{-i_s R_1 + i_s R_L \left( 1 + \frac{R_1}{R_2} + \frac{R_1}{R_L} \right)}{R_L}$

$= i_s \left[ \frac{-R_1}{R_L} + 1 + \frac{R_1}{R_2} + \frac{R_1}{R_L} \right]$

$i_o = i_s \left[ \frac{R_1}{R_2} + 1 \right]$

8 (0 points) FoEE 2.45

2.45 Find the Thévenin equivalent of the op-amp circuit shown in Fig. P2.45. (Hint: To find  $R_{eq}$ , apply a current source  $i_o$  and calculate the resulting voltage  $v_o$ .)

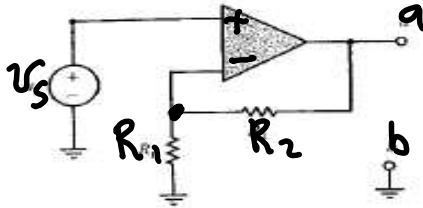
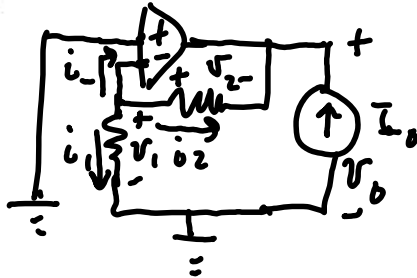
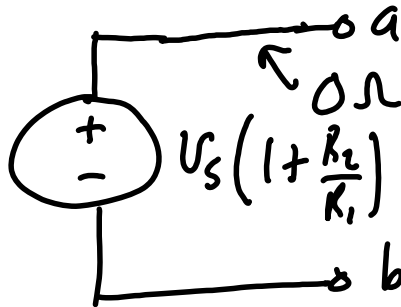


Fig. P2.45

To find  $R_{eq}$ :



Thévenin Eq.



$$KCL \text{ at } v_-: \frac{v_s}{R_1} = \frac{v_o - v_s}{R_2}$$

$$\text{So, } v_{oc} = v_s \left( \frac{1}{R_1} + \frac{1}{R_2} \right) R_2$$

$$v_{oc} = v_s \left( 1 + \frac{R_2}{R_1} \right)$$

$$v_- = 0 \text{ V so, } i_1 = 0.$$

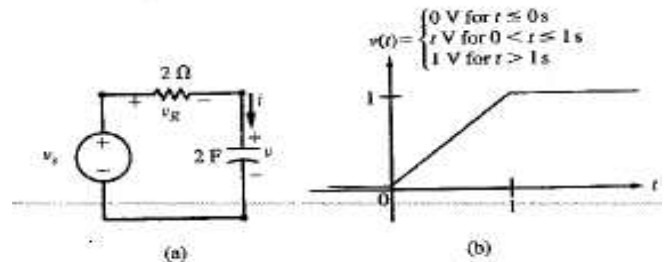
$$\text{Since } i_- = 0 \text{ } i_2 = 0.$$

$$\therefore v_2 = 0$$

$$\therefore v_o = 0 \therefore R_{eq} = 0.$$

9 (0 points) FoEE 3.7

3.7 For the circuit shown in Fig. P3.7a, suppose that  $v(t)$  is described by the function given in Fig. P3.7b. Sketch (a)  $i(t)$ , (b)  $w_c(t)$ , (c)  $p_R(t)$ , (d)  $v_R(t)$ , and (e)  $v_s(t)$ .



5) FoEE 3.1

$$v(t) = \begin{cases} 0 \text{ V} & t \leq 0 \\ t \text{ V} & 0 < t \leq 1 \\ 1 \text{ V} & t > 1 \end{cases}$$

$$a) i(t) = 2 \frac{dv}{dt} = \begin{cases} 0 & t \leq 0 \\ 2 & 0 < t \leq 1 \\ 0 & t > 1 \end{cases}$$

$$b) w_c(t) = \frac{1}{2} 2 v^2(t) = \begin{cases} 0 & t \leq 0 \\ t^2 & 0 < t \leq 1 \\ 1 & t > 1 \end{cases}$$

$$c) p_R(t) = R i^2(t) = \begin{cases} 0 & t \leq 0 \\ 4 & 0 < t \leq 1 \\ 0 & t > 1 \end{cases}$$

$$d) v_R(t) = R i(t) = 2 i(t) = \begin{cases} 0 & t \leq 0 \\ 4 & 0 < t \leq 1 \\ 0 & t > 1 \end{cases}$$

$$e) v_s(t) = v_R(t) + v(t) = \begin{cases} 0 & t \leq 0 \\ 4+t & 0 < t \leq 1 \\ 1 & t > 1 \end{cases}$$

