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AI MACHINE LEARNING & DATA SCIENCE RESEARCH

Genius or Subpar AI Mathematician? New Study Questions ChatGPT's **Mathematical Capabilities**





The November release of ChatGPT garnered unprecedented public and media attention. OpenAI's conversational large language model (LLM) was widely applauded for its ability to answer complex queries, generate correct computer code and coherent long-form essays, and even solve math problems. But might that last claim have been premature?

In the new paper Mathematical Capabilities of ChatGPT, a research team from the University of Oxford, TU Wein, University of Cambridge, University of Vienna, and Princeton University tests ChatGPT's mathematical capabilities on publicly available and hand-crafted datasets and evaluates its suitability as an assistant to professional mathematicians. The team concludes that despite the glowing media reviews, ChatGPT's mathematical abilities "are significantly below those of an average mathematics graduate student."

Mathematical Capabilities of ChatGPT

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February 1, 2023

The team summarizes their main contributions as follows:

- 1. Insight for mathematical use is provided. We show for which types of questions and which domains of mathematics ChatGPT may be useful and how it could be integrated into the workflow of a mathematician.
- 2. The failure modes of ChatGPT are identified, as well as the limits of its capabilities. This can aid future efforts to develop LLMs that perform better in mathematics.
- 3. We provide benchmarks for testing the mathematical capabilities of future LLMs so that they can be compared to ChatGPT across a range of aspects regarding advanced mathematical comprehension.

Dataset name	me Comprised of the file(s)	
Grad-Text	W. Rudin, Functional Analysis (ch. 1)	M3 Q4
	W. Rudin, Functional Analysis (ch. 2)	M3 Q4
	J. Munkres, Topology (ch. 1)	M3 Q4
	J. Munkres, Topology (ch. 2)	M3 Q4
	R. Durret, Probability Theory	M3 Q4
Holes-in-Proofs	Proofs Collection A	M3 Q2 Q5
	Proofs Collection B Prealgebra	M1 Q5
	Proofs Collection B Precalculus	M1 Q5
Olympiad-Problem-Solving	Olympiad Problem Solving	M4 Q4 D2
Symbolic-Integration	Symbolic Integration	M2 Q3 D1
MATH	MATH Algebra	M1 M2 M3 Q3 Q4
	MATH Counting and Probability	M1 M2 M3 Q3 Q4
	MATH Prealgebra	M1 Q3 Q4
	MATH Precalculus	M1 Q3 Q4
$oldsymbol{S}$ earch-Engine-Aspects	Definition Retrieval	M3 Q1 Q2 D3
	Reverse Definition Retrieval	M3 Q2 D3
	Named Theorem Proof Completion	M3 Q1 Q2 D3

Table 1: A summary of all datasets, together with their associated tags. The tags Mi, Qi, and Di relate to the level of Mathematical difficulty, the Question type, and the Out-of-Distribution type from Section 3.3, respectively.

To effectively evaluate ChatGPT on advanced math problems, the researchers build a new dataset, GHOSTS, comprising a total of 728 prompts in six carefully crafted subdatasets: Grad-Text, Holes-in-Proofs, Olympiad-Problem-Solving, Symbolic-Integration, MATH, and Search-Engine-Aspects. The researchers say the GHOST datasets surpass publicly available benchmark mathematical datasets in terms of sophistication and reasoning difficulty.

The researchers use <u>LaTeX</u> to encode the mathematical inputs for most of their subdatasets, which are categorized into four dimensions with ascending difficulty: 1) elementary arithmetic problems, 2) symbolic problems, 3) (under)graduate-level exercises from well-known textbooks and questions from <u>math.stackexchange.com</u>, and 4) exercises in the style of <u>Mathematical Olympiad</u> problems.

The team applied ChatGPT on the GHOST datasets and considered output length, stability of the answer under prompt engineering, and how close they judged ChatGPT to be to the correct answer.

