

Electronic Circuits

# ELEC 301

Mini-Project 2

Ruyi Zhou 49581911

2020-10-30

# Part I

## (a) Datasheet of 2N2222A

**Table 1.** The Small Signal Parameters  $h_{fe}$ ,  $h_{ie}$ , and  $h_{oc}$  of 2N2222A

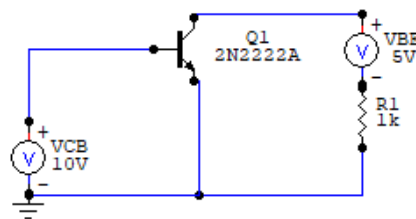
Description	Symbol	Range of value
Small Signal Current Gain	$h_{fe}$	50~300
Input Impedance	$h_{ie}$	2.0k $\Omega$ ~ 8.0k $\Omega$
Output Impedance	$h_{oc}$	5.0 $\mu$ 1/ $\Omega$ ~ 35.0 $\mu$ 1/ $\Omega$

\*All data are for  $V_{CE} = 10V$ ,  $I_c = 1mA$ ,  $f = 1kHz$  and  $T = 25$  Celsius. (Data from: <https://www.verical.com/datasheet/rectron-semiconductor-rf-bjt-2N2222A-4576108.pdf>)

## (b) The characteristics of 2N2222A

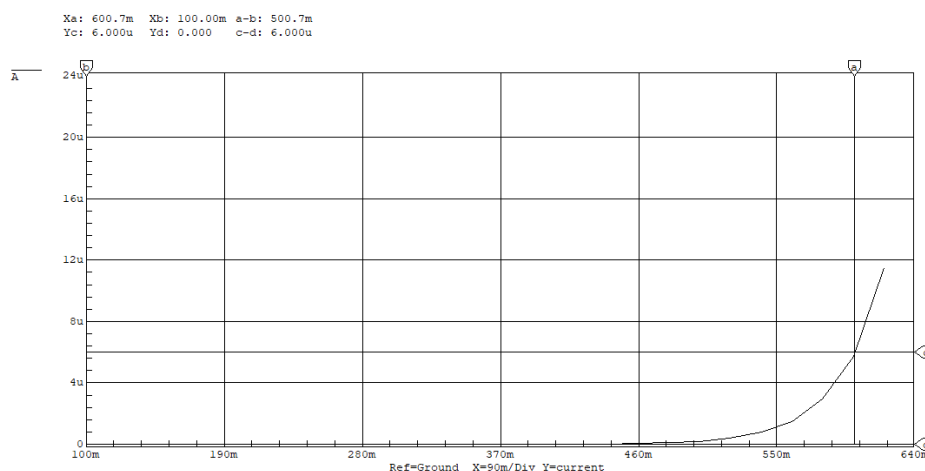
### i) $I_B$ vs $V_{BE}$

The simulated circuits are designed in *Circuitmaker*.



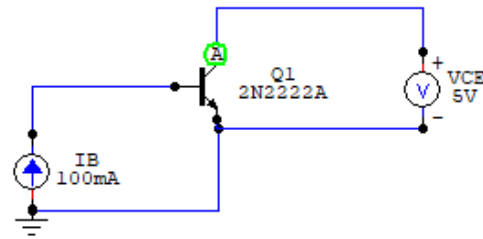
**Figure 1.** The test circuit of for  $I_B$  vs  $V_{BE}$

The DC-simulation is applied. In the DC Analysis set up, the start value of  $V_{BE}$  is 0 V; the stop value is 650mV; the step value is 20mV. The plot of  $I_B$  vs  $V_{BE}$  is:



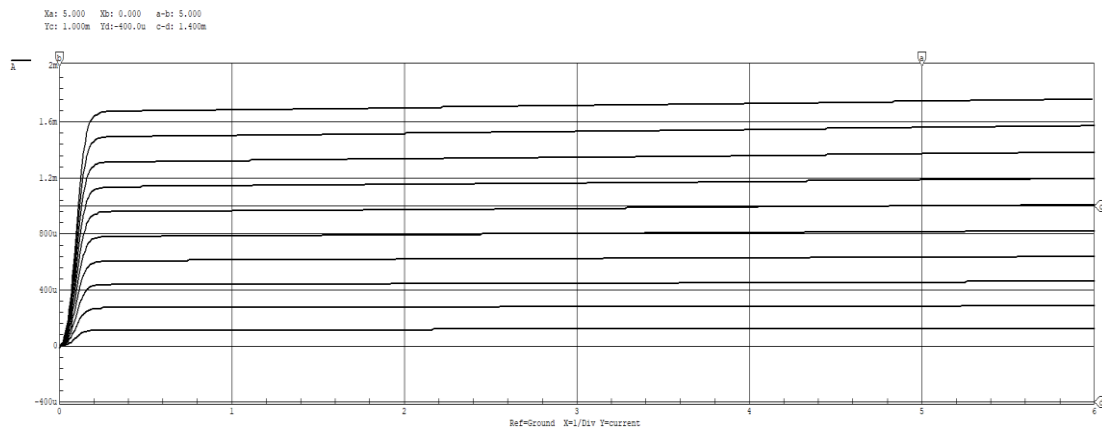
**Figure 2.** The plot of  $I_B$  vs  $V_{BE}$

ii)  $I_C$  vs  $V_{CE}$  with various  $I_B$



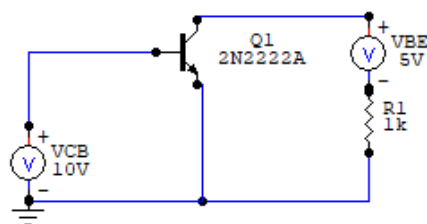
**Figure 3.** The test circuit for  $I_C$  vs  $V_{CE}$  with various  $I_B$

The DC-simulation is applied. In the DC Analysis set up, the start value of  $V_{CE}$  is 0V; the stop value is 6 V; the step value is 10 mV. Another variable  $I_B$  is used. The start value of  $I_B$  is 1uA; the stop value is 10 uA; the step value is 1 uA. The plot of  $I_C$  vs  $V_{CE}$  with different  $I_B$  is:



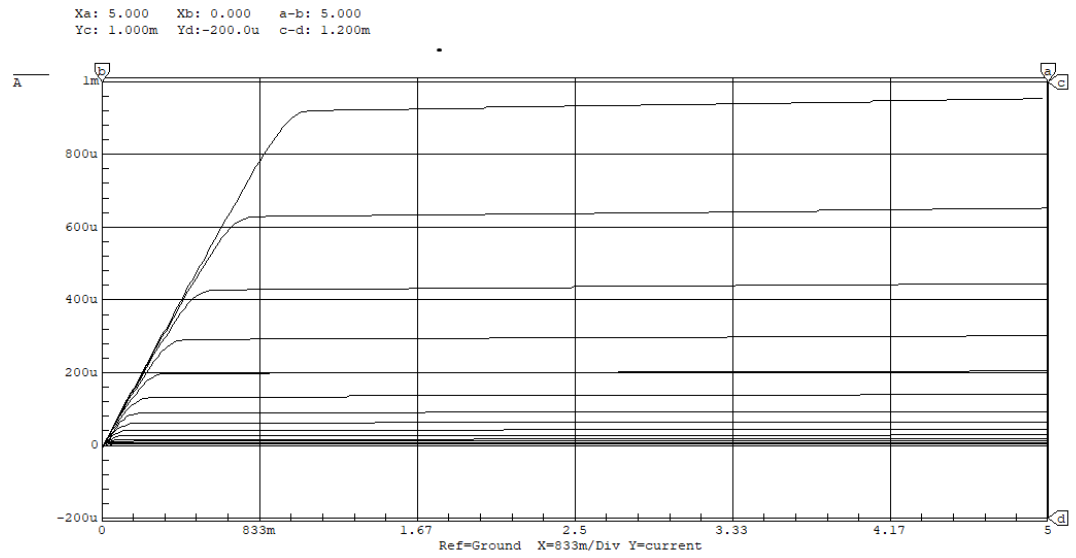
**Figure 4.** The plot of  $I_C$  vs  $V_{CE}$  with various  $I_B$

iii)  $I_C$  vs  $V_{CE}$  with various  $V_{BE}$



**Figure 5.** The test circuit for  $I_C$  vs  $V_{CE}$  with various  $V_{BE}$

In the DC Analysis set up, the start value of  $V_{CE}$  is 0V; the stop value is 5 V; the step value is 100 mV. Another variable  $V_{BE}$  is used. The start value of  $V_{BE}$  is 0V; the stop value is 5V; the step value is 500mV. The plot of  $I_C$  vs  $V_{CE}$  with different  $V_{BE}$  is:



**Figure 6.** The plot of  $I_C$  vs  $V_{CE}$  with various  $V_{BE}$

As shown in **Figure 4**, the step value of  $I_B$  is  $1\mu A$ . There are 10 lines in the **Figure 4**, each of them represents the relationship between  $I_C$  and  $V_{CE}$  with a different  $I_B$ . The  $I_B$  for the bottom line is  $1\mu A$ , for the top line is  $10\mu A$ . From **Figure 4**, when  $V_{CE} = 5V$  (line a) and  $I_C = 1mA$  line c),  $I_B$  is about  $6\mu A$  (the 6<sup>th</sup> line from bottom).

$$I_C = \beta \cdot I_B$$

$$\beta = \frac{I_C}{I_B} = \frac{1mA}{6\mu A} = \boxed{166.67}$$

According to the formula in the ELEC 301 lecture notes,  $g_m$ ,  $r_\pi$  and  $r_o$  can be calculated:

$$g_m = \frac{I_C}{V_T}$$

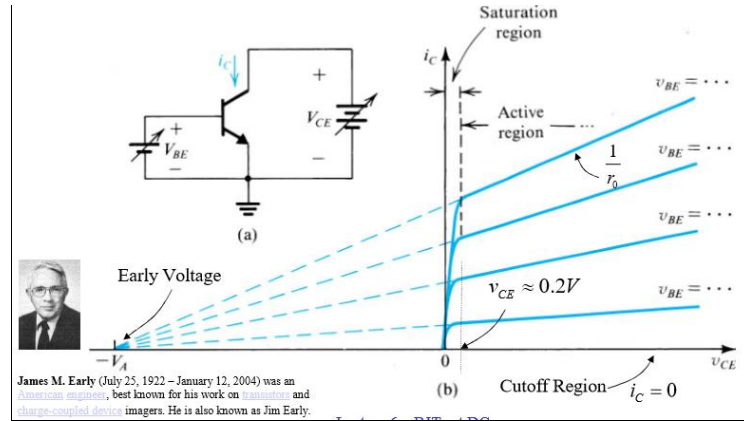
In this case, the temperature is 25 Celsius. Thus,  $V_T = 25\text{ mV}$  and  $I_C$  is  $1\text{ mA}$ .

$$g_m = \frac{1mA}{25\text{ mV}} = 0.04 \frac{1}{\Omega} = \boxed{0.04\text{ S}}$$

$$r_\pi = \frac{\beta \cdot V_T}{I_C} = \frac{166.67 \cdot 25\text{ mV}}{1\text{ mA}} = \boxed{4166.75\ \Omega}$$

To find  $r_o$  and  $V_A$ , the fundamental knowledge of BJT is needed.

Recall the Lecture 6 page 16 from ELEC 201 (Dr. Jesus Calvino-Fraga):



**Figure 7.** The characteristic of BJTs

\*The author of **Figure 7** is Dr. Jesus Calvino-Fraga and with his explicit permission

As **Figure 7** shown,  $V_A$  (Early Voltage) is the x-intercept of the extensions of the line of  $I_C$  vs  $V_{CE}$ . From **Figure 4**, the line  $I_B = 6 \mu A$ , called *line6* is chosen. Two points on *line6* are needed to generate the equation of the line. From the simulation plot, when  $I_{C1} = 960 \mu A$ ,  $V_{CE1} = 1V$ ; when  $I_{C2} = 1mA$ ,  $V_{CE2} = 5V$ . The equation can be generated:

$$\text{Slope} = \frac{I_{C2} - I_{C1}}{V_{CE2} - V_{CE1}} = \frac{1mA - 960\mu A}{5V - 1V} = 0.00001$$

$$(Y - y_1) = \text{Slope} (X - x_1), \text{ (Take } I_C = 1mA \text{ as } y_1 \text{ and } V_{CE} = 5V \text{ as } x_1)$$

$$Y = 0.00001X - x_1 * 0.00001 + y_1 = 0.00001X - 5V * 0.00001 + 1mA = 0.00001X + 0.00095$$

