































Notes for Mathematical System

2018.Oct.31

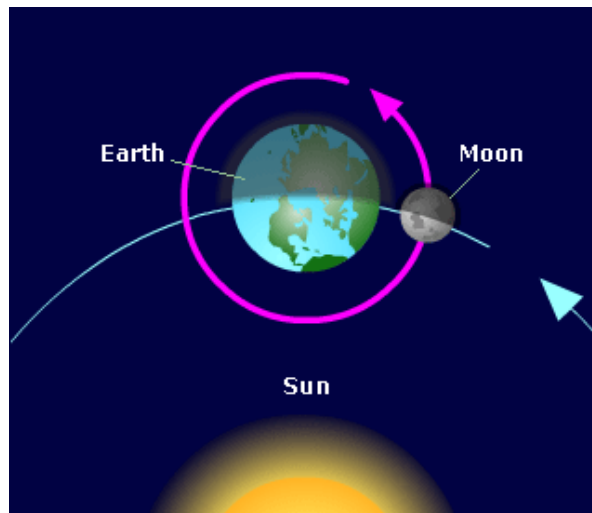
1. Representation

1.1 Categorical & Numerical

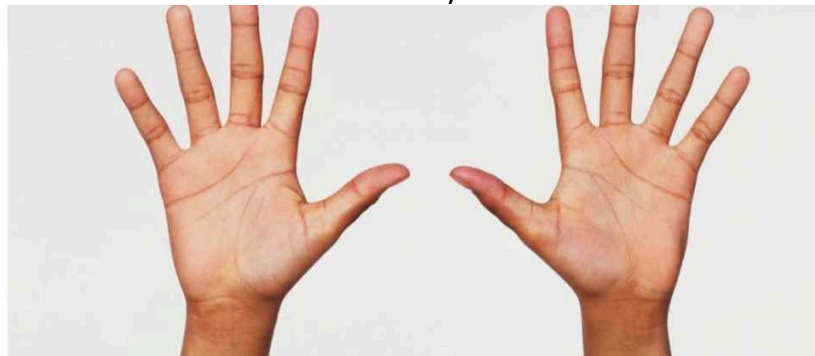
1.2 Numerical System:

1		11		100	
2		12		200	
3		20		300	
4		30		400	
5		40		500	
6		50		600	
7		60		700	
8		70		800	
9		80		900	
10		90		1000	

100-based-system



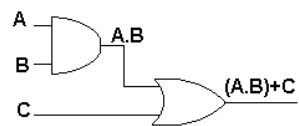
12-based-system



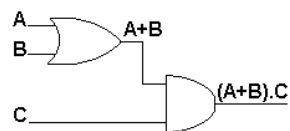
Decimal(Ten)/Quniary(Five) Based-System



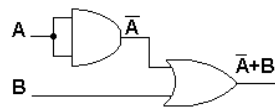
Electronic



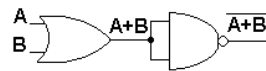
A and B high or C high will make the output high.



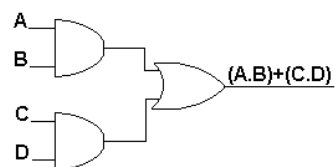
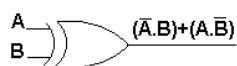
A or B high and C high will make the output high.



A low or B high will make the output high.



The long bar above the output means that the output goes low when A or B go high.



Binary Logic

Logic gates

Graphic Symbols and Input-Output Signals for Logic gates:

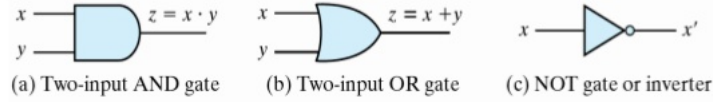


Fig. 1.4 Symbols for digital logic circuits

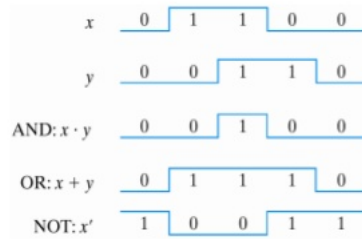


Fig. 1.5 Input-Output signals for gates

Binary-Based Operation

```
Offset(h) 00 01 02 03 04 05 06 07 08 09 0A 0B 0C 0D 0E 0F
00000660 48 65 6C 6C 6F 2C 20 77 6F 72 6C 64 2E 36 34 30 Hello, world.640
00000670 30 39 30 39 31 36 35 30 30 30 31 39 36 32 33 0D 090916500019623.
00000680 0A 3A 31 30 31 45 35 30 30 30 39 30 39 33 36 35 ..:101E5000909365
00000690 30 30 38 30 39 33 36 34 30 30 32 46 35 46 33 46 00809364002F5F3F
000006A0 34 46 38 30 39 31 36 36 30 31 45 46 0D 0A 3A 31 4F80916601EF...:1
000006B0 54 68 69 73 20 69 73 20 61 20 68 65 78 61 64 65 This is a hexade
000006C0 63 69 6D 61 6C 20 74 75 74 6F 72 69 61 6C 21 46 cimal tutorial!F
000006D0 38 39 34 45 31 39 39 33 36 0D 0A 3A 31 30 31 45 894E19936...:101E
000006E0 37 30 30 30 00 01 02 03 04 05 06 07 08 09 0A 0B 7000.....
000006F0 0C 0D 0E 0F 10 11 12 13 14 15 16 17 18 19 1A 1B .....
00000700 1C 1D 1E 1F 20 21 22 23 24 25 26 27 28 29 2A 2B .... !"$%&'()*+
00000710 2C 2D 2E 2F 30 31 32 33 34 35 36 37 38 39 3A 3B ,-. /0123456789;:
00000720 3C 3D 3E 3F 40 41 42 43 44 45 46 47 48 49 4A 4B <=>?@ABCDEFGHIJK
00000730 4C 4D 4E 4F 50 51 52 53 54 55 56 57 58 59 5A 5B LMNOPQRSTUVWXYZ[
00000740 5C 5D 5E 5F 60 61 62 63 64 65 66 67 68 69 6A 6B \]^_`abcdefghijk
00000750 6C 6D 6E 6F 70 71 72 73 74 75 76 77 78 79 7A 7B lmnopqrstuvwxyz{
00000760 7C 7D 7E 7F 80 81 82 83 84 85 86 87 88 89 8A 8B |}~.€.,f_m~t~%$<
00000770 8C 8D 8E 8F 90 91 92 93 94 95 96 97 98 99 9A 9B Œ.Ž...'"*~"m$>
00000780 9C 9D 9E 9F A0 A1 A2 A3 A4 A5 A6 A7 A8 A9 AA AB œ.žY ¡¢£¥¦§¨ª«
00000790 AC AD AE AF B0 B1 B2 B3 B4 B5 B6 B7 B8 B9 BA BB ¬.®¯°±²³´µ¶·¸¹º»
000007A0 BC BD BE BF C0 C1 C2 C3 C4 C5 C6 C7 C8 C9 CA CB ¼½¾¿ÀÁÂÃÄÅÆÇÈÉÊË
000007B0 CC CD CE CF D0 D1 D2 D3 D4 D5 D6 D7 D8 D9 DA DB ÌÍÎÏÐÑÒÓÔÕÖ×ØÙÚÛ
000007C0 DC DD DE DF E0 E1 E2 E3 E4 E5 E6 E7 E8 E9 EA EB ÜÝÞßàáâãäåæçèéêë
000007D0 EC ED EE EF F0 F1 F2 F3 F4 F5 F6 F7 F8 F9 FA FB ìíîïðñóôõö÷øùúû
000007E0 FC FD FE FF B3 39 43 0D 0A 3A 31 30 31 45 44 30 úýþÿ39C...:101ED0
000007F0 30 30 35 37 30 30 45 38 39 35 33 32 39 36 30 32 005700E895329602
```

Hexadecimal	Decimal	Binary
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

Heximal (16)

