

Robotic Mapping & Localization

Kaveh Fathian

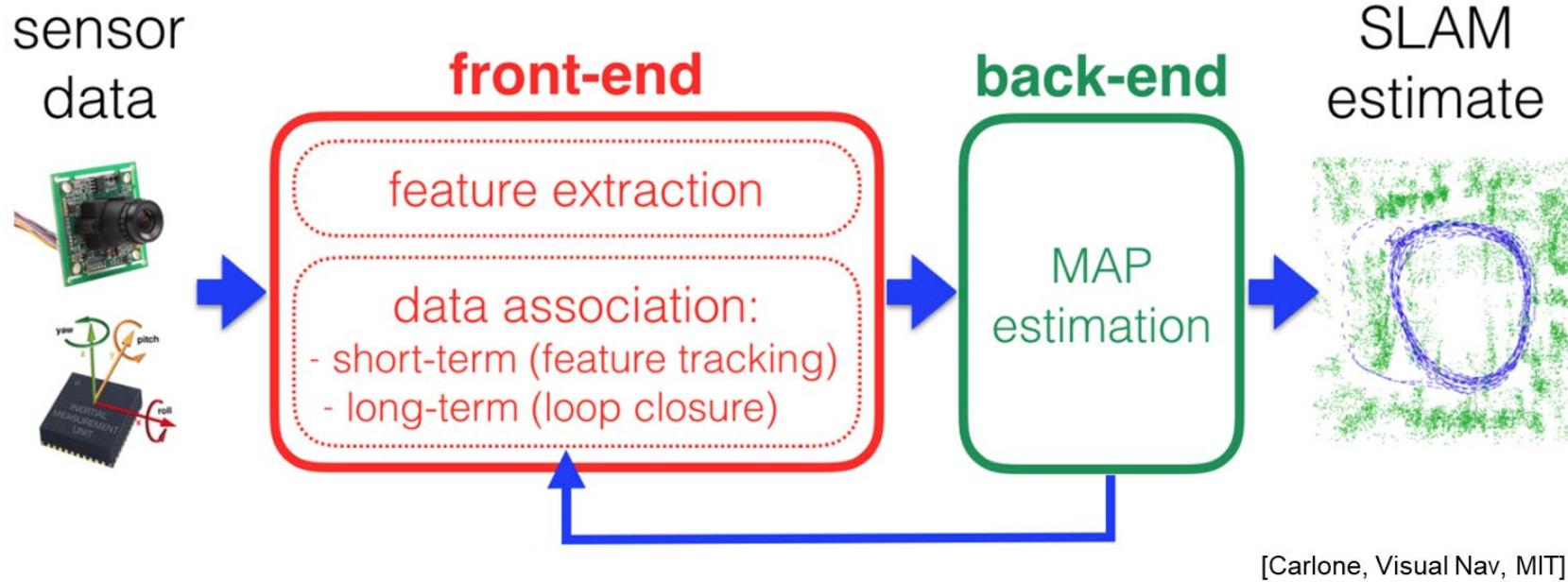
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Computer Science Department

Colorado School of Mines

Lec03: Image & Camera

Review



- A SLAM pipeline consists of
 - Sensors
 - Frontend algorithms
 - Backend algorithms

Structure from Motion (SfM)

