

Section V

The Transistor

Before 1950 electronic equipment used vacuum tubes, otherwise called valves, which acted as transistors. They usually consumed a few Watts of power each and as a result created a lot of heat. They were also quite bulky as you can see below:

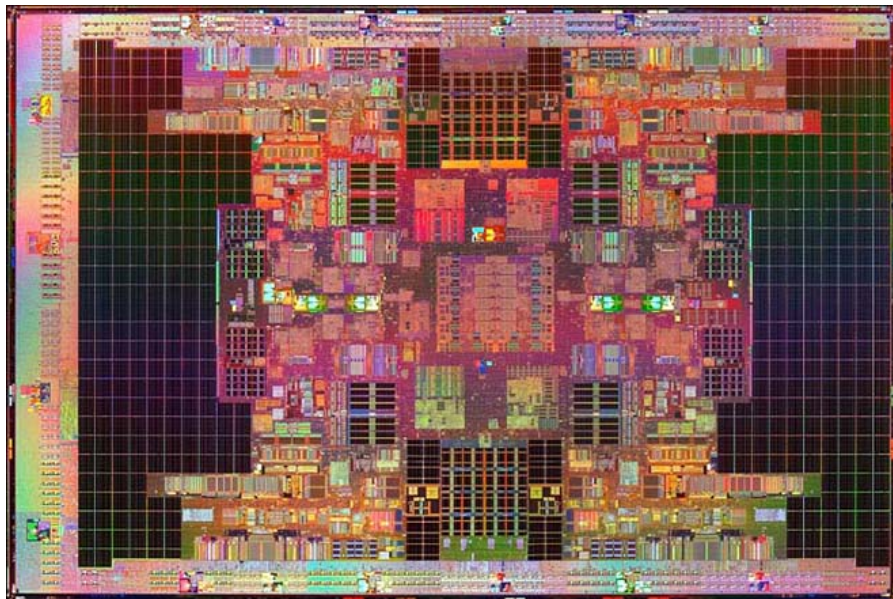
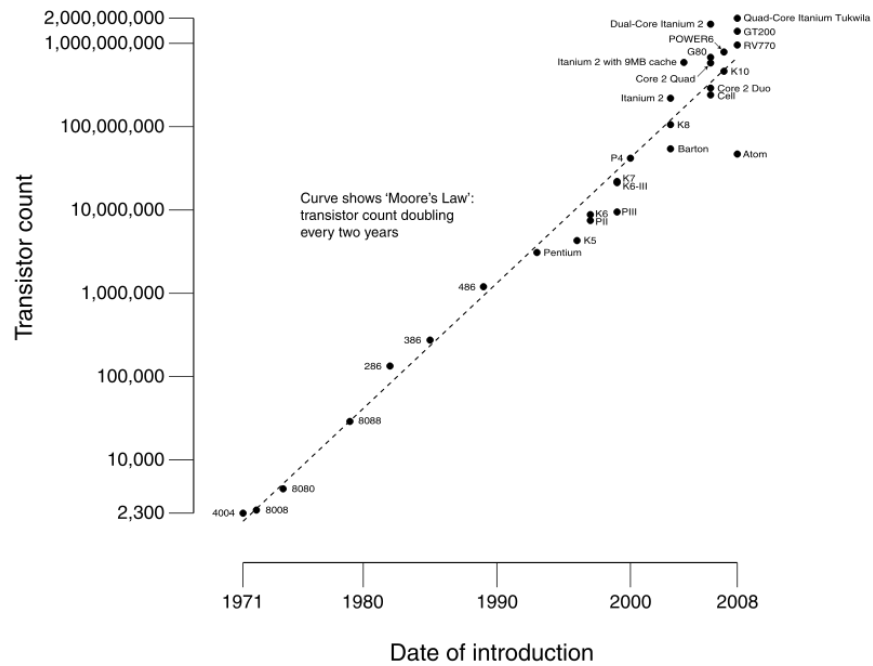


They worked by having an incandescent connection along with a separate cathode separated by a grid. Electrons flowed from the incandescent connection to the isolated cathode. The grid was connected to a supply voltage which modulated the current flow between the incandescent connection and the isolated cathode. In this way signal amplification was possible.

In 1951 William Shockley invented the first transistors based on semiconductors for which he received the Nobel Prize. The advantages of these types of transistor are that they can be made much smaller than a vacuum tube and that they consume much less power.

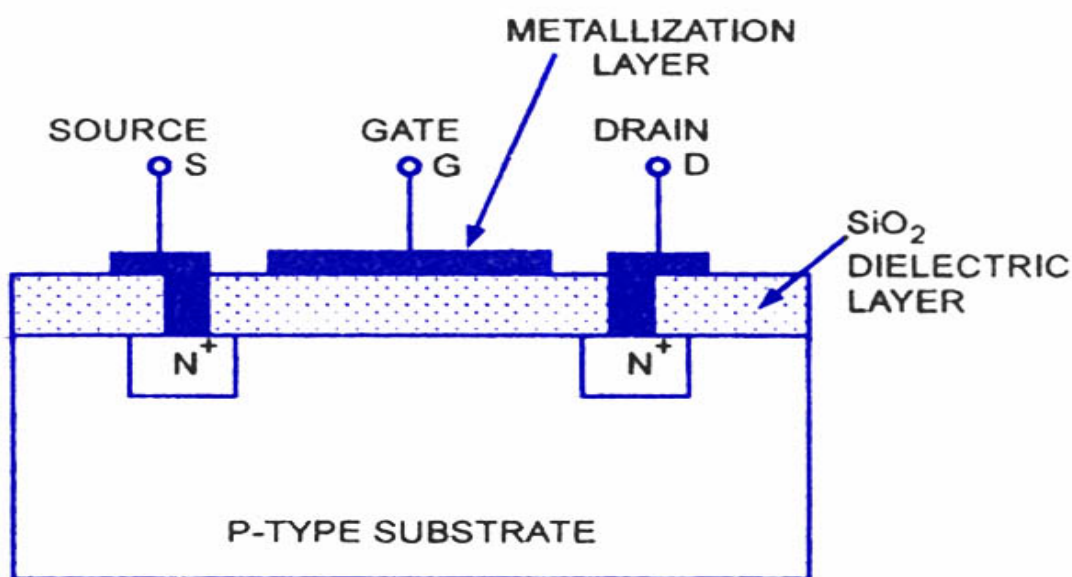
The transistor's impact on electronics has been enormous. Almost all electronic equipment produced today uses transistor technology. Before 1951 a computer filled an entire room and cost millions of euro. Today a much better computer sits on a desk with a few billion transistors in its CPU and costs roughly a thousand euro.