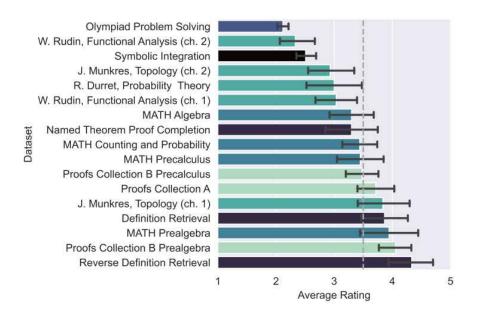


Figure 2: Average rating for each file in each subdataset (same colors indicate the files come from the same subdataset). Since the maximal ranking is 5, and the minimal ranking where the question was at least understood is 2, a passing grade (50% of points) would be 3.5, as indicated by the dotted line. The error bars represent 95% confidence intervals.

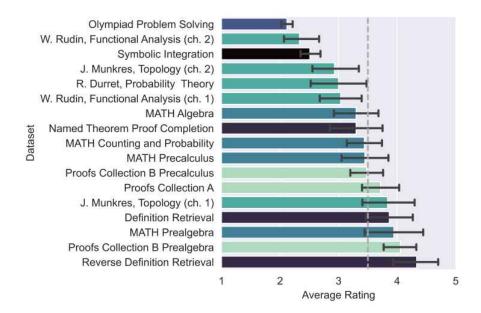


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ChatGPT failed on most of the problems, faring especially poorly on questions requiring deep insights and original solutions such as those found in the Mathematical Olympiads. The

paper concludes that while ChatGPT can effectively search for mathematical objects when given information about them, it struggles with advanced mathematics and delivering consistent, high-quality proofs or calculations.

The team hopes their work will inspire other professional mathematicians to contribute to building a more thorough benchmark for assessing and improving LLMs' mathematical abilities.

Just one day before this paper was published, OpenAI <u>announced</u> it had upgraded ChatGPT with improved mathematical capabilities. It's unclear how this latest version would perform in the experiments presented here.

The GHOSTS dataset will be released on the project's <u>GitHub</u>. The paper *Mathematical Capabilities of ChatGPT* is on <u>arXiv</u>.

Author: Hecate He | **Editor**: Michael Sarazen



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3 COMMENTS ON "GENIUS OR SUBPAR AI MATHEMATICIAN? NEW STUDY QUESTIONS CHATGPT'S MATHEMATICAL CAPABILITIES"



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As a math fan, this topic caught my attention.

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Darius Quid

2023-03-29

It's pretty interesting, and that's another proof that math can be actually complicated. Even Artificial Intelligence struggles with it, so I genuinely don't understand people who enjoy solving math problems, especially mathematical olympiad ones, it's way too much for me. I used to hate this class at school, and I even decided to get online math classes from brighterly math for my daughter because I know for a fact that I won't be able to explain anything to her besides the simplest basics. To be honest, I'm pretty sure that she's even better than me at math right now.