Scene Graph



Sparse Model



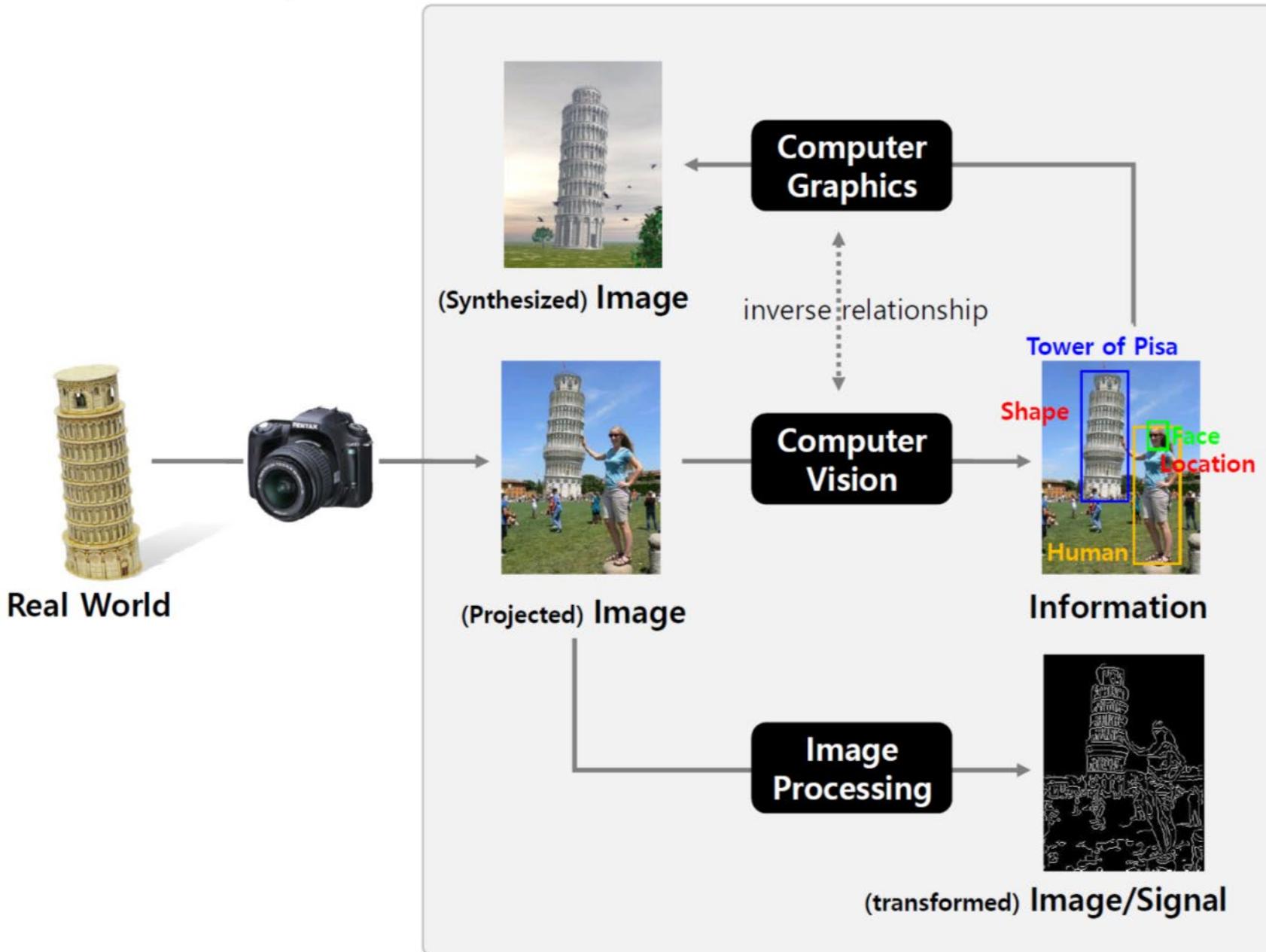
SfM

Dense Model

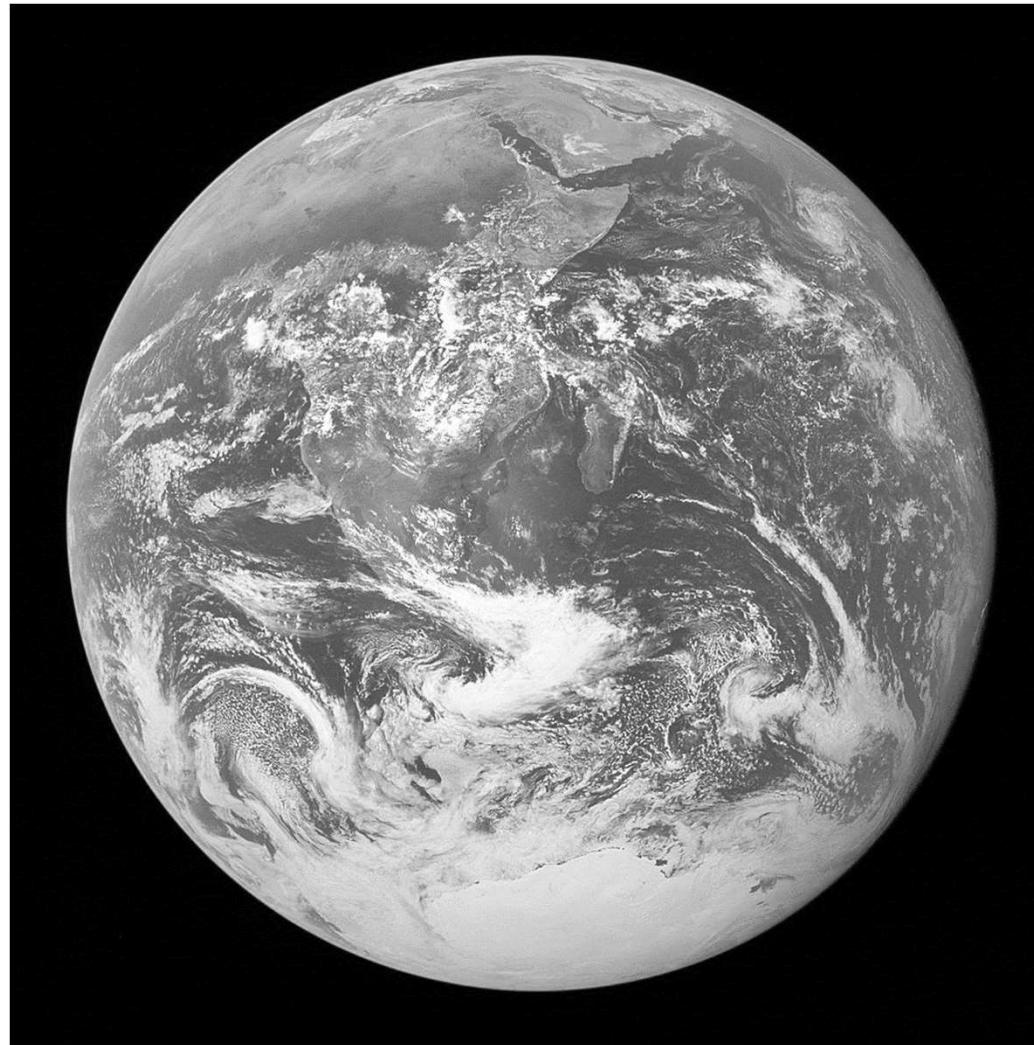


MVS

Computer Vision and Nearby Fields

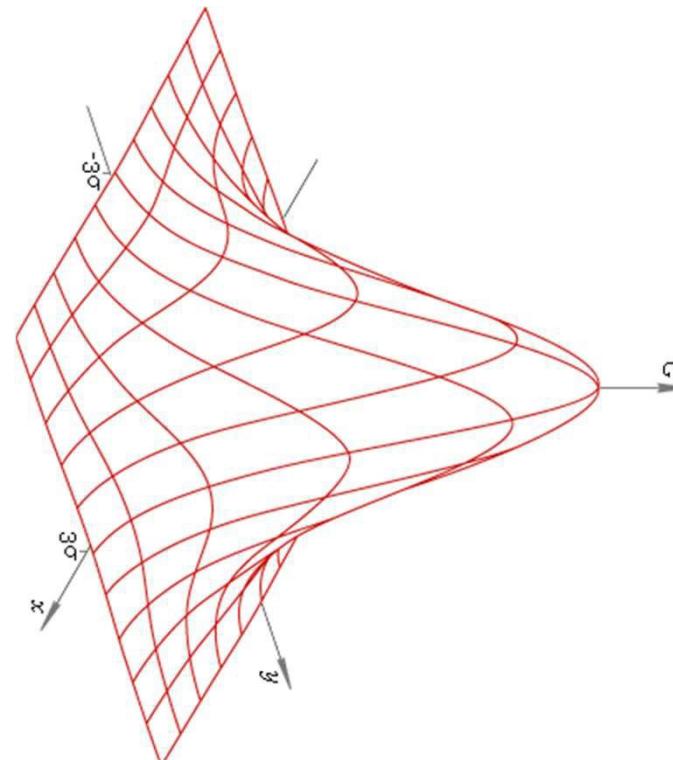
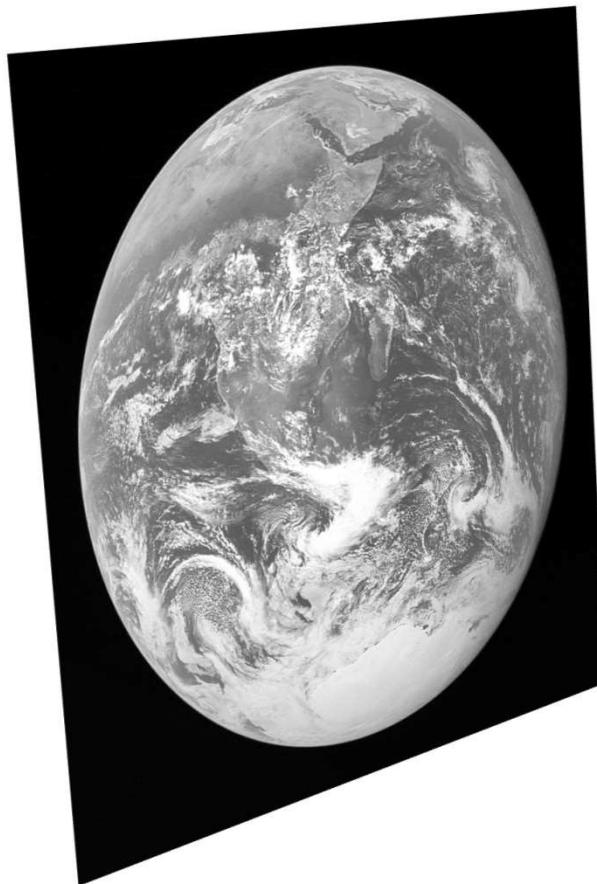


Image



Blue Marble. NASA | Apollo 17

Image

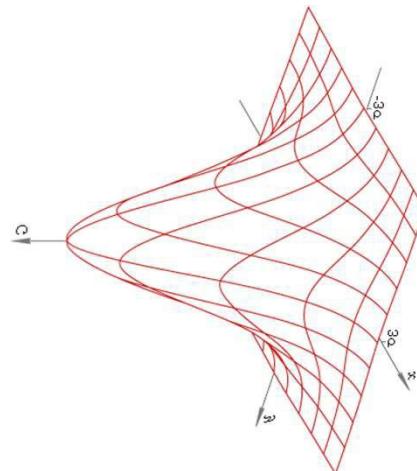
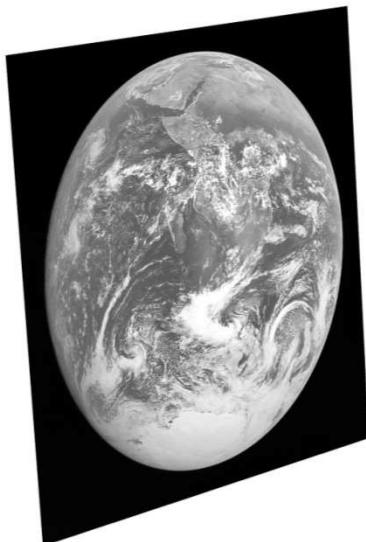


Blue Marble. NASA | Apollo 17

Signal

Definition

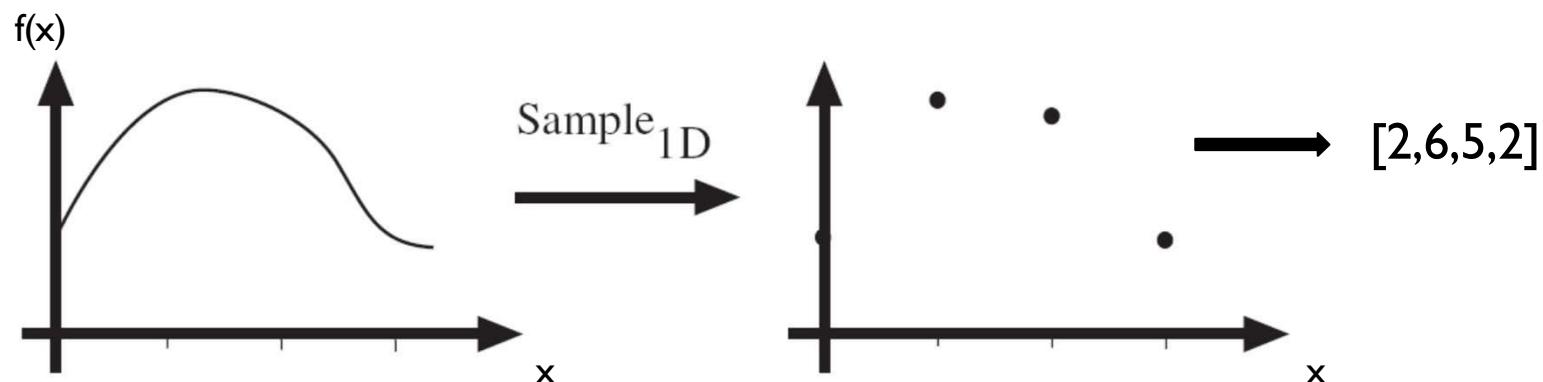
Signal: A (multi-dimensional) function that contains information about a phenomenon.