When  $Y = 0$  (x-intercept):

$$0 = 0.00001X + 0.00095$$

$$X = -95 \text{ (-}V_A\text{)}$$

$$\boxed{V_A = 95 V}$$

From the ELEC201 Lecture note,  $r_o$  can be calculated:

$$r_o \approx \frac{V_A}{I_C} = \frac{95 V}{1 mA} = \boxed{95000 \Omega}$$

$$\text{Admittance } y_o = 1/r_o = 10.526 \mu S$$

**Table 2.** The ‘measured’ value vs the value from datasheet

Symbol	Measured	Datasheet
$\beta$	166.67	50 ~ 300
$r_{\pi}$	4166.75	2000 ~ 8000 $\Omega$
$r_o$	10.526	5 $\mu$ ~ 35 $\mu$ S

\*The datasheet is from <https://datasheetspdf.com/pdf-file/490365/STMicroelectronics/2N2222A/1>.

As **Table 2** shown, the ‘measured’(calculated) values are in the range of the value from datasheet. Thus, the simulated circuit and the calculations are acceptable.

### **(c) $V_{CC} = 15\text{ V}$ and $I_C = 1\text{ mA}$**

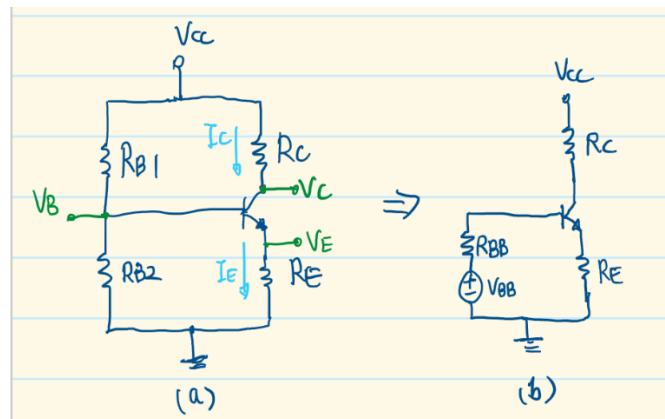
#### **i) ‘Measured’**

From **Figure 4**, for the  $V_{CE} = 4\text{ V}$  and  $I_C = 1\text{ Ma}$ ,  $I_B$  is about **6.05  $\mu\text{A}$**  (Slightly above the 6<sup>th</sup> line from bottom).

From **Figure 2**, when  $I_B$  is 6.05  $\mu\text{A}$ , the  $V_{BE}$  is 610mV = 0.601V.

$$I_E = I_B + I_C = 6.05\text{ }\mu\text{A} + 1.0\text{ mA} = 1.00605\text{ mA}$$

$$V_{CE} \text{ is } 4\text{V of less and } R_E = 0.5R_C$$



**Figure 8.** Simple bias network

From **Figure 8(a)**,  $V_{CC} = I_C * R_C + V_{CE} + I_E * R_E$ :

$$15\text{V} - 4\text{V} = 1\text{mA} * R_C + 1.0061\text{mA} * (0.5R_C)$$

$$R_C = \boxed{7318.45\text{ }\Omega}$$

$$R_E = 0.5R_C = \boxed{3659.23\text{ }\Omega}$$

$$V_C = V_{CC} - I_C * R_C = 15\text{V} - 1\text{mA} * 7318.70\Omega = \boxed{7.68\text{V}}$$

$$V_E = I_E * R_E = 1.006\text{mA} * 3659.35\Omega = \boxed{3.68\text{V}}$$

$$V_B = V_E + V_{BE} = 3.68\text{V} + 0.601\text{V} = \boxed{4.28\text{V}}$$

Applied KCL on node B in **Figure 8(a)**, The relationship  $R_1$  and  $R_2$  can be calculated ( $I_1$  is the current through  $R_{B1}$ ,  $I_2$  is the current through  $R_{B2}$ ):

$$I_1 - I_2 = \frac{V_{CC} - V_B}{R_{B1}} - \frac{V_B - 0}{R_{B2}} = I_B$$

$$\frac{10.72}{R_{B1}} - \frac{4.28}{R_{B2}} = 6.05 \mu A$$

$$R_{B1} = \frac{10.72 * R_{B2}}{6.05 \mu A * R_{B2} + 4.28}$$

Assume  $R_{B2} = 10k\Omega$ :

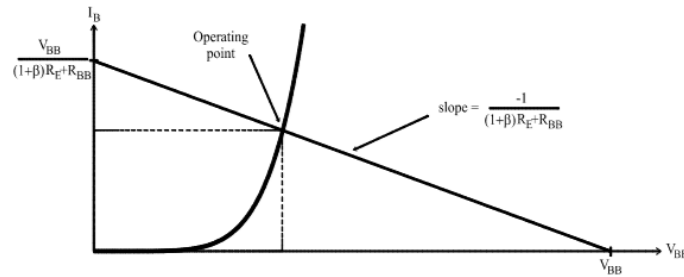
$$R_{B1} = 24697.62 \Omega$$

Thevenin Equivalent is applied on (a) to get (b) in **Figure 8**.

$$R_{BB} = R_{B1} || R_{B2} = 7117.96 \Omega$$

$$V_{BB} = V_{CC} * \left[ \frac{R_{B2}}{R_{B1} + R_{B2}} \right] = 4.323 V$$

To verify the assumed value is valid:



**Figure 9.**  $I_B$  vs  $V_{BE}$

The calculated values are plugged in to get the slope and the y-intercept:

$$\text{Slope} = \frac{-1}{(1+166.67)*3659.23+7117.96} = -1.61*10^{-6}$$

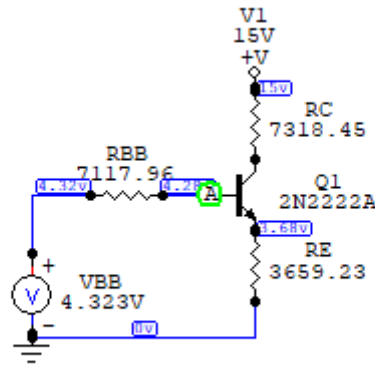
$$\text{Y-intercept} = \frac{4.323 V}{(1+166.67)*3659.23+7117.96} = 6.965*10^{-6}$$

At the operating point:

$$I_B = \text{Y-intercept} + V_{BE} * \text{Slope} = 6.965*10^{-6} + 0.601V * -1.61*10^{-6} \approx 6.0 \mu A$$

Thus, the assumed values are valid.

The figure below shows the Thevenin Equivalent circuit with the calculated resistances. The DC operating points are measured in this circuit.



**Figure 10.** The Thevenin equivalent circuit with the calculated resistance

**Table 3.** The measurements of DC operating points.

	$I_C$ (mA)	$I_B$ ( $\mu$ A)	$I_E$ (mA)	$V_C$ (V)	$V_B$ (V)	$V_E$ (V)
Measured	0.999	6.034	1.005	7.69	4.28	3.68
Calculated	1.0	6.05	1.00605	7.68	4.28	3.68

As shown in **Table 3**, with the chosen resistors, the measured values and the calculated values are extremely close. Therefore, the chosen resistors RB1 and RB2 are useable to bias the BJT.

## ii) Using 1/3<sup>rd</sup> Rule

For **Figure 8**, apply the 1<sup>st</sup> version of 1/3<sup>rd</sup> rule ( $I_C = 1\text{mA}$ ), where  $I_1$  is the current through  $R_{B1}$ ,  $I_2$  is the current through  $R_{B2}$ :

$$V_B = \frac{1}{3} V_{CC} = 15\text{V}/3 = \boxed{5\text{V}}$$

$$V_C = \frac{2}{3} V_{CC} = 15\text{V} \cdot 2/3 = \boxed{10\text{V}}$$

$$V_E = V_B - V_{BE} = 5\text{V} - 0.6\text{V} = \boxed{4.4\text{V}}$$

$$I_B = \frac{I_C}{\beta} = 1\text{mA} / 166.67 = \boxed{6.0\text{ }\mu\text{A}}$$

$$I_E = I_B + I_C = 6.0\text{ }\mu\text{A} + 1.0\text{mA} = \boxed{1.006\text{ mA}}$$

$$I_1 = \frac{I_E}{\sqrt{\beta}} = \frac{1.006\text{mA}}{\sqrt{166.67}} = 77.92\text{ }\mu\text{A}$$

$$I_2 = I_1 - I_B = 77.92\text{ }\mu\text{A} - 6.0\text{ }\mu\text{A} = 71.92\text{ }\mu\text{A}$$

$$R_C = \frac{V_{CC} - V_C}{I_C} = \frac{15\text{V} - 10\text{V}}{1\text{mA}} = \boxed{5\text{ k}\Omega}$$

$$R_{B1} = \frac{V_{CC} - V_B}{I_1} = \frac{15\text{V} - 5\text{V}}{77.92\text{ }\mu\text{A}} = \boxed{128.29\text{ k}\Omega}$$



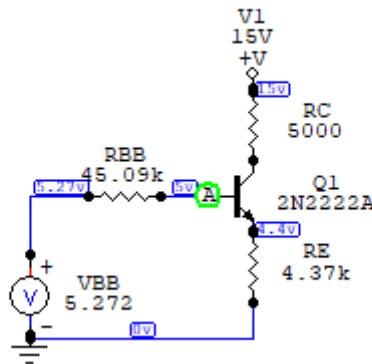
$$R_{B2} = \frac{V_B - 0}{I_2} = \frac{5V}{71.92\mu A} = \boxed{69.52 \text{ k}\Omega}$$

$$V_{BB} = V_{CC} * \left[ \frac{R_{B2}}{R_{B1} + R_{B2}} \right] = \boxed{5.27V}$$

$$R_{BB} = R_{B1} \parallel R_{B2} = \boxed{45.09 \text{ k}\Omega}$$

$$R_E = \frac{V_E - 0}{I_E} = \frac{4.4V}{1.006mA} = \boxed{4.37 \text{ k}\Omega}$$

The circuit below shows the calculated resistances and the DC measurements:



**Figure 11.** The 1/3<sup>rd</sup> rule circuit

**Table 4.** The measurements of DC operating points.

	$I_C$ (mA)	$I_B$ ( $\mu A$ )	$I_E$ (mA)	$V_C$ (V)	$V_B$ (V)	$V_E$ (V)
Measured	1.001	5.970	1.007	9.993	5.003	4.402
Calculated	1.000	6.000	1.006	10.000	5.000	4.400

As shown in **Table 4**, under the 1/3<sup>rd</sup> rule, the calculated values are very close to the actual values which are from the simulation.

### iii) The use of the closest commonly available resistors

**Table 5.** The calculated and standard values

	Calculated ( $\Omega$ )	Standard ( $\Omega$ )
$R_{B1}$	128.29 k	130 k
$R_{B2}$	69.52 k	68 k
$R_C$	5 k	5.1 k
$R_E$	4.37 k	4.3 k
$R_{BB}$	45.09 k	44.65 k (calculated)

\*The standard values are from: <http://ecee.colorado.edu/~mcclurel/resistorsandcaps.pdf>

The Standard-value resistors are placed into the circuit in Figure 11. The DC operating points are measured and listed below.

**Table 6.** The DC operating point with the assumed and standard resistors.

	$I_C$ (mA)	$I_B$ ( $\mu$ A)	$I_E$ (mA)	$V_C$ (V)	$V_B$ (V)	$V_E$ (V)
Assumed	1.001	5.970	1.007	9.993	5.003	4.402
Standard	1.023	6.064	1.017	9.812	5.001	4.400

After the resistors are replaced by the standard resistors, the operating currents and voltages does not have an obvious change compare to the assumed resistors. Therefore, these standard resistors can be used to bias this BJT.