CPU Transistor Counts 1971-2008 & Moore's Law



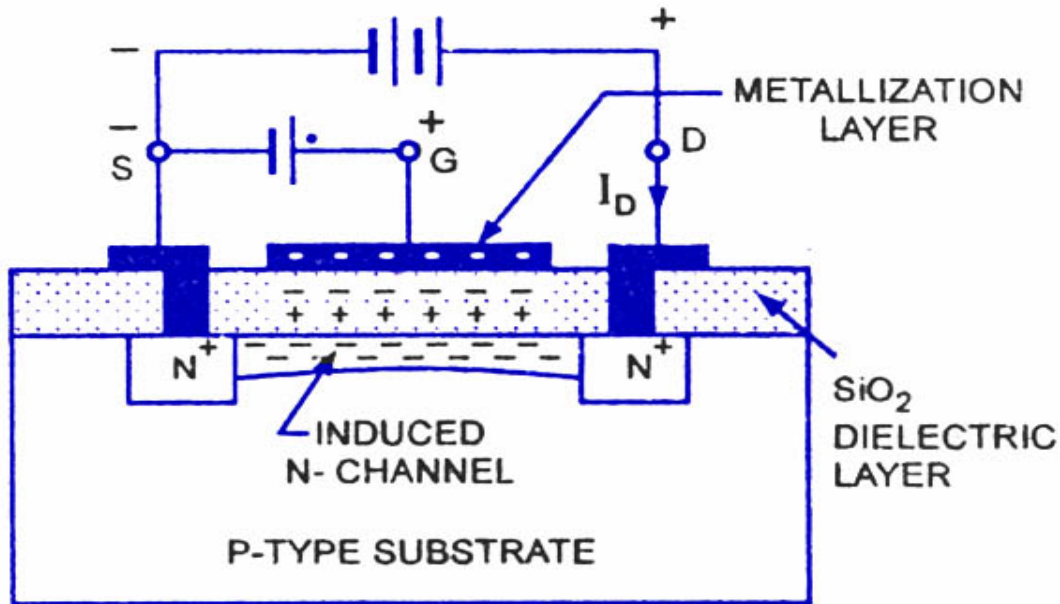
In this course we examine the most widely used transistor, the Enhancement Metal Oxide Field Effect Transistor – the Enhancement MOSFET (E-MOSFET). The advantage of these types of transistors over others is that faster switching speeds are possible which translates into, for example, faster computer processors. Furthermore the E-MOSFET is relatively easy to manufacture and can be used also as a resistor or a capacitor. It does not however achieve the same gain as, for example, the Bipolar Junction Transistor.

The structure of an n-channel E-MOSFET is as follows:

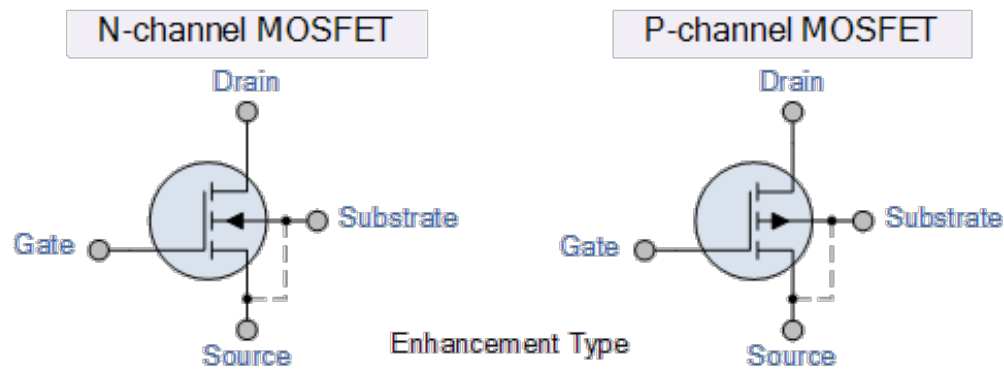


Between the gate and the substrate there is a layer of silicon dioxide which is a very good insulator. With a supply voltage connected between the drain and the source (ground) and a zero voltage between the gate and the source no current will flow because of the depletion regions that will exist between the n⁺ and p-type materials (the pn⁺ junction at the drain is in reverse bias and a depletion region exists at the pn⁺ junction at the source).

As the gate-source voltage is increased electrons are drawn from the source to the gate region forming an n-channel (lots of free electrons available for conduction) between the drain and the source and current starts to flow from the drain to the source (the depletion region at the pn⁺ junction at the drain is somewhat broken down due to this n-channel). The n-channel is called an inversion layer.



Note in the diagram above there is a small error. The gate is positively charged not negatively charged as indicated. Throughout this Section capital letters are used to denote dc voltages/currents which is to say time-independent voltages/currents. Small letters are used to denote time dependent voltages/currents. These may be purely ac or ac with a dc component. The minimum gate-source voltage that creates an inversion layer and breaks down the depletion regions sufficient for current to flow between the drain and the source, is called the *threshold voltage*, $V_{GS(th)}$. When v_{GS} is less than $V_{GS(th)}$, the drain-source current is zero. When v_{GS} is greater than $V_{GS(th)}$ the n-type inversion layer connects the drain and the source and we get current. The substrate is connected to the source to provide a source of electrons to feed the inversion layer. $V_{GS(th)}$ can vary from less than 1V to more than 5V depending on the particular device being used. The 3N169 is an example of an enhancement-type MOSFET. It has a threshold voltage of 1.5V. The symbols for enhancement-type MOSFETs are as follows:

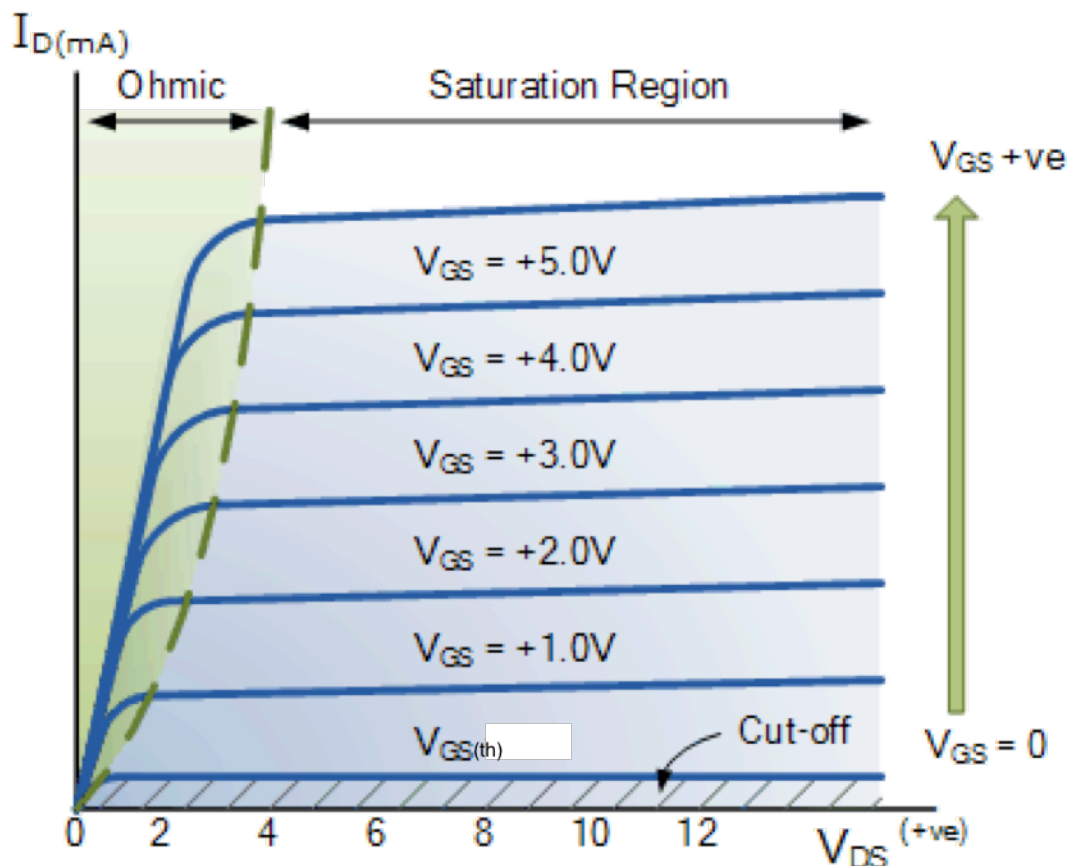


The operating principles for p-type MOSFETs are the same as for n-type only that v_{GS} is now negative.