- Signals can be
 - Continuous: light
 - Discrete: measurement of a light
 - Sampling: reduction of continuous signal to a discrete signal
- Any phenomenon
 - Light
 - Heat
 - Gravity

Sampling

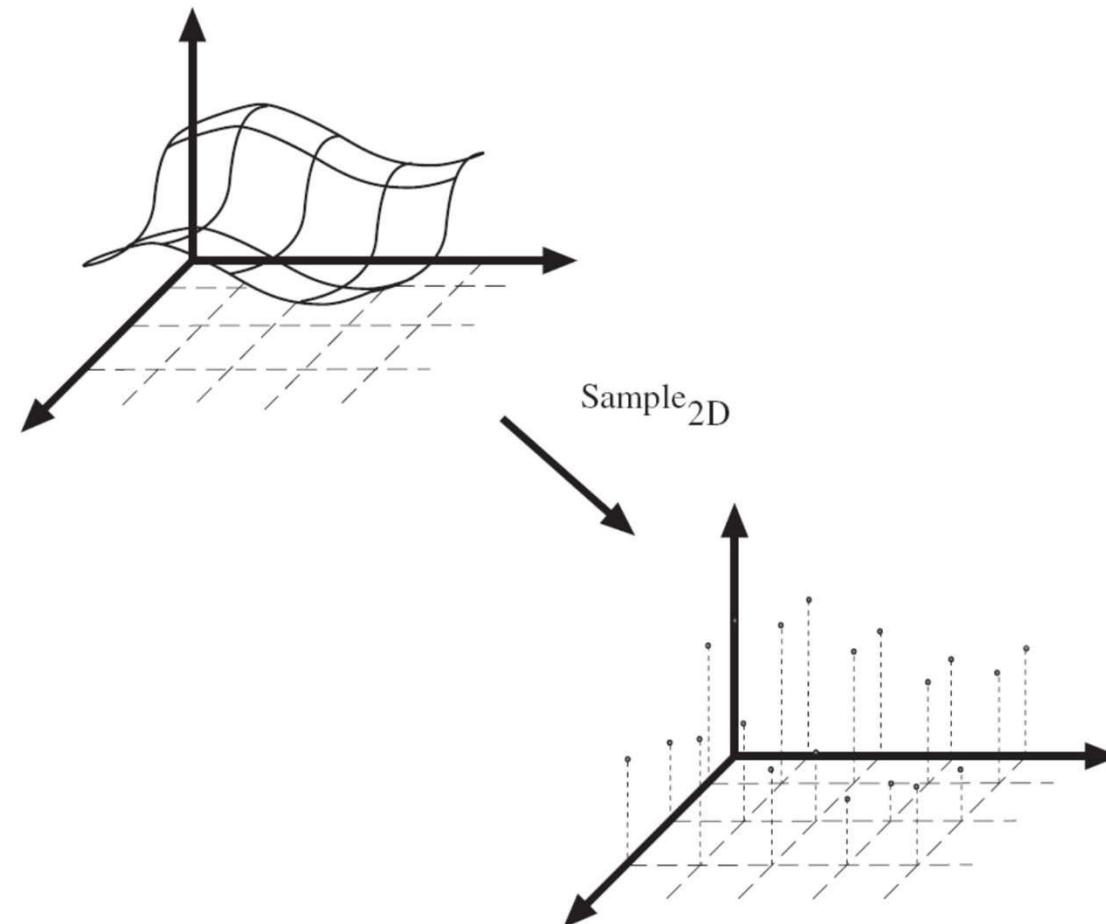
- Sampling in 1D takes a function and returns a vector whose elements are values of that function at the sample points.



Danny Alexander

Sampling

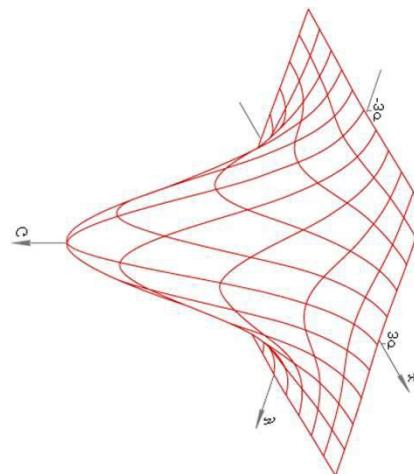
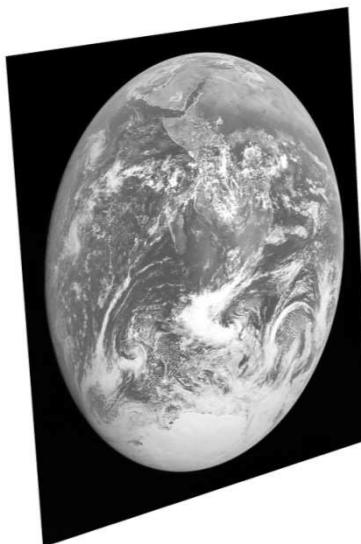
- Sampling in 2D takes a function and returns a matrix



2D Image

Definition

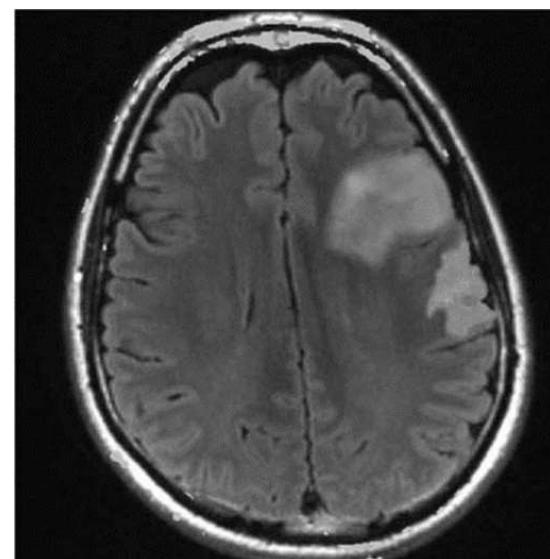
Image: A sampling of a function that contains information about a 2D* signal.



* or a 2D projection of a multi-dimensional signal

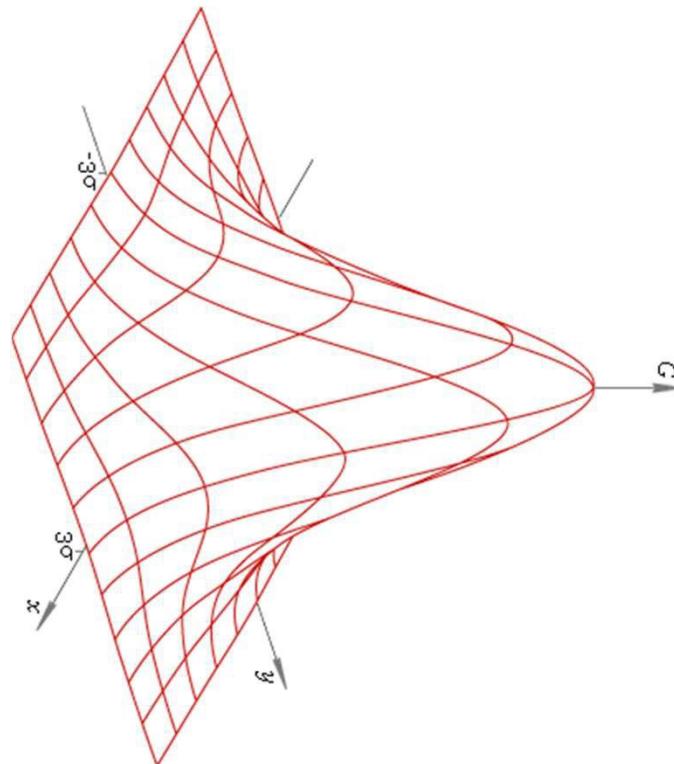
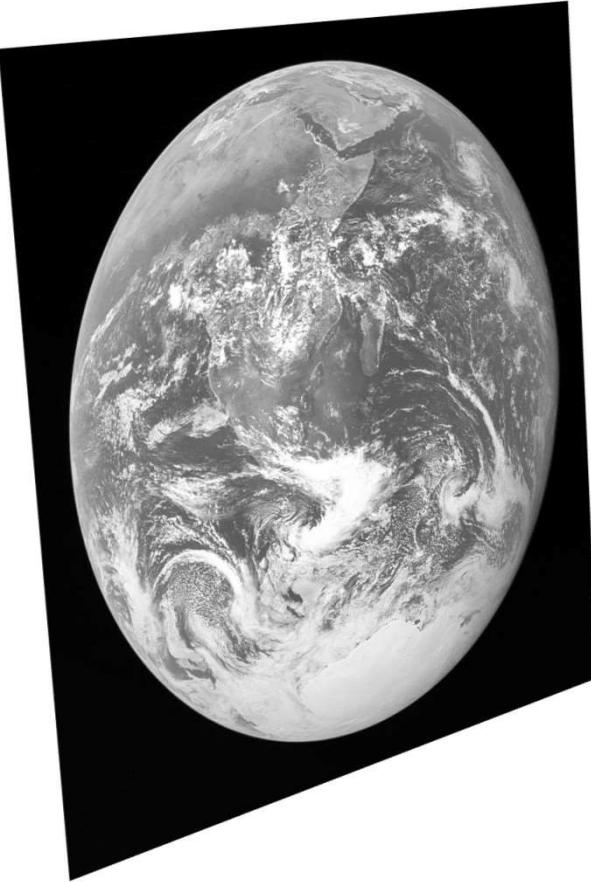
- Function stores ‘brightness’
- 2D signals are special for us
 - Brightness along x and y dimensions
- Video: xy-coordinates + time
 - Time-varying 2D signal