#### iv) Compare the DC operating points in i), ii) and iii)

**Table 7.** The DC operating points in non-1/3<sup>rd</sup> rule, 1/3<sup>rd</sup> rule and the standard resistors.

	$I_C$ (mA)	$I_B$ ( $\mu$ A)	$I_E$ (mA)	$V_C$ (V)	$V_B$ (V)	$V_E$ (V)
Non-1/3 <sup>rd</sup>	0.999	6.034	1.005	7.690	4.280	3.680
1/3 <sup>rd</sup>	1.001	5.970	1.007	9.993	5.003	4.402
Standard	1.023	6.064	1.017	9.812	5.001	4.400

As shown in **Table 7**, the operating current in those three methods are comparable. However, the operating voltages ( $V_C$ ,  $V_B$  and  $V_E$ ) have high differences. The 1/3<sup>rd</sup>-rule and the standard-resistors models have relative higher operating voltages than the non-1/3<sup>rd</sup> rule model. In the non-1/3<sup>rd</sup> rule model, the resistors are quite small ( $\sim 10\text{k}\Omega$ ) compare to the resistors used in the ii) and iii) ( $\sim 50\text{k}\Omega$ ). The high resistance can have more voltages than lower resistors.  $V_{CC}$  is constant. When the chosen resistors have high resistance, the voltages that go to the BJT (say  $V_C$ ,  $V_B$  and  $V_E$ ) are lower.

#### (d) The replacement of 2N3904 and 2N4401

In the standard-resistor circuit, the 2N2222A is replaced by 2N3904 and 2N4401. The measured DC operating points are listed in the **Table 7** below.

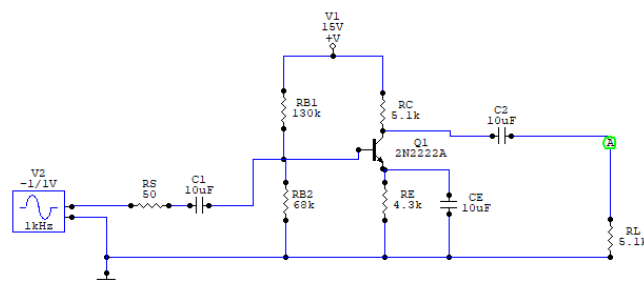
**Table 7.** The DC operating points of 2N2222A, 2N3904 and 2N4401 under the standard-resistor condition.

Transistors	$I_C$ (mA)	$I_B$ ( $\mu$ A)	$I_E$ (mA)	$V_C$ (V)	$V_B$ (V)	$V_E$ (V)
2N2222A	1.023	6.064	1.017	9.812	5.001	4.400
2N3904	0.982	8.287	0.990	9.994	4.902	4.265
2N4401	0.996	6.761	1.003	9.919	4.970	4.313

For all the three transistors,  $I_C$  is not 0 A, and  $V_{CE}$  ( $V_C - V_E$ ) is higher than 0.2V. According to the **Figure 7**, these transistors are not in the cut-off region or saturation region because  $I_C$  is not equal to 0 A and  $V_{CE}$  is higher than 0.2 V. Even though the DC operating points of the three transistors have little differences, the standard-resistor circuit still can be used to bias all the three transistors since they are all in active region, and the operating points are reasonable.

## Part II

The Common Emitter amplifier is built by the given resistor and three 10 $\mu$ F capacitors. The load resistor of **5.1 k $\Omega$**  is chosen because the output resistance  $R_C$  is 5.1 k $\Omega$ . The same resistance transfers the maximum **power**. The circuit is shown in **Figure 12** (for 2N2222A).



**Figure 12.** The Common Emitter Amplifier circuit

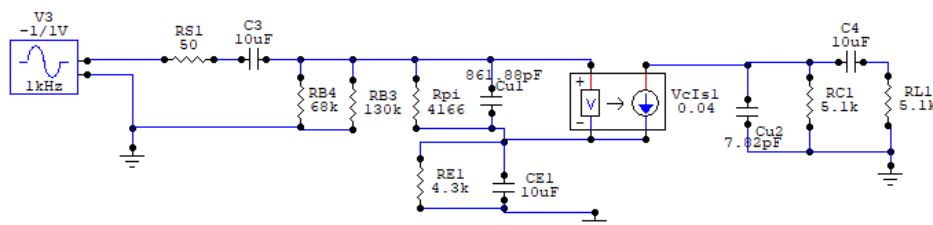
### (a) Poles and Zeros

For **2N2222A**, to calculate the poles and zeros, the circuit is converted to the small-signal model. In this model,  $C_\mu$  and  $C_\pi$  can be calculated by the formula ( $C_{JE}$ ,  $C_{JC}$ ,  $M_{JC}$ ,  $V_{JC}$  and  $TF$  are found in SPICE in *Circuitmaker*):

$$C_\pi \approx 2 * C_{JE} + TF * g_m = \mathbf{74.88 \text{ pF}}$$

$$C_\mu \approx C_{JC} / (1 + V_{CB} / V_{JC})^{M_{JC}} = \mathbf{7.74 \text{ pF}}$$

The **Miller Theorem** is applied to the small-signal model ( $k = -100.68$ ). The circuit becomes:



**Figure 13.** The Common Emitter Amplifier circuit with after Miller Theorem

$\omega_{Lz1}$  and  $\omega_{Lz2}$  are at zero since  $C3$  and  $C4$  are coupling. To find the  $\omega_{Lz3}$ , the admittance of the Emitter is 0. Thus,  $\omega_{Lz3} = 1 / (R_E * C_E) = \mathbf{3.70 \text{ Hz}}$

The Low-frequency poles can be calculated:

At the output:

$$\omega_{Lp2} = \frac{1}{10\mu F * (5.1k + 5.1k)\Omega} = \mathbf{1.56 \text{ Hz}}$$

At the input, the SC/OC test is applied on  $C3$  and  $CE1$ :

$$\tau_{SC}^{C3} = 10\mu F * (50 + 68k || 130k || 4166) = 0.0386s$$

$$\tau_{SC}^{CE} = 10\mu F * (4.3k || \frac{4166 + (68k || 130k || 50)}{1 + 166.7}) = 0.00025s$$

$\tau_{SC}^{CE}$  has smaller time constant (higher frequency) so it is valid. The  $\omega_{Lp3} = 1 / \tau_{SC}^{CE} = \mathbf{636.67 \text{ Hz}}$

Then, OC test is applied to  $C3$ :

$$\tau_{C3}^{oc} = 10\mu F * (50 + 68k || 130k || (4166 + 167.7 * 4.3k)) = 0.421s$$