MOSFETs have a very thin layer of silicon dioxide (most commonly found as quartz and sand - which is a very good insulator and the primary constituent of glass) between the gate and the substrate. This layer is kept as thin as possible to give the gate as much control over the drain current as possible. Because this insulating layer is so thin it is easily destroyed by excessive gate-source voltages. For example, if a MOSFET is supplied with a gate-source voltage greater than its maximum rating, $V_{GS(max)}$ then the MOSFET can be thrown away since it is most likely destroyed. A $\pm 30V$ rating is typical. However it is easy to destroy a MOSFET in other ways. If you insert the MOSFET into or remove it from a circuit with the power supply on then the inductive back-EMF may be enough to destroy the transistor. Even picking up a MOSFET may destroy it due to static electricity. This is why MOSFETs are often shipped with a wire ring around the leads. You remove the ring AFTER you have inserted the MOSFET into the circuit. Another way to protect a MOSFET is to build in a Zener diode in parallel with the gate-source connection. The idea is that the Zener breaks down before any damage occurs.

Characteristic Curves

Below is a set of Drain Curves (I_D vs V_{DS} for varying v_{GS}) for an n-channel E-MOSFET. The lowest curve is the $V_{GS(th)}$ curve. When v_{GS} is less than $V_{GS(th)}$ the drain current is extremely small and the transistor is effectively OFF. This region is known as the *Cutoff Region*. When v_{GS} is greater than $V_{GS(th)}$ significant drain current flows, with the amount depending on the value of v_{GS} .



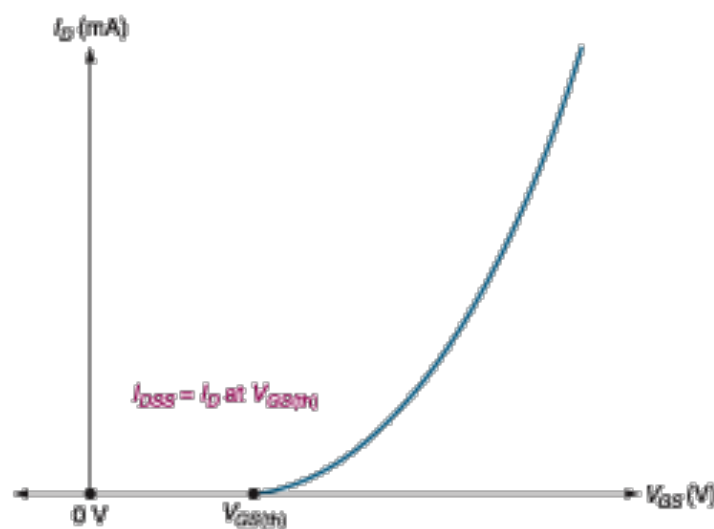
Note how for small V_{DS} there is an approximately linear relationship between I_D and V_{DS} . We therefore refer to this region as the *Linear Region* or *Ohmic Region*.

Each curve then 'flattens out'. With an increase in V_{DS} there is only a small increase in I_D . The reason for this is as follows: An increase in V_{DS} has the effect of forcing greater current flow between the drain and the source. However as V_{DS} is increased the PN Junction at the drain is

increasingly in reverse bias (like a diode) which, as the depletion region expands, has the effect of impeding current flow resulting in what is known as ‘pinch-off’. This results in little increased current flow for increased V_{DS} . Here the transistor is said to be saturated and hence this region is referred to as the *Saturation Region*. It is oftentimes also called the *Active Region*. The reason for this is that, when used as an amplifier, the transistor operates (or is active) in this region. The current in the saturation region is roughly constant for a given V_{GS} and is hence known as the *Saturation Current* ($I_{D(sat)}$) – or sometimes just referred to as the ‘On Current’ ($I_{D(on)}$) because the transistor is ON (or active) in this region for an amplifier.

Do note however, that for logic gates, the transistor is not chosen to be ON in this region. Rather, as we shall see later, it is biased to be ON in the Ohmic Region and OFF in the Cutoff Region.

Next is the transconductance curve which is the relationship between the **Saturation Current** ($I_{D(sat)}$ or $I_{D(on)}$) and the gate-source voltage (v_{GS}). Note that there is no dependence on V_{DS} since we are operating in the saturation region ($I_{D(sat)}$ does not vary with V_{DS} here).



The curve is a parabola with a vertex at $V_{GS(th)}$. The equation for this parabola is:

$$I_{D(on)} = K(v_{GS} - V_{GS(th)})^2$$

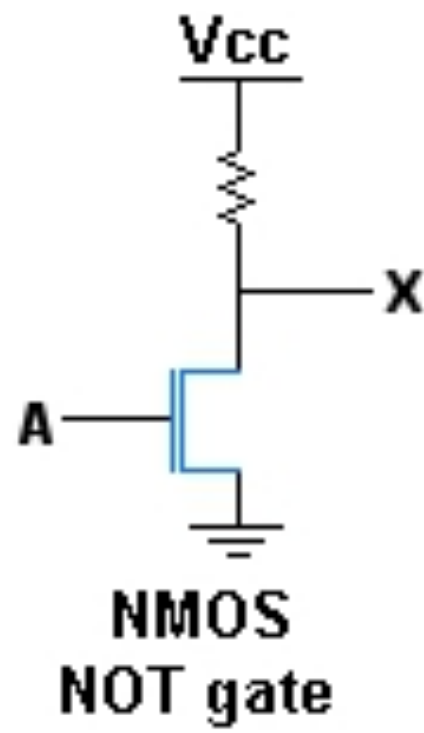
K is a constant that depends on the particular type of MOSFET being used. Data sheets usually give the coordinates for one point on the transconductance curve. This allows you to solve for K using the above equation.

Using transistors to build logic gates:

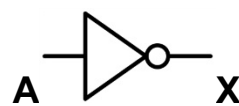
As you can see, from the diagrams below, transistors can be used to build logic gates. The principle of operation is fairly simple. Let's start with the inverter or NOT-gate. If the input is HIGH (i.e. a high voltage) then the transistor is switched ON (current flows from the drain to the source). If the resistor at the drain is chosen to be much greater than the 'ON' resistance of the transistor then the output will be LOW (i.e. a low voltage) since most of the supply voltage will be dropped across the drain resistor – recall the Potential Divider!