Example of 2D Images

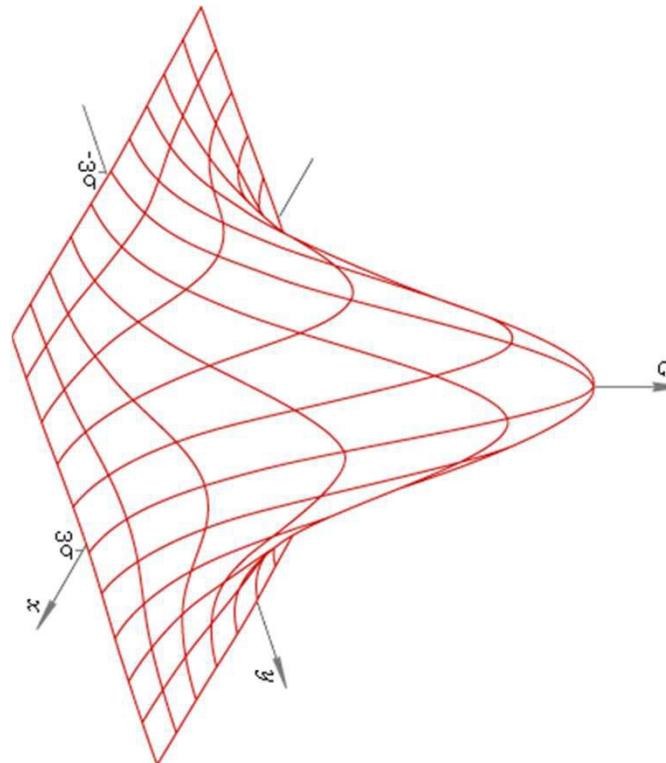
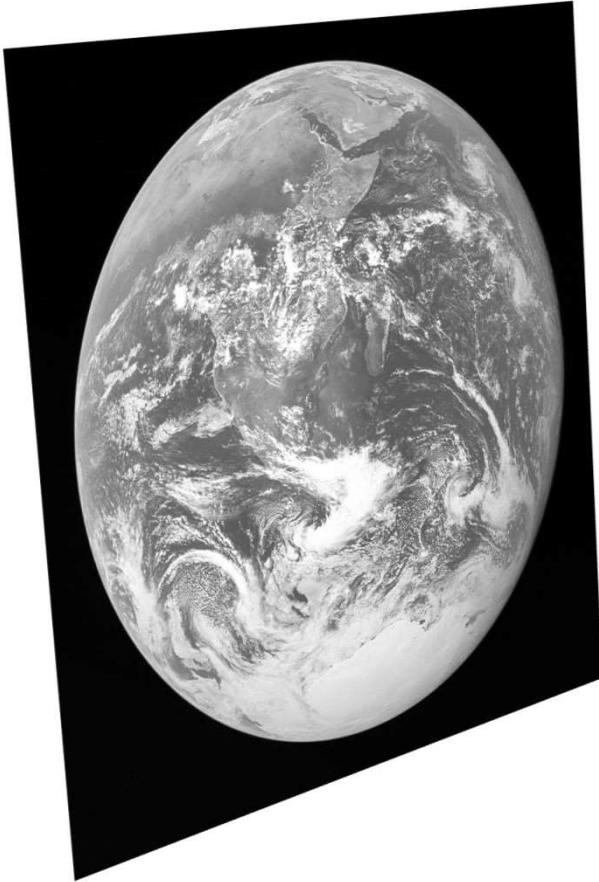


