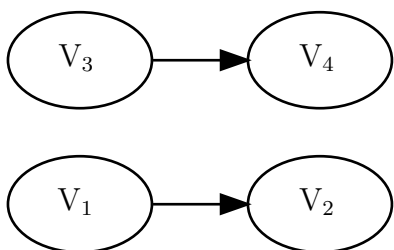


Power Walk Calculations

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Take the exemplar Graph from Figure 1:



$$\Gamma = I - nD_B^{-1}$$

Where we have the following:

$$\beta = 10$$

$$B = \beta^A$$

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

$$\Rightarrow B = \begin{bmatrix} 10 & 1 & 1 & 1 \\ 1 & 10 & 1 & 1 \\ 1 & 1 & 10 & 1 \\ 1 & 1 & 1 & 10 \end{bmatrix}$$

D_B is a diagonal matrix of the column sums:

$$D = \begin{bmatrix} 13 & 0 & 0 & 0 \\ 0 & 13 & 0 & 0 \\ 0 & 0 & 13 & 0 \\ 0 & 0 & 0 & 13 \end{bmatrix}$$

Hence the Inverse is:

$$D_B^{-1} = \frac{I}{13}$$

Putting it all together:

$$\begin{aligned} \Gamma &= I - nD_B^{-1} \\ &= I - \frac{4 \cdot I}{13} \\ &= \frac{9}{13} \cdot I \\ &= \begin{bmatrix} \frac{9}{13} & 0 & 0 & 0 \\ 0 & \frac{9}{13} & 0 & 0 \\ 0 & 0 & \frac{9}{13} & 0 \\ 0 & 0 & 0 & \frac{9}{13} \end{bmatrix} \\ &\approx \begin{bmatrix} 0.6923 & 0 & 0 & 0 \\ 0 & 0.6923 & 0 & 0 \\ 0 & 0 & 0.6923 & 0 \\ 0 & 0 & 0 & 0.6923 \end{bmatrix} \end{aligned}$$