

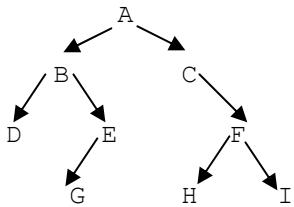
CSS 343 Exam The actual exam has space for your work. Be as clear as possible. You don't have to comment code, but use meaningful names and proper indentation. Show all work!!!! Don't erase.

1. Assume a Binary Tree class has a member function call play and a tree has been built as shown.

What's the output of main? Show the execution tree.

(10 pts)

```
int BinTree::play() const {  
    int n = 0;  
    return helper(root, n);  
}  
  
int BinTree::helper(Node* current, int n) const {  
    if (current == NULL)  
        return n;  
    if (current->right != NULL || current->left != NULL)  
        return 1 + helper(current->left, n+1) + helper(current->right, n+1);  
    return 0;  
}
```



2. Give the complexity (tight big-oh) of the following. You need not show work.

(15 pts)

(a). Find the smallest value in an AVL tree of n items.

(b). Find the smallest value in a binary heap of n items.

(c). Insert one item into a binary heap of n items.

(d). Destructor for a binary search tree of n items.

(e). Remove one edge in a graph of n nodes and E edges stored in an adjacency matrix.

(f). The maximum number of unique edges in an undirected graph of n nodes.

(g). Breadth-first ordering on a graph with n nodes and E edges stored in an adjacency matrix.

3. Given the following characters and frequency of occurrence in a message, use the Huffman encoding algorithm to find a unique encoding for the characters. Show all work.

(10 pts)

Letter	Frequency
a	10
b	15
c	20
d	22
e	30

4. Demonstrate the heap sort (done efficiently) on the values: 10 5 7 11 6 3 2 13 15 1 4. Show only the first three passes of the algorithm (three values are sorted). There is no code writing. Redraw your heaps when needed for clarity.

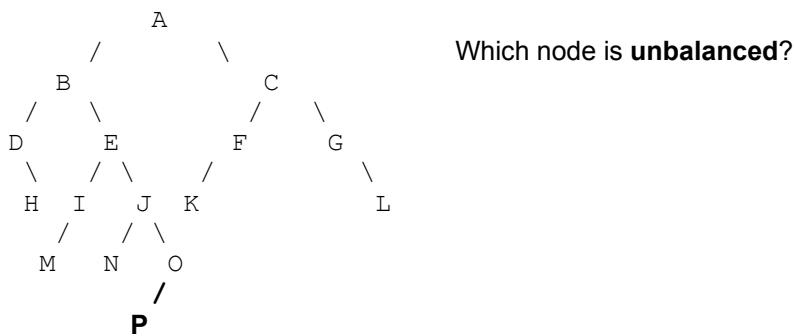
(15 pts)

5. Given the following AVL tree structure (letters represent appropriate values).

Suppose a value was added as shown (in the P position).

Show the balanced tree after the insertion. Show each step.

(5 pts)



6. Consider the following adjacency matrix for a directed graph. (A dash means there is no edge.) (20 pts)
Some graph is given.

(a). Draw the graph using these nodes →

(b). What is the breadth-first ordering? (No need to show work.)

(c). What is the depth-first ordering? (No need to show work.)

(d). Use Dijkstra's algorithm to find the shortest path from source node 1 to all other nodes in the graph.
Show `v`, `T[source][i].dist` and `T[source][i].path` at each state in the algorithm.

7. Consider your Polynomial class only the array content contains double : (10 pts)

```
class Poly {
    friend ...
public:
    Poly(int coeff=0, int maxExp=0);           // constructor, sets size=maxExp+1
    ~Poly();                                     // destructor
    Poly(const Poly &);                        // copy constructor
    void integrate();                           // integrate poly
    ...
private:
    double* ptr;                                // pointer to first array element
    int size;                                    // size of the array
};
```

Write the member function `integrate` which replaces the current polynomial with its integral (as in calculus). E.g.,

```
Poly A(0,4);
cin >> A;                               // user enters values so A = +10x^4 -7x^2 +3
A.integrate();
cout << A << endl;                     // outputs: +2.00x^5 -2.33x^3 +3.00x
```

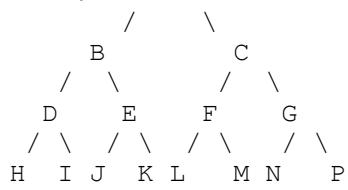
Now, don't freak out, it's not hard to find an integral. Reviewing your calculus, to integrate a polynomial, you find a new coefficient and new exponent for each term. To find the new coefficient, you add one to the exponent and divide the current coefficient by that value. The exponent becomes the old value plus one. (Technically it's also possibly plus a constant, but ignore that possibility.) Assume operator<< outputs correctly as shown. Anything you use, you must write.

For example, if the polynomial is $10x^4 - 7x^2 + 3$ its integral is:

$$\begin{aligned} & \frac{1}{5} \cdot 10x^{4+1} - \frac{1}{3} \cdot 7x^{2+1} + 3x^{0+1} \\ & = +2.00x^5 - 2.33x^3 + 3.00x \end{aligned}$$

8. Implement function(s) for a BSTree class that determine whether or not the tree is fully complete (all levels filled completely). Assume usual Node, with member data: `NodeData* data, Node* left, Node* right`
Any function you use, you must write. For example: (20 pts)

T1:



Sample main:

```
BSTree T1;
BSTree T2;
bool complete;
...
complete = T1.isComplete();      // returns true
complete = T2.isComplete();      // returns false
```

T2:

