

Naive Bayes Spam Classification Training Process

1. Data Collection

Gather a dataset of labeled emails. For example:

- Email 1 (Spam): "Get rich quick! Buy our product now!"
- Email 2 (Ham): "Hey friend, want to grab coffee tomorrow?"
- Email 3 (Spam): "Congratulations! You've won a free iPhone!"
- Email 4 (Ham): "Please find attached the report for our meeting."
- Email 5 (Spam): "Enlarge your profits with our business opportunity!"

2. Feature Extraction

Select key words as features:

["rich", "buy", "friend", "coffee", "won", "free", "report", "meeting", "business"]

3. Training Data Preparation

Create a table showing word occurrence in emails:

Email	Class	rich	buy	friend	coffee	won	free	report	meeting	business
1	Spam	1	1	0	0	0	0	0	0	0
2	Ham	0	0	1	1	0	0	0	0	0
3	Spam	0	0	0	0	1	1	0	0	0
4	Ham	0	0	0	0	0	0	1	1	0
5	Spam	0	0	0	0	0	0	0	0	1

4. Calculating Probabilities

a) Prior Probabilities:

- $P(\text{Spam}) = 3/5 = 0.6$
- $P(\text{Ham}) = 2/5 = 0.4$

b) Likelihood Probabilities:

Calculate $P(\text{word}|\text{Spam})$ and $P(\text{word}|\text{Ham})$ for each word.

Example calculations:

- $P(\text{"rich"}|\text{Spam}) = 1/3$
- $P(\text{"rich"}|\text{Ham}) = 0/2 = 0$
- $P(\text{"friend"}|\text{Spam}) = 0/3 = 0$
- $P(\text{"friend"}|\text{Ham}) = 1/2 = 0.5$

Apply Laplace smoothing to avoid zero probabilities:

- $P(\text{"rich"}|\text{Spam}) = (1+1) / (3+2) = 0.4$
- $P(\text{"rich"}|\text{Ham}) = (0+1) / (2+2) = 0.25$

5. Storing the Model

The trained model consists of:

- Prior probabilities: $P(\text{Spam})$ and $P(\text{Ham})$
- Likelihood probabilities: $P(\text{word}|\text{Spam})$ and $P(\text{word}|\text{Ham})$ for each word

6. Classification Step

To classify a new email:

1. Extract features (words) from the new email.
2. Calculate $P(\text{Spam}|\text{email})$ and $P(\text{Ham}|\text{email})$ using the stored probabilities:
 $P(\text{Spam}|\text{email}) \propto P(\text{Spam}) * \prod P(\text{word}|\text{Spam})$ for each word in the email
 $P(\text{Ham}|\text{email}) \propto P(\text{Ham}) * \prod P(\text{word}|\text{Ham})$ for each word in the email
3. Compare the two probabilities:
 - If $P(\text{Spam}|\text{email}) > P(\text{Ham}|\text{email})$, classify as Spam
 - Otherwise, classify as Ham

Example: New email: "Quick cash opportunity"

$$P(\text{Spam}|\text{email}) \propto 0.6 * P(\text{"quick"}|\text{Spam}) * P(\text{"cash"}|\text{Spam}) * P(\text{"opportunity"}|\text{Spam})$$
$$P(\text{Ham}|\text{email}) \propto 0.4 * P(\text{"quick"}|\text{Ham}) * P(\text{"cash"}|\text{Ham}) * P(\text{"opportunity"}|\text{Ham})$$

Calculate these values using the stored probabilities and compare them to determine the classification.

Note: In practice, we often work with log probabilities to avoid underflow issues with very small numbers.