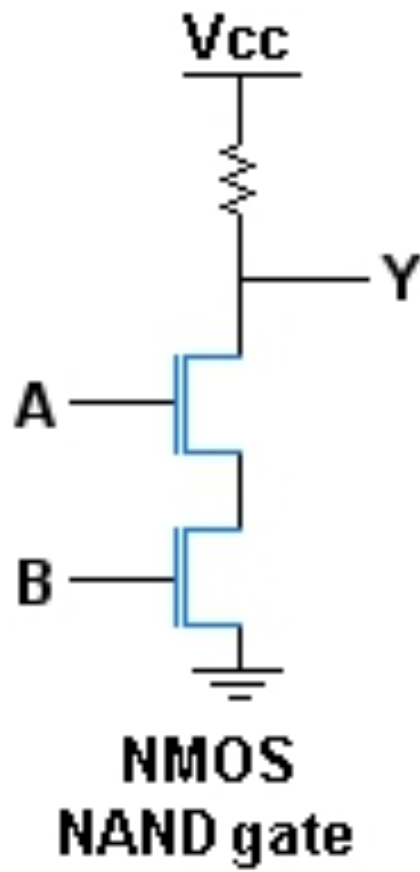
If the input is LOW then the transistor is OFF. There is no drain current and the output voltage is equal to the supply voltage (or rail voltage V_{DD}) i.e. HIGH. It is left to the student to figure out how the other logic gates work.

You will note with the NAND gate that two equivalent circuits are given. A transistor has a resistance albeit it not being an Ohmic device. Since a transistor occupies about 20 times less space on an IC as a resistor it is common to use transistors as 'resistors'.



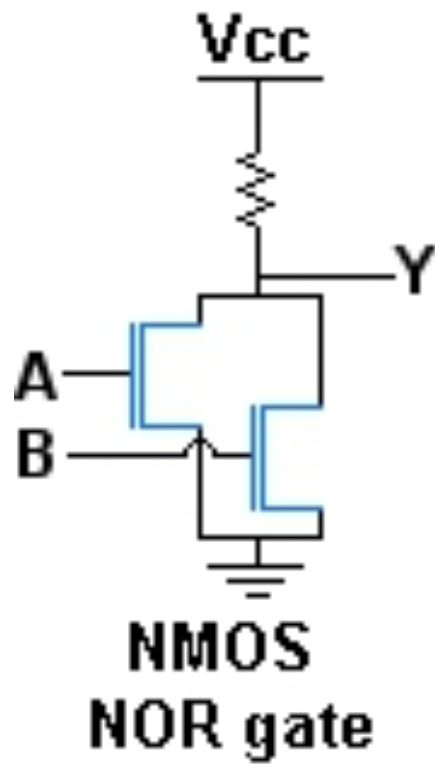
A	X = NOT A
0	1
1	0



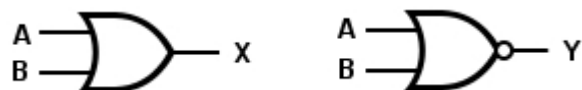


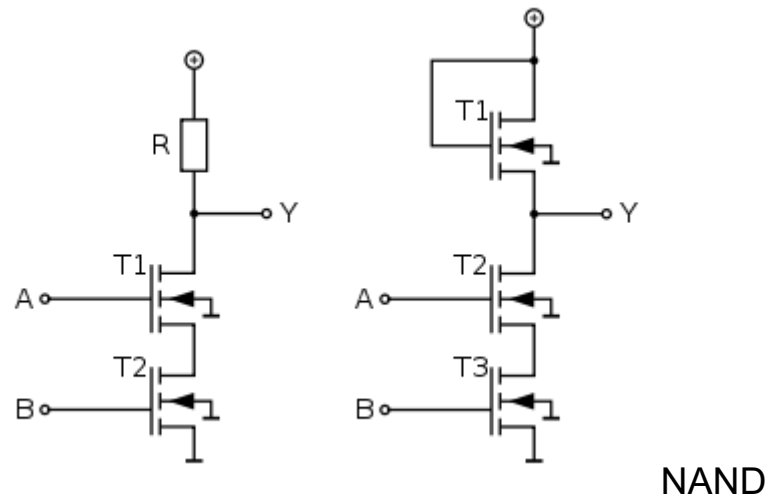
A	B	AND: $X = A \text{ AND } B$	NAND: $Y = \text{NOT}(A \text{ AND } B)$
0	0	0	1
0	1	0	1
1	0	0	1
1	1	1	0





A	B	OR: $X = A \text{ OR } B$	NOR: $Y = \text{NOT} (A \text{ OR } B)$
0	0	0	1
0	1	1	0
1	0	1	0
1	1	1	0





Staying with the inverter, one notes that the output voltage when a HIGH voltage is applied is that of a potential divider.

$$V_{out} = \frac{V_{DD}R_{ON}}{R_D + R_{ON}}$$

where R_D is the drain resistance and R_{ON} is the 'ON' resistance of the transistor. When we apply a voltage to the gate we want the output to be as close to zero as possible (within certain constraints as will be seen later). This means setting $R_D \gg R_{ON}$ which gives a better transition curve (from logic 1 to 0 and vice- versa). This is achieved by appropriate choice of resistor and transistor.

In effect what one is doing here is operating the transistor in the Cutoff and Linear (Ohmic) regions for small and large V_{GS} respectively. That is: for a LOW input $V_{GS} < V_{GS(th)}$ we are operating in the Cutoff Region and for a HIGH input $V_{GS} \approx V_{DD}$ (with V_{DS} made as small as possible by choosing $R_D \gg R_{ON}$) we are operating in the Linear Region. So for logic gates there are two operating points, Linear and Cutoff, corresponding to

HIGH and LOW inputs respectively at the gate. For this reason, in Digital Logic, the transistor is said to act as a switch. It is OFF (no current flow) when the input is LOW and ON (current flow) when the input is HIGH.

Biasing the Transistor when used as a Switch

The question now arises as to precisely what voltages (and consequently what resistance values) ought to be applied to the transistor. This process is referred to as biasing the transistor. Biasing means applying the correct dc operating voltages for the semiconductor device in question (recall we had Forward and Reverse Bias for diodes) such that it operates as desired.

To this end we employ a very useful concept known as the 'DC Load Line' (there is also an AC Load Line but we won't concern ourselves with that here). The Load Line is simply the relationship between I_D and V_{DS} and ***when the transistor is connected into the circuit!*** This relationship is obtained simply from Kirchoff's Voltage Law:

$$V_{DD} = I_D R_D + V_{DS}$$

or

$$I_D = \frac{-V_{DS}}{R_D} + \frac{V_{DD}}{R_D}$$

- which is a line (when plotting I_D Vs V_{DS}) with a slope of $-\frac{1}{R_D}$. This line intersects the vertical (I_D) axis at $\frac{V_{DD}}{R_D}$ and intersects the horizontal (V_{DS}) axis at V_{DD} . See figure below.

Now we have both a relationship between I_D and V_{DS} expressed as a set of drain curves (**regardless of what circuit the transistor is connected into**) and as a Load Line (**for when the transistor is connected into a particular circuit – with specified biasing resistor values**). **When the transistor is connected into the circuit in question** both curves must hold true which means that the operating point (V_{DS} , I_D) is somewhere at the intersections of the load line and drain curves. Which drain curve(s) exactly is (are) determined by one's choice(s) of V_{GS} .

The following is a plot of the Load Line superimposed on the drain curves. You can see that you can control the slope of the Load Line and its intersections with the drain curves by varying V_{DD} and R_D .

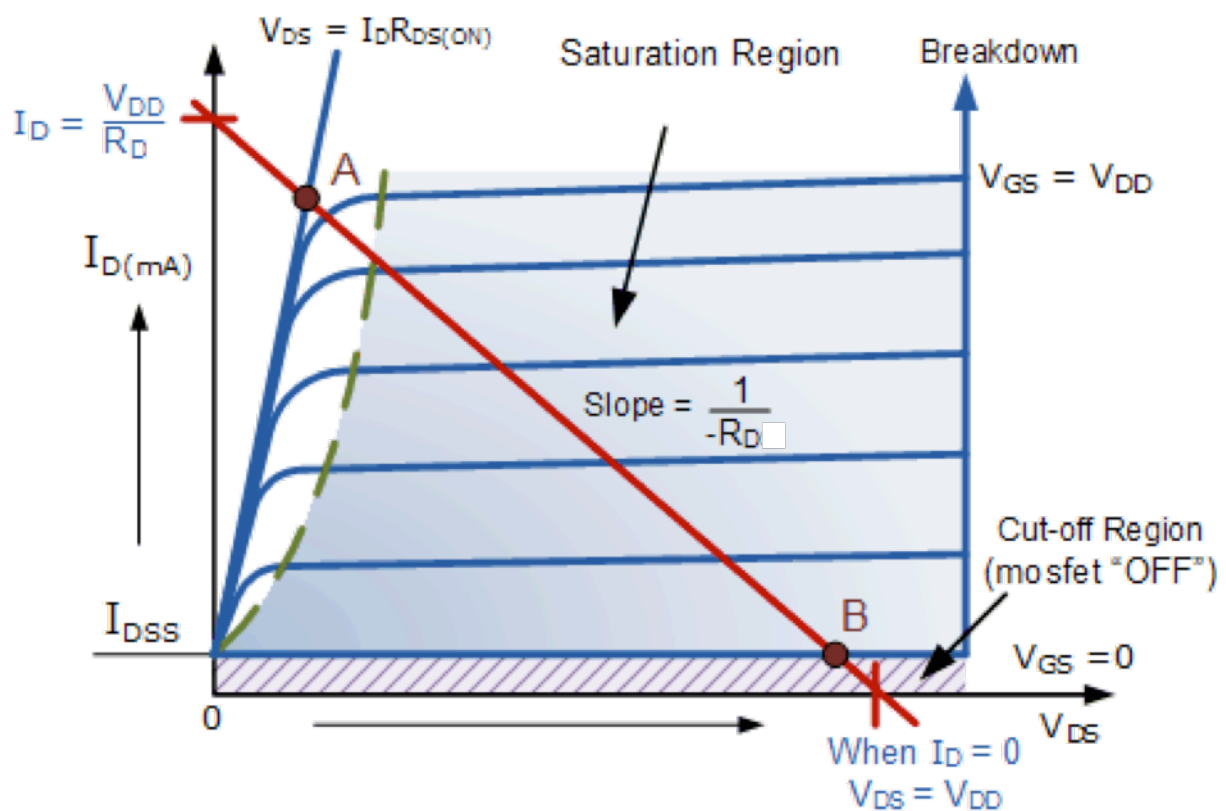
Now the question arises as to what values of V_{DD} and R_D to use?

- (i) V_{DD} is usually a 'given' for the circuit. It is desirable however that V_{DD} is as low as possible to minimise power dissipation. However low power devices are more expensive. There is also a technological limitation as to how low V_{DD} can actually be for the given application. Choice of V_{DD} is therefore both a cost-based decision and a practical one. Later we shall see that V_{DD} determines the potential amplification of the signal when the transistor is used as an amplifier.
- (ii) R_D should be chosen as accommodates the range of V_{GS} expected. This will normally be in the range $V_{GS} = 0$ to $V_{GS} = V_{DD}$ (LOW and HIGH resp').

For example, if one chooses R_D to be too high, then a small V_{GS} will switch the output (V_{DS}) LOW. In other words the inverter will be too sensitive. If R_D is made too low then V_{GS} may have to exceed V_{DD} to get LOW output. In other words the inverter is too insensitive.

The rule of thumb is to choose R_D that locates the operating point for a HIGH input, i.e. in the Ohmic Region, given by 'A' in the diagram i.e. such that $V_{GS} = V_{DD}$. This makes V_{DS} take on a low value as desired.

For a LOW input we are operating at point B (Cutoff) or lower ($V_{GS} < V_{GS(th)}$) on the load line. This gives us a HIGH output of $V_{DS} \sim V_{DD}$.

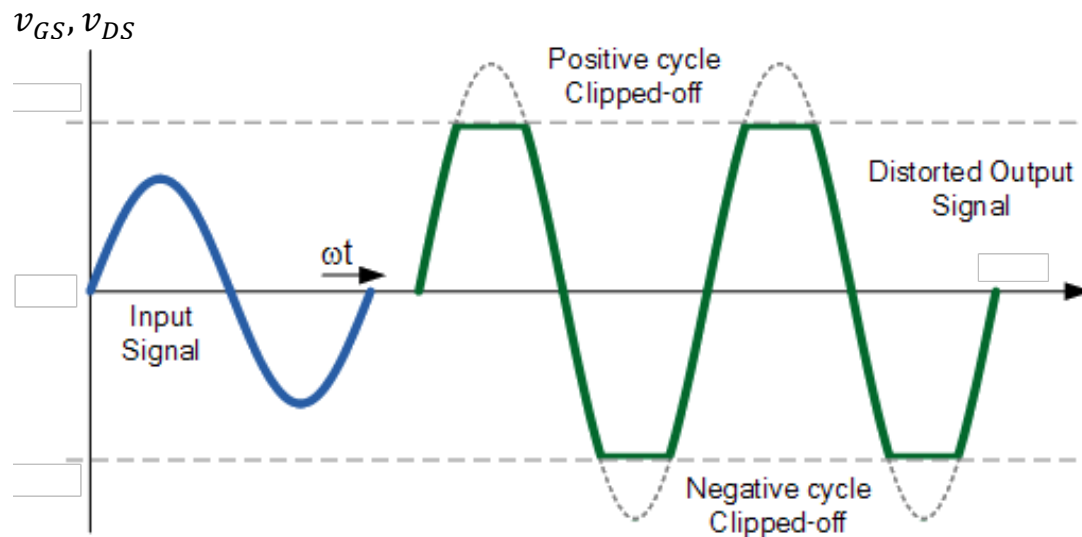


Using transistors to build amplifiers:

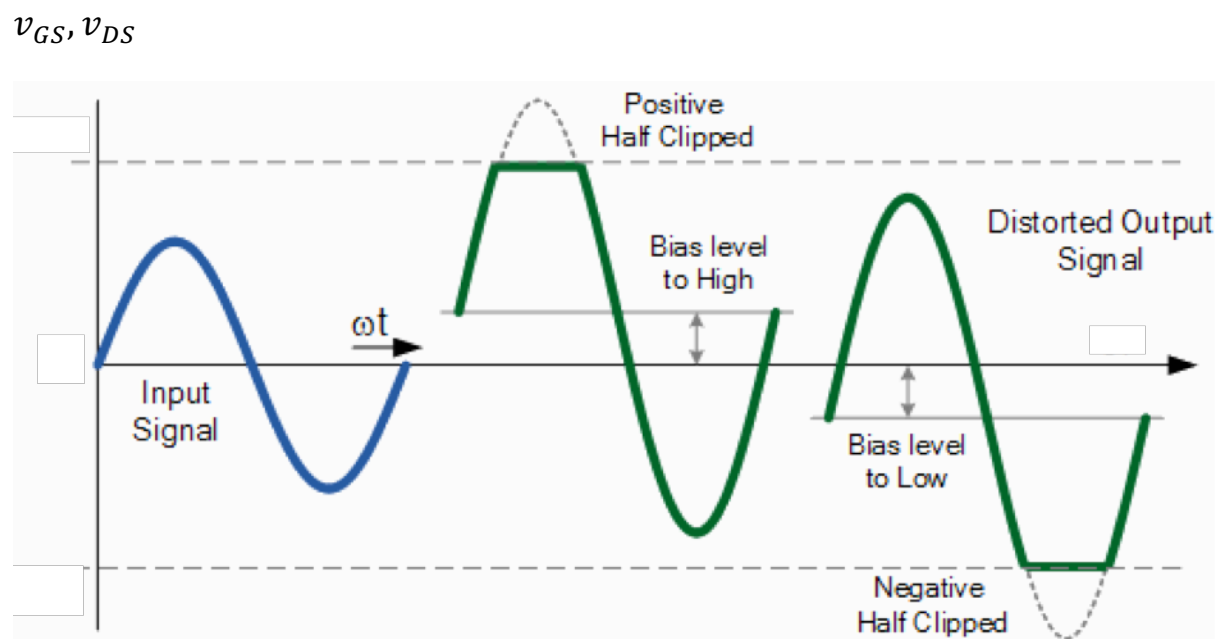
It is somewhat more complicated to use a transistor(s) to build amplifiers. Amplifiers are common in electronic systems but probably their most important function in relation to Computer Science is in telecommunications where a received wireless signal is amplified. This amplification is necessary to separate out the desired signal from all others and to make it large enough to process (and, for example, to convert to audible sound on phones etc.).

Biasing the E-MOSFETs for Amplifiers:

There are a number of ways by which the enhancement-type MOSFET can be biased when used as an amplifier. We will look at two here, namely, Voltage Divider Bias and Drain-Feedback Bias. As mentioned earlier, the first consideration in biasing an enhancement-type MOSFET is, that when used as an amplifier (as opposed to a switch) we have to ensure that the transistor is on at all times. This means setting V_{GS} to be sufficiently greater than $V_{GS(th)}$ such that variations in the input voltage (v_{GS}) will not cause the MOSFET to switch off while ensuring that V_{GS} is low enough such that operation is not pushed into the Ohmic Region where there will be little or no further increase in v_{DS} with increased v_{GS} . Operation in the Cutoff or Ohmic Regions will therefore result in clipping of the signal. In the Cutoff Region the transistor will simply switch off and the output will be approximately equal to V_{DD} . In the Ohmic Region the output voltage v_{DS} will take on a constant or near constant value despite an increase in v_{GS} . Note the slope of the line in the Ohmic region is very high.

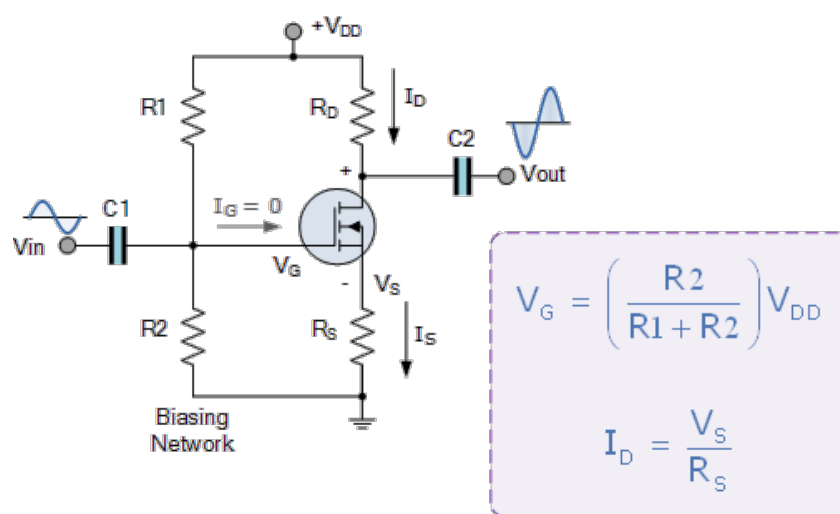


Above, the amplification of the input signal is too large resulting in clipping at either end of the output. This is remedied by making R_D smaller and/or V_{DD} larger or by simply reducing the amplitude of the input signal v_{GS} .



Apart from the reasons just given, the operating point for the transistor should be in the Active Region where there is the greatest variation in the output voltage v_{DS} versus the input voltage v_{GS} . In other words in this region we get greatest gain and if we stay in the Active Region we get no clipping of the output signal. Let us first consider voltage divider bias:

Voltage Divider Bias:



The potential divider formed by R_1 and R_2 provides a dc gate voltage in excess of $V_{GS(th)}$. This ensures that the transistor is on even for negative swings in the input voltage v_{GS} . The input voltage at the gate, v_{GS} , is the sum of the ac input signal and the dc biasing voltage. In other words the signal at the gate is an ac signal with a dc component. If the dc component is high enough the transistor will not switch off in negative swings of the input because the dc component prevents it from doing so. The capacitor C_1 at the gate allows the ac signal through while preventing dc to the source. In other words the capacitor serves to isolate the dc bias of the circuit. Ditto for capacitor C_2 . The capacitor values are chosen such that they provide negligible reactance at the frequencies of operation.

The time varying voltage at the gate (v_{GS}) causes a time varying current flow, i_D , through the transistor. This current also flows through the drain

resistor (R_D). Hence a time varying voltage appears at the output ($v_{DS} = V_{DD} - i_D R_D$). Hence the output voltage, v_{DS} , can vary from near 0

($i_D = \frac{V_{DD}}{R_D}$) to V_{DD} ($i_D = 0$). If the supply voltage at the rail (V_{DD}) is greater than the peak voltage at the input then we get same signal (albiet inverted) at the output as we have at the input albiet with a greater amplitude. ***It is in this way that amplification is achieved with a transistor.*** The gain or amplification is then given by:

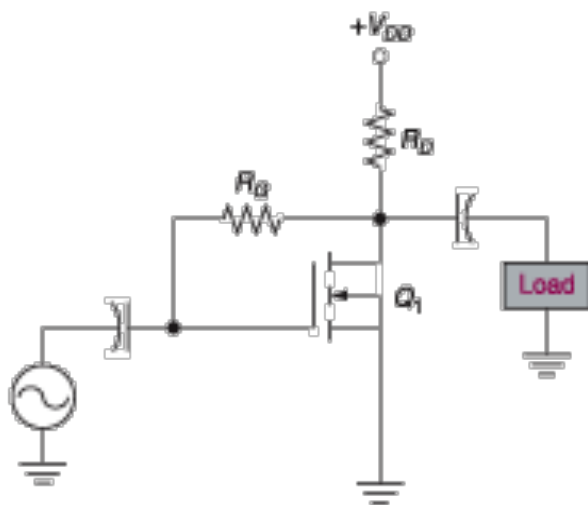
$$G = \frac{v_{out}}{v_{in}}$$

It is also of importance to note that the output for this amplifier design is inverted wrt the input! The solution to this problem is (if necessary) to pass the output through another *amplifier stage*.