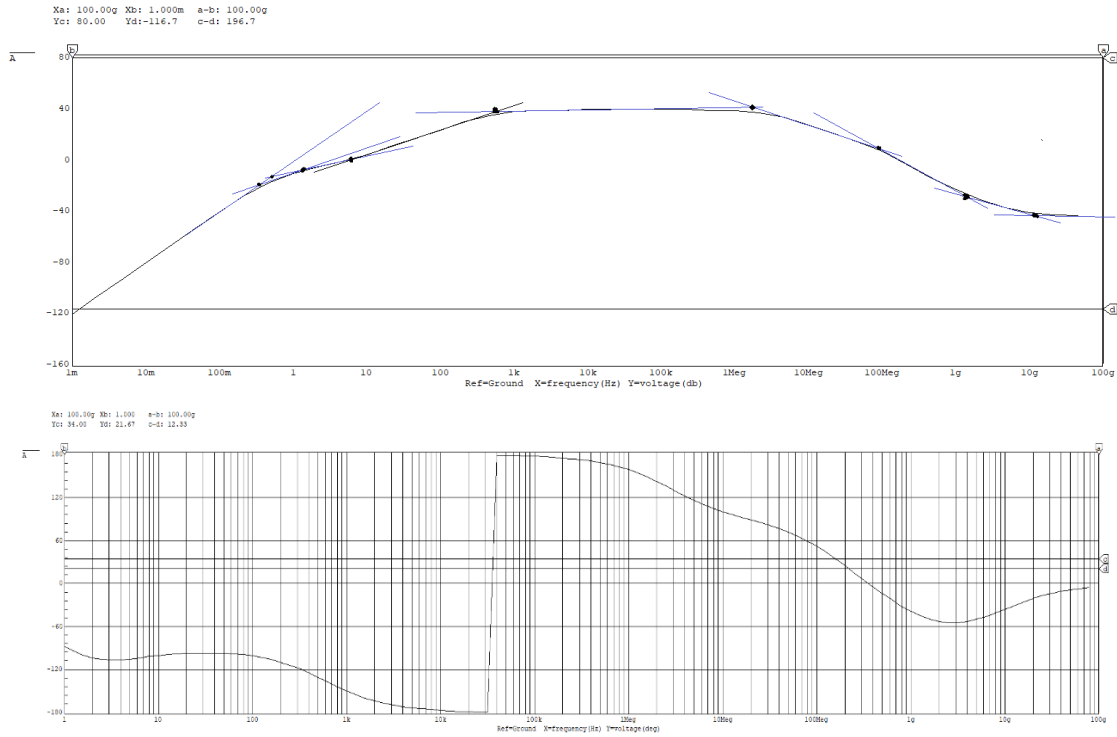
$$\omega_{Lp1} = 1/\tau_{C3}^{oc} = \boxed{0.38 \text{ Hz}}$$

Then, the High-frequency poles can be calculated:

At the input: 
$$\omega_{Hp1} = \frac{1}{861.88pF * (50 || 68k || 130k || 4166)\Omega} = \boxed{3.74 \text{ MHz}}$$

At the output: 
$$\omega_{Hp2} = \frac{1}{7.82pF * (5.1k || 5.1k)\Omega} = \boxed{8.57 \text{ MHz}}$$

The Bode and Phasor plot are below:



**Figure 14.** The BOD and PHR diagram of 2N2222A

**Table 8.** Pole and Zeros for 2N2222A

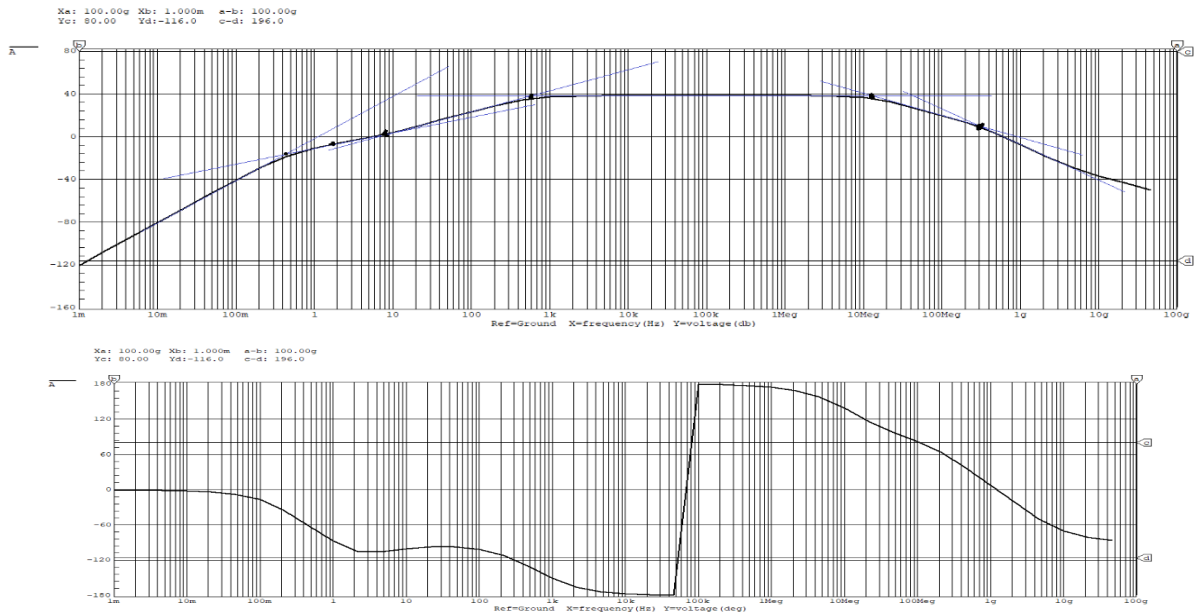
(Hz)	$\omega_{Lp1}$	$\omega_{Lp2}$	$\omega_{Lp3}$	$\omega_{Lz1}/Lz2$	$\omega_{Lz3}$	$\omega_{Hp1}$	$\omega_{Hp2}$
Calculated	0.38	1.56	636.67	0	3.70	3.74M	8.57M
Measured	0.36	1.58	648.6	0	3.63	3.16M	157.6M

The table shows that the calculated low-frequency poles and zeros are comparative to the measured value. However, the high-frequency poles are shifted a huge scale. The reason is that the calculated values are based on the **Miller Theorem**. In addition, the measured graph shows two high-frequency zeros which cannot be calculated since the H-frequency zeros tends to be  $\infty$ .

