## CS2010: ALGORITHMS AND DATA STRUCTURES

Lectures 15-16: Hashtables

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### Symbol tables

#### Key-value pair abstraction.

- · Insert a value with specified key.
- · Given a key, search for the corresponding value.

#### Ex. DNS lookup.

Insert domain name with specified IP address.

kev

· Given domain name, find corresponding IP address.

domain name	IP address
www.cs.princeton.edu	128.112.136.11
www.princeton.edu	128.112.128.15
www.yale.edu	130.132.143.21
www.harvard.edu	128.103.060.55
www.simpsons.com	209.052.165.60
<b>↑</b>	<b>↑</b>

value

## Symbol table applications

application	purpose of search	key	value	
dictionary	find definition	word	definition	
book index	find relevant pages	term	list of page numbers	
file share	find song to download	name of song	computer ID	
financial account	process transactions	account number	transaction details	
web search	find relevant web pages	keyword	list of page names	
compiler	find properties of variables	variable name	type and value	
routing table	route Internet packets	destination	best route	
DNS	find IP address	domain name	IP address	
reverse DNS	find domain name	IP address	domain name	
genomics	find markers	DNA string	known positions	
file system	find file on disk	filename	location on disk	

## Basic symbol table API

Associative array abstraction. Associate one value with each key.

public class	S ST <key, value=""></key,>		
	ST()	create an empty symbol table	
void	<pre>put(Key key, Value val)</pre>	put key-value pair into the table	_ a[key] = val;
Value	get(Key key)	value paired with key	_ a[key]
boolean	contains(Key key)	is there a value paired with key?	
void	<pre>delete(Key key)</pre>	remove key (and its value) from table	
boolean	isEmpty()	is the table empty?	
int	size()	number of key-value pairs in the table	
Iterable <key></key>	keys()	all the keys in the table	

#### Conventions

- Values are not null. ← Java allows null value
- Method get() returns null if key not present.
- Method put() overwrites old value with new value.

#### Intended consequences.

• Easy to implement contains().

```
public boolean contains(Key key)
{ return get(key) != null; }
```

• Can implement lazy version of delete().

```
public void delete(Key key)
{  put(key, null); }
```

## Keys and values

Value type. Any generic type.

specify Comparable in API.

#### Key type: several natural assumptions.

- Assume keys are Comparable, use compareTo().
- Assume keys are any generic type, use equals() to test equality.
- Assume keys are any generic type, use equals() to test equality;
   use hashCode() to scramble key.

Best practices. Use immutable types for symbol table keys.

• Immutable in Java: Integer, Double, String, java.io.File, ...

(stav tuned)

• Mutable in Java: StringBuilder, java.net.URL, arrays, ...

#### **Equality test**

All Java classes inherit a method equals().

Java requirements. For any references x, y and z:

```
• Reflexive: x.equals(x) is true.
```

- Symmetric: x.equals(y) iff y.equals(x).
- Transitive: if x.equals(y) and y.equals(z), then x.equals(z).
- Non-null: x.equals(null) is false.

```
do x and y refer to
the same object?
```

Default implementation. (x == y)

Customized implementations. Integer, Double, String, java.io.File, ...

User-defined implementations. Some care needed.

# Algorithms

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## 3.1 SYMBOL TABLES

- API
- elementary implementations
- ordered operations

## Examples of ordered symbol table API

```
values
                                  keys
                     min() \longrightarrow 09:00:00
                                            Chicago
                               09:00:03
                                            Phoenix
                               09:00:13 Houston
             get(09:00:13) - 09:00:59
                                           Chicago
                               09:01:10
                                            Houston
          floor(09:05:00) \longrightarrow 09:03:13
                                            Chicago
                               09:10:11
                                            Seattle.
                                            Seattle.
                 select(7) \longrightarrow 09:10:25
                               09:14:25
                                           Phoenix
                               09:19:32
                                            Chicago
                               09:19:46
                                            Chicago
keys(09:15:00, 09:25:00) \longrightarrow 09:21:05
                                            Chicago
                               09:22:43
                                            Seattle
                               09:22:54
                                           Seattle
                               09:25:52
                                           Chicago
        ceiling(09:30:00) \longrightarrow 09:35:21
                                            Chicago
                               09:36:14
                                            Seattle
                     max() \longrightarrow 09:37:44
                                            Phoenix
size(09:15:00, 09:25:00) is 5
     rank(09:10:25) is 7
```