http://radiologykey.com/wp-content/uploads/2016/01/9781604063325_c014_f004.jpg

Sampling in Practice

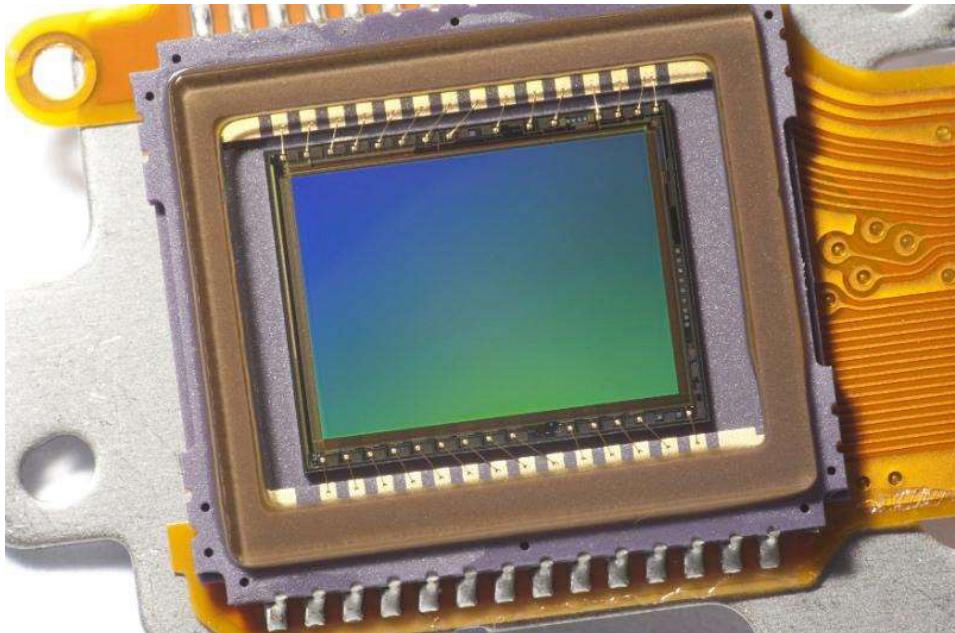


Sampling in Practice: Digital Image

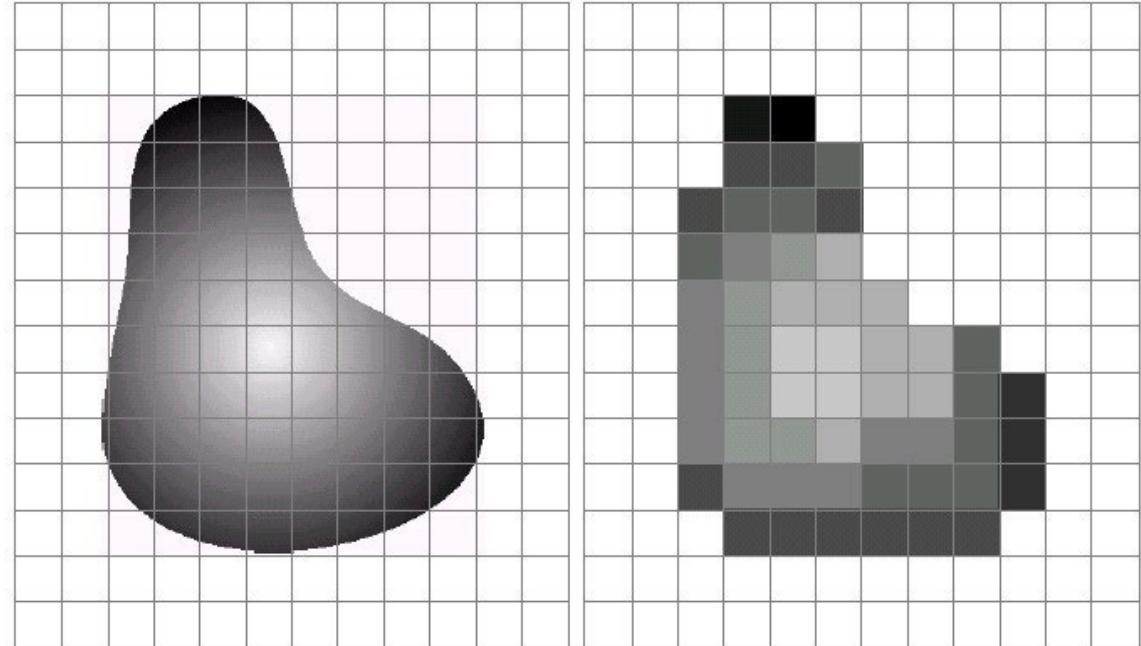


CMOS / CCD

Sensor Array



CMOS sensor



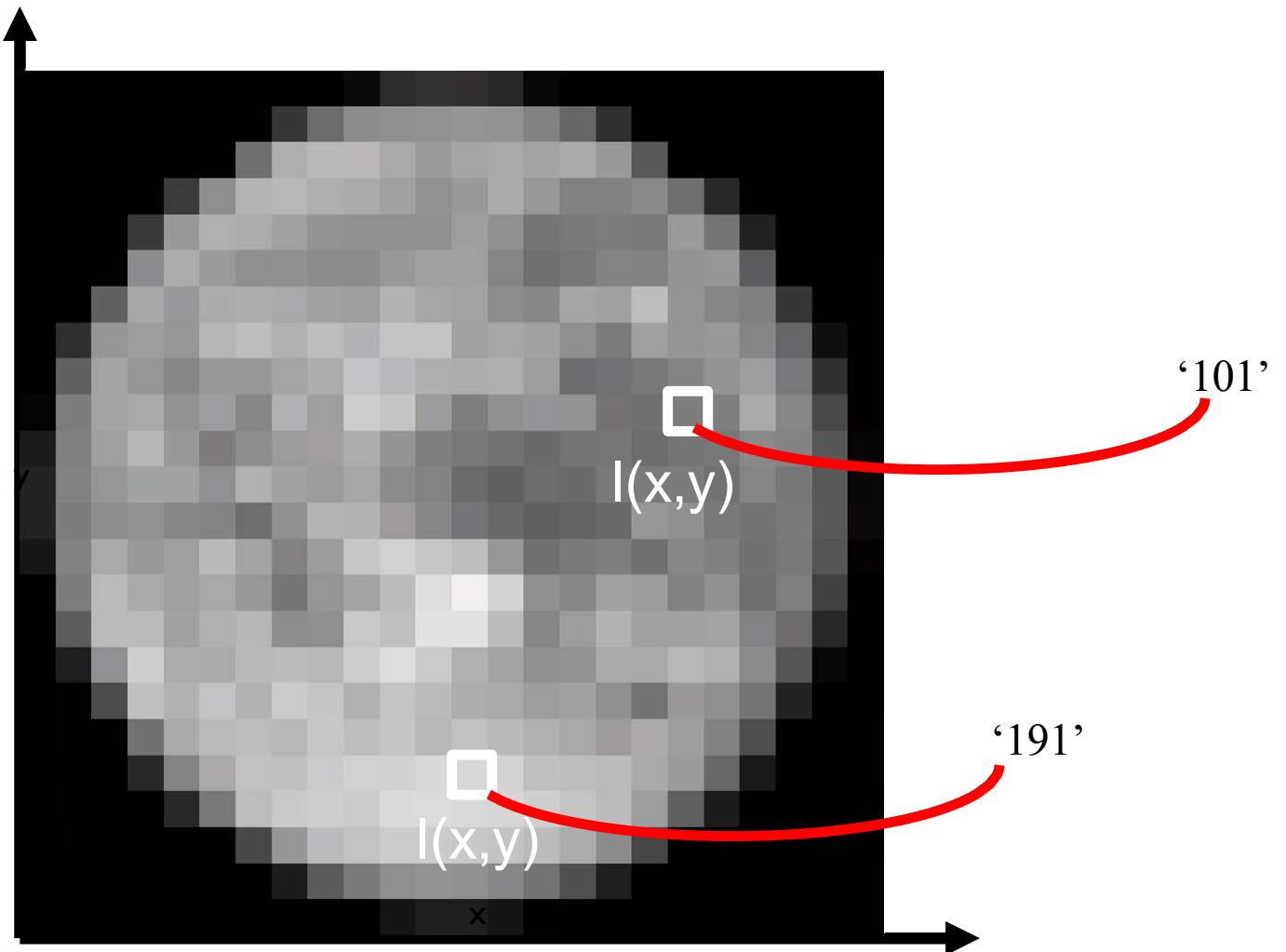
a b

FIGURE 2.17 (a) Continuous image projected onto a sensor array. (b) Result of image sampling and quantization.

