

Begin your response to **QUESTION 3** on this page.

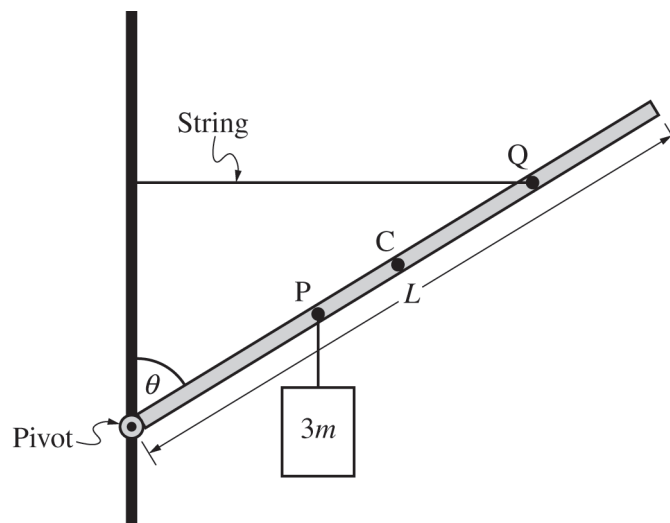
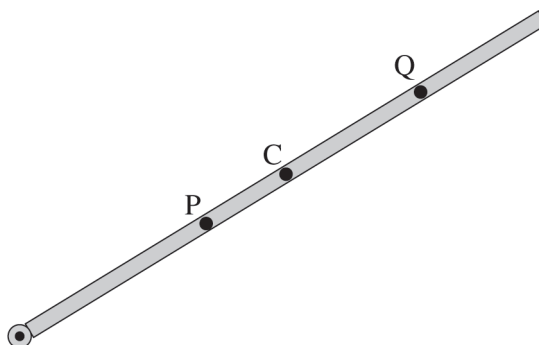


Figure 1

Note: Figure not drawn to scale.

3. A uniform rod of length  $L$  and mass  $m$  is attached to a pivot on a vertical pole, as shown in Figure 1. There is negligible friction between the rod and the pivot. A horizontal string connects Point Q on the rod to the pole. The rod makes an angle  $\theta$  with the pole. A block of mass  $3m$  hangs from the rod at Point P. The center of mass of the rod is located at Point C.
- (a) On the following representation of the rod, **draw** and **label** the forces (not components) that are exerted on the rod. Each force must be represented by a distinct arrow that starts on and points away from the point at which the force is exerted on the rod.



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- (b) In Figure 1, Point P is located  $\frac{3}{8}L$  from the pivot and Point Q is located  $\frac{6}{8}L$  from the pivot. **Derive** an equation for the tension  $F_T$  in the horizontal string in terms of  $L$ ,  $m$ ,  $\theta$ , and physical constants, as appropriate.

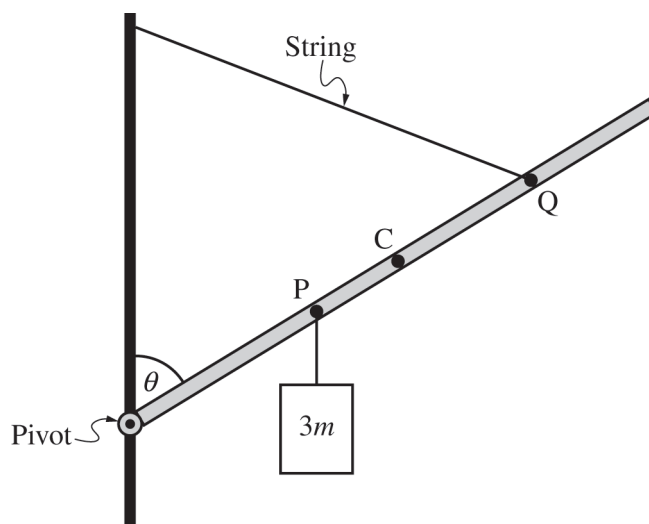


Figure 2

Note: Figure not drawn to scale.

- (c) The original string is replaced with a longer string that connects Point Q to a higher location on the vertical pole, as shown in Figure 2. The angle  $\theta$  remains the same. How does the new tension  $F_{T, \text{new}}$  compare with the original tension  $F_T$  from part (b) ? **Justify** your reasoning.

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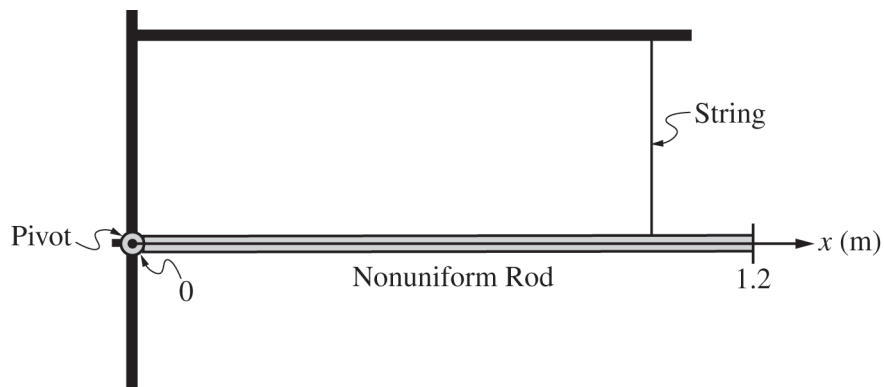


Figure 3

Note: Figure not drawn to scale.

- (d) A nonuniform rod is now attached to the pivot, as shown in Figure 3. There is negligible friction between the nonuniform rod and the pivot. The rod has a length of 1.2 m and a linear mass density  $\lambda(x) = A + Bx$ , where  $x$  is the distance from the pivot,  $A = 6.0 \text{ kg/m}$ , and  $B = 10.0 \text{ kg/m}^2$ .

i. **Calculate** the mass of the rod.

ii. **Calculate** the rotational inertia of the rod about the pivot.

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