## Ordered symbol table API

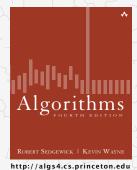
<pre>public class ST<key(extends comparable<key="">) Value&gt;</key(extends></pre>					
Key	min()	smallest key			
Key	max()	largest key			
Key	floor(Key key)	largest key less than or equal to key			
Key	ceiling(Key key)	smallest key greater than or equal to key			
int	rank(Key key)	number of keys less than key			
Key	select(int k)	key of rank k			
void	deleteMin()	delete smallest key			
void	deleteMax()	delete largest key			
int	size(Key lo, Key hi)	number of keys between lo and hi			
Iterable <key></key>	keys()	all keys, in sorted order			
Iterable <key></key>	keys(Key lo, Key hi)	keys between lo and hi, in sorted order			

## Symbol table implementations: summary

implementation -	guarantee			average case			ordered	key
	search	insert	delete	search hit	insert	delete	ops?	interface
sequential search (unordered list)	N	N	N	½ N	N	½ N		equals()
binary search (ordered array)	lg N	N	N	lg N	½ N	½ N	~	compareTo()
BST	N	N	N	1.39 lg <i>N</i>	1.39 lg <i>N</i>	$\sqrt{N}$	~	compareTo()
red-black BST	2 lg <i>N</i>	2 lg <i>N</i>	2 lg <i>N</i>	1.0 lg <i>N</i>	1.0 lg <i>N</i>	1.0 lg <i>N</i>	~	compareTo()

Q. Can we do better?

A. Yes, but with different access to the data.
Will NOT support ordered operations.



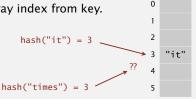
## 3.4 HASH TABLES

- hash functions
- separate chaining
- linear probing
- context

### Hashing: basic plan

Save items in a key-indexed table (index is a function of the key).

Hash function. Method for computing array index from key.



#### Issues.

- Computing the hash function.
- · Equality test: Method for checking whether two keys are equal.
- Collision resolution: Algorithm and data structure to handle two keys that hash to the same array index.

#### Classic space-time tradeoff.

- No space limitation: trivial hash function with key as index.
- No time limitation: trivial collision resolution with sequential search.
- · Space and time limitations: hashing (the real world).

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## 3.4 HASH TABLES

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## Computing the hash function

Idealistic goal. Scramble the keys uniformly to produce a table index.

- · Efficiently computable.
- Each table index equally likely for each key.



#### Ex 1. Phone numbers.

- · Bad: first three digits.
- · Better: last three digits.

## table index

kev

#### Ex 2. Social Security numbers.

- Bad: first three digits. 

  573 = California, 574 = Alaska
  (assigned in chronological order within geographic region)
- · Better: last three digits.

Practical challenge. Need different approach for each key type.

#### Java's hash code conventions

All Java classes inherit a method hashCode(), which returns a 32-bit int.

```
Requirement. If x.equals(y), then (x.hashCode() == y.hashCode()).
Highly desirable. If !x.equals(y), then (x.hashCode() != y.hashCode()).
Requirement. x.hashCode() == x.hashCode()
x
y
```

x.hashCode()

Default implementation. Memory address of x.
Legal (but poor) implementation. Always return 17.
Customized implementations. Integer, Double, String, File, URL, Date, ...
User-defined types. Users are on their own.

v.hashCode()