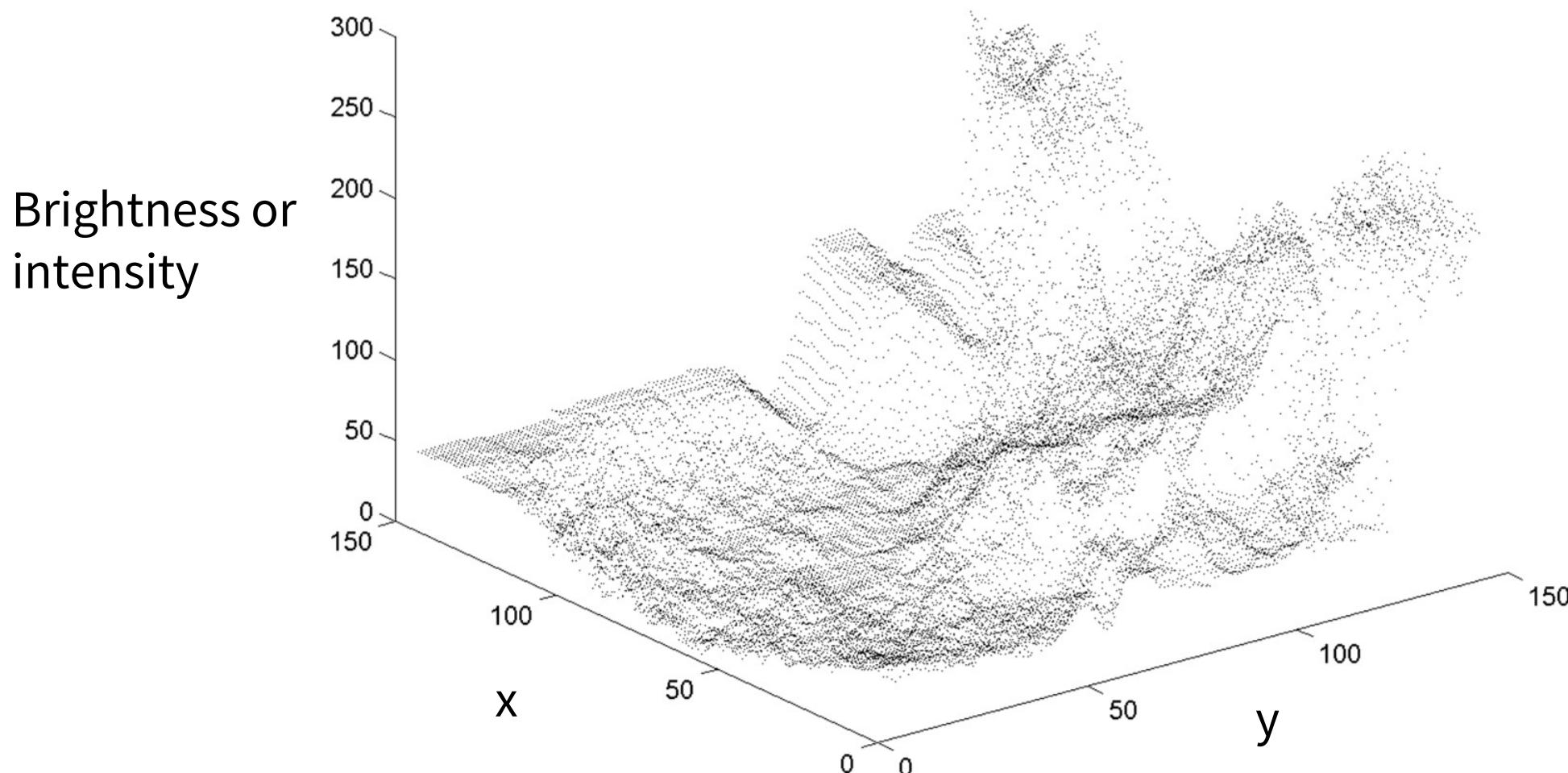
James Hays

Elements of a Digital Image

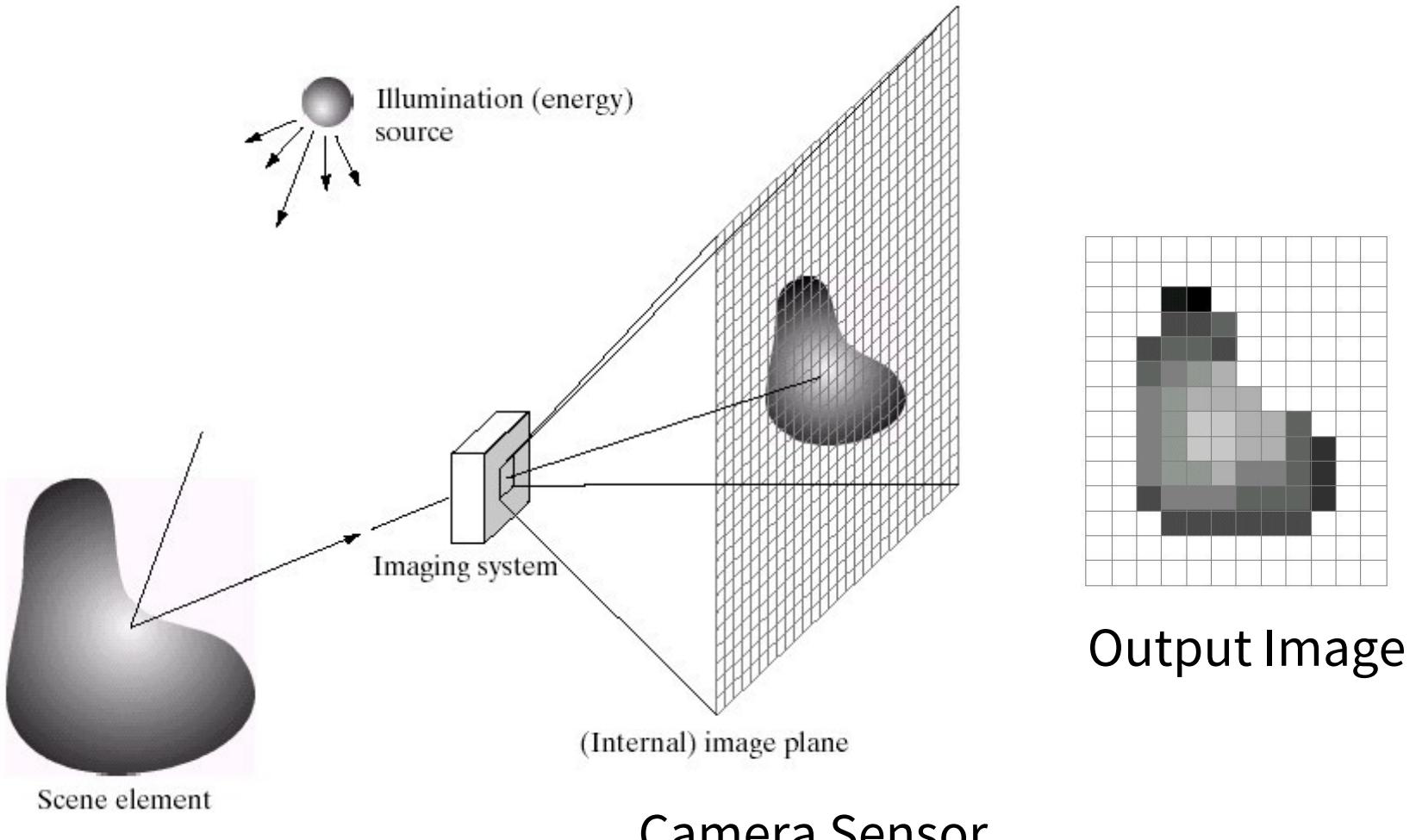
Pixel: picture element



Digital Image is a 2D Signal

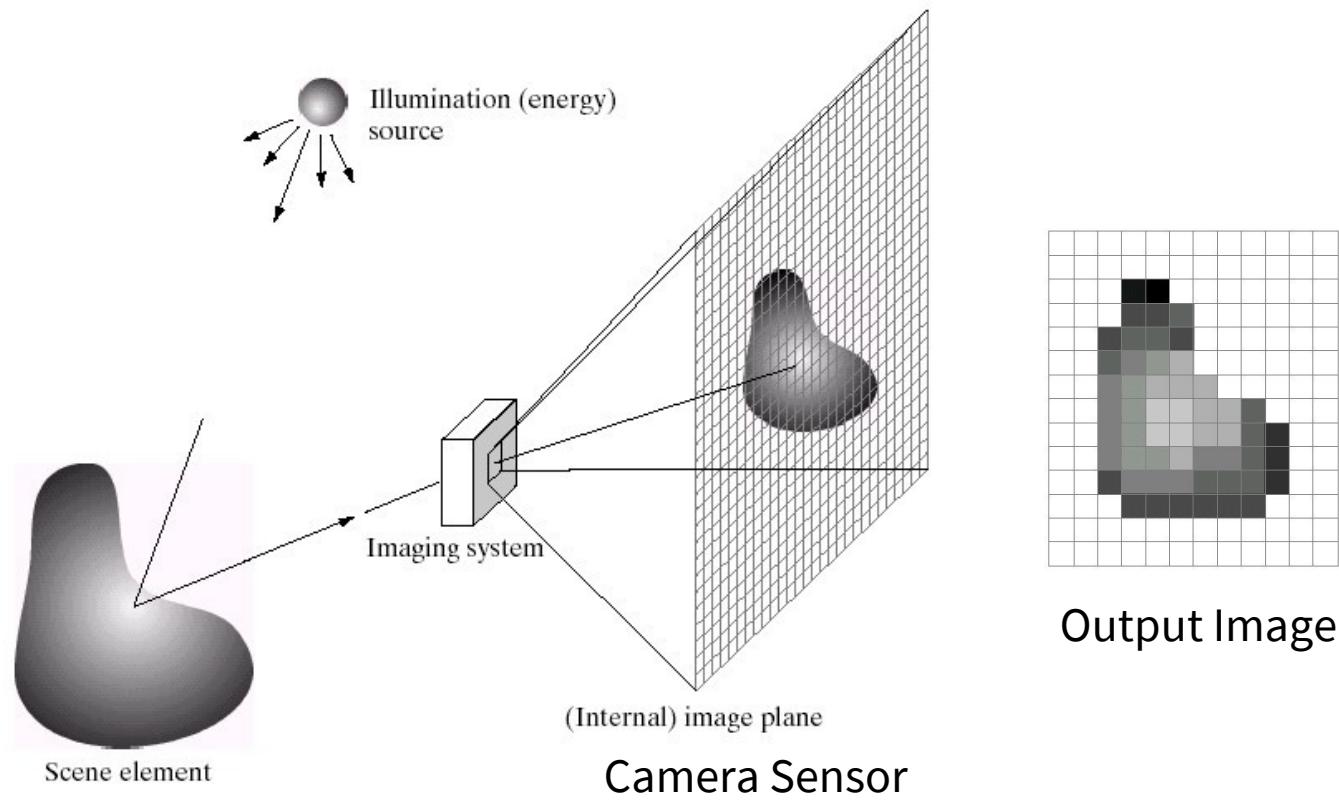


Light Integration Over the “Frustum”

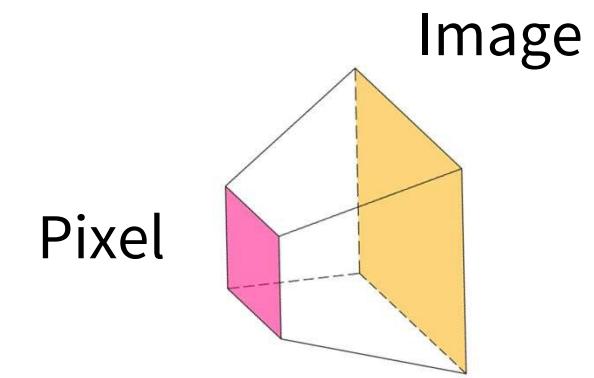


James Hays

Light Integration Over the “Frustum”



