

1. **[6 points]** Let $f = \{(x, y) \mid x^2 = 1 - y\}$.

Prove that f is a function.

2. **[6 points]** Let $f = \{(x, y) \mid x^2 = 1 - y^2\}$.

Prove that f is not a function.

3. **[8 points]** Let $f : \mathbb{R} \setminus \{0\} \rightarrow \mathbb{R} \setminus \{1\}$, $f(x) = 1 + \frac{1}{x}$.

(a) Prove that f is one-to-one.

(b) Prove that f is onto $\mathbb{R} \setminus \{1\}$.