The source resistance is not absolutely necessary but serves to stabilise the amplifier (keeping its gain constant) in the event of small variations in the rail voltage (V_{DD}). The source resistance is chosen to be small. If for some reason V_{DD} increases slightly then i_{DS} *increases*. This means that the voltage across the source resistance increases (since i_{DS} flows through it). The result of this is that the gate-source voltage decreases which has the effect of *reducing* i_{DS} so keeping the gain relatively constant. The same reasoning can be applied for V_{DD} decreasing. Sometimes you will see a capacitor in parallel with the source resistance. The idea is to allow ac to bypass the source resistance which provides stabilisation as described with its dc voltage while not reducing amplification of the ac signal (the source resistance on its own serves to reduce the ac gain of the amp').

Drain Feedback Bias:

Since resistors take up space on an IC another biasing method known as drain-feedback bias is used which reduces the resistor/transistor count.



Here the drain is connected to the gate via a high value resistor. There is no resistance at the source. Stabilisation is provided by the gate resistance (figure out how!). Since there is no gate current and no dc flow through the input capacitor, there will be no dc voltage drop across R_G (which has a very high value e.g. $50M\Omega$) and so $V_{GS} = V_{DS}$ (both of which are dc). In other words the dc equivalent circuit has the drain and the gate shorted. As before, the ac input signal, v_{GS} , 'sits' on the dc gate-source voltage. That is, the signal at the gate has both an ac and a dc component which can be treated separately (by Superposition). For the ac signal, since the gate-drain resistance is very high there is practically zero current and so it can be replaced with an open circuit. The drain feedback provides the bias at the gate to ensure the transistor is always

on i.e. $v_{GS} > V_{GS(th)}$ always. Of course this will also depend on the supply voltage V_{DD} and the resistor R_D both of which determine V_{DS} ($= v_{GS}$).

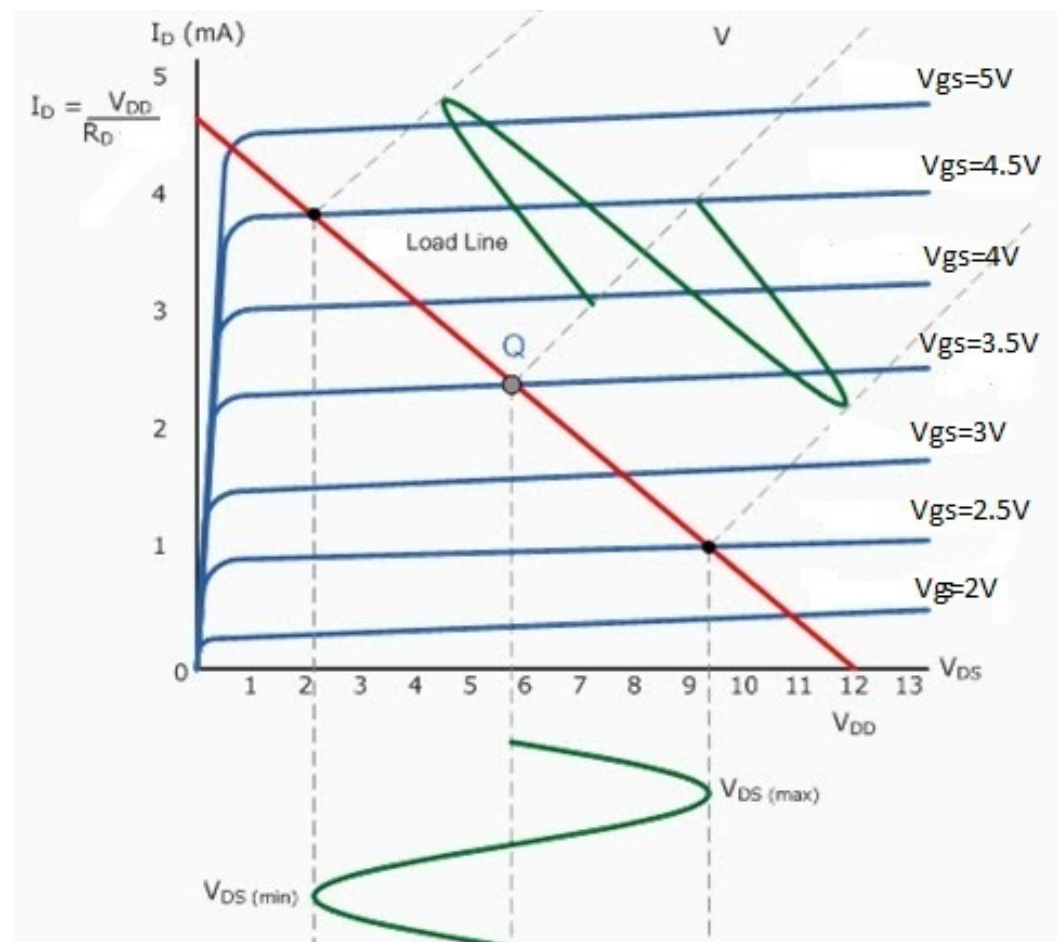
We shall see presently how to choose the bias resistance values for both voltage divider and drain feedback bias.

Choosing the Values of the Biasing Resistors

As before the dc load line is obtained via Ohm's Law and relates i_D and v_{DS} :

$$V_{DD} = v_{DS} + i_D R_D$$

For simplicity we have ignored the source resistance in voltage divider bias (in which case $R_D \rightarrow R_D + R_S$). As before a plot of the load line is then superimposed on the drain curves.



This time the operating point, often referred to as the Q-point (quiescent point) of the circuit is chosen to lie in the middle of the active region.

There are three reasons for this:

- (i) In the Active Region we can get the greatest variation in v_{DS} versus v_{GS} (as opposed to in the Ohmic Region), i.e. we get the greatest gain.
- (ii) We wish to avoid the transistor going into cutoff where we get clipping at the upper end of the output signal.
- (iii) We wish to avoid the transistor going into the linear region of operation where we get clipping at the lower end of the output signal.

You can see from the plot that the operating point moves up and down the Load Line about the Q-Point such that the gate-source voltage can vary without the MOSFET switching off or moving into the Linear Region (clipping).

One gets a consequent variation in v_{DS} potentially varying from near 0 to V_{DD} which is an amplification of v_{GS} .

To bias the transistor correctly we do the following:

- 1) Note the range of the input v_{GS} expected.
- 2) Choose the drain curve corresponding to middle (average) of this v_{GS} range - V_{GSQ} .
- 3) Choose V_{DD} - usually a given. This gives the point of intersection of the Load Line with the horizontal (v_{DS}) axis.
- 4) Choose R_D which (along with V_{DD}) determines the point of intersection of the Load Line with the vertical (i_D) axis.
- 5) Adjust R_D such that there is roughly an equal distance along the Load Line between the chosen drain curve and the Linear and Cutoff Regions respectively. In other words the Q-point should lie on the centre of the Load Line in the active region (see

diagram). Note that choosing R_D too high will push the operating point into the Linear Region (where we get clipping). Choosing R_D too low will result in unnecessary power dissipation.

