Let $X:=(x_n)$ and $Y:=(y_n)$ by sequences in $\mathbb R$ and let the partial sums of $\sum (y_n)$ be denoted by (s_0n) with $s_0:=0$

If m > n, then

$$\sum_{k=n+1}^{m} [x_k y_k] = (x_m s_m - x_{n+1} s_n) + \sum_{k=n+1}^{m} k = n + 1^{m-1} (x_k - x_k + 1) s_k \quad (1)$$