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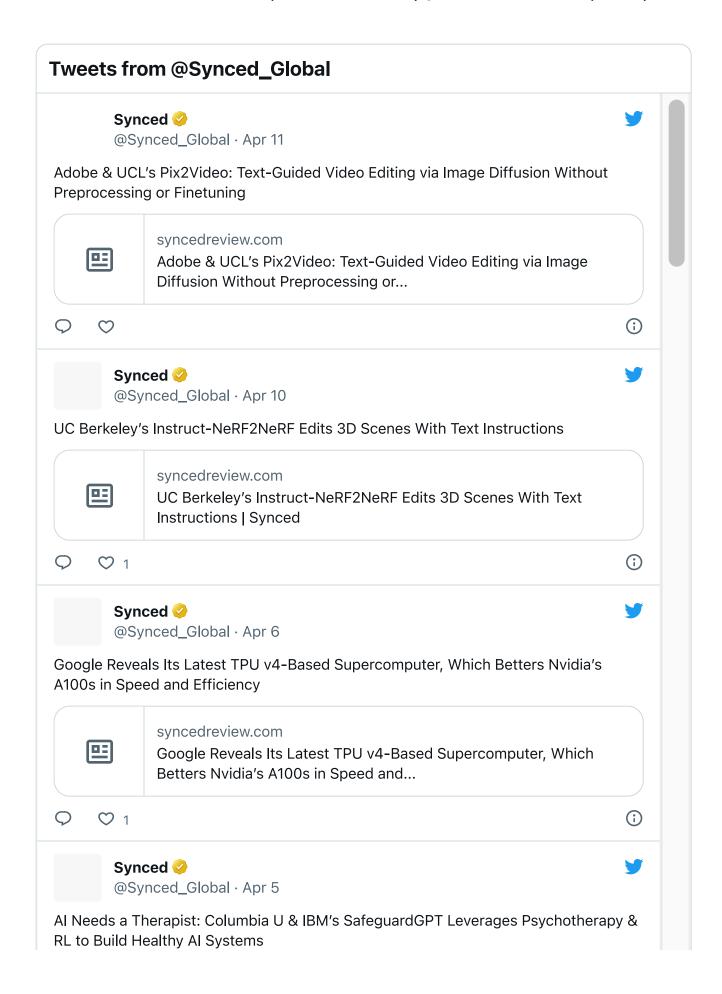
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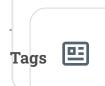
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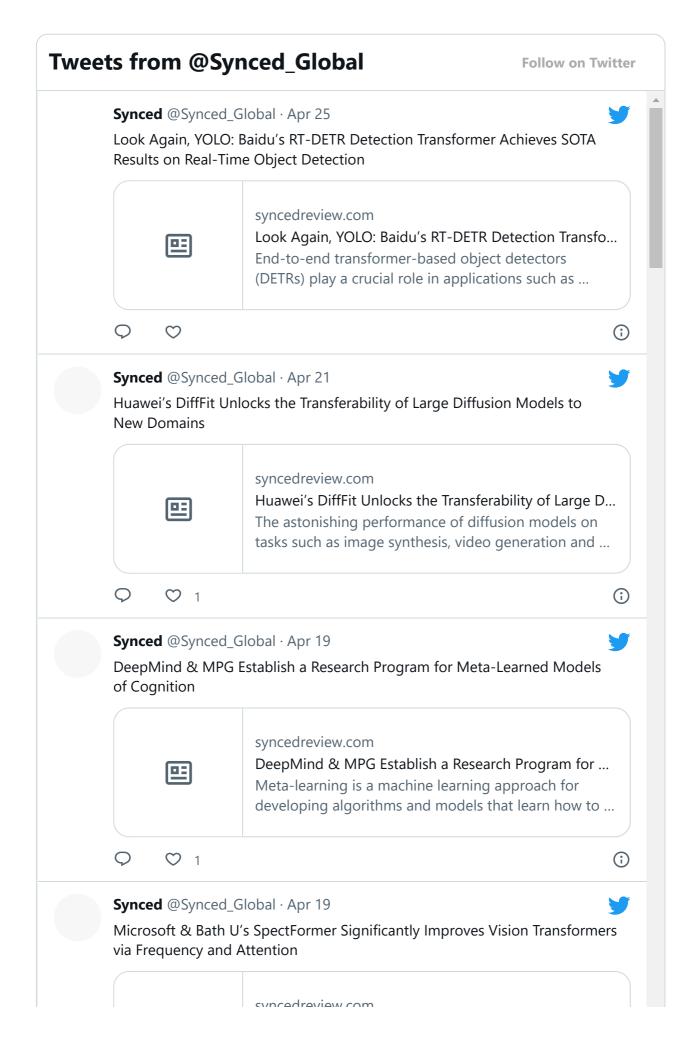
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Synced has conducted numerous in-depth interviews with industry leaders, for who provided valuable insight on industry dynamics and expertise. Past interviewees include the god father of Reinforcement Learning professor *Richard Sutton* from University of Alberta, chief scientist at Baidu Research Silicon Valley and adjunct professor at Stanford University *Andrew Ng*, Professor *Eric P. Xing* from *Carnegie Mellon University*, Microsoft Research's chief Artificial Intelligence scientist *Deng Li*, Professor *Qiang Yang* from Hong Kong University of Science and Technology, the founders of *MXNet*, Duke University's vice provost for research *Lawrence Carin*, Professor *Jack Gallant* from UC Berkeley, Nobel Laureate *Randy Schekman*, and so on. We have also reported on Baidu, Google, IBM, Microsoft, among other major technology companies, alongside many outstanding Artificial Intelligence companies and robotics startups around the world.

In addition to content production, *Synced* provides services to interested individuals in the artificial intelligence industry, including financial advisory, globalization strategy and talent recruitment. At the same time, *Synced* has covered young Chinese researchers in more than 40 colleges and universities in North America and Europe.