## Implementing hash code: integers, booleans, and doubles

#### Java library implementations

```
public final class Integer
{
   private final int value;
   ...

public int hashCode()
   { return value; }
}
```

```
public final class Double
   private final double value:
   public int hashCode()
       long bits = doubleToLongBits(value);
       return (int) (bits ^ (bits >>> 32));
            convert to IEEE 64-bit representation;
                xor most significant 32-bits
                with least significant 32-bits
```

Warning: -0.0 and +0.0 have different hash codes

## Implementing hash code: strings

#### Java library implementation

```
public final class String
{
   private final char[] s;
   ...

public int hashCode()
{
   int hash = 0;
   for (int i = 0; i < length(); i++)
        hash = s[i] + (31 * hash);
   return hash;
}

ith character of s</pre>
```

char	Unicode			
'a'	97			
'b'	98			
'c'	99			

- Horner's method to hash string of length L: L multiplies/adds.
- Equivalent to  $h = s[0] \cdot 31^{L-1} + ... + s[L-3] \cdot 31^2 + s[L-2] \cdot 31^1 + s[L-1] \cdot 31^0$ .

## Implementing hash code: strings

#### Performance optimization.

- · Cache the hash value in an instance variable.
- · Return cached value.

```
public final class String
                                                        cache of hash code
   private int hash = 0;
   private final char[] s;
   . . .
   public int hashCode()
      int h = hash:
                                                        return cached value
      if (h != 0) return h:
      for (int i = 0; i < length(); i++)
         h = s[i] + (31 * h);
                                                        store cache of hash code
      hash = h;
      return h:
```

Q. What if hashCode() of string is 0?

## Implementing hash code: user-defined types

```
public final class Transaction implements Comparable<Transaction>
   private final String who;
   private final Date
                          when:
   private final double amount:
   public Transaction(String who, Date when, double amount)
   { /* as before */ }
   . . .
   public boolean equals(Object y)
   { /* as before */ }
   public int hashCode()
                                  nonzero constant
                                                                          for reference types,
      int hash = 17;
                                                                          use hashCode()
      hash = 31*hash + who.hashCode():
      hash = 31*hash + when.hashCode():
                                                                          for primitive types,
      hash = 31*hash + ((Double) amount).hashCode():
                                                                          use hashCode()
      return hash;
                                                                          of wrapper type
                        typically a small prime
```

## Hash code design

#### "Standard" recipe for user-defined types.

- Combine each significant field using the 31x + y rule.
- If field is a primitive type, use wrapper type hashCode().
- If field is null, return 0.
- If field is a reference type, use hashCode(). ← applies rule recursively
- If field is an array, apply to each entry.
   ← or use Arrays.deepHashCode()

In practice. Recipe works reasonably well; used in Java libraries. In theory. Keys are bitstring; "universal" hash functions exist.

Basic rule. Need to use the whole key to compute hash code; consult an expert for state-of-the-art hash codes.

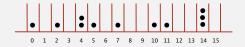
## Modular hashing

```
Hash code. An int between -231 and 231 - 1.
Hash function. An int between 0 and M - 1 (for use as array index).
                                                  typically a prime or power of 2
                                                                                  х
               private int hash(Key key)
                  return kev.hashCode() % M: }
             bug
                                                                             x.hashCode()
               private int hash(Key key)
                  return Math.abs(key.hashCode()) % M; }
             1-in-a-billion bug
                                                                               hash(x)
                                  hashCode() of "polygenelubricants" is -231
               private int hash(Key key)
                  return (key.hashCode() & 0x7ffffffff) % M; }
             correct
```

## Uniform hashing assumption

Uniform hashing assumption. Each key is equally likely to hash to an integer between 0 and M-1.

Bins and balls. Throw balls uniformly at random into M bins.



Birthday problem. Expect two balls in the same bin after  $\sim \sqrt{\pi M/2}$  tosses.

Coupon collector. Expect every bin has  $\geq 1$  ball after  $\sim M \ln M$  tosses.

Load balancing. After M tosses, expect most loaded bin has  $\Theta$  (  $\log M/\log\log M$  ) balls.

## Uniform hashing assumption

Uniform hashing assumption. Each key is equally likely to hash to an integer between 0 and M-1.

Bins and balls. Throw balls uniformly at random into M bins.





Java's String data uniformly distribute the keys of Tale of Two Cities

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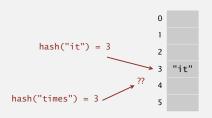
## 3.4 HASH TABLES

- hash functions
- separate chaining
- linear probing
- context

#### Collisions

Collision. Two distinct keys hashing to same index.

- Birthday problem ⇒ can't avoid collisions unless you have a ridiculous (quadratic) amount of memory.
- Coupon collector + load balancing ⇒ collisions are evenly distributed.

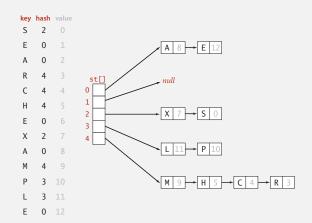


Challenge. Deal with collisions efficiently.

## Separate-chaining symbol table

### Use an array of M < N linked lists. [H. P. Luhn, IBM 1953]

- Hash: map key to integer i between 0 and M-1.
- Insert: put at front of *i*<sup>th</sup> chain (if not already there).
- Search: need to search only ith chain.



## Separate-chaining symbol table: Java implementation

```
public class SeparateChainingHashST<Key, Value>
  private int M = 97;
                    // number of chains
  private Node[] st = new Node[M]; // array of chains
  private static class Node
     private Object key; — no generic array creation
     private Node next:
  private int hash(Key key)
  { return (key.hashCode() & 0x7fffffff) % M; }
  public Value get(Key key) {
     int i = hash(key);
     for (Node x = st[i]; x != null; x = x.next)
       if (kev.equals(x.kev)) return (Value) x.val:
     return null:
```

array doubling and halving code omitted

## Separate-chaining symbol table: Java implementation

```
public class SeparateChainingHashST<Key, Value>
  private int M = 97;
                       // number of chains
  private Node[] st = new Node[M]; // array of chains
  private static class Node
     private Object kev:
     private Object val:
     private Node next:
  private int hash(Key key)
   { return (key.hashCode() & 0x7fffffff) % M; }
  public void put(Key key, Value val) {
     int i = hash(key);
     for (Node x = st[i]; x != null; x = x.next)
        if (key.equals(x.key)) { x.val = val; return; }
     st[i] = new Node(kev. val. st[i]):
```

## Analysis of separate chaining

Proposition. Under uniform hashing assumption, prob. that the number of keys in a list is within a constant factor of N/M is extremely close to 1.

Pf sketch. Distribution of list size obeys a binomial distribution.





Consequence. Number of probes for search/insert is proportional to N/M.

- M too large  $\Rightarrow$  too many empty chains.
- M too small  $\Rightarrow$  chains too long.
- Typical choice:  $M \sim N/4 \Rightarrow$  constant-time ops.

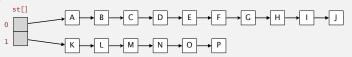
M times faster than sequential search

## Resizing in a separate-chaining hash table

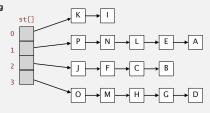
#### Goal. Average length of list N/M = constant.

- Double size of array M when  $N/M \ge 8$ .
- Halve size of array M when  $N/M \le 2$ .

#### before resizing



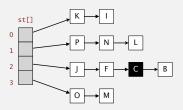
#### after resizing



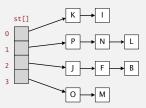
## Deletion in a separate-chaining hash table

- Q. How to delete a key (and its associated value)?
- A. Easy: need only consider chain containing key.

