CSC 6013 - Worksheet for Week 4

1) Complete this table rounding each decimal to the nearest integer. This should give you a sense of the comparative growth rates of the functions. Note that lg(n) means python's log 2(n).

lg(n)	\sqrt{n}	n	nlg(n)	n ²	n^3	2 ⁿ	n!
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(1.1	2	4	٦	8	ч	a a
7	a	-3	B	9	27	8	6
2	7	4	7	16	७५	16	24
2	2	5	3	25	125	32	120
3	2	6	5	36	218	64	720
3	3	7	6	49	343	128	5040
3	3	8	7	64	512	256	40320
3	3	9	9	81	729	512	362880
3	3	10	10	100	1000	1024	3628800

For #2, 3, and 4, solve each summation in two ways: write out all terms of the sum and perform the arithmetic; then use one of the formulas in the class notes to confirm your answer.

2)
$$1^{2} + \lambda^{2} + 3^{2} + 4^{2} + 5^{2} + 6^{2} + 7^{2} + 4^{2} + 4^{2} + 10^{2} + 11^{2} + 13^{2} + 14^{2} + 15^{2}$$

$$= 1240$$

$$\sum_{i=1}^{15} i^{2} \frac{\Lambda(\Lambda+i)(2\pi+1)}{6} = \frac{15(15+1)(2(15)+1)}{6}$$

$$= 1240$$
3) $2^{0} + 2^{1} + 2^{2} + 2^{3} + 2^{4} + 2^{5} + 2^{6} + 2^{7} + 2^{8} + 2^{9} + 2^{10}$

$$\sum_{i=0}^{10} 2^{i} = 3047$$

$$2^{\Lambda+1} - 1 = 2^{(0+1)} - 1 = 2047$$

4) Follow the same instructions for #2 and #3; round off this answer to three decimal places.

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$$\sum_{i=1}^{8} 2^{-i} + 2^{-3} + 2^{-3} + 2^{-4} + 2^{-5} + 2^{-6} + 2^{-7} + 2^{-8} + 2^{-7} +$$

$$\sum_{i=1}^{5} i \frac{(n-i)n}{2} = \frac{1}{2} \cdot (n-i)n = \frac{1}{2}n^2 - \frac{1}{2}n$$

Asymptotic analysis for #6 and #7: Determine the Big-Oh class of each algorithm. That is, **formally** compute the worst-case running time as we did on class using a table to produce a function that tracks the work required by all lines of code. Include all steps of the algebraic simplification, but you do not need to provide comments to justify each step.

6) Arithmetic mean = "add them all up, and divide by how many". Let the size of the problem = n = the number of entries in the array.

7) Sum of entries in an upper triangular nxn array. Let the size of the problem = n = the dimension of the nxn matrix.

$$T(n) = C_1(1) + C_2(n) + C_3 \frac{(n-1)n}{2} + C_4(n) + C_2(n)$$

$$= (c_1 + c_2) - 1 + \frac{1}{2} c_3 n^2 - \frac{1}{2} c_3 n + \frac{1}{2} c_4 n + C_2(n)$$

$$= (c_1 + c_2) + C_1(n) + C_4$$

$$= (c_1(n^2) + C_1(n^2) + C_6(n^2)$$

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