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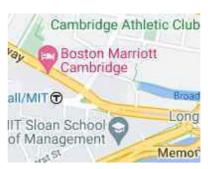


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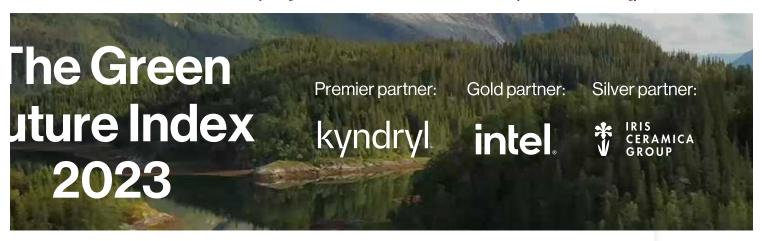
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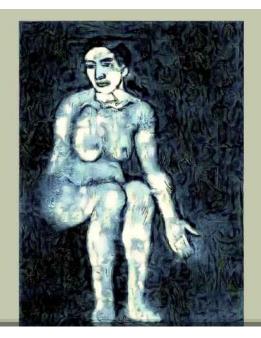
HUMANS AND TECHNOLOGY

This Picasso painting had never been seen before. Until a neural network painted it.

With help from a neural network, researchers reconstructed an image the artist created and painted over during his Blue Period.

By Emerging Technology from the arXiv

September 20, 2019



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The Old Guitarist is probably the most famous painting from Picasso's Blue Period. It dates from 1903-1904, when the young artist was living in poverty in Paris. Picasso used the color blue to represent the emotional pain and desolation he was experiencing at the time.

But *The Old Guitarist* is interesting for another reason. Art historians have long noted the presence of a ghostly woman's face faintly visible beneath the paint. In 1998, conservators at the Art Institute of Chicago, where the painting hangs, photographed it using x-rays and infrared light to see what lies beneath the surface.

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These images show an entirely different painting. It depicts a seated woman holding out her left arm. The researchers then matched this painting to a composition Picasso had sketched out in a letter to a colleague at the time.

The findings fascinated the art world. Artists often paint over earlier works, particularly during periods of penury when canvas is in short supply.

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The new image provided an important insight into the progression of Picasso's work, his subjects, and his thinking during his Blue Period. Since he is perhaps the most important artist of 20th century, that's hugely significant.

But from an aesthetic point of view, what the researchers managed to retrieve is disappointing. Infrared and x-ray images show only the faintest outlines, and while they can be used to infer the amount of paint the artist used, they do not show color or style. So a way to reconstruct the lost

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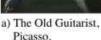
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The researchers have used the same technique to retrieve lost paintings by other artists and say it has the potential to transform the way art historians work.







b) X-radiograph of The Old Guitarist.



c) Content image. constructed from b).



d) Style image, Picasso's e) Stylised image, La Vie.



La femme perdue.

Courtesy of the researchers

First some background. Neural style transfer was developed in 2015 by Leon Gatys and colleagues at the University of Tubingen in Germany. It comes about from a fascinating insight into the way neural networks learn to recognize images of different kinds.

Neural networks consist of layers that analyze an image at different scales. The first layer might recognize broad features like edges, the next layer sees how these edges form simple shapes like circles, the next layer recognizes patterns of shapes, such as two circles close together, and yet another layer might label these pairs of circles as eyes.

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This kind of network would be able to recognize eyes in paintings in a wide variety of styles, from Leonardo da Vinci to Van Gogh to Picasso. In each case, the eyes form a similar pattern that the machine can pick out.

Gatys and co went further by training such a network to recognize artistic style; for example, to distinguish a Van Gogh from a Picasso.

Their key discovery was that the ability to distinguish style was entirely separate from the ability to see faces or other objects. In fact, Gatys and co were able to separate this ability and use it in reverse. They fed a picture into the neural network, which then superimposed the style onto the image.

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This work has been hugely influential. Various groups have used it to produce artworks, <u>comics</u>, or <u>even movies</u> in the style of any chosen artist.

This process works just as well with Picasso, making it possible to produce an image in the style of Picasso's cubist paintings, or his Rose Period, or indeed his Blue Period.

This is where Bourached and Cann come in. They have taken a manually edited version of the x-ray images of the ghostly woman beneath *The Old Guitarist* and passed it through a neural style transfer network. This network was trained to convert images into the style of another artwork from Picasso's Blue Period.