#### before deleting C



#### after deleting C



## Symbol table implementations: summary

implementation -	guarantee			average case			ordered	key
	search	insert	delete	search hit	insert	delete	ops?	interface
sequential search (unordered list)	N	N	N	½ N	N	½ N		equals()
binary search (ordered array)	lg N	N	N	lg N	½ N	½ N	•	compareTo()
BST	N	N	N	1.39 lg <i>N</i>	1.39 lg <i>N</i>	$\sqrt{N}$	•	compareTo()
red-black BST	2 lg <i>N</i>	2 lg <i>N</i>	2 lg <i>N</i>	1.0 lg <i>N</i>	1.0 lg <i>N</i>	1.0 lg <i>N</i>	•	compareTo()
separate chaining	N	N	N	3-5 *	3-5 *	3-5 *		equals() hashCode()

<sup>\*</sup> under uniform hashing assumption

## Algorithms

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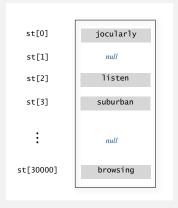
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## 3.4 HASH TABLES

- hash functions
- separate chaining
- linear probing
- context

## Collision resolution: open addressing

Open addressing. [Amdahl-Boehme-Rocherster-Samuel, IBM 1953] When a new key collides, find next empty slot, and put it there.



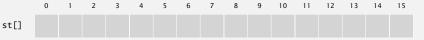
linear probing (M = 30001, N = 15000)

## Linear-probing hash table demo

Hash. Map key to integer i between 0 and M-1.

Insert. Put at table index i if free; if not try i+1, i+2, etc.

linear-probing hash table



M = 16



# Linear-probing hash table demo

Hash. Map key to integer i between 0 and M-1.

Search. Search table index i; if occupied but no match, try i+1, i+2, etc.

search K hash(K) = 5



M=16 K search miss (return null)

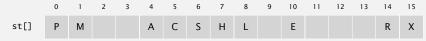
# Linear-probing hash table summary

Hash. Map key to integer i between 0 and M-1.

Insert. Put at table index i if free; if not try i+1, i+2, etc.

Search. Search table index i; if occupied but no match, try i+1, i+2, etc.

Note. Array size M must be greater than number of key-value pairs N.



M = 16

# Linear-probing symbol table: Java implementation

```
public class LinearProbingHashST<Key, Value>
   private int M = 30001;
                                                                    array doubling and
   private Value[] vals = (Value[]) new Object[M];
                                                                   halving code omitted
   private Key[] keys = (Key[]) new Object[M];
  private int hash(Key key) { /* as before */ }
   private void put(Kev kev. Value val) { /* next slide */ }
   public Value get(Key key)
      for (int i = hash(key); keys[i] != null; i = (i+1) % M)
        if (key.equals(keys[i]))
            return vals[i];
      return null;
```

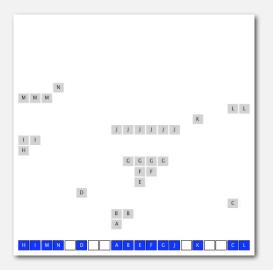
# Linear-probing symbol table: Java implementation

```
public class LinearProbingHashST<Key, Value>
  private int M = 30001;
  private Value[] vals = (Value[]) new Object[M];
  private Key[] keys = (Key[]) new Object[M];
  private Value get(Kev kev) { /* previous slide */ }
  public void put(Key key, Value val)
     int i:
     for (i = hash(key); keys[i] != null; i = (i+1) % M)
       if (keys[i].equals(key))
           break:
     keys[i] = key:
     vals[i] = val;
```

# Clustering

Cluster. A contiguous block of items.

Observation. New keys likely to hash into middle of big clusters.



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# Knuth's parking problem

Model. Cars arrive at one-way street with M parking spaces. Each desires a random space i: if space i is taken, try i + 1, i + 2, etc.

Q. What is mean displacement of a car?



Half-full. With M/2 cars, mean displacement is ~ 3/2.

Full. With M cars, mean displacement is  $\sim \sqrt{\pi M/8}$ .

#### Analysis of linear probing

Proposition. Under uniform hashing assumption, the average # of probes in a linear probing hash table of size M that contains  $N = \alpha M$  keys is:

$$\sim \frac{1}{2} \left(1 \,+\, \frac{1}{1-\alpha}\right) \qquad \sim \frac{1}{2} \left(1 \,+\, \frac{1}{(1-\alpha)^2}\right)$$

search hit

search miss / insert

Pf.