6) In the case of Voltage Divider bias, choose two (fairly large – so as to minimise power dissipation) resistors, R_1 and R_2 , to give V_{GSQ} at the gate.

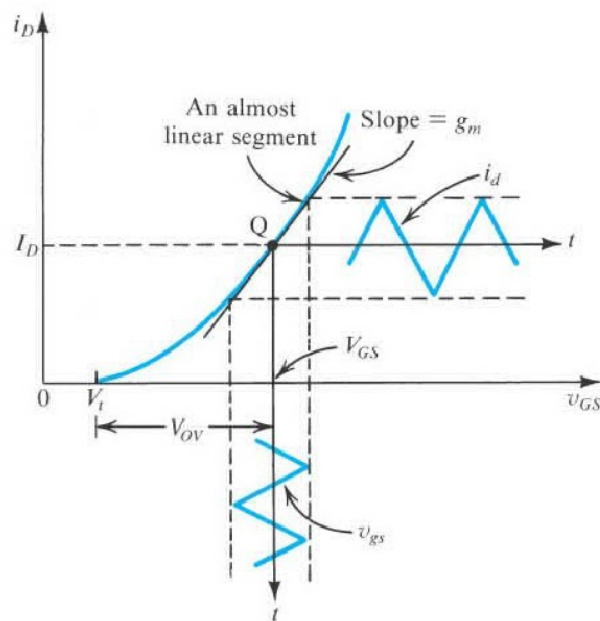
7) In the case of Drain Feedback Bias choose a very large gate resistance (e.g. $50\text{M}\Omega$). Note the saturation drain current I_{DQ} at V_{GSQ} and choose R_D such that you get V_{GSQ} at the gate (remember R_D and the transistor form a voltage divider).

Usually however the datasheet that comes with the transistor will provide biasing information and maximum ratings so that some of this design work is already done for you.

If you want to increase/decrease amplification you must either increase/decrease V_{DD} . Amplification comes at a price however since the power consumption will increase with increased V_{DD} . Typically one tries to keep i_D as low as possible for a given application. However if you want greater amplification you must increase the power.

The operation of a transistor can also be observed on the Transconductance Curve. The output is then, as before,

$$v_{DS} = V_{DD} - i_D R_D.$$



What is notable here is that there is only an *approximately* linear relationship between the output and the input. The greater the amplification the more noticeable this non-linearity becomes. Good amplifier design includes good choice of transistor (usually more expensive) and other components such that this non-linearity is not noticeable. However non-linearity cannot be eliminated entirely.

Problem:

For a drain feedback E-MOSFET amplifier the data sheet specifies $I_{D(on)} = 3mA$ for $V_{DS(on)} = 10V$ (Q-Point). If $V_{DD} = 25V$ select a value of R_D that allows the MOSFET operate at the specified Q-point.

Solution:

$$v_{DS} = V_{DD} - i_D R_D$$

$$R_D = \frac{25V - 10V}{3mA} = 5k\Omega$$

Problem:

For an n-channel E-MOSFET the manufacturer specifies $V_{GS(th)} = 4V$ and $I_{DS} = 7.2mA$ at $V_{GS} = 10V$. For Drain Feedback Bias with $V_{DD} = 24V$ and $R_G = 100M\Omega$ specify R_D for operation at $V_{DS} = 8V$.

Solution:

Given:

$$i_{D(on)} = K(v_{GS} - V_{GS(th)})^2$$

Then:

$$i_{D(on)} = 0.0072 = K(v_{GS} - V_{GS(th)})^2 = K(10 - 4)^2$$

$$\therefore K = \frac{0.0072}{6^2} = 0.0002 \text{ A/V}^2$$

Because $i_G = 0$ there is no dc voltage drop across the resistor R_G .

Hence $v_{GS} = v_{DS} = 8V$ and $i_{D(on)} = 0.0002(8 - 4)^2 = 3.2mA$.

But:

$$v_{DS} = V_{DD} - i_D R_D$$

Solving for R_D gives $R_D = 5k\Omega$

Problem:

For a Voltage Divider Bias configuration using a Depletion MOSFET (which operates for V_{GS} positive and negative) with $V_{DD} = 16V$, $V_D = 12V$, $V_{GSQ} = -2V$, $R_1 = 91K\Omega$, $R_2 = 47K\Omega$, $R_D = 1.8K\Omega$ find R_S .

Solution:

$$V_G = \frac{47.16}{47 + 91} = 5.44V$$

$$I_D = \frac{V_{DD} - V_D}{R_D} = 2.22mA$$

Now:

$$V_{GS} = V_G - I_D R_S$$

$$\Rightarrow R_S = 3.35K\Omega$$

The nearest commercial value is $3.3K\Omega$

Problem:

For a drain feedback biased E-MOSFET we are given the following information: $V_{DS} = \frac{1}{2} V_{DD}$, $I_D = I_{D(sat)} = 4mA$ and $V_{GS} = V_{GS(th)} = 6V$. Find V_{DD} and R_D .

Solution:

$$V_{GS} = V_{DS} = \frac{1}{2}V_{DD} = 6V$$

$$\Rightarrow V_{DD} = 12V$$

$$R_D = \frac{V_{DD} - V_{DS}}{I_D} = 1.5k\Omega$$

Problem:

For an E-MOSFET with Voltage Divider Bias we are given the following information:

$R_1, R_2 = 1M\Omega$; $R_D, R_S = 6K\Omega$; $V_{DD} = 10V$; $V_{GS(th)} = 1V$ and

$K = 0.5mA/V^2$.

We may assume that the MOSFET is operating in the Saturation Region as these are recommended values.

Find V_{GS} , V_{DS} and I_D .

Solution:

$$V_G = \frac{R_2}{R_1 + R_2}V_{DD} = \frac{1}{2}V_{DD} = 5V$$

Then:

$$V_{GS} = V_G - V_S = V_G - I_D R_S = 5 - 6I_D$$

The drain current can be computed thus:

$$I_D = K(V_{GS} - V_{GS(th)})^2 = 0.5(5 - 6I_D - 1)^2 = 36I_D^2 - 50I_D + 16 = 0$$

Using $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ this yields two potential solutions for I_D :

$$I_D = 0.89mA$$

and

$$I_D = 0.5mA$$

To determine which of the solutions is correct we compute the gate-source voltage for each:

For $I_D = 0.89mA$, $V_{GS} = 5 - 6I_D = -0.34V$ and for $I_D = 0.5mA$, $V_{GS} = 5 - 6I_D = 2V$. Since $V_{GS} > V_{GS(th)}$ for operation in the saturation region then:

$$I_D = 0.5mA, \quad V_{GS} = 2V$$

The corresponding drain voltage is then:

$$V_D = V_{DD} - I_D R_D = 10 - 6I_D = 7V$$

Hence:

$$V_{DS} = V_D - V_S = V_D - I_D R_S = 7 - 3 = 4V$$