For **2N3904**, the same bias circuit is used and the 2N2222A is replaced by 2N3904. The  $C_{\pi}$  and  $C_{\mu}$  can be calculated by the same formula.  $C_{\pi} = 25 \text{ pF}$  ;  $C_{\mu} = 1.75 \text{ pF}$ . The low-frequency poles, zeros and high-frequency poles are calculated by the same method used in the calculations of poles and zeros of 2N2222A. The result and the Bode and phasor diagram are below:

**Table 9.** Pole and Zeros for 2N3904

(Hz)	$\omega_{Lp1}$	$\omega_{Lp2}$	$\omega_{Lp3}$	$\omega_{Lz1}/Lz2$	$\omega_{Lz3}$	$\omega_{Hp1}$	$\omega_{Hp2}$
Calculated	0.38	1.56	636.67	0	3.70	15.89M	35.26M
Measured	0.40	1.59	664.9	0	3.65	14.01M	299.0M

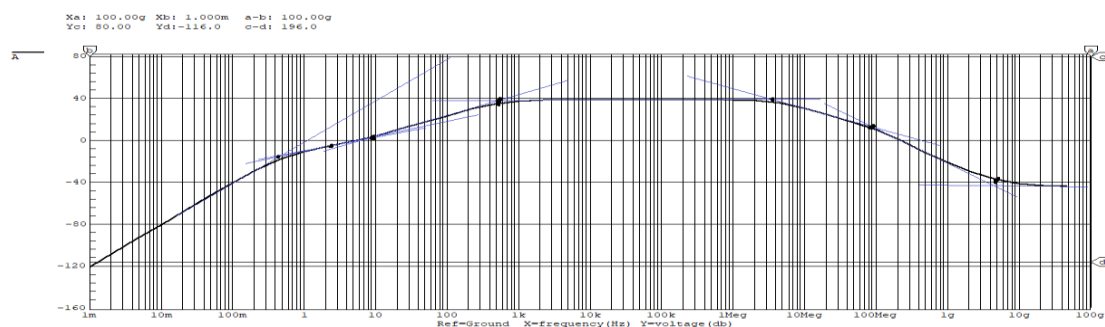
**Figure 15.** The BOD and PHR diagram of 2N3904

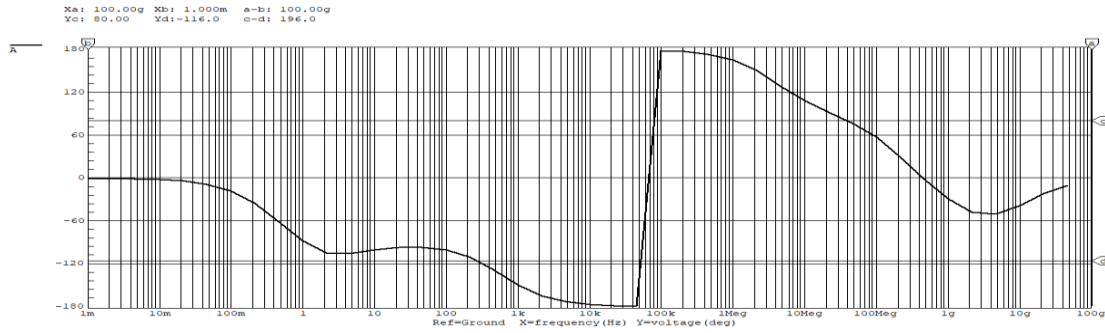
The calculated values are comparative to the measured values except the high-frequency poles. Even though there are two high-frequency zeros on the measured diagram, the zeros cannot be calculated since the capacitances tend to be  $\infty$ .

For **2N4401**, the same bias circuit is used and the 2N3904 is replaced by 2N4401. The  $C_\pi$  and  $C_\mu$  can be calculated by the same formula.  $C_\pi = 67.28$  pF ;  $C_\mu = 5.15$  pF. The low-frequency poles, zeros and high-frequency poles are calculated by the same method used in the calculations of poles and zeros of 2N2222A. The result and the Bode and phasor diagram are below:

**Table 10.** Pole and Zeros for 2N4401

(Hz)	$\omega_{Lp1}$	$\omega_{Lp2}$	$\omega_{Lp3}$	$\omega_{Lz1}/Lz2$	$\omega_{Lz3}$	$\omega_{Hp1}$	$\omega_{Hp2}$
Calculated	0.38	1.56	636.67	0	3.70	5.46M	12.00M
Measured	0.37	1.53	658.3	0	3.65	3.82M	84.21M



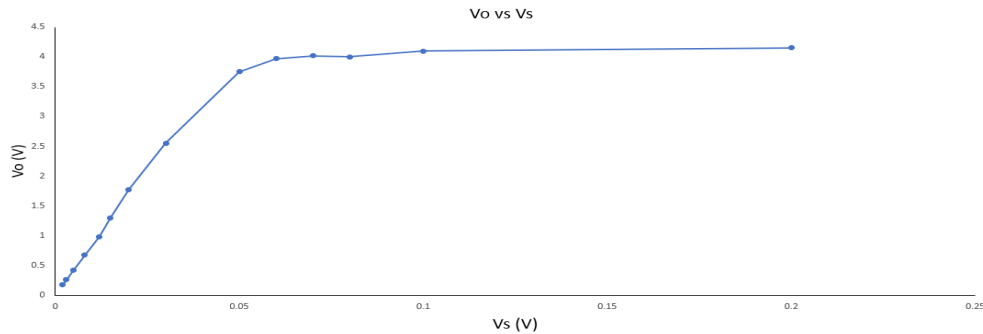


**Figure 16.** The BOD and PHR diagram of 2N4401

As shown above, the calculated values and measured values are also similar. The high-frequency zeros on the figure still cannot be calculated. The shift of bandwidths of 2N2222A, 2N3901 and 2N4401 are different because they are from the small signal model and the Miller's Theorem. The different  $C_\pi$  and  $C_\mu$  provides different high-frequency poles.