NOTES ON "OPEN" ADDRESSING.

(nuth 7/22/63

A Introduction and Definitions, then hadressing is a widely-used technique for Keeping (symbol tables." The method was first used in 1954 by Sammel, Amedah, and Bochme in an assembly program for the IBM 701. An extensive discussion of the method to the sethod was given by Peterson in 1957 [1], and frequent references have been made to it ever since (e.g. Schay and Spruin [2], Twercon [3]). However, the inling characteristics have supparently never been exactly established, and indeed thing the scheduling characteristics who falled to find the solution after some trial. Therefore it is the purpose of this note to



#### Parameters.

- M too large  $\Rightarrow$  too many empty array entries.
- M too small  $\Rightarrow$  search time blows up.
- Typical choice:  $\alpha = N/M \sim \frac{1}{2}$ . # probes for search mix is about 5/2 # probes for search miss is about 5/2

# Resizing in a linear-probing hash table

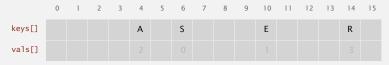
#### Goal. Average length of list $N/M \le \frac{1}{2}$ .

- Double size of array M when  $N/M \ge \frac{1}{2}$ .
- Halve size of array M when  $N/M \le \frac{1}{8}$ .
- · Need to rehash all keys when resizing.

#### before resizing

	U	- '	2	3	4	5	б	/
keys[]		E	S			R	Α	
vals[]								

#### after resizing



# Deletion in a linear-probing hash table

- Q. How to delete a key (and its associated value)?
- A. Requires some care: can't just delete array entries.

#### before deleting S

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
keys[]	Р	М			Α	С	S	Н	L		Е				R	Х
vals[]																



# ST implementations: summary

implementation		guarantee			average case	ordered	key	
implementation	search	insert	delete	search hit	insert	delete	ops?	interface
sequential search (unordered list)	N	N	N	½ N	N	½ N		equals()
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BST	N	N	N	1.39 lg <i>N</i>	1.39 lg <i>N</i>	$\sqrt{N}$	V	compareTo()
red-black BST	2 lg <i>N</i>	2 lg <i>N</i>	2 lg <i>N</i>	1.0 lg <i>N</i>	1.0 lg <i>N</i>	1.0 lg <i>N</i>	V	compareTo()
separate chaining	N	N	N	3-5 *	3-5 *	3-5 *		equals() hashCode()
linear probing	N	N	N	3-5 *	3-5 *	3-5 *		equals() hashCode()

 $<sup>^{</sup>st}$  under uniform hashing assumption

# Algorithms

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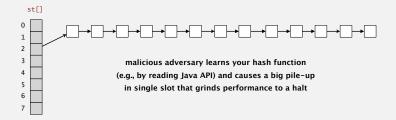
http://algs4.cs.princeton.edu

# 3.4 HASH TABLES

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- Inear probing
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# War story: algorithmic complexity attacks

- Q. Is the uniform hashing assumption important in practice?
- A. Obvious situations: aircraft control, nuclear reactor, pacemaker.
- A. Surprising situations: denial-of-service attacks.



#### Real-world exploits. [Crosby-Wallach 2003]

- Bro server: send carefully chosen packets to DOS the server, using less bandwidth than a dial-up modem.
- Perl 5.8.0: insert carefully chosen strings into associative array.
- Linux 2.4.20 kernel: save files with carefully chosen names.

# War story: algorithmic complexity attacks

#### A Java bug report.

#### Jan Lieskovsky 2011-11-01 10:13:47 EDT

Description

Julian Wälde and Alexander Klink reported that the String.hashCode() hash function is not sufficiently collision resistant. hashCode() value is used in the implementations of HashMap and Hashtable classes:

http://docs.oracle.com/javase/6/docs/api/java/util/HashMap.html http://docs.oracle.com/javase/6/docs/api/java/util/Hashtable.html

A specially-crafted set of keys could trigger hash function collisions, which can degrade performance of HashMap or Hashtable by changing hash table operations complexity from an expected/average O(1) to the worst case O(n). Reporters were able to find colliding strings efficiently using equivalent substrings and meet in the middle techniques.