ASCII Table

Dec	Hex	Oct	Char	Dec	Hex	Oct	Char	Dec	Hex	Oct	Char	Dec	Hex	Oct	Char
0	0	0		32	20	40	[space]	64	40	100	@	96	60	140	`
1	1	1		33	21	41	!	65	41	101	A	97	61	141	a
2	2	2		34	22	42	"	66	42	102	B	98	62	142	b
3	3	3		35	23	43	#	67	43	103	C	99	63	143	c
4	4	4		36	24	44	\$	68	44	104	D	100	64	144	d
5	5	5		37	25	45	%	69	45	105	E	101	65	145	e
6	6	6		38	26	46	&	70	46	106	F	102	66	146	f
7	7	7		39	27	47	'	71	47	107	G	103	67	147	g
8	8	10		40	28	50	(72	48	110	H	104	68	150	h
9	9	11		41	29	51)	73	49	111	I	105	69	151	i
10	A	12		42	2A	52	*	74	4A	112	J	106	6A	152	j
11	B	13		43	2B	53	+	75	4B	113	K	107	6B	153	k
12	C	14		44	2C	54	,	76	4C	114	L	108	6C	154	l
13	D	15		45	2D	55	-	77	4D	115	M	109	6D	155	m
14	E	16		46	2E	56	.	78	4E	116	N	110	6E	156	n
15	F	17		47	2F	57	/	79	4F	117	O	111	6F	157	o
16	10	20		48	30	60	0	80	50	120	P	112	70	160	p
17	11	21		49	31	61	1	81	51	121	Q	113	71	161	q
18	12	22		50	32	62	2	82	52	122	R	114	72	162	r
19	13	23		51	33	63	3	83	53	123	S	115	73	163	s
20	14	24		52	34	64	4	84	54	124	T	116	74	164	t
21	15	25		53	35	65	5	85	55	125	U	117	75	165	u
22	16	26		54	36	66	6	86	56	126	V	118	76	166	v
23	17	27		55	37	67	7	87	57	127	W	119	77	167	w
24	18	30		56	38	70	8	88	58	130	X	120	78	170	x
25	19	31		57	39	71	9	89	59	131	Y	121	79	171	y
26	1A	32		58	3A	72	:	90	5A	132	Z	122	7A	172	z
27	1B	33		59	3B	73	;	91	5B	133	[123	7B	173	{
28	1C	34		60	3C	74	<	92	5C	134	\	124	7C	174	
29	1D	35		61	3D	75	=	93	5D	135]	125	7D	175	}
30	1E	36		62	3E	76	>	94	5E	136	^	126	7E	176	~
31	1F	37		63	3F	77	?	95	5F	137	_	127	7F	177	

0020	0	0030	@	0040	P	0050	`	0060	p	0070		00A0	°	00B0	À	00C0	Ð	00D0	à	00E0	ð	00F0
0021	!	0031	A	0041	Q	0051	a	0061	q	0071	i	00A1	±	00B1	Á	00C1	Ñ	00D1	á	00E1	ñ	00F1
0022	"	0032	B	0042	R	0052	b	0062	r	0072	¢	00A2	²	00B2	Â	00C2	Ò	00D2	â	00E2	ò	00F2
0023	#	0033	C	0043	S	0053	c	0063	s	0073	£	00A3	³	00B3	Ã	00C3	Ó	00D3	ã	00E3	ó	00F3
0024	\$	0034	D	0044	T	0054	d	0064	t	0074	¤	00A4	´	00B4	Ä	00C4	Ô	00D4	ä	00E4	ô	00F4
0025	%	0035	E	0045	U	0055	e	0065	u	0075	¥	00A5	µ	00B5	Å	00C5	Õ	00D5	å	00E5	õ	00F5
0026	&	0036	F	0046	V	0056	f	0066	v	0076	¦	00A6	¶	00B6	Æ	00C6	Ö	00D6	æ	00E6	ö	00F6
0027	'	0037	G	0047	W	0057	g	0067	w	0077	§	00A7	·	00B7	Ç	00C7	×	00D7	ç	00E7	÷	00F7
0028	(0038	H	0048	X	0058	h	0068	x	0078	¨	00A8	,	00B8	È	00C8	Ø	00D8	è	00E8	ø	00F8
0029)	0039	I	0049	Y	0059	i	0069	y	0079	©	00A9	¹	00B9	É	00C9	Ù	00D9	é	00E9	ù	00F9
002A	*	003A	J	004A	Z	005A	j	006A	z	007A	ª	00AA	º	00BA	Ê	00CA	Ú	00DA	ê	00EA	ú	00FA
002B	+	003B	K	004B	[005B	k	006B	{	007B	«	00AB	»	00BB	Ë	00CB	Û	00DB	ë	00EB	û	00FB
002C	,	003C	L	004C	\	005C	l	006C		007C	¬	00AC	¼	00BC	Ì	00CC	Ü	00DC	ì	00EC	ü	00FC
002D	-	003D	M	004D]	005D	m	006D	}	007D	¯	00AD	½	00BD	Í	00CD	Ý	00DD	í	00ED	ý	00FD
002E	.	003E	N	004E	^	005E	n	006E	~	007E	®	00AE	¾	00BE	Î	00CE	Þ	00DE	î	00EE	þ	00FE
002F	/	003F	O	004F	_	005F	o	006F		007F	™	00AF	¿	00BF	Ï	00CF	ß	00DF	ï	00EF	ÿ	00FF