### (b) Various Amplitude of input signal

From **Figure 14**, the mid-band bandwidth is from 630 Hz to 3.1 MHz. Therefore, **10 kHz** is chosen for the generator. The diagram that represents the relationship between  $V_s$  and  $V_o$  is below:



**Figure 17.** The diagram of  $V_s$  vs  $V_o$

It can be seen from the figure that the relationship between the input signal and the output signal becomes non-linear near  $V_s = 0.05$  V. The reason is when  $V_s$  is greater than this value, the transistor is in saturated mode, so the output signal is not significant anymore.

### (c) Input Impedance at mid band

For **2N2222A**, the Oscilloscope probe is located at the right node of  $C_1$  in **Figure 12** (the  $50 \Omega$  resistor is removed). The peak to peak voltage and peak to peak current are measured:  $V_{in} = 0.02$  V ;  $I_{in} = 3.98 \mu A$ . Therefore, the measured input impedance is equal to  $Z_{in} = V_{in} / I_{in} = \boxed{5.03 \text{ k}\Omega}$ . The calculated input impedance is equal to  $Z_{in} = R_{B1} || R_{B2} || R_\pi = \boxed{3.81 \text{ k}\Omega}$

For **2N3904** and **2N4401**, the same method above is used to get the measured input impedance and the calculated input impedance. The results are listed in the table below:

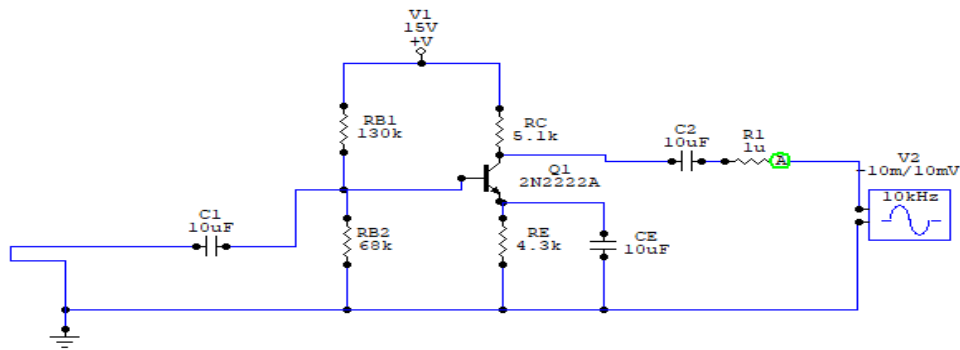
**Table 11.** The input impedance of 2N4401, 2N3904 and 2N4401

Model	Measured (k $\Omega$ )	Calculated (k $\Omega$ )
2N2222A	5.03	3.81
2N3904	4.16	3.40
2N4401	4.22	2.80

From the table, the calculated impedances are relatively smaller than the measured values. Even though the calculated values and the measured values have small deviations, the calculated values are still expected.

#### (d) Output Impedance at mid band

To calculate the output impedance, the input generator is shorted, and the RL is removed. Another generator is moved to the load terminals with a small resistor in series to measure the current.

**Figure 18.** The circuit to measure the output impedance

For **2N2222A**, the Oscilloscope probe is located at the right node of R1 in **Figure 18** to measure the current. The peak to peak voltage and peak to peak current are measured:  $V_{out} = 0.02V$  ;  $I_{out} = 3.85\mu A$ . Therefore, the measured output impedance is equal to  $Z_{out} = V_{out} / I_{out} = \boxed{5.19 \text{ k}\Omega}$ . The calculated output impedance is the load impedance, in this case,  $Z_{out} = \boxed{5.1 \text{ k}\Omega}$ . For **2N3904** and **2N4401**, the same method above is used to get the measured output impedance and the calculated output impedance. The results are listed in the table below:

**Table 12.** The output impedance of 2N4401, 2N3904 and 2N4401

Model	Measured (k $\Omega$ )	Calculated (k $\Omega$ )
2N2222A	5.19	5.1
2N3904	5.21	5.1
2N4401	5.23	5.1

From **Table 12**, the calculated output impedances are close to the measured output impedances for all the three models. It is safe to say that the calculated values are accurate.

### **(e) The best-performance transistor**

In **Figure 14, 15 and 16**, 2N3904 and 2N4401 have the highest mid-band gain (40 decibel) at the mid band, which is higher than the mid-band gain of 2N2222A (slightly lower than 40 dB). In addition, the 2N2222A has the bandwidth from 600 Hz – 3.74 MHz; 2N3904 has the bandwidth from 600 Hz – 15.89 MHz which is the widest in these three transistors; 2N4401's bandwidth is from 600Hz – 5.46 MHz. Among them, 2N3904 has the highest mid-band gain and the widest work region (bandwidth). Therefore, **2N3904** gives the best performance.

## **Conclusion**

In part I, the transistor is biasing by designing a bias circuit. The circuit is converted to the small-signal model by calculating the  $\beta$ ,  $R_\pi$ ,  $g_m$  and  $R_o$ . The DC operating points are then measured in the *Circuitmaker*. In this circuit, the resistance ( $R_{B1}$ ,  $R_{B2}$ ,  $R_C$ ,  $R_E$ ) are determined to make sure the transistor can work at the DC operating points. To calculate and determine these resistances, the Miller Theorem and the 1/3<sup>rd</sup> rule are used. In part II, a common-emitter amplifier is investigated. The location of low-frequency and high-frequency poles and zeros are calculated and compared with the measured values. The calculated values are reasonable. In addition, the bandwidths and the mid-band gains of 2N2222A, 2N3904 and 2N4401 are compared, and a summary is conducted that 2N3904 has the best performance due to the widest bandwidth and the highest mid-band gain. This mini project provides advanced knowledge of BJTs, which is useful in the future career.



## Reference

- [1] ELEC 301 Notes
- [2] A. Sedra and K. Smith, “Microelectronic Circuits.”5<sup>th</sup>(or higher)Ed., Oxford University Press, New York.
- [3] CircuitMaker™ (or other circuit simulator) User’s Manual.
- [4] Notes on Canvas.
- [5] ELEC 201 Notes