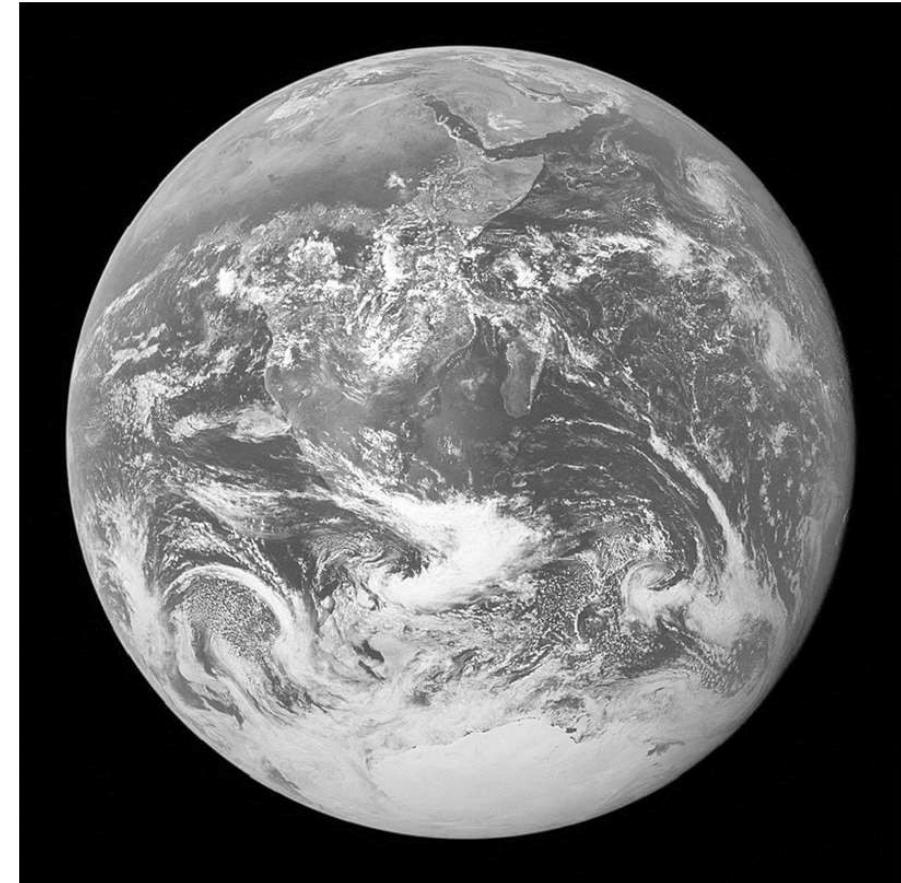
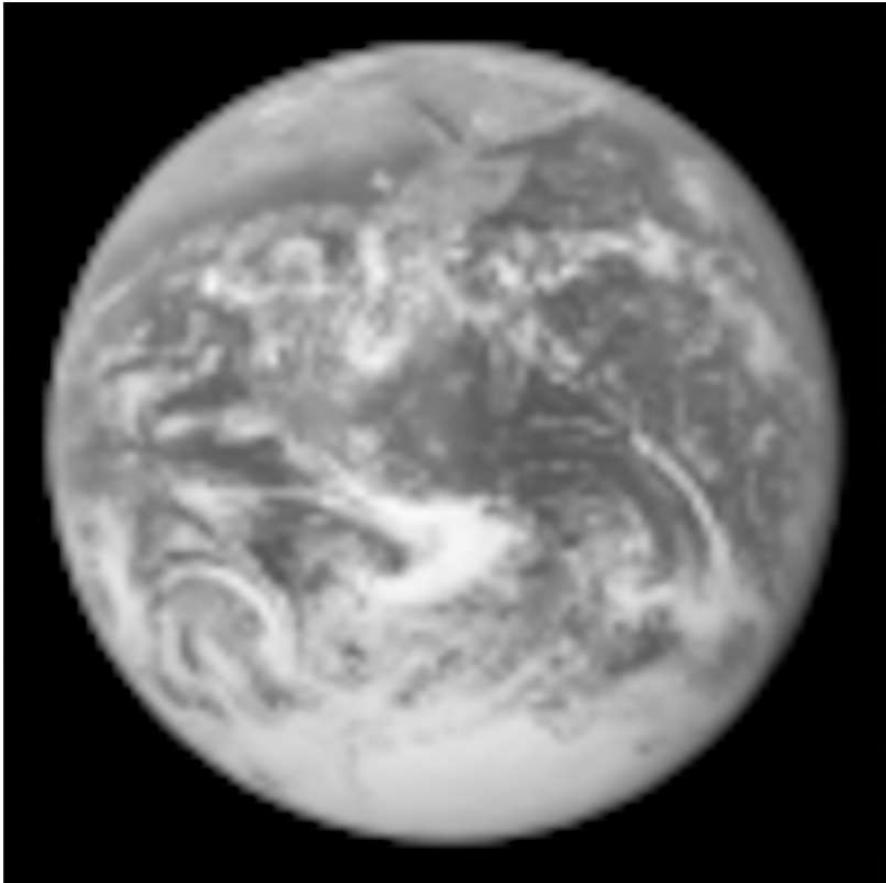
James Hays



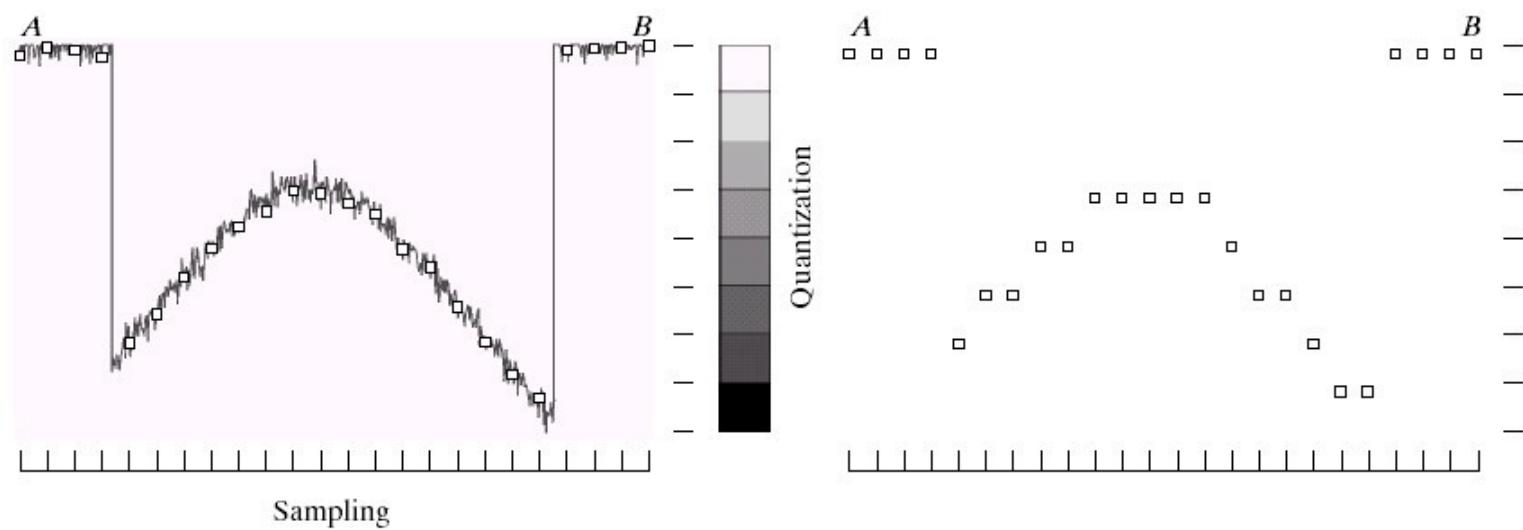
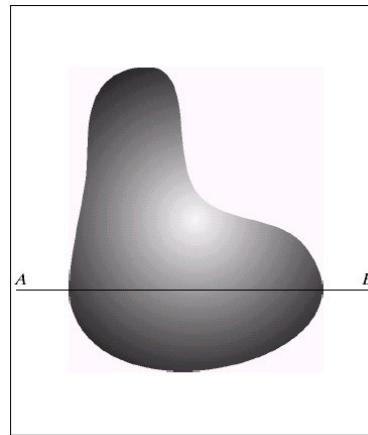
A frustum approximates the ray space that a pixel samples

Resolution: geometric vs. spatial

Both images are 1000x1000 pixels:



Quantization



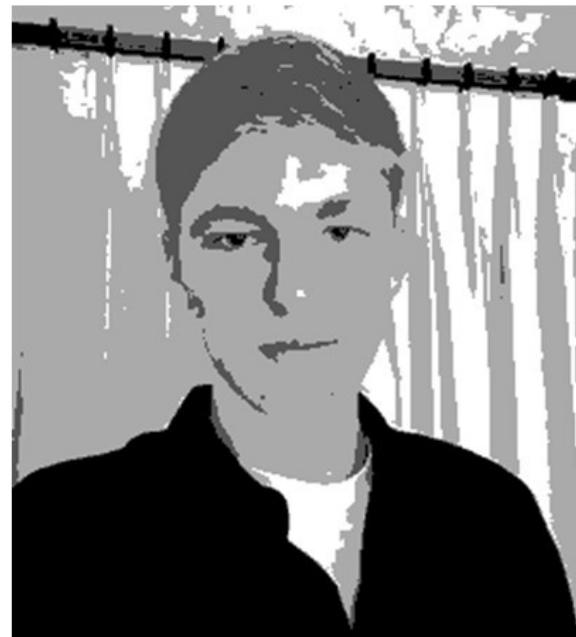
Quantization Effects – Radiometric Resolution



8 bit – 256 levels



4 bit – 16 levels



2 bit – 4 levels



1 bit – 2 levels

We often call this ***bit depth***.