This problem can be used to start a denial of service attack against Java applications that use untrusted inputs as HashMap or Hashtable keys. An example of such application is web application server (such as tomcat, see bus #750821) that may fill hash tables with data from HTTP request (such as GET or POST parameters). A remote attack could use that to make JVM use excessive amount of CPU time by sending a POST request with large amount of parameters which hash to the same value.

http://www.cs.rice.edu/~scrosby/hash/CrosbyWallach UsenixSec2003.pdf

# Algorithmic complexity attack on Java

Goal. Find family of strings with the same hash code.

Solution. The base-31 hash code is part of Java's string API.

key	hashCode()
"Aa"	2112
"BB"	2112

key	hashCode()
"AaAaAaAa"	-540425984
"AaAaAaBB"	-540425984
"AaAaBBAa"	-540425984
"AaAaBBBB"	-540425984
"AaBBAaAa"	-540425984
"AaBBAaBB"	-540425984
"AaBBBBAa"	-540425984
"AaBBBBBB"	-540425984

key	hashCode()
"BBAaAaAa"	-540425984
"BBAaAaBB"	-540425984
"BBAaBBAa"	-540425984
"BBAaBBBB"	-540425984
"BBBBAaAa"	-540425984
"BBBBAaBB"	-540425984
"BBBBBBBAa"	-540425984
"BBBBBBBB"	-540425984

2N strings of length 2N that hash to same value!

# Diversion: one-way hash functions

One-way hash function. "Hard" to find a key that will hash to a desired value (or two keys that hash to same value).

```
Ex. MD4, MD5, SHA-0, SHA-1, SHA-2, WHIRLPOOL, RIPEMD-160, ....
```

```
String password = args[0];
MessageDigest sha1 = MessageDigest.getInstance("SHA1");
byte[] bytes = sha1.digest(password);

/* prints bytes as hex string */
```

Applications. Digital fingerprint, message digest, storing passwords. Caveat. Too expensive for use in ST implementations.

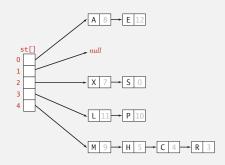
# Separate chaining vs. linear probing

#### Separate chaining.

- Performance degrades gracefully.
- · Clustering less sensitive to poorly-designed hash function.

#### Linear probing.

- · Less wasted space.
- · Better cache performance.



keys[]	
vals[]	

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Р	М			Α	С	S	Н	L		Е				R	Х
10	9			8	4	0	5	11		12				3	7

# Hashing: variations on the theme

Many improved versions have been studied.

#### Two-probe hashing. [separate-chaining variant]

- Hash to two positions, insert key in shorter of the two chains.
- Reduces expected length of the longest chain to  $\log \log N$ .

#### Double hashing. [linear-probing variant]

- Use linear probing, but skip a variable amount, not just 1 each time.
- · Effectively eliminates clustering.
- · Can allow table to become nearly full.
- · More difficult to implement delete.

#### Cuckoo hashing. [linear-probing variant]

- Hash key to two positions; insert key into either position; if occupied, reinsert displaced key into its alternative position (and recur).
- · Constant worst-case time for search.

#### Hash tables vs. balanced search trees

#### Hash tables.

- Simpler to code.
- · No effective alternative for unordered keys.
- Faster for simple keys (a few arithmetic ops versus  $\log N$  compares).
- Better system support in Java for strings (e.g., cached hash code).

#### Balanced search trees.

- · Stronger performance guarantee.
- · Support for ordered ST operations.
- Easier to implement compareTo() correctly than equals() and hashCode().

#### Java system includes both.

- Red-black BSTs: java.util.TreeMap, java.util.TreeSet.
- Hash tables: java.util.HashMap, java.util.IdentityHashMap.