The result is a full-color version of the painting in exactly the style Picasso was exploring when he painted it. "We present a novel method of reconstructing lost artwork, by applying neural style transfer to x-radiographs of artwork with secondary interior artwork beneath a primary exterior, so as to reconstruct lost artwork," they say.

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Of course, there is no way of knowing that Picasso painted the image this way. But Bourached and Cann say their goal is to broaden the insight into an artist's intentions, mistakes, and musings by reconstructing artwork that has been hidden. "Our method of combining original but hidden artwork, subjective human input, and neural style transfer helps to broaden an insight into an artist's creative process," they say.

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That is surely just the start, and a technique that art historians might feel has the potential to go much further.

Ref: <u>arxiv.org/abs/1909.05677</u>: Raiders of the Lost Art

by Emerging Technology from the arXiv



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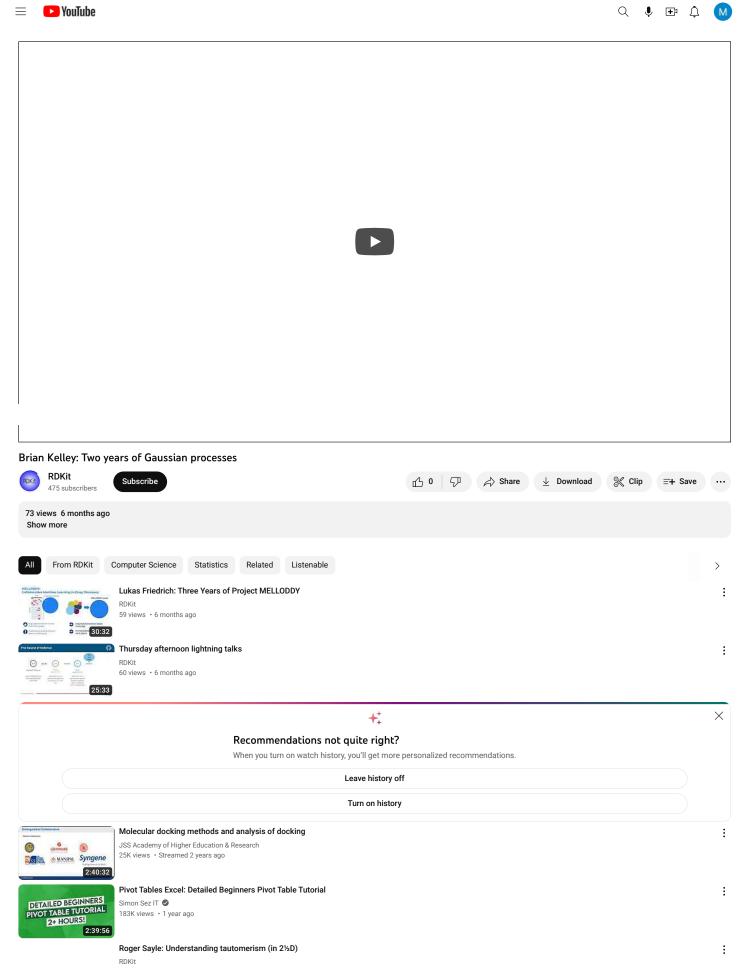








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Tanimoto Kernel



Using Ryan-Rhys Griffith's kernel (compute Tanimoto over matrix input)

$$||\mathbf{X}||^2$$
 Xs = tf.reduce_sum(tf.square(X), axis=-1) # Squared L2-norm of X

$$||\mathbf{X}^{\dagger}||^2$$
 X2s = tf.reduce_sum(tf.square(X2), axis=-1) # Squared L2-norm of X2

$$||\mathbf{x}||^2 + ||\mathbf{x}'||^2 - \langle \mathbf{x}, \mathbf{x}' \rangle$$

denominator = -outer_product + broadcasting_elementwise(tf.add, Xs, X2s)

kernel = self.variance * outer_product / denominator

Variance is what is being trained (in addition to noise)

This just makes tensorflow fast

https://towardsdatascience.com/gaussian-process-regression-on-molecules-in-gpflow-ee6fedab2130

Brian Kelley: Two years of Gaussian processes

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