For photography, this is also related to ***dynamic range***.

Images in Python (import numpy)

$N \times M$ grayscale image “im”

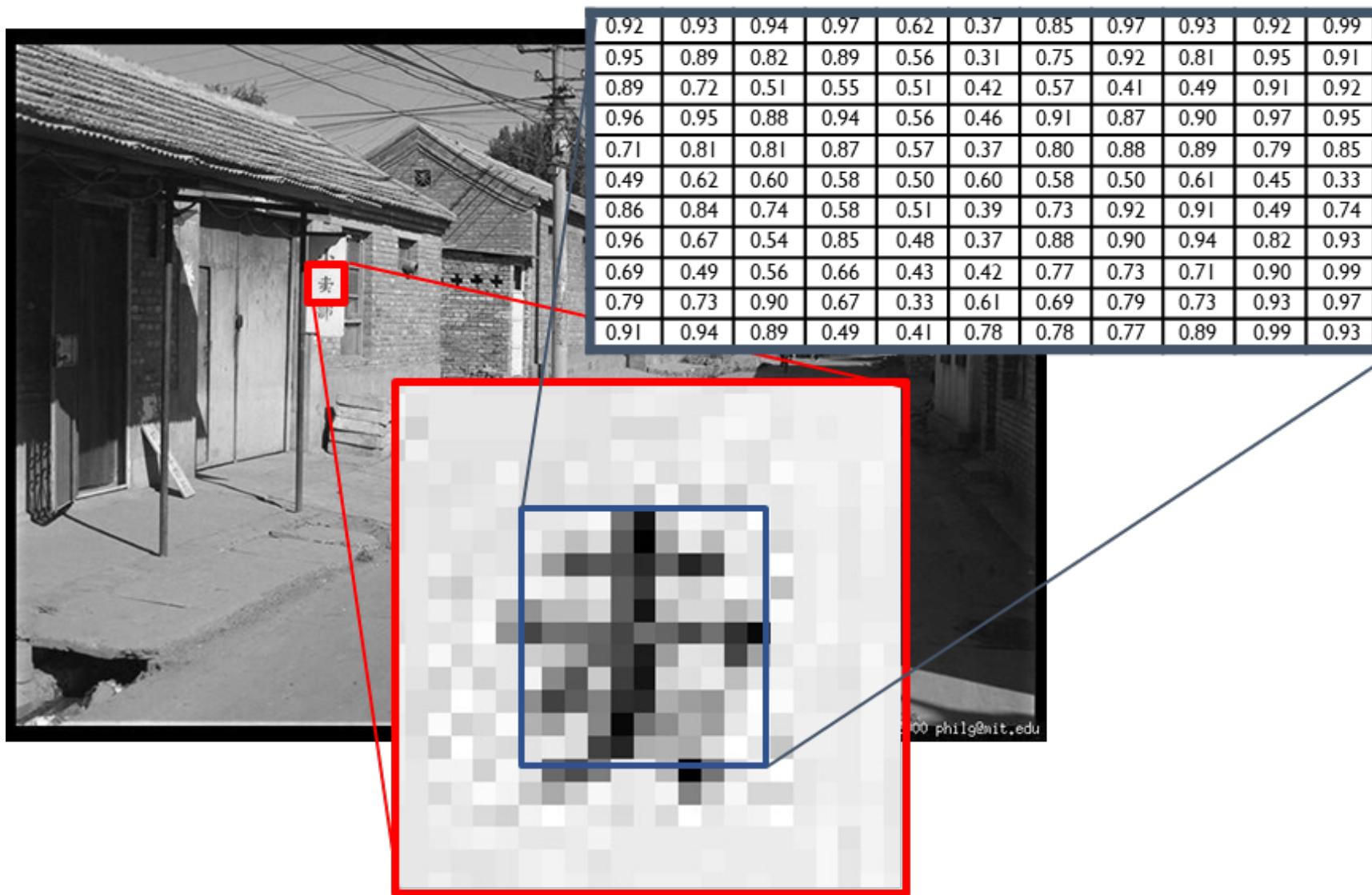
- $im[0, 0]$ = top-left pixel value
- $im[y, x]$ = y pixels down, x pixels to right
- $im[N-1, M-1]$ = bottom-right pixel

Row ↓ Column →

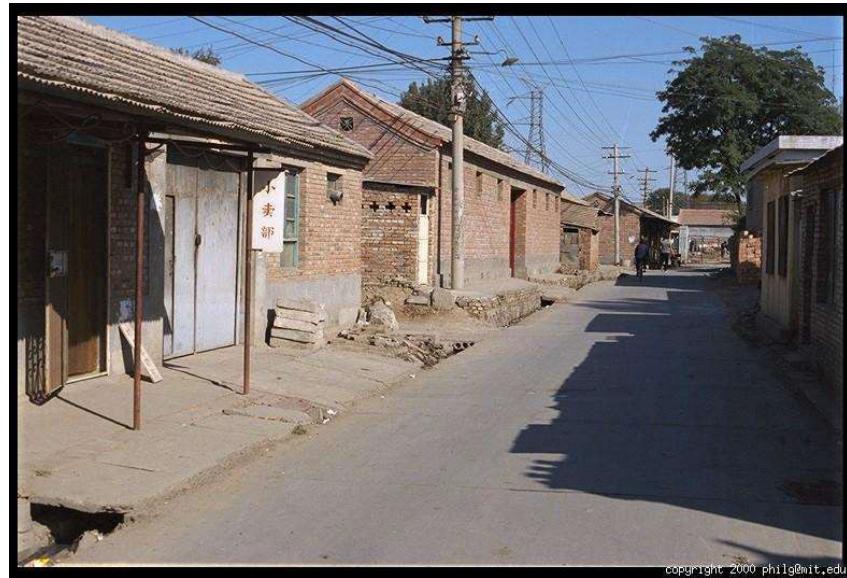
0.92	0.93	0.94	0.97	0.62	0.37	0.85	0.97	0.93	0.92	0.99
0.95	0.89	0.82	0.89	0.56	0.31	0.75	0.92	0.81	0.95	0.91
0.89	0.72	0.51	0.55	0.51	0.42	0.57	0.41	0.49	0.91	0.92
0.96	0.95	0.88	0.94	0.56	0.46	0.91	0.87	0.90	0.97	0.95
0.71	0.81	0.81	0.87	0.57	0.37	0.80	0.88	0.89	0.79	0.85
0.49	0.62	0.60	0.58	0.50	0.60	0.58	0.50	0.61	0.45	0.33
0.86	0.84	0.74	0.58	0.51	0.39	0.73	0.92	0.91	0.49	0.74
0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93
0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99
0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97
0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93

James Hays

Grayscale Intensity



Color



Red intensity



Green



Blue

Images in Python (import numpy)

$N \times M$ grayscale image “im”

- $im[0, 0, 0]$ = top-left pixel value, **red channel**
- $im[y, x, 1]$ = y pixels down, x pixels to right, **green channel**
- $im[N-1, M-1, 2]$ = bottom-right pixel, **blue channel**

0.92	0.93	0.94	0.97	0.62	0.37	0.85	0.97	0.93	0.92	0.99
0.95	0.89	0.82	0.89	0.56	0.31	0.75	0.92	0.81	0.95	0.91
0.89	0.72	0.51	0.55	0.51	0.42	0.57	0.41	0.49	0.91	0.92
0.96	0.95	0.88	0.94	0.56	0.46	0.91	0.87	0.90	0.97	0.95
0.71	0.81	0.81	0.87	0.57	0.37	0.80	0.88	0.89	0.79	0.85
0.49	0.62	0.60	0.58	0.50	0.60	0.58	0.50	0.61	0.45	0.33
0.86	0.84	0.74	0.58	0.51	0.39	0.73	0.92	0.91	0.49	0.74
0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93
0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99
0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97
0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93
0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97
0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93
0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97
0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93

James Hays