Aegean_Numbers

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03	04	05	06	07	08	09	0A	0B	0C	0D	0E	0F	UTF8
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𠂔	𠂕	𠂖	𠂗	𠂘	𠂙	𠂚	𠂛	𠂜	𠂝	𠂞	𠂟	𠂠	E5A490
𠂡	𠂢	𠂣	𠂤	𠂥	𠂦	𠂧	𠂨	𠂩	𠂪	𠂫	𠂬	𠂭	E5A4A0
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𠃢	𠃣	𠃤	𠃥	𠃦	𠃧	𠃨	𠃩	𠃪	𠃫	𠃬	𠃭	𠃮	E5A5B0
𠃯	𠃰	𠃱	𠃲	𠃳	𠃴	𠃵	𠃶	𠃷	𠃸	𠃹	𠃺	𠃻	E5A680
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Unicode

Python >> ord('测')

2. Calculus

The Counts Operation is about: Add (+)

Two power, two things, two force..

Each one has the same influence of one result.

We write the $a_1 + a_2 + a_3 + \dots + a_N$:

$$\sum_{k=1}^n a_k$$

$$\sum_{k=1}^{\infty} a_k$$

If the limit does not exist, the series diverges; otherwise, it converges.

Some Feature:

$$\sum_{k=1}^n (ca_k + b_k) = c \sum_{k=1}^n a_k + \sum_{k=1}^n b_k .$$

$$\sum_{k=1}^n k = 1 + 2 + \dots + n .$$

$$\sum_{k=1}^n k = \frac{1}{2}n(n+1)$$

Geometric series:

$$\sum_{k=0}^n x^k = 1 + x + x^2 + \dots + x^n$$

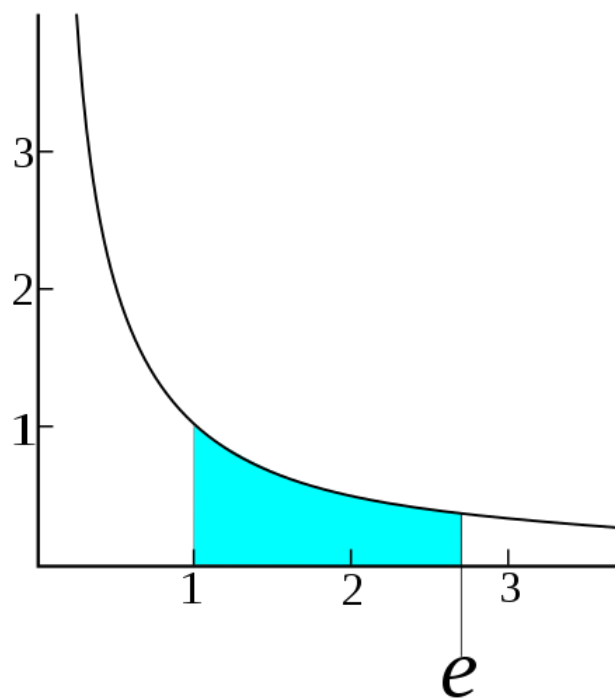
$$\sum_{k=0}^n x^k = \frac{x^{n+1} - 1}{x - 1}$$

If $|x| < 1$:

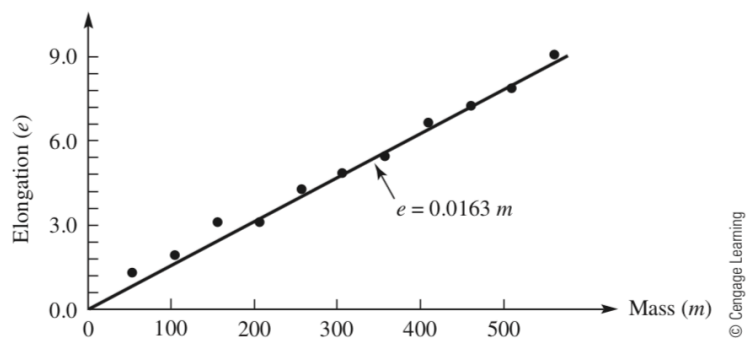
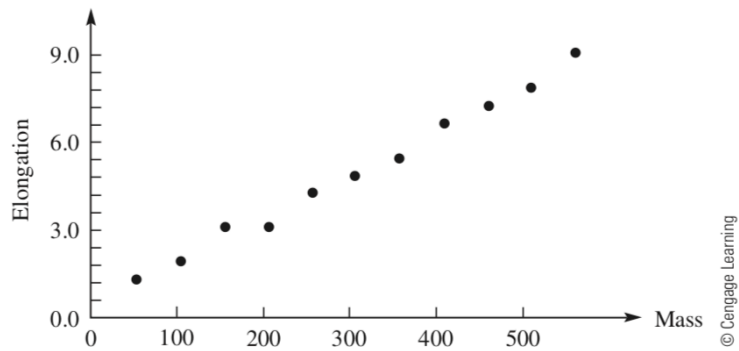
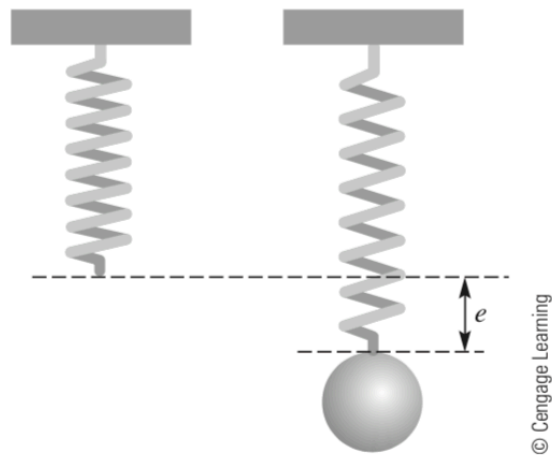
$$\sum_{k=0}^{\infty} x^k = \frac{1}{1-x} .$$

Natural Logarithm:

$$e = \sum_{n=0}^{\infty} \frac{1}{n!} = \frac{1}{1} + \frac{1}{1} + \frac{1}{1 \cdot 2} + \frac{1}{1 \cdot 2 \cdot 3} + \dots$$



Multiplication *:



$$Y = kx;$$

Two variable y and x are **proportional** if one is always a constant multiple of the other.

For some nonzero constant k , We write:

$$y \propto x.$$

Product:

$$\prod_{k=1}^n a_k$$

$$\lg\left(\prod_{k=1}^n a_k\right) = \sum_{k=1}^n \lg a_k \; .$$

3. Logic

Set, a collection of distinguishable objects.

\in

$$S = \{1, 2, 3\} = \{2, 3, 1\} = \{3, 1, 2\}$$

- \emptyset denotes the **empty set**, that is, the set containing no members.
- \mathbb{Z} denotes the set of **integers**, that is, the set $\{\dots, -2, -1, 0, 1, 2, \dots\}$.
- \mathbb{R} denotes the set of **real numbers**.
- \mathbb{N} denotes the set of **natural numbers**, that is, the set $\{0, 1, 2, \dots\}$.²

- The ***intersection*** of sets A and B is the set

$$A \cap B = \{x : x \in A \text{ and } x \in B\} .$$

- The ***union*** of sets A and B is the set

$$A \cup B = \{x : x \in A \text{ or } x \in B\} .$$

- The ***difference*** between two sets A and B is the set

$$A - B = \{x : x \in A \text{ and } x \notin B\} .$$

Associative laws:

$$A \cap (B \cap C) = (A \cap B) \cap C ,$$

$$A \cup (B \cup C) = (A \cup B) \cup C .$$

Distributive laws:

$$A \cap (B \cup C) = (A \cap B) \cup (A \cap C) ,$$

$$A \cup (B \cap C) = (A \cup B) \cap (A \cup C) .$$

Absorption laws:

$$A \cap (A \cup B) = A ,$$

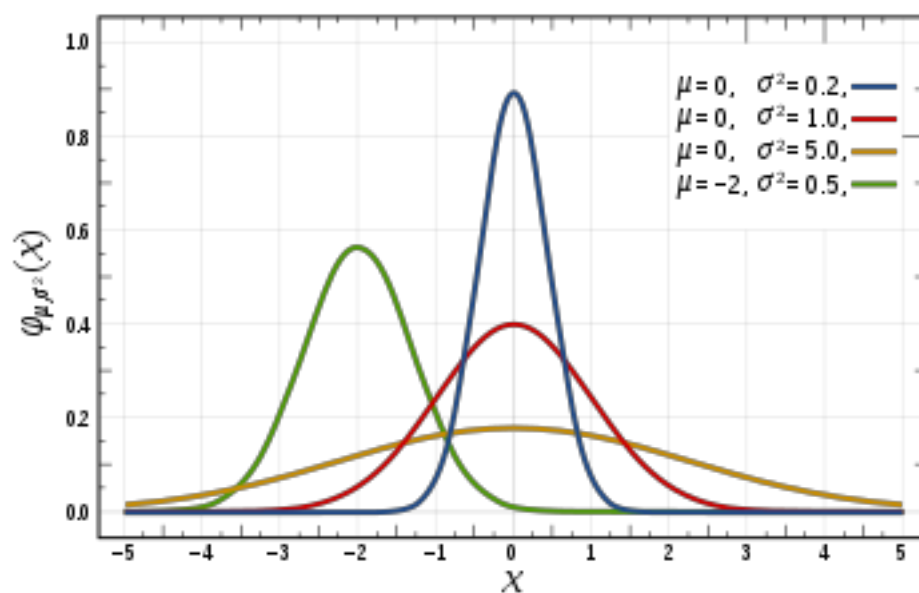
$$A \cup (A \cap B) = A .$$

The Mark:

- \exists
- \forall
- s.t
- \ddots
- \therefore
- $\operatorname{argmax}()$

5. Linear Algebra

6. Probability



$$f(x \mid \mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

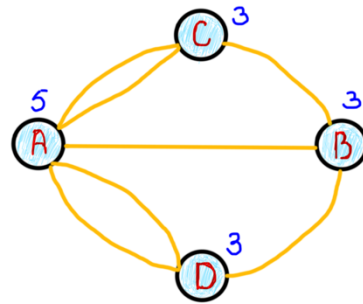
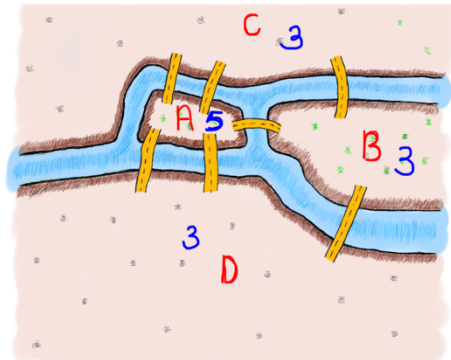
where

- μ is the [mean](#) or [expectation](#) of the distribution (and also its [median](#) and [mode](#)),
- σ is the [standard deviation](#), and
- σ^2 is the [variance](#).

$$\text{Var}(X) = E[(X - \mu)^2].$$

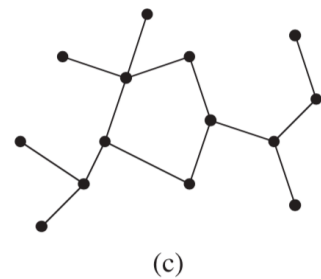
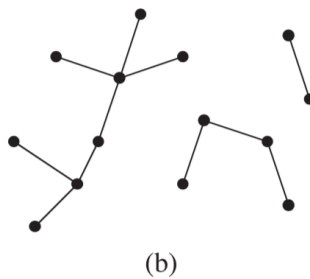
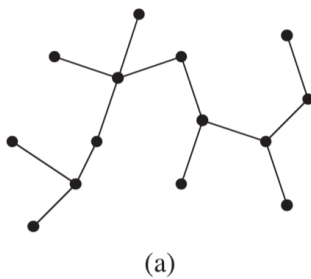
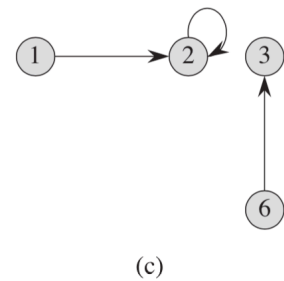
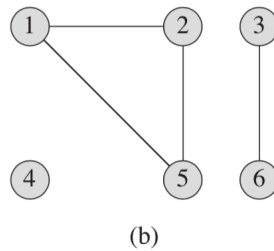
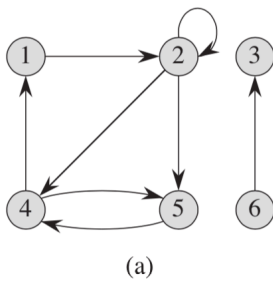
7. Graph

Degree of a vertex is the number of edges incident to the vertex.



$$\deg(A) = 5$$

$$\deg(B) = \deg(C) = \deg(D) = 3$$



8. Dynamic Programming